

# Mathematica 11.3 Integration Test Results

Test results for the 1373 problems in "4.5.4.2 (a+b sec)^m (d sec)^n (A+B sec+C sec^2).m"

**Problem 1: Result unnecessarily involves imaginary or complex numbers.**

$$\int \text{Sec}[c + d x]^2 (b \text{Sec}[c + d x])^{1/3} (A + C \text{Sec}[c + d x]^2) dx$$

Optimal (type 5, 95 leaves, 4 steps):

$$\left( 3 (10 A + 7 C) \text{Hypergeometric2F1}\left[-\frac{2}{3}, \frac{1}{2}, \frac{1}{3}, \text{Cos}[c + d x]^2\right] (b \text{Sec}[c + d x])^{4/3} \text{Sin}[c + d x] \right) / \left( 40 b d \sqrt{\text{Sin}[c + d x]^2} \right) + \frac{3 C (b \text{Sec}[c + d x])^{7/3} \text{Tan}[c + d x]}{10 b^2 d}$$

Result (type 5, 189 leaves):

$$\left( 3 (b \text{Sec}[c + d x])^{1/3} (A + C \text{Sec}[c + d x]^2) \left( -2 i 2^{1/3} (10 A + 7 C) \left( \frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}} \right)^{1/3} (1 + e^{2i(c+dx)})^{1/3} \text{Hypergeometric2F1}\left[\frac{1}{6}, \frac{1}{3}, \frac{7}{6}, -e^{2i(c+dx)}\right] + (5(2A + 3C) + (10A + 7C) \text{Cos}[2(c+dx)]) \text{Sec}[c + d x]^{10/3} \text{Sin}[c + d x] \right) \right) / (40 d (A + 2C + A \text{Cos}[2(c+dx)]) \text{Sec}[c + d x]^{7/3})$$

**Problem 2: Result unnecessarily involves imaginary or complex numbers.**

$$\int \text{Sec}[c + d x] (b \text{Sec}[c + d x])^{1/3} (A + C \text{Sec}[c + d x]^2) dx$$

Optimal (type 5, 92 leaves, 4 steps):

$$\left( 3 (7 A + 4 C) \text{Hypergeometric2F1}\left[-\frac{1}{6}, \frac{1}{2}, \frac{5}{6}, \text{Cos}[c + d x]^2\right] (b \text{Sec}[c + d x])^{1/3} \text{Sin}[c + d x] \right) / \left( 7 d \sqrt{\text{Sin}[c + d x]^2} \right) + \frac{3 C (b \text{Sec}[c + d x])^{4/3} \text{Tan}[c + d x]}{7 b d}$$

Result (type 5, 183 leaves):

$$-\left( \left( 6 i e^{-i(c+dx)} \cos[c+dx]^3 \left( -7 A (1+e^{2i(c+dx)})^2 - 2 C (2+5 e^{2i(c+dx)} + e^{4i(c+dx)}) + (7 A + 4 C) (1+e^{2i(c+dx)})^{7/3} \operatorname{Hypergeometric2F1}\left[-\frac{1}{3}, \frac{1}{3}, \frac{2}{3}, -e^{2i(c+dx)}\right] \right) (b \operatorname{Sec}[c+dx])^{4/3} (A+C \operatorname{Sec}[c+dx]^2) \right) / \left( 7 b d (1+e^{2i(c+dx)})^2 (A+2 C+A \cos[2(c+dx)]) \right) \right)$$

**Problem 3: Result unnecessarily involves imaginary or complex numbers.**

$$\int (b \operatorname{Sec}[c+dx])^{1/3} (A+C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 5, 88 leaves, 3 steps):

$$-\left( \left( 3 b (4 A + C) \operatorname{Hypergeometric2F1}\left[\frac{1}{3}, \frac{1}{2}, \frac{4}{3}, \cos[c+dx]^2\right] \sin[c+dx] \right) / \left( 8 d (b \operatorname{Sec}[c+dx])^{2/3} \sqrt{\sin[c+dx]^2} \right) + \frac{3 C (b \operatorname{Sec}[c+dx])^{1/3} \tan[c+dx]}{4 d} \right)$$

Result (type 5, 162 leaves):

$$\left( 3 (b \operatorname{Sec}[c+dx])^{1/3} (A+C \operatorname{Sec}[c+dx]^2) \left( -i 2^{1/3} (4 A + C) \left( \frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}} \right)^{1/3} (1+e^{2i(c+dx)})^{1/3} \operatorname{Hypergeometric2F1}\left[\frac{1}{6}, \frac{1}{3}, \frac{7}{6}, -e^{2i(c+dx)}\right] + C \operatorname{Sec}[c+dx]^{4/3} \sin[c+dx] \right) \right) / \left( 2 d (A+2 C+A \cos[2(c+dx)]) \operatorname{Sec}[c+dx]^{7/3} \right)$$

**Problem 6: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c+dx]^2 (b \operatorname{Sec}[c+dx])^{4/3} (A+C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 5, 95 leaves, 4 steps):

$$\left( 3 (13 A + 10 C) \operatorname{Hypergeometric2F1}\left[-\frac{7}{6}, \frac{1}{2}, -\frac{1}{6}, \cos[c+dx]^2\right] (b \operatorname{Sec}[c+dx])^{7/3} \sin[c+dx] \right) / \left( 91 b d \sqrt{\sin[c+dx]^2} \right) + \frac{3 C (b \operatorname{Sec}[c+dx])^{10/3} \tan[c+dx]}{13 b^2 d}$$

Result (type 5, 235 leaves):

$$-\left( \left( 12 i e^{-i(c+dx)} \cos[c+dx]^3 \left( -13 A (1+e^{2i(c+dx)})^2 (2+5 e^{2i(c+dx)} + e^{4i(c+dx)}) - 2 C (10+45 e^{2i(c+dx)} + 79 e^{4i(c+dx)} + 21 e^{6i(c+dx)} + 5 e^{8i(c+dx)}) + 2 (13 A + 10 C) (1+e^{2i(c+dx)})^{13/3} \operatorname{Hypergeometric2F1}\left[-\frac{1}{3}, \frac{1}{3}, \frac{2}{3}, -e^{2i(c+dx)}\right] \right) (b \operatorname{Sec}[c+dx])^{4/3} (A+C \operatorname{Sec}[c+dx]^2) \right) / \left( 91 d (1+e^{2i(c+dx)})^4 (A+2 C+A \cos[2(c+dx)]) \right) \right)$$

**Problem 7: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \text{Sec}[c + d x] (b \text{Sec}[c + d x])^{4/3} (A + C \text{Sec}[c + d x]^2) dx$$

Optimal (type 5, 92 leaves, 4 steps):

$$\left( 3 (10 A + 7 C) \text{Hypergeometric2F1}\left[-\frac{2}{3}, \frac{1}{2}, \frac{1}{3}, \text{Cos}[c + d x]^2\right] (b \text{Sec}[c + d x])^{4/3} \text{Sin}[c + d x] \right) / \left( 40 d \sqrt{\text{Sin}[c + d x]^2} \right) + \frac{3 C (b \text{Sec}[c + d x])^{7/3} \text{Tan}[c + d x]}{10 b d}$$

Result (type 5, 192 leaves):

$$\left( 3 (b \text{Sec}[c + d x])^{7/3} (A + C \text{Sec}[c + d x]^2) \left( -2 i^{2^{1/3}} (10 A + 7 C) \left( \frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}} \right)^{1/3} (1 + e^{2i(c+dx)})^{1/3} \text{Hypergeometric2F1}\left[\frac{1}{6}, \frac{1}{3}, \frac{7}{6}, -e^{2i(c+dx)}\right] + (5(2A + 3C) + (10A + 7C) \text{Cos}[2(c+dx)]) \text{Sec}[c + d x]^{10/3} \text{Sin}[c + d x] \right) \right) / (40 b d (A + 2C + A \text{Cos}[2(c+dx)]) \text{Sec}[c + d x]^{13/3})$$

**Problem 8: Result unnecessarily involves imaginary or complex numbers.**

$$\int (b \text{Sec}[c + d x])^{4/3} (A + C \text{Sec}[c + d x]^2) dx$$

Optimal (type 5, 90 leaves, 3 steps):

$$\left( 3 b (7 A + 4 C) \text{Hypergeometric2F1}\left[-\frac{1}{6}, \frac{1}{2}, \frac{5}{6}, \text{Cos}[c + d x]^2\right] (b \text{Sec}[c + d x])^{1/3} \text{Sin}[c + d x] \right) / \left( 7 d \sqrt{\text{Sin}[c + d x]^2} \right) + \frac{3 C (b \text{Sec}[c + d x])^{4/3} \text{Tan}[c + d x]}{7 d}$$

Result (type 5, 180 leaves):

$$\left( \left( 6 i e^{-i(c+dx)} \text{Cos}[c + d x]^3 \left( -7 A (1 + e^{2i(c+dx)})^2 - 2 C (2 + 5 e^{2i(c+dx)} + e^{4i(c+dx)}) + (7 A + 4 C) (1 + e^{2i(c+dx)})^{7/3} \text{Hypergeometric2F1}\left[-\frac{1}{3}, \frac{1}{3}, \frac{2}{3}, -e^{2i(c+dx)}\right] \right) (b \text{Sec}[c + d x])^{4/3} (A + C \text{Sec}[c + d x]^2) \right) / \left( 7 d (1 + e^{2i(c+dx)})^2 (A + 2C + A \text{Cos}[2(c+dx)]) \right) \right)$$

**Problem 9: Result unnecessarily involves imaginary or complex numbers.**

$$\int \text{Cos}[c + d x] (b \text{Sec}[c + d x])^{4/3} (A + C \text{Sec}[c + d x]^2) dx$$

Optimal (type 5, 91 leaves, 4 steps):

$$-\left( \left( 3 b^2 (4 A + C) \operatorname{Hypergeometric2F1} \left[ \frac{1}{3}, \frac{1}{2}, \frac{4}{3}, \cos [c + d x]^2 \right] \sin [c + d x] \right) / \right. \\ \left. \left( 8 d (b \operatorname{Sec}[c + d x])^{2/3} \sqrt{\sin [c + d x]^2} \right) + \frac{3 b C (b \operatorname{Sec}[c + d x])^{1/3} \tan [c + d x]}{4 d} \right)$$

Result (type 5, 163 leaves):

$$\left( 3 b (b \operatorname{Sec}[c + d x])^{1/3} (A + C \operatorname{Sec}[c + d x]^2) \left( -i 2^{1/3} (4 A + C) \left( \frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}} \right)^{1/3} (1 + e^{2i(c+dx)})^{1/3} \right. \right. \\ \left. \left. \operatorname{Hypergeometric2F1} \left[ \frac{1}{6}, \frac{1}{3}, \frac{7}{6}, -e^{2i(c+dx)} \right] + C \operatorname{Sec}[c + d x]^{4/3} \sin [c + d x] \right) \right) / \\ (2 d (A + 2 C + A \cos [2(c + d x)]) \operatorname{Sec}[c + d x]^{7/3})$$

**Problem 11: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c + d x]^2 (A + C \operatorname{Sec}[c + d x]^2)}{(b \operatorname{Sec}[c + d x])^{1/3}} dx$$

Optimal (type 5, 95 leaves, 4 steps):

$$\left( 3 (8 A + 5 C) \operatorname{Hypergeometric2F1} \left[ -\frac{1}{3}, \frac{1}{2}, \frac{2}{3}, \cos [c + d x]^2 \right] (b \operatorname{Sec}[c + d x])^{2/3} \sin [c + d x] \right) / \\ \left( 16 b d \sqrt{\sin [c + d x]^2} \right) + \frac{3 C (b \operatorname{Sec}[c + d x])^{5/3} \tan [c + d x]}{8 b^2 d}$$

Result (type 5, 207 leaves):

$$-\left( \left( 3 i \left( -8 A (1 + e^{2i(c+dx)})^2 - C (5 + 14 e^{2i(c+dx)} + e^{4i(c+dx)}) + (8 A + 5 C) (1 + e^{2i(c+dx)})^{8/3} \right. \right. \right. \\ \left. \left. \operatorname{Hypergeometric2F1} \left[ -\frac{1}{6}, \frac{2}{3}, \frac{5}{6}, -e^{2i(c+dx)} \right] \right) (A + C \operatorname{Sec}[c + d x]^2) \right) / \\ \left( 4 \times 2^{1/3} d \left( \frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}} \right)^{1/3} (1 + e^{2i(c+dx)})^3 (A + 2 C + A \cos [2(c + d x)]) \right. \\ \left. \operatorname{Sec}[c + d x]^{5/3} (b \operatorname{Sec}[c + d x])^{1/3} \right)$$

**Problem 12: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\operatorname{Sec}[c + d x] (A + C \operatorname{Sec}[c + d x]^2)}{(b \operatorname{Sec}[c + d x])^{1/3}} dx$$

Optimal (type 5, 92 leaves, 4 steps):

$$- \left( \left( 3 (5A + 2C) \operatorname{Hypergeometric2F1} \left[ \frac{1}{6}, \frac{1}{2}, \frac{7}{6}, \cos [c + dx]^2 \right] \sin [c + dx] \right) / \right. \\ \left. \left( 5d (b \sec [c + dx])^{1/3} \sqrt{\sin [c + dx]^2} \right) \right) + \frac{3C (b \sec [c + dx])^{2/3} \tan [c + dx]}{5bd}$$

Result (type 5, 168 leaves):

$$\left( 3 (b \sec [c + dx])^{2/3} (A + C \sec [c + dx]^2) \left( -i 2^{2/3} (5A + 2C) \left( \frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}} \right)^{2/3} (1 + e^{2i(c+dx)})^{2/3} \right. \right. \\ \left. \left. \operatorname{Hypergeometric2F1} \left[ \frac{1}{3}, \frac{2}{3}, \frac{4}{3}, -e^{2i(c+dx)} \right] + 2C \sec [c + dx]^{5/3} \sin [c + dx] \right) \right) / \\ (5bd (A + 2C + A \cos [2(c + dx)]) \sec [c + dx]^{8/3})$$

**Problem 13: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{A + C \sec [c + dx]^2}{(b \sec [c + dx])^{1/3}} dx$$

Optimal (type 5, 90 leaves, 3 steps):

$$- \left( \left( 3b (2A - C) \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{5}{3}, \cos [c + dx]^2 \right] \sin [c + dx] \right) / \right. \\ \left. \left( 8d (b \sec [c + dx])^{4/3} \sqrt{\sin [c + dx]^2} \right) \right) + \frac{3C \tan [c + dx]}{2d (b \sec [c + dx])^{1/3}}$$

Result (type 5, 98 leaves):

$$- \left( \left( 3i \left( A - C + A e^{2i(c+dx)} + (-2A + C) (1 + e^{2i(c+dx)})^{2/3} \right. \right. \right. \\ \left. \left. \operatorname{Hypergeometric2F1} \left[ -\frac{1}{6}, \frac{2}{3}, \frac{5}{6}, -e^{2i(c+dx)} \right] \right) \right) / \left( d (1 + e^{2i(c+dx)}) (b \sec [c + dx])^{1/3} \right)$$

**Problem 14: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\cos [c + dx] (A + C \sec [c + dx]^2)}{(b \sec [c + dx])^{1/3}} dx$$

Optimal (type 5, 88 leaves, 4 steps):

$$\frac{3(A + 4C) \operatorname{Hypergeometric2F1} \left[ \frac{1}{6}, \frac{1}{2}, \frac{7}{6}, \cos [c + dx]^2 \right] \sin [c + dx]}{4d (b \sec [c + dx])^{1/3} \sqrt{\sin [c + dx]^2}} + \frac{3Ab \tan [c + dx]}{4d (b \sec [c + dx])^{4/3}}$$

Result (type 5, 121 leaves):

$$- \left( \left( 3i e^{-i(c+dx)} \left( A (-1 + e^{4i(c+dx)}) + 2(A + 4C) e^{2i(c+dx)} (1 + e^{2i(c+dx)})^{2/3} \right. \right. \right. \\ \left. \left. \operatorname{Hypergeometric2F1} \left[ \frac{1}{3}, \frac{2}{3}, \frac{4}{3}, -e^{2i(c+dx)} \right] \right) \right) / \left( 8d (1 + e^{2i(c+dx)}) (b \sec [c + dx])^{1/3} \right)$$

**Problem 16: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\sec [c+d x]^2 (A+C \sec [c+d x]^2)}{(b \sec [c+d x])^{4/3}} dx$$

Optimal (type 5, 95 leaves, 4 steps):

$$-\left( \left( 3 (5 A+2 C) \operatorname{Hypergeometric2F1} \left[ \frac{1}{6}, \frac{1}{2}, \frac{7}{6}, \cos [c+d x]^2 \right] \sin [c+d x] \right) / \left( 5 b d (b \sec [c+d x])^{1/3} \sqrt{\sin [c+d x]^2} \right) \right) + \frac{3 C (b \sec [c+d x])^{2/3} \tan [c+d x]}{5 b^2 d}$$

Result (type 5, 165 leaves):

$$\left( 3 (A+C \sec [c+d x]^2) \left( -i 2^{2/3} (5 A+2 C) \left( \frac{e^{i(c+d x)}}{1+e^{2 i(c+d x)}} \right)^{2/3} (1+e^{2 i(c+d x)})^{2/3} \operatorname{Hypergeometric2F1} \left[ \frac{1}{3}, \frac{2}{3}, \frac{4}{3}, -e^{2 i(c+d x)} \right] + 2 C \sec [c+d x]^{5/3} \sin [c+d x] \right) \right) / \left( 5 d (A+2 C+A \cos [2(c+d x)]) \sec [c+d x]^{2/3} (b \sec [c+d x])^{4/3} \right)$$

**Problem 17: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\sec [c+d x] (A+C \sec [c+d x]^2)}{(b \sec [c+d x])^{4/3}} dx$$

Optimal (type 5, 92 leaves, 4 steps):

$$-\frac{3 (2 A-C) \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{5}{3}, \cos [c+d x]^2 \right] \sin [c+d x]}{8 d (b \sec [c+d x])^{4/3} \sqrt{\sin [c+d x]^2}} + \frac{3 C \tan [c+d x]}{2 b d (b \sec [c+d x])^{1/3}}$$

Result (type 5, 101 leaves):

$$-\left( \left( 3 i \left( A-C+A e^{2 i(c+d x)} + (-2 A+C) (1+e^{2 i(c+d x)})^{2/3} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{6}, \frac{2}{3}, \frac{5}{6}, -e^{2 i(c+d x)} \right] \right) \right) / \left( b d (1+e^{2 i(c+d x)}) (b \sec [c+d x])^{1/3} \right) \right)$$

**Problem 18: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{A+C \sec [c+d x]^2}{(b \sec [c+d x])^{4/3}} dx$$

Optimal (type 5, 90 leaves, 3 steps):

$$-\frac{3 (A+4 C) \operatorname{Hypergeometric2F1} \left[ \frac{1}{6}, \frac{1}{2}, \frac{7}{6}, \cos [c+d x]^2 \right] \sin [c+d x]}{4 b d (b \sec [c+d x])^{1/3} \sqrt{\sin [c+d x]^2}} + \frac{3 A \tan [c+d x]}{4 d (b \sec [c+d x])^{4/3}}$$

Result (type 5, 124 leaves):

$$- \left( \left( 3 \operatorname{Im} e^{-i(c+dx)} \left( A (-1 + e^{4i(c+dx)}) + 2(A+4C) e^{2i(c+dx)} (1 + e^{2i(c+dx)})^{2/3} \operatorname{Hypergeometric2F1} \left[ \frac{1}{3}, \frac{2}{3}, \frac{4}{3}, -e^{2i(c+dx)} \right] \right) \right) / \left( 8bd (1 + e^{2i(c+dx)}) (b \operatorname{Sec}[c+dx])^{1/3} \right) \right)$$

**Problem 21: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c+dx]^m (b \operatorname{Sec}[c+dx])^{4/3} (A+C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 5, 146 leaves, 4 steps):

$$\frac{3bC \operatorname{Sec}[c+dx]^{2+m} (b \operatorname{Sec}[c+dx])^{1/3} \operatorname{Sin}[c+dx]}{d(7+3m)} + \left( 3b(C(4+3m) + A(7+3m)) \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{1}{6}(-1-3m), \frac{1}{6}(5-3m), \operatorname{Cos}[c+dx]^2 \right] \operatorname{Sec}[c+dx]^m (b \operatorname{Sec}[c+dx])^{1/3} \operatorname{Sin}[c+dx] \right) / \left( d(1+3m)(7+3m) \sqrt{\operatorname{Sin}[c+dx]^2} \right)$$

Result (type 5, 333 leaves):

$$- \left( \left( 3 \operatorname{Im} 2^{7/3+m} e^{-\frac{1}{3}i d(4+3m)x} \left( \frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}} \right)^{\frac{4}{3}+m} (1 + e^{2i(c+dx)})^{\frac{4}{3}+m} \left( \frac{1}{10+3m} 2(A+2C) e^{\frac{1}{3}i(6c+d(10+3m)x)} \operatorname{Hypergeometric2F1} \left[ \frac{5}{3} + \frac{m}{2}, \frac{10}{3} + m, \frac{8}{3} + \frac{m}{2}, -e^{2i(c+dx)} \right] + \frac{1}{16+3m} A e^{4i c + \frac{1}{3}i d(16+3m)x} \operatorname{Hypergeometric2F1} \left[ \frac{8}{3} + \frac{m}{2}, \frac{10}{3} + m, \frac{1}{6}(22+3m), -e^{2i(c+dx)} \right] + \frac{1}{4+3m} A e^{\frac{1}{3}i d(4+3m)x} \operatorname{Hypergeometric2F1} \left[ \frac{10}{3} + m, \frac{1}{6}(4+3m), \frac{5}{3} + \frac{m}{2}, -e^{2i(c+dx)} \right] \right) \right) / \left( d(A+2C+A \operatorname{Cos}[2c+2dx]) \operatorname{Sec}[c+dx]^{10/3} \right)$$

**Problem 22: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c+dx]^m (b \operatorname{Sec}[c+dx])^{2/3} (A+C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 5, 146 leaves, 4 steps):

$$\frac{3C \operatorname{Sec}[c+dx]^{1+m} (b \operatorname{Sec}[c+dx])^{2/3} \operatorname{Sin}[c+dx]}{d(5+3m)} - \left( 3(C(2+3m) + A(5+3m)) \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{1}{6}(1-3m), \frac{1}{6}(7-3m), \operatorname{Cos}[c+dx]^2 \right] \operatorname{Sec}[c+dx]^{-1+m} (b \operatorname{Sec}[c+dx])^{2/3} \operatorname{Sin}[c+dx] \right) / \left( d(1-3m)(5+3m) \sqrt{\operatorname{Sin}[c+dx]^2} \right)$$

Result (type 5, 336 leaves):

$$\frac{1}{d (A + 2 C + A \cos [2 c + 2 d x]) \operatorname{Sec}[c + d x]^{8/3}}$$

$$3 \frac{1}{2} \frac{e^{5 i m}}{2^{3+m}} e^{-\frac{1}{3} i d (2+3 m) x} \left( \frac{e^{i (c+d x)}}{1 + e^{2 i (c+d x)}} \right)^{\frac{2}{3}+m} \left( 1 + e^{2 i (c+d x)} \right)^{\frac{2}{3}+m}$$

$$\left( \frac{1}{14 + 3 m} A e^{4 i c + \frac{1}{3} i d (14+3 m) x} \operatorname{Hypergeometric2F1}\left[\frac{7}{3} + \frac{m}{2}, \frac{8}{3} + m, \frac{1}{6} (20 + 3 m), -e^{2 i (c+d x)}\right] + \right.$$

$$\left. \left( e^{\frac{1}{3} i d (2+3 m) x} \left( A (8 + 3 m) \operatorname{Hypergeometric2F1}\left[\frac{8}{3} + m, \frac{1}{6} (2 + 3 m), \frac{1}{6} (8 + 3 m), -e^{2 i (c+d x)}\right] + \right. \right. \right.$$

$$\left. \left. 2 (A + 2 C) e^{2 i (c+d x)} (2 + 3 m) \operatorname{Hypergeometric2F1}\left[\frac{8}{3} + m, \frac{1}{6} (8 + 3 m), \frac{7}{3} + \frac{m}{2}, -e^{2 i (c+d x)}\right] \right) \right) \left/ \left( (2 + 3 m) (8 + 3 m) \right) \right) (b \operatorname{Sec}[c + d x])^{2/3} (A + C \operatorname{Sec}[c + d x]^2)$$

Problem 23: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[c + d x]^m (b \operatorname{Sec}[c + d x])^{1/3} (A + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 5, 144 leaves, 4 steps):

$$\frac{3 C \operatorname{Sec}[c + d x]^{1+m} (b \operatorname{Sec}[c + d x])^{1/3} \operatorname{Sin}[c + d x]}{d (4 + 3 m)}$$

$$\left( 3 (C + 3 C m + A (4 + 3 m)) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{6} (2 - 3 m), \frac{1}{6} (8 - 3 m), \cos [c + d x]^2\right] \right.$$

$$\left. \operatorname{Sec}[c + d x]^{-1+m} (b \operatorname{Sec}[c + d x])^{1/3} \operatorname{Sin}[c + d x] \right) \left/ \left( d (2 - 3 m) (4 + 3 m) \sqrt{\operatorname{Sin}[c + d x]^2} \right) \right)$$

Result (type 5, 336 leaves):

$$\frac{1}{(A + 2 C + A \cos [2 c + 2 d x]) \operatorname{Sec}[c + d x]^{7/3}}$$

$$3 \frac{1}{2} \frac{e^{4 i m}}{2^{3+m}} e^{-\frac{1}{3} i d (1+3 m) x} \left( \frac{e^{i (c+d x)}}{1 + e^{2 i (c+d x)}} \right)^{\frac{1}{3}+m} \left( 1 + e^{2 i (c+d x)} \right)^{\frac{1}{3}+m}$$

$$\left( \frac{1}{d + 3 d m} A e^{\frac{1}{3} i (d+3 d m) x} \operatorname{Hypergeometric2F1}\left[\frac{7}{3} + m, \frac{1}{6} (1 + 3 m), \frac{1}{6} (7 + 3 m), -e^{2 i (c+d x)}\right] + \right.$$

$$\left. \left( e^{\frac{1}{3} i (6 c + d (7+3 m) x)} \left( 2 (A + 2 C) (13 + 3 m) \right. \right. \right.$$

$$\left. \left. \operatorname{Hypergeometric2F1}\left[\frac{7}{3} + m, \frac{1}{6} (7 + 3 m), \frac{1}{6} (13 + 3 m), -e^{2 i (c+d x)}\right] + A e^{2 i (c+d x)} \right. \right.$$

$$\left. \left. (7 + 3 m) \operatorname{Hypergeometric2F1}\left[\frac{7}{3} + m, \frac{1}{6} (13 + 3 m), \frac{1}{6} (19 + 3 m), -e^{2 i (c+d x)}\right] \right) \right) \left/ \left( d (7 + 3 m) (13 + 3 m) \right) \right) (b \operatorname{Sec}[c + d x])^{1/3} (A + C \operatorname{Sec}[c + d x]^2)$$



**Problem 24: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\text{Sec}[c + d x]^m (A + C \text{Sec}[c + d x]^2)}{(b \text{Sec}[c + d x])^{1/3}} dx$$

Optimal (type 5, 147 leaves, 4 steps):

$$\frac{3 C \text{Sec}[c + d x]^{1+m} \text{Sin}[c + d x]}{d (2 + 3 m) (b \text{Sec}[c + d x])^{1/3}} + \left( 3 (C (1 - 3 m) - A (2 + 3 m)) \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{6} (4 - 3 m), \frac{1}{6} (10 - 3 m), \text{Cos}[c + d x]^2\right] \text{Sec}[c + d x]^{-1+m} \text{Sin}[c + d x] \right) / \left( d (4 - 3 m) (2 + 3 m) (b \text{Sec}[c + d x])^{1/3} \sqrt{\text{Sin}[c + d x]^2} \right)$$

Result (type 5, 311 leaves):

$$- \left( \left( 3 i 2^{\frac{2}{3}+m} \left( \frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}} \right)^{-\frac{1}{3}+m} (1 + e^{2i(c+dx)})^{-\frac{1}{3}+m} \left( A (55 + 48 m + 9 m^2) \text{Hypergeometric2F1}\left[\frac{5}{3} + m, \frac{1}{6} (-1 + 3 m), \frac{1}{6} (5 + 3 m), -e^{2i(c+dx)}\right] + e^{2i(c+dx)} (-1 + 3 m) \left( 2 (A + 2 C) (11 + 3 m) \text{Hypergeometric2F1}\left[\frac{5}{3} + m, \frac{1}{6} (5 + 3 m), \frac{1}{6} (11 + 3 m), -e^{2i(c+dx)}\right] + A e^{2i(c+dx)} (5 + 3 m) \text{Hypergeometric2F1}\left[\frac{5}{3} + m, \frac{1}{6} (11 + 3 m), \frac{1}{6} (17 + 3 m), -e^{2i(c+dx)}\right] \right) \right) \right) / \left( d (-1 + 3 m) (5 + 3 m) (11 + 3 m) (A + 2 C + A \text{Cos}[2 c + 2 d x]) \text{Sec}[c + d x]^{5/3} (b \text{Sec}[c + d x])^{1/3} \right)$$

**Problem 25: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\text{Sec}[c + d x]^m (A + C \text{Sec}[c + d x]^2)}{(b \text{Sec}[c + d x])^{2/3}} dx$$

Optimal (type 5, 145 leaves, 4 steps):

$$\frac{3 C \text{Sec}[c + d x]^{1+m} \text{Sin}[c + d x]}{d (1 + 3 m) (b \text{Sec}[c + d x])^{2/3}} - \left( 3 (A - C (2 - 3 m) + 3 A m) \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{6} (5 - 3 m), \frac{1}{6} (11 - 3 m), \text{Cos}[c + d x]^2\right] \text{Sec}[c + d x]^{-1+m} \text{Sin}[c + d x] \right) / \left( d (5 - 3 m) (1 + 3 m) (b \text{Sec}[c + d x])^{2/3} \sqrt{\text{Sin}[c + d x]^2} \right)$$

Result (type 5, 311 leaves):

$$\begin{aligned}
 & - \left( \left( 3 \operatorname{Im} 2^{\frac{1}{3}+m} \left( \frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}} \right)^{-\frac{2}{3}+m} (1+e^{2i(c+dx)})^{-\frac{2}{3}+m} \right. \right. \\
 & \quad \left( A e^{4i(c+dx)} (-8+6m+9m^2) \operatorname{Hypergeometric2F1} \left[ \frac{5}{3} + \frac{m}{2}, \frac{4}{3} + m, \frac{8}{3} + \frac{m}{2}, -e^{2i(c+dx)} \right] + (10+3m) \right. \\
 & \quad \left. \left( A (4+3m) \operatorname{Hypergeometric2F1} \left[ \frac{4}{3} + m, \frac{1}{6} (-2+3m), \frac{1}{6} (4+3m), -e^{2i(c+dx)} \right] + 2 (A+2C) \right. \right. \\
 & \quad \left. \left. e^{2i(c+dx)} (-2+3m) \operatorname{Hypergeometric2F1} \left[ \frac{4}{3} + m, \frac{1}{6} (4+3m), \frac{5}{3} + \frac{m}{2}, -e^{2i(c+dx)} \right] \right) \right) \\
 & \left. (A+C \operatorname{Sec}[c+dx]^2) \right) / \left( d (-2+3m) (4+3m) (10+3m) (A+2C+A \operatorname{Cos}[2c+2dx]) \right) \\
 & \left. \operatorname{Sec}[c+dx]^{4/3} (b \operatorname{Sec}[c+dx])^{2/3} \right)
 \end{aligned}$$

**Problem 26: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c+dx]^m (A+C \operatorname{Sec}[c+dx]^2)}{(b \operatorname{Sec}[c+dx])^{4/3}} dx$$

Optimal (type 5, 148 leaves, 4 steps):

$$\begin{aligned}
 & - \frac{3 C \operatorname{Sec}[c+dx]^m \operatorname{Sin}[c+dx]}{b d (1-3m) (b \operatorname{Sec}[c+dx])^{1/3}} - \\
 & \left( 3 (A+C (4-3m) - 3 A m) \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{1}{6} (7-3m), \frac{1}{6} (13-3m), \operatorname{Cos}[c+dx]^2 \right] \right. \\
 & \left. \operatorname{Sec}[c+dx]^{-2+m} \operatorname{Sin}[c+dx] \right) / \left( b d (1-3m) (7-3m) (b \operatorname{Sec}[c+dx])^{1/3} \sqrt{\operatorname{Sin}[c+dx]^2} \right)
 \end{aligned}$$

Result (type 5, 340 leaves):

$$\begin{aligned}
 & - \left( \left( 3 \operatorname{Im} 2^{-\frac{1}{3}+m} e^{-\frac{1}{3}i(6c+d(2+3m)x)} \left( \frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}} \right)^{\frac{2}{3}+m} (1+e^{2i(c+dx)})^{\frac{2}{3}+m} \right. \right. \\
 & \quad \left( \frac{1}{-4+3m} A e^{\frac{1}{3}id(-4+3m)x} \operatorname{Hypergeometric2F1} \left[ \frac{2}{3} + m, \frac{1}{6} (-4+3m), \frac{1}{6} (2+3m), -e^{2i(c+dx)} \right] + \right. \\
 & \quad \left( e^{\frac{1}{3}i(6c+d(2+3m)x)} \left( 2 (A+2C) (8+3m) \operatorname{Hypergeometric2F1} \left[ \frac{2}{3} + m, \frac{1}{6} (2+3m), \frac{1}{6} (8+3m), \right. \right. \right. \\
 & \quad \left. \left. \left. -e^{2i(c+dx)} \right] + A e^{2i(c+dx)} (2+3m) \operatorname{Hypergeometric2F1} \left[ \frac{2}{3} + m, \frac{1}{6} (8+3m), \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{7}{3} + \frac{m}{2}, -e^{2i(c+dx)} \right] \right) \right) / \left( (2+3m) (8+3m) \right) (A+C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \left. \left( d (A+2C+A \operatorname{Cos}[2c+2dx]) \operatorname{Sec}[c+dx]^{2/3} (b \operatorname{Sec}[c+dx])^{4/3} \right) \right)
 \end{aligned}$$

**Problem 27: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \text{Sec}[c+dx]^m (b \text{Sec}[c+dx])^n (A+C \text{Sec}[c+dx]^2) dx$$

Optimal (type 5, 145 leaves, 4 steps):

$$\frac{C \text{Sec}[c+dx]^{1+m} (b \text{Sec}[c+dx])^n \text{Sin}[c+dx]}{d(1+m+n)} - \left( (C(m+n) + A(1+m+n)) \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{2}(1-m-n), \frac{1}{2}(3-m-n), \text{Cos}[c+dx]^2\right] \text{Sec}[c+dx]^{-1+m} (b \text{Sec}[c+dx])^n \text{Sin}[c+dx] \right) / \left( d(1-m-n)(1+m+n) \sqrt{\text{Sin}[c+dx]^2} \right)$$

Result (type 5, 303 leaves):

$$-\frac{1}{d(A+2C+A \text{Cos}[2c+2dx])} i^{2^{1+m+n}} e^{-i d(m+n)x} \left( \frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}} \right)^{m+n} (1+e^{2i(c+dx)})^{m+n} \left( \frac{1}{m+n} A e^{i d(m+n)x} \text{Hypergeometric2F1}\left[\frac{m+n}{2}, 2+m+n, \frac{1}{2}(2+m+n), -e^{2i(c+dx)}\right] + e^{2ic} \left( \frac{1}{2+m+n} 2(A+2C) e^{i d(2+m+n)x} \text{Hypergeometric2F1}\left[\frac{1}{2}(2+m+n), 2+m+n, \frac{1}{2}(4+m+n), -e^{2i(c+dx)}\right] + \frac{1}{4+m+n} A e^{i(2c+d(4+m+n)x)} \text{Hypergeometric2F1}\left[2+m+n, \frac{1}{2}(4+m+n), \frac{1}{2}(6+m+n), -e^{2i(c+dx)}\right] \right) \right) \text{Sec}[c+dx]^{-2-n} (b \text{Sec}[c+dx])^n (A+C \text{Sec}[c+dx]^2)$$

**Problem 28: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \text{Sec}[c+dx]^2 (b \text{Sec}[c+dx])^n (A+C \text{Sec}[c+dx]^2) dx$$

Optimal (type 5, 120 leaves, 4 steps):

$$\left( (C(2+n) + A(3+n)) \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{2}(-1-n), \frac{1-n}{2}, \text{Cos}[c+dx]^2\right] (b \text{Sec}[c+dx])^{1+n} \text{Sin}[c+dx] \right) / \left( b d(1+n)(3+n) \sqrt{\text{Sin}[c+dx]^2} \right) + \frac{C(b \text{Sec}[c+dx])^{2+n} \text{Tan}[c+dx]}{b^2 d(3+n)}$$

Result (type 5, 289 leaves):

$$\begin{aligned}
 & - \left( \int \left( i 2^{3+n} e^{2 i c - i d n x} \left( \frac{e^{i (c+d x)}}{1 + e^{2 i (c+d x)}} \right)^n (1 + e^{2 i (c+d x)})^n \right. \right. \\
 & \quad \left( \frac{A e^{i d (2+n) x} \text{Hypergeometric2F1} \left[ \frac{2+n}{2}, 4+n, \frac{4+n}{2}, -e^{2 i (c+d x)} \right]}{2+n} + \frac{1}{(4+n)(6+n)} \right. \\
 & \quad \left. e^{i (2c+d(4+n)x} \left( 2(A+2C)(6+n) \text{Hypergeometric2F1} \left[ \frac{4+n}{2}, 4+n, \frac{6+n}{2}, -e^{2 i (c+d x)} \right] + \right. \right. \\
 & \quad \left. \left. A e^{2 i (c+d x)} (4+n) \text{Hypergeometric2F1} \left[ 4+n, \frac{6+n}{2}, \frac{8+n}{2}, -e^{2 i (c+d x)} \right] \right) \right) \\
 & \quad \left. \left. \text{Sec}[c+d x]^{-2-n} (b \text{Sec}[c+d x])^n (A+C \text{Sec}[c+d x]^2) \right) \right) / \left( d (A+2C+A \text{Cos}[2c+2d x]) \right)
 \end{aligned}$$

**Problem 29: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \text{Sec}[c+d x] (b \text{Sec}[c+d x])^n (A+C \text{Sec}[c+d x]^2) dx$$

Optimal (type 5, 109 leaves, 4 steps):

$$\begin{aligned}
 & \left( (C(1+n) + A(2+n)) \text{Hypergeometric2F1} \left[ \frac{1}{2}, -\frac{n}{2}, \frac{2-n}{2}, \text{Cos}[c+d x]^2 \right] (b \text{Sec}[c+d x])^n \right. \\
 & \quad \left. \text{Sin}[c+d x] \right) / \left( d n (2+n) \sqrt{\text{Sin}[c+d x]^2} \right) + \frac{C (b \text{Sec}[c+d x])^{1+n} \text{Tan}[c+d x]}{b d (2+n)}
 \end{aligned}$$

Result (type 5, 284 leaves):

$$\begin{aligned}
 & - \left( \int \left( i 2^{2+n} e^{i (c-d n x)} \left( \frac{e^{i (c+d x)}}{1 + e^{2 i (c+d x)}} \right)^n (1 + e^{2 i (c+d x)})^n \right. \right. \\
 & \quad \left( \frac{A e^{i d (1+n) x} \text{Hypergeometric2F1} \left[ \frac{1+n}{2}, 3+n, \frac{3+n}{2}, -e^{2 i (c+d x)} \right]}{1+n} + \frac{1}{3+n} \right. \\
 & \quad \left. 2(A+2C) e^{i (2c+d(3+n)x} \text{Hypergeometric2F1} \left[ \frac{3+n}{2}, 3+n, \frac{5+n}{2}, -e^{2 i (c+d x)} \right] + \frac{1}{5+n} \right. \\
 & \quad \left. \left. A e^{i (4c+d(5+n)x} \text{Hypergeometric2F1} \left[ 3+n, \frac{5+n}{2}, \frac{7+n}{2}, -e^{2 i (c+d x)} \right] \right) \text{Sec}[c+d x]^{-2-n} \right) \\
 & \quad \left. \left. (b \text{Sec}[c+d x])^n (A+C \text{Sec}[c+d x]^2) \right) \right) / \left( d (A+2C+A \text{Cos}[2c+2d x]) \right)
 \end{aligned}$$

**Problem 30: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int (b \operatorname{Sec}[c+dx])^n (A+C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 5, 113 leaves, 3 steps):

$$-\left( \left( b (A+An+Cn) \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{1-n}{2}, \frac{3-n}{2}, \cos[c+dx]^2 \right] (b \operatorname{Sec}[c+dx])^{-1+n} \right. \right. \\ \left. \left. \operatorname{Sin}[c+dx] \right) / \left( d (1-n) (1+n) \sqrt{\operatorname{Sin}[c+dx]^2} \right) \right) + \frac{C (b \operatorname{Sec}[c+dx])^n \operatorname{Tan}[c+dx]}{d (1+n)}$$

Result (type 5, 262 leaves):

$$-\frac{1}{dn(2+n)(4+n)(A+2C+A \cos[2c+2dx])} i^{2^{1+n}} \left( \frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}} \right)^n \\ (1+e^{2i(c+dx)})^n \left( A(8+6n+n^2) \operatorname{Hypergeometric2F1} \left[ \frac{n}{2}, 2+n, \frac{2+n}{2}, -e^{2i(c+dx)} \right] + \right. \\ \left. 2(A+2C) e^{2i(c+dx)} n(4+n) \operatorname{Hypergeometric2F1} \left[ \frac{2+n}{2}, 2+n, \frac{4+n}{2}, -e^{2i(c+dx)} \right] + \right. \\ \left. A e^{4i(c+dx)} n(2+n) \operatorname{Hypergeometric2F1} \left[ 2+n, \frac{4+n}{2}, \frac{6+n}{2}, -e^{2i(c+dx)} \right] \right) \\ \operatorname{Sec}[c+dx]^{-2-n} (b \operatorname{Sec}[c+dx])^n (A+C \operatorname{Sec}[c+dx]^2)$$

**Problem 31: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c+dx] (b \operatorname{Sec}[c+dx])^n (A+C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 5, 117 leaves, 4 steps):

$$\left( b^2 (C(1-n) - An) \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{2-n}{2}, \frac{4-n}{2}, \cos[c+dx]^2 \right] (b \operatorname{Sec}[c+dx])^{-2+n} \right. \\ \left. \operatorname{Sin}[c+dx] \right) / \left( d(2-n)n \sqrt{\operatorname{Sin}[c+dx]^2} \right) + \frac{bC (b \operatorname{Sec}[c+dx])^{-1+n} \operatorname{Tan}[c+dx]}{dn}$$

Result (type 6, 6049 leaves):

$$-\left( \left( 6 \operatorname{Sec}[c+dx]^{-n} (b \operatorname{Sec}[c+dx])^n \right. \right. \\ \left. \left( \frac{1}{2} A \cos[2(c+dx)] \operatorname{Sec}[c+dx]^{1+n} + \operatorname{Sec}[c+dx] \left( \frac{1}{2} A \operatorname{Sec}[c+dx]^n + C \operatorname{Sec}[c+dx]^n \right) \right) \right. \\ \left. \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \left( \frac{1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{1 - \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \right)^n \right)$$



$$\begin{aligned}
 & \left( \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)^2 \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 2 - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right] \right]^2, \right. \right. \\
 & \quad \left. \left. - \tan \left[ \frac{1}{2} (c + d x) \right] \right)^2 + 2 \left( (-2 + n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 3 - n, \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + n \operatorname{AppellF1} \left[ \frac{3}{2}, 1 + n, 2 - n, \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) + \\
 & \left( C \operatorname{AppellF1} \left[ \frac{1}{2}, 1 + n, -n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) / \\
 & \left( \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)^2 \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, 1 + n, -n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right] \right]^2, \right. \right. \\
 & \quad \left. \left. - \tan \left[ \frac{1}{2} (c + d x) \right] \right)^2 + 2 \left( n \operatorname{AppellF1} \left[ \frac{3}{2}, 1 + n, 1 - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. - \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + (1 + n) \operatorname{AppellF1} \left[ \frac{3}{2}, 2 + n, -n, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) - \\
 & 6 n \tan \left[ \frac{1}{2} (c + d x) \right] \left( \frac{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2} \right)^{-1+n} \left( \frac{\sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right]}{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2} + \right. \\
 & \quad \left. \frac{\sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right)}{\left( 1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right)^2} \right) \\
 & \left( \left( A \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1 - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \right) / \\
 & \left( \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)^2 \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1 - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right] \right]^2, \right. \right. \\
 & \quad \left. \left. - \tan \left[ \frac{1}{2} (c + d x) \right] \right)^2 + 2 \left( (-1 + n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 2 - n, \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + n \operatorname{AppellF1} \left[ \frac{3}{2}, 1 + n, 1 - n, \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) - \\
 & \left( 2 A \operatorname{AppellF1} \left[ \frac{1}{2}, n, 2 - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) / \\
 & \left( \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)^2 \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 2 - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right] \right]^2, \right. \right. \\
 & \quad \left. \left. - \tan \left[ \frac{1}{2} (c + d x) \right] \right)^2 + 2 \left( (-2 + n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 3 - n, \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + n \operatorname{AppellF1} \left[ \frac{3}{2}, 1 + n, 2 - n, \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left( C \operatorname{AppellF1} \left[ \frac{1}{2}, 1+n, -n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) / \\
 & \left( \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, 1+n, -n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + 2 \left( n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + (1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, 2+n, -n, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) - \\
 6 \tan \left[ \frac{1}{2} (c+dx) \right] & \left( \frac{\left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^n}{\left( 1 - \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^2} \right) \left( - \left( \left( A \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \right) / \\
 & \left( \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^2 \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 2-n, \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 1-n, \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) + \\
 (A \left( -\frac{1}{3} (1-n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{1}{3} n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \right) / \\
 & \left( \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 2-n, \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 1-n, \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) + \\
 (4 A \operatorname{AppellF1} \left[ \frac{1}{2}, n, 2-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \\
 & \quad \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) / \\
 & \left( \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^3 \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 2-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + 2 \left( (-2+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 3-n, \frac{5}{2}, \right. \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & \left( \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
 & \left. \left( 2A \left( -\frac{1}{3} (2-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right) \right) / \\
 & \left( \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \right. \\
 & \quad \left. \left. \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + 2 \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \right. \\
 & \quad \left. \left. \left. + n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right) \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \\
 & \left( C \operatorname{AppellF1}\left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) / \\
 & \left( \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \right. \\
 & \quad \left. \left. \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + 2 \left( n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \right. \\
 & \quad \left. \left. \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + (1+n) \operatorname{AppellF1}\left[\frac{3}{2}, 2+n, -n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right) \right) + \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + \\
 & \left( C \left( \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{3} (1+n) \operatorname{AppellF1}\left[\frac{3}{2}, 2+n, -n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right) \right) / \\
 & \left( \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \right. \\
 & \quad \left. \left. \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + 2 \left( n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \right. \\
 & \quad \left. \left. \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + (1+n) \operatorname{AppellF1}\left[\frac{3}{2}, 2+n, -n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right) \right) - \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \\
 & \left( A \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right)
 \end{aligned}$$



$$\begin{aligned}
 & \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \left( (-2+n) \left( -\frac{3}{5}(3-n) \operatorname{AppellF1}\left[\frac{5}{2}, n, 4-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \quad \left. \frac{3}{5} n \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, 3-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + n \left( -\frac{3}{5}(2-n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, \right. \right. \right. \\
 & \quad \left. \left. \left. 3-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right. \right. \\
 & \quad \left. \left. \left. + \frac{3}{5}(1+n) \operatorname{AppellF1}\left[\frac{5}{2}, 2+n, 2-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \right) / \\
 & \left( \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) - \\
 & \left( C \operatorname{AppellF1}\left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left( 2 \left( n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. (1+n) \operatorname{AppellF1}\left[\frac{3}{2}, 2+n, -n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 3 \left( \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \quad \left. \left. \frac{1}{3}(1+n) \operatorname{AppellF1}\left[\frac{3}{2}, 2+n, -n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) + 2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \left( n \left( -\frac{3}{5}(1-n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, 2-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{3}{5}(1+n) \right. \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{5}{2}, 2+n, 1-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) + (1+n) \left( \frac{3}{5} n \operatorname{AppellF1}\left[\frac{5}{2}, 2+n, \right. \right. \right.
 \end{aligned}$$

$$\left. \left( \left( \left( \left( \left( \left( 1-n, \frac{7}{2}, \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \text{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \text{Tan} \left[ \frac{1}{2} (c+dx) \right] + \frac{3}{5} (2+n) \text{AppellF1} \left[ \frac{5}{2}, 3+n, -n, \frac{7}{2}, \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \text{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \text{Tan} \left[ \frac{1}{2} (c+dx) \right] \right) \right) \right) \right) \right) \right) / \left( \left( \left( \left( -1 + \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \left( 3 \text{AppellF1} \left[ \frac{1}{2}, 1+n, -n, \frac{3}{2}, \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] + 2 \left( n \text{AppellF1} \left[ \frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] + (1+n) \text{AppellF1} \left[ \frac{3}{2}, 2+n, -n, \frac{5}{2}, \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \right) \right) \right) \right) \right)$$

**Problem 32: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \text{Cos}[c+dx]^2 (b \text{Sec}[c+dx])^n (A+C \text{Sec}[c+dx]^2) dx$$

Optimal (type 5, 132 leaves, 4 steps):

$$-\left( \left( b^3 (A(1-n) + C(2-n)) \text{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3-n}{2}, \frac{5-n}{2}, \text{Cos}[c+dx]^2 \right] (b \text{Sec}[c+dx])^{-3+n} \text{Sin}[c+dx] \right) / \left( d(1-n)(3-n) \sqrt{\text{Sin}[c+dx]^2} \right) \right) - \frac{b^2 C (b \text{Sec}[c+dx])^{-2+n} \text{Tan}[c+dx]}{d(1-n)}$$

Result (type 6, 8395 leaves):

$$\left( 6 \text{Sec}[c+dx]^{-n} (b \text{Sec}[c+dx])^n \left( \frac{1}{2} A \text{Sec}[c+dx]^n + C \text{Sec}[c+dx]^n + \frac{1}{2} A \text{Cos}[2(c+dx)] \text{Sec}[c+dx]^n \right) \text{Tan} \left[ \frac{1}{2} (c+dx) \right] \left( \frac{1}{1 - \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \right)^n \left( 1 + \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right)^{-3+n} \left( \left( A \text{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \left( 1 + \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right)^2 \right) / \left( 3 \text{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] + 2 \left( (-1+n) \text{AppellF1} \left[ \frac{3}{2}, n, 2-n, \frac{5}{2}, \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] + n \text{AppellF1} \left[ \frac{3}{2}, n, 2-n, \frac{5}{2}, \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \right) \right)$$

$$\begin{aligned}
 & \left. \left( \frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + \\
 & \left( C \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left. \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \right. \\
 & \quad \left. \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \\
 & \left( 4 A \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left. \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \right. \\
 & \quad \left. \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + \\
 & \left( 4 A \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \right. \\
 & \quad \left. \left( (-3+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \\
 & \left( d \left( 6 (-3+n) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( \frac{1}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^n \right. \right. \\
 & \quad \left. \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^{-4+n} \left( \left( A \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) \right) / \right. \\
 & \quad \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + \left( C \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{2}(c+dx)\right]^2 \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^2 - \left(4A \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \left( (-2+n) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + n \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + \\
 & \left(4A \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \left( (-3+n) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + n \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. 1+n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \Big/ \\
 & 3 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left(\frac{1}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}\right)^n \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^{-3+n} \\
 & \left( \left( A \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \right) \right) \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^2 + \left(C \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \\
 & \quad \tan \left[ \frac{1}{2} (c+dx) \right]^2 - \left( 4A \operatorname{AppellF1} \left[ \frac{1}{2}, n, 2-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 2-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + 2 \left( (-2+n) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, n, 3-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + n \operatorname{AppellF1} \left[ \frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. 1+n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) + \\
 & \left( 4A \operatorname{AppellF1} \left[ \frac{1}{2}, n, 3-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 3-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + 2 \left( (-3+n) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, n, 4-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + n \operatorname{AppellF1} \left[ \frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. 1+n, 3-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) + \\
 & 6n \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right]^2 \left( \frac{1}{1 - \tan \left[ \frac{1}{2} (c+dx) \right]^2} \right)^{1+n} \\
 & \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^{-3+n} \\
 & \left( \left( A \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \right. \\
 & \quad \left. \left. \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^2 \right) \right) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \\
 & \quad \tan \left[ \frac{1}{2} (c+dx) \right]^2 + \left( C \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^2 \right) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \left. 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^2 - \left(4A \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2\left((-2+n) \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + n \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
 & \left. \left. \left. 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2\right) + \\
 & \left(4A \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2\left((-3+n) \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + n \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
 & \left. \left. \left. 1+n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2\right) + \\
 & 6 \tan\left[\frac{1}{2}(c+dx)\right] \left(\frac{1}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}\right)^n \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^{-3+n} \\
 & \left(\left(2A \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right)\right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2\left((-1+n) \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + n \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
 & \left. \left. \left. 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2\right) + \\
 & \left(2C \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \left. 2\left((-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \right. \\
 & \left. \tan\left[\frac{1}{2}(c+dx)\right]^2\right) + \left(A \left(-\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \right. \right. \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & \left. \begin{aligned}
 & \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \\
 & \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
 & \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \right) \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^2 \Big) + \left( C \left( -\frac{1}{3} (1-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \left. \left. \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
 & \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \right) \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \right) \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^2 \Big) - \left(4 A \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & 2 \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \right) \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^2 \Big) - \left(4 A \left( -\frac{1}{3} (2-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \left. \left. \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
 & \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \left( (-2+n) \right) \right)
 \end{aligned}
 \right.
 \end{aligned}$$

$$\begin{aligned}
 & \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + n \operatorname{AppellF1}\left[\frac{3}{2}, \right. \\
 & \quad \left. 1+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \Big) + \\
 & \left(4A \left(-\frac{1}{3}(3-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{1}{3}n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right] \Big) \Big) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. 2 \left( (-3+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 - \left( A \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \right. \right. \\
 & \quad \left. \left( 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \right. \\
 & \quad \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 3 \left( -\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \quad \left. \left. \frac{1}{3}n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) + 2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \left. \left( (-1+n) \left( -\frac{3}{5}(2-n) \operatorname{AppellF1}\left[\frac{5}{2}, n, 3-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \quad \left. \left. \frac{3}{5}n \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, 2-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) + n \left( -\frac{3}{5}(1-n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, \right. \right. \right. \\
 & \quad \left. \left. 2-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[ \right. \right. \\
 & \quad \left. \left. \frac{1}{2}(c+dx)\right] + \frac{3}{5}(1+n) \operatorname{AppellF1}\left[\frac{5}{2}, 2+n, 1-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \Big) \Big) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \quad n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \quad \quad \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 - \\
 & \left. \left( C \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \left( 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \quad \left. \left. 3 \left( -\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \right. \\
 & \quad \quad \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) + \right. \\
 & \quad \left. 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( (-1+n) \left( -\frac{3}{5}(2-n) \operatorname{AppellF1}\left[\frac{5}{2}, n, 3-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{3}{5} n \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \right. \\
 & \quad \quad \left. \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + n \left( -\frac{3}{5}(1-n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, \right. \right. \right. \\
 & \quad \quad \left. \left. \left. 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right. \right. \right. \\
 & \quad \quad \left. \left. \left. + \frac{3}{5}(1+n) \operatorname{AppellF1}\left[\frac{5}{2}, 2+n, 1-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \right) / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \quad n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \quad \quad \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 + \\
 & \left. \left( 4 A \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
& \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
& \left( 2 \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
& \quad \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
& \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 3 \left( -\frac{1}{3}(2-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
& \quad \left. \left. \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
& \quad \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
& \quad \left( (-2+n) \left( -\frac{3}{5}(3-n) \operatorname{AppellF1}\left[\frac{5}{2}, n, 4-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{3}{5} n \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, 3-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
& \quad \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + n \left( -\frac{3}{5}(2-n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, \right. \right. \\
& \quad \left. \left. 3-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right. \right. \\
& \quad \left. \left. + \frac{3}{5}(1+n) \operatorname{AppellF1}\left[\frac{5}{2}, 2+n, 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) / \\
& \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2 \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 - \\
& \left( 4 A \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left( 2 \left( (-3+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
& \quad \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
& \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 3 \left( -\frac{1}{3}(3-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \left( (-3+n) \left( -\frac{3}{5} (4-n) \operatorname{AppellF1}\left[\frac{5}{2}, n, 5-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \quad \left. \frac{3}{5} n \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, 4-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + n \left( -\frac{3}{5} (3-n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, \right. \right. \\
 & \quad \left. \left. 4-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right. \\
 & \quad \left. \left. + \frac{3}{5} (1+n) \operatorname{AppellF1}\left[\frac{5}{2}, 2+n, 3-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \Bigg) / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. 2 \left( (-3+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \Bigg)
 \end{aligned}$$

**Problem 33: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c+dx]^3 (b \sec[c+dx])^n (A+C \sec[c+dx]^2) dx$$

Optimal (type 5, 132 leaves, 4 steps):

$$\begin{aligned}
 & - \left( \left( b^4 (A(2-n) + C(3-n)) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{4-n}{2}, \frac{6-n}{2}, \cos[c+dx]^2\right] (b \sec[c+dx])^{-4+n} \right. \right. \\
 & \quad \left. \left. \sin[c+dx] \right) / \left( d(2-n)(4-n) \sqrt{\sin[c+dx]^2} \right) - \frac{b^3 C (b \sec[c+dx])^{-3+n} \tan[c+dx]}{d(2-n)} \right)
 \end{aligned}$$

Result (type 6, 12608 leaves):

$$\begin{aligned}
 & - \left( \left( 6 b \sec[c+dx]^{1-n} (b \sec[c+dx])^{-1+n} \right. \right. \\
 & \quad \left. \left. \left( \frac{1}{2} A \cos[2(c+dx)] \sec[c+dx]^{-1+n} + \cos[c+dx] \left( \frac{1}{2} A \sec[c+dx]^n + C \sec[c+dx]^n \right) \right) \right)
 \end{aligned}$$

$$\begin{aligned}
& \tan\left[\frac{1}{2}(c+dx)\right] \left(\frac{1}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}\right)^n \left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^{-4+n} \\
& \left(\left(A \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right.\right. \\
& \quad \left.\left. \left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^3\right)\right) / \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2 \left(\left(-1+n\right) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \\
& \quad \tan\left[\frac{1}{2}(c+dx)\right]^2 + \left(C \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right.\right. \\
& \quad \left.\left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^3\right) / \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2 \left(\left(-1+n\right) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \\
& \quad \tan\left[\frac{1}{2}(c+dx)\right]^2 - \left(6 A \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right.\right. \\
& \quad \left.\left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2\right) / \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2 \left(\left(-2+n\right) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \\
& \quad \tan\left[\frac{1}{2}(c+dx)\right]^2 - \left(2 C \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right.\right. \\
& \quad \left.\left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2\right) / \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2 \left(\left(-2+n\right) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \\
& \quad \tan\left[\frac{1}{2}(c+dx)\right]^2 + \left(12 A \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right.\right.
\end{aligned}$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{2}(c+dx)\right]^2 \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2\left((-3+n) \right. \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + n \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \\
 & \quad \left. \left. 1+n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 - \right. \\
 & \left. \left(8 A \operatorname{AppellF1}\left[\frac{1}{2}, n, 4-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \Big/ \right. \\
 & \left. \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 4-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2\left((-4+n) \right. \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}, n, 5-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + n \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. 1+n, 4-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \Big/ \\
 & \left(d \left(-6(-4+n) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left(\frac{1}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}\right)^n \right. \right. \\
 & \quad \left. \left. \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^{-5+n} \left(\left(A \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^3\right) \Big/ \right. \right. \\
 & \quad \left. \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \quad \left. 2\left((-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2\right) + \left(C \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^3\right) \Big/ \right. \\
 & \quad \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. 2\left((-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2\right) - \left(6 A \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2\right) \Big/ \\
 & \quad \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 \left( (-2+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 3-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \\
 & \quad \tan \left[ \frac{1}{2} (c+dx) \right]^2 - \left( 2C \operatorname{AppellF1} \left[ \frac{1}{2}, n, 2-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^2 \right) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 2-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & 2 \left( (-2+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 3-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \\
 & \quad \tan \left[ \frac{1}{2} (c+dx) \right]^2 + \left( 12A \operatorname{AppellF1} \left[ \frac{1}{2}, n, 3-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 3-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & 2 \left( (-3+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 4-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 - \\
 & \left( 8A \operatorname{AppellF1} \left[ \frac{1}{2}, n, 4-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 4-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & 2 \left( (-4+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 5-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 4-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) - \\
 & 3 \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \left( \frac{1}{1 - \tan \left[ \frac{1}{2} (c+dx) \right]^2} \right)^n \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^{-4+n} \\
 & \left( \left( A \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \right. \\
 & \quad \left. \left. \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^3 \right) \right) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right.
 \end{aligned}$$



$$\begin{aligned}
 & 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \\
 & \quad \tan \left[ \frac{1}{2} (c+dx) \right]^2 + \left( C \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^3 \right) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \\
 & \quad \tan \left[ \frac{1}{2} (c+dx) \right]^2 - \left( 6 A \operatorname{AppellF1} \left[ \frac{1}{2}, n, 2-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^2 \right) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 2-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & 2 \left( (-2+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 3-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \\
 & \quad \tan \left[ \frac{1}{2} (c+dx) \right]^2 - \left( 2 C \operatorname{AppellF1} \left[ \frac{1}{2}, n, 2-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^2 \right) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 2-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & 2 \left( (-2+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 3-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \\
 & \quad \tan \left[ \frac{1}{2} (c+dx) \right]^2 + \left( 12 A \operatorname{AppellF1} \left[ \frac{1}{2}, n, 3-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 3-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & 2 \left( (-3+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 4-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 -
 \end{aligned}$$

$$\begin{aligned}
 & \left( 8 A \operatorname{AppellF1}\left[\frac{1}{2}, n, 4-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 4-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad 2 \left( (-4+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 5-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \quad n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 4-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \quad \quad \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \\
 & 6 n \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( \frac{1}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1+n} \\
 & \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^{-4+n} \\
 & \left( \left( A \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
 & \quad \left. \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^3 \right) / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \quad n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
 & \quad \tan\left[\frac{1}{2}(c+dx)\right]^2 + \left( C \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^3 \right) / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \quad n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
 & \quad \tan\left[\frac{1}{2}(c+dx)\right]^2 - \left( 6 A \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad 2 \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \quad n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \tan\left[\frac{1}{2}(c+dx)\right]^2 - \left(2 C \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right.\right. \\
 & \quad \left. \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2\right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad 2 \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \quad \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
 & \quad \tan\left[\frac{1}{2}(c+dx)\right]^2 + \left(12 A \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right.\right. \\
 & \quad \left. \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad 2 \left( (-3+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \quad \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right.\right. \\
 & \quad \quad \left. \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 - \\
 & \left(8 A \operatorname{AppellF1}\left[\frac{1}{2}, n, 4-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 4-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad 2 \left( (-4+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 5-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \quad \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 4-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right.\right. \\
 & \quad \quad \left. \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \\
 & 6 \tan\left[\frac{1}{2}(c+dx)\right] \left(\frac{1}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}\right)^n \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^{-4+n} \\
 & \left( \left(3 A \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right.\right. \\
 & \quad \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2\right) \right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \quad \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{2}(c+dx)\right]^2\right)\tan\left[\frac{1}{2}(c+dx)\right]^2\right)+ \\
 & \left(3C\operatorname{AppellF1}\left[\frac{1}{2},n,1-n,\frac{3}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,-\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right. \\
 & \quad \left.\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2\tan\left[\frac{1}{2}(c+dx)\right]\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2\right)\right)/ \\
 & \left(3\operatorname{AppellF1}\left[\frac{1}{2},n,1-n,\frac{3}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,-\tan\left[\frac{1}{2}(c+dx)\right]^2\right]+ \right. \\
 & \quad 2\left(\left(-1+n\right)\operatorname{AppellF1}\left[\frac{3}{2},n,2-n,\frac{5}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,-\tan\left[\frac{1}{2}(c+dx)\right]^2\right]+ \right. \\
 & \quad \left. n\operatorname{AppellF1}\left[\frac{3}{2},1+n,1-n,\frac{5}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,-\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \\
 & \quad \tan\left[\frac{1}{2}(c+dx)\right]^2\right)+\left(A\left(-\frac{1}{3}(1-n)\operatorname{AppellF1}\left[\frac{3}{2},n,2-n,\frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2,-\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2\tan\left[\frac{1}{2}(c+dx)\right]+\frac{1}{3} \right. \right. \\
 & \quad \left. \left. n\operatorname{AppellF1}\left[\frac{3}{2},1+n,1-n,\frac{5}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,-\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2\tan\left[\frac{1}{2}(c+dx)\right]\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^3\right)\right)/ \\
 & \left(3\operatorname{AppellF1}\left[\frac{1}{2},n,1-n,\frac{3}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,-\tan\left[\frac{1}{2}(c+dx)\right]^2\right]+ \right. \\
 & \quad 2\left(\left(-1+n\right)\operatorname{AppellF1}\left[\frac{3}{2},n,2-n,\frac{5}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,-\tan\left[\frac{1}{2}(c+dx)\right]^2\right]+ \right. \\
 & \quad \left. n\operatorname{AppellF1}\left[\frac{3}{2},1+n,1-n,\frac{5}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,-\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \\
 & \quad \tan\left[\frac{1}{2}(c+dx)\right]^2\right)+\left(C\left(-\frac{1}{3}(1-n)\operatorname{AppellF1}\left[\frac{3}{2},n,2-n,\frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2,-\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2\tan\left[\frac{1}{2}(c+dx)\right]+\frac{1}{3} \right. \right. \\
 & \quad \left. \left. n\operatorname{AppellF1}\left[\frac{3}{2},1+n,1-n,\frac{5}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,-\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2\tan\left[\frac{1}{2}(c+dx)\right]\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^3\right)\right)/ \\
 & \left(3\operatorname{AppellF1}\left[\frac{1}{2},n,1-n,\frac{3}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,-\tan\left[\frac{1}{2}(c+dx)\right]^2\right]+ \right. \\
 & \quad 2\left(\left(-1+n\right)\operatorname{AppellF1}\left[\frac{3}{2},n,2-n,\frac{5}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,-\tan\left[\frac{1}{2}(c+dx)\right]^2\right]+ \right. \\
 & \quad \left. n\operatorname{AppellF1}\left[\frac{3}{2},1+n,1-n,\frac{5}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,-\tan\left[\frac{1}{2}(c+dx)\right]^2\right], \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right)\tan\left[\frac{1}{2}(c+dx)\right]^2\right)- \\
 & \left(12A\operatorname{AppellF1}\left[\frac{1}{2},n,2-n,\frac{3}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,-\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \\
 & \quad \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2\tan\left[\frac{1}{2}(c+dx)\right]\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right)/
 \end{aligned}$$



$$\begin{aligned}
 & \tan\left[\frac{1}{2}(c+dx)\right]^2 + \left(12A \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \right. \\
 & \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \left. 2\left((-3+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right)\right) \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^2 + \left(12A\left(-\frac{1}{3}(3-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{3} \right. \right. \\
 & \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \left. 2\left((-3+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2\right) - \\
 & \left(8A\left(-\frac{1}{3}(4-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 5-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{3}n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 4-n, \frac{5}{2}, \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right)\right) \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 4-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \left. 2\left((-4+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 5-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 4-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right)\right) \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^2 - \left(A \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^3 \right. \\
 & \left. \left(2\left((-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \right. \\
 & \left. \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right)\right)\right)
 \end{aligned}$$

$$\begin{aligned}
 & \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right] + 3 \left(-\frac{1}{3}(1-n) \text{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \right.\right. \\
 & \quad \left.\left.\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left.\frac{1}{3}n \text{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left.\text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right]\right) + 2 \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \left( (-1+n) \left(-\frac{3}{5}(2-n) \text{AppellF1}\left[\frac{5}{2}, n, 3-n, \frac{7}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right.\right.\right. \\
 & \quad \left.\left.\left.-\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right] + \right.\right. \\
 & \quad \left.\frac{3}{5}n \text{AppellF1}\left[\frac{5}{2}, 1+n, 2-n, \frac{7}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left.\text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right]\right) + n \left(-\frac{3}{5}(1-n) \text{AppellF1}\left[\frac{5}{2}, 1+n, \right.\right. \\
 & \quad \left.\left.2-n, \frac{7}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left.\frac{1}{2}(c+dx)\right) + \frac{3}{5}(1+n) \text{AppellF1}\left[\frac{5}{2}, 2+n, 1-n, \frac{7}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \quad \left.\left.-\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right]\right) \Big) \Big) \Big) \Big) / \\
 & \left( 3 \text{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \right. \\
 & \quad \left( (-1+n) \text{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. n \text{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right.\right. \\
 & \quad \left.\left.-\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 - \\
 & \left( C \text{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left. \left(1 + \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^3 \right. \\
 & \quad \left. \left( 2 \left( (-1+n) \text{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right.\right. \right. \\
 & \quad \left. \left. n \text{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
 & \quad \left. \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right] + 3 \left(-\frac{1}{3}(1-n) \text{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \right.\right. \right. \\
 & \quad \left.\left.\left.\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right] + \right.\right. \\
 & \quad \left.\frac{1}{3}n \text{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left.\left.\text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right]\right) + 2 \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( (-1+n) \left( -\frac{3}{5} (2-n) \operatorname{AppellF1} \left[ \frac{5}{2}, n, 3-n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \right. \\
 & \quad \left. \frac{3}{5} n \operatorname{AppellF1} \left[ \frac{5}{2}, 1+n, 2-n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) + n \left( -\frac{3}{5} (1-n) \operatorname{AppellF1} \left[ \frac{5}{2}, 1+n, \right. \right. \\
 & \quad \left. \left. 2-n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \right. \right. \\
 & \quad \left. \left. \frac{1}{2} (c+dx) \right] + \frac{3}{5} (1+n) \operatorname{AppellF1} \left[ \frac{5}{2}, 2+n, 1-n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \Big) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + 2 \right. \\
 & \quad \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \Big)^2 + \\
 & \left( 6 A \operatorname{AppellF1} \left[ \frac{1}{2}, n, 2-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
 & \quad \left. \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^2 \right. \\
 & \quad \left( 2 \left( (-2+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 3-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \right. \\
 & \quad \left. \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \right. \\
 & \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + 3 \left( -\frac{1}{3} (2-n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 3-n, \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \right. \\
 & \quad \left. \frac{1}{3} n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
 & \quad \left. \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) + 2 \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right. \\
 & \quad \left( (-2+n) \left( -\frac{3}{5} (3-n) \operatorname{AppellF1} \left[ \frac{5}{2}, n, 4-n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \right. \\
 & \quad \left. \frac{3}{5} n \operatorname{AppellF1} \left[ \frac{5}{2}, 1+n, 3-n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
 & \quad \left. \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) + n \left( -\frac{3}{5} (2-n) \operatorname{AppellF1} \left[ \frac{5}{2}, 1+n, \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & \left( 3 - n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \\
 & + \frac{3}{5}(1+n) \operatorname{AppellF1}\left[\frac{5}{2}, 2+n, 2-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \\
 & \left. \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right) \right) / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \right. \\
 & \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
 & \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + \\
 & \left( 2 C \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
 & \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \\
 & \left( 2 \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right) \\
 & \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 3 \left( -\frac{1}{3}(2-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \left. \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
 & \left. \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) + 2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \left( (-2+n) \left( -\frac{3}{5}(3-n) \operatorname{AppellF1}\left[\frac{5}{2}, n, 4-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right) \\
 & \left. \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) + \\
 & \frac{3}{5} n \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, 3-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \\
 & \left. \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) + n \left( -\frac{3}{5}(2-n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, \right. \right. \\
 & \left. \left. 3-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right. \\
 & \left. \left. \left. \left. \left. \left. \frac{1}{2}(c+dx)\right] + \frac{3}{5}(1+n) \operatorname{AppellF1}\left[\frac{5}{2}, 2+n, 2-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \right) \right) \right) / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \right)
 \end{aligned}$$

$$\begin{aligned}
& \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
& \quad \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 - \\
& \left( 12A \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
& \quad \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
& \left( 2 \left( (-3+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
& \quad \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right) \\
& \quad \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 3 \left( -\frac{1}{3}(3-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \right. \right. \\
& \quad \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + \\
& \quad \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
& \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \left( (-3+n) \left( -\frac{3}{5}(4-n) \operatorname{AppellF1}\left[\frac{5}{2}, n, 5-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
& \quad \left. \frac{3}{5} n \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, 4-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + n \left( -\frac{3}{5}(3-n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, \right. \right. \right. \\
& \quad \left. \left. 4-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{3}{5}(1+n) \operatorname{AppellF1}\left[\frac{5}{2}, 2+n, 3-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \Big/ \\
& \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \right. \\
& \quad \left( (-3+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + \\
& \left( 8A \operatorname{AppellF1}\left[\frac{1}{2}, n, 4-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right)
\end{aligned}$$

$$\begin{aligned}
& \left( 2 \left( (-4 + n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 5 - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + \right. \right. \\
& \quad \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1 + n, 4 - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) \\
& \quad \sec \left[ \frac{1}{2} (c + dx) \right]^2 \tan \left[ \frac{1}{2} (c + dx) \right] + 3 \left( -\frac{1}{3} (4 - n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 5 - n, \frac{5}{2}, \right. \right. \\
& \quad \quad \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \sec \left[ \frac{1}{2} (c + dx) \right]^2 \tan \left[ \frac{1}{2} (c + dx) \right] + \\
& \quad \left. \frac{1}{3} n \operatorname{AppellF1} \left[ \frac{3}{2}, 1 + n, 4 - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) \\
& \quad \left. \sec \left[ \frac{1}{2} (c + dx) \right]^2 \tan \left[ \frac{1}{2} (c + dx) \right] \right) + 2 \tan \left[ \frac{1}{2} (c + dx) \right]^2 \\
& \quad \left( (-4 + n) \left( -\frac{3}{5} (5 - n) \operatorname{AppellF1} \left[ \frac{5}{2}, n, 6 - n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \right. \right. \right. \\
& \quad \quad \left. \left. -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \sec \left[ \frac{1}{2} (c + dx) \right]^2 \tan \left[ \frac{1}{2} (c + dx) \right] + \right. \\
& \quad \quad \left. \frac{3}{5} n \operatorname{AppellF1} \left[ \frac{5}{2}, 1 + n, 5 - n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) \\
& \quad \quad \left. \sec \left[ \frac{1}{2} (c + dx) \right]^2 \tan \left[ \frac{1}{2} (c + dx) \right] \right) + n \left( -\frac{3}{5} (4 - n) \operatorname{AppellF1} \left[ \frac{5}{2}, 1 + n, \right. \right. \\
& \quad \quad \left. \left. 5 - n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \sec \left[ \frac{1}{2} (c + dx) \right]^2 \tan \left[ \right. \right. \\
& \quad \quad \left. \left. \frac{1}{2} (c + dx) \right] + \frac{3}{5} (1 + n) \operatorname{AppellF1} \left[ \frac{5}{2}, 2 + n, 4 - n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \right. \right. \\
& \quad \quad \left. \left. -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \sec \left[ \frac{1}{2} (c + dx) \right]^2 \tan \left[ \frac{1}{2} (c + dx) \right] \right) \right) \Big/ \\
& \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 4 - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + 2 \right. \\
& \quad \left( (-4 + n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 5 - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + \right. \\
& \quad \quad \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1 + n, 4 - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \right. \right. \\
& \quad \quad \left. \left. -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \right) \Big) \Big) \Big) \Big) \Big) \Big)
\end{aligned}$$

**Problem 34:** Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \sec[c + dx]^{5/2} (b \sec[c + dx])^n (A + C \sec[c + dx]^2) dx$$

Optimal (type 5, 142 leaves, 4 steps):

$$\frac{2 C \operatorname{Sec}[c+d x]^{7/2} (b \operatorname{Sec}[c+d x])^n \operatorname{Sin}[c+d x]}{d(7+2 n)} +$$

$$\left( 2 (C(5+2 n) + A(7+2 n)) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{4}(-3-2 n), \frac{1}{4}(1-2 n), \operatorname{Cos}[c+d x]^2\right] \right.$$

$$\left. \operatorname{Sec}[c+d x]^{3/2} (b \operatorname{Sec}[c+d x])^n \operatorname{Sin}[c+d x] \right) / \left( d(3+2 n)(7+2 n) \sqrt{\operatorname{Sin}[c+d x]^2} \right)$$

Result (type 5, 341 leaves):

$$-\frac{1}{d(A+2 C+A \operatorname{Cos}[2 c+2 d x])} i^{2 \frac{9}{2}+n} e^{2 i c-\frac{1}{2} i d(1+2 n)} x \left( \frac{e^{i(c+d x)}}{1+e^{2 i(c+d x)}} \right)^{\frac{1}{2}+n} (1+e^{2 i(c+d x)})^{\frac{1}{2}+n}$$

$$\left( \frac{1}{5+2 n} A e^{\frac{1}{2} i d(5+2 n)} x \operatorname{Hypergeometric2F1}\left[\frac{9}{2}+n, \frac{1}{4}(5+2 n), \frac{1}{4}(9+2 n), -e^{2 i(c+d x)}\right] + \right.$$

$$\left( e^{\frac{1}{2} i(4 c+d(9+2 n))} x \left( 2(A+2 C)(13+2 n) \right. \right.$$

$$\left. \operatorname{Hypergeometric2F1}\left[\frac{9}{2}+n, \frac{1}{4}(9+2 n), \frac{1}{4}(13+2 n), -e^{2 i(c+d x)}\right] + A e^{2 i(c+d x)} \right.$$

$$\left. \left. (9+2 n) \operatorname{Hypergeometric2F1}\left[\frac{9}{2}+n, \frac{1}{4}(13+2 n), \frac{1}{4}(17+2 n), -e^{2 i(c+d x)}\right] \right) \right) /$$

$$\left( (9+2 n)(13+2 n) \right) \operatorname{Sec}[c+d x]^{-2-n} (b \operatorname{Sec}[c+d x])^n (A+C \operatorname{Sec}[c+d x]^2)$$

**Problem 35: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c+d x]^{3/2} (b \operatorname{Sec}[c+d x])^n (A+C \operatorname{Sec}[c+d x]^2) dx$$

Optimal (type 5, 142 leaves, 4 steps):

$$\frac{2 C \operatorname{Sec}[c+d x]^{5/2} (b \operatorname{Sec}[c+d x])^n \operatorname{Sin}[c+d x]}{d(5+2 n)} +$$

$$\left( 2 (C(3+2 n) + A(5+2 n)) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{4}(-1-2 n), \frac{1}{4}(3-2 n), \operatorname{Cos}[c+d x]^2\right] \right.$$

$$\left. \sqrt{\operatorname{Sec}[c+d x]} (b \operatorname{Sec}[c+d x])^n \operatorname{Sin}[c+d x] \right) / \left( d(1+2 n)(5+2 n) \sqrt{\operatorname{Sin}[c+d x]^2} \right)$$

Result (type 5, 335 leaves):

$$\begin{aligned}
 & - \frac{1}{d (A + 2 C + A \cos [2 c + 2 d x])} i^{2^{\frac{7}{2}+n}} e^{-\frac{1}{2} i d (3+2 n) x} \left( \frac{e^{i (c+d x)}}{1 + e^{2 i (c+d x)}} \right)^{\frac{3}{2}+n} (1 + e^{2 i (c+d x)})^{\frac{3}{2}+n} \\
 & \left( \frac{1}{3 + 2 n} A e^{\frac{1}{2} i d (3+2 n) x} \text{Hypergeometric2F1} \left[ \frac{7}{2} + n, \frac{1}{4} (3 + 2 n), \frac{1}{4} (7 + 2 n), -e^{2 i (c+d x)} \right] + \right. \\
 & \left. \left( e^{\frac{1}{2} i (4 c+d (7+2 n) x)} \left( 2 (A + 2 C) (11 + 2 n) \right. \right. \right. \\
 & \quad \left. \left. \text{Hypergeometric2F1} \left[ \frac{7}{2} + n, \frac{1}{4} (7 + 2 n), \frac{1}{4} (11 + 2 n), -e^{2 i (c+d x)} \right] + A e^{2 i (c+d x)} \right. \right. \\
 & \quad \left. \left. (7 + 2 n) \text{Hypergeometric2F1} \left[ \frac{7}{2} + n, \frac{1}{4} (11 + 2 n), \frac{1}{4} (15 + 2 n), -e^{2 i (c+d x)} \right] \right) \right) \Bigg/ \\
 & \left( (7 + 2 n) (11 + 2 n) \right) \text{Sec} [c + d x]^{-2-n} (b \text{Sec} [c + d x])^n (A + C \text{Sec} [c + d x]^2)
 \end{aligned}$$

**Problem 36: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \sqrt{\text{Sec} [c + d x]} (b \text{Sec} [c + d x])^n (A + C \text{Sec} [c + d x]^2) dx$$

Optimal (type 5, 140 leaves, 4 steps):

$$\begin{aligned}
 & \frac{2 C \text{Sec} [c + d x]^{3/2} (b \text{Sec} [c + d x])^n \text{Sin} [c + d x]}{d (3 + 2 n)} \\
 & \left( 2 (C + 2 C n + A (3 + 2 n)) \text{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{1}{4} (1 - 2 n), \frac{1}{4} (5 - 2 n), \text{Cos} [c + d x]^2 \right] \right. \\
 & \left. (b \text{Sec} [c + d x])^n \text{Sin} [c + d x] \right) \Bigg/ \left( d (1 - 2 n) (3 + 2 n) \sqrt{\text{Sec} [c + d x]} \sqrt{\text{Sin} [c + d x]^2} \right)
 \end{aligned}$$

Result (type 5, 336 leaves):

$$\begin{aligned}
 & - \frac{1}{A + 2 C + A \cos [2 c + 2 d x]} i^{2^{\frac{5}{2}+n}} e^{-\frac{1}{2} i d (1+2 n) x} \left( \frac{e^{i (c+d x)}}{1 + e^{2 i (c+d x)}} \right)^{\frac{1}{2}+n} (1 + e^{2 i (c+d x)})^{\frac{1}{2}+n} \\
 & \left( \frac{1}{d + 2 d n} A e^{\frac{1}{2} i (d+2 d n) x} \text{Hypergeometric2F1} \left[ \frac{5}{2} + n, \frac{1}{4} (1 + 2 n), \frac{1}{4} (5 + 2 n), -e^{2 i (c+d x)} \right] + \right. \\
 & \left. \left( e^{\frac{1}{2} i (4 c+d (5+2 n) x)} \left( 2 (A + 2 C) (9 + 2 n) \right. \right. \right. \\
 & \quad \left. \left. \text{Hypergeometric2F1} \left[ \frac{5}{2} + n, \frac{1}{4} (5 + 2 n), \frac{1}{4} (9 + 2 n), -e^{2 i (c+d x)} \right] + A e^{2 i (c+d x)} \right. \right. \\
 & \quad \left. \left. (5 + 2 n) \text{Hypergeometric2F1} \left[ \frac{5}{2} + n, \frac{1}{4} (9 + 2 n), \frac{1}{4} (13 + 2 n), -e^{2 i (c+d x)} \right] \right) \right) \Bigg/ \\
 & \left( d (5 + 2 n) (9 + 2 n) \right) \text{Sec} [c + d x]^{-2-n} (b \text{Sec} [c + d x])^n (A + C \text{Sec} [c + d x]^2)
 \end{aligned}$$

**Problem 37: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(b \operatorname{Sec}[c + d x])^n (A + C \operatorname{Sec}[c + d x]^2)}{\sqrt{\operatorname{Sec}[c + d x]}} dx$$

Optimal (type 5, 141 leaves, 4 steps):

$$\frac{2 C \sqrt{\operatorname{Sec}[c + d x]} (b \operatorname{Sec}[c + d x])^n \operatorname{Sin}[c + d x]}{d (1 + 2 n)} - \left( 2 (A - C (1 - 2 n) + 2 A n) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{4} (3 - 2 n), \frac{1}{4} (7 - 2 n), \operatorname{Cos}[c + d x]^2\right] (b \operatorname{Sec}[c + d x])^n \operatorname{Sin}[c + d x] \right) / \left( d (3 - 2 n) (1 + 2 n) \operatorname{Sec}[c + d x]^{3/2} \sqrt{\operatorname{Sin}[c + d x]^2} \right)$$

Result (type 5, 311 leaves):

$$\frac{1}{d (-1 + 2 n) (3 + 2 n) (7 + 2 n) (A + 2 C + A \operatorname{Cos}[2 c + 2 d x])} - i 2^{\frac{3}{2} + n} \left( \frac{e^{i (c + d x)}}{1 + e^{2 i (c + d x)}} \right)^{-\frac{1}{2} + n} (1 + e^{2 i (c + d x)})^{-\frac{1}{2} + n} \left( A (21 + 20 n + 4 n^2) \operatorname{Hypergeometric2F1}\left[\frac{3}{2} + n, \frac{1}{4} (-1 + 2 n), \frac{1}{4} (3 + 2 n), -e^{2 i (c + d x)}\right] + e^{2 i (c + d x)} (-1 + 2 n) \left( 2 (A + 2 C) (7 + 2 n) \operatorname{Hypergeometric2F1}\left[\frac{3}{2} + n, \frac{1}{4} (3 + 2 n), \frac{1}{4} (7 + 2 n), -e^{2 i (c + d x)}\right] + A e^{2 i (c + d x)} (3 + 2 n) \operatorname{Hypergeometric2F1}\left[\frac{3}{2} + n, \frac{1}{4} (7 + 2 n), \frac{1}{4} (11 + 2 n), -e^{2 i (c + d x)}\right] \right) \right) \operatorname{Sec}[c + d x]^{-2 - n} (b \operatorname{Sec}[c + d x])^n (A + C \operatorname{Sec}[c + d x]^2)$$

**Problem 38: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(b \operatorname{Sec}[c + d x])^n (A + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[c + d x]^{3/2}} dx$$

Optimal (type 5, 140 leaves, 4 steps):

$$\frac{2 C (b \operatorname{Sec}[c + d x])^n \operatorname{Sin}[c + d x]}{d (1 - 2 n) \sqrt{\operatorname{Sec}[c + d x]}} - \left( 2 (A + C (3 - 2 n) - 2 A n) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{4} (5 - 2 n), \frac{1}{4} (9 - 2 n), \operatorname{Cos}[c + d x]^2\right] (b \operatorname{Sec}[c + d x])^n \operatorname{Sin}[c + d x] \right) / \left( d (1 - 2 n) (5 - 2 n) \operatorname{Sec}[c + d x]^{5/2} \sqrt{\operatorname{Sin}[c + d x]^2} \right)$$

Result (type 5, 343 leaves):

$$\begin{aligned}
 & - \frac{1}{A + 2C + A \cos[2c + 2dx]} \\
 & \frac{1}{2^{1/2+n}} e^{-\frac{1}{2}i(4c+d(1+2n)x)} \left( \frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}} \right)^{\frac{1}{2}+n} (1 + e^{2i(c+dx)})^{\frac{1}{2}+n} \left( \frac{1}{d(-3+2n)} A e^{\frac{1}{2}id(-3+2n)x} \right. \\
 & \quad \text{Hypergeometric2F1}\left[\frac{1}{2} + n, \frac{1}{4}(-3+2n), \frac{1}{4}(1+2n), -e^{2i(c+dx)}\right] + \left( e^{\frac{1}{2}i(4c+d(1+2n)x)} \right. \\
 & \quad \left. \left( 2(A+2C)(5+2n) \text{Hypergeometric2F1}\left[\frac{1}{2} + n, \frac{1}{4}(1+2n), \frac{1}{4}(5+2n), -e^{2i(c+dx)}\right] + \right. \right. \\
 & \quad \left. \left. A e^{2i(c+dx)}(1+2n) \text{Hypergeometric2F1}\left[\frac{1}{2} + n, \frac{1}{4}(5+2n), \frac{1}{4}(9+2n), -e^{2i(c+dx)}\right] \right) \right) / \\
 & \quad \left. (d(1+2n)(5+2n)) \right) \sec[c+dx]^{-2-n} (b \sec[c+dx])^n (A + C \sec[c+dx]^2)
 \end{aligned}$$

**Problem 39: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(b \sec[c+dx])^n (A + C \sec[c+dx]^2)}{\sec[c+dx]^{5/2}} dx$$

Optimal (type 5, 142 leaves, 4 steps):

$$\begin{aligned}
 & - \frac{2C(b \sec[c+dx])^n \sin[c+dx]}{d(3-2n)\sec[c+dx]^{3/2}} \\
 & \left( 2(A(3-2n) + C(5-2n)) \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{4}(7-2n), \frac{1}{4}(11-2n), \cos[c+dx]^2\right] \right. \\
 & \quad \left. (b \sec[c+dx])^n \sin[c+dx] \right) / \left( d(3-2n)(7-2n)\sec[c+dx]^{7/2} \sqrt{\sin[c+dx]^2} \right)
 \end{aligned}$$

Result (type 5, 338 leaves):

$$\begin{aligned}
 & - \frac{1}{d(A + 2C + A \cos[2c + 2dx])} \frac{1}{2^{-1/2+n}} e^{-\frac{1}{2}i(4c+d(-1+2n)x)} \left( \frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}} \right)^{-\frac{1}{2}+n} (1 + e^{2i(c+dx)})^{-\frac{1}{2}+n} \\
 & \quad \left( \frac{1}{-5+2n} A e^{\frac{1}{2}id(-5+2n)x} \text{Hypergeometric2F1}\left[-\frac{1}{2} + n, \frac{1}{4}(-5+2n), \frac{1}{4}(-1+2n), -e^{2i(c+dx)}\right] + \right. \\
 & \quad \frac{1}{-3+4n+4n^2} e^{\frac{1}{2}i(4c+d(-1+2n)x)} \\
 & \quad \left. \left( 2(A+2C)(3+2n) \text{Hypergeometric2F1}\left[-\frac{1}{2} + n, \frac{1}{4}(-1+2n), \frac{1}{4}(3+2n), -e^{2i(c+dx)}\right] + \right. \right. \\
 & \quad \left. \left. A e^{2i(c+dx)}(-1+2n) \text{Hypergeometric2F1}\left[-\frac{1}{2} + n, \frac{1}{4}(3+2n), \frac{1}{4}(7+2n), -e^{2i(c+dx)}\right] \right) \right) \\
 & \quad \sec[c+dx]^{-2-n} (b \sec[c+dx])^n (A + C \sec[c+dx]^2)
 \end{aligned}$$

**Problem 41: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \text{Sec}[c + d x]^2 (b \text{Sec}[c + d x])^{2/3} (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) dx$$

Optimal (type 5, 154 leaves, 7 steps):

$$\begin{aligned} & \left( 3 (11 A + 8 C) \text{Hypergeometric2F1}\left[-\frac{5}{6}, \frac{1}{2}, \frac{1}{6}, \text{Cos}[c + d x]^2\right] (b \text{Sec}[c + d x])^{5/3} \text{Sin}[c + d x] \right) / \\ & \left( 55 b d \sqrt{\text{Sin}[c + d x]^2} \right) + \\ & \left( 3 B \text{Hypergeometric2F1}\left[-\frac{4}{3}, \frac{1}{2}, -\frac{1}{3}, \text{Cos}[c + d x]^2\right] (b \text{Sec}[c + d x])^{8/3} \text{Sin}[c + d x] \right) / \\ & \left( 8 b^2 d \sqrt{\text{Sin}[c + d x]^2} \right) + \frac{3 C (b \text{Sec}[c + d x])^{8/3} \text{Tan}[c + d x]}{11 b^2 d} \end{aligned}$$

Result (type 5, 461 leaves):

$$\begin{aligned} & - \left( \left( 3 i e^{-i (c+d x)} \left( \frac{e^{i (c+d x)}}{1 + e^{2 i (c+d x)}} \right)^{2/3} \left( 275 B (1 + e^{2 i (c+d x)}) + 275 B (-1 + e^{2 i c}) (1 + e^{2 i (c+d x)})^{2/3} \right. \right. \right. \\ & \quad \text{Hypergeometric2F1}\left[-\frac{1}{6}, \frac{2}{3}, \frac{5}{6}, -e^{2 i (c+d x)}\right] + 16 (11 A + 8 C) e^{i (c+d x)} \\ & \quad \left. \left. (-1 + e^{2 i c}) (1 + e^{2 i (c+d x)})^{2/3} \text{Hypergeometric2F1}\left[\frac{1}{3}, \frac{2}{3}, \frac{4}{3}, -e^{2 i (c+d x)}\right] \right) \right) \\ & \quad \left. (b \text{Sec}[c + d x])^{2/3} (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) \right) / \\ & \left( 220 \times 2^{1/3} d (-1 + e^{2 i c}) (A + 2 C + 2 B \text{Cos}[c + d x] + A \text{Cos}[2 c + 2 d x]) \text{Sec}[c + d x]^{8/3} \right) + \\ & \left( \text{Cos}[c + d x]^2 (b \text{Sec}[c + d x])^{2/3} (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) \right. \\ & \quad \left( \frac{15 B \text{Cos}[d x] \text{Csc}[c]}{8 d} + \frac{6 C \text{Sec}[c] \text{Sec}[c + d x]^3 \text{Sin}[d x]}{11 d} + \right. \\ & \quad \left. \frac{3 \text{Sec}[c] \text{Sec}[c + d x]^2 (8 C \text{Sin}[c] + 11 B \text{Sin}[d x])}{44 d} + \frac{1}{220 d} \right. \\ & \quad \left. \left. 3 \text{Sec}[c] \text{Sec}[c + d x] (55 B \text{Sin}[c] + 88 A \text{Sin}[d x] + 64 C \text{Sin}[d x]) + \frac{6 (11 A + 8 C) \text{Tan}[c]}{55 d} \right) \right) / \\ & (A + 2 C + 2 B \text{Cos}[c + d x] + A \text{Cos}[2 c + 2 d x]) \end{aligned}$$

**Problem 42: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \text{Sec}[c + d x] (b \text{Sec}[c + d x])^{2/3} (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) dx$$

Optimal (type 5, 151 leaves, 7 steps):



$$\begin{aligned} & \left( 3 (8A + 5C) \operatorname{Hypergeometric2F1} \left[ -\frac{1}{3}, \frac{1}{2}, \frac{2}{3}, \cos [c + dx]^2 \right] (b \operatorname{Sec} [c + dx])^{2/3} \sin [c + dx] \right) / \\ & \left( 16 d \sqrt{\sin [c + dx]^2} \right) + \\ & \left( 3 B \operatorname{Hypergeometric2F1} \left[ -\frac{5}{6}, \frac{1}{2}, \frac{1}{6}, \cos [c + dx]^2 \right] (b \operatorname{Sec} [c + dx])^{5/3} \sin [c + dx] \right) / \\ & \left( 5 b d \sqrt{\sin [c + dx]^2} \right) + \frac{3 C (b \operatorname{Sec} [c + dx])^{5/3} \tan [c + dx]}{8 b d} \end{aligned}$$

Result (type 5, 689 leaves):

$$\begin{aligned} & \frac{1}{b} \left( - \left( \left( 3 A e^{-i (2c+dx)} \left( \frac{e^{i (c+dx)}}{1 + e^{2i (c+dx)}} \right)^{2/3} \operatorname{Csc} [c] \left( 1 + e^{2i (c+dx)} + \right. \right. \right. \right. \\ & \quad \left. \left. \left. (-1 + e^{2i c}) (1 + e^{2i (c+dx)})^{2/3} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{6}, \frac{2}{3}, \frac{5}{6}, -e^{2i (c+dx)} \right] \right) \right) \right. \\ & \quad \left. \left. (b \operatorname{Sec} [c + dx])^{5/3} (A + B \operatorname{Sec} [c + dx] + C \operatorname{Sec} [c + dx]^2) \right) \right) / \\ & \left( 2^{1/3} d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \operatorname{Sec} [c + dx]^{11/3} \right) - \\ & \left( 15 C e^{-i (2c+dx)} \left( \frac{e^{i (c+dx)}}{1 + e^{2i (c+dx)}} \right)^{2/3} \operatorname{Csc} [c] \right. \\ & \quad \left. \left( 1 + e^{2i (c+dx)} + (-1 + e^{2i c}) (1 + e^{2i (c+dx)})^{2/3} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{6}, \frac{2}{3}, \frac{5}{6}, -e^{2i (c+dx)} \right] \right) \right) / \\ & \quad \left. (b \operatorname{Sec} [c + dx])^{5/3} (A + B \operatorname{Sec} [c + dx] + C \operatorname{Sec} [c + dx]^2) \right) / \\ & \left( 8 \times 2^{1/3} d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \operatorname{Sec} [c + dx]^{11/3} \right) - \\ & \left( 6 i 2^{2/3} B \left( \frac{e^{i (c+dx)}}{1 + e^{2i (c+dx)}} \right)^{2/3} (1 + e^{2i (c+dx)})^{2/3} \operatorname{Hypergeometric2F1} \left[ \frac{1}{3}, \frac{2}{3}, \frac{4}{3}, -e^{2i (c+dx)} \right] \right. \\ & \quad \left. (b \operatorname{Sec} [c + dx])^{5/3} (A + B \operatorname{Sec} [c + dx] + C \operatorname{Sec} [c + dx]^2) \right) / \\ & \left( 5 d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \operatorname{Sec} [c + dx]^{11/3} \right) + \\ & \left( \cos [c + dx]^3 (b \operatorname{Sec} [c + dx])^{5/3} (A + B \operatorname{Sec} [c + dx] + C \operatorname{Sec} [c + dx]^2) \right. \\ & \quad \left( \frac{3 (8A + 5C) \cos [dx] \operatorname{Csc} [c]}{8 d} + \frac{3 C \operatorname{Sec} [c] \operatorname{Sec} [c + dx]^2 \sin [dx]}{4 d} + \right. \\ & \quad \left. \frac{3 \operatorname{Sec} [c] \operatorname{Sec} [c + dx] (5 C \sin [c] + 8 B \sin [dx])}{20 d} + \frac{6 B \tan [c]}{5 d} \right) \left. \right) / \\ & \left( A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx] \right) \end{aligned}$$

**Problem 43: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int (b \operatorname{Sec}[c + d x])^{2/3} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 5, 146 leaves, 6 steps):

$$\begin{aligned} & - \left( \left( 3 b (5 A + 2 C) \operatorname{Hypergeometric2F1} \left[ \frac{1}{6}, \frac{1}{2}, \frac{7}{6}, \operatorname{Cos}[c + d x]^2 \right] \operatorname{Sin}[c + d x] \right) / \right. \\ & \quad \left. \left( 5 d (b \operatorname{Sec}[c + d x])^{1/3} \sqrt{\operatorname{Sin}[c + d x]^2} \right) \right) + \\ & \left( 3 B \operatorname{Hypergeometric2F1} \left[ -\frac{1}{3}, \frac{1}{2}, \frac{2}{3}, \operatorname{Cos}[c + d x]^2 \right] (b \operatorname{Sec}[c + d x])^{2/3} \operatorname{Sin}[c + d x] \right) / \\ & \left( 2 d \sqrt{\operatorname{Sin}[c + d x]^2} \right) + \frac{3 C (b \operatorname{Sec}[c + d x])^{2/3} \operatorname{Tan}[c + d x]}{5 d} \end{aligned}$$

Result (type 5, 311 leaves):

$$\begin{aligned} & \left( (b \operatorname{Sec}[c + d x])^{2/3} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\ & \quad \left( - \left( \left( 3 i 2^{2/3} e^{-i(c+d x)} \left( \frac{e^{i(c+d x)}}{1 + e^{2i(c+d x)}} \right)^{2/3} \left( 5 B (1 + e^{2i(c+d x)}) + \right. \right. \right. \\ & \quad \quad 5 B (-1 + e^{2i c}) (1 + e^{2i(c+d x)})^{2/3} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{6}, \frac{2}{3}, \frac{5}{6}, -e^{2i(c+d x)} \right] + \right. \\ & \quad \quad \left. \left. (5 A + 2 C) e^{i(c+d x)} (-1 + e^{2i c}) (1 + e^{2i(c+d x)})^{2/3} \right. \right. \\ & \quad \quad \left. \left. \operatorname{Hypergeometric2F1} \left[ \frac{1}{3}, \frac{2}{3}, \frac{4}{3}, -e^{2i(c+d x)} \right] \right) \right) / (d (-1 + e^{2i c}) \operatorname{Sec}[c + d x]^{8/3}) \right) + \\ & \quad \left. \frac{1}{d} 3 \operatorname{Cos}[c + d x] (5 B \operatorname{Cos}[d x] \operatorname{Cos}[c + d x] \operatorname{Csc}[c] + 2 C \operatorname{Sin}[c + d x]) \right) / \\ & \quad \left. (5 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2(c + d x)])) \right) \end{aligned}$$

**Problem 47: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c + d x]^2 (b \operatorname{Sec}[c + d x])^{4/3} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 5, 154 leaves, 7 steps):

$$\begin{aligned} & \left( 3 (13 A + 10 C) \operatorname{Hypergeometric2F1}\left[-\frac{7}{6}, \frac{1}{2}, -\frac{1}{6}, \cos[c + dx]^2\right] (b \sec[c + dx])^{7/3} \sin[c + dx] \right) / \\ & \left( 91 b d \sqrt{\sin[c + dx]^2} \right) + \\ & \left( 3 B \operatorname{Hypergeometric2F1}\left[-\frac{5}{3}, \frac{1}{2}, -\frac{2}{3}, \cos[c + dx]^2\right] (b \sec[c + dx])^{10/3} \sin[c + dx] \right) / \\ & \left( 10 b^2 d \sqrt{\sin[c + dx]^2} \right) + \frac{3 C (b \sec[c + dx])^{10/3} \tan[c + dx]}{13 b^2 d} \end{aligned}$$

Result (type 5, 759 leaves):

$$\begin{aligned} & - \left( \left( 12 \times 2^{1/3} A e^{-i(2c+dx)} \left( \frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}} \right)^{1/3} \operatorname{Csc}[c] \right. \right. \\ & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) (1 + e^{2i(c+dx)})^{1/3} \operatorname{Hypergeometric2F1}\left[-\frac{1}{3}, \frac{1}{3}, \frac{2}{3}, -e^{2i(c+dx)}\right] \right) \right. \\ & \quad \left. (b \sec[c + dx])^{4/3} (A + B \sec[c + dx] + C \sec[c + dx]^2) \right) / \\ & \quad \left( 7 d (A + 2 C + 2 B \cos[c + dx] + A \cos[2c + 2dx]) \sec[c + dx]^{10/3} \right) - \\ & \left( 120 \times 2^{1/3} C e^{-i(2c+dx)} \left( \frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}} \right)^{1/3} \operatorname{Csc}[c] \right. \\ & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) (1 + e^{2i(c+dx)})^{1/3} \operatorname{Hypergeometric2F1}\left[-\frac{1}{3}, \frac{1}{3}, \frac{2}{3}, -e^{2i(c+dx)}\right] \right) \right. \\ & \quad \left. (b \sec[c + dx])^{4/3} (A + B \sec[c + dx] + C \sec[c + dx]^2) \right) / \\ & \quad \left( 91 d (A + 2 C + 2 B \cos[c + dx] + A \cos[2c + 2dx]) \sec[c + dx]^{10/3} \right) - \\ & \left( 21 i B \left( \frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}} \right)^{1/3} (1 + e^{2i(c+dx)})^{1/3} \operatorname{Hypergeometric2F1}\left[\frac{1}{6}, \frac{1}{3}, \frac{7}{6}, -e^{2i(c+dx)}\right] \right. \\ & \quad \left. (b \sec[c + dx])^{4/3} (A + B \sec[c + dx] + C \sec[c + dx]^2) \right) / \\ & \quad \left( 10 \times 2^{2/3} d (A + 2 C + 2 B \cos[c + dx] + A \cos[2c + 2dx]) \sec[c + dx]^{10/3} \right) + \\ & \quad \left( \cos[c + dx]^3 (b \sec[c + dx])^{4/3} (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\ & \quad \left( \frac{24 (13 A + 10 C) \cos[dx] \operatorname{Csc}[c]}{91 d} + \frac{6 C \sec[c] \sec[c + dx]^4 \sin[dx]}{13 d} + \right. \\ & \quad \frac{3 \sec[c] \sec[c + dx]^3 (10 C \sin[c] + 13 B \sin[dx])}{65 d} + \frac{1}{1820 d} \\ & \quad \left. 3 \sec[c] \sec[c + dx] (520 A \sin[c] + 400 C \sin[c] + 637 B \sin[dx]) + \frac{1}{455 d} \right. \\ & \quad \left. \left. 3 \sec[c] \sec[c + dx]^2 (91 B \sin[c] + 130 A \sin[dx] + 100 C \sin[dx]) + \frac{21 B \tan[c]}{20 d} \right) \right) / \\ & \quad (A + 2 C + 2 B \cos[c + dx] + A \cos[2c + 2dx]) \end{aligned}$$

**Problem 48: Result unnecessarily involves complex numbers and more than**

twice size of optimal antiderivative.

$$\int \text{Sec}[c+dx] (b \text{Sec}[c+dx])^{4/3} (A+B \text{Sec}[c+dx] + C \text{Sec}[c+dx]^2) dx$$

Optimal (type 5, 151 leaves, 7 steps):

$$\left( 3 (10A+7C) \text{Hypergeometric2F1}\left[-\frac{2}{3}, \frac{1}{2}, \frac{1}{3}, \text{Cos}[c+dx]^2\right] (b \text{Sec}[c+dx])^{4/3} \text{Sin}[c+dx] \right) / \\ \left( 40d \sqrt{\text{Sin}[c+dx]^2} \right) + \\ \left( 3B \text{Hypergeometric2F1}\left[-\frac{7}{6}, \frac{1}{2}, -\frac{1}{6}, \text{Cos}[c+dx]^2\right] (b \text{Sec}[c+dx])^{7/3} \text{Sin}[c+dx] \right) / \\ \left( 7bd \sqrt{\text{Sin}[c+dx]^2} \right) + \frac{3C (b \text{Sec}[c+dx])^{7/3} \text{Tan}[c+dx]}{10bd}$$

Result (type 5, 465 leaves):

$$\frac{1}{b} \left( - \left( \left( 3i e^{-i(c+dx)} \left( \frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}} \right)^{1/3} \left( 160B (1+e^{2i(c+dx)}) + 160B (-1+e^{2ic}) (1+e^{2i(c+dx)})^{1/3} \right. \right. \right. \right. \\ \left. \left. \left. \text{Hypergeometric2F1}\left[-\frac{1}{3}, \frac{1}{3}, \frac{2}{3}, -e^{2i(c+dx)}\right] + 7(10A+7C) e^{i(c+dx)} \right. \right. \right. \\ \left. \left. \left. (-1+e^{2ic}) (1+e^{2i(c+dx)})^{1/3} \text{Hypergeometric2F1}\left[\frac{1}{6}, \frac{1}{3}, \frac{7}{6}, -e^{2i(c+dx)}\right] \right) \right) \right) \\ \left( b \text{Sec}[c+dx] \right)^{7/3} (A+B \text{Sec}[c+dx] + C \text{Sec}[c+dx]^2) \Bigg) / \\ \left( 70 \times 2^{2/3} d (-1+e^{2ic}) (A+2C+2B \text{Cos}[c+dx] + A \text{Cos}[2c+2dx]) \text{Sec}[c+dx]^{13/3} \right) + \\ \left( \text{Cos}[c+dx]^4 (b \text{Sec}[c+dx])^{7/3} (A+B \text{Sec}[c+dx] + C \text{Sec}[c+dx]^2) \right. \\ \left( \frac{24B \text{Cos}[dx] \text{Csc}[c]}{7d} + \frac{3C \text{Sec}[c] \text{Sec}[c+dx]^3 \text{Sin}[dx]}{5d} + \right. \\ \left. \frac{3 \text{Sec}[c] \text{Sec}[c+dx]^2 (7C \text{Sin}[c] + 10B \text{Sin}[dx])}{35d} + \frac{1}{140d} 3 \text{Sec}[c] \text{Sec}[c+dx] \right. \\ \left. \left. (40B \text{Sin}[c] + 70A \text{Sin}[dx] + 49C \text{Sin}[dx]) + \frac{3(10A+7C) \text{Tan}[c]}{20d} \right) \right) / \\ (A+2C+2B \text{Cos}[c+dx] + A \text{Cos}[2c+2dx]) \Bigg)$$

Problem 49: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int (b \text{Sec}[c+dx])^{4/3} (A+B \text{Sec}[c+dx] + C \text{Sec}[c+dx]^2) dx$$

Optimal (type 5, 146 leaves, 6 steps):

$$\begin{aligned} & \left( 3 b (7 A + 4 C) \operatorname{Hypergeometric2F1}\left[-\frac{1}{6}, \frac{1}{2}, \frac{5}{6}, \cos [c+d x]^2\right] (b \operatorname{Sec}[c+d x])^{1/3} \sin [c+d x]\right) / \\ & \left( 7 d \sqrt{\sin [c+d x]^2}\right) + \\ & \left( 3 B \operatorname{Hypergeometric2F1}\left[-\frac{2}{3}, \frac{1}{2}, \frac{1}{3}, \cos [c+d x]^2\right] (b \operatorname{Sec}[c+d x])^{4/3} \sin [c+d x]\right) / \\ & \left( 4 d \sqrt{\sin [c+d x]^2}\right) + \frac{3 C (b \operatorname{Sec}[c+d x])^{4/3} \tan [c+d x]}{7 d} \end{aligned}$$

Result (type 5, 683 leaves):

$$\begin{aligned} & - \left( \left( 3 \times 2^{1/3} A e^{-i(2 c+d x)} \left( \frac{e^{i(c+d x)}}{1+e^{2 i(c+d x)}} \right)^{1/3} \operatorname{Csc}[c] \right. \right. \\ & \quad \left. \left( 1+e^{2 i(c+d x)} + (-1+e^{2 i c}) (1+e^{2 i(c+d x)})^{1/3} \operatorname{Hypergeometric2F1}\left[-\frac{1}{3}, \frac{1}{3}, \frac{2}{3}, -e^{2 i(c+d x)}\right] \right) \right. \\ & \quad \left. (b \operatorname{Sec}[c+d x])^{4/3} (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \right) / \\ & \quad \left. (d(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \operatorname{Sec}[c+d x]^{10/3}) \right) - \\ & \left( 12 \times 2^{1/3} C e^{-i(2 c+d x)} \left( \frac{e^{i(c+d x)}}{1+e^{2 i(c+d x)}} \right)^{1/3} \operatorname{Csc}[c] \right. \\ & \quad \left. \left( 1+e^{2 i(c+d x)} + (-1+e^{2 i c}) (1+e^{2 i(c+d x)})^{1/3} \operatorname{Hypergeometric2F1}\left[-\frac{1}{3}, \frac{1}{3}, \frac{2}{3}, -e^{2 i(c+d x)}\right] \right) \right. \\ & \quad \left. (b \operatorname{Sec}[c+d x])^{4/3} (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \right) / \\ & \quad \left. (7 d(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \operatorname{Sec}[c+d x]^{10/3}) - \right. \\ & \left. \left( 3 i B \left( \frac{e^{i(c+d x)}}{1+e^{2 i(c+d x)}} \right)^{1/3} (1+e^{2 i(c+d x)})^{1/3} \operatorname{Hypergeometric2F1}\left[\frac{1}{6}, \frac{1}{3}, \frac{7}{6}, -e^{2 i(c+d x)}\right] \right. \right. \\ & \quad \left. \left. (b \operatorname{Sec}[c+d x])^{4/3} (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \right) / \right. \\ & \quad \left. (2^{2/3} d(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \operatorname{Sec}[c+d x]^{10/3}) + \right. \\ & \quad \left. \left( \cos [c+d x]^3 (b \operatorname{Sec}[c+d x])^{4/3} (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \right. \right. \\ & \quad \left. \left( \frac{6(7 A+4 C) \cos [d x] \operatorname{Csc}[c]}{7 d} + \frac{6 C \operatorname{Sec}[c] \operatorname{Sec}[c+d x]^2 \sin [d x]}{7 d} + \right. \right. \\ & \quad \left. \left. \frac{3 \operatorname{Sec}[c] \operatorname{Sec}[c+d x] (4 C \sin [c]+7 B \sin [d x])}{14 d} + \frac{3 B \tan [c]}{2 d} \right) \right) / \\ & \quad \left. (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right) \end{aligned}$$

**Problem 50: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \cos [c+d x] (b \operatorname{Sec}[c+d x])^{4/3} (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) dx$$

Optimal (type 5, 146 leaves, 7 steps):

$$\begin{aligned}
 & - \left( \left( 3 b^2 (4 A + C) \operatorname{Hypergeometric2F1} \left[ \frac{1}{3}, \frac{1}{2}, \frac{4}{3}, \cos [c + d x]^2 \right] \sin [c + d x] \right) / \right. \\
 & \quad \left. \left( 8 d (b \operatorname{Sec}[c + d x])^{2/3} \sqrt{\sin [c + d x]^2} \right) \right) + \frac{1}{d \sqrt{\sin [c + d x]^2}} \\
 & 3 b B \operatorname{Hypergeometric2F1} \left[ -\frac{1}{6}, \frac{1}{2}, \frac{5}{6}, \cos [c + d x]^2 \right] (b \operatorname{Sec}[c + d x])^{1/3} \sin [c + d x] + \\
 & \frac{3 b C (b \operatorname{Sec}[c + d x])^{1/3} \tan [c + d x]}{4 d}
 \end{aligned}$$

Result (type 5, 303 leaves):

$$\begin{aligned}
 & \frac{1}{2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 (c + d x)]) \operatorname{Sec}[c + d x]^{7/3}} \\
 & 3 b (b \operatorname{Sec}[c + d x])^{1/3} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\
 & \left( -\frac{1}{-1 + e^{2 i c}} i 2^{1/3} e^{-i (c + d x)} \left( \frac{e^{i (c + d x)}}{1 + e^{2 i (c + d x)}} \right)^{1/3} \left( 4 B (1 + e^{2 i (c + d x)}) + \right. \right. \\
 & \quad 4 B (-1 + e^{2 i c}) (1 + e^{2 i (c + d x)})^{1/3} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{3}, \frac{1}{3}, \frac{2}{3}, -e^{2 i (c + d x)} \right] + (4 A + C) \\
 & \quad \left. e^{i (c + d x)} (-1 + e^{2 i c}) (1 + e^{2 i (c + d x)})^{1/3} \operatorname{Hypergeometric2F1} \left[ \frac{1}{6}, \frac{1}{3}, \frac{7}{6}, -e^{2 i (c + d x)} \right] \right) + \\
 & \operatorname{Sec}[c + d x]^{1/3} (4 B \cos [d x] \operatorname{Csc}[c] + C \tan [c + d x]) \Big)
 \end{aligned}$$

**Problem 53: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\operatorname{Sec}[c + d x]^2 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{(b \operatorname{Sec}[c + d x])^{2/3}} dx$$

Optimal (type 5, 154 leaves, 7 steps):

$$\begin{aligned}
 & \left( 3 (7 A + 4 C) \operatorname{Hypergeometric2F1} \left[ -\frac{1}{6}, \frac{1}{2}, \frac{5}{6}, \cos [c + d x]^2 \right] (b \operatorname{Sec}[c + d x])^{1/3} \sin [c + d x] \right) / \\
 & \quad \left( 7 b d \sqrt{\sin [c + d x]^2} \right) + \\
 & \left( 3 B \operatorname{Hypergeometric2F1} \left[ -\frac{2}{3}, \frac{1}{2}, \frac{1}{3}, \cos [c + d x]^2 \right] (b \operatorname{Sec}[c + d x])^{4/3} \sin [c + d x] \right) / \\
 & \quad \left( 4 b^2 d \sqrt{\sin [c + d x]^2} \right) + \frac{3 C (b \operatorname{Sec}[c + d x])^{4/3} \tan [c + d x]}{7 b^2 d}
 \end{aligned}$$

Result (type 5, 299 leaves):

$$\begin{aligned}
 & - \left( \left( 3 b e^{-i(2c+dx)} (-1 + e^{2ic}) \operatorname{Csc}[c] \right. \right. \\
 & \quad \left( -28 A - 16 C - 7 B e^{i(c+dx)} - 56 A e^{2i(c+dx)} - 40 C e^{2i(c+dx)} - 28 A e^{4i(c+dx)} - 8 C e^{4i(c+dx)} + \right. \\
 & \quad \left. 7 B e^{5i(c+dx)} + 4(7 A + 4 C) (1 + e^{2i(c+dx)})^{7/3} \operatorname{Hypergeometric2F1}\left[-\frac{1}{3}, \frac{1}{3}, \frac{2}{3}, -e^{2i(c+dx)}\right] + \right. \\
 & \quad \left. 7 B e^{i(c+dx)} (1 + e^{2i(c+dx)})^{7/3} \operatorname{Hypergeometric2F1}\left[\frac{1}{6}, \frac{1}{3}, \frac{7}{6}, -e^{2i(c+dx)}\right] \right) \\
 & \quad \left. (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right) / \\
 & \left( 28 d (1 + e^{2i(c+dx)})^2 (A + 2 C + 2 B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2(c + dx)]) (b \operatorname{Sec}[c + dx])^{5/3} \right)
 \end{aligned}$$

**Problem 54: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c + dx] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2)}{(b \operatorname{Sec}[c + dx])^{2/3}} dx$$

Optimal (type 5, 147 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{3(4A + C) \operatorname{Hypergeometric2F1}\left[\frac{1}{3}, \frac{1}{2}, \frac{4}{3}, \operatorname{Cos}[c + dx]^2\right] \operatorname{Sin}[c + dx]}{8 d (b \operatorname{Sec}[c + dx])^{2/3} \sqrt{\operatorname{Sin}[c + dx]^2}} + \\
 & \left( 3 B \operatorname{Hypergeometric2F1}\left[-\frac{1}{6}, \frac{1}{2}, \frac{5}{6}, \operatorname{Cos}[c + dx]^2\right] (b \operatorname{Sec}[c + dx])^{1/3} \operatorname{Sin}[c + dx] \right) / \\
 & \left( b d \sqrt{\operatorname{Sin}[c + dx]^2} \right) + \frac{3 C (b \operatorname{Sec}[c + dx])^{1/3} \operatorname{Tan}[c + dx]}{4 b d}
 \end{aligned}$$

Result (type 5, 305 leaves):

$$\begin{aligned}
 & \frac{1}{2 b d (A + 2 C + 2 B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2(c + dx)]) \operatorname{Sec}[c + dx]^{7/3}} \\
 & 3 (b \operatorname{Sec}[c + dx])^{1/3} (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \\
 & \left( -\frac{1}{-1 + e^{2ic}} i^{2/3} e^{-i(c+dx)} \left( \frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}} \right)^{1/3} \left( 4 B (1 + e^{2i(c+dx)}) + \right. \right. \\
 & \quad \left. 4 B (-1 + e^{2ic}) (1 + e^{2i(c+dx)})^{1/3} \operatorname{Hypergeometric2F1}\left[-\frac{1}{3}, \frac{1}{3}, \frac{2}{3}, -e^{2i(c+dx)}\right] + (4 A + C) \right. \\
 & \quad \left. e^{i(c+dx)} (-1 + e^{2ic}) (1 + e^{2i(c+dx)})^{1/3} \operatorname{Hypergeometric2F1}\left[\frac{1}{6}, \frac{1}{3}, \frac{7}{6}, -e^{2i(c+dx)}\right] \right) + \\
 & \quad \left. \operatorname{Sec}[c + dx]^{1/3} (4 B \operatorname{Cos}[dx] \operatorname{Csc}[c] + C \operatorname{Tan}[c + dx]) \right)
 \end{aligned}$$

**Problem 55: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2}{(b \operatorname{Sec}[c + dx])^{2/3}} dx$$

Optimal (type 5, 142 leaves, 6 steps):

$$-\left( \left( 3 b (A - 2 C) \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{5}{6}, \frac{11}{6}, \cos [c + d x]^2 \right] \sin [c + d x] \right) / \left( 5 d (b \operatorname{Sec} [c + d x])^{5/3} \sqrt{\sin [c + d x]^2} \right) \right) - \frac{3 B \operatorname{Hypergeometric2F1} \left[ \frac{1}{3}, \frac{1}{2}, \frac{4}{3}, \cos [c + d x]^2 \right] \sin [c + d x]}{2 d (b \operatorname{Sec} [c + d x])^{2/3} \sqrt{\sin [c + d x]^2}} + \frac{3 C \tan [c + d x]}{d (b \operatorname{Sec} [c + d x])^{2/3}}$$

Result (type 5, 154 leaves):

$$-\frac{1}{4 b d} 3 i e^{-i (c + d x)} \left( A - 4 C + A e^{2 i (c + d x)} - 2 (A - 2 C) (1 + e^{2 i (c + d x)})^{1/3} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{3}, \frac{1}{3}, \frac{2}{3}, -e^{2 i (c + d x)} \right] + 4 B e^{i (c + d x)} (1 + e^{2 i (c + d x)})^{1/3} \operatorname{Hypergeometric2F1} \left[ \frac{1}{6}, \frac{1}{3}, \frac{7}{6}, -e^{2 i (c + d x)} \right] \right) (b \operatorname{Sec} [c + d x])^{1/3}$$

**Problem 56: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec} [c + d x] (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2)}{(b \operatorname{Sec} [c + d x])^{2/3}} dx$$

Optimal (type 5, 147 leaves, 7 steps):

$$-\frac{3 (4 A + C) \operatorname{Hypergeometric2F1} \left[ \frac{1}{3}, \frac{1}{2}, \frac{4}{3}, \cos [c + d x]^2 \right] \sin [c + d x]}{8 d (b \operatorname{Sec} [c + d x])^{2/3} \sqrt{\sin [c + d x]^2}} + \left( 3 B \operatorname{Hypergeometric2F1} \left[ -\frac{1}{6}, \frac{1}{2}, \frac{5}{6}, \cos [c + d x]^2 \right] (b \operatorname{Sec} [c + d x])^{1/3} \sin [c + d x] \right) / \left( b d \sqrt{\sin [c + d x]^2} \right) + \frac{3 C (b \operatorname{Sec} [c + d x])^{1/3} \tan [c + d x]}{4 b d}$$

Result (type 5, 305 leaves):

$$\frac{1}{2 b d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 (c + d x)]) \operatorname{Sec} [c + d x]^{7/3}} \left( 3 (b \operatorname{Sec} [c + d x])^{1/3} (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) \left( -\frac{1}{-1 + e^{2 i c}} i 2^{1/3} e^{-i (c + d x)} \left( \frac{e^{i (c + d x)}}{1 + e^{2 i (c + d x)}} \right)^{1/3} (4 B (1 + e^{2 i (c + d x)}) + 4 B (-1 + e^{2 i c}) (1 + e^{2 i (c + d x)})^{1/3} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{3}, \frac{1}{3}, \frac{2}{3}, -e^{2 i (c + d x)} \right] + (4 A + C) e^{i (c + d x)} (-1 + e^{2 i c}) (1 + e^{2 i (c + d x)})^{1/3} \operatorname{Hypergeometric2F1} \left[ \frac{1}{6}, \frac{1}{3}, \frac{7}{6}, -e^{2 i (c + d x)} \right] \right) + \operatorname{Sec} [c + d x]^{1/3} (4 B \cos [d x] \operatorname{Csc} [c] + C \tan [c + d x]) \right)$$



**Problem 57: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\text{Sec}[c + dx]^2 (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2)}{(b \text{Sec}[c + dx])^{2/3}} dx$$

Optimal (type 5, 154 leaves, 7 steps):

$$\begin{aligned} & \left( 3 (7A + 4C) \text{Hypergeometric2F1}\left[-\frac{1}{6}, \frac{1}{2}, \frac{5}{6}, \text{Cos}[c + dx]^2\right] (b \text{Sec}[c + dx])^{1/3} \text{Sin}[c + dx] \right) / \\ & \left( 7bd \sqrt{\text{Sin}[c + dx]^2} \right) + \\ & \left( 3B \text{Hypergeometric2F1}\left[-\frac{2}{3}, \frac{1}{2}, \frac{1}{3}, \text{Cos}[c + dx]^2\right] (b \text{Sec}[c + dx])^{4/3} \text{Sin}[c + dx] \right) / \\ & \left( 4b^2 d \sqrt{\text{Sin}[c + dx]^2} \right) + \frac{3C (b \text{Sec}[c + dx])^{4/3} \text{Tan}[c + dx]}{7b^2 d} \end{aligned}$$

Result (type 5, 299 leaves):

$$\begin{aligned} & - \left( \left( 3b e^{-i(2c+dx)} (-1 + e^{2ic}) \text{Csc}[c] \right. \right. \\ & \quad \left( -28A - 16C - 7B e^{i(c+dx)} - 56A e^{2i(c+dx)} - 40C e^{2i(c+dx)} - 28A e^{4i(c+dx)} - 8C e^{4i(c+dx)} + \right. \\ & \quad \left. 7B e^{5i(c+dx)} + 4(7A + 4C) (1 + e^{2i(c+dx)})^{7/3} \text{Hypergeometric2F1}\left[-\frac{1}{3}, \frac{1}{3}, \frac{2}{3}, -e^{2i(c+dx)}\right] + \right. \\ & \quad \left. \left. 7B e^{i(c+dx)} (1 + e^{2i(c+dx)})^{7/3} \text{Hypergeometric2F1}\left[\frac{1}{6}, \frac{1}{3}, \frac{7}{6}, -e^{2i(c+dx)}\right] \right) \right) / \\ & \left( 28d (1 + e^{2i(c+dx)})^2 (A + 2C + 2B \text{Cos}[c + dx] + A \text{Cos}[2(c + dx)]) (b \text{Sec}[c + dx])^{5/3} \right) \end{aligned}$$

**Problem 58: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\text{Sec}[c + dx]^3 (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2)}{(b \text{Sec}[c + dx])^{2/3}} dx$$

Optimal (type 5, 154 leaves, 7 steps):

$$\begin{aligned} & \left( 3 (10A + 7C) \text{Hypergeometric2F1}\left[-\frac{2}{3}, \frac{1}{2}, \frac{1}{3}, \text{Cos}[c + dx]^2\right] (b \text{Sec}[c + dx])^{4/3} \text{Sin}[c + dx] \right) / \\ & \left( 40b^2 d \sqrt{\text{Sin}[c + dx]^2} \right) + \\ & \left( 3B \text{Hypergeometric2F1}\left[-\frac{7}{6}, \frac{1}{2}, -\frac{1}{6}, \text{Cos}[c + dx]^2\right] (b \text{Sec}[c + dx])^{7/3} \text{Sin}[c + dx] \right) / \\ & \left( 7b^3 d \sqrt{\text{Sin}[c + dx]^2} \right) + \frac{3C (b \text{Sec}[c + dx])^{7/3} \text{Tan}[c + dx]}{10b^3 d} \end{aligned}$$

Result (type 5, 333 leaves):

$$\frac{1}{140 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 (c + d x)]) (b \sec [c + d x])^{2/3} (A + B \sec [c + d x] + C \sec [c + d x]^2)}$$

$$\left( - \left( \left( 3 i 2^{1/3} e^{-i (c+d x)} \left( \frac{e^{i (c+d x)}}{1 + e^{2 i (c+d x)}} \right)^{1/3} \left( 160 B (1 + e^{2 i (c+d x)}) + 160 B (-1 + e^{2 i c}) (1 + e^{2 i (c+d x)})^{1/3} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{3}, \frac{1}{3}, \frac{2}{3}, -e^{2 i (c+d x)} \right] + 7 (10 A + 7 C) e^{i (c+d x)} (-1 + e^{2 i c}) (1 + e^{2 i (c+d x)})^{1/3} \operatorname{Hypergeometric2F1} \left[ \frac{1}{6}, \frac{1}{3}, \frac{7}{6}, -e^{2 i (c+d x)} \right] \right) \right) / \right.$$

$$\left. \left( d (-1 + e^{2 i c}) \sec [c + d x]^{4/3} \right) + \frac{1}{d} 3 (160 B \cos [d x] \cos [c + d x] \csc [c] + 7 (10 A + 7 C) \sin [c + d x] + 4 (10 B + 7 C \sec [c + d x]) \tan [c + d x]) \right)$$

**Problem 59: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\sec [c + d x]^2 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{(b \sec [c + d x])^{4/3}} dx$$

Optimal (type 5, 154 leaves, 7 steps):

$$- \left( \left( 3 (5 A + 2 C) \operatorname{Hypergeometric2F1} \left[ \frac{1}{6}, \frac{1}{2}, \frac{7}{6}, \cos [c + d x]^2 \right] \sin [c + d x] \right) / \right.$$

$$\left. \left( 5 b d (b \sec [c + d x])^{1/3} \sqrt{\sin [c + d x]^2} \right) \right) +$$

$$\left( 3 B \operatorname{Hypergeometric2F1} \left[ -\frac{1}{3}, \frac{1}{2}, \frac{2}{3}, \cos [c + d x]^2 \right] (b \sec [c + d x])^{2/3} \sin [c + d x] \right) /$$

$$\left( 2 b^2 d \sqrt{\sin [c + d x]^2} \right) + \frac{3 C (b \sec [c + d x])^{2/3} \tan [c + d x]}{5 b^2 d}$$

Result (type 5, 299 leaves):

$$\left( (A + B \sec [c + d x] + C \sec [c + d x]^2) \right.$$

$$\left( - \left( \left( 3 i 2^{2/3} e^{-i (c+d x)} \left( \frac{e^{i (c+d x)}}{1 + e^{2 i (c+d x)}} \right)^{2/3} \left( 5 B (1 + e^{2 i (c+d x)}) + 5 B (-1 + e^{2 i c}) (1 + e^{2 i (c+d x)})^{2/3} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{6}, \frac{2}{3}, \frac{5}{6}, -e^{2 i (c+d x)} \right] + (5 A + 2 C) e^{i (c+d x)} (-1 + e^{2 i c}) (1 + e^{2 i (c+d x)})^{2/3} \operatorname{Hypergeometric2F1} \left[ \frac{1}{3}, \frac{2}{3}, \frac{4}{3}, -e^{2 i (c+d x)} \right] \right) \right) / \right.$$

$$\left. \left( d (-1 + e^{2 i c}) \sec [c + d x]^{2/3} \right) + \frac{3 (5 B \cos [d x] \csc [c] + 2 C \tan [c + d x])}{d} \right) \right) /$$

$$\left( 5 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 (c + d x)]) (b \sec [c + d x])^{4/3} \right)$$

**Problem 60: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\text{Sec}[c + d x] (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2)}{(b \text{Sec}[c + d x])^{4/3}} dx$$

Optimal (type 5, 149 leaves, 7 steps):

$$\frac{3 (2 A - C) \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{2}{3}, \frac{5}{3}, \text{Cos}[c + d x]^2\right] \text{Sin}[c + d x]}{8 d (b \text{Sec}[c + d x])^{4/3} \sqrt{\text{Sin}[c + d x]^2}} + \frac{3 B \text{Hypergeometric2F1}\left[\frac{1}{6}, \frac{1}{2}, \frac{7}{6}, \text{Cos}[c + d x]^2\right] \text{Sin}[c + d x]}{b d (b \text{Sec}[c + d x])^{1/3} \sqrt{\text{Sin}[c + d x]^2}} + \frac{3 C \text{Tan}[c + d x]}{2 b d (b \text{Sec}[c + d x])^{1/3}}$$

Result (type 5, 174 leaves):

$$\frac{1}{2 b^2 d} 3 e^{-i (3 c + 2 d x)} \left( A - C + A e^{2 i (c + d x)} + (-2 A + C) (1 + e^{2 i (c + d x)})^{2/3} \text{Hypergeometric2F1}\left[-\frac{1}{6}, \frac{2}{3}, \frac{5}{6}, -e^{2 i (c + d x)}\right] + B e^{i (c + d x)} (1 + e^{2 i (c + d x)})^{2/3} \text{Hypergeometric2F1}\left[\frac{1}{3}, \frac{2}{3}, \frac{4}{3}, -e^{2 i (c + d x)}\right] \right) (b \text{Sec}[c + d x])^{2/3} (-i \text{Cos}[2 c + d x] + \text{Sin}[2 c + d x])$$

**Problem 61: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2}{(b \text{Sec}[c + d x])^{4/3}} dx$$

Optimal (type 5, 146 leaves, 6 steps):

$$\frac{3 B \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{2}{3}, \frac{5}{3}, \text{Cos}[c + d x]^2\right] \text{Sin}[c + d x]}{4 d (b \text{Sec}[c + d x])^{4/3} \sqrt{\text{Sin}[c + d x]^2}} + \frac{3 (A + 4 C) \text{Hypergeometric2F1}\left[\frac{1}{6}, \frac{1}{2}, \frac{7}{6}, \text{Cos}[c + d x]^2\right] \text{Sin}[c + d x]}{4 b d (b \text{Sec}[c + d x])^{1/3} \sqrt{\text{Sin}[c + d x]^2}} + \frac{3 A \text{Tan}[c + d x]}{4 d (b \text{Sec}[c + d x])^{4/3}}$$

Result (type 5, 143 leaves):

$$\left( 3 \left( 8 i B \text{Hypergeometric2F1}\left[-\frac{1}{6}, \frac{2}{3}, \frac{5}{6}, -e^{2 i (c + d x)}\right] - i (A + 4 C) e^{i (c + d x)} \text{Hypergeometric2F1}\left[\frac{1}{3}, \frac{2}{3}, \frac{4}{3}, -e^{2 i (c + d x)}\right] + (1 + e^{2 i (c + d x)})^{1/3} (-4 i B + A \text{Sin}[c + d x]) \right) \right) / (4 b d (1 + e^{2 i (c + d x)})^{1/3} (b \text{Sec}[c + d x])^{1/3})$$

### Problem 62: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\text{Sec}[c + d x] (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2)}{(b \text{Sec}[c + d x])^{4/3}} dx$$

Optimal (type 5, 149 leaves, 7 steps):

$$\frac{3(2A - C) \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{2}{3}, \frac{5}{3}, \text{Cos}[c + d x]^2\right] \text{Sin}[c + d x]}{8 d (b \text{Sec}[c + d x])^{4/3} \sqrt{\text{Sin}[c + d x]^2}} + \frac{3 B \text{Hypergeometric2F1}\left[\frac{1}{6}, \frac{1}{2}, \frac{7}{6}, \text{Cos}[c + d x]^2\right] \text{Sin}[c + d x]}{b d (b \text{Sec}[c + d x])^{1/3} \sqrt{\text{Sin}[c + d x]^2}} + \frac{3 C \text{Tan}[c + d x]}{2 b d (b \text{Sec}[c + d x])^{1/3}}$$

Result (type 5, 174 leaves):

$$\frac{1}{2 b^2 d} 3 e^{-i(3c+2dx)} \left( A - C + A e^{2i(c+dx)} + (-2A + C) (1 + e^{2i(c+dx)})^{2/3} \text{Hypergeometric2F1}\left[-\frac{1}{6}, \frac{2}{3}, \frac{5}{6}, -e^{2i(c+dx)}\right] + B e^{i(c+dx)} (1 + e^{2i(c+dx)})^{2/3} \text{Hypergeometric2F1}\left[\frac{1}{3}, \frac{2}{3}, \frac{4}{3}, -e^{2i(c+dx)}\right] \right) (b \text{Sec}[c + d x])^{2/3} (-i \text{Cos}[2c + d x] + \text{Sin}[2c + d x])$$

### Problem 63: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\text{Sec}[c + d x]^2 (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2)}{(b \text{Sec}[c + d x])^{4/3}} dx$$

Optimal (type 5, 154 leaves, 7 steps):

$$\frac{-\left(3(5A + 2C) \text{Hypergeometric2F1}\left[\frac{1}{6}, \frac{1}{2}, \frac{7}{6}, \text{Cos}[c + d x]^2\right] \text{Sin}[c + d x]\right)}{5 b d (b \text{Sec}[c + d x])^{1/3} \sqrt{\text{Sin}[c + d x]^2}} + \frac{3 B \text{Hypergeometric2F1}\left[-\frac{1}{3}, \frac{1}{2}, \frac{2}{3}, \text{Cos}[c + d x]^2\right] (b \text{Sec}[c + d x])^{2/3} \text{Sin}[c + d x]}{2 b^2 d \sqrt{\text{Sin}[c + d x]^2}} + \frac{3 C (b \text{Sec}[c + d x])^{2/3} \text{Tan}[c + d x]}{5 b^2 d}$$

Result (type 5, 299 leaves):

$$\begin{aligned}
 & \left( (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \left( - \left( \left( 3 i^{2/3} e^{-i(c+dx)} \left( \frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}} \right)^{2/3} \left( 5 B (1 + e^{2i(c+dx)}) + 5 B (-1 + e^{2i c}) (1 + e^{2i(c+dx)})^{2/3} \right. \right. \right. \\
 & \quad \operatorname{Hypergeometric2F1}\left[-\frac{1}{6}, \frac{2}{3}, \frac{5}{6}, -e^{2i(c+dx)}\right] + (5 A + 2 C) e^{i(c+dx)} \\
 & \quad \left. \left. (-1 + e^{2i c}) (1 + e^{2i(c+dx)})^{2/3} \operatorname{Hypergeometric2F1}\left[\frac{1}{3}, \frac{2}{3}, \frac{4}{3}, -e^{2i(c+dx)}\right] \right) \right) \Bigg/ \\
 & \left. \left( d (-1 + e^{2i c}) \operatorname{Sec}[c + d x]^{2/3} \right) + \frac{3 (5 B \operatorname{Cos}[d x] \operatorname{Csc}[c] + 2 C \operatorname{Tan}[c + d x])}{d} \right) \Bigg/ \\
 & \left( 5 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2(c + d x)]) \right) \\
 & \left. (b \operatorname{Sec}[c + d x])^{4/3} \right)
 \end{aligned}$$

**Problem 64: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c + d x]^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{(b \operatorname{Sec}[c + d x])^{4/3}} dx$$

Optimal (type 5, 154 leaves, 7 steps):

$$\begin{aligned}
 & \left( 3 (8 A + 5 C) \operatorname{Hypergeometric2F1}\left[-\frac{1}{3}, \frac{1}{2}, \frac{2}{3}, \operatorname{Cos}[c + d x]^2\right] (b \operatorname{Sec}[c + d x])^{2/3} \operatorname{Sin}[c + d x] \right) \Bigg/ \\
 & \left( 16 b^2 d \sqrt{\operatorname{Sin}[c + d x]^2} \right) + \\
 & \left( 3 B \operatorname{Hypergeometric2F1}\left[-\frac{5}{6}, \frac{1}{2}, \frac{1}{6}, \operatorname{Cos}[c + d x]^2\right] (b \operatorname{Sec}[c + d x])^{5/3} \operatorname{Sin}[c + d x] \right) \Bigg/ \\
 & \left( 5 b^3 d \sqrt{\operatorname{Sin}[c + d x]^2} \right) + \frac{3 C (b \operatorname{Sec}[c + d x])^{5/3} \operatorname{Tan}[c + d x]}{8 b^3 d}
 \end{aligned}$$

Result (type 5, 677 leaves):

$$\begin{aligned}
& - \left( \left( 3 A e^{-i (2 c+d x)} \left( \frac{e^{i (c+d x)}}{1+e^{2 i (c+d x)}} \right)^{2/3} \operatorname{Csc}[c] \right. \right. \\
& \quad \left. \left( 1+e^{2 i (c+d x)} + (-1+e^{2 i c}) (1+e^{2 i (c+d x)})^{2/3} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{6}, \frac{2}{3}, \frac{5}{6}, -e^{2 i (c+d x)} \right] \right) \right. \\
& \quad \left. \left. (A+B \operatorname{Sec}[c+d x] + C \operatorname{Sec}[c+d x]^2) \right) \right) / \\
& \quad \left( 2^{1/3} d (A+2 C+2 B \operatorname{Cos}[c+d x] + A \operatorname{Cos}[2 c+2 d x]) \operatorname{Sec}[c+d x]^{2/3} (b \operatorname{Sec}[c+d x])^{4/3} \right) - \\
& \left( 15 C e^{-i (2 c+d x)} \left( \frac{e^{i (c+d x)}}{1+e^{2 i (c+d x)}} \right)^{2/3} \operatorname{Csc}[c] \right. \\
& \quad \left. \left( 1+e^{2 i (c+d x)} + (-1+e^{2 i c}) (1+e^{2 i (c+d x)})^{2/3} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{6}, \frac{2}{3}, \frac{5}{6}, -e^{2 i (c+d x)} \right] \right) \right. \\
& \quad \left. \left. (A+B \operatorname{Sec}[c+d x] + C \operatorname{Sec}[c+d x]^2) \right) \right) / \\
& \quad \left( 8 \times 2^{1/3} d (A+2 C+2 B \operatorname{Cos}[c+d x] + A \operatorname{Cos}[2 c+2 d x]) \operatorname{Sec}[c+d x]^{2/3} (b \operatorname{Sec}[c+d x])^{4/3} \right) - \\
& \left( 6 i 2^{2/3} B \left( \frac{e^{i (c+d x)}}{1+e^{2 i (c+d x)}} \right)^{2/3} (1+e^{2 i (c+d x)})^{2/3} \right. \\
& \quad \left. \operatorname{Hypergeometric2F1} \left[ \frac{1}{3}, \frac{2}{3}, \frac{4}{3}, -e^{2 i (c+d x)} \right] (A+B \operatorname{Sec}[c+d x] + C \operatorname{Sec}[c+d x]^2) \right) / \\
& \quad \left( 5 d (A+2 C+2 B \operatorname{Cos}[c+d x] + A \operatorname{Cos}[2 c+2 d x]) \operatorname{Sec}[c+d x]^{2/3} (b \operatorname{Sec}[c+d x])^{4/3} \right) + \\
& \quad \left( (A+B \operatorname{Sec}[c+d x] + C \operatorname{Sec}[c+d x]^2) \right. \\
& \quad \left. \left( \frac{3 (8 A+5 C) \operatorname{Cos}[d x] \operatorname{Csc}[c]}{8 d} + \frac{3 C \operatorname{Sec}[c] \operatorname{Sec}[c+d x]^2 \operatorname{Sin}[d x]}{4 d} + \right. \right. \\
& \quad \left. \left. \frac{3 \operatorname{Sec}[c] \operatorname{Sec}[c+d x] (5 C \operatorname{Sin}[c] + 8 B \operatorname{Sin}[d x])}{20 d} + \frac{6 B \operatorname{Tan}[c]}{5 d} \right) \right) / \\
& \quad \left( (A+2 C+2 B \operatorname{Cos}[c+d x] + A \operatorname{Cos}[2 c+2 d x]) (b \operatorname{Sec}[c+d x])^{4/3} \right)
\end{aligned}$$

**Problem 65: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c+d x]^m (b \operatorname{Sec}[c+d x])^{4/3} (A+B \operatorname{Sec}[c+d x] + C \operatorname{Sec}[c+d x]^2) dx$$

Optimal (type 5, 230 leaves, 7 steps):

$$\frac{3 b C \operatorname{Sec}[c+d x]^{2+m} (b \operatorname{Sec}[c+d x])^{1/3} \operatorname{Sin}[c+d x]}{d(7+3 m)} +$$

$$\left( 3 b (C(4+3 m) + A(7+3 m)) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{6}(-1-3 m), \frac{1}{6}(5-3 m), \operatorname{Cos}[c+d x]^2\right] \right.$$

$$\left. \operatorname{Sec}[c+d x]^m (b \operatorname{Sec}[c+d x])^{1/3} \operatorname{Sin}[c+d x] \right) / \left( d(1+3 m)(7+3 m) \sqrt{\operatorname{Sin}[c+d x]^2} \right) +$$

$$\left( 3 b B \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{6}(-4-3 m), \frac{1}{6}(2-3 m), \operatorname{Cos}[c+d x]^2\right] \operatorname{Sec}[c+d x]^{1+m} \right.$$

$$\left. (b \operatorname{Sec}[c+d x])^{1/3} \operatorname{Sin}[c+d x] \right) / \left( d(4+3 m) \sqrt{\operatorname{Sin}[c+d x]^2} \right)$$

Result (type 5, 484 leaves):

$$\frac{1}{d(A+2C+2B \operatorname{Cos}[c+d x] + A \operatorname{Cos}[2c+2dx]) \operatorname{Sec}[c+d x]^{10/3}}$$

$$3 i 2^{7/3+m} e^{-\frac{1}{3} i d(4+3 m)x} \left( \frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}} \right)^{\frac{4}{3}+m} (1+e^{2i(c+dx)})^{\frac{4}{3}+m}$$

$$\left( \frac{1}{10+3 m} 2(A+2C) e^{\frac{1}{3} i(6c+d(10+3 m)x)} \operatorname{Hypergeometric2F1}\left[\frac{5}{3}+\frac{m}{2}, \frac{10}{3}+m, \frac{8}{3}+\frac{m}{2}, -e^{2i(c+dx)}\right] + \right.$$

$$\frac{1}{16+3 m} A e^{4i c+\frac{1}{3} i d(16+3 m)x} \operatorname{Hypergeometric2F1}\left[\frac{8}{3}+\frac{m}{2}, \frac{10}{3}+m, \frac{1}{6}(22+3 m), -e^{2i(c+dx)}\right] +$$

$$\frac{1}{4+3 m} A e^{\frac{1}{3} i d(4+3 m)x} \operatorname{Hypergeometric2F1}\left[\frac{10}{3}+m, \frac{1}{6}(4+3 m), \frac{5}{3}+\frac{m}{2}, -e^{2i(c+dx)}\right] + \frac{1}{7+3 m} 2 B$$

$$e^{\frac{1}{3} i(3c+d(7+3 m)x)} \operatorname{Hypergeometric2F1}\left[\frac{10}{3}+m, \frac{1}{6}(7+3 m), \frac{1}{6}(13+3 m), -e^{2i(c+dx)}\right] + \frac{1}{13+3 m}$$

$$\left. 2 B e^{\frac{1}{3} i(9c+d(13+3 m)x)} \operatorname{Hypergeometric2F1}\left[\frac{10}{3}+m, \frac{1}{6}(13+3 m), \frac{1}{6}(19+3 m), -e^{2i(c+dx)}\right] \right)$$

$$(b \operatorname{Sec}[c+d x])^{4/3} (A+B \operatorname{Sec}[c+d x] + C \operatorname{Sec}[c+d x]^2)$$

**Problem 66: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c+d x]^m (b \operatorname{Sec}[c+d x])^{2/3} (A+B \operatorname{Sec}[c+d x] + C \operatorname{Sec}[c+d x]^2) dx$$

Optimal (type 5, 227 leaves, 7 steps):

$$\frac{3 C \operatorname{Sec}[c+d x]^{1+m} (b \operatorname{Sec}[c+d x])^{2/3} \operatorname{Sin}[c+d x]}{d(5+3 m)}$$

$$\left( 3 (C(2+3 m) + A(5+3 m)) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{6}(1-3 m), \frac{1}{6}(7-3 m), \operatorname{Cos}[c+d x]^2\right] \right.$$

$$\left. \operatorname{Sec}[c+d x]^{-1+m} (b \operatorname{Sec}[c+d x])^{2/3} \operatorname{Sin}[c+d x] \right) / \left( d(1-3 m)(5+3 m) \sqrt{\operatorname{Sin}[c+d x]^2} \right) +$$

$$\left( 3 B \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{6}(-2-3 m), \frac{1}{6}(4-3 m), \operatorname{Cos}[c+d x]^2\right] \operatorname{Sec}[c+d x]^m \right.$$

$$\left. (b \operatorname{Sec}[c+d x])^{2/3} \operatorname{Sin}[c+d x] \right) / \left( d(2+3 m) \sqrt{\operatorname{Sin}[c+d x]^2} \right)$$

Result (type 5, 547 leaves):

$$\begin{aligned}
 & - \frac{1}{d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \sec [c + d x]^{8/3}} \\
 & 3 i 2^{5+m} e^{-\frac{1}{3} i d (2+3 m) x} \left( \frac{e^{i (c+d x)}}{1 + e^{2 i (c+d x)}} \right)^{\frac{2}{3}+m} \left( 1 + e^{2 i (c+d x)} \right)^{\frac{2}{3}+m} \\
 & \left( \frac{1}{14 + 3 m} A e^{4 i c + \frac{1}{3} i d (14+3 m) x} \text{Hypergeometric2F1} \left[ \frac{7}{3} + \frac{m}{2}, \frac{8}{3} + m, \frac{1}{6} (20 + 3 m), -e^{2 i (c+d x)} \right] + \frac{1}{2 + 3 m} \right. \\
 & A e^{\frac{1}{3} i d (2+3 m) x} \text{Hypergeometric2F1} \left[ \frac{8}{3} + m, \frac{1}{6} (2 + 3 m), \frac{1}{6} (8 + 3 m), -e^{2 i (c+d x)} \right] + \frac{1}{5 + 3 m} \\
 & 2 B e^{\frac{1}{3} i (3 c+d (5+3 m) x)} \text{Hypergeometric2F1} \left[ \frac{8}{3} + m, \frac{1}{6} (5 + 3 m), \frac{1}{6} (11 + 3 m), -e^{2 i (c+d x)} \right] + \frac{1}{8 + 3 m} \\
 & 2 A e^{\frac{1}{3} i (6 c+d (8+3 m) x)} \text{Hypergeometric2F1} \left[ \frac{8}{3} + m, \frac{1}{6} (8 + 3 m), \frac{7}{3} + \frac{m}{2}, -e^{2 i (c+d x)} \right] + \frac{1}{8 + 3 m} \\
 & 4 C e^{\frac{1}{3} i (6 c+d (8+3 m) x)} \text{Hypergeometric2F1} \left[ \frac{8}{3} + m, \frac{1}{6} (8 + 3 m), \frac{7}{3} + \frac{m}{2}, -e^{2 i (c+d x)} \right] + \frac{1}{11 + 3 m} \\
 & \left. 2 B e^{\frac{1}{3} i (9 c+d (11+3 m) x)} \text{Hypergeometric2F1} \left[ \frac{8}{3} + m, \frac{1}{6} (11 + 3 m), \frac{1}{6} (17 + 3 m), -e^{2 i (c+d x)} \right] \right) \\
 & (b \sec [c + d x])^{2/3} (A + B \sec [c + d x] + C \sec [c + d x]^2)
 \end{aligned}$$

**Problem 67: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \sec [c + d x]^m (b \sec [c + d x])^{1/3} (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 5, 225 leaves, 7 steps):

$$\begin{aligned}
 & \frac{3 C \sec [c + d x]^{1+m} (b \sec [c + d x])^{1/3} \sin [c + d x]}{d (4 + 3 m)} - \\
 & \left( 3 (C + 3 C m + A (4 + 3 m)) \text{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{1}{6} (2 - 3 m), \frac{1}{6} (8 - 3 m), \cos [c + d x]^2 \right] \right. \\
 & \left. \sec [c + d x]^{-1+m} (b \sec [c + d x])^{1/3} \sin [c + d x] \right) / \left( d (2 - 3 m) (4 + 3 m) \sqrt{\sin [c + d x]^2} \right) + \\
 & \left( 3 B \text{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{1}{6} (-1 - 3 m), \frac{1}{6} (5 - 3 m), \cos [c + d x]^2 \right] \sec [c + d x]^m \right. \\
 & \left. (b \sec [c + d x])^{1/3} \sin [c + d x] \right) / \left( d (1 + 3 m) \sqrt{\sin [c + d x]^2} \right)
 \end{aligned}$$

Result (type 5, 494 leaves):



$$\begin{aligned}
 & \frac{1}{(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sec[c + dx]^{7/3}} \\
 & 3 \int 2^{\frac{4}{3}+m} e^{-\frac{1}{3}i d (1+3m)x} \left( \frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}} \right)^{\frac{1}{3}+m} (1 + e^{2i(c+dx)})^{\frac{1}{3}+m} \\
 & \left( \frac{1}{d(10+3m)} 2B e^{\frac{1}{3}i(9c+d(10+3m)x)} \text{Hypergeometric2F1}\left[\frac{5}{3} + \frac{m}{2}, \frac{7}{3} + m, \frac{8}{3} + \frac{m}{2}, -e^{2i(c+dx)}\right] + \right. \\
 & \frac{1}{d+3dm} A e^{\frac{1}{3}i(d+3dm)x} \text{Hypergeometric2F1}\left[\frac{7}{3} + m, \frac{1}{6}(1+3m), \frac{1}{6}(7+3m), -e^{2i(c+dx)}\right] + \\
 & \frac{1}{d} e^{ic} \left( \frac{1}{4+3m} 2B e^{\frac{1}{3}id(4+3m)x} \text{Hypergeometric2F1}\left[\frac{7}{3} + m, \frac{1}{6}(4+3m), \frac{5}{3} + \frac{m}{2}, -e^{2i(c+dx)}\right] + \right. \\
 & \left. \left( e^{\frac{1}{3}i(3c+d(7+3m)x)} \left( 2(A+2C)(13+3m) \text{Hypergeometric2F1}\left[\frac{7}{3} + m, \frac{1}{6}(7+3m), \frac{1}{6}(13+3m), -e^{2i(c+dx)}\right] + A e^{2i(c+dx)}(7+3m) \text{Hypergeometric2F1}\left[\frac{7}{3} + m, \frac{1}{6}(13+3m), \frac{1}{6}(19+3m), -e^{2i(c+dx)}\right] \right) \right) \right) / \left( (7+3m)(13+3m) \right) \Big) \\
 & (b \sec[c + dx])^{1/3} (A + B \sec[c + dx] + C \sec[c + dx]^2)
 \end{aligned}$$

**Problem 68: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\sec[c + dx]^m (A + B \sec[c + dx] + C \sec[c + dx]^2)}{(b \sec[c + dx])^{1/3}} dx$$

Optimal (type 5, 228 leaves, 7 steps):

$$\begin{aligned}
 & \frac{3C \sec[c + dx]^{1+m} \sin[c + dx]}{d(2+3m)(b \sec[c + dx])^{1/3}} + \\
 & \left( 3(C(1-3m) - A(2+3m)) \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{6}(4-3m), \frac{1}{6}(10-3m), \cos[c + dx]^2\right] \right. \\
 & \left. \sec[c + dx]^{-1+m} \sin[c + dx] \right) / \left( d(4-3m)(2+3m)(b \sec[c + dx])^{1/3} \sqrt{\sin[c + dx]^2} \right) - \\
 & \left( 3B \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{6}(1-3m), \frac{1}{6}(7-3m), \cos[c + dx]^2\right] \sec[c + dx]^m \sin[c + dx] \right) / \\
 & \left( d(1-3m)(b \sec[c + dx])^{1/3} \sqrt{\sin[c + dx]^2} \right)
 \end{aligned}$$

Result (type 5, 548 leaves):

$$\begin{aligned}
 & - \left( \left( 3 \, i \, 2^{\frac{2}{3}m} e^{-\frac{1}{3} i (3c+d(2+3m)x)} \left( \frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}} \right)^{\frac{2}{3}+m} \right. \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} \right)^{\frac{2}{3}+m} \left( A e^{\frac{1}{3} i d (-1+3m)x} (880 + 2418 m + 2079 m^2 + 702 m^3 + 81 m^4) \right. \right. \\
 & \quad \text{Hypergeometric2F1} \left[ \frac{5}{3} + m, \frac{1}{6} (-1 + 3 m), \frac{1}{6} (5 + 3 m), -e^{2i(c+dx)} \right] + \\
 & \quad e^{i c} (-1 + 3 m) \left( 2 B e^{\frac{1}{3} i d (2+3m)x} (440 + 549 m + 216 m^2 + 27 m^3) \text{Hypergeometric2F1} \left[ \right. \right. \\
 & \quad \left. \left. \frac{5}{3} + m, \frac{1}{6} (2 + 3 m), \frac{1}{6} (8 + 3 m), -e^{2i(c+dx)} \right] + e^{\frac{1}{3} i (3c+d(5+3m)x)} (2 + 3 m) \right. \\
 & \quad \left. \left( 2 (A + 2 C) (88 + 57 m + 9 m^2) \text{Hypergeometric2F1} \left[ \frac{5}{3} + m, \frac{1}{6} (5 + 3 m), \frac{1}{6} \right. \right. \right. \\
 & \quad \left. \left. (11 + 3 m), -e^{2i(c+dx)} \right] + e^{i(c+dx)} (5 + 3 m) \left( 2 B (11 + 3 m) \right. \right. \\
 & \quad \left. \left. \text{Hypergeometric2F1} \left[ \frac{5}{3} + m, \frac{1}{6} (8 + 3 m), \frac{7}{3} + \frac{m}{2}, -e^{2i(c+dx)} \right] + A e^{i(c+dx)} (8 + 3 m) \right. \right. \\
 & \quad \left. \left. \left. \left. \text{Hypergeometric2F1} \left[ \frac{5}{3} + m, \frac{1}{6} (11 + 3 m), \frac{1}{6} (17 + 3 m), -e^{2i(c+dx)} \right] \right] \right] \right) \right) \\
 & \left. (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \right) / \left( d (-1 + 3 m) (2 + 3 m) \right. \\
 & \quad (5 + 3 m) \\
 & \quad (8 + 3 m) \\
 & \quad (11 + 3 m) \\
 & \quad (A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2c + 2dx]) \\
 & \quad \left. \left. \left. \left. \text{Sec}[c + dx]^{5/3} \right. \right. \right. \\
 & \quad \left. \left. \left. \left. (b \text{Sec}[c + dx])^{1/3} \right) \right) \right)
 \end{aligned}$$

**Problem 69: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\text{Sec}[c + dx]^m (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2)}{(b \text{Sec}[c + dx])^{2/3}} dx$$

Optimal (type 5, 226 leaves, 7 steps):

$$\frac{3 C \operatorname{Sec}[c+d x]^{1+m} \operatorname{Sin}[c+d x]}{d(1+3 m)(b \operatorname{Sec}[c+d x])^{2/3}} - \left( 3(A-C(2-3m)+3Am) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{6}(5-3m), \frac{1}{6}(11-3m), \operatorname{Cos}[c+d x]^2\right] \operatorname{Sec}[c+d x]^{-1+m} \operatorname{Sin}[c+d x] \right) / \left( d(5-3m)(1+3m)(b \operatorname{Sec}[c+d x])^{2/3} \sqrt{\operatorname{Sin}[c+d x]^2} \right) - \left( 3B \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{6}(2-3m), \frac{1}{6}(8-3m), \operatorname{Cos}[c+d x]^2\right] \operatorname{Sec}[c+d x]^m \operatorname{Sin}[c+d x] \right) / \left( d(2-3m)(b \operatorname{Sec}[c+d x])^{2/3} \sqrt{\operatorname{Sin}[c+d x]^2} \right)$$

Result (type 5, 545 leaves):

$$- \left( \left( 3 i 2^{\frac{1}{3}+m} e^{-\frac{1}{3} i (3c+d(1+3m)x)} \left( \frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}} \right)^{\frac{1}{3}+m} \right. \right. \\ \left. \left. (1+e^{2i(c+dx)})^{\frac{1}{3}+m} \left( A e^{4i c+\frac{1}{3} i d(10+3m)x} (-56-150m+135m^2+270m^3+81m^4) \right. \right. \right. \\ \left. \left. \operatorname{Hypergeometric2F1}\left[\frac{5}{3}+\frac{m}{2}, \frac{4}{3}+m, \frac{8}{3}+\frac{m}{2}, -e^{2i(c+dx)}\right] + \right. \right. \\ \left. \left. (10+3m) \left( A e^{\frac{1}{3} i d(-2+3m)x} (28+117m+108m^2+27m^3) \operatorname{Hypergeometric2F1}\left[\frac{4}{3}+m, \right. \right. \right. \\ \left. \left. \frac{1}{6}(-2+3m), \frac{1}{6}(4+3m), -e^{2i(c+dx)}\right] + 2 e^{\frac{1}{3} i (3c+d(1+3m)x)} (-2+3m) \right. \right. \\ \left. \left. \left( B(28+33m+9m^2) \operatorname{Hypergeometric2F1}\left[\frac{4}{3}+m, \frac{1}{6}(1+3m), \frac{1}{6}(7+3m), -e^{2i(c+dx)}\right] + \right. \right. \\ \left. \left. e^{i(c+dx)} (1+3m) \left( (A+2C)(7+3m) \operatorname{Hypergeometric2F1}\left[\frac{4}{3}+m, \right. \right. \right. \\ \left. \left. \frac{1}{6}(4+3m), \frac{5}{3}+\frac{m}{2}, -e^{2i(c+dx)}\right] + B e^{i(c+dx)} (4+3m) \right. \right. \\ \left. \left. \left. \left. \operatorname{Hypergeometric2F1}\left[\frac{4}{3}+m, \frac{1}{6}(7+3m), \frac{1}{6}(13+3m), -e^{2i(c+dx)}\right] \right) \right) \right) \right) \\ \left. \left. \left. \left. \left. (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) \right) \right) / \left( d(-2+3m)(1+3m) \right. \\ \left. (4+3m) \right. \\ \left. (7+3m) \right. \\ \left. (10+3m) \right. \\ \left. (A+2C+2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) \right. \\ \left. \operatorname{Sec}[c+dx]^{4/3} \right. \\ \left. (b \operatorname{Sec}[c+dx])^{2/3} \right)$$

**Problem 70: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\text{Sec}[c + d x]^m (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2)}{(b \text{Sec}[c + d x])^{4/3}} dx$$

Optimal (type 5, 234 leaves, 7 steps):

$$\frac{3 C \text{Sec}[c + d x]^m \text{Sin}[c + d x]}{b d (1 - 3 m) (b \text{Sec}[c + d x])^{1/3}} - \left( 3 (A + C (4 - 3 m) - 3 A m) \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{6} (7 - 3 m), \frac{1}{6} (13 - 3 m), \text{Cos}[c + d x]^2\right] \text{Sec}[c + d x]^{-2+m} \text{Sin}[c + d x] \right) / \left( b d (1 - 3 m) (7 - 3 m) (b \text{Sec}[c + d x])^{1/3} \sqrt{\text{Sin}[c + d x]^2} \right) - \left( 3 B \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{6} (4 - 3 m), \frac{1}{6} (10 - 3 m), \text{Cos}[c + d x]^2\right] \text{Sec}[c + d x]^{-1+m} \text{Sin}[c + d x] \right) / \left( b d (4 - 3 m) (b \text{Sec}[c + d x])^{1/3} \sqrt{\text{Sin}[c + d x]^2} \right)$$

Result (type 5, 492 leaves):

$$- \left( \left( 3 i 2^{-\frac{1}{3}+m} e^{-\frac{1}{3} i (6 c+d (2+3 m) x)} \left( \frac{e^{i (c+d x)}}{1 + e^{2 i (c+d x)}} \right)^{\frac{2}{3}+m} (1 + e^{2 i (c+d x)})^{\frac{2}{3}+m} \right. \right. \\ \left. \left( \frac{1}{-4 + 3 m} A e^{\frac{1}{3} i d (-4+3 m) x} \text{Hypergeometric2F1}\left[\frac{2}{3} + m, \frac{1}{6} (-4 + 3 m), \frac{1}{6} (2 + 3 m), -e^{2 i (c+d x)}\right] + \right. \right. \\ \left. \frac{1}{-1 + 3 m} 2 B e^{\frac{1}{3} i (3 c+d (-1+3 m) x)} \text{Hypergeometric2F1}\left[\frac{2}{3} + m, \frac{1}{6} (-1 + 3 m), \right. \right. \\ \left. \left. \frac{1}{6} (5 + 3 m), -e^{2 i (c+d x)}\right] + e^{2 i c} \left( \frac{1}{2 + 3 m} 2 (A + 2 C) e^{\frac{1}{3} i d (2+3 m) x} \right. \right. \\ \left. \left. \text{Hypergeometric2F1}\left[\frac{2}{3} + m, \frac{1}{6} (2 + 3 m), \frac{1}{6} (8 + 3 m), -e^{2 i (c+d x)}\right] + \frac{1}{5 + 3 m} \right. \right. \\ \left. \left. 2 B e^{\frac{1}{3} i (3 c+d (5+3 m) x)} \text{Hypergeometric2F1}\left[\frac{2}{3} + m, \frac{1}{6} (5 + 3 m), \frac{1}{6} (11 + 3 m), -e^{2 i (c+d x)}\right] + \right. \right. \\ \left. \left. \frac{1}{8 + 3 m} A e^{\frac{1}{3} i (6 c+d (8+3 m) x)} \text{Hypergeometric2F1}\left[\frac{2}{3} + m, \frac{1}{6} (8 + 3 m), \frac{7}{3} + \frac{m}{2}, -e^{2 i (c+d x)}\right] \right) \right) \\ \left. (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) \right) / \left( d (A + 2 C + 2 B \text{Cos}[c + d x] + A \text{Cos}[2 c + 2 d x]) \text{Sec}[c + d x]^{2/3} (b \text{Sec}[c + d x])^{4/3} \right)$$

**Problem 71: Result unnecessarily involves imaginary or complex numbers.**

$$\int \text{Sec}[c + d x]^m (b \text{Sec}[c + d x])^n (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) dx$$

Optimal (type 5, 226 leaves, 7 steps):

$$\frac{C \operatorname{Sec}[c+d x]^{1+m} (b \operatorname{Sec}[c+d x])^n \operatorname{Sin}[c+d x]}{d(1+m+n)} -$$

$$\left( (C(m+n) + A(1+m+n)) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{2}(1-m-n), \frac{1}{2}(3-m-n), \operatorname{Cos}[c+d x]^2\right] \right.$$

$$\left. \operatorname{Sec}[c+d x]^{-1+m} (b \operatorname{Sec}[c+d x])^n \operatorname{Sin}[c+d x] \right) / \left( d(1-m-n)(1+m+n) \sqrt{\operatorname{Sin}[c+d x]^2} \right) +$$

$$\left( B \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{2}(-m-n), \frac{1}{2}(2-m-n), \operatorname{Cos}[c+d x]^2\right] \operatorname{Sec}[c+d x]^m \right.$$

$$\left. (b \operatorname{Sec}[c+d x])^n \operatorname{Sin}[c+d x] \right) / \left( d(m+n) \sqrt{\operatorname{Sin}[c+d x]^2} \right)$$

Result (type 5, 436 leaves):

$$\frac{1}{d(A+2C+2B \operatorname{Cos}[c+d x] + A \operatorname{Cos}[2c+2dx])}$$

$$i 2^{1+m+n} e^{-i d(m+n)x} \left( \frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}} \right)^{m+n} (1+e^{2i(c+dx)})^{m+n}$$

$$\left( \frac{1}{m+n} A e^{i d(m+n)x} \operatorname{Hypergeometric2F1}\left[\frac{m+n}{2}, 2+m+n, \frac{1}{2}(2+m+n), -e^{2i(c+dx)}\right] + \frac{1}{1+m+n} \right.$$

$$2B e^{i(c+d(1+m+n)x)} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}(1+m+n), 2+m+n, \frac{1}{2}(3+m+n), -e^{2i(c+dx)}\right] +$$

$$e^{2ic} \left( \frac{1}{2+m+n} 2(A+2C) e^{i d(2+m+n)x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}(2+m+n), \right.$$

$$2+m+n, \frac{1}{2}(4+m+n), -e^{2i(c+dx)}\right] + \frac{1}{3+m+n} 2B e^{i(c+d(3+m+n)x)} \operatorname{Hypergeometric2F1}\left[2+m+n, \frac{1}{2}(3+m+n), \frac{1}{2}(5+m+n), -e^{2i(c+dx)}\right] + \frac{1}{4+m+n}$$

$$\left. \left. A e^{i(2c+d(4+m+n)x)} \operatorname{Hypergeometric2F1}\left[2+m+n, \frac{1}{2}(4+m+n), \frac{1}{2}(6+m+n), -e^{2i(c+dx)}\right] \right) \right)$$

$$\operatorname{Sec}[c+d x]^{-2-n} (b \operatorname{Sec}[c+d x])^n (A+B \operatorname{Sec}[c+d x] + C \operatorname{Sec}[c+d x]^2)$$

**Problem 72: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c+d x]^2 (b \operatorname{Sec}[c+d x])^n (A+B \operatorname{Sec}[c+d x] + C \operatorname{Sec}[c+d x]^2) dx$$

Optimal (type 5, 189 leaves, 7 steps):

$$\left( (C(2+n) + A(3+n)) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{2}(-1-n), \frac{1-n}{2}, \operatorname{Cos}[c+d x]^2\right] \right.$$

$$\left. (b \operatorname{Sec}[c+d x])^{1+n} \operatorname{Sin}[c+d x] \right) / \left( b d(1+n)(3+n) \sqrt{\operatorname{Sin}[c+d x]^2} \right) +$$

$$\left( B \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{2}(-2-n), -\frac{n}{2}, \operatorname{Cos}[c+d x]^2\right] (b \operatorname{Sec}[c+d x])^{2+n} \operatorname{Sin}[c+d x] \right) /$$

$$\left( b^2 d(2+n) \sqrt{\operatorname{Sin}[c+d x]^2} \right) + \frac{C (b \operatorname{Sec}[c+d x])^{2+n} \operatorname{Tan}[c+d x]}{b^2 d(3+n)}$$

Result (type 5, 462 leaves):

$$\begin{aligned}
 & - \frac{1}{d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])} i^{2^{3+n}} e^{2 i c - i d n x} \left( \frac{e^{i (c+d x)}}{1 + e^{2 i (c+d x)}} \right)^n \\
 & \left( 1 + e^{2 i (c+d x)} \right)^n \left( \frac{A e^{i d (2+n) x} \text{Hypergeometric2F1} \left[ \frac{2+n}{2}, 4+n, \frac{4+n}{2}, -e^{2 i (c+d x)} \right]}{2+n} + \right. \\
 & \frac{2 B e^{i (c+d (3+n) x)} \text{Hypergeometric2F1} \left[ \frac{3+n}{2}, 4+n, \frac{5+n}{2}, -e^{2 i (c+d x)} \right]}{3+n} + \\
 & \frac{2 A e^{i (2 c+d (4+n) x)} \text{Hypergeometric2F1} \left[ \frac{4+n}{2}, 4+n, \frac{6+n}{2}, -e^{2 i (c+d x)} \right]}{4+n} + \\
 & \frac{4 C e^{i (2 c+d (4+n) x)} \text{Hypergeometric2F1} \left[ \frac{4+n}{2}, 4+n, \frac{6+n}{2}, -e^{2 i (c+d x)} \right]}{4+n} + \\
 & \left. \frac{2 B e^{i (3 c+d (5+n) x)} \text{Hypergeometric2F1} \left[ 4+n, \frac{5+n}{2}, \frac{7+n}{2}, -e^{2 i (c+d x)} \right]}{5+n} + \right. \\
 & \left. \frac{A e^{i (4 c+d (6+n) x)} \text{Hypergeometric2F1} \left[ 4+n, \frac{6+n}{2}, \frac{8+n}{2}, -e^{2 i (c+d x)} \right]}{6+n} \right) \\
 & \sec [c + d x]^{-2-n} (b \sec [c + d x])^n (A + B \sec [c + d x] + C \sec [c + d x]^2)
 \end{aligned}$$

**Problem 73: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \sec [c + d x] (b \sec [c + d x])^n (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 5, 182 leaves, 7 steps):

$$\begin{aligned}
 & \left( (C (1+n) + A (2+n)) \text{Hypergeometric2F1} \left[ \frac{1}{2}, -\frac{n}{2}, \frac{2-n}{2}, \cos [c + d x]^2 \right] \right. \\
 & \left. (b \sec [c + d x])^n \sin [c + d x] \right) / \left( d n (2+n) \sqrt{\sin [c + d x]^2} \right) + \\
 & \left( B \text{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{1}{2} (-1-n), \frac{1-n}{2}, \cos [c + d x]^2 \right] (b \sec [c + d x])^{1+n} \sin [c + d x] \right) / \\
 & \left( b d (1+n) \sqrt{\sin [c + d x]^2} \right) + \frac{C (b \sec [c + d x])^{1+n} \tan [c + d x]}{b d (2+n)}
 \end{aligned}$$

Result (type 5, 460 leaves):

$$\begin{aligned}
 & - \frac{1}{d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])} i^{2^{2+n}} e^{i (c-d n x)} \left( \frac{e^{i (c+d x)}}{1 + e^{2 i (c+d x)}} \right)^n \\
 & \left( 1 + e^{2 i (c+d x)} \right)^n \left( \frac{A e^{i d (1+n) x} \text{Hypergeometric2F1} \left[ \frac{1+n}{2}, 3+n, \frac{3+n}{2}, -e^{2 i (c+d x)} \right]}{1+n} + \right. \\
 & \frac{2 B e^{i (c+d (2+n) x)} \text{Hypergeometric2F1} \left[ \frac{2+n}{2}, 3+n, \frac{4+n}{2}, -e^{2 i (c+d x)} \right]}{2+n} + \\
 & \frac{2 A e^{i (2 c+d (3+n) x)} \text{Hypergeometric2F1} \left[ \frac{3+n}{2}, 3+n, \frac{5+n}{2}, -e^{2 i (c+d x)} \right]}{3+n} + \\
 & \frac{4 C e^{i (2 c+d (3+n) x)} \text{Hypergeometric2F1} \left[ \frac{3+n}{2}, 3+n, \frac{5+n}{2}, -e^{2 i (c+d x)} \right]}{3+n} + \\
 & \left. \frac{2 B e^{i (3 c+d (4+n) x)} \text{Hypergeometric2F1} \left[ 3+n, \frac{4+n}{2}, \frac{6+n}{2}, -e^{2 i (c+d x)} \right]}{4+n} + \right. \\
 & \left. \frac{A e^{i (4 c+d (5+n) x)} \text{Hypergeometric2F1} \left[ 3+n, \frac{5+n}{2}, \frac{7+n}{2}, -e^{2 i (c+d x)} \right]}{5+n} \right) \\
 & \sec [c + d x]^{-2-n} (b \sec [c + d x])^n (A + B \sec [c + d x] + C \sec [c + d x]^2)
 \end{aligned}$$

**Problem 74: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int (b \sec [c + d x])^n (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 5, 175 leaves, 6 steps):

$$\begin{aligned}
 & - \left( \left( b (A + A n + C n) \text{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{1-n}{2}, \frac{3-n}{2}, \cos [c + d x]^2 \right] \right. \right. \\
 & \left. \left. (b \sec [c + d x])^{-1+n} \sin [c + d x] \right) / \left( d (1-n) (1+n) \sqrt{\sin [c + d x]^2} \right) \right) + \\
 & \left( B \text{Hypergeometric2F1} \left[ \frac{1}{2}, -\frac{n}{2}, \frac{2-n}{2}, \cos [c + d x]^2 \right] (b \sec [c + d x])^n \sin [c + d x] \right) / \\
 & \left( d n \sqrt{\sin [c + d x]^2} \right) + \frac{C (b \sec [c + d x])^n \tan [c + d x]}{d (1+n)}
 \end{aligned}$$

Result (type 5, 401 leaves):

$$\begin{aligned}
& - \frac{1}{d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx])} \int 2^{1+n} e^{-i dx} \left( \frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}} \right)^n \\
& (1 + e^{2i(c+dx)})^n \left( \frac{A e^{i dx} \text{Hypergeometric2F1} \left[ \frac{n}{2}, 2+n, \frac{2+n}{2}, -e^{2i(c+dx)} \right]}{n} + \right. \\
& \frac{2B e^{i(c+d(1+n)x)} \text{Hypergeometric2F1} \left[ \frac{1+n}{2}, 2+n, \frac{3+n}{2}, -e^{2i(c+dx)} \right]}{1+n} + \\
& e^{2ic} \left( \frac{1}{2+n} 2(A+2C) e^{i d(2+n)x} \text{Hypergeometric2F1} \left[ \frac{2+n}{2}, 2+n, \frac{4+n}{2}, -e^{2i(c+dx)} \right] + \right. \\
& \frac{1}{3+n} 2B e^{i(c+d(3+n)x)} \text{Hypergeometric2F1} \left[ 2+n, \frac{3+n}{2}, \frac{5+n}{2}, -e^{2i(c+dx)} \right] + \\
& \left. \left. \frac{1}{4+n} A e^{i(2c+d(4+n)x)} \text{Hypergeometric2F1} \left[ 2+n, \frac{4+n}{2}, \frac{6+n}{2}, -e^{2i(c+dx)} \right] \right) \right) \\
& \text{Sec}[c+dx]^{-2-n} (b \text{Sec}[c+dx])^n (A+B \text{Sec}[c+dx] + C \text{Sec}[c+dx]^2)
\end{aligned}$$

**Problem 75: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c + dx] (b \text{Sec}[c + dx])^n (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) dx$$

Optimal (type 5, 191 leaves, 7 steps):

$$\begin{aligned}
& \left( b^2 (C(1-n) - An) \text{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{2-n}{2}, \frac{4-n}{2}, \cos [c + dx]^2 \right] \right. \\
& \left. (b \text{Sec}[c + dx])^{-2+n} \sin [c + dx] \right) / \left( d(2-n)n \sqrt{\sin [c + dx]^2} \right) - \\
& \left( bB \text{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{1-n}{2}, \frac{3-n}{2}, \cos [c + dx]^2 \right] (b \text{Sec}[c + dx])^{-1+n} \sin [c + dx] \right) / \\
& \left( d(1-n) \sqrt{\sin [c + dx]^2} \right) + \frac{bC (b \text{Sec}[c + dx])^{-1+n} \tan [c + dx]}{dn}
\end{aligned}$$

Result (type 6, 6083 leaves):

$$\begin{aligned}
& - \left( \left( 6 \text{Sec}[c + dx]^{-n} (b \text{Sec}[c + dx])^n \left( B \text{Sec}[c + dx]^n + \frac{1}{2} A \cos [2(c + dx)] \text{Sec}[c + dx]^{1+n} + \right. \right. \right. \\
& \left. \left. \left. \text{Sec}[c + dx] \left( \frac{1}{2} A \text{Sec}[c + dx]^n + C \text{Sec}[c + dx]^n \right) \tan \left[ \frac{1}{2} (c + dx) \right] \left( \frac{1 + \tan \left[ \frac{1}{2} (c + dx) \right]^2}{1 - \tan \left[ \frac{1}{2} (c + dx) \right]^2} \right)^n \right. \right. \right. \\
& \left. \left( (A - B) \text{AppellF1} \left[ \frac{1}{2}, n, 1 - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) / \right. \\
& \left. \left( \left( 1 + \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \left( 3 \text{AppellF1} \left[ \frac{1}{2}, n, 1 - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \right. \right. \right. \right. \\
& \left. \left. \left. -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + 2 \left( (-1 + n) \text{AppellF1} \left[ \frac{3}{2}, n, 2 - n, \frac{5}{2}, \right. \right. \right. \right.
\end{aligned}$$



$$\begin{aligned}
 & \left( \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \right. \\
 & \left. \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \Big) - \\
 & \left( 2A \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) / \\
 & \left( \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \right. \right. \right. \\
 & \left. \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
 & \left( C \operatorname{AppellF1}\left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) / \\
 & \left( \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right. \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \left. 2 \left( n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + (1+n) \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}, 2+n, -n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Big) / \left( d \left( -3 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \right)^2 \left( \frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^n \right. \\
 & \left. \left( (A-B) \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right) / \\
 & \left( \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \right. \right. \right. \\
 & \left. \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) - \\
 & \left( 2A \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) / \\
 & \left( \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& \left. \left. \left. \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) + \right. \\
& \left. \left( C \operatorname{AppellF1}\left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) / \right. \\
& \left. \left( \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + 2 \left( n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + (1+n) \operatorname{AppellF1}\left[\frac{3}{2}, 2+n, -n, \frac{5}{2}, \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right) - \\
& 6n \tan\left[\frac{1}{2}(c+dx)\right] \left( \frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{-1+n} \left( \frac{\sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} + \right. \\
& \left. \frac{\sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)}{\left(1 - \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2} \right) \\
& \left( \left( (A-B) \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) / \right. \\
& \left( \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) - \\
& \left( 2A \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) / \\
& \left( \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + 2 \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) + \\
& \left( C \operatorname{AppellF1}\left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) / \\
& \left( \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + 2 \left( n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + (1+n) \operatorname{AppellF1}\left[\frac{3}{2}, 2+n, -n, \frac{5}{2}, \right. \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & \left. \left( \left( \left( \left( \left( \left( \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right)^2\right) \right)^2\right) \right)^2\right) - \\
 6 \tan\left[\frac{1}{2}(c+dx)\right] & \left( \frac{\left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^n}{\left(1 - \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2} \left( - \left( \left( (A-B) \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) \right) \right) / \\
 & \left( \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \right. \right. \right. \\
 & \left. \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) + \\
 & \left( (A-B) \left( -\frac{1}{3} (1-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) / \\
 & \left( \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^3 \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \right. \right. \right. \\
 & \left. \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) + \\
 & \left( 4A \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) / \\
 & \left( \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^3 \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \right. \right. \right. \\
 & \left. \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) - \\
 & \left( 2A \left( -\frac{1}{3} (2-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left( \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right] \right)^2, -\tan\left[\frac{1}{2}(c+dx)\right] \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) / \\
 & \left( \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right] \right)^2 \right)^2 \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right] \right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{2}(c+dx)\right] \right]^2 + 2 \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \right. \right. \\
 & \quad \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right] \right] + n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \right. \\
 & \quad \quad \left. \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right] \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \\
 & \left( C \operatorname{AppellF1}\left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right] \right]^2 \right) \\
 & \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) / \\
 & \left( \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right] \right)^2 \right)^2 \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right] \right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{2}(c+dx)\right] \right]^2 + 2 \left( n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right] \right]^2, \right. \\
 & \quad \quad \left. -\tan\left[\frac{1}{2}(c+dx)\right] \right] + (1+n) \operatorname{AppellF1}\left[\frac{3}{2}, 2+n, -n, \frac{5}{2}, \right. \\
 & \quad \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right] \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + \\
 & \left( C \left( \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right] \right]^2 \right) \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{3} (1+n) \operatorname{AppellF1}\left[\frac{3}{2}, 2+n, -n, \frac{5}{2}, \right. \right. \\
 & \quad \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right] \right] \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) / \\
 & \left( \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right] \right)^2 \right)^2 \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right] \right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{2}(c+dx)\right] \right]^2 + 2 \left( n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right] \right]^2, \right. \\
 & \quad \quad \left. -\tan\left[\frac{1}{2}(c+dx)\right] \right] + (1+n) \operatorname{AppellF1}\left[\frac{3}{2}, 2+n, -n, \frac{5}{2}, \right. \\
 & \quad \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right] \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \\
 & \left( (A-B) \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right] \right]^2 \right) \\
 & \quad \left( 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right] \right]^2 \right) + \right. \\
 & \quad \quad \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right] \right]^2 \right) \\
 & \quad \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 3 \left( -\frac{1}{3} (1-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \right. \right. \\
 & \quad \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right] \right] \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \left( (-1+n) \left( -\frac{3}{5} (2-n) \operatorname{AppellF1}\left[\frac{5}{2}, n, 3-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \quad \left. \frac{3}{5} n \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + n \left( -\frac{3}{5} (1-n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, \right. \right. \\
 & \quad \left. \left. 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right. \\
 & \quad \left. \left. + \frac{3}{5} (1+n) \operatorname{AppellF1}\left[\frac{5}{2}, 2+n, 1-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \Big/ \\
 & \left( \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
 & \left( 2 A \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left. \left( 2 \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \right. \right. \\
 & \quad \left. \left. \left. + n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 3 \left( -\frac{1}{3} (2-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \quad \left. \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \quad \left( (-2+n) \left( -\frac{3}{5} (3-n) \operatorname{AppellF1}\left[\frac{5}{2}, n, 4-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \quad \left. \frac{3}{5} n \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, 3-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \Big/
 \end{aligned}$$

$$\begin{aligned}
& \left( \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + n \left( -\frac{3}{5}(2-n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, \right. \right. \\
& \left. \left. 3-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
& \left. \left. + \frac{3}{5}(1+n) \operatorname{AppellF1}\left[\frac{5}{2}, 2+n, 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) / \\
& \left( \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \right. \right. \right. \right. \\
& \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \right. \right. \right. \right. \\
& \left. \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) - \\
& \left( c \operatorname{AppellF1}\left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \left. \left( 2 \left( n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \right. \right. \\
& \left. \left. \left. (1+n) \operatorname{AppellF1}\left[\frac{3}{2}, 2+n, -n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right) \right. \\
& \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 3 \left( \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \right. \right. \right. \right. \\
& \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + \right. \\
& \left. \frac{1}{3}(1+n) \operatorname{AppellF1}\left[\frac{3}{2}, 2+n, -n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
& \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \left( n \left( -\frac{3}{5}(1-n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 + \frac{3}{5}(1+n) \right. \right. \\
& \left. \left. \operatorname{AppellF1}\left[\frac{5}{2}, 2+n, 1-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
& \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + (1+n) \left( \frac{3}{5} n \operatorname{AppellF1}\left[\frac{5}{2}, 2+n, \right. \right. \\
& \left. \left. 1-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
& \left. \left. + \frac{3}{5}(2+n) \operatorname{AppellF1}\left[\frac{5}{2}, 3+n, -n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) / \\
& \left( \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + 2 \left( n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + (1+n) \operatorname{AppellF1}\left[\frac{3}{2}, 2+n, -n, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right) \right) \right)
 \end{aligned}$$

**Problem 76: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c+dx]^2 (b \operatorname{Sec}[c+dx])^n (A+B \operatorname{Sec}[c+dx]+C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 5, 208 leaves, 7 steps):

$$\begin{aligned}
 & -\left( \left( b^3 (A(1-n) + C(2-n)) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3-n}{2}, \frac{5-n}{2}, \cos [c+dx]^2\right] \right. \right. \\
 & \quad \left. \left. (b \operatorname{Sec}[c+dx])^{-3+n} \sin [c+dx] \right) / \left( d(1-n)(3-n) \sqrt{\sin [c+dx]^2} \right) \right) - \\
 & \left( b^2 B \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{2-n}{2}, \frac{4-n}{2}, \cos [c+dx]^2\right] (b \operatorname{Sec}[c+dx])^{-2+n} \sin [c+dx] \right) / \\
 & \left( d(2-n) \sqrt{\sin [c+dx]^2} \right) - \frac{b^2 C (b \operatorname{Sec}[c+dx])^{-2+n} \operatorname{Tan}[c+dx]}{d(1-n)}
 \end{aligned}$$

Result (type 6, 12574 leaves):

$$\begin{aligned}
 & \left( 6 \operatorname{Sec}[c+dx]^{-n} (b \operatorname{Sec}[c+dx])^n \right. \\
 & \quad \left( B \operatorname{Sec}[c+dx]^{-1+n} + \frac{1}{2} A \operatorname{Sec}[c+dx]^n + C \operatorname{Sec}[c+dx]^n + \frac{1}{2} A \cos [2(c+dx)] \operatorname{Sec}[c+dx]^n \right) \\
 & \quad \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \left( \frac{1}{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^n \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right)^{-3+n} \\
 & \quad \left( \left( A \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) / \right. \\
 & \quad \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \right. \\
 & \quad \left. \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + n \operatorname{AppellF1}\left[ \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - \\
 & \quad \left. \left( B \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right)
 \end{aligned}$$





$$\left. \left. \left. \left. \frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right)\right) \Bigg/$$

$$\left( d \left( 6(-3+n) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( \frac{1}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^n \right. \right.$$

$$\left. \left. \left( 1+\tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^{-4+n} \left( \left( A \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \right. \right. \right. \right.$$

$$\left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left( 1+\tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right)\right) \Bigg/$$

$$\left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right.$$

$$2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right.$$

$$\left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right.$$

$$\left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \left( B \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right.$$

$$\left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left( 1+\tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right)\right) \Bigg/$$

$$\left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right.$$

$$2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right.$$

$$\left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right.$$

$$\left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + \left( C \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right.$$

$$\left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left( 1+\tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right)\right) \Bigg/$$

$$\left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right.$$

$$2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right.$$

$$\left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right.$$

$$\left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \left( 4 A \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right.$$

$$\left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left( 1+\tan\left[\frac{1}{2}(c+dx)\right]^2 \right)\right)\right) \Bigg/$$

$$\left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right.$$

$$2 \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right.$$

$$\left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right)$$

$$\begin{aligned}
& \left. \left( \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + \left( 2B \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
& \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \right) / \\
& \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \left( (-2+n) \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + n \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
& \quad \left. \left. \left. 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + \\
& \left( 4A \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) / \\
& \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \left( (-3+n) \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + n \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
& \quad \left. \left. \left. 1+n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
& 3 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left( \frac{1}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^n \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^{-3+n} \\
& \left( \left( A \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
& \quad \left. \left. \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) \right) / \\
& \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right) \\
& \quad \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \left( B \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) \right) / \\
& \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right) \\
& \quad \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + \left( C \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) \right) /
\end{aligned}$$

$$\begin{aligned}
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \\
 & \tan \left[ \frac{1}{2} (c+dx) \right]^2 \Big) - \left( 4 A \operatorname{AppellF1} \left[ \frac{1}{2}, n, 2-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 2-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & 2 \left( (-2+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 3-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \\
 & \tan \left[ \frac{1}{2} (c+dx) \right]^2 \Big) + \left( 2 B \operatorname{AppellF1} \left[ \frac{1}{2}, n, 2-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 2-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + 2 \left( (-2+n) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, n, 3-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + n \operatorname{AppellF1} \left[ \frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. 1+n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) + \\
 & \left( 4 A \operatorname{AppellF1} \left[ \frac{1}{2}, n, 3-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 3-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + 2 \left( (-3+n) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, n, 4-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + n \operatorname{AppellF1} \left[ \frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. 1+n, 3-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \Big) + \\
 & 6 n \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right]^2 \left( \frac{1}{1 - \tan \left[ \frac{1}{2} (c+dx) \right]^2} \right)^{1+n} \\
 & \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^{-3+n} \\
 & \left( \left( A \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \right. \\
 & \quad \left. \left. \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^2 \right) \right) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right.
 \end{aligned}$$



$$\begin{aligned}
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 3-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + 2 \left( (-3+n) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, n, 4-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + n \operatorname{AppellF1} \left[ \frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. 1+n, 3-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) + \\
 & 6 \tan \left[ \frac{1}{2} (c+dx) \right] \left( \frac{1}{1 - \tan \left[ \frac{1}{2} (c+dx) \right]^2} \right)^n \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^{-3+n} \\
 & \left( \left( 2 A \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \right. \\
 & \quad \left. \left. \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \right) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + 2 \left( (-1+n) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + n \operatorname{AppellF1} \left[ \frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. 1+n, 1-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) - \\
 & \left( 2 B \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
 & \quad \left. \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + 2 \left( (-1+n) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + n \operatorname{AppellF1} \left[ \frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. 1+n, 1-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) + \\
 & \left( 2 C \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
 & \quad \left. \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \left. 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \right. \\
 & \quad \left. \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \right) \\
 & \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) + \left( A \left( -\frac{1}{3} (1-n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 2-n, \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \right. \\
 & \quad \left. \frac{1}{3} n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right)
 \end{aligned}$$

$$\begin{aligned}
& \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \Big/ \\
& \left(3 \text{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& 2 \left( (-1+n) \text{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left. n \text{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
& \tan\left[\frac{1}{2}(c+dx)\right]^2 \Big) - \left( B \left( -\frac{1}{3} (1-n) \text{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
& \quad \left. \left. \frac{1}{3} n \text{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
& \quad \left. \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \Big/ \right. \\
& \left. \left(3 \text{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
& 2 \left( (-1+n) \text{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left. n \text{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
& \tan\left[\frac{1}{2}(c+dx)\right]^2 \Big) + \left( C \left( -\frac{1}{3} (1-n) \text{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
& \quad \left. \left. \frac{1}{3} n \text{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
& \quad \left. \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \Big/ \right. \\
& \left. \left(3 \text{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
& 2 \left( (-1+n) \text{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left. n \text{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
& \tan\left[\frac{1}{2}(c+dx)\right]^2 \Big) - \left( 4 A \text{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \Big) \Big/ \right. \\
& \left. \left(3 \text{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
& 2 \left( (-2+n) \text{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left. n \text{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right)
\end{aligned}$$

$$\begin{aligned}
 & \tan\left[\frac{1}{2}(c+dx)\right]^2 + \left(2B \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \left. 2\left((-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right)\right) \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^2 - \left(4A\left(-\frac{1}{3}(2-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \left. \frac{1}{3}n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right)\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \left. 2\left((-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right)\right) \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^2 + \left(2B\left(-\frac{1}{3}(2-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \left. \frac{1}{3}n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right)\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2\left((-2+n) \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + n \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
 & \left. \left. \left. 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right)\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 + \\
 & \left(4A\left(-\frac{1}{3}(3-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{3}n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right)\right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 \left( (-3+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
 & \quad \tan\left[\frac{1}{2}(c+dx)\right]^2 - \left( A \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \right. \\
 & \quad \left( 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 3 \left( -\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \quad \left. \left. \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \left( (-1+n) \left( -\frac{3}{5}(2-n) \operatorname{AppellF1}\left[\frac{5}{2}, n, 3-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \quad \left. \left. \frac{3}{5} n \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + n \left( -\frac{3}{5}(1-n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, \right. \right. \right. \\
 & \quad \left. \left. 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right. \right. \\
 & \quad \left. \left. \frac{1}{2}(c+dx) \right) + \frac{3}{5}(1+n) \operatorname{AppellF1}\left[\frac{5}{2}, 2+n, 1-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \Big/ \\
 & \quad \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 + \\
 & \quad \left( B \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left. \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \left( 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2] + n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \\
 & 3 \left( -\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) + \\
 & 2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left( (-1+n) \left( -\frac{3}{5}(2-n) \operatorname{AppellF1}\left[\frac{5}{2}, n, 3-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \left. \frac{3}{5} n \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, 2-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) + n \left( -\frac{3}{5}(1-n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, \right. \right. \\
 & \left. \left. 2-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right. \\
 & \left. \left. + \frac{3}{5}(1+n) \operatorname{AppellF1}\left[\frac{5}{2}, 2+n, 1-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) \Big/ \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 - \\
 & \left( C \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \left. \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right. \\
 & \left. \left( 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \right. \\
 & \left. \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right) \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 3 \left( -\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \left. \left. \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
& \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
& \left( (-1+n) \left( -\frac{3}{5}(2-n) \operatorname{AppellF1}\left[\frac{5}{2}, n, 3-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
& \quad \left. \frac{3}{5}n \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, 2-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) + n \left( -\frac{3}{5}(1-n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, \right. \right. \\
& \quad \left. \left. 2-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right. \\
& \quad \left. \left. + \frac{3}{5}(1+n) \operatorname{AppellF1}\left[\frac{5}{2}, 2+n, 1-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) \Big/ \\
& \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \Big)^2 + \\
& \left( 4 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left. \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right. \\
& \quad \left. \left( 2 \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \right. \\
& \quad \left. \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right) \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 3 \left( -\frac{1}{3}(2-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \right. \right. \right. \\
& \quad \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
& \quad \left. \frac{1}{3}n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) + 2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
& \quad \left( (-2+n) \left( -\frac{3}{5}(3-n) \operatorname{AppellF1}\left[\frac{5}{2}, n, 4-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
& \quad \left. \left. \frac{3}{5}n \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, 3-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right)
\end{aligned}$$

$$\begin{aligned}
 & \left( \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + n \left( -\frac{3}{5}(2-n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, \right. \right. \\
 & \quad \left. \left. 3-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \left. \left. + \frac{3}{5}(1+n) \operatorname{AppellF1}\left[\frac{5}{2}, 2+n, 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \right) / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad 2 \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \quad \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 - \\
 & \left. \left( 2 \operatorname{BAppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
 & \quad \left. \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \\
 & \left( 2 \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right) \\
 & \quad \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 3 \left( -\frac{1}{3}(2-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
 & \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \left( (-2+n) \left( -\frac{3}{5}(3-n) \operatorname{AppellF1}\left[\frac{5}{2}, n, 4-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \frac{3}{5} n \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, 3-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + n \left( -\frac{3}{5}(2-n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, \right. \right. \\
 & \quad \left. \left. 3-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \left. \left. + \frac{3}{5}(1+n) \operatorname{AppellF1}\left[\frac{5}{2}, 2+n, 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad 2 \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \quad n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \quad \quad \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 - \\
 & \left. \left( 4 A \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right) \\
 & \quad \left( 2 \left( (-3+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \quad \quad \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right) \\
 & \quad \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 3 \left( -\frac{1}{3}(3-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \right. \right. \\
 & \quad \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \quad \left. \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \left. \left( (-3+n) \left( -\frac{3}{5}(4-n) \operatorname{AppellF1}\left[\frac{5}{2}, n, 5-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \quad \quad \left. \frac{3}{5} n \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, 4-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + n \left( -\frac{3}{5}(3-n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, \right. \right. \right. \\
 & \quad \quad \left. \left. \left. 4-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right. \right. \\
 & \quad \quad \left. \left. \left. + \frac{3}{5}(1+n) \operatorname{AppellF1}\left[\frac{5}{2}, 2+n, 3-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \right) / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad 2 \left( (-3+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \quad n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \quad \quad \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right)
 \end{aligned}$$

**Problem 77: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c+d x]^3 (b \sec [c+d x])^n (A+B \sec [c+d x]+C \sec [c+d x]^2) d x$$

Optimal (type 5, 208 leaves, 7 steps):

$$\begin{aligned} & - \left( \left( b^4 (A(2-n) + C(3-n)) \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{4-n}{2}, \frac{6-n}{2}, \cos [c+d x]^2 \right] \right. \right. \\ & \quad \left. \left. (b \sec [c+d x])^{-4+n} \sin [c+d x] \right) / \left( d(2-n)(4-n) \sqrt{\sin [c+d x]^2} \right) \right) - \\ & \left( b^3 B \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3-n}{2}, \frac{5-n}{2}, \cos [c+d x]^2 \right] (b \sec [c+d x])^{-3+n} \sin [c+d x] \right) / \\ & \left( d(3-n) \sqrt{\sin [c+d x]^2} \right) - \frac{b^3 C (b \sec [c+d x])^{-3+n} \tan [c+d x]}{d(2-n)} \end{aligned}$$

Result (type 6, 18886 leaves):

$$\begin{aligned} & - \left( \left( 6 b \sec [c+d x]^{1-n} (b \sec [c+d x])^{-1+n} \left( B \sec [c+d x]^{-2+n} + \right. \right. \right. \\ & \quad \left. \left. \frac{1}{2} A \cos [2(c+d x)] \sec [c+d x]^{-1+n} + \cos [c+d x] \left( \frac{1}{2} A \sec [c+d x]^n + C \sec [c+d x]^n \right) \right) \right. \\ & \quad \left. \tan \left[ \frac{1}{2} (c+d x) \right] \left( \frac{1}{1 - \tan \left[ \frac{1}{2} (c+d x) \right]^2} \right)^n \left( 1 + \tan \left[ \frac{1}{2} (c+d x) \right]^2 \right)^{-4+n} \right. \\ & \quad \left( \left( A \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2 \right] \right. \right. \\ & \quad \left. \left. \left( 1 + \tan \left[ \frac{1}{2} (c+d x) \right]^2 \right)^3 \right) \right) / \\ & \quad \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2 \right] + \right. \\ & \quad \left. 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2 \right] + \right. \right. \\ & \quad \left. \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2 \right] \right) \right. \\ & \quad \left. \tan \left[ \frac{1}{2} (c+d x) \right]^2 \right) - \left( B \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, \right. \right. \\ & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+d x) \right]^2 \right] \left( 1 + \tan \left[ \frac{1}{2} (c+d x) \right]^2 \right)^3 \right) / \\ & \quad \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2 \right] + \right. \\ & \quad \left. 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2 \right] + \right. \right. \\ & \quad \left. \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2 \right] \right) \right) \end{aligned}$$

$$\begin{aligned}
& \tan\left[\frac{1}{2}(c+dx)\right]^2 + \left(C \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2\right], \right. \\
& \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^3 \Big/ \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
& \tan\left[\frac{1}{2}(c+dx)\right]^2 - \left(6A \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \right) \Big/ \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& 2 \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
& \tan\left[\frac{1}{2}(c+dx)\right]^2 + \left(4B \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \right) \Big/ \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& 2 \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
& \tan\left[\frac{1}{2}(c+dx)\right]^2 - \left(2C \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \right) \Big/ \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& 2 \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
& \tan\left[\frac{1}{2}(c+dx)\right]^2 + \left(12A \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \Big/ \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right.
\end{aligned}$$

$$\begin{aligned}
 & 2 \left( (-3+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 4-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \\
 & \quad \tan \left[ \frac{1}{2} (c+dx) \right]^2 - \left( 4B \operatorname{AppellF1} \left[ \frac{1}{2}, n, 3-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 3-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + 2 \left( (-3+n) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, n, 4-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + n \operatorname{AppellF1} \left[ \frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. 1+n, 3-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) - \\
 & \left( 8A \operatorname{AppellF1} \left[ \frac{1}{2}, n, 4-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 4-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + 2 \left( (-4+n) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, n, 5-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + n \operatorname{AppellF1} \left[ \frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. 1+n, 4-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \Big) / \\
 & \left( d \left( -6(-4+n) \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right]^2 \left( \frac{1}{1 - \tan \left[ \frac{1}{2} (c+dx) \right]^2} \right)^n \right. \right. \\
 & \quad \left. \left. \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^{-5+n} \left( \left( A \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^3 \right) \right) / \right. \\
 & \quad \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \left. 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \right. \\
 & \quad \left. \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \right) \\
 & \quad \tan \left[ \frac{1}{2} (c+dx) \right]^2 - \left( B \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^3 \right) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \left. 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \right. \\
 & \quad \left. \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
& \tan\left[\frac{1}{2}(c+dx)\right]^2 + \left(C \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2\right], \right. \\
& \quad \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^3 \Big/ \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \quad \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
& \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2\right) - \left(6A \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \right) \Big/ \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2 \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \quad \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
& \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2\right) + \left(4B \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \right) \Big/ \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2 \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \quad \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
& \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2\right) - \left(2C \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \right) \Big/ \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2 \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \quad \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
& \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2\right) + \left(12A \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \Big/ \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right.
\end{aligned}$$



$$\begin{aligned}
 & 2 \left( (-3+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 4-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \\
 & \quad \tan \left[ \frac{1}{2} (c+dx) \right]^2 - \left( 4 B \operatorname{AppellF1} \left[ \frac{1}{2}, n, 3-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 3-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad 2 \left( (-3+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 4-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 - \\
 & \left( 8 A \operatorname{AppellF1} \left[ \frac{1}{2}, n, 4-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 4-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad 2 \left( (-4+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 5-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 4-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) - \\
 & 3 \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \left( \frac{1}{1 - \tan \left[ \frac{1}{2} (c+dx) \right]^2} \right)^n \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^{-4+n} \\
 & \left( \left( A \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \right. \\
 & \quad \left. \left. \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^3 \right) \right) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \\
 & \quad \tan \left[ \frac{1}{2} (c+dx) \right]^2 - \left( B \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^3 \right) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right.
 \end{aligned}$$



$$\begin{aligned}
 & -\tan\left[\frac{1}{2}(c+dx)\right]^2 \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & 2 \left( (-3+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^2 - \left(4 B \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & 2 \left( (-3+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 - \\
 & \left(8 A \operatorname{AppellF1}\left[\frac{1}{2}, n, 4-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 4-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & 2 \left( (-4+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 5-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 4-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Big) - \\
 & 6 n \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left(\frac{1}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}\right)^{1+n} \\
 & \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^{-4+n} \\
 & \left(\left(A \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^3\right) \right) \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right)
 \end{aligned}$$

$$\begin{aligned}
& \tan\left[\frac{1}{2}(c+dx)\right]^2 - \left( B \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^3 \right) / \\
& \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \quad \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
& \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + \left( C \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^3 \right) / \\
& \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \quad \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
& \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \left( 6 A \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \right) / \\
& \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2 \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \quad \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
& \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + \left( 4 B \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \right) / \\
& \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2 \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \quad \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
& \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \left( 2 C \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \right) / \\
& \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right.
\end{aligned}$$

$$\begin{aligned}
 & 2 \left( (-2+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 3-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \\
 & \quad \tan \left[ \frac{1}{2} (c+dx) \right]^2 + \left( 12 A \operatorname{AppellF1} \left[ \frac{1}{2}, n, 3-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 3-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad 2 \left( (-3+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 4-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \\
 & \quad \tan \left[ \frac{1}{2} (c+dx) \right]^2 - \left( 4 B \operatorname{AppellF1} \left[ \frac{1}{2}, n, 3-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 3-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad 2 \left( (-3+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 4-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 - \\
 & \left( 8 A \operatorname{AppellF1} \left[ \frac{1}{2}, n, 4-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 4-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad 2 \left( (-4+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 5-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 4-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) - \\
 & 6 \tan \left[ \frac{1}{2} (c+dx) \right] \left( \frac{1}{1 - \tan \left[ \frac{1}{2} (c+dx) \right]^2} \right)^n \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^{-4+n} \\
 & \left( \left( 3 A \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \right. \\
 & \quad \left. \left. \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^2 \right) \right) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \\
 & \quad \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 - \\
 & \left( 3 B \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^2 \right) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \quad n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \\
 & \quad \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 + \\
 & \left( 3 C \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^2 \right) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \quad n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \\
 & \quad \tan \left[ \frac{1}{2} (c+dx) \right]^2 + \left( A \left( -\frac{1}{3} (1-n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 2-n, \frac{5}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{1}{3} \right. \right. \\
 & \quad \quad \left. \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \right. \\
 & \quad \quad \left. \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^3 \right) \right) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \quad n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \\
 & \quad \tan \left[ \frac{1}{2} (c+dx) \right]^2 - \left( B \left( -\frac{1}{3} (1-n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 2-n, \frac{5}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{1}{3} \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^3 / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^2 + \left( C \left( -\frac{1}{3} (1-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{3} \right. \right. \\
 & \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^3 / \right. \\
 & \left. \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 - \right. \\
 & \left. \left(12 A \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) / \right. \\
 & \left. \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & 2 \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 + \right. \\
 & \left. \left(8 B \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) / \right. \\
 & \left. \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & 2 \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right.
 \end{aligned}$$





$$\begin{aligned}
 & n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & 2 \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Big) + \\
 & \left(12 A \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & 2 \left( (-3+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Big) - \\
 & \left(4 B \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & 2 \left( (-3+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \Big) \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^2 \Big) + \left(12 A \left(-\frac{1}{3}(3-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{3} \right. \right. \\
 & \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & 2 \left( (-3+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^2 - \left(4B \left(-\frac{1}{3}(3-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \right.\right.\right. \\
 & \quad \left.\left.\left.\tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{3}\right.\right.\right. \\
 & \quad \left.\left.\left.\operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right.\right.\right. \\
 & \quad \left.\left.\left.\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right)\left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) / \right. \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left.2 \left((-3+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right.\right. \\
 & \quad \left.\left.\operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right.\right.\right. \\
 & \quad \left.\left.\left.-\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 - \right. \\
 & \left(8A \left(-\frac{1}{3}(4-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 5-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right.\right. \\
 & \quad \left.\left.\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{3}n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 4-n, \frac{5}{2}, \right.\right.\right. \\
 & \quad \left.\left.\left.\tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right)\right) / \right. \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 4-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left.2 \left((-4+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 5-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right.\right. \\
 & \quad \left.\left.\operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 4-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \right. \\
 & \quad \left.\tan\left[\frac{1}{2}(c+dx)\right]^2 - \left(A \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right.\right.\right. \\
 & \quad \left.\left.\left.-\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right)\left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^3 \right. \\
 & \left(2 \left((-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right.\right. \\
 & \quad \left.\left.\operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \right. \\
 & \quad \left.\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 3 \left(-\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \right.\right.\right. \\
 & \quad \left.\left.\left.\tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right.\right.\right. \\
 & \quad \left.\left.\frac{1}{3}n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right.\right. \\
 & \quad \left.\left.\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) + 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( (-1+n) \left( -\frac{3}{5} (2-n) \operatorname{AppellF1} \left[ \frac{5}{2}, n, 3-n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \right. \right. \\
 & \quad \left. \frac{3}{5} n \operatorname{AppellF1} \left[ \frac{5}{2}, 1+n, 2-n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) + n \left( -\frac{3}{5} (1-n) \operatorname{AppellF1} \left[ \frac{5}{2}, 1+n, \right. \right. \\
 & \quad \left. \left. 2-n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \right. \right. \\
 & \quad \left. \left. \frac{1}{2} (c+dx) \right] + \frac{3}{5} (1+n) \operatorname{AppellF1} \left[ \frac{5}{2}, 2+n, 1-n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \Big) \Big) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + 2 \right. \\
 & \quad \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \Big)^2 + \\
 & \left( B \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
 & \quad \left. \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^3 \right. \\
 & \quad \left( 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \right. \\
 & \quad \left. \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \right. \\
 & \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + 3 \left( -\frac{1}{3} (1-n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 2-n, \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \right. \\
 & \quad \left. \frac{1}{3} n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
 & \quad \left. \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) + 2 \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right. \\
 & \quad \left( (-1+n) \left( -\frac{3}{5} (2-n) \operatorname{AppellF1} \left[ \frac{5}{2}, n, 3-n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \right. \right. \\
 & \quad \left. \frac{3}{5} n \operatorname{AppellF1} \left[ \frac{5}{2}, 1+n, 2-n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) + n \left( -\frac{3}{5} (1-n) \operatorname{AppellF1} \left[ \frac{5}{2}, 1+n, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 - n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \\
 & + \frac{3}{5}(1+n) \operatorname{AppellF1}\left[\frac{5}{2}, 2+n, 1-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right] \Big/ \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \right. \\
 & \left. \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 - \\
 & \left( C \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \left. \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^3 \right. \\
 & \left. \left( 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \right. \\
 & \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
 & \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 3 \left( -\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \left. \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right. \\
 & \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \left. \left( (-1+n) \left( -\frac{3}{5}(2-n) \operatorname{AppellF1}\left[\frac{5}{2}, n, 3-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right. \right. \right. \\
 & \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + \right. \\
 & \left. \frac{3}{5} n \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right. \\
 & \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + n \left( -\frac{3}{5}(1-n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, \right. \right. \right. \\
 & \left. \left. 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right. \\
 & \left. \left. + \frac{3}{5}(1+n) \operatorname{AppellF1}\left[\frac{5}{2}, 2+n, 1-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right. \right. \\
 & \left. \left. \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \Big/ \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 + \\
 & \left( 6A \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left. \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right. \\
 & \quad \left( 2 \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \quad \quad \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 3 \left( -\frac{1}{3}(2-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \quad \quad \left. \left. \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \quad \quad \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \left. \left( (-2+n) \left( -\frac{3}{5}(3-n) \operatorname{AppellF1}\left[\frac{5}{2}, n, 4-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \quad \quad \left. \frac{3}{5} n \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, 3-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + n \left( -\frac{3}{5}(2-n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, \right. \right. \\
 & \quad \quad \left. \left. 3-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right. \\
 & \quad \quad \left. \left. \frac{1}{2}(c+dx)\right] + \frac{3}{5}(1+n) \operatorname{AppellF1}\left[\frac{5}{2}, 2+n, 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \Big/ \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \right. \\
 & \quad \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \quad n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \quad \quad \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 - \\
 & \left( 4B \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]\right)^2 \\
 & \left(2 \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 3 \left( -\frac{1}{3} (2-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + \right. \\
 & \quad \left. \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \left( (-2+n) \left( -\frac{3}{5} (3-n) \operatorname{AppellF1}\left[\frac{5}{2}, n, 4-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \frac{3}{5} n \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, 3-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + n \left( -\frac{3}{5} (2-n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, \right. \right. \\
 & \quad \left. \left. 3-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right. \\
 & \quad \left. \left. + \frac{3}{5} (1+n) \operatorname{AppellF1}\left[\frac{5}{2}, 2+n, 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \Big/ \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \right. \\
 & \quad \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \quad \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 + \\
 & \left( 2 C \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left. \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]\right)^2 \right. \\
 & \quad \left( 2 \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \quad \quad \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 3 \left( -\frac{1}{3} (2-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \\
 & \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
 & \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \left( (-2+n) \left( -\frac{3}{5} (3-n) \operatorname{AppellF1}\left[\frac{5}{2}, n, 4-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \quad \left. \frac{3}{5} n \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, 3-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + n \left( -\frac{3}{5} (2-n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, \right. \right. \\
 & \quad \left. \left. 3-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right. \\
 & \quad \left. \left. + \frac{3}{5} (1+n) \operatorname{AppellF1}\left[\frac{5}{2}, 2+n, 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 2-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \right. \\
 & \quad \left( (-2+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 - \\
 & \left( 12 A \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left. \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right. \\
 & \quad \left( 2 \left( (-3+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 3 \left( -\frac{1}{3} (3-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + \right. \\
 & \quad \left. \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \quad \left( (-3+n) \left( -\frac{3}{5} (4-n) \operatorname{AppellF1}\left[\frac{5}{2}, n, 5-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \\
 & \frac{3}{5} n \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, 4-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + n \left(-\frac{3}{5}(3-n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, \right. \right. \\
 & \left. \left. 4-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{3}{5}(1+n) \operatorname{AppellF1}\left[\frac{5}{2}, 2+n, 3-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \right. \\
 & \left. \left(\left(-3+n\right) \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) + \\
 & \left(4 B \operatorname{AppellF1}\left[\frac{1}{2}, n, 3-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \left. \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \right. \\
 & \left. \left(2 \left(\left(-3+n\right) \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \right. \\
 & \left. \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \right. \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 3 \left(-\frac{1}{3}(3-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 4-n, \frac{5}{2}, \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \left. \left. \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 3-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) + 2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \left. \left(\left(-3+n\right) \left(-\frac{3}{5}(4-n) \operatorname{AppellF1}\left[\frac{5}{2}, n, 5-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \left. \left. \frac{3}{5} n \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, 4-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) + n \left(-\frac{3}{5}(3-n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, \right. \right. \right. \\
 & \left. \left. \left. 4-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & \frac{1}{2} (c + d x) + \frac{3}{5} (1 + n) \operatorname{AppellF1}\left[\frac{5}{2}, 2 + n, 3 - n, \frac{7}{2}, \tan\left[\frac{1}{2} (c + d x)\right]^2, \right. \\
 & \left. -\tan\left[\frac{1}{2} (c + d x)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2} (c + d x)\right]^2 \tan\left[\frac{1}{2} (c + d x)\right]^2 \Big) \Big) \Big) \Big) \Big) / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 3 - n, \frac{3}{2}, \tan\left[\frac{1}{2} (c + d x)\right]^2, -\tan\left[\frac{1}{2} (c + d x)\right]^2\right] + 2 \right. \\
 & \left( (-3 + n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 4 - n, \frac{5}{2}, \tan\left[\frac{1}{2} (c + d x)\right]^2, -\tan\left[\frac{1}{2} (c + d x)\right]^2\right] + \right. \\
 & \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1 + n, 3 - n, \frac{5}{2}, \tan\left[\frac{1}{2} (c + d x)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2} (c + d x)\right]^2\right] \right) \tan\left[\frac{1}{2} (c + d x)\right]^2 \Big) + \\
 & \left( 8 A \operatorname{AppellF1}\left[\frac{1}{2}, n, 4 - n, \frac{3}{2}, \tan\left[\frac{1}{2} (c + d x)\right]^2, -\tan\left[\frac{1}{2} (c + d x)\right]^2\right] \right. \\
 & \left( 2 \left( (-4 + n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 5 - n, \frac{5}{2}, \tan\left[\frac{1}{2} (c + d x)\right]^2, -\tan\left[\frac{1}{2} (c + d x)\right]^2\right] + \right. \right. \\
 & \left. \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1 + n, 4 - n, \frac{5}{2}, \tan\left[\frac{1}{2} (c + d x)\right]^2, -\tan\left[\frac{1}{2} (c + d x)\right]^2\right] \right) \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2} (c + d x)\right]^2 \tan\left[\frac{1}{2} (c + d x)\right] + 3 \left( -\frac{1}{3} (4 - n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 5 - n, \frac{5}{2}, \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2} (c + d x)\right]^2, -\tan\left[\frac{1}{2} (c + d x)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2} (c + d x)\right]^2 \tan\left[\frac{1}{2} (c + d x)\right] + \right. \right. \\
 & \left. \left. \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1 + n, 4 - n, \frac{5}{2}, \tan\left[\frac{1}{2} (c + d x)\right]^2, -\tan\left[\frac{1}{2} (c + d x)\right]^2\right] \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2} (c + d x)\right]^2 \tan\left[\frac{1}{2} (c + d x)\right] \right) + 2 \tan\left[\frac{1}{2} (c + d x)\right]^2 \right. \\
 & \left( (-4 + n) \left( -\frac{3}{5} (5 - n) \operatorname{AppellF1}\left[\frac{5}{2}, n, 6 - n, \frac{7}{2}, \tan\left[\frac{1}{2} (c + d x)\right]^2, \right. \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2} (c + d x)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2} (c + d x)\right]^2 \tan\left[\frac{1}{2} (c + d x)\right] + \right. \\
 & \left. \frac{3}{5} n \operatorname{AppellF1}\left[\frac{5}{2}, 1 + n, 5 - n, \frac{7}{2}, \tan\left[\frac{1}{2} (c + d x)\right]^2, -\tan\left[\frac{1}{2} (c + d x)\right]^2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2} (c + d x)\right]^2 \tan\left[\frac{1}{2} (c + d x)\right] \right) + n \left( -\frac{3}{5} (4 - n) \operatorname{AppellF1}\left[\frac{5}{2}, 1 + n, \right. \right. \\
 & \left. \left. 5 - n, \frac{7}{2}, \tan\left[\frac{1}{2} (c + d x)\right]^2, -\tan\left[\frac{1}{2} (c + d x)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2} (c + d x)\right]^2 \tan\left[\frac{1}{2} (c + d x)\right] \right. \\
 & \left. \left. \frac{1}{2} (c + d x) + \frac{3}{5} (1 + n) \operatorname{AppellF1}\left[\frac{5}{2}, 2 + n, 4 - n, \frac{7}{2}, \tan\left[\frac{1}{2} (c + d x)\right]^2, \right. \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2} (c + d x)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2} (c + d x)\right]^2 \tan\left[\frac{1}{2} (c + d x)\right] \right) \Big) \Big) \Big) \Big) \Big) / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 4 - n, \frac{3}{2}, \tan\left[\frac{1}{2} (c + d x)\right]^2, -\tan\left[\frac{1}{2} (c + d x)\right]^2\right] + 2 \right. \\
 & \left( (-4 + n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 5 - n, \frac{5}{2}, \tan\left[\frac{1}{2} (c + d x)\right]^2, -\tan\left[\frac{1}{2} (c + d x)\right]^2\right] + \right. \\
 & \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1 + n, 4 - n, \frac{5}{2}, \tan\left[\frac{1}{2} (c + d x)\right]^2, \right. \right.
 \end{aligned}$$

$$- \operatorname{Tan} \left[ \frac{1}{2} (c + d x)^2 \right] \operatorname{Tan} \left[ \frac{1}{2} (c + d x)^2 \right] \right) \right) \right) \right)$$

**Problem 78: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c + d x]^{5/2} (b \operatorname{Sec}[c + d x])^n (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 5, 223 leaves, 7 steps):

$$\frac{2 C \operatorname{Sec}[c + d x]^{7/2} (b \operatorname{Sec}[c + d x])^n \operatorname{Sin}[c + d x]}{d (7 + 2 n)} +$$

$$\left( 2 (C (5 + 2 n) + A (7 + 2 n)) \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{1}{4} (-3 - 2 n), \frac{1}{4} (1 - 2 n), \operatorname{Cos}[c + d x]^2 \right] \right.$$

$$\left. \operatorname{Sec}[c + d x]^{3/2} (b \operatorname{Sec}[c + d x])^n \operatorname{Sin}[c + d x] \right) / \left( d (3 + 2 n) (7 + 2 n) \sqrt{\operatorname{Sin}[c + d x]^2} \right) +$$

$$\left( 2 B \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{1}{4} (-5 - 2 n), \frac{1}{4} (-1 - 2 n), \operatorname{Cos}[c + d x]^2 \right] \right.$$

$$\left. \operatorname{Sec}[c + d x]^{5/2} (b \operatorname{Sec}[c + d x])^n \operatorname{Sin}[c + d x] \right) / \left( d (5 + 2 n) \sqrt{\operatorname{Sin}[c + d x]^2} \right)$$

Result (type 5, 493 leaves):

$$- \frac{1}{d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x])}$$

$$i^{9/2+n} e^{2 i c - \frac{1}{2} i d (1+2 n) x} \left( \frac{e^{i (c+d x)}}{1 + e^{2 i (c+d x)}} \right)^{\frac{1}{2}+n} (1 + e^{2 i (c+d x)})^{\frac{1}{2}+n}$$

$$\left( \frac{1}{5 + 2 n} A e^{\frac{1}{2} i d (5+2 n) x} \operatorname{Hypergeometric2F1} \left[ \frac{9}{2} + n, \frac{1}{4} (5 + 2 n), \frac{1}{4} (9 + 2 n), -e^{2 i (c+d x)} \right] + \frac{1}{7 + 2 n} \right.$$

$$2 B e^{\frac{1}{2} i (2 c+d (7+2 n) x)} \operatorname{Hypergeometric2F1} \left[ \frac{9}{2} + n, \frac{1}{4} (7 + 2 n), \frac{1}{4} (11 + 2 n), -e^{2 i (c+d x)} \right] +$$

$$e^{2 i c} \left( \frac{1}{9 + 2 n} 2 (A + 2 C) e^{\frac{1}{2} i d (9+2 n) x} \operatorname{Hypergeometric2F1} \left[ \frac{9}{2} + n, \right.$$

$$\left. \frac{1}{4} (9 + 2 n), \frac{1}{4} (13 + 2 n), -e^{2 i (c+d x)} \right] + \frac{1}{11 + 2 n} 2 B e^{\frac{1}{2} i (2 c+d (11+2 n) x)} \right.$$

$$\left. \operatorname{Hypergeometric2F1} \left[ \frac{9}{2} + n, \frac{1}{4} (11 + 2 n), \frac{1}{4} (15 + 2 n), -e^{2 i (c+d x)} \right] + \frac{1}{13 + 2 n} \right.$$

$$\left. A e^{\frac{1}{2} i (4 c+d (13+2 n) x)} \operatorname{Hypergeometric2F1} \left[ \frac{9}{2} + n, \frac{1}{4} (13 + 2 n), \frac{1}{4} (17 + 2 n), -e^{2 i (c+d x)} \right] \right) \right)$$

$$\operatorname{Sec}[c + d x]^{-2-n} (b \operatorname{Sec}[c + d x])^n (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)$$

**Problem 79: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \text{Sec}[c+dx]^{3/2} (b \text{Sec}[c+dx])^n (A+B \text{Sec}[c+dx]+C \text{Sec}[c+dx]^2) dx$$

Optimal (type 5, 223 leaves, 7 steps):

$$\frac{2 C \text{Sec}[c+dx]^{5/2} (b \text{Sec}[c+dx])^n \text{Sin}[c+dx]}{d (5+2n)} +$$

$$\left( 2 (C (3+2n) + A (5+2n)) \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{4}(-1-2n), \frac{1}{4}(3-2n), \text{Cos}[c+dx]^2\right] \right.$$

$$\left. \sqrt{\text{Sec}[c+dx]} (b \text{Sec}[c+dx])^n \text{Sin}[c+dx] \right) / \left( d (1+2n) (5+2n) \sqrt{\text{Sin}[c+dx]^2} \right) +$$

$$\left( 2 B \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{4}(-3-2n), \frac{1}{4}(1-2n), \text{Cos}[c+dx]^2\right] \text{Sec}[c+dx]^{3/2} \right.$$

$$\left. (b \text{Sec}[c+dx])^n \text{Sin}[c+dx] \right) / \left( d (3+2n) \sqrt{\text{Sin}[c+dx]^2} \right)$$

Result (type 5, 487 leaves):

$$\frac{1}{d (A+2C+2B \text{Cos}[c+dx]+A \text{Cos}[2c+2dx])}$$

$$i^{2n} 2^{7/2+n} e^{-\frac{1}{2} i d (3+2n) x} \left( \frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}} \right)^{\frac{3}{2}+n} (1+e^{2i(c+dx)})^{\frac{3}{2}+n}$$

$$\left( \frac{1}{3+2n} A e^{\frac{1}{2} i d (3+2n) x} \text{Hypergeometric2F1}\left[\frac{7}{2}+n, \frac{1}{4}(3+2n), \frac{1}{4}(7+2n), -e^{2i(c+dx)}\right] + \frac{1}{5+2n} \right.$$

$$2 B e^{\frac{1}{2} i (2c+d(5+2n)x)} \text{Hypergeometric2F1}\left[\frac{7}{2}+n, \frac{1}{4}(5+2n), \frac{1}{4}(9+2n), -e^{2i(c+dx)}\right] +$$

$$e^{2ic} \left( \frac{1}{7+2n} 2 (A+2C) e^{\frac{1}{2} i d (7+2n) x} \text{Hypergeometric2F1}\left[\frac{7}{2}+n, \right.$$

$$\left. \frac{1}{4}(7+2n), \frac{1}{4}(11+2n), -e^{2i(c+dx)}\right] + \frac{1}{9+2n} 2 B e^{\frac{1}{2} i (2c+d(9+2n)x)} \right.$$

$$\left. \text{Hypergeometric2F1}\left[\frac{7}{2}+n, \frac{1}{4}(9+2n), \frac{1}{4}(13+2n), -e^{2i(c+dx)}\right] + \frac{1}{11+2n} \right.$$

$$\left. \left. A e^{\frac{1}{2} i (4c+d(11+2n)x)} \text{Hypergeometric2F1}\left[\frac{7}{2}+n, \frac{1}{4}(11+2n), \frac{1}{4}(15+2n), -e^{2i(c+dx)}\right] \right) \right)$$

$$\text{Sec}[c+dx]^{-2-n} (b \text{Sec}[c+dx])^n (A+B \text{Sec}[c+dx]+C \text{Sec}[c+dx]^2)$$

**Problem 80: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \sqrt{\text{Sec}[c+dx]} (b \text{Sec}[c+dx])^n (A+B \text{Sec}[c+dx]+C \text{Sec}[c+dx]^2) dx$$

Optimal (type 5, 221 leaves, 7 steps):

$$\frac{2 C \operatorname{Sec}[c+d x]^{3/2} (b \operatorname{Sec}[c+d x])^n \operatorname{Sin}[c+d x]}{d(3+2 n)} -$$

$$\left( 2 (C+2 C n+A(3+2 n)) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{4}(1-2 n), \frac{1}{4}(5-2 n), \operatorname{Cos}[c+d x]^2\right] \right.$$

$$\left. (b \operatorname{Sec}[c+d x])^n \operatorname{Sin}[c+d x] \right) / \left( d(1-2 n)(3+2 n) \sqrt{\operatorname{Sec}[c+d x]} \sqrt{\operatorname{Sin}[c+d x]^2} \right) +$$

$$\left( 2 B \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{4}(-1-2 n), \frac{1}{4}(3-2 n), \operatorname{Cos}[c+d x]^2\right] \sqrt{\operatorname{Sec}[c+d x]} \right.$$

$$\left. (b \operatorname{Sec}[c+d x])^n \operatorname{Sin}[c+d x] \right) / \left( d(1+2 n) \sqrt{\operatorname{Sin}[c+d x]^2} \right)$$

Result (type 5, 492 leaves):

$$-\frac{1}{A+2 C+2 B \operatorname{Cos}[c+d x]+A \operatorname{Cos}[2 c+2 d x]} i 2^{\frac{5}{2}+n} e^{-\frac{1}{2} i d(1+2 n) x} \left( \frac{e^{i(c+d x)}}{1+e^{2 i(c+d x)}} \right)^{\frac{1}{2}+n} \left( 1+e^{2 i(c+d x)} \right)^{\frac{1}{2}+n}$$

$$\left( \frac{1}{d+2 d n} A e^{\frac{1}{2} i(d+2 d n) x} \operatorname{Hypergeometric2F1}\left[\frac{5}{2}+n, \frac{1}{4}(1+2 n), \frac{1}{4}(5+2 n), -e^{2 i(c+d x)}\right] + \frac{1}{d} \right.$$

$$e^{i c} \left( \frac{1}{3+2 n} 2 B e^{\frac{1}{2} i d(3+2 n) x} \operatorname{Hypergeometric2F1}\left[\frac{5}{2}+n, \frac{1}{4}(3+2 n), \frac{1}{4}(7+2 n), -e^{2 i(c+d x)}\right] + \right.$$

$$e^{i c} \left( \frac{1}{5+2 n} 2(A+2 C) e^{\frac{1}{2} i d(5+2 n) x} \operatorname{Hypergeometric2F1}\left[\frac{5}{2}+n, \right.$$

$$\left. \frac{1}{4}(5+2 n), \frac{1}{4}(9+2 n), -e^{2 i(c+d x)}\right] + \frac{1}{7+2 n} 2 B e^{\frac{1}{2} i(2 c+d(7+2 n) x)} \right.$$

$$\left. \operatorname{Hypergeometric2F1}\left[\frac{5}{2}+n, \frac{1}{4}(7+2 n), \frac{1}{4}(11+2 n), -e^{2 i(c+d x)}\right] + \frac{1}{9+2 n} \right.$$

$$\left. \left. A e^{\frac{1}{2} i(4 c+d(9+2 n) x)} \operatorname{Hypergeometric2F1}\left[\frac{5}{2}+n, \frac{1}{4}(9+2 n), \frac{1}{4}(13+2 n), -e^{2 i(c+d x)}\right] \right) \right) \right)$$

$$\operatorname{Sec}[c+d x]^{-2-n} (b \operatorname{Sec}[c+d x])^n (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2)$$

**Problem 81: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(b \operatorname{Sec}[c+d x])^n (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2)}{\sqrt{\operatorname{Sec}[c+d x]}} dx$$

Optimal (type 5, 222 leaves, 7 steps):

$$\frac{2 C \sqrt{\operatorname{Sec}[c+d x]} (b \operatorname{Sec}[c+d x])^n \operatorname{Sin}[c+d x]}{d(1+2 n)} -$$

$$\left( 2 (A-C(1-2 n)+2 A n) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{4}(3-2 n), \frac{1}{4}(7-2 n), \operatorname{Cos}[c+d x]^2\right] \right.$$

$$\left. (b \operatorname{Sec}[c+d x])^n \operatorname{Sin}[c+d x] \right) / \left( d(3-2 n)(1+2 n) \operatorname{Sec}[c+d x]^{3/2} \sqrt{\operatorname{Sin}[c+d x]^2} \right) -$$

$$\left( 2 B \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{4}(1-2 n), \frac{1}{4}(5-2 n), \operatorname{Cos}[c+d x]^2\right] (b \operatorname{Sec}[c+d x])^n \right.$$

$$\left. \operatorname{Sin}[c+d x] \right) / \left( d(1-2 n) \sqrt{\operatorname{Sec}[c+d x]} \sqrt{\operatorname{Sin}[c+d x]^2} \right)$$

Result (type 5, 548 leaves):

$$\begin{aligned}
 & - \left( \left( i 2^{\frac{3}{2}+n} e^{-\frac{1}{2} i (2c+d(1+2n)x)} \left( \frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}} \right)^{\frac{1}{2}+n} \right. \right. \\
 & \quad \left. \left( 1+e^{2i(c+dx)} \right)^{\frac{1}{2}+n} \left( A e^{\frac{1}{2} i d (-1+2n)x} (105+352n+344n^2+128n^3+16n^4) \right. \right. \\
 & \quad \text{Hypergeometric2F1} \left[ \frac{3}{2}+n, \frac{1}{4}(-1+2n), \frac{1}{4}(3+2n), -e^{2i(c+dx)} \right] + \\
 & \quad e^{i c} (-1+2n) \left( 2 B e^{\frac{1}{2} i d (1+2n)x} (105+142n+60n^2+8n^3) \text{Hypergeometric2F1} \left[ \right. \right. \\
 & \quad \quad \left. \left. \frac{3}{2}+n, \frac{1}{4}(1+2n), \frac{1}{4}(5+2n), -e^{2i(c+dx)} \right] + e^{\frac{1}{2} i (2c+d(3+2n)x)} (1+2n) \right. \\
 & \quad \left. \left( 2(A+2C)(35+24n+4n^2) \text{Hypergeometric2F1} \left[ \frac{3}{2}+n, \frac{1}{4}(3+2n), \frac{1}{4} \right. \right. \right. \\
 & \quad \quad \left. \left. (7+2n), -e^{2i(c+dx)} \right] + e^{i(c+dx)} (3+2n) \left( 2B(7+2n) \right. \right. \\
 & \quad \quad \left. \left. \text{Hypergeometric2F1} \left[ \frac{3}{2}+n, \frac{1}{4}(5+2n), \frac{1}{4}(9+2n), -e^{2i(c+dx)} \right] + A e^{i(c+dx)} \right. \right. \\
 & \quad \quad \left. \left. (5+2n) \text{Hypergeometric2F1} \left[ \frac{3}{2}+n, \frac{1}{4}(7+2n), \frac{1}{4}(11+2n), -e^{2i(c+dx)} \right] \right) \right) \right) \\
 & \quad \left. \text{Sec}[c+dx]^{-2-n} (b \text{Sec}[c+dx])^n (A+B \text{Sec}[c+dx]+C \text{Sec}[c+dx]^2) \right) / (d \\
 & \quad (-1+2n) \\
 & \quad (1+2n) \\
 & \quad (3+2n) \\
 & \quad (5+2n) \\
 & \quad (7+2n) \\
 & \quad \left. (A+2C+2B \text{Cos}[c+dx]+A \text{Cos}[2c+2dx]) \right)
 \end{aligned}$$

**Problem 82: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(b \text{Sec}[c+dx])^n (A+B \text{Sec}[c+dx]+C \text{Sec}[c+dx]^2)}{\text{Sec}[c+dx]^{3/2}} dx$$

Optimal (type 5, 221 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{2 C (b \operatorname{Sec}[c+d x])^n \operatorname{Sin}[c+d x]}{d (1-2 n) \sqrt{\operatorname{Sec}[c+d x]}} - \\
 & \left( 2 (A+C (3-2 n) - 2 A n) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{4} (5-2 n), \frac{1}{4} (9-2 n), \operatorname{Cos}[c+d x]^2\right] \right. \\
 & \quad \left. (b \operatorname{Sec}[c+d x])^n \operatorname{Sin}[c+d x] \right) / \left( d (1-2 n) (5-2 n) \operatorname{Sec}[c+d x]^{5/2} \sqrt{\operatorname{Sin}[c+d x]^2} \right) - \\
 & \left( 2 B \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{4} (3-2 n), \frac{1}{4} (7-2 n), \operatorname{Cos}[c+d x]^2\right] (b \operatorname{Sec}[c+d x])^n \right. \\
 & \quad \left. \operatorname{Sin}[c+d x] \right) / \left( d (3-2 n) \operatorname{Sec}[c+d x]^{3/2} \sqrt{\operatorname{Sin}[c+d x]^2} \right)
 \end{aligned}$$

Result (type 5, 502 leaves):

$$\begin{aligned}
 & - \frac{1}{A+2 C+2 B \operatorname{Cos}[c+d x]+A \operatorname{Cos}[2 c+2 d x]} \\
 & \frac{i 2^{\frac{1}{2}+n} e^{-\frac{1}{2} i (4 c+d (1+2 n) x)} \left( \frac{e^{i (c+d x)}}{1+e^{2 i (c+d x)}} \right)^{\frac{1}{2}+n} \left( 1+e^{2 i (c+d x)} \right)^{\frac{1}{2}+n}}{\left( \frac{1}{d (-3+2 n)} A e^{\frac{1}{2} i d (-3+2 n) x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}+n, \frac{1}{4} (-3+2 n), \frac{1}{4} (1+2 n), -e^{2 i (c+d x)}\right] + \right.} \\
 & \quad \frac{1}{d (-1+2 n)} 2 B e^{\frac{1}{2} i (2 c+d (-1+2 n) x)} \\
 & \quad \left. \operatorname{Hypergeometric2F1}\left[\frac{1}{2}+n, \frac{1}{4} (-1+2 n), \frac{1}{4} (3+2 n), -e^{2 i (c+d x)}\right] + e^{2 i c} \left( \frac{1}{d+2 d n} \right. \right. \\
 & \quad \left. \left. 2 (A+2 C) e^{\frac{1}{2} i d (1+2 n) x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}+n, \frac{1}{4} (1+2 n), \frac{1}{4} (5+2 n), -e^{2 i (c+d x)}\right] + \right. \right. \\
 & \quad \left. \left. \left( e^{\frac{1}{2} i (2 c+d (3+2 n) x)} \left( 2 B (5+2 n) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}+n, \frac{1}{4} (3+2 n), \frac{1}{4} (7+2 n), \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. -e^{2 i (c+d x)}\right] + A e^{i (c+d x)} (3+2 n) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}+n, \frac{1}{4} (5+2 n), \frac{1}{4} \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. (9+2 n), -e^{2 i (c+d x)}\right] \right) \right) \right) / \left( d (3+2 n) (5+2 n) \right) \right) \\
 & \operatorname{Sec}[c+d x]^{-2-n} (b \operatorname{Sec}[c+d x])^n (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2)
 \end{aligned}$$

**Problem 83: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(b \operatorname{Sec}[c+d x])^n (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2)}{\operatorname{Sec}[c+d x]^{5/2}} dx$$

Optimal (type 5, 223 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{2 C (b \operatorname{Sec}[c+d x])^n \operatorname{Sin}[c+d x]}{d (3-2 n) \operatorname{Sec}[c+d x]^{3/2}} - \\
 & \left( 2 (A (3-2 n) + C (5-2 n)) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{4} (7-2 n), \frac{1}{4} (11-2 n), \operatorname{Cos}[c+d x]^2\right] \right. \\
 & \quad \left. (b \operatorname{Sec}[c+d x])^n \operatorname{Sin}[c+d x] \right) / \left( d (3-2 n) (7-2 n) \operatorname{Sec}[c+d x]^{7/2} \sqrt{\operatorname{Sin}[c+d x]^2} \right) - \\
 & \left( 2 B \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{4} (5-2 n), \frac{1}{4} (9-2 n), \operatorname{Cos}[c+d x]^2\right] (b \operatorname{Sec}[c+d x])^n \right. \\
 & \quad \left. \operatorname{Sin}[c+d x] \right) / \left( d (5-2 n) \operatorname{Sec}[c+d x]^{5/2} \sqrt{\operatorname{Sin}[c+d x]^2} \right)
 \end{aligned}$$

Result (type 5, 502 leaves):

$$\begin{aligned}
 & \frac{1}{A+2 C+2 B \operatorname{Cos}[c+d x]+A \operatorname{Cos}[2 c+2 d x]} \\
 & i 2^{-\frac{1}{2}+n} e^{-\frac{1}{2} i (4 c+d (-1+2 n) x)} \left( \frac{e^{i (c+d x)}}{1+e^{2 i (c+d x)}} \right)^{-\frac{1}{2}+n} \left( 1+e^{2 i (c+d x)} \right)^{-\frac{1}{2}+n} \left( \frac{1}{d (-5+2 n)} A e^{\frac{1}{2} i d (-5+2 n) x} \right. \\
 & \quad \operatorname{Hypergeometric2F1}\left[-\frac{1}{2}+n, \frac{1}{4} (-5+2 n), \frac{1}{4} (-1+2 n), -e^{2 i (c+d x)}\right] + \frac{1}{d (-3+2 n)} \\
 & \quad 2 B e^{\frac{1}{2} i (2 c+d (-3+2 n) x)} \operatorname{Hypergeometric2F1}\left[-\frac{1}{2}+n, \frac{1}{4} (-3+2 n), \frac{1}{4} (1+2 n), -e^{2 i (c+d x)}\right] + \\
 & \quad e^{2 i c} \left( \frac{1}{d (-1+2 n)} 2 (A+2 C) e^{\frac{1}{2} i d (-1+2 n) x} \operatorname{Hypergeometric2F1}\left[-\frac{1}{2}+n, \right. \right. \\
 & \quad \left. \left. \frac{1}{4} (-1+2 n), \frac{1}{4} (3+2 n), -e^{2 i (c+d x)}\right] + \frac{1}{d+2 d n} 2 B e^{\frac{1}{2} i (2 c+d x+2 d n x)} \right. \\
 & \quad \left. \operatorname{Hypergeometric2F1}\left[-\frac{1}{2}+n, \frac{1}{4} (1+2 n), \frac{1}{4} (5+2 n), -e^{2 i (c+d x)}\right] + \frac{1}{d (3+2 n)} \right. \\
 & \quad \left. \left. A e^{\frac{1}{2} i (4 c+d (3+2 n) x)} \operatorname{Hypergeometric2F1}\left[-\frac{1}{2}+n, \frac{1}{4} (3+2 n), \frac{1}{4} (7+2 n), -e^{2 i (c+d x)}\right] \right) \right) \\
 & \operatorname{Sec}[c+d x]^{-2-n} (b \operatorname{Sec}[c+d x])^n (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2)
 \end{aligned}$$

**Problem 84: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c+d x]^3 (a+a \operatorname{Sec}[c+d x]) (A+C \operatorname{Sec}[c+d x]^2) dx$$

Optimal (type 3, 140 leaves, 7 steps):

$$\begin{aligned}
 & \frac{a (4 A+3 C) \operatorname{ArcTanh}[\operatorname{Sin}[c+d x]]}{8 d} + \frac{a (5 A+4 C) \operatorname{Tan}[c+d x]}{5 d} + \\
 & \frac{a (4 A+3 C) \operatorname{Sec}[c+d x] \operatorname{Tan}[c+d x]}{8 d} + \frac{a C \operatorname{Sec}[c+d x]^3 \operatorname{Tan}[c+d x]}{4 d} + \\
 & \frac{a C \operatorname{Sec}[c+d x]^4 \operatorname{Tan}[c+d x]}{5 d} + \frac{a (5 A+4 C) \operatorname{Tan}[c+d x]^3}{15 d}
 \end{aligned}$$

Result (type 3, 426 leaves):

$$\begin{aligned}
& - \frac{a A \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right]}{2d} - \frac{3 a C \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right]}{8d} + \\
& \frac{a A \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right]}{2d} + \frac{3 a C \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right]}{8d} + \\
& \frac{16 d \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^4}{3 a C} + \frac{4 d \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^2}{a A} + \\
& \frac{16 d \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^2}{a A} - \frac{16 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^4}{3 a C} - \\
& \frac{4 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^2}{3 a C} - \frac{16 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^2}{a A} + \\
& \frac{2 a A \operatorname{Tan}[c+dx]}{3d} + \frac{8 a C \operatorname{Tan}[c+dx]}{15d} + \frac{a A \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx]}{3d} + \\
& \frac{4 a C \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx]}{15d} + \frac{a C \operatorname{Sec}[c+dx]^4 \operatorname{Tan}[c+dx]}{5d}
\end{aligned}$$

**Problem 85: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c+dx]^2 (a + a \operatorname{Sec}[c+dx]) (A + C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 3, 117 leaves, 7 steps):

$$\begin{aligned}
& \frac{a (4 A + 3 C) \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{8d} + \frac{a (3 A + 2 C) \operatorname{Tan}[c+dx]}{3d} + \\
& \frac{a (4 A + 3 C) \operatorname{Sec}[c+dx] \operatorname{Tan}[c+dx]}{8d} + \frac{a C \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx]}{3d} + \frac{a C \operatorname{Sec}[c+dx]^3 \operatorname{Tan}[c+dx]}{4d}
\end{aligned}$$

Result (type 3, 377 leaves):

$$\begin{aligned}
& - \frac{a A \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right]}{2d} - \frac{3 a C \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right]}{8d} + \\
& \frac{a A \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right]}{2d} + \frac{3 a C \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right]}{8d} + \\
& \frac{16 d \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^4}{3 a C} + \frac{4 d \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^2}{a A} + \\
& \frac{16 d \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^2}{a A} - \frac{16 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^4}{3 a C} - \\
& \frac{4 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^2}{3 a C} - \frac{16 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^2}{a A} + \\
& \frac{a A \operatorname{Tan}[c+dx]}{d} + \frac{2 a C \operatorname{Tan}[c+dx]}{3d} + \frac{a C \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx]}{3d}
\end{aligned}$$



**Problem 87: Result more than twice size of optimal antiderivative.**

$$\int (a + a \sec [c + d x]) (A + C \sec [c + d x]^2) dx$$

Optimal (type 3, 58 leaves, 5 steps):

$$a A x + \frac{a (2 A + C) \operatorname{ArcTanh}[\sin [c + d x]]}{2 d} + \frac{a C \tan [c + d x]}{d} + \frac{a C \sec [c + d x] \tan [c + d x]}{2 d}$$

Result (type 3, 218 leaves):

$$\begin{aligned} a A x - \frac{a A \operatorname{Log}\left[\cos \left[\frac{c}{2} + \frac{d x}{2}\right] - \sin \left[\frac{c}{2} + \frac{d x}{2}\right]\right]}{d} + \\ \frac{a A \operatorname{Log}\left[\cos \left[\frac{c}{2} + \frac{d x}{2}\right] + \sin \left[\frac{c}{2} + \frac{d x}{2}\right]\right] - a C \operatorname{Log}\left[\cos \left[\frac{1}{2}(c + d x)\right] - \sin \left[\frac{1}{2}(c + d x)\right]\right]}{2 d} + \\ \frac{a C \operatorname{Log}\left[\cos \left[\frac{1}{2}(c + d x)\right] + \sin \left[\frac{1}{2}(c + d x)\right]\right]}{2 d} + \frac{a C}{4 d \left(\cos \left[\frac{1}{2}(c + d x)\right] - \sin \left[\frac{1}{2}(c + d x)\right]\right)^2} - \\ \frac{a C}{4 d \left(\cos \left[\frac{1}{2}(c + d x)\right] + \sin \left[\frac{1}{2}(c + d x)\right]\right)^2} + \frac{a C \tan [c + d x]}{d} \end{aligned}$$

**Problem 88: Result more than twice size of optimal antiderivative.**

$$\int \cos [c + d x] (a + a \sec [c + d x]) (A + C \sec [c + d x]^2) dx$$

Optimal (type 3, 42 leaves, 5 steps):

$$a A x + \frac{a C \operatorname{ArcTanh}[\sin [c + d x]]}{d} + \frac{a A \sin [c + d x]}{d} + \frac{a C \tan [c + d x]}{d}$$

Result (type 3, 112 leaves):

$$\begin{aligned} a A x - \frac{a C \operatorname{Log}\left[\cos \left[\frac{c}{2} + \frac{d x}{2}\right] - \sin \left[\frac{c}{2} + \frac{d x}{2}\right]\right]}{d} + \frac{a C \operatorname{Log}\left[\cos \left[\frac{c}{2} + \frac{d x}{2}\right] + \sin \left[\frac{c}{2} + \frac{d x}{2}\right]\right]}{d} + \\ \frac{a A \cos [d x] \sin [c]}{d} + \frac{a A \cos [c] \sin [d x]}{d} + \frac{a C \tan [c + d x]}{d} \end{aligned}$$

**Problem 94: Result more than twice size of optimal antiderivative.**

$$\int \sec [c + d x] (a + a \sec [c + d x])^2 (A + C \sec [c + d x]^2) dx$$

Optimal (type 3, 132 leaves, 7 steps):

$$\frac{a^2 (12 A + 7 C) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{8 d} + \frac{a^2 (12 A + 7 C) \operatorname{Tan}[c + d x]}{6 d} + \frac{a^2 (12 A + 7 C) \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x]}{24 d} - \frac{C (a + a \operatorname{Sec}[c + d x])^2 \operatorname{Tan}[c + d x]}{12 d} + \frac{C (a + a \operatorname{Sec}[c + d x])^3 \operatorname{Tan}[c + d x]}{4 a d}$$

Result (type 3, 291 leaves):

$$-\frac{1}{384 d (A + 2 C + A \operatorname{Cos}[2 (c + d x)])} a^2 (1 + \operatorname{Cos}[c + d x])^2 \left( (C + A \operatorname{Cos}[c + d x]^2) \operatorname{Sec}\left[\frac{1}{2} (c + d x)\right]^4 \operatorname{Sec}[c + d x]^4 \left( 24 (12 A + 7 C) \operatorname{Cos}[c + d x]^4 \left( \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2} (c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]\right] - \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2} (c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]\right] \right) - \operatorname{Sec}[c] \left( -48 (3 A + 2 C) \operatorname{Sin}[c] + 3 (4 A + 15 C) \operatorname{Sin}[d x] + 12 A \operatorname{Sin}[2 c + d x] + 45 C \operatorname{Sin}[2 c + d x] + 144 A \operatorname{Sin}[c + 2 d x] + 128 C \operatorname{Sin}[c + 2 d x] - 48 A \operatorname{Sin}[3 c + 2 d x] + 12 A \operatorname{Sin}[2 c + 3 d x] + 21 C \operatorname{Sin}[2 c + 3 d x] + 12 A \operatorname{Sin}[4 c + 3 d x] + 21 C \operatorname{Sin}[4 c + 3 d x] + 48 A \operatorname{Sin}[3 c + 4 d x] + 32 C \operatorname{Sin}[3 c + 4 d x] \right) \right)$$

**Problem 95: Result more than twice size of optimal antiderivative.**

$$\int (a + a \operatorname{Sec}[c + d x])^2 (A + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 3, 96 leaves, 6 steps):

$$a^2 A x + \frac{a^2 (2 A + C) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{d} + \frac{a^2 (A + C) \operatorname{Tan}[c + d x]}{d} + \frac{C (a + a \operatorname{Sec}[c + d x])^2 \operatorname{Tan}[c + d x]}{3 d} + \frac{C (a^2 + a^2 \operatorname{Sec}[c + d x]) \operatorname{Tan}[c + d x]}{3 d}$$

Result (type 3, 1090 leaves):

$$\begin{aligned}
 & \left( A x \cos [c + d x]^4 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a + a \sec [c + d x])^2 (A + C \sec [c + d x]^2) \right) / \\
 & \left( 2 (A + 2 C + A \cos [2 c + 2 d x]) \right) + \\
 & \left( (-2 A - C) \cos [c + d x]^4 \log \left[ \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \right. \\
 & \left. (a + a \sec [c + d x])^2 (A + C \sec [c + d x]^2) \right) / \left( 2 d (A + 2 C + A \cos [2 c + 2 d x]) \right) + \\
 & \left( (2 A + C) \cos [c + d x]^4 \log \left[ \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \right. \\
 & \left. (a + a \sec [c + d x])^2 (A + C \sec [c + d x]^2) \right) / \left( 2 d (A + 2 C + A \cos [2 c + 2 d x]) \right) + \\
 & \left( C \cos [c + d x]^4 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a + a \sec [c + d x])^2 (A + C \sec [c + d x]^2) \sin \left[ \frac{d x}{2} \right] \right) / \\
 & \left( 12 d (A + 2 C + A \cos [2 c + 2 d x]) \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right)^3 \right) + \\
 & \left( \cos [c + d x]^4 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a + a \sec [c + d x])^2 (A + C \sec [c + d x]^2) \left( 7 C \cos \left[ \frac{c}{2} \right] - 5 C \sin \left[ \frac{c}{2} \right] \right) \right) / \\
 & \left( 24 d (A + 2 C + A \cos [2 c + 2 d x]) \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right)^2 \right) + \\
 & \left( \cos [c + d x]^4 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a + a \sec [c + d x])^2 \right. \\
 & \left. (A + C \sec [c + d x]^2) \left( 3 A \sin \left[ \frac{d x}{2} \right] + 5 C \sin \left[ \frac{d x}{2} \right] \right) \right) / \\
 & \left( 6 d (A + 2 C + A \cos [2 c + 2 d x]) \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right) \right) + \\
 & \left( C \cos [c + d x]^4 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a + a \sec [c + d x])^2 (A + C \sec [c + d x]^2) \sin \left[ \frac{d x}{2} \right] \right) / \\
 & \left( 12 d (A + 2 C + A \cos [2 c + 2 d x]) \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right)^3 \right) + \\
 & \left( \cos [c + d x]^4 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a + a \sec [c + d x])^2 \right. \\
 & \left. (A + C \sec [c + d x]^2) \left( -7 C \cos \left[ \frac{c}{2} \right] - 5 C \sin \left[ \frac{c}{2} \right] \right) \right) / \\
 & \left( 24 d (A + 2 C + A \cos [2 c + 2 d x]) \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right)^2 \right) + \\
 & \left( \cos [c + d x]^4 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a + a \sec [c + d x])^2 \right. \\
 & \left. (A + C \sec [c + d x]^2) \left( 3 A \sin \left[ \frac{d x}{2} \right] + 5 C \sin \left[ \frac{d x}{2} \right] \right) \right) / \\
 & \left( 6 d (A + 2 C + A \cos [2 c + 2 d x]) \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right) \right)
 \end{aligned}$$

**Problem 96: Result more than twice size of optimal antiderivative.**

$$\int \cos [c + d x] (a + a \sec [c + d x])^2 (A + C \sec [c + d x]^2) dx$$

Optimal (type 3, 112 leaves, 6 steps):

$$2 a^2 A x + \frac{a^2 (2 A + 3 C) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{2 d} + \frac{A (a + a \operatorname{Sec}[c + d x])^2 \operatorname{Sin}[c + d x]}{d} - \frac{a^2 (2 A - 3 C) \operatorname{Tan}[c + d x]}{2 d} - \frac{(2 A - C) (a^2 + a^2 \operatorname{Sec}[c + d x]) \operatorname{Tan}[c + d x]}{2 d}$$

Result (type 3, 330 leaves):

$$\frac{1}{8 (A + 2 C + A \operatorname{Cos}[2 (c + d x)])} a^2 \operatorname{Cos}[c + d x]^4 \operatorname{Sec}\left[\frac{1}{2} (c + d x)\right]^4 (1 + \operatorname{Sec}[c + d x])^2$$

$$(A + C \operatorname{Sec}[c + d x]^2) \left( 8 A x - \frac{2 (2 A + 3 C) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2} (c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]\right]}{d} + \frac{2 (2 A + 3 C) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2} (c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]\right]}{d} + \frac{4 A \operatorname{Cos}[d x] \operatorname{Sin}[c]}{d} + \frac{4 A \operatorname{Cos}[c] \operatorname{Sin}[d x]}{d} + \frac{C}{d \left(\operatorname{Cos}\left[\frac{1}{2} (c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]\right)^2} + \frac{8 C \operatorname{Sin}\left[\frac{d x}{2}\right]}{d \left(\operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right]\right) \left(\operatorname{Cos}\left[\frac{1}{2} (c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]\right)} - \frac{8 C \operatorname{Sin}\left[\frac{d x}{2}\right]}{d \left(\operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right]\right) \left(\operatorname{Cos}\left[\frac{1}{2} (c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]\right)} \right)$$

**Problem 97: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Cos}[c + d x]^2 (a + a \operatorname{Sec}[c + d x])^2 (A + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 3, 119 leaves, 5 steps):

$$\frac{1}{2} a^2 (3 A + 2 C) x + \frac{2 a^2 C \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{d} + \frac{a^2 (3 A - 2 C) \operatorname{Sin}[c + d x]}{2 d} + \frac{A \operatorname{Cos}[c + d x] (a + a \operatorname{Sec}[c + d x])^2 \operatorname{Sin}[c + d x]}{2 d} - \frac{(A - 2 C) (a^2 + a^2 \operatorname{Sec}[c + d x]) \operatorname{Sin}[c + d x]}{2 d}$$

Result (type 3, 292 leaves):

$$\begin{aligned}
 & - \left( \left( a^2 \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right] \right)^2 \left( 4 \operatorname{Cos} [d x] \left( 3 A d x + 2 C d x - 4 C \operatorname{Log} \left[ \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] \right] \right) + \right. \\
 & \quad \left. 4 C \operatorname{Log} \left[ \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] \right] \right) + \\
 & \quad 4 \operatorname{Cos} [2 c + d x] \left( 3 A d x + 2 C d x - 4 C \operatorname{Log} \left[ \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] \right] \right) + \\
 & \quad \left. 4 C \operatorname{Log} \left[ \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] \right] \right) + A \operatorname{Sin} [d x] + \\
 & \quad 16 C \operatorname{Sin} [d x] + A \operatorname{Sin} [2 c + d x] + 8 A \operatorname{Sin} [c + 2 d x] + 8 A \operatorname{Sin} [3 c + 2 d x] + \\
 & \quad \left. A \operatorname{Sin} [2 c + 3 d x] + A \operatorname{Sin} [4 c + 3 d x] \right) \Bigg) / \\
 & \left( 16 d \left( \operatorname{Cos} \left[ \frac{c}{2} \right] - \operatorname{Sin} \left[ \frac{c}{2} \right] \right) \left( \operatorname{Cos} \left[ \frac{c}{2} \right] + \operatorname{Sin} \left[ \frac{c}{2} \right] \right) \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right) \right. \\
 & \quad \left. \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right) \right)
 \end{aligned}$$

### Problem 103: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Sec} [c + d x] (a + a \operatorname{Sec} [c + d x])^3 (A + C \operatorname{Sec} [c + d x]^2) dx$$

Optimal (type 3, 157 leaves, 11 steps):

$$\begin{aligned}
 & \frac{a^3 (20 A + 13 C) \operatorname{ArcTanh} [\operatorname{Sin} [c + d x]]}{8 d} + \frac{a^3 (20 A + 13 C) \operatorname{Tan} [c + d x]}{5 d} + \\
 & \frac{3 a^3 (20 A + 13 C) \operatorname{Sec} [c + d x] \operatorname{Tan} [c + d x]}{40 d} - \frac{C (a + a \operatorname{Sec} [c + d x])^3 \operatorname{Tan} [c + d x]}{20 d} + \\
 & \frac{C (a + a \operatorname{Sec} [c + d x])^4 \operatorname{Tan} [c + d x]}{5 a d} + \frac{a^3 (20 A + 13 C) \operatorname{Tan} [c + d x]^3}{60 d}
 \end{aligned}$$

Result (type 3, 323 leaves):

$$\begin{aligned}
 & - \frac{1}{7680 d (A + 2 C + A \operatorname{Cos} [2 (c + d x)])} a^3 (1 + \operatorname{Cos} [c + d x])^3 \\
 & \quad (C + A \operatorname{Cos} [c + d x]^2) \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^6 \operatorname{Sec} [c + d x]^5 \left( 240 (20 A + 13 C) \operatorname{Cos} [c + d x]^5 \right. \\
 & \quad \left. \left( \operatorname{Log} \left[ \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] \right] - \operatorname{Log} \left[ \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] \right] \right) - \right. \\
 & \quad \left. \operatorname{Sec} [c] (80 (34 A + 29 C) \operatorname{Sin} [d x] - 240 (7 A + 3 C) \operatorname{Sin} [2 c + d x] + 360 A \operatorname{Sin} [c + 2 d x] + \right. \\
 & \quad \left. 750 C \operatorname{Sin} [c + 2 d x] + 360 A \operatorname{Sin} [3 c + 2 d x] + 750 C \operatorname{Sin} [3 c + 2 d x] + 1840 A \operatorname{Sin} [2 c + 3 d x] + \right. \\
 & \quad \left. 1520 C \operatorname{Sin} [2 c + 3 d x] - 360 A \operatorname{Sin} [4 c + 3 d x] + 180 A \operatorname{Sin} [3 c + 4 d x] + 195 C \operatorname{Sin} [3 c + 4 d x] + \right. \\
 & \quad \left. 180 A \operatorname{Sin} [5 c + 4 d x] + 195 C \operatorname{Sin} [5 c + 4 d x] + 440 A \operatorname{Sin} [4 c + 5 d x] + 304 C \operatorname{Sin} [4 c + 5 d x] \right) \Bigg)
 \end{aligned}$$

### Problem 104: Result more than twice size of optimal antiderivative.

$$\int (a + a \operatorname{Sec} [c + d x])^3 (A + C \operatorname{Sec} [c + d x]^2) dx$$

Optimal (type 3, 147 leaves, 7 steps):

$$a^3 A x + \frac{a^3 (28 A + 15 C) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{8 d} + \frac{5 a^3 (4 A + 3 C) \operatorname{Tan}[c + d x]}{8 d} + \frac{C (a + a \operatorname{Sec}[c + d x])^3 \operatorname{Tan}[c + d x]}{4 d} + \frac{C (a^2 + a^2 \operatorname{Sec}[c + d x])^2 \operatorname{Tan}[c + d x]}{4 a d} + \frac{(4 A + 5 C) (a^3 + a^3 \operatorname{Sec}[c + d x]) \operatorname{Tan}[c + d x]}{8 d}$$

Result (type 3, 363 leaves):

$$\frac{1}{256 d (A + 2 C + A \operatorname{Cos}[2 (c + d x)])} a^3 (1 + \operatorname{Cos}[c + d x])^3 (C + A \operatorname{Cos}[c + d x]^2) \operatorname{Sec}\left[\frac{1}{2} (c + d x)\right]^6 \operatorname{Sec}[c + d x]^4 \left(-8 (28 A + 15 C) \operatorname{Cos}[c + d x]^4 \left(\operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2} (c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]\right] - \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2} (c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]\right]\right) + \operatorname{Sec}[c] (24 A d x \operatorname{Cos}[c] + 16 A d x \operatorname{Cos}[c + 2 d x] + 16 A d x \operatorname{Cos}[3 c + 2 d x] + 4 A d x \operatorname{Cos}[3 c + 4 d x] + 4 A d x \operatorname{Cos}[5 c + 4 d x] - 72 A \operatorname{Sin}[c] - 72 C \operatorname{Sin}[c] + 4 A \operatorname{Sin}[d x] + 23 C \operatorname{Sin}[d x] + 4 A \operatorname{Sin}[2 c + d x] + 23 C \operatorname{Sin}[2 c + d x] + 72 A \operatorname{Sin}[c + 2 d x] + 88 C \operatorname{Sin}[c + 2 d x] - 24 A \operatorname{Sin}[3 c + 2 d x] - 8 C \operatorname{Sin}[3 c + 2 d x] + 4 A \operatorname{Sin}[2 c + 3 d x] + 15 C \operatorname{Sin}[2 c + 3 d x] + 4 A \operatorname{Sin}[4 c + 3 d x] + 15 C \operatorname{Sin}[4 c + 3 d x] + 24 A \operatorname{Sin}[3 c + 4 d x] + 24 C \operatorname{Sin}[3 c + 4 d x])\right)$$

### Problem 105: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cos}[c + d x] (a + a \operatorname{Sec}[c + d x])^3 (A + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 3, 145 leaves, 7 steps):

$$3 a^3 A x + \frac{a^3 (6 A + 5 C) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{2 d} + \frac{A (a + a \operatorname{Sec}[c + d x])^3 \operatorname{Sin}[c + d x]}{d} + \frac{5 a^3 C \operatorname{Tan}[c + d x]}{2 d} - \frac{(3 A - C) (a^2 + a^2 \operatorname{Sec}[c + d x])^2 \operatorname{Tan}[c + d x]}{3 a d} - \frac{(6 A - 5 C) (a^3 + a^3 \operatorname{Sec}[c + d x]) \operatorname{Tan}[c + d x]}{6 d}$$

Result (type 3, 1250 leaves):

$$\left(3 A x \operatorname{Cos}[c + d x]^5 \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \operatorname{Sec}[c + d x])^3 (A + C \operatorname{Sec}[c + d x]^2)\right) / \left(4 (A + 2 C + A \operatorname{Cos}[2 c + 2 d x])\right) + \left((-6 A - 5 C) \operatorname{Cos}[c + d x]^5 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right] - \operatorname{Sin}\left[\frac{c}{2} + \frac{d x}{2}\right]\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \operatorname{Sec}[c + d x])^3 (A + C \operatorname{Sec}[c + d x]^2)\right) / \left(8 d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x])\right) + \left((6 A + 5 C) \operatorname{Cos}[c + d x]^5 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{d x}{2}\right]\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \operatorname{Sec}[c + d x])^3 (A + C \operatorname{Sec}[c + d x]^2)\right) / \left(8 d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x])\right)$$

$$\begin{aligned}
 & \left. (a + a \operatorname{Sec}[c + d x])^3 (A + C \operatorname{Sec}[c + d x]^2) \right) / (8 d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x])) + \\
 & \left( A \operatorname{Cos}[d x] \operatorname{Cos}[c + d x]^5 \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \operatorname{Sec}[c + d x])^3 (A + C \operatorname{Sec}[c + d x]^2) \operatorname{Sin}[c] \right) / \\
 & (4 d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x])) + \\
 & \left( A \operatorname{Cos}[c] \operatorname{Cos}[c + d x]^5 \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \operatorname{Sec}[c + d x])^3 (A + C \operatorname{Sec}[c + d x]^2) \operatorname{Sin}[d x] \right) / \\
 & (4 d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x])) + \\
 & \left( C \operatorname{Cos}[c + d x]^5 \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \operatorname{Sec}[c + d x])^3 (A + C \operatorname{Sec}[c + d x]^2) \operatorname{Sin}\left[\frac{d x}{2}\right] \right) / \\
 & \left( 24 d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) \left( \operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right] - \operatorname{Sin}\left[\frac{c}{2} + \frac{d x}{2}\right] \right)^3 \right) + \\
 & \left( \operatorname{Cos}[c + d x]^5 \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \operatorname{Sec}[c + d x])^3 (A + C \operatorname{Sec}[c + d x]^2) \left( 5 C \operatorname{Cos}\left[\frac{c}{2}\right] - 4 C \operatorname{Sin}\left[\frac{c}{2}\right] \right) \right) / \\
 & \left( 24 d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) \left( \operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right] - \operatorname{Sin}\left[\frac{c}{2} + \frac{d x}{2}\right] \right)^2 \right) + \\
 & \left( \operatorname{Cos}[c + d x]^5 \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \operatorname{Sec}[c + d x])^3 \right. \\
 & \quad \left. (A + C \operatorname{Sec}[c + d x]^2) \left( 3 A \operatorname{Sin}\left[\frac{d x}{2}\right] + 11 C \operatorname{Sin}\left[\frac{d x}{2}\right] \right) \right) / \\
 & \left( 12 d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) \left( \operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right] - \operatorname{Sin}\left[\frac{c}{2} + \frac{d x}{2}\right] \right) \right) + \\
 & \left( C \operatorname{Cos}[c + d x]^5 \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \operatorname{Sec}[c + d x])^3 (A + C \operatorname{Sec}[c + d x]^2) \operatorname{Sin}\left[\frac{d x}{2}\right] \right) / \\
 & \left( 24 d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) \left( \operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{d x}{2}\right] \right)^3 \right) + \\
 & \left( \operatorname{Cos}[c + d x]^5 \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \operatorname{Sec}[c + d x])^3 \right. \\
 & \quad \left. (A + C \operatorname{Sec}[c + d x]^2) \left( -5 C \operatorname{Cos}\left[\frac{c}{2}\right] - 4 C \operatorname{Sin}\left[\frac{c}{2}\right] \right) \right) / \\
 & \left( 24 d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) \left( \operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{d x}{2}\right] \right)^2 \right) + \\
 & \left( \operatorname{Cos}[c + d x]^5 \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \operatorname{Sec}[c + d x])^3 \right. \\
 & \quad \left. (A + C \operatorname{Sec}[c + d x]^2) \left( 3 A \operatorname{Sin}\left[\frac{d x}{2}\right] + 11 C \operatorname{Sin}\left[\frac{d x}{2}\right] \right) \right) / \\
 & \left( 12 d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) \left( \operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{d x}{2}\right] \right) \right)
 \end{aligned}$$

### Problem 106: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cos}[c + d x]^2 (a + a \operatorname{Sec}[c + d x])^3 (A + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 3, 162 leaves, 6 steps):

$$\frac{1}{2} a^3 (7 A + 2 C) x + \frac{a^3 (2 A + 7 C) \text{ArcTanh}[\text{Sin}[c + d x]]}{2 d} +$$

$$\frac{5 a^3 (A - C) \text{Sin}[c + d x]}{2 d} + \frac{A \text{Cos}[c + d x] (a + a \text{Sec}[c + d x])^3 \text{Sin}[c + d x]}{2 d} -$$

$$\frac{(A - C) (a^2 + a^2 \text{Sec}[c + d x])^2 \text{Sin}[c + d x]}{2 a d} - \frac{(A - 4 C) (a^3 + a^3 \text{Sec}[c + d x]) \text{Sin}[c + d x]}{2 d}$$

Result (type 3, 1074 leaves):



$$\begin{aligned}
 & \left( (7A + 2C) x \cos[c + dx]^5 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 (A + C \sec[c + dx]^2) \right) / \\
 & \left( 8(A + 2C + A \cos[2c + 2dx]) \right) + \\
 & \left( (-2A - 7C) \cos[c + dx]^5 \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \right. \\
 & \left. (a + a \sec[c + dx])^3 (A + C \sec[c + dx]^2) \right) / \left( 8d(A + 2C + A \cos[2c + 2dx]) \right) + \\
 & \left( (2A + 7C) \cos[c + dx]^5 \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \right. \\
 & \left. (a + a \sec[c + dx])^3 (A + C \sec[c + dx]^2) \right) / \left( 8d(A + 2C + A \cos[2c + 2dx]) \right) + \\
 & \left( 3A \cos[dx] \cos[c + dx]^5 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 (A + C \sec[c + dx]^2) \sin[c] \right) / \\
 & \left( 4d(A + 2C + A \cos[2c + 2dx]) \right) + \\
 & \left( A \cos[2dx] \cos[c + dx]^5 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 (A + C \sec[c + dx]^2) \sin[2c] \right) / \\
 & \left( 16d(A + 2C + A \cos[2c + 2dx]) \right) + \\
 & \left( 3A \cos[c] \cos[c + dx]^5 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 (A + C \sec[c + dx]^2) \sin[dx] \right) / \\
 & \left( 4d(A + 2C + A \cos[2c + 2dx]) \right) + \\
 & \left( A \cos[2c] \cos[c + dx]^5 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 (A + C \sec[c + dx]^2) \sin[2dx] \right) / \\
 & \left( 16d(A + 2C + A \cos[2c + 2dx]) \right) + \\
 & \left( C \cos[c + dx]^5 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 (A + C \sec[c + dx]^2) \right) / \\
 & \left( 16d(A + 2C + A \cos[2c + 2dx]) \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right)^2 \right) + \\
 & \left( 3C \cos[c + dx]^5 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 (A + C \sec[c + dx]^2) \sin\left[\frac{dx}{2}\right] \right) / \\
 & \left( 4d(A + 2C + A \cos[2c + 2dx]) \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right) \right) - \\
 & \left( C \cos[c + dx]^5 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 (A + C \sec[c + dx]^2) \right) / \\
 & \left( 16d(A + 2C + A \cos[2c + 2dx]) \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right)^2 \right) + \\
 & \left( 3C \cos[c + dx]^5 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 (A + C \sec[c + dx]^2) \sin\left[\frac{dx}{2}\right] \right) / \\
 & \left( 4d(A + 2C + A \cos[2c + 2dx]) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right) \right)
 \end{aligned}$$

**Problem 107: Result more than twice size of optimal antiderivative.**

$$\int \cos[c + dx]^3 (a + a \sec[c + dx])^3 (A + C \sec[c + dx]^2) dx$$

Optimal (type 3, 156 leaves, 6 steps):

$$\frac{1}{2} a^3 (5 A + 6 C) x + \frac{3 a^3 C \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{d} +$$

$$\frac{5 a^3 A \operatorname{Sin}[c + d x]}{2 d} + \frac{A \operatorname{Cos}[c + d x]^2 (a + a \operatorname{Sec}[c + d x])^3 \operatorname{Sin}[c + d x]}{3 d} +$$

$$\frac{A \operatorname{Cos}[c + d x] (a^2 + a^2 \operatorname{Sec}[c + d x])^2 \operatorname{Sin}[c + d x]}{2 a d} - \frac{(5 A - 6 C) (a^3 + a^3 \operatorname{Sec}[c + d x]) \operatorname{Sin}[c + d x]}{6 d}$$

Result (type 3, 1014 leaves):

$$\begin{aligned}
 & a^3 \left( \left( (5A + 6C) x \cos[c + dx]^2 (1 + \cos[c + dx])^3 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (A + C \sec[c + dx]^2) \right) / \right. \\
 & \quad \left. (8(A + 2C + A \cos[2c + 2dx])) - \right. \\
 & \quad \left( 3C \cos[c + dx]^2 (1 + \cos[c + dx])^3 \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \right. \\
 & \quad \quad \left. \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (A + C \sec[c + dx]^2) \right) / (4d(A + 2C + A \cos[2c + 2dx])) + \\
 & \quad \left( 3C \cos[c + dx]^2 (1 + \cos[c + dx])^3 \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \right. \\
 & \quad \quad \left. \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (A + C \sec[c + dx]^2) \right) / (4d(A + 2C + A \cos[2c + 2dx])) + \\
 & \quad \left( (15A + 4C) \cos[dx] \cos[c + dx]^2 (1 + \cos[c + dx])^3 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \right. \\
 & \quad \quad \left. (A + C \sec[c + dx]^2) \sin[c] \right) / (16d(A + 2C + A \cos[2c + 2dx])) + \\
 & \quad \left( 3A \cos[2dx] \cos[c + dx]^2 (1 + \cos[c + dx])^3 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (A + C \sec[c + dx]^2) \sin[2c] \right) / \\
 & \quad \left( 16d(A + 2C + A \cos[2c + 2dx])) + \right. \\
 & \quad \left( A \cos[3dx] \cos[c + dx]^2 (1 + \cos[c + dx])^3 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (A + C \sec[c + dx]^2) \sin[3c] \right) / \\
 & \quad \left( 48d(A + 2C + A \cos[2c + 2dx])) + \right. \\
 & \quad \left( (15A + 4C) \cos[c] \cos[c + dx]^2 (1 + \cos[c + dx])^3 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \right. \\
 & \quad \quad \left. (A + C \sec[c + dx]^2) \sin[dx] \right) / (16d(A + 2C + A \cos[2c + 2dx])) + \\
 & \quad \left( 3A \cos[2c] \cos[c + dx]^2 (1 + \cos[c + dx])^3 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (A + C \sec[c + dx]^2) \sin[2dx] \right) / \\
 & \quad \left( 16d(A + 2C + A \cos[2c + 2dx])) + \right. \\
 & \quad \left( A \cos[3c] \cos[c + dx]^2 (1 + \cos[c + dx])^3 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (A + C \sec[c + dx]^2) \sin[3dx] \right) / \\
 & \quad \left( 48d(A + 2C + A \cos[2c + 2dx])) + \right. \\
 & \quad \left( C \cos[c + dx]^2 (1 + \cos[c + dx])^3 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (A + C \sec[c + dx]^2) \sin\left[\frac{dx}{2}\right] \right) / \\
 & \quad \left( 4d(A + 2C + A \cos[2c + 2dx]) \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right) \right) + \\
 & \quad \left( C \cos[c + dx]^2 (1 + \cos[c + dx])^3 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (A + C \sec[c + dx]^2) \sin\left[\frac{dx}{2}\right] \right) / \\
 & \quad \left( 4d(A + 2C + A \cos[2c + 2dx]) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right) \right) \Big)
 \end{aligned}$$

**Problem 111: Result more than twice size of optimal antiderivative.**

$$\int \sec[c + dx]^2 (a + a \sec[c + dx])^4 (A + C \sec[c + dx]^2) dx$$

Optimal (type 3, 228 leaves, 15 steps):

$$\frac{a^4 (14 A + 11 C) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{4 d} + \frac{16 a^4 (14 A + 11 C) \operatorname{Tan}[c + d x]}{35 d} +$$

$$\frac{27 a^4 (14 A + 11 C) \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x]}{140 d} + \frac{a^4 (14 A + 11 C) \operatorname{Sec}[c + d x]^3 \operatorname{Tan}[c + d x]}{70 d} +$$

$$\frac{(21 A + 4 C) (a + a \operatorname{Sec}[c + d x])^4 \operatorname{Tan}[c + d x]}{105 d} + \frac{C \operatorname{Sec}[c + d x]^2 (a + a \operatorname{Sec}[c + d x])^4 \operatorname{Tan}[c + d x]}{7 d} +$$

$$\frac{2 C (a + a \operatorname{Sec}[c + d x])^5 \operatorname{Tan}[c + d x]}{21 a d} + \frac{8 a^4 (14 A + 11 C) \operatorname{Tan}[c + d x]^3}{105 d}$$

Result (type 3, 574 leaves):

$$\left( (-14 A - 11 C) \operatorname{Cos}[c + d x]^6 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right] - \operatorname{Sin}\left[\frac{c}{2} + \frac{d x}{2}\right]\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^8 \right. \\ \left. (a + a \operatorname{Sec}[c + d x])^4 (A + C \operatorname{Sec}[c + d x]^2) \right) / (32 d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x])) +$$

$$\left( (14 A + 11 C) \operatorname{Cos}[c + d x]^6 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{d x}{2}\right]\right] \right. \\ \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^8 (a + a \operatorname{Sec}[c + d x])^4 (A + C \operatorname{Sec}[c + d x]^2) \right) /$$

$$(32 d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x])) + \frac{1}{215040 d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x])}$$

$$\operatorname{Sec}[c] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^8 \operatorname{Sec}[c + d x] (a + a \operatorname{Sec}[c + d x])^4 (A + C \operatorname{Sec}[c + d x]^2)$$

$$(50960 A \operatorname{Sin}[d x] + 46480 C \operatorname{Sin}[d x] - 30380 A \operatorname{Sin}[2 c + d x] - 17080 C \operatorname{Sin}[2 c + d x] +$$

$$10710 A \operatorname{Sin}[c + 2 d x] + 16415 C \operatorname{Sin}[c + 2 d x] + 10710 A \operatorname{Sin}[3 c + 2 d x] +$$

$$16415 C \operatorname{Sin}[3 c + 2 d x] + 41244 A \operatorname{Sin}[2 c + 3 d x] + 37296 C \operatorname{Sin}[2 c + 3 d x] -$$

$$7560 A \operatorname{Sin}[4 c + 3 d x] - 840 C \operatorname{Sin}[4 c + 3 d x] + 7560 A \operatorname{Sin}[3 c + 4 d x] + 7700 C \operatorname{Sin}[3 c + 4 d x] +$$

$$7560 A \operatorname{Sin}[5 c + 4 d x] + 7700 C \operatorname{Sin}[5 c + 4 d x] + 15848 A \operatorname{Sin}[4 c + 5 d x] +$$

$$12712 C \operatorname{Sin}[4 c + 5 d x] - 420 A \operatorname{Sin}[6 c + 5 d x] + 1470 A \operatorname{Sin}[5 c + 6 d x] + 1155 C \operatorname{Sin}[5 c + 6 d x] +$$

$$1470 A \operatorname{Sin}[7 c + 6 d x] + 1155 C \operatorname{Sin}[7 c + 6 d x] + 2324 A \operatorname{Sin}[6 c + 7 d x] + 1816 C \operatorname{Sin}[6 c + 7 d x])$$

### Problem 112: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[c + d x] (a + a \operatorname{Sec}[c + d x])^4 (A + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 3, 188 leaves, 14 steps):

$$\frac{7 a^4 (10 A + 7 C) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{16 d} +$$

$$\frac{4 a^4 (10 A + 7 C) \operatorname{Tan}[c + d x]}{5 d} + \frac{27 a^4 (10 A + 7 C) \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x]}{80 d} +$$

$$\frac{a^4 (10 A + 7 C) \operatorname{Sec}[c + d x]^3 \operatorname{Tan}[c + d x]}{40 d} - \frac{C (a + a \operatorname{Sec}[c + d x])^4 \operatorname{Tan}[c + d x]}{30 d} +$$

$$\frac{C (a + a \operatorname{Sec}[c + d x])^5 \operatorname{Tan}[c + d x]}{6 a d} + \frac{2 a^4 (10 A + 7 C) \operatorname{Tan}[c + d x]^3}{15 d}$$

Result (type 3, 530 leaves):

$$\begin{aligned}
 & - \left( \left( 7 (10A + 7C) \cos [c + dx]^6 \log \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] - \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right] \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^8 \right. \right. \\
 & \quad \left. \left. (a + a \sec [c + dx])^4 (A + C \sec [c + dx]^2) \right) / (128 d (A + 2C + A \cos [2c + 2dx])) \right) + \\
 & \left( 7 (10A + 7C) \cos [c + dx]^6 \log \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] + \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right] \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^8 \right. \\
 & \quad \left. (a + a \sec [c + dx])^4 (A + C \sec [c + dx]^2) \right) / (128 d (A + 2C + A \cos [2c + 2dx])) + \\
 & \frac{1}{61440 d (A + 2C + A \cos [2c + 2dx])} \sec [c] \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^8 (a + a \sec [c + dx])^4 \\
 & \left( (A + C \sec [c + dx]^2) (-16000A \sin [c] - 11520C \sin [c] + 1860A \sin [dx] + 3750C \sin [dx] + \right. \\
 & \quad 1860A \sin [2c + dx] + 3750C \sin [2c + dx] + 17280A \sin [c + 2dx] + 15360C \sin [c + 2dx] - \\
 & \quad 6720A \sin [3c + 2dx] - 1920C \sin [3c + 2dx] + 2670A \sin [2c + 3dx] + 3845C \sin [2c + 3dx] + \\
 & \quad 2670A \sin [4c + 3dx] + 3845C \sin [4c + 3dx] + 8640A \sin [3c + 4dx] + \\
 & \quad 6912C \sin [3c + 4dx] - 960A \sin [5c + 4dx] + 810A \sin [4c + 5dx] + 735C \sin [4c + 5dx] + \\
 & \quad \left. 810A \sin [6c + 5dx] + 735C \sin [6c + 5dx] + 1600A \sin [5c + 6dx] + 1152C \sin [5c + 6dx] \right)
 \end{aligned}$$

### Problem 113: Result more than twice size of optimal antiderivative.

$$\int (a + a \sec [c + dx])^4 (A + C \sec [c + dx]^2) dx$$

Optimal (type 3, 177 leaves, 8 steps):

$$\begin{aligned}
 & a^4 Ax + \frac{a^4 (12A + 7C) \operatorname{ArcTanh} [\sin [c + dx]]}{2d} + \frac{a^4 (10A + 7C) \tan [c + dx]}{2d} + \\
 & \frac{aC (a + a \sec [c + dx])^3 \tan [c + dx]}{5d} + \frac{C (a + a \sec [c + dx])^4 \tan [c + dx]}{5d} + \\
 & \frac{(5A + 7C) (a^2 + a^2 \sec [c + dx])^2 \tan [c + dx]}{15d} + \frac{(8A + 7C) (a^4 + a^4 \sec [c + dx]) \tan [c + dx]}{6d}
 \end{aligned}$$

Result (type 3, 418 leaves):

$$\begin{aligned}
 & \frac{1}{3840 d (A + 2C + A \cos [2(c + dx)])} a^4 (1 + \cos [c + dx])^4 \\
 & \left( (C + A \cos [c + dx]^2) \sec \left[ \frac{1}{2} (c + dx) \right]^8 \sec [c + dx]^5 \left( -240 (12A + 7C) \cos [c + dx]^5 \right. \right. \\
 & \quad \left. \left. \left( \log \left[ \cos \left[ \frac{1}{2} (c + dx) \right] - \sin \left[ \frac{1}{2} (c + dx) \right] \right] - \log \left[ \cos \left[ \frac{1}{2} (c + dx) \right] + \sin \left[ \frac{1}{2} (c + dx) \right] \right] \right) \right) + \\
 & \quad \left( \sec [c] (150A dx \cos [dx] + 150A dx \cos [2c + dx] + 75A dx \cos [2c + 3dx] + \right. \\
 & \quad 75A dx \cos [4c + 3dx] + 15A dx \cos [4c + 5dx] + 15A dx \cos [6c + 5dx] + \\
 & \quad 1220A \sin [dx] + 1180C \sin [dx] - 780A \sin [2c + dx] - 480C \sin [2c + dx] + \\
 & \quad 120A \sin [c + 2dx] + 330C \sin [c + 2dx] + 120A \sin [3c + 2dx] + 330C \sin [3c + 2dx] + \\
 & \quad 820A \sin [2c + 3dx] + 800C \sin [2c + 3dx] - 180A \sin [4c + 3dx] - \\
 & \quad 30C \sin [4c + 3dx] + 60A \sin [3c + 4dx] + 105C \sin [3c + 4dx] + 60A \sin [5c + 4dx] + \\
 & \quad \left. \left. 105C \sin [5c + 4dx] + 200A \sin [4c + 5dx] + 166C \sin [4c + 5dx] \right) \right)
 \end{aligned}$$

**Problem 114: Result more than twice size of optimal antiderivative.**

$$\int \cos [c+d x] (a+a \operatorname{Sec}[c+d x])^4 (A+C \operatorname{Sec}[c+d x]^2) dx$$

Optimal (type 3, 181 leaves, 8 steps):

$$\begin{aligned} & 4 a^4 A x + \frac{a^4 (52 A+35 C) \operatorname{ArcTanh}[\operatorname{Sin}[c+d x]]}{8 d} + \frac{A (a+a \operatorname{Sec}[c+d x])^4 \operatorname{Sin}[c+d x]}{d} + \\ & \frac{5 a^4 (4 A+7 C) \operatorname{Tan}[c+d x]}{8 d} - \frac{a (4 A-C) (a+a \operatorname{Sec}[c+d x])^3 \operatorname{Tan}[c+d x]}{4 d} - \\ & \frac{(12 A-7 C) (a^2+a^2 \operatorname{Sec}[c+d x])^2 \operatorname{Tan}[c+d x]}{12 d} - \frac{(12 A-35 C) (a^4+a^4 \operatorname{Sec}[c+d x]) \operatorname{Tan}[c+d x]}{24 d} \end{aligned}$$

Result (type 3, 379 leaves):

$$\begin{aligned} & \frac{1}{1536 d (A+2 C+A \operatorname{Cos}[2(c+d x)])} \\ & a^4 (C+A \operatorname{Cos}[c+d x]^2) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^8 (1+\operatorname{Sec}[c+d x])^4 \left(-24(52 A+35 C) \operatorname{Cos}[c+d x]^4 \right. \\ & \left. \left(\operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]-\operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]\right) + \right. \\ & \left. \operatorname{Sec}[c] (288 A d x \operatorname{Cos}[c]+192 A d x \operatorname{Cos}[c+2 d x]+192 A d x \operatorname{Cos}[3 c+2 d x]+ \right. \\ & 48 A d x \operatorname{Cos}[3 c+4 d x]+48 A d x \operatorname{Cos}[5 c+4 d x]-288 A \operatorname{Sin}[c]-480 C \operatorname{Sin}[c]+ \\ & 24 A \operatorname{Sin}[d x]+105 C \operatorname{Sin}[d x]+24 A \operatorname{Sin}[2 c+d x]+105 C \operatorname{Sin}[2 c+d x]+ \\ & 288 A \operatorname{Sin}[c+2 d x]+544 C \operatorname{Sin}[c+2 d x]-96 A \operatorname{Sin}[3 c+2 d x]-96 C \operatorname{Sin}[3 c+2 d x]+ \\ & 30 A \operatorname{Sin}[2 c+3 d x]+81 C \operatorname{Sin}[2 c+3 d x]+30 A \operatorname{Sin}[4 c+3 d x]+81 C \operatorname{Sin}[4 c+3 d x]+ \\ & \left. \left. 96 A \operatorname{Sin}[3 c+4 d x]+160 C \operatorname{Sin}[3 c+4 d x]+6 A \operatorname{Sin}[4 c+5 d x]+6 A \operatorname{Sin}[6 c+5 d x]\right)\right) \end{aligned}$$

**Problem 115: Result more than twice size of optimal antiderivative.**

$$\int \cos [c+d x]^2 (a+a \operatorname{Sec}[c+d x])^4 (A+C \operatorname{Sec}[c+d x]^2) dx$$

Optimal (type 3, 192 leaves, 7 steps):

$$\begin{aligned} & \frac{1}{2} a^4 (13 A+2 C) x + \frac{2 a^4 (2 A+3 C) \operatorname{ArcTanh}[\operatorname{Sin}[c+d x]]}{d} + \frac{5 a^4 (A-2 C) \operatorname{Sin}[c+d x]}{2 d} - \\ & \frac{a (3 A-2 C) (a+a \operatorname{Sec}[c+d x])^3 \operatorname{Sin}[c+d x]}{6 d} + \frac{A \operatorname{Cos}[c+d x] (a+a \operatorname{Sec}[c+d x])^4 \operatorname{Sin}[c+d x]}{2 d} - \\ & \frac{(A-2 C) (a^2+a^2 \operatorname{Sec}[c+d x])^2 \operatorname{Sin}[c+d x]}{2 d} + \frac{(3 A+22 C) (a^4+a^4 \operatorname{Sec}[c+d x]) \operatorname{Sin}[c+d x]}{6 d} \end{aligned}$$

Result (type 3, 1420 leaves):

$$\begin{aligned} & \left( (13 A+2 C) x \operatorname{Cos}[c+d x]^6 \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \operatorname{Sec}[c+d x])^4 (A+C \operatorname{Sec}[c+d x]^2) \right) / \\ & (16 (A+2 C+A \operatorname{Cos}[2 c+2 d x])) + \end{aligned}$$

$$\begin{aligned}
 & \left( (-2A - 3C) \cos[c + dx]^6 \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^8 \right. \\
 & \quad \left. (a + a \sec[c + dx])^4 (A + C \sec[c + dx]^2) \right) / (4d (A + 2C + A \cos[2c + 2dx])) + \\
 & \left( (2A + 3C) \cos[c + dx]^6 \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^8 \right. \\
 & \quad \left. (a + a \sec[c + dx])^4 (A + C \sec[c + dx]^2) \right) / (4d (A + 2C + A \cos[2c + 2dx])) + \\
 & \left( A \cos[dx] \cos[c + dx]^6 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \sec[c + dx])^4 (A + C \sec[c + dx]^2) \sin[c] \right) / \\
 & \quad (2d (A + 2C + A \cos[2c + 2dx])) + \\
 & \left( A \cos[2dx] \cos[c + dx]^6 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \sec[c + dx])^4 (A + C \sec[c + dx]^2) \sin[2c] \right) / \\
 & \quad (32d (A + 2C + A \cos[2c + 2dx])) + \\
 & \left( A \cos[c] \cos[c + dx]^6 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \sec[c + dx])^4 (A + C \sec[c + dx]^2) \sin[dx] \right) / \\
 & \quad (2d (A + 2C + A \cos[2c + 2dx])) + \\
 & \left( A \cos[2c] \cos[c + dx]^6 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \sec[c + dx])^4 (A + C \sec[c + dx]^2) \sin[2dx] \right) / \\
 & \quad (32d (A + 2C + A \cos[2c + 2dx])) + \\
 & \left( C \cos[c + dx]^6 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \sec[c + dx])^4 (A + C \sec[c + dx]^2) \sin\left[\frac{dx}{2}\right] \right) / \\
 & \quad \left( 48d (A + 2C + A \cos[2c + 2dx]) \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right)^3 \right) + \\
 & \left( \cos[c + dx]^6 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \sec[c + dx])^4 \right. \\
 & \quad \left. (A + C \sec[c + dx]^2) \left( 13C \cos\left[\frac{c}{2}\right] - 11C \sin\left[\frac{c}{2}\right] \right) \right) / \\
 & \quad \left( 96d (A + 2C + A \cos[2c + 2dx]) \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right)^2 \right) + \\
 & \left( \cos[c + dx]^6 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \sec[c + dx])^4 \right. \\
 & \quad \left. (A + C \sec[c + dx]^2) \left( 3A \sin\left[\frac{dx}{2}\right] + 20C \sin\left[\frac{dx}{2}\right] \right) \right) / \\
 & \quad \left( 24d (A + 2C + A \cos[2c + 2dx]) \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right) \right) + \\
 & \left( C \cos[c + dx]^6 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \sec[c + dx])^4 (A + C \sec[c + dx]^2) \sin\left[\frac{dx}{2}\right] \right) / \\
 & \quad \left( 48d (A + 2C + A \cos[2c + 2dx]) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right)^3 \right) + \\
 & \left( \cos[c + dx]^6 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \sec[c + dx])^4 \right. \\
 & \quad \left. (A + C \sec[c + dx]^2) \left( -13C \cos\left[\frac{c}{2}\right] - 11C \sin\left[\frac{c}{2}\right] \right) \right) / \\
 & \quad \left( 96d (A + 2C + A \cos[2c + 2dx]) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right)^2 \right) +
 \end{aligned}$$

$$\left( \cos [c+d x]^6 \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \operatorname{Sec}[c+d x])^4 (A+C \operatorname{Sec}[c+d x]^2) \left(3 A \sin\left[\frac{d x}{2}\right]+20 C \sin\left[\frac{d x}{2}\right]\right) \right) / \left(24 d (A+2 C+A \cos [2 c+2 d x]) \left(\cos\left[\frac{c}{2}\right]+\sin\left[\frac{c}{2}\right]\right) \left(\cos\left[\frac{c}{2}+\frac{d x}{2}\right]+\sin\left[\frac{c}{2}+\frac{d x}{2}\right]\right)\right)$$

**Problem 116: Result more than twice size of optimal antiderivative.**

$$\int \cos [c+d x]^3 (a+a \operatorname{Sec}[c+d x])^4 (A+C \operatorname{Sec}[c+d x]^2) dx$$

Optimal (type 3, 198 leaves, 7 steps):

$$\begin{aligned} & 2 a^4 (3 A+2 C) x + \frac{a^4 (2 A+13 C) \operatorname{ArcTanh}[\sin [c+d x]]}{2 d} + \\ & \frac{5 a^4 (2 A-C) \sin [c+d x]}{2 d} + \frac{2 a A \cos [c+d x] (a+a \operatorname{Sec}[c+d x])^3 \sin [c+d x]}{3 d} + \\ & \frac{A \cos [c+d x]^2 (a+a \operatorname{Sec}[c+d x])^4 \sin [c+d x]}{3 d} - \\ & \frac{(2 A-C) (a^2+a^2 \operatorname{Sec}[c+d x])^2 \sin [c+d x]}{2 d} - \frac{(4 A-9 C) (a^4+a^4 \operatorname{Sec}[c+d x]) \sin [c+d x]}{3 d} \end{aligned}$$

Result (type 3, 1250 leaves):



$$\begin{aligned}
 & \left( (3A + 2C) x \cos [c + dx]^6 \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^8 (a + a \sec [c + dx])^4 (A + C \sec [c + dx]^2) \right) / \\
 & \quad (4 (A + 2C + A \cos [2c + 2dx])) + \\
 & \left( (-2A - 13C) \cos [c + dx]^6 \log \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] - \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right] \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^8 \right. \\
 & \quad \left. (a + a \sec [c + dx])^4 (A + C \sec [c + dx]^2) \right) / (16d (A + 2C + A \cos [2c + 2dx])) + \\
 & \left( (2A + 13C) \cos [c + dx]^6 \log \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] + \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right] \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^8 \right. \\
 & \quad \left. (a + a \sec [c + dx])^4 (A + C \sec [c + dx]^2) \right) / (16d (A + 2C + A \cos [2c + 2dx])) + \\
 & \left( (27A + 4C) \cos [dx] \cos [c + dx]^6 \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^8 (a + a \sec [c + dx])^4 \right. \\
 & \quad \left. (A + C \sec [c + dx]^2) \sin [c] \right) / (32d (A + 2C + A \cos [2c + 2dx])) + \\
 & \left( A \cos [2dx] \cos [c + dx]^6 \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^8 (a + a \sec [c + dx])^4 (A + C \sec [c + dx]^2) \sin [2c] \right) / \\
 & \quad (8d (A + 2C + A \cos [2c + 2dx])) + \\
 & \left( A \cos [3dx] \cos [c + dx]^6 \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^8 (a + a \sec [c + dx])^4 (A + C \sec [c + dx]^2) \sin [3c] \right) / \\
 & \quad (96d (A + 2C + A \cos [2c + 2dx])) + \\
 & \left( (27A + 4C) \cos [c] \cos [c + dx]^6 \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^8 (a + a \sec [c + dx])^4 \right. \\
 & \quad \left. (A + C \sec [c + dx]^2) \sin [dx] \right) / (32d (A + 2C + A \cos [2c + 2dx])) + \\
 & \left( A \cos [2c] \cos [c + dx]^6 \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^8 (a + a \sec [c + dx])^4 (A + C \sec [c + dx]^2) \sin [2dx] \right) / \\
 & \quad (8d (A + 2C + A \cos [2c + 2dx])) + \\
 & \left( A \cos [3c] \cos [c + dx]^6 \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^8 (a + a \sec [c + dx])^4 (A + C \sec [c + dx]^2) \sin [3dx] \right) / \\
 & \quad (96d (A + 2C + A \cos [2c + 2dx])) + \\
 & \left( C \cos [c + dx]^6 \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^8 (a + a \sec [c + dx])^4 (A + C \sec [c + dx]^2) \right) / \\
 & \quad \left( 32d (A + 2C + A \cos [2c + 2dx]) \left( \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] - \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right)^2 \right) + \\
 & \left( C \cos [c + dx]^6 \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^8 (a + a \sec [c + dx])^4 (A + C \sec [c + dx]^2) \sin \left[ \frac{dx}{2} \right] \right) / \\
 & \quad \left( 2d (A + 2C + A \cos [2c + 2dx]) \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] - \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right) \right) - \\
 & \left( C \cos [c + dx]^6 \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^8 (a + a \sec [c + dx])^4 (A + C \sec [c + dx]^2) \right) / \\
 & \quad \left( 32d (A + 2C + A \cos [2c + 2dx]) \left( \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] + \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right)^2 \right) + \\
 & \left( C \cos [c + dx]^6 \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^8 (a + a \sec [c + dx])^4 (A + C \sec [c + dx]^2) \sin \left[ \frac{dx}{2} \right] \right) / \\
 & \quad \left( 2d (A + 2C + A \cos [2c + 2dx]) \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] + \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right) \right)
 \end{aligned}$$

### Problem 121: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Sec}[c + dx]^4 (A + C \text{Sec}[c + dx]^2)}{a + a \text{Sec}[c + dx]} dx$$

Optimal (type 3, 165 leaves, 7 steps):

$$\frac{3(4A + 5C) \text{ArcTanh}[\text{Sin}[c + dx]]}{8ad} - \frac{(3A + 4C) \text{Tan}[c + dx]}{ad} + \frac{3(4A + 5C) \text{Sec}[c + dx] \text{Tan}[c + dx]}{8ad} + \frac{(4A + 5C) \text{Sec}[c + dx]^3 \text{Tan}[c + dx]}{4ad} - \frac{(A + C) \text{Sec}[c + dx]^4 \text{Tan}[c + dx]}{d(a + a \text{Sec}[c + dx])} - \frac{(3A + 4C) \text{Tan}[c + dx]^3}{3ad}$$

Result (type 3, 792 leaves):

$$\begin{aligned} & - \left( \left( 3(4A + 5C) \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c + dx] \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] (A + C \text{Sec}[c + dx]^2) \right) \right) / \\ & \quad \left( 2d(A + 2C + A \cos[2c + 2dx]) (a + a \text{Sec}[c + dx]) \right) + \\ & \left( 3(4A + 5C) \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c + dx] \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] (A + C \text{Sec}[c + dx]^2) \right) / \\ & \quad \left( 2d(A + 2C + A \cos[2c + 2dx]) (a + a \text{Sec}[c + dx]) \right) + \\ & \quad \frac{1}{192d(A + 2C + A \cos[2c + 2dx]) (a + a \text{Sec}[c + dx])} \\ & \quad \cos\left[\frac{c}{2} + \frac{dx}{2}\right] \text{Sec}\left[\frac{c}{2}\right] \text{Sec}[c] \text{Sec}[c + dx]^3 (A + C \text{Sec}[c + dx]^2) \\ & \quad \left( -60A \sin\left[\frac{dx}{2}\right] - 75C \sin\left[\frac{dx}{2}\right] - 60A \sin\left[\frac{3dx}{2}\right] - 91C \sin\left[\frac{3dx}{2}\right] + 204A \sin\left[c - \frac{dx}{2}\right] + \right. \\ & \quad 219C \sin\left[c - \frac{dx}{2}\right] - 60A \sin\left[c + \frac{dx}{2}\right] + 21C \sin\left[c + \frac{dx}{2}\right] + 84A \sin\left[2c + \frac{dx}{2}\right] + \\ & \quad 165C \sin\left[2c + \frac{dx}{2}\right] + 36A \sin\left[c + \frac{3dx}{2}\right] + 5C \sin\left[c + \frac{3dx}{2}\right] + 36A \sin\left[2c + \frac{3dx}{2}\right] + \\ & \quad 69C \sin\left[2c + \frac{3dx}{2}\right] + 132A \sin\left[3c + \frac{3dx}{2}\right] + 165C \sin\left[3c + \frac{3dx}{2}\right] - \\ & \quad 156A \sin\left[c + \frac{5dx}{2}\right] - 211C \sin\left[c + \frac{5dx}{2}\right] - 60A \sin\left[2c + \frac{5dx}{2}\right] - \\ & \quad 115C \sin\left[2c + \frac{5dx}{2}\right] - 60A \sin\left[3c + \frac{5dx}{2}\right] - 51C \sin\left[3c + \frac{5dx}{2}\right] + \\ & \quad 36A \sin\left[4c + \frac{5dx}{2}\right] + 45C \sin\left[4c + \frac{5dx}{2}\right] - 12A \sin\left[2c + \frac{7dx}{2}\right] - 19C \sin\left[2c + \frac{7dx}{2}\right] + \\ & \quad 12A \sin\left[3c + \frac{7dx}{2}\right] + 5C \sin\left[3c + \frac{7dx}{2}\right] + 12A \sin\left[4c + \frac{7dx}{2}\right] + 21C \sin\left[4c + \frac{7dx}{2}\right] + \\ & \quad 36A \sin\left[5c + \frac{7dx}{2}\right] + 45C \sin\left[5c + \frac{7dx}{2}\right] - 48A \sin\left[3c + \frac{9dx}{2}\right] - 64C \sin\left[3c + \frac{9dx}{2}\right] - \\ & \quad \left. 24A \sin\left[4c + \frac{9dx}{2}\right] - 40C \sin\left[4c + \frac{9dx}{2}\right] - 24A \sin\left[5c + \frac{9dx}{2}\right] - 24C \sin\left[5c + \frac{9dx}{2}\right] \right) \end{aligned}$$

**Problem 122: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Sec}[c + d x]^3 (A + C \text{Sec}[c + d x]^2)}{a + a \text{Sec}[c + d x]} dx$$

Optimal (type 3, 133 leaves, 6 steps):

$$\begin{aligned} & - \frac{(2A + 3C) \text{ArcTanh}[\text{Sin}[c + d x]]}{2 a d} + \frac{(3A + 4C) \text{Tan}[c + d x]}{a d} - \\ & \frac{(2A + 3C) \text{Sec}[c + d x] \text{Tan}[c + d x]}{2 a d} - \frac{(A + C) \text{Sec}[c + d x]^3 \text{Tan}[c + d x]}{d (a + a \text{Sec}[c + d x])} + \frac{(3A + 4C) \text{Tan}[c + d x]^3}{3 a d} \end{aligned}$$

Result (type 3, 1090 leaves):

$$\begin{aligned}
 & \left( 2 (2 A + 3 C) \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \cos [c + dx] \log \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] - \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right] (A + C \sec [c + dx]^2) \right) / \\
 & \left( d (A + 2 C + A \cos [2 c + 2 dx]) (a + a \sec [c + dx]) \right) - \\
 & \left( 2 (2 A + 3 C) \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \cos [c + dx] \log \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] + \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right] (A + C \sec [c + dx]^2) \right) / \\
 & \left( d (A + 2 C + A \cos [2 c + 2 dx]) (a + a \sec [c + dx]) \right) + \\
 & \left( 4 \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] \cos [c + dx] \sec \left[ \frac{c}{2} \right] (A + C \sec [c + dx]^2) \left( A \sin \left[ \frac{dx}{2} \right] + C \sin \left[ \frac{dx}{2} \right] \right) \right) / \\
 & \left( d (A + 2 C + A \cos [2 c + 2 dx]) (a + a \sec [c + dx]) \right) + \\
 & \left( 2 C \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \cos [c + dx] (A + C \sec [c + dx]^2) \sin \left[ \frac{dx}{2} \right] \right) / \left( 3 d (A + 2 C + A \cos [2 c + 2 dx]) \right. \\
 & \left. (a + a \sec [c + dx]) \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] - \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right)^3 \right) - \\
 & \left( 2 \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \cos [c + dx] (A + C \sec [c + dx]^2) \left( C \cos \left[ \frac{c}{2} \right] - 2 C \sin \left[ \frac{c}{2} \right] \right) \right) / \\
 & \left( 3 d (A + 2 C + A \cos [2 c + 2 dx]) (a + a \sec [c + dx]) \right. \\
 & \left. \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] - \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right)^2 \right) + \\
 & \left( 4 \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \cos [c + dx] (A + C \sec [c + dx]^2) \left( 3 A \sin \left[ \frac{dx}{2} \right] + 5 C \sin \left[ \frac{dx}{2} \right] \right) \right) / \\
 & \left( 3 d (A + 2 C + A \cos [2 c + 2 dx]) (a + a \sec [c + dx]) \right. \\
 & \left. \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] - \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right) \right) + \\
 & \left( 2 C \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \cos [c + dx] (A + C \sec [c + dx]^2) \sin \left[ \frac{dx}{2} \right] \right) / \left( 3 d (A + 2 C + A \cos [2 c + 2 dx]) \right. \\
 & \left. (a + a \sec [c + dx]) \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] + \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right)^3 \right) + \\
 & \left( 2 \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \cos [c + dx] (A + C \sec [c + dx]^2) \left( C \cos \left[ \frac{c}{2} \right] + 2 C \sin \left[ \frac{c}{2} \right] \right) \right) / \\
 & \left( 3 d (A + 2 C + A \cos [2 c + 2 dx]) (a + a \sec [c + dx]) \right. \\
 & \left. \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] + \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right)^2 \right) + \\
 & \left( 4 \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \cos [c + dx] (A + C \sec [c + dx]^2) \left( 3 A \sin \left[ \frac{dx}{2} \right] + 5 C \sin \left[ \frac{dx}{2} \right] \right) \right) / \\
 & \left( 3 d (A + 2 C + A \cos [2 c + 2 dx]) (a + a \sec [c + dx]) \right. \\
 & \left. \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] + \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right) \right)
 \end{aligned}$$

**Problem 123: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c + dx]^2 (A + C \sec [c + dx]^2)}{a + a \sec [c + dx]} dx$$

Optimal (type 3, 107 leaves, 6 steps):

$$\frac{(2A+3C) \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{2ad} - \frac{(A+2C) \operatorname{Tan}[c+dx]}{ad} + \frac{(2A+3C) \operatorname{Sec}[c+dx] \operatorname{Tan}[c+dx]}{2ad} - \frac{(A+C) \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx]}{d(a+a \operatorname{Sec}[c+dx])}$$

Result (type 3, 316 leaves):

$$\frac{1}{ad(A+2C+A \operatorname{Cos}[2(c+dx)])(1+\operatorname{Sec}[c+dx])} \cos\left[\frac{1}{2}(c+dx)\right] \cos[c+dx] (A+C \operatorname{Sec}[c+dx])^2 \left( -4(A+C) \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sin}\left[\frac{dx}{2}\right] + \cos\left[\frac{1}{2}(c+dx)\right] \left( -2(2A+3C) \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + 4A \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + 6C \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + \frac{C}{\left(\cos\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^2} - \frac{C}{\left(\cos\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^2} \right) \right) \left( \frac{4C \operatorname{Sin}[dx]}{\left(\left(\cos\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right]\right)\left(\cos\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right]\right)\right)} \right) \right)$$

**Problem 124: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c+dx] (A+C \operatorname{Sec}[c+dx]^2)}{a+a \operatorname{Sec}[c+dx]} dx$$

Optimal (type 3, 57 leaves, 4 steps):

$$-\frac{C \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{ad} + \frac{C \operatorname{Tan}[c+dx]}{ad} + \frac{(A+C) \operatorname{Tan}[c+dx]}{ad(1+\operatorname{Sec}[c+dx])}$$

Result (type 3, 227 leaves):

$$\left( 4 \cos\left[\frac{1}{2}(c+dx)\right] \cos[c+dx] (A+C \operatorname{Sec}[c+dx])^2 \left( (A+C) \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sin}\left[\frac{dx}{2}\right] + C \cos\left[\frac{1}{2}(c+dx)\right] \right) \left( \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + \operatorname{Sin}[dx] \right) \right) \left( \frac{C}{\left(\cos\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right]\right)\left(\cos\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right]\right)} \right) \left( \cos\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \left( \cos\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \left( \frac{4C \operatorname{Sin}[dx]}{\left(\left(\cos\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right]\right)\left(\cos\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right]\right)\right)} \right) \right) \left( \frac{1}{ad(A+2C+A \operatorname{Cos}[2(c+dx)])(1+\operatorname{Sec}[c+dx])} \right)$$

### Problem 125: Result more than twice size of optimal antiderivative.

$$\int \frac{A + C \operatorname{Sec}[c + dx]^2}{a + a \operatorname{Sec}[c + dx]} dx$$

Optimal (type 3, 49 leaves, 4 steps):

$$\frac{Ax}{a} + \frac{C \operatorname{ArcTanh}[\operatorname{Sin}[c + dx]]}{ad} - \frac{(A + C) \operatorname{Tan}[c + dx]}{ad(1 + \operatorname{Sec}[c + dx])}$$

Result (type 3, 143 leaves):

$$\begin{aligned} & - \left( \left( 4 \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] (C + A \operatorname{Cos}[c + dx])^2 \right. \right. \\ & \quad \left. \left( -\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] \left( Adx - C \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right] \right) + \right. \right. \\ & \quad \left. \left. C \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right] \right) + (A + C) \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sin}\left[\frac{dx}{2}\right] \right) \Big/ \\ & \quad \left( ad(1 + \operatorname{Cos}[c + dx]) (A + 2C + A \operatorname{Cos}[2(c + dx)]) \right) \end{aligned}$$

### Problem 126: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cos}[c + dx] (A + C \operatorname{Sec}[c + dx]^2)}{a + a \operatorname{Sec}[c + dx]} dx$$

Optimal (type 3, 52 leaves, 4 steps):

$$-\frac{Ax}{a} + \frac{(2A + C) \operatorname{Sin}[c + dx]}{ad} - \frac{(A + C) \operatorname{Sin}[c + dx]}{d(a + a \operatorname{Sec}[c + dx])}$$

Result (type 3, 108 leaves):

$$\begin{aligned} & \frac{1}{4ad} \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right] \left( -2Adx \operatorname{Cos}\left[\frac{dx}{2}\right] - 2Adx \operatorname{Cos}\left[c + \frac{dx}{2}\right] + \right. \\ & \quad \left. 5A \operatorname{Sin}\left[\frac{dx}{2}\right] + 4C \operatorname{Sin}\left[\frac{dx}{2}\right] + A \operatorname{Sin}\left[c + \frac{dx}{2}\right] + A \operatorname{Sin}\left[c + \frac{3dx}{2}\right] + A \operatorname{Sin}\left[2c + \frac{3dx}{2}\right] \right) \end{aligned}$$

### Problem 130: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Sec}[c + dx]^4 (A + C \operatorname{Sec}[c + dx]^2)}{(a + a \operatorname{Sec}[c + dx])^2} dx$$

Optimal (type 3, 172 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{(2A+5C) \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{a^2 d} + \frac{(5A+12C) \operatorname{Tan}[c+dx]}{a^2 d} \\
 & \frac{(2A+5C) \operatorname{Sec}[c+dx] \operatorname{Tan}[c+dx]}{a^2 d} - \frac{2(2A+5C) \operatorname{Sec}[c+dx]^3 \operatorname{Tan}[c+dx]}{3a^2 d (1+\operatorname{Sec}[c+dx])} \\
 & \frac{(A+C) \operatorname{Sec}[c+dx]^4 \operatorname{Tan}[c+dx]}{3d (a+a \operatorname{Sec}[c+dx])^2} + \frac{(5A+12C) \operatorname{Tan}[c+dx]^3}{3a^2 d}
 \end{aligned}$$

Result (type 3, 623 leaves):

$$\begin{aligned}
 & \frac{1}{24a^2 d (A+2C+A \operatorname{Cos}[2(c+dx)]) (1+\operatorname{Sec}[c+dx])^2} \\
 & \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] (A+C \operatorname{Sec}[c+dx]^2) \left(192(2A+5C) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^3 \right. \\
 & \quad \left. \left(\operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]\right) + \right. \\
 & \quad \operatorname{Sec}\left[\frac{C}{2}\right] \operatorname{Sec}[c] \operatorname{Sec}[c+dx]^3 \left(-3(8A+C) \operatorname{Sin}\left[\frac{dx}{2}\right] + (66A+155C) \operatorname{Sin}\left[\frac{3dx}{2}\right] - \right. \\
 & \quad 60A \operatorname{Sin}\left[c - \frac{dx}{2}\right] - 153C \operatorname{Sin}\left[c - \frac{dx}{2}\right] + 24A \operatorname{Sin}\left[c + \frac{dx}{2}\right] + 21C \operatorname{Sin}\left[c + \frac{dx}{2}\right] - \\
 & \quad 60A \operatorname{Sin}\left[2c + \frac{dx}{2}\right] - 135C \operatorname{Sin}\left[2c + \frac{dx}{2}\right] - 4A \operatorname{Sin}\left[c + \frac{3dx}{2}\right] + 25C \operatorname{Sin}\left[c + \frac{3dx}{2}\right] + \\
 & \quad 36A \operatorname{Sin}\left[2c + \frac{3dx}{2}\right] + 45C \operatorname{Sin}\left[2c + \frac{3dx}{2}\right] - 34A \operatorname{Sin}\left[3c + \frac{3dx}{2}\right] - \\
 & \quad 85C \operatorname{Sin}\left[3c + \frac{3dx}{2}\right] + 42A \operatorname{Sin}\left[c + \frac{5dx}{2}\right] + 99C \operatorname{Sin}\left[c + \frac{5dx}{2}\right] + 21C \operatorname{Sin}\left[2c + \frac{5dx}{2}\right] + \\
 & \quad 24A \operatorname{Sin}\left[3c + \frac{5dx}{2}\right] + 33C \operatorname{Sin}\left[3c + \frac{5dx}{2}\right] - 18A \operatorname{Sin}\left[4c + \frac{5dx}{2}\right] - \\
 & \quad 45C \operatorname{Sin}\left[4c + \frac{5dx}{2}\right] + 24A \operatorname{Sin}\left[2c + \frac{7dx}{2}\right] + 57C \operatorname{Sin}\left[2c + \frac{7dx}{2}\right] + \\
 & \quad 3A \operatorname{Sin}\left[3c + \frac{7dx}{2}\right] + 18C \operatorname{Sin}\left[3c + \frac{7dx}{2}\right] + 15A \operatorname{Sin}\left[4c + \frac{7dx}{2}\right] + 24C \operatorname{Sin}\left[4c + \frac{7dx}{2}\right] - \\
 & \quad 6A \operatorname{Sin}\left[5c + \frac{7dx}{2}\right] - 15C \operatorname{Sin}\left[5c + \frac{7dx}{2}\right] + 10A \operatorname{Sin}\left[3c + \frac{9dx}{2}\right] + 24C \operatorname{Sin}\left[3c + \frac{9dx}{2}\right] + \\
 & \quad \left. \left. 3A \operatorname{Sin}\left[4c + \frac{9dx}{2}\right] + 11C \operatorname{Sin}\left[4c + \frac{9dx}{2}\right] + 7A \operatorname{Sin}\left[5c + \frac{9dx}{2}\right] + 13C \operatorname{Sin}\left[5c + \frac{9dx}{2}\right]\right) \right)
 \end{aligned}$$

**Problem 131: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c+dx]^3 (A+C \operatorname{Sec}[c+dx]^2)}{(a+a \operatorname{Sec}[c+dx])^2} dx$$

Optimal (type 3, 150 leaves, 7 steps):

$$\frac{(2A+7C) \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{2a^2d} - \frac{4(A+4C) \operatorname{Tan}[c+dx]}{3a^2d} + \frac{(2A+7C) \operatorname{Sec}[c+dx] \operatorname{Tan}[c+dx]}{2a^2d} - \frac{2(A+4C) \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx]}{3a^2d(1+\operatorname{Sec}[c+dx])} - \frac{(A+C) \operatorname{Sec}[c+dx]^3 \operatorname{Tan}[c+dx]}{3d(a+a \operatorname{Sec}[c+dx])^2}$$

Result (type 3, 513 leaves):

$$\frac{1}{24a^2d(A+2C+A \operatorname{Cos}[2(c+dx)]) (1+\operatorname{Sec}[c+dx])^2} \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] (A+C \operatorname{Sec}[c+dx]^2) \left(96(2A+7C) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^3 \left(\operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]\right) + \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c] \operatorname{Sec}[c+dx]^2 \left(-2(10A+7C) \operatorname{Sin}\left[\frac{dx}{2}\right] + (22A+97C) \operatorname{Sin}\left[\frac{3dx}{2}\right] - 36A \operatorname{Sin}\left[c - \frac{dx}{2}\right] - 126C \operatorname{Sin}\left[c - \frac{dx}{2}\right] + 36A \operatorname{Sin}\left[c + \frac{dx}{2}\right] + 42C \operatorname{Sin}\left[c + \frac{dx}{2}\right] - 20A \operatorname{Sin}\left[2c + \frac{dx}{2}\right] - 98C \operatorname{Sin}\left[2c + \frac{dx}{2}\right] - 18A \operatorname{Sin}\left[c + \frac{3dx}{2}\right] - 3C \operatorname{Sin}\left[c + \frac{3dx}{2}\right] + 22A \operatorname{Sin}\left[2c + \frac{3dx}{2}\right] + 37C \operatorname{Sin}\left[2c + \frac{3dx}{2}\right] - 18A \operatorname{Sin}\left[3c + \frac{3dx}{2}\right] - 63C \operatorname{Sin}\left[3c + \frac{3dx}{2}\right] + 18A \operatorname{Sin}\left[c + \frac{5dx}{2}\right] + 75C \operatorname{Sin}\left[c + \frac{5dx}{2}\right] - 6A \operatorname{Sin}\left[2c + \frac{5dx}{2}\right] + 15C \operatorname{Sin}\left[2c + \frac{5dx}{2}\right] + 18A \operatorname{Sin}\left[3c + \frac{5dx}{2}\right] + 39C \operatorname{Sin}\left[3c + \frac{5dx}{2}\right] - 6A \operatorname{Sin}\left[4c + \frac{5dx}{2}\right] - 21C \operatorname{Sin}\left[4c + \frac{5dx}{2}\right] + 8A \operatorname{Sin}\left[2c + \frac{7dx}{2}\right] + 32C \operatorname{Sin}\left[2c + \frac{7dx}{2}\right] + 12C \operatorname{Sin}\left[3c + \frac{7dx}{2}\right] + 8A \operatorname{Sin}\left[4c + \frac{7dx}{2}\right] + 20C \operatorname{Sin}\left[4c + \frac{7dx}{2}\right]\right)\right)$$

**Problem 132: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c+dx]^2 (A+C \operatorname{Sec}[c+dx]^2)}{(a+a \operatorname{Sec}[c+dx])^2} dx$$

Optimal (type 3, 99 leaves, 6 steps):

$$\frac{2C \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{a^2d} + \frac{(A+4C) \operatorname{Tan}[c+dx]}{3a^2d} + \frac{2C \operatorname{Tan}[c+dx]}{a^2d(1+\operatorname{Sec}[c+dx])} - \frac{(A+C) \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx]}{3d(a+a \operatorname{Sec}[c+dx])^2}$$

Result (type 3, 280 leaves):



$$\frac{1}{3 a^2 d (A+2 C+A \cos [2 (c+d x)]) (1+\sec [c+d x])^2} 4 \cos \left[\frac{1}{2}(c+d x)\right] (A+C \sec [c+d x])^2$$

$$\left( (A+C) \sec \left[\frac{c}{2}\right] \sin \left[\frac{d x}{2}\right] + 2 (A+7 C) \cos \left[\frac{1}{2}(c+d x)\right]^2 \sec \left[\frac{c}{2}\right] \sin \left[\frac{d x}{2}\right] + 6 C \cos \left[\frac{1}{2}(c+d x)\right]^3 \right.$$

$$\left. \left( 2 \log \left[\cos \left[\frac{1}{2}(c+d x)\right] - \sin \left[\frac{1}{2}(c+d x)\right]\right] - 2 \log \left[\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right] + \right.$$

$$\left. \sin [d x] \right) / \left( \left( \cos \left[\frac{c}{2}\right] - \sin \left[\frac{c}{2}\right] \right) \left( \cos \left[\frac{c}{2}\right] + \sin \left[\frac{c}{2}\right] \right) \left( \cos \left[\frac{1}{2}(c+d x)\right] - \sin \left[\frac{1}{2}(c+d x)\right] \right) \right.$$

$$\left. \left( \cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right] \right) \right) + (A+C) \cos \left[\frac{1}{2}(c+d x)\right] \tan \left[\frac{c}{2}\right]$$

**Problem 133: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c+d x] (A+C \sec [c+d x])^2}{(a+a \sec [c+d x])^2} dx$$

Optimal (type 3, 75 leaves, 4 steps):

$$\frac{C \operatorname{ArcTanh}[\sin [c+d x]]}{a^2 d} + \frac{(A-5 C) \tan [c+d x]}{3 a^2 d (1+\sec [c+d x])} + \frac{(A+C) \tan [c+d x]}{3 d (a+a \sec [c+d x])^2}$$

Result (type 3, 377 leaves):

$$-\frac{1}{6 a^2 d (1+\sec [c+d x])^2} \cos \left[\frac{1}{2}(c+d x)\right] \sec \left[\frac{c}{2}\right]$$

$$\sec [c+d x]^2 \left( 3 C \cos \left[c+\frac{3 d x}{2}\right] \log \left[\cos \left[\frac{1}{2}(c+d x)\right] - \sin \left[\frac{1}{2}(c+d x)\right]\right] + \right.$$

$$3 C \cos \left[2 c+\frac{3 d x}{2}\right] \log \left[\cos \left[\frac{1}{2}(c+d x)\right] - \sin \left[\frac{1}{2}(c+d x)\right]\right] + \right.$$

$$9 C \cos \left[\frac{d x}{2}\right] \left( \log \left[\cos \left[\frac{1}{2}(c+d x)\right] - \sin \left[\frac{1}{2}(c+d x)\right]\right] - \right.$$

$$\left. \log \left[\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right] \right) + 9 C \cos \left[c+\frac{d x}{2}\right]$$

$$\left( \log \left[\cos \left[\frac{1}{2}(c+d x)\right] - \sin \left[\frac{1}{2}(c+d x)\right]\right] - \log \left[\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right] \right) -$$

$$3 C \cos \left[c+\frac{3 d x}{2}\right] \log \left[\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right] -$$

$$3 C \cos \left[2 c+\frac{3 d x}{2}\right] \log \left[\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right] - 6 A \sin \left[\frac{d x}{2}\right] +$$

$$18 C \sin \left[\frac{d x}{2}\right] + 6 A \sin \left[c+\frac{d x}{2}\right] - 6 C \sin \left[c+\frac{d x}{2}\right] - 4 A \sin \left[c+\frac{3 d x}{2}\right] + 8 C \sin \left[c+\frac{3 d x}{2}\right]$$

**Problem 134: Result more than twice size of optimal antiderivative.**

$$\int \frac{A+C \sec [c+d x]^2}{(a+a \sec [c+d x])^2} dx$$

Optimal (type 3, 68 leaves, 3 steps):

$$\frac{A x}{a^2} - \frac{2(2A-C) \tan[c+dx]}{3a^2 d (1+\sec[c+dx])} - \frac{(A+C) \tan[c+dx]}{3d (a+a \sec[c+dx])^2}$$

Result (type 3, 141 leaves):

$$\frac{1}{24 a^2 d} \sec\left[\frac{c}{2}\right] \sec\left[\frac{1}{2}(c+dx)\right]^3 \\ \left(9 A d x \cos\left[\frac{dx}{2}\right] + 9 A d x \cos\left[c + \frac{dx}{2}\right] + 3 A d x \cos\left[c + \frac{3 dx}{2}\right] + 3 A d x \cos\left[2c + \frac{3 dx}{2}\right] - \right. \\ \left. 18 A \sin\left[\frac{dx}{2}\right] + 6 C \sin\left[\frac{dx}{2}\right] + 12 A \sin\left[c + \frac{dx}{2}\right] - 10 A \sin\left[c + \frac{3 dx}{2}\right] + 2 C \sin\left[c + \frac{3 dx}{2}\right]\right)$$

**Problem 135: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c+dx] (A+C \sec[c+dx]^2)}{(a+a \sec[c+dx])^2} dx$$

Optimal (type 3, 82 leaves, 5 steps):

$$-\frac{2Ax}{a^2} + \frac{(10A+C) \sin[c+dx]}{3a^2 d} - \frac{2A \sin[c+dx]}{a^2 d (1+\sec[c+dx])} - \frac{(A+C) \sin[c+dx]}{3d (a+a \sec[c+dx])^2}$$

Result (type 3, 195 leaves):

$$\frac{1}{48 a^2 d} \sec\left[\frac{c}{2}\right] \sec\left[\frac{1}{2}(c+dx)\right]^3 \\ \left(-36 A d x \cos\left[\frac{dx}{2}\right] - 36 A d x \cos\left[c + \frac{dx}{2}\right] - 12 A d x \cos\left[c + \frac{3 dx}{2}\right] - 12 A d x \cos\left[2c + \frac{3 dx}{2}\right] + \right. \\ \left. 66 A \sin\left[\frac{dx}{2}\right] + 12 C \sin\left[\frac{dx}{2}\right] - 30 A \sin\left[c + \frac{dx}{2}\right] - 12 C \sin\left[c + \frac{dx}{2}\right] + 41 A \sin\left[c + \frac{3 dx}{2}\right] + \right. \\ \left. 8 C \sin\left[c + \frac{3 dx}{2}\right] + 9 A \sin\left[2c + \frac{3 dx}{2}\right] + 3 A \sin\left[2c + \frac{5 dx}{2}\right] + 3 A \sin\left[3c + \frac{5 dx}{2}\right]\right)$$

**Problem 136: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c+dx]^2 (A+C \sec[c+dx]^2)}{(a+a \sec[c+dx])^2} dx$$

Optimal (type 3, 137 leaves, 6 steps):

$$\frac{(7A+2C)x}{2a^2} - \frac{4(4A+C) \sin[c+dx]}{3a^2 d} + \frac{(7A+2C) \cos[c+dx] \sin[c+dx]}{2a^2 d} - \\ \frac{2(4A+C) \cos[c+dx] \sin[c+dx]}{3a^2 d (1+\sec[c+dx])} - \frac{(A+C) \cos[c+dx] \sin[c+dx]}{3d (a+a \sec[c+dx])^2}$$

Result (type 3, 281 leaves):

$$\frac{1}{48 a^2 d (1 + \operatorname{Sec}[c + d x])^2} \cos\left[\frac{1}{2}(c + d x)\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c + d x]^2 \left( 36 (7 A + 2 C) d x \cos\left[\frac{d x}{2}\right] + 36 (7 A + 2 C) d x \cos\left[c + \frac{d x}{2}\right] + 84 A d x \cos\left[c + \frac{3 d x}{2}\right] + 24 C d x \cos\left[c + \frac{3 d x}{2}\right] + 84 A d x \cos\left[2 c + \frac{3 d x}{2}\right] + 24 C d x \cos\left[2 c + \frac{3 d x}{2}\right] - 381 A \sin\left[\frac{d x}{2}\right] - 144 C \sin\left[\frac{d x}{2}\right] + 147 A \sin\left[c + \frac{d x}{2}\right] + 96 C \sin\left[c + \frac{d x}{2}\right] - 239 A \sin\left[c + \frac{3 d x}{2}\right] - 80 C \sin\left[c + \frac{3 d x}{2}\right] - 63 A \sin\left[2 c + \frac{3 d x}{2}\right] - 15 A \sin\left[2 c + \frac{5 d x}{2}\right] - 15 A \sin\left[3 c + \frac{5 d x}{2}\right] + 3 A \sin\left[3 c + \frac{7 d x}{2}\right] + 3 A \sin\left[4 c + \frac{7 d x}{2}\right] \right)$$

**Problem 137: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c + d x]^3 (A + C \operatorname{Sec}[c + d x]^2)}{(a + a \operatorname{Sec}[c + d x])^2} dx$$

Optimal (type 3, 163 leaves, 7 steps):

$$\frac{(5 A + 2 C) x}{a^2} + \frac{(12 A + 5 C) \sin[c + d x]}{a^2 d} - \frac{(5 A + 2 C) \cos[c + d x] \sin[c + d x]}{a^2 d} - \frac{2 (5 A + 2 C) \cos[c + d x]^2 \sin[c + d x]}{3 a^2 d (1 + \operatorname{Sec}[c + d x])} - \frac{(A + C) \cos[c + d x]^2 \sin[c + d x]}{3 d (a + a \operatorname{Sec}[c + d x])^2} - \frac{(12 A + 5 C) \sin[c + d x]^3}{3 a^2 d}$$

Result (type 3, 349 leaves):

$$\frac{1}{48 a^2 d (1 + \operatorname{Sec}[c + d x])^2} \cos\left[\frac{1}{2}(c + d x)\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c + d x]^2 \left( -72 (5 A + 2 C) d x \cos\left[\frac{d x}{2}\right] - 72 (5 A + 2 C) d x \cos\left[c + \frac{d x}{2}\right] - 120 A d x \cos\left[c + \frac{3 d x}{2}\right] - 48 C d x \cos\left[c + \frac{3 d x}{2}\right] - 120 A d x \cos\left[2 c + \frac{3 d x}{2}\right] - 48 C d x \cos\left[2 c + \frac{3 d x}{2}\right] + 516 A \sin\left[\frac{d x}{2}\right] + 264 C \sin\left[\frac{d x}{2}\right] - 156 A \sin\left[c + \frac{d x}{2}\right] - 120 C \sin\left[c + \frac{d x}{2}\right] + 342 A \sin\left[c + \frac{3 d x}{2}\right] + 164 C \sin\left[c + \frac{3 d x}{2}\right] + 118 A \sin\left[2 c + \frac{3 d x}{2}\right] + 36 C \sin\left[2 c + \frac{3 d x}{2}\right] + 30 A \sin\left[2 c + \frac{5 d x}{2}\right] + 12 C \sin\left[2 c + \frac{5 d x}{2}\right] + 30 A \sin\left[3 c + \frac{5 d x}{2}\right] + 12 C \sin\left[3 c + \frac{5 d x}{2}\right] - 3 A \sin\left[3 c + \frac{7 d x}{2}\right] - 3 A \sin\left[4 c + \frac{7 d x}{2}\right] + A \sin\left[4 c + \frac{9 d x}{2}\right] + A \sin\left[5 c + \frac{9 d x}{2}\right] \right)$$

**Problem 138: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Sec}[c + d x]^4 (A + C \text{Sec}[c + d x]^2)}{(a + a \text{Sec}[c + d x])^3} dx$$

Optimal (type 3, 198 leaves, 8 steps):

$$\begin{aligned} & \frac{(2A + 13C) \text{ArcTanh}[\text{Sin}[c + d x]]}{2a^3 d} - \frac{2(11A + 76C) \text{Tan}[c + d x]}{15a^3 d} + \\ & \frac{(2A + 13C) \text{Sec}[c + d x] \text{Tan}[c + d x]}{2a^3 d} - \frac{(A + C) \text{Sec}[c + d x]^4 \text{Tan}[c + d x]}{5d(a + a \text{Sec}[c + d x])^3} - \\ & \frac{(A + 11C) \text{Sec}[c + d x]^3 \text{Tan}[c + d x]}{15ad(a + a \text{Sec}[c + d x])^2} - \frac{(11A + 76C) \text{Sec}[c + d x]^2 \text{Tan}[c + d x]}{15d(a^3 + a^3 \text{Sec}[c + d x])} \end{aligned}$$

Result (type 3, 632 leaves):

$$\begin{aligned} & - \frac{1}{240a^3 d (A + 2C + A \text{Cos}[2(c + d x)]) (1 + \text{Sec}[c + d x])^3} \\ & \text{Cos}\left[\frac{1}{2}(c + d x)\right] \text{Sec}[c + d x] (A + C \text{Sec}[c + d x]^2) \\ & \left( 1920(2A + 13C) \text{Cos}\left[\frac{1}{2}(c + d x)\right]^5 \left( \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right] - \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - \right. \right. \\ & \quad \left. \left. \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right] + \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right]\right) + \text{Sec}\left[\frac{c}{2}\right] \text{Sec}[c] \text{Sec}[c + d x]^2 \right. \\ & \quad \left. - 5(98A + 247C) \text{Sin}\left[\frac{d x}{2}\right] + 5(106A + 761C) \text{Sin}\left[\frac{3 d x}{2}\right] - 654A \text{Sin}\left[c - \frac{d x}{2}\right] - \right. \\ & \quad 4329C \text{Sin}\left[c - \frac{d x}{2}\right] + 654A \text{Sin}\left[c + \frac{d x}{2}\right] + 1989C \text{Sin}\left[c + \frac{d x}{2}\right] - 490A \text{Sin}\left[2c + \frac{d x}{2}\right] - \\ & \quad 3575C \text{Sin}\left[2c + \frac{d x}{2}\right] - 350A \text{Sin}\left[c + \frac{3 d x}{2}\right] - 475C \text{Sin}\left[c + \frac{3 d x}{2}\right] + 530A \text{Sin}\left[2c + \frac{3 d x}{2}\right] + \\ & \quad 2005C \text{Sin}\left[2c + \frac{3 d x}{2}\right] - 350A \text{Sin}\left[3c + \frac{3 d x}{2}\right] - 2275C \text{Sin}\left[3c + \frac{3 d x}{2}\right] + \\ & \quad 378A \text{Sin}\left[c + \frac{5 d x}{2}\right] + 2673C \text{Sin}\left[c + \frac{5 d x}{2}\right] - 150A \text{Sin}\left[2c + \frac{5 d x}{2}\right] + 105C \text{Sin}\left[2c + \frac{5 d x}{2}\right] + \\ & \quad 378A \text{Sin}\left[3c + \frac{5 d x}{2}\right] + 1593C \text{Sin}\left[3c + \frac{5 d x}{2}\right] - 150A \text{Sin}\left[4c + \frac{5 d x}{2}\right] - \\ & \quad 975C \text{Sin}\left[4c + \frac{5 d x}{2}\right] + 190A \text{Sin}\left[2c + \frac{7 d x}{2}\right] + 1325C \text{Sin}\left[2c + \frac{7 d x}{2}\right] - 30A \\ & \quad \left. \text{Sin}\left[3c + \frac{7 d x}{2}\right] + 255C \text{Sin}\left[3c + \frac{7 d x}{2}\right] + 190A \text{Sin}\left[4c + \frac{7 d x}{2}\right] + 875C \text{Sin}\left[4c + \frac{7 d x}{2}\right] - \right. \\ & \quad \left. 30A \text{Sin}\left[5c + \frac{7 d x}{2}\right] - 195C \text{Sin}\left[5c + \frac{7 d x}{2}\right] + 44A \text{Sin}\left[3c + \frac{9 d x}{2}\right] + 304C \text{Sin}\left[3c + \frac{9 d x}{2}\right] + \right. \\ & \quad \left. 90C \text{Sin}\left[4c + \frac{9 d x}{2}\right] + 44A \text{Sin}\left[5c + \frac{9 d x}{2}\right] + 214C \text{Sin}\left[5c + \frac{9 d x}{2}\right] \right) \end{aligned}$$

**Problem 139: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Sec}[c + dx]^3 (A + C \text{Sec}[c + dx]^2)}{(a + a \text{Sec}[c + dx])^3} dx$$

Optimal (type 3, 145 leaves, 7 steps):

$$-\frac{3 C \text{ArcTanh}[\text{Sin}[c + dx]]}{a^3 d} + \frac{(2 A + 27 C) \text{Tan}[c + dx]}{15 a^3 d} - \frac{(A + C) \text{Sec}[c + dx]^3 \text{Tan}[c + dx]}{5 d (a + a \text{Sec}[c + dx])^3} + \frac{(A - 9 C) \text{Sec}[c + dx]^2 \text{Tan}[c + dx]}{15 a d (a + a \text{Sec}[c + dx])^2} + \frac{3 C \text{Tan}[c + dx]}{d (a^3 + a^3 \text{Sec}[c + dx])}$$

Result (type 3, 457 leaves):

$$\frac{1}{60 a^3 d (A + 2 C + A \text{Cos}[2(c + dx)]) (1 + \text{Sec}[c + dx])^3} \text{Cos}\left[\frac{1}{2}(c + dx)\right] \text{Sec}[c + dx] (A + C \text{Sec}[c + dx]^2) \left(2880 C \text{Cos}\left[\frac{1}{2}(c + dx)\right]^5 \left(\text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + dx)\right] - \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right] - \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + dx)\right] + \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right]\right) + \text{Sec}\left[\frac{c}{2}\right] \text{Sec}[c] \text{Sec}[c + dx] \left(-5(4A + 51C) \text{Sin}\left[\frac{dx}{2}\right] + (22A + 567C) \text{Sin}\left[\frac{3dx}{2}\right] - 10A \text{Sin}\left[c - \frac{dx}{2}\right] - 600C \text{Sin}\left[c - \frac{dx}{2}\right] + 10A \text{Sin}\left[c + \frac{dx}{2}\right] + 375C \text{Sin}\left[c + \frac{dx}{2}\right] - 20A \text{Sin}\left[2c + \frac{dx}{2}\right] - 480C \text{Sin}\left[2c + \frac{dx}{2}\right] - 60C \text{Sin}\left[c + \frac{3dx}{2}\right] + 22A \text{Sin}\left[2c + \frac{3dx}{2}\right] + 402C \text{Sin}\left[2c + \frac{3dx}{2}\right] - 225C \text{Sin}\left[3c + \frac{3dx}{2}\right] + 10A \text{Sin}\left[c + \frac{5dx}{2}\right] + 315C \text{Sin}\left[c + \frac{5dx}{2}\right] + 30C \text{Sin}\left[2c + \frac{5dx}{2}\right] + 10A \text{Sin}\left[3c + \frac{5dx}{2}\right] + 240C \text{Sin}\left[3c + \frac{5dx}{2}\right] - 45C \text{Sin}\left[4c + \frac{5dx}{2}\right] + 2A \text{Sin}\left[2c + \frac{7dx}{2}\right] + 72C \text{Sin}\left[2c + \frac{7dx}{2}\right] + 15C \text{Sin}\left[3c + \frac{7dx}{2}\right] + 2A \text{Sin}\left[4c + \frac{7dx}{2}\right] + 57C \text{Sin}\left[4c + \frac{7dx}{2}\right]\right)$$

**Problem 142: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + C \text{Sec}[c + dx]^2}{(a + a \text{Sec}[c + dx])^3} dx$$

Optimal (type 3, 106 leaves, 4 steps):

$$\frac{Ax}{a^3} - \frac{(A + C) \text{Tan}[c + dx]}{5 d (a + a \text{Sec}[c + dx])^3} - \frac{(7A - 3C) \text{Tan}[c + dx]}{15 a d (a + a \text{Sec}[c + dx])^2} - \frac{(22A - 3C) \text{Tan}[c + dx]}{15 d (a^3 + a^3 \text{Sec}[c + dx])}$$

Result (type 3, 227 leaves):

$$\frac{1}{480 a^3 d} \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^5 \left(150 A d x \cos\left[\frac{d x}{2}\right] + 150 A d x \cos\left[c + \frac{d x}{2}\right] + 75 A d x \cos\left[c + \frac{3 d x}{2}\right] + 75 A d x \cos\left[2 c + \frac{3 d x}{2}\right] + 15 A d x \cos\left[2 c + \frac{5 d x}{2}\right] + 15 A d x \cos\left[3 c + \frac{5 d x}{2}\right] - 370 A \sin\left[\frac{d x}{2}\right] + 30 C \sin\left[\frac{d x}{2}\right] + 270 A \sin\left[c + \frac{d x}{2}\right] - 30 C \sin\left[c + \frac{d x}{2}\right] - 230 A \sin\left[c + \frac{3 d x}{2}\right] + 30 C \sin\left[c + \frac{3 d x}{2}\right] + 90 A \sin\left[2 c + \frac{3 d x}{2}\right] - 64 A \sin\left[2 c + \frac{5 d x}{2}\right] + 6 C \sin\left[2 c + \frac{5 d x}{2}\right]\right)$$

**Problem 143: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c+d x] (A+C \sec[c+d x]^2)}{(a+a \sec[c+d x])^3} dx$$

Optimal (type 3, 120 leaves, 6 steps):

$$-\frac{3 A x}{a^3} + \frac{2(36 A+C) \sin[c+d x]}{15 a^3 d} - \frac{(A+C) \sin[c+d x]}{5 d (a+a \sec[c+d x])^3} - \frac{(9 A-C) \sin[c+d x]}{15 a d (a+a \sec[c+d x])^2} - \frac{3 A \sin[c+d x]}{d (a^3+a^3 \sec[c+d x])}$$

Result (type 3, 283 leaves):

$$\frac{1}{960 a^3 d} \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^5 \left(900 A d x \cos\left[\frac{d x}{2}\right] + 900 A d x \cos\left[c + \frac{d x}{2}\right] + 450 A d x \cos\left[c + \frac{3 d x}{2}\right] + 450 A d x \cos\left[2 c + \frac{3 d x}{2}\right] + 90 A d x \cos\left[2 c + \frac{5 d x}{2}\right] + 90 A d x \cos\left[3 c + \frac{5 d x}{2}\right] - 1755 A \sin\left[\frac{d x}{2}\right] - 160 C \sin\left[\frac{d x}{2}\right] + 1125 A \sin\left[c + \frac{d x}{2}\right] + 120 C \sin\left[c + \frac{d x}{2}\right] - 1215 A \sin\left[c + \frac{3 d x}{2}\right] - 80 C \sin\left[c + \frac{3 d x}{2}\right] + 225 A \sin\left[2 c + \frac{3 d x}{2}\right] + 60 C \sin\left[2 c + \frac{3 d x}{2}\right] - 363 A \sin\left[2 c + \frac{5 d x}{2}\right] - 28 C \sin\left[2 c + \frac{5 d x}{2}\right] - 75 A \sin\left[3 c + \frac{5 d x}{2}\right] - 15 A \sin\left[3 c + \frac{7 d x}{2}\right] - 15 A \sin\left[4 c + \frac{7 d x}{2}\right]\right)$$

**Problem 144: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c+d x]^2 (A+C \sec[c+d x]^2)}{(a+a \sec[c+d x])^3} dx$$

Optimal (type 3, 183 leaves, 7 steps):

$$\frac{(13A+2C)x}{2a^3} - \frac{2(76A+11C)\sin[c+dx]}{15a^3d} +$$

$$\frac{(13A+2C)\cos[c+dx]\sin[c+dx]}{2a^3d} - \frac{(A+C)\cos[c+dx]\sin[c+dx]}{5d(a+a\sec[c+dx])^3} -$$

$$\frac{(11A+C)\cos[c+dx]\sin[c+dx]}{15ad(a+a\sec[c+dx])^2} - \frac{(76A+11C)\cos[c+dx]\sin[c+dx]}{15d(a^3+a^3\sec[c+dx])}$$

Result (type 3, 385 leaves):

$$\frac{1}{3840a^3d} \sec\left[\frac{c}{2}\right] \sec\left[\frac{1}{2}(c+dx)\right]^5$$

$$\left(600(13A+2C)dx \cos\left[\frac{dx}{2}\right] + 600(13A+2C)dx \cos\left[c+\frac{dx}{2}\right] + 3900Adx \cos\left[c+\frac{3dx}{2}\right] +\right.$$

$$600Cdx \cos\left[c+\frac{3dx}{2}\right] + 3900Adx \cos\left[2c+\frac{3dx}{2}\right] + 600Cdx \cos\left[2c+\frac{3dx}{2}\right] +$$

$$780Adx \cos\left[2c+\frac{5dx}{2}\right] + 120Cdx \cos\left[2c+\frac{5dx}{2}\right] + 780Adx \cos\left[3c+\frac{5dx}{2}\right] +$$

$$120Cdx \cos\left[3c+\frac{5dx}{2}\right] - 12760A \sin\left[\frac{dx}{2}\right] - 2960C \sin\left[\frac{dx}{2}\right] + 7560A \sin\left[c+\frac{dx}{2}\right] +$$

$$2160C \sin\left[c+\frac{dx}{2}\right] - 9230A \sin\left[c+\frac{3dx}{2}\right] - 1840C \sin\left[c+\frac{3dx}{2}\right] + 930A \sin\left[2c+\frac{3dx}{2}\right] +$$

$$720C \sin\left[2c+\frac{3dx}{2}\right] - 2782A \sin\left[2c+\frac{5dx}{2}\right] - 512C \sin\left[2c+\frac{5dx}{2}\right] - 750A \sin\left[3c+\frac{5dx}{2}\right] -$$

$$\left.105A \sin\left[3c+\frac{7dx}{2}\right] - 105A \sin\left[4c+\frac{7dx}{2}\right] + 15A \sin\left[4c+\frac{9dx}{2}\right] + 15A \sin\left[5c+\frac{9dx}{2}\right]\right)$$

**Problem 145: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c+dx]^3 (A+C \sec[c+dx])^2}{(a+a \sec[c+dx])^3} dx$$

Optimal (type 3, 216 leaves, 8 steps):

$$-\frac{(23A+6C)x}{2a^3} + \frac{4(34A+9C)\sin[c+dx]}{5a^3d} - \frac{(23A+6C)\cos[c+dx]\sin[c+dx]}{2a^3d} -$$

$$\frac{(A+C)\cos[c+dx]^2\sin[c+dx]}{5d(a+a\sec[c+dx])^3} - \frac{(13A+3C)\cos[c+dx]^2\sin[c+dx]}{15ad(a+a\sec[c+dx])^2} -$$

$$\frac{(23A+6C)\cos[c+dx]^2\sin[c+dx]}{3d(a^3+a^3\sec[c+dx])} - \frac{4(34A+9C)\sin[c+dx]^3}{15a^3d}$$

Result (type 3, 455 leaves):

$$\begin{aligned}
 & - \frac{1}{3840 a^3 d} \\
 & \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^5 \left( 600(23A+6C) dx \operatorname{Cos}\left[\frac{dx}{2}\right] + 600(23A+6C) dx \operatorname{Cos}\left[c+\frac{dx}{2}\right] + \right. \\
 & \quad 6900A dx \operatorname{Cos}\left[c+\frac{3dx}{2}\right] + 1800C dx \operatorname{Cos}\left[c+\frac{3dx}{2}\right] + 6900A dx \operatorname{Cos}\left[2c+\frac{3dx}{2}\right] + \\
 & \quad 1800C dx \operatorname{Cos}\left[2c+\frac{3dx}{2}\right] + 1380A dx \operatorname{Cos}\left[2c+\frac{5dx}{2}\right] + 360C dx \operatorname{Cos}\left[2c+\frac{5dx}{2}\right] + \\
 & \quad 1380A dx \operatorname{Cos}\left[3c+\frac{5dx}{2}\right] + 360C dx \operatorname{Cos}\left[3c+\frac{5dx}{2}\right] - 20410A \operatorname{Sin}\left[\frac{dx}{2}\right] - \\
 & \quad 7020C \operatorname{Sin}\left[\frac{dx}{2}\right] + 11110A \operatorname{Sin}\left[c+\frac{dx}{2}\right] + 4500C \operatorname{Sin}\left[c+\frac{dx}{2}\right] - 15380A \operatorname{Sin}\left[c+\frac{3dx}{2}\right] - \\
 & \quad 4860C \operatorname{Sin}\left[c+\frac{3dx}{2}\right] + 380A \operatorname{Sin}\left[2c+\frac{3dx}{2}\right] + 900C \operatorname{Sin}\left[2c+\frac{3dx}{2}\right] - 4777A \operatorname{Sin}\left[2c+\frac{5dx}{2}\right] - \\
 & \quad 1452C \operatorname{Sin}\left[2c+\frac{5dx}{2}\right] - 1625A \operatorname{Sin}\left[3c+\frac{5dx}{2}\right] - 300C \operatorname{Sin}\left[3c+\frac{5dx}{2}\right] - \\
 & \quad 230A \operatorname{Sin}\left[3c+\frac{7dx}{2}\right] - 60C \operatorname{Sin}\left[3c+\frac{7dx}{2}\right] - 230A \operatorname{Sin}\left[4c+\frac{7dx}{2}\right] - 60C \operatorname{Sin}\left[4c+\frac{7dx}{2}\right] + \\
 & \quad \left. 20A \operatorname{Sin}\left[4c+\frac{9dx}{2}\right] + 20A \operatorname{Sin}\left[5c+\frac{9dx}{2}\right] - 5A \operatorname{Sin}\left[5c+\frac{11dx}{2}\right] - 5A \operatorname{Sin}\left[6c+\frac{11dx}{2}\right] \right)
 \end{aligned}$$

**Problem 146: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c+dx]^5 (A+C \operatorname{Sec}[c+dx]^2)}{(a+a \operatorname{Sec}[c+dx])^4} dx$$

Optimal (type 3, 232 leaves, 9 steps):

$$\begin{aligned}
 & \frac{(2A+21C) \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{2a^4 d} - \\
 & \frac{32(5A+54C) \operatorname{Tan}[c+dx]}{105a^4 d} + \frac{(2A+21C) \operatorname{Sec}[c+dx] \operatorname{Tan}[c+dx]}{2a^4 d} - \\
 & \frac{(10A+129C) \operatorname{Sec}[c+dx]^3 \operatorname{Tan}[c+dx]}{105a^4 d (1+\operatorname{Sec}[c+dx])^2} - \frac{16(5A+54C) \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx]}{105a^4 d (1+\operatorname{Sec}[c+dx])} - \\
 & \frac{(A+C) \operatorname{Sec}[c+dx]^5 \operatorname{Tan}[c+dx]}{7d(a+a \operatorname{Sec}[c+dx])^4} - \frac{2C \operatorname{Sec}[c+dx]^4 \operatorname{Tan}[c+dx]}{5ad(a+a \operatorname{Sec}[c+dx])^3}
 \end{aligned}$$

Result (type 3, 890 leaves):



$$\begin{aligned}
 & - \left( \left( 16 (2A + 21C) \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^8 \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \sec[c + dx]^2 \right. \right. \\
 & \quad \left. \left. (A + C \sec[c + dx]^2) \right) / \left( d (A + 2C + A \cos[2c + 2dx]) (a + a \sec[c + dx]^4) \right) \right) + \\
 & \left( 16 (2A + 21C) \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^8 \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \sec[c + dx]^2 \right. \\
 & \quad \left. (A + C \sec[c + dx]^2) \right) / \left( d (A + 2C + A \cos[2c + 2dx]) (a + a \sec[c + dx]^4) \right) + \\
 & \quad \quad \quad 1 \\
 & \frac{3360 d (A + 2C + A \cos[2c + 2dx]) (a + a \sec[c + dx]^4)}{\cos\left[\frac{c}{2} + \frac{dx}{2}\right] \sec\left[\frac{c}{2}\right] \sec[c] \sec[c + dx]^4 (A + C \sec[c + dx]^2)} \\
 & \left( 14140 A \sin\left[\frac{dx}{2}\right] + 73206 C \sin\left[\frac{dx}{2}\right] - 15160 A \sin\left[\frac{3dx}{2}\right] - 166668 C \sin\left[\frac{3dx}{2}\right] + \right. \\
 & \quad 17220 A \sin\left[c - \frac{dx}{2}\right] + 183162 C \sin\left[c - \frac{dx}{2}\right] - 17220 A \sin\left[c + \frac{dx}{2}\right] - 100842 C \sin\left[c + \frac{dx}{2}\right] + \\
 & \quad 14140 A \sin\left[2c + \frac{dx}{2}\right] + 155526 C \sin\left[2c + \frac{dx}{2}\right] + 9800 A \sin\left[c + \frac{3dx}{2}\right] + \\
 & \quad 37380 C \sin\left[c + \frac{3dx}{2}\right] - 15160 A \sin\left[2c + \frac{3dx}{2}\right] - 101148 C \sin\left[2c + \frac{3dx}{2}\right] + \\
 & \quad 9800 A \sin\left[3c + \frac{3dx}{2}\right] + 102900 C \sin\left[3c + \frac{3dx}{2}\right] - 10920 A \sin\left[c + \frac{5dx}{2}\right] - \\
 & \quad 119364 C \sin\left[c + \frac{5dx}{2}\right] + 4760 A \sin\left[2c + \frac{5dx}{2}\right] + 8820 C \sin\left[2c + \frac{5dx}{2}\right] - \\
 & \quad 10920 A \sin\left[3c + \frac{5dx}{2}\right] - 78204 C \sin\left[3c + \frac{5dx}{2}\right] + 4760 A \sin\left[4c + \frac{5dx}{2}\right] + \\
 & \quad 49980 C \sin\left[4c + \frac{5dx}{2}\right] - 5890 A \sin\left[2c + \frac{7dx}{2}\right] - 64053 C \sin\left[2c + \frac{7dx}{2}\right] + \\
 & \quad 1470 A \sin\left[3c + \frac{7dx}{2}\right] - 3885 C \sin\left[3c + \frac{7dx}{2}\right] - 5890 A \sin\left[4c + \frac{7dx}{2}\right] - \\
 & \quad 44733 C \sin\left[4c + \frac{7dx}{2}\right] + 1470 A \sin\left[5c + \frac{7dx}{2}\right] + 15435 C \sin\left[5c + \frac{7dx}{2}\right] - \\
 & \quad 2030 A \sin\left[3c + \frac{9dx}{2}\right] - 21987 C \sin\left[3c + \frac{9dx}{2}\right] + 210 A \sin\left[4c + \frac{9dx}{2}\right] - 3675 C \\
 & \quad \sin\left[4c + \frac{9dx}{2}\right] - 2030 A \sin\left[5c + \frac{9dx}{2}\right] - 16107 C \sin\left[5c + \frac{9dx}{2}\right] + 210 A \sin\left[6c + \frac{9dx}{2}\right] + \\
 & \quad 2205 C \sin\left[6c + \frac{9dx}{2}\right] - 320 A \sin\left[4c + \frac{11dx}{2}\right] - 3456 C \sin\left[4c + \frac{11dx}{2}\right] - \\
 & \quad \left. 840 C \sin\left[5c + \frac{11dx}{2}\right] - 320 A \sin\left[6c + \frac{11dx}{2}\right] - 2616 C \sin\left[6c + \frac{11dx}{2}\right] \right)
 \end{aligned}$$

**Problem 147: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec[c + dx]^4 (A + C \sec[c + dx]^2)}{(a + a \sec[c + dx])^4} dx$$

Optimal (type 3, 183 leaves, 8 steps):

$$-\frac{4 C \operatorname{ArcTanh}[\operatorname{Sin}[c+d x]]}{a^4 d} + \frac{2(3 A+122 C) \operatorname{Tan}[c+d x]}{105 a^4 d} + \frac{(3 A-88 C) \operatorname{Sec}[c+d x]^2 \operatorname{Tan}[c+d x]}{105 a^4 d(1+\operatorname{Sec}[c+d x])^2} +$$

$$\frac{4 C \operatorname{Tan}[c+d x]}{a^4 d(1+\operatorname{Sec}[c+d x])} - \frac{(A+C) \operatorname{Sec}[c+d x]^4 \operatorname{Tan}[c+d x]}{7 d(a+a \operatorname{Sec}[c+d x])^4} + \frac{2(A-6 C) \operatorname{Sec}[c+d x]^3 \operatorname{Tan}[c+d x]}{35 a d(a+a \operatorname{Sec}[c+d x])^3}$$

Result (type 3, 544 leaves):

$$\frac{1}{840 a^4 d(A+2 C+A \operatorname{Cos}[2(c+d x)])(1+\operatorname{Sec}[c+d x])^4}$$

$$\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] \operatorname{Sec}[c+d x]^2(A+C \operatorname{Sec}[c+d x]^2)\left(107520 C \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^7\right.$$

$$\left.\left(\operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]-\operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]\right)+$$

$$\operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c] \operatorname{Sec}[c+d x]\left(-70(3 A+154 C) \operatorname{Sin}\left[\frac{d x}{2}\right]+28(9 A+671 C) \operatorname{Sin}\left[\frac{3 d x}{2}\right]-\right.$$

$$126 A \operatorname{Sin}\left[c-\frac{d x}{2}\right]-20524 C \operatorname{Sin}\left[c-\frac{d x}{2}\right]+126 A \operatorname{Sin}\left[c+\frac{d x}{2}\right]+14644 C \operatorname{Sin}\left[c+\frac{d x}{2}\right]-$$

$$210 A \operatorname{Sin}\left[2 c+\frac{d x}{2}\right]-16660 C \operatorname{Sin}\left[2 c+\frac{d x}{2}\right]-4690 C \operatorname{Sin}\left[c+\frac{3 d x}{2}\right]+$$

$$252 A \operatorname{Sin}\left[2 c+\frac{3 d x}{2}\right]+14378 C \operatorname{Sin}\left[2 c+\frac{3 d x}{2}\right]-9100 C \operatorname{Sin}\left[3 c+\frac{3 d x}{2}\right]+$$

$$132 A \operatorname{Sin}\left[c+\frac{5 d x}{2}\right]+11668 C \operatorname{Sin}\left[c+\frac{5 d x}{2}\right]-630 C \operatorname{Sin}\left[2 c+\frac{5 d x}{2}\right]+$$

$$132 A \operatorname{Sin}\left[3 c+\frac{5 d x}{2}\right]+9358 C \operatorname{Sin}\left[3 c+\frac{5 d x}{2}\right]-2940 C \operatorname{Sin}\left[4 c+\frac{5 d x}{2}\right]+$$

$$42 A \operatorname{Sin}\left[2 c+\frac{7 d x}{2}\right]+4228 C \operatorname{Sin}\left[2 c+\frac{7 d x}{2}\right]+315 C \operatorname{Sin}\left[3 c+\frac{7 d x}{2}\right]+$$

$$42 A \operatorname{Sin}\left[4 c+\frac{7 d x}{2}\right]+3493 C \operatorname{Sin}\left[4 c+\frac{7 d x}{2}\right]-420 C \operatorname{Sin}\left[5 c+\frac{7 d x}{2}\right]+6 A \operatorname{Sin}\left[3 c+\frac{9 d x}{2}\right]+$$

$$664 C \operatorname{Sin}\left[3 c+\frac{9 d x}{2}\right]+105 C \operatorname{Sin}\left[4 c+\frac{9 d x}{2}\right]+6 A \operatorname{Sin}\left[5 c+\frac{9 d x}{2}\right]+559 C \operatorname{Sin}\left[5 c+\frac{9 d x}{2}\right]\left.\right)$$

**Problem 151: Result more than twice size of optimal antiderivative.**

$$\int \frac{A+C \operatorname{Sec}[c+d x]^2}{(a+a \operatorname{Sec}[c+d x])^4} dx$$

Optimal (type 3, 136 leaves, 5 steps):

$$\frac{A x}{a^4} - \frac{(55 A-8 C) \operatorname{Tan}[c+d x]}{105 a^4 d(1+\operatorname{Sec}[c+d x])^2} - \frac{8(20 A-C) \operatorname{Tan}[c+d x]}{105 a^4 d(1+\operatorname{Sec}[c+d x])} -$$

$$\frac{(A+C) \operatorname{Tan}[c+d x]}{7 d(a+a \operatorname{Sec}[c+d x])^4} - \frac{2(5 A-2 C) \operatorname{Tan}[c+d x]}{35 a d(a+a \operatorname{Sec}[c+d x])^3}$$

Result (type 3, 315 leaves):

$$\frac{1}{13440 a^4 d} \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^7 \left( 3675 A dx \operatorname{Cos}\left[\frac{dx}{2}\right] + 3675 A dx \operatorname{Cos}\left[c + \frac{dx}{2}\right] + 2205 A dx \operatorname{Cos}\left[c + \frac{3dx}{2}\right] + \right. \\ \left. 2205 A dx \operatorname{Cos}\left[2c + \frac{3dx}{2}\right] + 735 A dx \operatorname{Cos}\left[2c + \frac{5dx}{2}\right] + 735 A dx \operatorname{Cos}\left[3c + \frac{5dx}{2}\right] + \right. \\ \left. 105 A dx \operatorname{Cos}\left[3c + \frac{7dx}{2}\right] + 105 A dx \operatorname{Cos}\left[4c + \frac{7dx}{2}\right] - 9940 A \operatorname{Sin}\left[\frac{dx}{2}\right] + 560 C \operatorname{Sin}\left[\frac{dx}{2}\right] + \right. \\ \left. 8260 A \operatorname{Sin}\left[c + \frac{dx}{2}\right] - 350 C \operatorname{Sin}\left[c + \frac{dx}{2}\right] - 7140 A \operatorname{Sin}\left[c + \frac{3dx}{2}\right] + 336 C \operatorname{Sin}\left[c + \frac{3dx}{2}\right] + \right. \\ \left. 3780 A \operatorname{Sin}\left[2c + \frac{3dx}{2}\right] - 210 C \operatorname{Sin}\left[2c + \frac{3dx}{2}\right] - 2800 A \operatorname{Sin}\left[2c + \frac{5dx}{2}\right] + \right. \\ \left. 182 C \operatorname{Sin}\left[2c + \frac{5dx}{2}\right] + 840 A \operatorname{Sin}\left[3c + \frac{5dx}{2}\right] - 520 A \operatorname{Sin}\left[3c + \frac{7dx}{2}\right] + 26 C \operatorname{Sin}\left[3c + \frac{7dx}{2}\right] \right)$$

**Problem 152: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Cos}[c+dx] (A+C \operatorname{Sec}[c+dx]^2)}{(a+a \operatorname{Sec}[c+dx])^4} dx$$

Optimal (type 3, 152 leaves, 7 steps):

$$-\frac{4Ax}{a^4} + \frac{2(332A+3C) \operatorname{Sin}[c+dx]}{105a^4d} - \frac{(88A-3C) \operatorname{Sin}[c+dx]}{105a^4d(1+\operatorname{Sec}[c+dx])^2} - \\ \frac{4A \operatorname{Sin}[c+dx]}{a^4d(1+\operatorname{Sec}[c+dx])} - \frac{(A+C) \operatorname{Sin}[c+dx]}{7d(a+a \operatorname{Sec}[c+dx])^4} - \frac{2(6A-C) \operatorname{Sin}[c+dx]}{35ad(a+a \operatorname{Sec}[c+dx])^3}$$

Result (type 3, 371 leaves):

$$-\frac{1}{26880 a^4 d} \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^7 \left( 29400 A dx \operatorname{Cos}\left[\frac{dx}{2}\right] + 29400 A dx \operatorname{Cos}\left[c + \frac{dx}{2}\right] + 17640 A dx \operatorname{Cos}\left[c + \frac{3dx}{2}\right] + \right. \\ \left. 17640 A dx \operatorname{Cos}\left[2c + \frac{3dx}{2}\right] + 5880 A dx \operatorname{Cos}\left[2c + \frac{5dx}{2}\right] + 5880 A dx \operatorname{Cos}\left[3c + \frac{5dx}{2}\right] + \right. \\ \left. 840 A dx \operatorname{Cos}\left[3c + \frac{7dx}{2}\right] + 840 A dx \operatorname{Cos}\left[4c + \frac{7dx}{2}\right] - 60830 A \operatorname{Sin}\left[\frac{dx}{2}\right] - \right. \\ \left. 2520 C \operatorname{Sin}\left[\frac{dx}{2}\right] + 46130 A \operatorname{Sin}\left[c + \frac{dx}{2}\right] + 2520 C \operatorname{Sin}\left[c + \frac{dx}{2}\right] - 46116 A \operatorname{Sin}\left[c + \frac{3dx}{2}\right] - \right. \\ \left. 1764 C \operatorname{Sin}\left[c + \frac{3dx}{2}\right] + 18060 A \operatorname{Sin}\left[2c + \frac{3dx}{2}\right] + 1260 C \operatorname{Sin}\left[2c + \frac{3dx}{2}\right] - \right. \\ \left. 19292 A \operatorname{Sin}\left[2c + \frac{5dx}{2}\right] - 588 C \operatorname{Sin}\left[2c + \frac{5dx}{2}\right] + 2100 A \operatorname{Sin}\left[3c + \frac{5dx}{2}\right] + \right. \\ \left. 420 C \operatorname{Sin}\left[3c + \frac{5dx}{2}\right] - 3791 A \operatorname{Sin}\left[3c + \frac{7dx}{2}\right] - 144 C \operatorname{Sin}\left[3c + \frac{7dx}{2}\right] - \right. \\ \left. 735 A \operatorname{Sin}\left[4c + \frac{7dx}{2}\right] - 105 A \operatorname{Sin}\left[4c + \frac{9dx}{2}\right] - 105 A \operatorname{Sin}\left[5c + \frac{9dx}{2}\right] \right)$$

### Problem 153: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^2 (A+C \operatorname{Sec}[c+d x]^2)}{(a+a \operatorname{Sec}[c+d x])^4} dx$$

Optimal (type 3, 215 leaves, 8 steps):

$$\frac{(21 A+2 C) x}{2 a^4} - \frac{32 (54 A+5 C) \sin [c+d x]}{105 a^4 d} + \frac{(21 A+2 C) \cos [c+d x] \sin [c+d x]}{2 a^4 d} -$$

$$\frac{(129 A+10 C) \cos [c+d x] \sin [c+d x]}{105 a^4 d (1+\operatorname{Sec}[c+d x])^2} - \frac{16 (54 A+5 C) \cos [c+d x] \sin [c+d x]}{105 a^4 d (1+\operatorname{Sec}[c+d x])} -$$

$$\frac{(A+C) \cos [c+d x] \sin [c+d x]}{7 d (a+a \operatorname{Sec}[c+d x])^4} - \frac{2 A \cos [c+d x] \sin [c+d x]}{5 a d (a+a \operatorname{Sec}[c+d x])^3}$$

Result (type 3, 505 leaves):

$$\frac{1}{107520 a^4 d} \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^7$$

$$\left(14700 (21 A+2 C) d x \cos \left[\frac{d x}{2}\right] + 14700 (21 A+2 C) d x \cos \left[c+\frac{d x}{2}\right] + 185220 A d x \cos \left[c+\frac{3 d x}{2}\right] +\right.$$

$$17640 C d x \cos \left[c+\frac{3 d x}{2}\right] + 185220 A d x \cos \left[2 c+\frac{3 d x}{2}\right] + 17640 C d x \cos \left[2 c+\frac{3 d x}{2}\right] +$$

$$61740 A d x \cos \left[2 c+\frac{5 d x}{2}\right] + 5880 C d x \cos \left[2 c+\frac{5 d x}{2}\right] + 61740 A d x \cos \left[3 c+\frac{5 d x}{2}\right] +$$

$$5880 C d x \cos \left[3 c+\frac{5 d x}{2}\right] + 8820 A d x \cos \left[3 c+\frac{7 d x}{2}\right] + 840 C d x \cos \left[3 c+\frac{7 d x}{2}\right] +$$

$$8820 A d x \cos \left[4 c+\frac{7 d x}{2}\right] + 840 C d x \cos \left[4 c+\frac{7 d x}{2}\right] - 539490 A \sin \left[\frac{d x}{2}\right] - 79520 C \sin \left[\frac{d x}{2}\right] +$$

$$386190 A \sin \left[c+\frac{d x}{2}\right] + 66080 C \sin \left[c+\frac{d x}{2}\right] - 422478 A \sin \left[c+\frac{3 d x}{2}\right] - 57120 C \sin \left[c+\frac{3 d x}{2}\right] +$$

$$132930 A \sin \left[2 c+\frac{3 d x}{2}\right] + 30240 C \sin \left[2 c+\frac{3 d x}{2}\right] - 181461 A \sin \left[2 c+\frac{5 d x}{2}\right] -$$

$$22400 C \sin \left[2 c+\frac{5 d x}{2}\right] + 3675 A \sin \left[3 c+\frac{5 d x}{2}\right] + 6720 C \sin \left[3 c+\frac{5 d x}{2}\right] -$$

$$36003 A \sin \left[3 c+\frac{7 d x}{2}\right] - 4160 C \sin \left[3 c+\frac{7 d x}{2}\right] - 9555 A \sin \left[4 c+\frac{7 d x}{2}\right] -$$

$$945 A \sin \left[4 c+\frac{9 d x}{2}\right] - 945 A \sin \left[5 c+\frac{9 d x}{2}\right] + 105 A \sin \left[5 c+\frac{11 d x}{2}\right] + 105 A \sin \left[6 c+\frac{11 d x}{2}\right] \left.)\right)$$

### Problem 154: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^3 (A+C \operatorname{Sec}[c+d x]^2)}{(a+a \operatorname{Sec}[c+d x])^4} dx$$

Optimal (type 3, 248 leaves, 9 steps):

$$\begin{aligned}
 & - \frac{2(11A+2C)x}{a^4} + \frac{4(454A+83C)\sin[c+dx]}{35a^4d} - \\
 & \frac{2(11A+2C)\cos[c+dx]\sin[c+dx]}{a^4d} - \frac{(178A+31C)\cos[c+dx]^2\sin[c+dx]}{105a^4d(1+\sec[c+dx])^2} - \\
 & \frac{4(11A+2C)\cos[c+dx]^2\sin[c+dx]}{3a^4d(1+\sec[c+dx])} - \frac{(A+C)\cos[c+dx]^2\sin[c+dx]}{7d(a+a\sec[c+dx])^4} - \\
 & \frac{2(8A+C)\cos[c+dx]^2\sin[c+dx]}{35ad(a+a\sec[c+dx])^3} - \frac{4(454A+83C)\sin[c+dx]^3}{105a^4d}
 \end{aligned}$$

Result (type 3, 575 leaves):

$$\begin{aligned}
 & - \frac{1}{107520a^4d} \\
 & \sec\left[\frac{c}{2}\right] \sec\left[\frac{1}{2}(c+dx)\right]^7 \left( 58800(11A+2C)dx \cos\left[\frac{dx}{2}\right] + 58800(11A+2C)dx \cos\left[c+\frac{dx}{2}\right] + \right. \\
 & 388080Adx \cos\left[c+\frac{3dx}{2}\right] + 70560Cdx \cos\left[c+\frac{3dx}{2}\right] + 388080Adx \cos\left[2c+\frac{3dx}{2}\right] + \\
 & 70560Cdx \cos\left[2c+\frac{3dx}{2}\right] + 129360Adx \cos\left[2c+\frac{5dx}{2}\right] + 23520Cdx \cos\left[2c+\frac{5dx}{2}\right] + \\
 & 129360Adx \cos\left[3c+\frac{5dx}{2}\right] + 23520Cdx \cos\left[3c+\frac{5dx}{2}\right] + 18480Adx \cos\left[3c+\frac{7dx}{2}\right] + \\
 & 3360Cdx \cos\left[3c+\frac{7dx}{2}\right] + 18480Adx \cos\left[4c+\frac{7dx}{2}\right] + 3360Cdx \cos\left[4c+\frac{7dx}{2}\right] - \\
 & 1010660A \sin\left[\frac{dx}{2}\right] - 243320C \sin\left[\frac{dx}{2}\right] + 687260A \sin\left[c+\frac{dx}{2}\right] + \\
 & 184520C \sin\left[c+\frac{dx}{2}\right] - 814107A \sin\left[c+\frac{3dx}{2}\right] - 184464C \sin\left[c+\frac{3dx}{2}\right] + \\
 & 204645A \sin\left[2c+\frac{3dx}{2}\right] + 72240C \sin\left[2c+\frac{3dx}{2}\right] - 357609A \sin\left[2c+\frac{5dx}{2}\right] - \\
 & 77168C \sin\left[2c+\frac{5dx}{2}\right] - 18025A \sin\left[3c+\frac{5dx}{2}\right] + 8400C \sin\left[3c+\frac{5dx}{2}\right] - \\
 & 72522A \sin\left[3c+\frac{7dx}{2}\right] - 15164C \sin\left[3c+\frac{7dx}{2}\right] - 24010A \sin\left[4c+\frac{7dx}{2}\right] - \\
 & 2940C \sin\left[4c+\frac{7dx}{2}\right] - 2310A \sin\left[4c+\frac{9dx}{2}\right] - 420C \sin\left[4c+\frac{9dx}{2}\right] - \\
 & 2310A \sin\left[5c+\frac{9dx}{2}\right] - 420C \sin\left[5c+\frac{9dx}{2}\right] + 175A \sin\left[5c+\frac{11dx}{2}\right] + \\
 & \left. 175A \sin\left[6c+\frac{11dx}{2}\right] - 35A \sin\left[6c+\frac{13dx}{2}\right] - 35A \sin\left[7c+\frac{13dx}{2}\right] \right)
 \end{aligned}$$

**Problem 160: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c+dx] \sqrt{a+a\sec[c+dx]} (A+C\sec[c+dx]^2) dx$$

Optimal (type 3, 94 leaves, 5 steps):

$$\frac{\sqrt{a} A \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{d} + \frac{A \sqrt{a+a \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{d} - \frac{a(A-2C) \operatorname{Tan}[c+dx]}{d \sqrt{a+a \operatorname{Sec}[c+dx]}}$$

Result (type 4, 398 leaves):

$$\begin{aligned} & \frac{1}{d} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1+\operatorname{Sec}[c+dx])} \left(\frac{1}{2}(-A+4C) \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + \frac{1}{2} A \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right]\right) - \\ & \frac{1}{d} 4(-3-2\sqrt{2}) A \operatorname{Cos}\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7-5\sqrt{2}+(10-7\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}{1+\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}} \\ & \sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}{1+\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}} \left(1-\sqrt{2}+(-2+\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \\ & \left(\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] + \right. \\ & \left. 2 \operatorname{EllipticPi}\left[-3+2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right]\right) \\ & \sqrt{\left(-1-\sqrt{2}+(2+\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]} \\ & \operatorname{Sec}[c+dx] \sqrt{a(1+\operatorname{Sec}[c+dx])} \sqrt{3-2\sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \end{aligned}$$

**Problem 161: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \operatorname{Cos}[c+dx]^2 \sqrt{a+a \operatorname{Sec}[c+dx]} (A+C \operatorname{Sec}[c+dx])^2 dx$$

Optimal (type 3, 110 leaves, 4 steps):

$$\frac{\sqrt{a}(3A+8C) \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{4d} + \frac{aA \operatorname{Sin}[c+dx]}{4d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{A \operatorname{Cos}[c+dx] \sqrt{a+a \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{2d}$$

Result (type 4, 410 leaves):

$$\begin{aligned}
 & \frac{1}{d} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1+\operatorname{Sec}[c+dx])} \\
 & \left(-\frac{1}{8}A \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + \frac{1}{4}A \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right] + \frac{1}{8}A \operatorname{Sin}\left[\frac{5}{2}(c+dx)\right]\right) + \\
 & \frac{1}{d} \left(2 + \frac{3}{\sqrt{2}}\right) (3A+8C) \operatorname{Cos}\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7-5\sqrt{2}+(10-7\sqrt{2})\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}{1+\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}} \\
 & \left(1-\sqrt{2}+(-2+\sqrt{2})\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \left(\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] + \right. \\
 & \left. 2 \operatorname{EllipticPi}\left[-3+2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right]\right) \\
 & \sqrt{\left(-1+\sqrt{2}-(-2+\sqrt{2})\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \sqrt{\left(-1-\sqrt{2}+(2+\sqrt{2})\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]} \\
 & \operatorname{Sec}[c+dx] \sqrt{a(1+\operatorname{Sec}[c+dx])} \sqrt{3-2\sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}
 \end{aligned}$$

**Problem 162: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \operatorname{Cos}[c+dx]^3 \sqrt{a+a \operatorname{Sec}[c+dx]} (A+C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 3, 153 leaves, 5 steps):

$$\begin{aligned}
 & \frac{\sqrt{a} (5A+8C) \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{8d} + \frac{a (5A+8C) \operatorname{Sin}[c+dx]}{8d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \\
 & \frac{a A \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx]}{12d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{A \operatorname{Cos}[c+dx]^2 \sqrt{a+a \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{3d}
 \end{aligned}$$

Result (type 4, 439 leaves):

$$\begin{aligned} & \frac{1}{d} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1+\operatorname{Sec}[c+dx])} \left( -\frac{1}{48}(11A+24C) \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + \right. \\ & \quad \left. \frac{1}{6}(2A+3C) \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right] + \frac{1}{16}A \operatorname{Sin}\left[\frac{5}{2}(c+dx)\right] + \frac{1}{24}A \operatorname{Sin}\left[\frac{7}{2}(c+dx)\right] \right) + \\ & \frac{1}{d} \left( 1 + \frac{3}{2\sqrt{2}} \right) (5A+8C) \operatorname{Cos}\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7-5\sqrt{2}+(10-7\sqrt{2})\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}{1+\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}} \\ & \left( 1 - \sqrt{2} + (-2+\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \right) \left( \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] + \right. \\ & \quad \left. 2 \operatorname{EllipticPi}\left[-3+2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \right) \\ & \sqrt{\left( -1 + \sqrt{2} - (-2+\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2} \\ & \sqrt{\left( -1 - \sqrt{2} + (2+\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]} \\ & \operatorname{Sec}[c+dx] \sqrt{a(1+\operatorname{Sec}[c+dx])} \sqrt{3-2\sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \end{aligned}$$

**Problem 163: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \operatorname{Cos}[c+dx]^4 \sqrt{a+a \operatorname{Sec}[c+dx]} (A+C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 3, 196 leaves, 6 steps):

$$\begin{aligned} & \frac{\sqrt{a} (35A+48C) \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{64d} + \\ & \frac{a(35A+48C) \operatorname{Sin}[c+dx]}{64d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{a(35A+48C) \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx]}{96d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \\ & \frac{aA \operatorname{Cos}[c+dx]^2 \operatorname{Sin}[c+dx]}{24d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{A \operatorname{Cos}[c+dx]^3 \sqrt{a+a \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{4d} \end{aligned}$$

Result (type 4, 460 leaves):



$$\begin{aligned}
 & \frac{1}{d} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1+\operatorname{Sec}[c+dx])} \\
 & \left(-\frac{1}{384}(41A+48C) \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + \frac{1}{48}(11A+12C) \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right] + \right. \\
 & \quad \left. \frac{1}{128}(15A+16C) \operatorname{Sin}\left[\frac{5}{2}(c+dx)\right] + \frac{1}{48}A \operatorname{Sin}\left[\frac{7}{2}(c+dx)\right] + \frac{1}{64}A \operatorname{Sin}\left[\frac{9}{2}(c+dx)\right]\right) + \\
 & \frac{1}{(-64+48\sqrt{2})d} (35A+48C) \operatorname{Cos}\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7-5\sqrt{2}+(10-7\sqrt{2})\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}{1+\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}} \\
 & \left(1-\sqrt{2}+(-2+\sqrt{2})\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \left(\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] + \right. \\
 & \quad \left. 2 \operatorname{EllipticPi}\left[-3+2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right]\right) \\
 & \sqrt{\left(-1+\sqrt{2}-(-2+\sqrt{2})\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \sqrt{\left(-1-\sqrt{2}+(2+\sqrt{2})\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]} \\
 & \operatorname{Sec}[c+dx] \sqrt{a(1+\operatorname{Sec}[c+dx])} \sqrt{3-2\sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}
 \end{aligned}$$

**Problem 169: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \operatorname{Cos}[c+dx]^2 (a+a \operatorname{Sec}[c+dx])^{3/2} (A+C \operatorname{Sec}[c+dx])^2 dx$$

Optimal (type 3, 151 leaves, 5 steps):

$$\begin{aligned}
 & \frac{a^{3/2} (7A+8C) \operatorname{ArcTan}\left[\frac{-\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{4d} + \frac{a^2 (5A-8C) \operatorname{Sin}[c+dx]}{4d \sqrt{a+a \operatorname{Sec}[c+dx]}} - \\
 & \frac{a(A-4C) \sqrt{a+a \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{2d} + \frac{A \operatorname{Cos}[c+dx] (a+a \operatorname{Sec}[c+dx])^{3/2} \operatorname{Sin}[c+dx]}{2d}
 \end{aligned}$$

Result (type 4, 424 leaves):

$$\begin{aligned} & \frac{1}{2} \left( \frac{1}{d} \cos [c+d x] \operatorname{Sec} \left[ \frac{1}{2} (c+d x) \right]^3 (a (1+\operatorname{Sec} [c+d x]))^{3/2} \right. \\ & \quad \left. \left( -\frac{1}{8} (5 A-16 C) \sin \left[ \frac{1}{2} (c+d x) \right] + \frac{3}{4} A \sin \left[ \frac{3}{2} (c+d x) \right] + \frac{1}{8} A \sin \left[ \frac{5}{2} (c+d x) \right] \right) + \right. \\ & \quad \frac{1}{d} \left( 2 + \frac{3}{\sqrt{2}} \right) (7 A+8 C) \cos \left[ \frac{1}{4} (c+d x) \right]^4 \sqrt{\frac{7-5 \sqrt{2}+(10-7 \sqrt{2}) \cos \left[ \frac{1}{2} (c+d x) \right]}{1+\cos \left[ \frac{1}{2} (c+d x) \right]}} \\ & \quad \left( 1-\sqrt{2}+(-2+\sqrt{2}) \cos \left[ \frac{1}{2} (c+d x) \right] \right) \left( \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\operatorname{Tan} \left[ \frac{1}{4} (c+d x) \right]}{\sqrt{3-2 \sqrt{2}}} \right], 17-12 \sqrt{2} \right] + \right. \\ & \quad \left. 2 \operatorname{EllipticPi} \left[ -3+2 \sqrt{2}, -\operatorname{ArcSin} \left[ \frac{\operatorname{Tan} \left[ \frac{1}{4} (c+d x) \right]}{\sqrt{3-2 \sqrt{2}}} \right], 17-12 \sqrt{2} \right] \right) \\ & \quad \sqrt{\left( -1+\sqrt{2}-(-2+\sqrt{2}) \cos \left[ \frac{1}{2} (c+d x) \right] \right) \operatorname{Sec} \left[ \frac{1}{4} (c+d x) \right]^2} \\ & \quad \sqrt{\left( -1-\sqrt{2}+(2+\sqrt{2}) \cos \left[ \frac{1}{2} (c+d x) \right] \right) \operatorname{Sec} \left[ \frac{1}{4} (c+d x) \right]^2} \\ & \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c+d x) \right]^3 (a (1+\operatorname{Sec} [c+d x]))^{3/2} \sqrt{3-2 \sqrt{2}-\operatorname{Tan} \left[ \frac{1}{4} (c+d x) \right]^2} \right) \end{aligned}$$

**Problem 171: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c+d x]^4 (a+a \operatorname{Sec} [c+d x])^{3/2} (A+C \operatorname{Sec} [c+d x]^2) dx$$

Optimal (type 3, 200 leaves, 6 steps):

$$\begin{aligned} & \frac{a^{3/2} (75 A+112 C) \operatorname{ArcTan} \left[ \frac{\sqrt{a} \operatorname{Tan} [c+d x]}{\sqrt{a+a \operatorname{Sec} [c+d x]}} \right]}{64 d} + \frac{a^2 (75 A+112 C) \sin [c+d x]}{64 d \sqrt{a+a \operatorname{Sec} [c+d x]}} + \\ & \frac{a^2 (13 A+16 C) \cos [c+d x] \sin [c+d x]}{32 d \sqrt{a+a \operatorname{Sec} [c+d x]}} + \frac{a A \cos [c+d x]^2 \sqrt{a+a \operatorname{Sec} [c+d x]} \sin [c+d x]}{8 d} + \\ & \frac{A \cos [c+d x]^3 (a+a \operatorname{Sec} [c+d x])^{3/2} \sin [c+d x]}{4 d} \end{aligned}$$

Result (type 4, 534 leaves):

$$\begin{aligned}
 & \left( \cos [c + d x]^3 \sec \left[ \frac{1}{2} (c + d x) \right]^3 (a (1 + \sec [c + d x]))^{3/2} (A + C \sec [c + d x]^2) \right. \\
 & \quad \left( -\frac{1}{128} (43 A + 80 C) \sin \left[ \frac{1}{2} (c + d x) \right] + \frac{3}{16} (3 A + 4 C) \sin \left[ \frac{3}{2} (c + d x) \right] + \right. \\
 & \quad \left. \frac{1}{128} (23 A + 16 C) \sin \left[ \frac{5}{2} (c + d x) \right] + \frac{1}{16} A \sin \left[ \frac{7}{2} (c + d x) \right] + \frac{1}{64} A \sin \left[ \frac{9}{2} (c + d x) \right] \right) / \\
 & \quad (d (A + 2 C + A \cos [2 c + 2 d x])) + \frac{1}{(-64 + 48 \sqrt{2}) d (A + 2 C + A \cos [2 c + 2 d x])} \\
 & \quad (75 A + 112 C) \cos \left[ \frac{1}{4} (c + d x) \right]^4 \sqrt{\frac{7 - 5 \sqrt{2} + (10 - 7 \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right]}{1 + \cos \left[ \frac{1}{2} (c + d x) \right]}} \\
 & \quad \left( 1 - \sqrt{2} + (-2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right] \right) \cos [c + d x]^2 \\
 & \quad \left( \text{EllipticF} \left[ \text{ArcSin} \left[ \frac{\tan \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] + \right. \\
 & \quad \left. 2 \text{EllipticPi} \left[ -3 + 2 \sqrt{2}, -\text{ArcSin} \left[ \frac{\tan \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \right) \\
 & \quad \sqrt{\left( -1 + \sqrt{2} - (-2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right] \right) \sec \left[ \frac{1}{4} (c + d x) \right]^2} \\
 & \quad \sqrt{\left( -1 - \sqrt{2} + (2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right] \right) \sec \left[ \frac{1}{4} (c + d x) \right]^2 \sec \left[ \frac{1}{2} (c + d x) \right]^3} \\
 & \quad (a (1 + \sec [c + d x]))^{3/2} (A + C \sec [c + d x]^2) \sqrt{3 - 2 \sqrt{2} - \tan \left[ \frac{1}{4} (c + d x) \right]^2}
 \end{aligned}$$

**Problem 172:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \cos [c + d x]^5 (a + a \sec [c + d x])^{3/2} (A + C \sec [c + d x]^2) dx$$

Optimal (type 3, 245 leaves, 7 steps):

$$\frac{a^{3/2} (133 A + 176 C) \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{128 d} +$$

$$\frac{a^2 (133 A + 176 C) \operatorname{Sin}[c+dx]}{128 d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{a^2 (133 A + 176 C) \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx]}{192 d \sqrt{a+a \operatorname{Sec}[c+dx]}} +$$

$$\frac{a^2 (67 A + 80 C) \operatorname{Cos}[c+dx]^2 \operatorname{Sin}[c+dx]}{240 d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{3 a A \operatorname{Cos}[c+dx]^3 \sqrt{a+a \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{40 d} +$$

$$\frac{A \operatorname{Cos}[c+dx]^4 (a+a \operatorname{Sec}[c+dx])^{3/2} \operatorname{Sin}[c+dx]}{5 d}$$

Result(type 4, 556 leaves):

$$\left( \operatorname{Cos}[c+dx]^3 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^3 (a(1+\operatorname{Sec}[c+dx]))^{3/2} (A+C \operatorname{Sec}[c+dx]^2) \right.$$

$$\left. \left( -\frac{(1019 A + 1360 C) \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]}{3840} + \frac{1}{480} (239 A + 280 C) \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right] + \right.$$

$$\frac{1}{256} (49 A + 48 C) \operatorname{Sin}\left[\frac{5}{2}(c+dx)\right] + \frac{1}{240} (17 A + 10 C) \operatorname{Sin}\left[\frac{7}{2}(c+dx)\right] +$$

$$\left. \left. \frac{3}{128} A \operatorname{Sin}\left[\frac{9}{2}(c+dx)\right] + \frac{1}{160} A \operatorname{Sin}\left[\frac{11}{2}(c+dx)\right] \right) \right) / (d(A+2C+A \operatorname{Cos}[2c+2dx])) +$$

$$\frac{1}{64 d (A+2C+A \operatorname{Cos}[2c+2dx])} (4+3\sqrt{2}) (133 A + 176 C) \operatorname{Cos}\left[\frac{1}{4}(c+dx)\right]^4$$

$$\sqrt{\frac{7-5\sqrt{2}+(10-7\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}{1+\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}} \left( (1-\sqrt{2}+(-2+\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]) \right.$$

$$\operatorname{Cos}[c+dx]^2 \left( \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] + \right.$$

$$\left. \left. 2 \operatorname{EllipticPi}\left[-3+2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \right) \right)$$

$$\sqrt{\left( -1+\sqrt{2}-(-2+\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2}$$

$$\sqrt{\left( -1-\sqrt{2}+(2+\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^3}$$

$$(a(1+\operatorname{Sec}[c+dx]))^{3/2} (A+C \operatorname{Sec}[c+dx]^2) \sqrt{3-2\sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}$$

**Problem 178: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c + d x]^2 (a + a \sec [c + d x])^{5/2} (A + C \sec [c + d x]^2) dx$$

Optimal (type 3, 188 leaves, 6 steps):

$$\frac{a^{5/2} (19 A + 8 C) \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \sec [c+dx]}}\right]}{4 d} +$$

$$\frac{a^3 (27 A - 56 C) \operatorname{Sin}[c + d x]}{12 d \sqrt{a + a \sec [c + d x]}} - \frac{a^2 (A - 8 C) \sqrt{a + a \sec [c + d x]} \operatorname{Sin}[c + d x]}{2 d} -$$

$$\frac{a (3 A - 4 C) (a + a \sec [c + d x])^{3/2} \operatorname{Sin}[c + d x]}{6 d} + \frac{A \cos [c + d x] (a + a \sec [c + d x])^{5/2} \operatorname{Sin}[c + d x]}{2 d}$$

Result (type 4, 455 leaves):

$$\frac{1}{2}$$

$$\left( \frac{1}{d} \cos [c + d x]^2 \sec \left[ \frac{1}{2} (c + d x) \right]^5 (a (1 + \sec [c + d x]))^{5/2} \left( -\frac{1}{48} (27 A - 128 C) \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] + \frac{1}{3} \right. \right.$$

$$\left. \left. C \sec [c + d x] \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] + \frac{5}{8} A \operatorname{Sin} \left[ \frac{3}{2} (c + d x) \right] + \frac{1}{16} A \operatorname{Sin} \left[ \frac{5}{2} (c + d x) \right] \right) +$$

$$\frac{1}{d} \left( 1 + \frac{3}{2 \sqrt{2}} \right) (19 A + 8 C) \cos \left[ \frac{1}{4} (c + d x) \right]^4 \sqrt{\frac{7 - 5 \sqrt{2} + (10 - 7 \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right]}{1 + \cos \left[ \frac{1}{2} (c + d x) \right]}}$$

$$\left( 1 - \sqrt{2} + (-2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right] \right) \cos [c + d x] \left( \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], \right. \right.$$

$$\left. \left. 17 - 12 \sqrt{2} \right] + 2 \operatorname{EllipticPi} \left[ -3 + 2 \sqrt{2}, -\operatorname{ArcSin} \left[ \frac{\operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \right)$$

$$\sqrt{\left( -1 + \sqrt{2} - (-2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right] \right) \sec \left[ \frac{1}{4} (c + d x) \right]^2}$$

$$\sqrt{\left( -1 - \sqrt{2} + (2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right] \right) \sec \left[ \frac{1}{4} (c + d x) \right]^2}$$

$$\left. \sec \left[ \frac{1}{2} (c + d x) \right]^5 (a (1 + \sec [c + d x]))^{5/2} \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \right)$$

**Problem 180: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c + d x]^4 (a + a \operatorname{Sec} [c + d x])^{5/2} (A + C \operatorname{Sec} [c + d x]^2) dx$$

Optimal (type 3, 200 leaves, 6 steps):

$$\frac{a^{5/2} (163 A + 304 C) \operatorname{ArcTan} \left[ \frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}} \right]}{64 d} + \frac{a^3 (299 A + 432 C) \operatorname{Sin}[c + d x]}{192 d \sqrt{a + a \operatorname{Sec}[c + d x]}} +$$

$$\frac{a^2 (17 A + 16 C) \operatorname{Cos}[c + d x] \sqrt{a + a \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{32 d} +$$

$$\frac{5 a A \operatorname{Cos}[c + d x]^2 (a + a \operatorname{Sec}[c + d x])^{3/2} \operatorname{Sin}[c + d x]}{24 d} +$$

$$\frac{A \operatorname{Cos}[c + d x]^3 (a + a \operatorname{Sec}[c + d x])^{5/2} \operatorname{Sin}[c + d x]}{4 d}$$

Result (type 4, 535 leaves):

$$\begin{aligned}
 & \left( \cos [c + d x]^4 \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^5 (a (1 + \operatorname{Sec} [c + d x]))^{5/2} (A + C \operatorname{Sec} [c + d x]^2) \right. \\
 & \quad \left( -\frac{1}{768} (265 A + 432 C) \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] + \frac{5}{96} (11 A + 12 C) \operatorname{Sin} \left[ \frac{3}{2} (c + d x) \right] + \right. \\
 & \quad \left. \frac{1}{256} (47 A + 16 C) \operatorname{Sin} \left[ \frac{5}{2} (c + d x) \right] + \frac{5}{96} A \operatorname{Sin} \left[ \frac{7}{2} (c + d x) \right] + \frac{1}{128} A \operatorname{Sin} \left[ \frac{9}{2} (c + d x) \right] \right) \Bigg) / \\
 & \quad \left( d (A + 2 C + A \operatorname{Cos} [2 c + 2 d x]) \right) + \frac{1}{64 d (A + 2 C + A \operatorname{Cos} [2 c + 2 d x])} \\
 & \quad (4 + 3 \sqrt{2}) (163 A + 304 C) \operatorname{Cos} \left[ \frac{1}{4} (c + d x) \right]^4 \\
 & \quad \sqrt{\frac{7 - 5 \sqrt{2} + (10 - 7 \sqrt{2}) \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right]}{1 + \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right]}} \left( 1 - \sqrt{2} + (-2 + \sqrt{2}) \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right] \right) \\
 & \quad \operatorname{Cos} [c + d x]^3 \left( \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] + \right. \\
 & \quad \left. 2 \operatorname{EllipticPi} \left[ -3 + 2 \sqrt{2}, -\operatorname{ArcSin} \left[ \frac{\operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \right) \\
 & \quad \sqrt{\left( -1 + \sqrt{2} - (-2 + \sqrt{2}) \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right] \right) \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2} \\
 & \quad \sqrt{\left( -1 - \sqrt{2} + (2 + \sqrt{2}) \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right] \right) \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^5} \\
 & \quad (a (1 + \operatorname{Sec} [c + d x]))^{5/2} (A + C \operatorname{Sec} [c + d x]^2) \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}
 \end{aligned}$$

**Problem 181:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \cos [c + d x]^5 (a + a \operatorname{Sec} [c + d x])^{5/2} (A + C \operatorname{Sec} [c + d x]^2) dx$$

Optimal (type 3, 245 leaves, 7 steps):

$$\begin{aligned}
 & \frac{a^{5/2} (283 A + 400 C) \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{128 d} + \\
 & \frac{a^3 (283 A + 400 C) \operatorname{Sin}[c+dx]}{128 d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{a^3 (787 A + 1040 C) \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx]}{960 d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \\
 & \frac{a^2 (79 A + 80 C) \operatorname{Cos}[c+dx]^2 \sqrt{a+a \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{240 d} + \\
 & \frac{a A \operatorname{Cos}[c+dx]^3 (a+a \operatorname{Sec}[c+dx])^{3/2} \operatorname{Sin}[c+dx]}{8 d} + \\
 & \frac{A \operatorname{Cos}[c+dx]^4 (a+a \operatorname{Sec}[c+dx])^{5/2} \operatorname{Sin}[c+dx]}{5 d}
 \end{aligned}$$

Result (type 4, 556 leaves):



$$\begin{aligned}
 & \left( \cos [c + d x]^4 \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^5 (a (1 + \operatorname{Sec} [c + d x]))^{5/2} (A + C \operatorname{Sec} [c + d x]^2) \right. \\
 & \quad \left( - \frac{(2309 A + 3760 C) \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right]}{7680} + \frac{1}{960} (509 A + 640 C) \operatorname{Sin} \left[ \frac{3}{2} (c + d x) \right] + \right. \\
 & \quad \frac{5}{512} (19 A + 16 C) \operatorname{Sin} \left[ \frac{5}{2} (c + d x) \right] + \frac{1}{240} (16 A + 5 C) \operatorname{Sin} \left[ \frac{7}{2} (c + d x) \right] + \\
 & \quad \left. \left. \frac{5}{256} A \operatorname{Sin} \left[ \frac{9}{2} (c + d x) \right] + \frac{1}{320} A \operatorname{Sin} \left[ \frac{11}{2} (c + d x) \right] \right) \right) / (d (A + 2 C + A \cos [2 c + 2 d x])) + \\
 & \frac{1}{64 d (A + 2 C + A \cos [2 c + 2 d x])} \left( 2 + \frac{3}{\sqrt{2}} \right) (283 A + 400 C) \cos \left[ \frac{1}{4} (c + d x) \right]^4 \\
 & \sqrt{\frac{7 - 5 \sqrt{2} + (10 - 7 \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right]}{1 + \cos \left[ \frac{1}{2} (c + d x) \right]}} \left( 1 - \sqrt{2} + (-2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right] \right) \\
 & \cos [c + d x]^3 \left( \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] + \right. \\
 & \quad \left. 2 \operatorname{EllipticPi} \left[ -3 + 2 \sqrt{2}, -\operatorname{ArcSin} \left[ \frac{\operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \right) \\
 & \sqrt{\left( -1 + \sqrt{2} - (-2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right] \right) \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2} \\
 & \sqrt{\left( -1 - \sqrt{2} + (2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right] \right) \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^5} \\
 & (a (1 + \operatorname{Sec} [c + d x]))^{5/2} (A + C \operatorname{Sec} [c + d x]^2) \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}
 \end{aligned}$$

**Problem 182: Result unnecessarily involves higher level functions.**

$$\int \cos [c + d x]^6 (a + a \operatorname{Sec} [c + d x])^{5/2} (A + C \operatorname{Sec} [c + d x]^2) dx$$

Optimal (type 3, 290 leaves, 8 steps):

$$\begin{aligned}
 & \frac{a^{5/2} (1015 A + 1304 C) \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{512 d} + \frac{a^3 (1015 A + 1304 C) \operatorname{Sin}[c+dx]}{512 d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \\
 & \frac{a^3 (1015 A + 1304 C) \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx]}{768 d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{a^3 (109 A + 136 C) \operatorname{Cos}[c+dx]^2 \operatorname{Sin}[c+dx]}{192 d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \\
 & \frac{a^2 (23 A + 24 C) \operatorname{Cos}[c+dx]^3 \sqrt{a+a \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{96 d} + \\
 & \frac{a A \operatorname{Cos}[c+dx]^4 (a+a \operatorname{Sec}[c+dx])^{3/2} \operatorname{Sin}[c+dx]}{12 d} + \\
 & \frac{A \operatorname{Cos}[c+dx]^5 (a+a \operatorname{Sec}[c+dx])^{5/2} \operatorname{Sin}[c+dx]}{6 d}
 \end{aligned}$$

Result (type 4, 577 leaves):

$$\begin{aligned}
 & \left( \cos [c + d x]^4 \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^5 (a (1 + \operatorname{Sec} [c + d x]))^{5/2} (A + C \operatorname{Sec} [c + d x]^2) \right. \\
 & \quad \left( - \frac{(1589 A + 2120 C) \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right]}{6144} + \frac{11}{384} (17 A + 20 C) \operatorname{Sin} \left[ \frac{3}{2} (c + d x) \right] + \right. \\
 & \quad \frac{(1145 A + 1128 C) \operatorname{Sin} \left[ \frac{5}{2} (c + d x) \right]}{6144} + \frac{1}{384} (29 A + 20 C) \operatorname{Sin} \left[ \frac{7}{2} (c + d x) \right] + \\
 & \quad \left. \left. \frac{(83 A + 24 C) \operatorname{Sin} \left[ \frac{9}{2} (c + d x) \right]}{3072} + \frac{1}{128} A \operatorname{Sin} \left[ \frac{11}{2} (c + d x) \right] + \frac{1}{768} A \operatorname{Sin} \left[ \frac{13}{2} (c + d x) \right] \right) \right) / \\
 & (d (A + 2 C + A \operatorname{Cos} [2 c + 2 d x])) + \frac{1}{512 d (A + 2 C + A \operatorname{Cos} [2 c + 2 d x])} \\
 & (4 + 3 \sqrt{2}) (1015 A + 1304 C) \operatorname{Cos} \left[ \frac{1}{4} (c + d x) \right]^4 \\
 & \sqrt{\frac{7 - 5 \sqrt{2} + (10 - 7 \sqrt{2}) \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right]}{1 + \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right]}} \left( 1 - \sqrt{2} + (-2 + \sqrt{2}) \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right] \right) \\
 & \operatorname{Cos} [c + d x]^3 \left( \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] + \right. \\
 & \quad \left. 2 \operatorname{EllipticPi} \left[ -3 + 2 \sqrt{2}, -\operatorname{ArcSin} \left[ \frac{\operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \right) \\
 & \sqrt{\left( -1 + \sqrt{2} - (-2 + \sqrt{2}) \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right] \right) \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2} \\
 & \sqrt{\left( -1 - \sqrt{2} + (2 + \sqrt{2}) \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right] \right) \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^5} \\
 & (a (1 + \operatorname{Sec} [c + d x]))^{5/2} (A + C \operatorname{Sec} [c + d x]^2) \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}
 \end{aligned}$$

**Problem 183: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec} [c + d x]^4 (A + C \operatorname{Sec} [c + d x]^2)}{\sqrt{a + a \operatorname{Sec} [c + d x]}} dx$$

Optimal (type 3, 236 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{\sqrt{2} (A + C) \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{2} \sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{\sqrt{a} d} + \frac{4 (147 A + 143 C) \operatorname{Tan}[c + dx]}{315 d \sqrt{a + a \operatorname{Sec}[c + dx]}} + \\
 & \frac{2 (21 A + 19 C) \operatorname{Sec}[c + dx]^2 \operatorname{Tan}[c + dx]}{105 d \sqrt{a + a \operatorname{Sec}[c + dx]}} - \frac{2 C \operatorname{Sec}[c + dx]^3 \operatorname{Tan}[c + dx]}{63 d \sqrt{a + a \operatorname{Sec}[c + dx]}} + \\
 & \frac{2 C \operatorname{Sec}[c + dx]^4 \operatorname{Tan}[c + dx]}{9 d \sqrt{a + a \operatorname{Sec}[c + dx]}} - \frac{2 (21 A + 29 C) \sqrt{a + a \operatorname{Sec}[c + dx]} \operatorname{Tan}[c + dx]}{315 a d}
 \end{aligned}$$

Result (type 3, 474 leaves):

$$\begin{aligned}
 & \frac{1}{(A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{a (1 + \operatorname{Sec}[c + d x])}} \operatorname{Cos}[c + d x]^2 \sqrt{(1 + \operatorname{Cos}[c + d x]) \operatorname{Sec}[c + d x]} \\
 & \sqrt{1 + \operatorname{Sec}[c + d x]} (A + C \operatorname{Sec}[c + d x]^2) \left( \frac{8 (-84 A - 126 C + 273 A \operatorname{Cos}[c] + 257 C \operatorname{Cos}[c]) \operatorname{Sin}\left[\frac{c}{2}\right]}{315 d (\operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Cos}\left[\frac{3c}{2}\right])} + \right. \\
 & \left. \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] (357 A \operatorname{Sin}\left[\frac{dx}{2}\right] + 383 C \operatorname{Sin}\left[\frac{dx}{2}\right])}{315 d} + \frac{4 C \operatorname{Sec}[c] \operatorname{Sec}[c + d x]^4 \operatorname{Sin}[dx]}{9 d} + \right. \\
 & \left. \frac{1}{315 d} 4 \operatorname{Sec}[c] \operatorname{Sec}[c + d x] (63 A \operatorname{Sin}[c] + 97 C \operatorname{Sin}[c] - 84 A \operatorname{Sin}[dx] - 126 C \operatorname{Sin}[dx]) - \right. \\
 & \left. \frac{1}{315 d} 4 \operatorname{Sec}[c] \operatorname{Sec}[c + d x]^2 (40 C \operatorname{Sin}[c] - 63 A \operatorname{Sin}[dx] - 97 C \operatorname{Sin}[dx]) + \right. \\
 & \left. \frac{4 \operatorname{Sec}[c] \operatorname{Sec}[c + d x]^3 (7 C \operatorname{Sin}[c] - 8 C \operatorname{Sin}[dx])}{63 d} \right) + \\
 & \left( 2 \sqrt{2} (A + C) \operatorname{ArcTan}\left[\frac{\sqrt{2}}{\sqrt{-1 + \operatorname{Sec}[c + d x]}}\right] \operatorname{Cos}[c + d x]^4 \sqrt{-1 + \operatorname{Sec}[c + d x]} \right. \\
 & \left. (1 + \operatorname{Sec}[c + d x])^2 (A + C \operatorname{Sec}[c + d x]^2) \operatorname{Sin}[c + d x] \right) / \\
 & \left( d (1 + \operatorname{Cos}[c + d x]) \sqrt{1 - \operatorname{Cos}[c + d x]^2} (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) \right. \\
 & \left. \sqrt{a (1 + \operatorname{Sec}[c + d x])} \sqrt{\operatorname{Cos}[c + d x]^2 (-1 + \operatorname{Sec}[c + d x]) (1 + \operatorname{Sec}[c + d x])} \right)
 \end{aligned}$$

**Problem 184: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c + d x]^3 (A + C \operatorname{Sec}[c + d x]^2)}{\sqrt{a + a \operatorname{Sec}[c + d x]}} dx$$

Optimal (type 3, 193 leaves, 6 steps):

$$\frac{\sqrt{2} (A+C) \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{2} \sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{\sqrt{a} d} - \frac{4 (35 A+37 C) \operatorname{Tan}[c+dx]}{105 d \sqrt{a+a \operatorname{Sec}[c+dx]}} - \frac{2 C \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx]}{35 d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{2 C \operatorname{Sec}[c+dx]^3 \operatorname{Tan}[c+dx]}{7 d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{2 (35 A+31 C) \sqrt{a+a \operatorname{Sec}[c+dx]} \operatorname{Tan}[c+dx]}{105 a d}$$

Result (type 3, 432 leaves):

$$\left( \operatorname{Cos}[c+dx]^2 \sqrt{(1+\operatorname{Cos}[c+dx]) \operatorname{Sec}[c+dx]} \sqrt{1+\operatorname{Sec}[c+dx]} \right. \\ \left. (A+C \operatorname{Sec}[c+dx]^2) \left( -\frac{8 (-35 A-49 C+35 A \operatorname{Cos}[c]+43 C \operatorname{Cos}[c]) \operatorname{Sin}\left[\frac{c}{2}\right]}{105 d (\operatorname{Cos}\left[\frac{c}{2}\right]+\operatorname{Cos}\left[\frac{3c}{2}\right])} - \frac{8 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}+\frac{dx}{2}\right] (35 A \operatorname{Sin}\left[\frac{dx}{2}\right]+46 C \operatorname{Sin}\left[\frac{dx}{2}\right])}{105 d} + \frac{4 C \operatorname{Sec}[c] \operatorname{Sec}[c+dx]^3 \operatorname{Sin}[dx]}{7 d} - \frac{1}{105 d} 4 \operatorname{Sec}[c] \operatorname{Sec}[c+dx] (18 C \operatorname{Sin}[c]-35 A \operatorname{Sin}[dx]-49 C \operatorname{Sin}[dx]) + \frac{4 \operatorname{Sec}[c] \operatorname{Sec}[c+dx]^2 (5 C \operatorname{Sin}[c]-6 C \operatorname{Sin}[dx])}{35 d} \right) \right) / \\ \left( (A+2 C+A \operatorname{Cos}[2 c+2 d x]) \sqrt{a(1+\operatorname{Sec}[c+dx])} \right) - \\ \left( 2 \sqrt{2} (A+C) \operatorname{ArcTan}\left[\frac{\sqrt{2}}{\sqrt{-1+\operatorname{Sec}[c+dx]}}\right] \operatorname{Cos}[c+dx]^4 \sqrt{-1+\operatorname{Sec}[c+dx]} \right. \\ \left. (1+\operatorname{Sec}[c+dx])^2 (A+C \operatorname{Sec}[c+dx]^2) \operatorname{Sin}[c+dx] \right) / \\ \left( d (1+\operatorname{Cos}[c+dx]) \sqrt{1-\operatorname{Cos}[c+dx]^2} (A+2 C+A \operatorname{Cos}[2 c+2 d x]) \right. \\ \left. \sqrt{a(1+\operatorname{Sec}[c+dx])} \sqrt{\operatorname{Cos}[c+dx]^2 (-1+\operatorname{Sec}[c+dx]) (1+\operatorname{Sec}[c+dx])} \right)$$

**Problem 185: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c+dx]^2 (A+C \operatorname{Sec}[c+dx]^2)}{\sqrt{a+a \operatorname{Sec}[c+dx]}} dx$$

Optimal (type 3, 152 leaves, 5 steps):

$$-\frac{\sqrt{2} (A+C) \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{2} \sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{\sqrt{a} d} + \frac{2 (15 A+14 C) \operatorname{Tan}[c+dx]}{15 d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{2 C \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx]}{5 d \sqrt{a+a \operatorname{Sec}[c+dx]}} - \frac{2 C \sqrt{a+a \operatorname{Sec}[c+dx]} \operatorname{Tan}[c+dx]}{15 a d}$$

Result (type 3, 392 leaves):

$$\left( \begin{aligned} & \cos [c+d x]^2 \sqrt{(1+\cos [c+d x]) \sec [c+d x]} \sqrt{1+\sec [c+d x]} \\ & (A+C \sec [c+d x]^2) \left( \frac{8(-4 C+15 A \cos [c]+13 C \cos [c]) \sin \left[\frac{c}{2}\right]}{15 d\left(\cos \left[\frac{c}{2}\right]+\cos \left[\frac{3 c}{2}\right]\right)} + \right. \\ & \frac{4 \sec \left[\frac{c}{2}\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]\left(15 A \sin \left[\frac{d x}{2}\right]+17 C \sin \left[\frac{d x}{2}\right]\right)}{15 d} + \\ & \left. \frac{4 C \sec [c] \sec [c+d x]^2 \sin [d x]}{5 d} + \frac{4 \sec [c] \sec [c+d x]\left(3 C \sin [c]-4 C \sin [d x]\right)}{15 d} \right) \Bigg) / \\ & \left( (A+2 C+A \cos [2 c+2 d x]) \sqrt{a(1+\sec [c+d x])} \right) + \\ & \left( 2 \sqrt{2}(A+C) \operatorname{ArcTan}\left[\frac{\sqrt{2}}{\sqrt{-1+\sec [c+d x]}}\right] \cos [c+d x]^4 \sqrt{-1+\sec [c+d x]} \right. \\ & \left. (1+\sec [c+d x])^2 (A+C \sec [c+d x]^2) \sin [c+d x] \right) \Bigg) / \\ & \left( d(1+\cos [c+d x]) \sqrt{1-\cos [c+d x]^2} (A+2 C+A \cos [2 c+2 d x]) \right. \\ & \left. \sqrt{a(1+\sec [c+d x])} \sqrt{\cos [c+d x]^2(-1+\sec [c+d x])(1+\sec [c+d x])} \right) \end{aligned} \right)$$

**Problem 192: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c+d x]^4 (A+C \sec [c+d x]^2)}{(a+a \sec [c+d x])^{3/2}} dx$$

Optimal (type 3, 259 leaves, 7 steps):

$$\begin{aligned} & \frac{(11 A+19 C) \operatorname{ArcTan}\left[\frac{\sqrt{a} \tan [c+d x]}{\sqrt{2} \sqrt{a+a \sec [c+d x]}}\right]}{2 \sqrt{2} a^{3/2} d} - \frac{(A+C) \sec [c+d x]^4 \tan [c+d x]}{2 d(a+a \sec [c+d x])^{3/2}} - \\ & \frac{(455 A+799 C) \tan [c+d x]}{105 a d \sqrt{a+a \sec [c+d x]}} - \frac{(35 A+67 C) \sec [c+d x]^2 \tan [c+d x]}{70 a d \sqrt{a+a \sec [c+d x]}} + \\ & \frac{(7 A+11 C) \sec [c+d x]^3 \tan [c+d x]}{14 a d \sqrt{a+a \sec [c+d x]}} + \frac{(245 A+397 C) \sqrt{a+a \sec [c+d x]} \tan [c+d x]}{210 a^2 d} \end{aligned}$$

Result (type 3, 528 leaves):

$$\begin{aligned}
 & \frac{1}{(A+2C+A \cos[2c+2dx]) (a(1+\sec[c+dx]))^{3/2}} \\
 & \cos[c+dx]^2 \sqrt{(1+\cos[c+dx]) \sec[c+dx]} (1+\sec[c+dx])^{3/2} \\
 & (A+C \sec[c+dx]^2) \left( -\frac{2(-140A-448C+665A \cos[c]+1201C \cos[c]) \sin[\frac{c}{2}]}{105d (\cos[\frac{c}{2}]+\cos[\frac{3c}{2}])} + \right. \\
 & \frac{\sec[\frac{c}{2}] \sec[\frac{c}{2}+\frac{dx}{2}]^2 (A \sin[\frac{c}{2}]+C \sin[\frac{c}{2}])}{2d} + \\
 & \frac{\sec[\frac{c}{2}] \sec[\frac{c}{2}+\frac{dx}{2}] (-805A \sin[\frac{dx}{2}]-1649C \sin[\frac{dx}{2}])}{105d} + \\
 & \frac{\sec[\frac{c}{2}] \sec[\frac{c}{2}+\frac{dx}{2}]^3 (A \sin[\frac{dx}{2}]+C \sin[\frac{dx}{2}])}{2d} + \frac{4C \sec[c] \sec[c+dx]^3 \sin[dx]}{7d} - \\
 & \frac{1}{105d} 4 \sec[c] \sec[c+dx] (39C \sin[c]-35A \sin[dx]-112C \sin[dx]) + \\
 & \left. \frac{4 \sec[c] \sec[c+dx]^2 (5C \sin[c]-13C \sin[dx])}{35d} \right) - \\
 & \left( (11A+19C) \operatorname{ArcTan}\left[\frac{\sqrt{2}}{\sqrt{-1+\sec[c+dx]}}\right] \cos[c+dx]^4 \sqrt{-1+\sec[c+dx]} \right. \\
 & \left. (1+\sec[c+dx])^3 (A+C \sec[c+dx]^2) \sin[c+dx] \right) / \\
 & \left( \sqrt{2} d (1+\cos[c+dx]) \sqrt{1-\cos[c+dx]^2} (A+2C+A \cos[2c+2dx]) \right. \\
 & \left. (a(1+\sec[c+dx]))^{3/2} \sqrt{\cos[c+dx]^2 (-1+\sec[c+dx]) (1+\sec[c+dx])} \right)
 \end{aligned}$$

**Problem 193: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec[c+dx]^3 (A+C \sec[c+dx]^2)}{(a+a \sec[c+dx])^{3/2}} dx$$

Optimal (type 3, 214 leaves, 6 steps):

$$\begin{aligned}
 & \frac{(7A+15C) \operatorname{ArcTan}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{2} \sqrt{a+a \sec[c+dx]}}\right]}{2\sqrt{2} a^{3/2} d} - \\
 & \frac{(A+C) \sec[c+dx]^3 \tan[c+dx]}{2d (a+a \sec[c+dx])^{3/2}} + \frac{(15A+31C) \tan[c+dx]}{5ad \sqrt{a+a \sec[c+dx]}} + \\
 & \frac{(5A+9C) \sec[c+dx]^2 \tan[c+dx]}{10ad \sqrt{a+a \sec[c+dx]}} - \frac{(5A+13C) \sqrt{a+a \sec[c+dx]} \tan[c+dx]}{10a^2 d}
 \end{aligned}$$

Result (type 3, 490 leaves):

$$\frac{1}{(A + 2C + A \cos[2c + 2dx]) (a (1 + \sec[c + dx]))^{3/2}}$$

$$\cos[c + dx]^2 \sqrt{(1 + \cos[c + dx]) \sec[c + dx]} (1 + \sec[c + dx])^{3/2} (A + C \sec[c + dx]^2)$$

$$\left( \frac{2(-12C + 25A \cos[c] + 49C \cos[c]) \sin\left[\frac{c}{2}\right] + \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 (-A \sin\left[\frac{c}{2}\right] - C \sin\left[\frac{c}{2}\right])}{5d \left(\cos\left[\frac{c}{2}\right] + \cos\left[\frac{3c}{2}\right]\right)} + \frac{\sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 (-A \sin\left[\frac{dx}{2}\right] - C \sin\left[\frac{dx}{2}\right])}{2d} + \frac{\sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right] (25A \sin\left[\frac{dx}{2}\right] + 61C \sin\left[\frac{dx}{2}\right])}{5d} + \frac{4C \sec[c] \sec[c + dx]^2 \sin[dx]}{5d} + \frac{4 \sec[c] \sec[c + dx] (C \sin[c] - 3C \sin[dx])}{5d} \right) +$$

$$\left( (7A + 15C) \operatorname{ArcTan}\left[\frac{\sqrt{2}}{\sqrt{-1 + \sec[c + dx]}}\right] \cos[c + dx]^4 \sqrt{-1 + \sec[c + dx]} (1 + \sec[c + dx])^3 (A + C \sec[c + dx]^2) \sin[c + dx] \right) /$$

$$\left( \sqrt{2} d (1 + \cos[c + dx]) \sqrt{1 - \cos[c + dx]^2} (A + 2C + A \cos[2c + 2dx]) (a (1 + \sec[c + dx]))^{3/2} \sqrt{\cos[c + dx]^2 (-1 + \sec[c + dx]) (1 + \sec[c + dx])} \right)$$

**Problem 194: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec[c + dx]^2 (A + C \sec[c + dx]^2)}{(a + a \sec[c + dx])^{3/2}} dx$$

Optimal (type 3, 169 leaves, 5 steps):

$$\frac{(3A + 11C) \operatorname{ArcTan}\left[\frac{\sqrt{a} \tan[c + dx]}{\sqrt{2} \sqrt{a + a \sec[c + dx]}}\right]}{2 \sqrt{2} a^{3/2} d} - \frac{(A + C) \sec[c + dx]^2 \tan[c + dx]}{2d (a + a \sec[c + dx])^{3/2}} - \frac{(3A + 13C) \tan[c + dx]}{3ad \sqrt{a + a \sec[c + dx]}} + \frac{(3A + 7C) \sqrt{a + a \sec[c + dx]} \tan[c + dx]}{6a^2 d}$$

Result (type 3, 458 leaves):



$$\begin{aligned}
 & \left( \cos [c+d x]^2 \sqrt{(1+\cos [c+d x]) \sec [c+d x]} (1+\sec [c+d x])^{3/2} (A+C \sec [c+d x])^2 \right. \\
 & \left. - \frac{2(-4 C+3 A \cos [c]+19 C \cos [c]) \sin \left[\frac{c}{2}\right]}{3 d\left(\cos \left[\frac{c}{2}\right]+\cos \left[\frac{3 c}{2}\right]\right)} + \frac{\sec \left[\frac{c}{2}\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^2\left(A \sin \left[\frac{c}{2}\right]+C \sin \left[\frac{c}{2}\right]\right)}{2 d} \right. \\
 & \left. + \frac{\sec \left[\frac{c}{2}\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]\left(-3 A \sin \left[\frac{d x}{2}\right]-23 C \sin \left[\frac{d x}{2}\right]\right)}{3 d} + \right. \\
 & \left. \frac{\sec \left[\frac{c}{2}\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^3\left(A \sin \left[\frac{d x}{2}\right]+C \sin \left[\frac{d x}{2}\right]\right)}{2 d} + \frac{4 C \sec [c] \sec [c+d x] \sin [d x]}{3 d} \right) / \\
 & \left( (A+2 C+A \cos [2 c+2 d x]) (a(1+\sec [c+d x]))^{3/2} - \right. \\
 & \left. \left( (3 A+11 C) \operatorname{ArcTan}\left[\frac{\sqrt{2}}{\sqrt{-1+\sec [c+d x]}}\right] \cos [c+d x]^4 \sqrt{-1+\sec [c+d x]} \right. \right. \\
 & \left. \left. (1+\sec [c+d x])^3 (A+C \sec [c+d x])^2 \sin [c+d x] \right) \right) / \\
 & \left( \sqrt{2} d(1+\cos [c+d x]) \sqrt{1-\cos [c+d x]^2} (A+2 C+A \cos [2 c+2 d x]) \right. \\
 & \left. (a(1+\sec [c+d x]))^{3/2} \sqrt{\cos [c+d x]^2(-1+\sec [c+d x]) (1+\sec [c+d x])} \right)
 \end{aligned}$$

### Problem 204: Result more than twice size of optimal antiderivative.

$$\int \frac{A+C \sec [c+d x]^2}{(a+a \sec [c+d x])^{5/2}} dx$$

Optimal (type 3, 162 leaves, 7 steps):

$$\frac{2 A \operatorname{ArcTan}\left[\frac{\sqrt{a} \tan [c+d x]}{\sqrt{a+a \sec [c+d x]}}\right]}{a^{5/2} d} - \frac{(43 A-5 C) \operatorname{ArcTan}\left[\frac{\sqrt{a} \tan [c+d x]}{\sqrt{2} \sqrt{a+a \sec [c+d x]}}\right]}{16 \sqrt{2} a^{5/2} d} - \frac{(A+C) \tan [c+d x]}{4 d(a+a \sec [c+d x])^{5/2}} - \frac{(11 A-5 C) \tan [c+d x]}{16 a d(a+a \sec [c+d x])^{3/2}}$$

Result (type 3, 725 leaves):

$$\begin{aligned}
 & \left( \cos [c+d x]^2 (1+\sec [c+d x])^{5/2} (A+C \sec [c+d x]^2) \right. \\
 & \quad \left( - \left( \left( \sqrt{2} (-11 A+5 C) \operatorname{ArcTan} \left[ \frac{\sqrt{2}}{\sqrt{-1+\sec [c+d x]}} \right] \cos [c+d x]^2 \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{-1+\sec [c+d x]} (1+\sec [c+d x])^{3/2} \sin [c+d x] \right) \right) / \left( d (1+\cos [c+d x]) \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1-\cos [c+d x]^2} \sqrt{\cos [c+d x]^2 (-1+\sec [c+d x]) (1+\sec [c+d x])} \right) \right) \right) + \\
 & \quad \left( 32 A \left( \sqrt{2} \operatorname{ArcTan} \left[ \frac{\sqrt{2}}{\sqrt{-1+\sec [c+d x]}} \right] + \operatorname{ArcTan} \left[ \frac{-2+\sqrt{1+\sec [c+d x]}}{\sqrt{-1+\sec [c+d x]}} \right] - \right. \right. \\
 & \quad \left. \left. \operatorname{ArcTan} \left[ \frac{2+\sqrt{1+\sec [c+d x]}}{\sqrt{-1+\sec [c+d x]}} \right] \right) \cos [c+d x]^2 \sqrt{-1+\sec [c+d x]} \right. \\
 & \quad \left. (1+\sec [c+d x])^{3/2} \sin [c+d x] \right) / \left( d (1+\cos [c+d x]) \sqrt{1-\cos [c+d x]^2} \right. \\
 & \quad \left. \left. \left. \sqrt{\cos [c+d x]^2 (-1+\sec [c+d x]) (1+\sec [c+d x])} \right) \right) \right) / \\
 & \quad \left( 16 (A+2 C+A \cos [2 c+2 d x]) (a (1+\sec [c+d x]))^{5/2} \right) + \\
 & \quad \frac{1}{(A+2 C+A \cos [2 c+2 d x]) (a (1+\sec [c+d x]))^{5/2} \cos [c+d x]^2} \\
 & \quad \frac{\sqrt{(1+\cos [c+d x]) \sec [c+d x]}}{(1+\sec [c+d x])^{5/2} (A+C \sec [c+d x]^2)} \\
 & \quad \left( \frac{\sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (-A \sin \left[ \frac{c}{2} \right] - C \sin \left[ \frac{c}{2} \right])}{8 d} + \right. \\
 & \quad \frac{\sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 (19 A \sin \left[ \frac{c}{2} \right] + 3 C \sin \left[ \frac{c}{2} \right])}{16 d} + \\
 & \quad \frac{\sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^5 (-A \sin \left[ \frac{d x}{2} \right] - C \sin \left[ \frac{d x}{2} \right])}{8 d} + \\
 & \quad \frac{\sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right] (-15 A \sin \left[ \frac{d x}{2} \right] + C \sin \left[ \frac{d x}{2} \right])}{8 d} + \\
 & \quad \left. \frac{\sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^3 (19 A \sin \left[ \frac{d x}{2} \right] + 3 C \sin \left[ \frac{d x}{2} \right])}{16 d} - \frac{(15 A - C) \tan \left[ \frac{c}{2} \right]}{8 d} \right)
 \end{aligned}$$

### Problem 205: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x] (A+C \sec [c+d x]^2)}{(a+a \sec [c+d x])^{5/2}} dx$$

Optimal (type 3, 199 leaves, 8 steps):

$$\begin{aligned} & - \frac{5 A \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \sec [c+d x]}}\right]}{a^{5/2} d} + \frac{(115 A+3 C) \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{2} \sqrt{a+a \sec [c+d x]}}\right]}{16 \sqrt{2} a^{5/2} d} \\ & - \frac{(A+C) \operatorname{Sin}[c+d x]}{4 d (a+a \sec [c+d x])^{5/2}} - \frac{(15 A-C) \operatorname{Sin}[c+d x]}{16 a d (a+a \sec [c+d x])^{3/2}} + \frac{(35 A+3 C) \operatorname{Sin}[c+d x]}{16 a^2 d \sqrt{a+a \sec [c+d x]}} \end{aligned}$$

Result (type 3, 739 leaves):

$$\begin{aligned}
 & \left( \cos [c+d x]^2 (1+\sec [c+d x])^{5/2} (A+C \sec [c+d x])^2 \right. \\
 & \left. \left( \left( \sqrt{2} (-35 A-3 C) \operatorname{ArcTan} \left[ \frac{\sqrt{2}}{\sqrt{-1+\sec [c+d x]}} \right] \cos [c+d x]^2 \right. \right. \right. \\
 & \left. \left. \left. \sqrt{-1+\sec [c+d x]} (1+\sec [c+d x])^{3/2} \sin [c+d x] \right) \right) / \left( d (1+\cos [c+d x]) \right. \right. \\
 & \left. \left. \sqrt{1-\cos [c+d x]^2} \sqrt{\cos [c+d x]^2 (-1+\sec [c+d x]) (1+\sec [c+d x])} \right) - \right. \\
 & \left. \left( 80 A \left( \sqrt{2} \operatorname{ArcTan} \left[ \frac{\sqrt{2}}{\sqrt{-1+\sec [c+d x]}} \right] + \operatorname{ArcTan} \left[ \frac{-2+\sqrt{1+\sec [c+d x]}}{\sqrt{-1+\sec [c+d x]}} \right] - \right. \right. \right. \\
 & \left. \left. \left. \operatorname{ArcTan} \left[ \frac{2+\sqrt{1+\sec [c+d x]}}{\sqrt{-1+\sec [c+d x]}} \right] \right) \cos [c+d x]^2 \sqrt{-1+\sec [c+d x]} \right. \right. \\
 & \left. \left. (1+\sec [c+d x])^{3/2} \sin [c+d x] \right) \right) / \left( d (1+\cos [c+d x]) \sqrt{1-\cos [c+d x]^2} \right. \\
 & \left. \left. \sqrt{\cos [c+d x]^2 (-1+\sec [c+d x]) (1+\sec [c+d x])} \right) \right) \right) / \\
 & \frac{\left( 16 (A+2 C+A \cos [2 c+2 d x]) (a (1+\sec [c+d x]))^{5/2} \right) +}{1} \\
 & \frac{(A+2 C+A \cos [2 c+2 d x]) (a (1+\sec [c+d x]))^{5/2}}{\cos [c+d x]^2} \\
 & \frac{\sqrt{(1+\cos [c+d x]) \sec [c+d x]}}{(1+\sec [c+d x])^{5/2}} \\
 & \frac{(A+C \sec [c+d x])^2}{\left( \frac{\sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \left( -27 A \sin \left[ \frac{c}{2} \right] - 11 C \sin \left[ \frac{c}{2} \right] \right)}{16 d} + \right.} \\
 & \frac{\sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \left( A \sin \left[ \frac{c}{2} \right] + C \sin \left[ \frac{c}{2} \right] \right)}{8 d} + \frac{2 A \cos [d x] \sin [c]}{d} + \\
 & \frac{\sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^3 \left( -27 A \sin \left[ \frac{d x}{2} \right] - 11 C \sin \left[ \frac{d x}{2} \right] \right)}{16 d} + \\
 & \frac{7 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right] \left( A \sin \left[ \frac{d x}{2} \right] + C \sin \left[ \frac{d x}{2} \right] \right)}{8 d} + \\
 & \left. \frac{\sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^5 \left( A \sin \left[ \frac{d x}{2} \right] + C \sin \left[ \frac{d x}{2} \right] \right)}{8 d} + \frac{2 A \cos [c] \sin [d x]}{d} + \frac{7 (A+C) \tan \left[ \frac{c}{2} \right]}{8 d} \right)
 \end{aligned}$$

Problem 207: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \text{Sec}[c + d x]^{3/2} (a + a \text{Sec}[c + d x]) (A + C \text{Sec}[c + d x]^2) dx$$

Optimal (type 4, 205 leaves, 9 steps):

$$\begin{aligned} & -\frac{1}{5d} 2a(5A+3C) \sqrt{\text{Cos}[c+dx]} \text{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\text{Sec}[c+dx]} + \\ & \frac{1}{21d} 2a(7A+5C) \sqrt{\text{Cos}[c+dx]} \text{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\text{Sec}[c+dx]} + \\ & \frac{2a(5A+3C) \sqrt{\text{Sec}[c+dx]} \text{Sin}[c+dx]}{5d} + \frac{2a(7A+5C) \text{Sec}[c+dx]^{3/2} \text{Sin}[c+dx]}{21d} + \\ & \frac{2aC \text{Sec}[c+dx]^{5/2} \text{Sin}[c+dx]}{5d} + \frac{2aC \text{Sec}[c+dx]^{7/2} \text{Sin}[c+dx]}{7d} \end{aligned}$$

Result (type 5, 624 leaves):

$$\begin{aligned}
 & a \left( - \left( \left( 2 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^2 \operatorname{Csc}[c] \right. \right. \right. \\
 & \quad \left. \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \right. \\
 & \quad \left. \left. (A + C \operatorname{Sec}[c+dx]^2) \right) / (d(A + 2C + A \cos[2c + 2dx])) \right) - \\
 & \left( 6 \sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^2 \operatorname{Csc}[c] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. (A + C \operatorname{Sec}[c+dx]^2) \right) / (5d(A + 2C + A \cos[2c + 2dx])) + \\
 & \left( 4 A \cos[c+dx]^{5/2} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\operatorname{Sec}[c+dx]} (A + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad (3d(A + 2C + A \cos[2c + 2dx])) + \\
 & \left( 20 C \cos[c+dx]^{5/2} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\operatorname{Sec}[c+dx]} (A + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad (21d(A + 2C + A \cos[2c + 2dx])) + \\
 & \left( (A + C \operatorname{Sec}[c+dx]^2) \left( \frac{4(5A + 3C) \cos[dx] \operatorname{Csc}[c]}{5d} + \frac{4C \operatorname{Sec}[c] \operatorname{Sec}[c+dx]^3 \operatorname{Sin}[dx]}{7d} \right. \right. \\
 & \quad \left. \left. \frac{4 \operatorname{Sec}[c] \operatorname{Sec}[c+dx]^2 (5C \operatorname{Sin}[c] + 7C \operatorname{Sin}[dx])}{35d} + \frac{1}{105d} 4 \operatorname{Sec}[c] \operatorname{Sec}[c+dx] \right. \right. \\
 & \quad \left. \left. (21C \operatorname{Sin}[c] + 35A \operatorname{Sin}[dx] + 25C \operatorname{Sin}[dx]) + \frac{4(7A + 5C) \operatorname{Tan}[c]}{21d} \right) \right) / \\
 & \quad \left. \left( (A + 2C + A \cos[2c + 2dx]) \operatorname{Sec}[c+dx]^{3/2} \right) \right)
 \end{aligned}$$

**Problem 208: Result unnecessarily involves higher level functions.**

$$\int \sqrt{\operatorname{Sec}[c+dx]} (a + a \operatorname{Sec}[c+dx]) (A + C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 4, 172 leaves, 8 steps):

$$\begin{aligned}
 & -\frac{1}{5d} 2a (5A+3C) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\
 & \frac{2a(3A+C) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{3d} + \\
 & \frac{2a(5A+3C) \sqrt{\sec[c+dx]} \sin[c+dx]}{5d} + \\
 & \frac{2aC \sec[c+dx]^{3/2} \sin[c+dx]}{3d} + \frac{2aC \sec[c+dx]^{5/2} \sin[c+dx]}{5d}
 \end{aligned}$$

Result (type 5, 282 leaves):

$$\begin{aligned}
 & \frac{1}{15d(1+e^{2i(c+dx)})^2(A+2C+A\cos[2(c+dx)])} \sec[c+dx]^{3/2} 2ae^{-i(2c+dx)}(-1+e^{2ic})\operatorname{Csc}[c] \\
 & \left(15A+9C+5Ce^{i(c+dx)}+30Ae^{2i(c+dx)}+24Ce^{2i(c+dx)}+15Ae^{4i(c+dx)}+3Ce^{4i(c+dx)}- \right. \\
 & \left. 5Ce^{5i(c+dx)}-5i(3A+C)e^{i(c+dx)}(1+e^{2i(c+dx)})^2\sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]- \right. \\
 & \left. 3(5A+3C)(1+e^{2i(c+dx)})^{5/2} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right]\right) (A+C\sec[c+dx])^2
 \end{aligned}$$

**Problem 209: Result unnecessarily involves higher level functions.**

$$\int \frac{(a+a\sec[c+dx])(A+C\sec[c+dx]^2)}{\sqrt{\sec[c+dx]}} dx$$

Optimal (type 4, 135 leaves, 7 steps):

$$\begin{aligned}
 & \frac{2a(A-C) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{d} + \\
 & \frac{2a(3A+C) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{3d} + \\
 & \frac{2aC \sqrt{\sec[c+dx]} \sin[c+dx]}{d} + \frac{2aC \sec[c+dx]^{3/2} \sin[c+dx]}{3d}
 \end{aligned}$$

Result (type 5, 197 leaves):

$$\begin{aligned}
 & \frac{1}{3d} ae^{-i(2c+dx)} \sec[c+dx]^{3/2} \left(-3iA+3iC-3iA\cos[2(c+dx)] + \right. \\
 & \left. 3iC\cos[2(c+dx)] + 2(3A+C)\cos[c+dx]^{3/2} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] + \right. \\
 & \left. 3i(A-C)e^{-2i(c+dx)}(1+e^{2i(c+dx)})^{3/2} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + \right. \\
 & \left. 2C\sin[c+dx] + 3C\sin[2(c+dx)]\right) (\cos[2c+dx] + i\sin[2c+dx])
 \end{aligned}$$

**Problem 210: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + a \operatorname{Sec}[c + d x]) (A + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[c + d x]^{3/2}} dx$$

Optimal (type 4, 135 leaves, 7 steps):

$$\frac{2 a (A - C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{d} +$$

$$\frac{2 a (A + 3 C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{3 d} +$$

$$\frac{2 a A \operatorname{Sin}[c + d x]}{3 d \sqrt{\operatorname{Sec}[c + d x]}} + \frac{2 a C \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{d}$$

Result (type 5, 182 leaves):

$$\frac{1}{3 d} a e^{-i(2 c + d x)} \sqrt{\operatorname{Sec}[c + d x]}$$

$$\left( -6 i A \operatorname{Cos}[c + d x] + 6 i C \operatorname{Cos}[c + d x] + 2 (A + 3 C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] + \right.$$

$$6 i (A - C) e^{-i(c + d x)} \sqrt{1 + e^{2 i(c + d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c + d x)}\right] +$$

$$\left. 6 C \operatorname{Sin}[c + d x] + A \operatorname{Sin}[2(c + d x)] \right) (\operatorname{Cos}[2 c + d x] + i \operatorname{Sin}[2 c + d x])$$

**Problem 211: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + a \operatorname{Sec}[c + d x]) (A + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[c + d x]^{5/2}} dx$$

Optimal (type 4, 141 leaves, 7 steps):

$$\frac{2 a (3 A + 5 C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{5 d} +$$

$$\frac{2 a (A + 3 C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{3 d} +$$

$$\frac{2 a A \operatorname{Sin}[c + d x]}{5 d \operatorname{Sec}[c + d x]^{3/2}} + \frac{2 a A \operatorname{Sin}[c + d x]}{3 d \sqrt{\operatorname{Sec}[c + d x]}}$$

Result (type 5, 183 leaves):



$$\frac{1}{30d} a e^{-i(2c+dx)} \sqrt{\sec[c+dx]} \left( 20(A+3C) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] + \right. \\ \left. 12i(3A+5C) e^{-i(c+dx)} \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + \right. \\ \left. 2 \cos[c+dx] \left( -6i(3A+5C) + 10A \sin[c+dx] + 3A \sin[2(c+dx)] \right) \right) \\ (\cos[2c+dx] + i \sin[2c+dx])$$

**Problem 212: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + a \sec[c+dx]) (A + C \sec[c+dx]^2)}{\sec[c+dx]^{7/2}} dx$$

Optimal (type 4, 174 leaves, 8 steps):

$$\frac{2a(3A+5C) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{5d} + \\ \frac{1}{21d} 2a(5A+7C) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\ \frac{2aA \sin[c+dx]}{7d \sec[c+dx]^{5/2}} + \frac{2aA \sin[c+dx]}{5d \sec[c+dx]^{3/2}} + \frac{2a(5A+7C) \sin[c+dx]}{21d \sqrt{\sec[c+dx]}}$$

Result (type 5, 202 leaves):

$$\frac{1}{420d} a e^{-i(2c+dx)} \sqrt{\sec[c+dx]} \\ \left( 40(5A+7C) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] + 168i(3A+5C) e^{-i(c+dx)} \right. \\ \left. \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + 2 \cos[c+dx] \right. \\ \left. (-84i(3A+5C) + 5(23A+28C) \sin[c+dx] + 42A \sin[2(c+dx)] + 15A \sin[3(c+dx)]) \right) \\ (\cos[2c+dx] + i \sin[2c+dx])$$

**Problem 213: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + a \sec[c+dx]) (A + C \sec[c+dx]^2)}{\sec[c+dx]^{9/2}} dx$$

Optimal (type 4, 205 leaves, 9 steps):

$$\frac{2a(7A+9C) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{15d} + \frac{1}{21d} \\ 2a(5A+7C) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \frac{2aA \sin[c+dx]}{9d \sec[c+dx]^{7/2}} + \\ \frac{2aA \sin[c+dx]}{7d \sec[c+dx]^{5/2}} + \frac{2a(7A+9C) \sin[c+dx]}{45d \sec[c+dx]^{3/2}} + \frac{2a(5A+7C) \sin[c+dx]}{21d \sqrt{\sec[c+dx]}}$$

Result (type 5, 218 leaves):

$$\frac{1}{2520 d} a e^{-i (2 c+d x)} \sqrt{\operatorname{Sec}[c+d x]} \left( 240 (5 A+7 C) \sqrt{\operatorname{Cos}[c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] + 336 i (7 A+9 C) e^{-i(c+d x)} \sqrt{1+e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right] + 2 \operatorname{Cos}[c+d x] \right. \\ \left. (-1176 i A-1512 i C+30(23 A+28 C) \operatorname{Sin}[c+d x]+14(19 A+18 C) \operatorname{Sin}[2(c+d x)]+90 A \operatorname{Sin}[3(c+d x)]+35 A \operatorname{Sin}[4(c+d x)]) \right) (\operatorname{Cos}[2 c+d x]+i \operatorname{Sin}[2 c+d x])$$

**Problem 214: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c+d x]^{3/2} (a+a \operatorname{Sec}[c+d x])^2 (A+C \operatorname{Sec}[c+d x])^2 dx$$

Optimal (type 4, 270 leaves, 10 steps):

$$-\frac{1}{15 d} 16 a^2 (3 A+2 C) \sqrt{\operatorname{Cos}[c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\operatorname{Sec}[c+d x]} + \frac{1}{21 d} 4 a^2 (7 A+5 C) \sqrt{\operatorname{Cos}[c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\operatorname{Sec}[c+d x]} + \frac{16 a^2 (3 A+2 C) \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{15 d} + \frac{4 a^2 (7 A+5 C) \operatorname{Sec}[c+d x]^{3/2} \operatorname{Sin}[c+d x]}{21 d} + \frac{2 a^2 (21 A+19 C) \operatorname{Sec}[c+d x]^{5/2} \operatorname{Sin}[c+d x]}{105 d} + \frac{2 C \operatorname{Sec}[c+d x]^{5/2} (a+a \operatorname{Sec}[c+d x])^2 \operatorname{Sin}[c+d x]}{9 d} + \frac{8 C \operatorname{Sec}[c+d x]^{5/2} (a^2+a^2 \operatorname{Sec}[c+d x]) \operatorname{Sin}[c+d x]}{63 d}$$

Result (type 5, 801 leaves):

$$\begin{aligned}
 & - \left( \left( 4 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^4 \operatorname{Csc}[c] \right. \right. \\
 & \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \operatorname{Sec}[c+dx])^2 (A+C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad \left( 5d(A+2C+A \cos[2c+2dx]) \right) - \left( 8 \sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^4 \operatorname{Csc}[c] \right. \\
 & \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \operatorname{Sec}[c+dx])^2 (A+C \operatorname{Sec}[c+dx]^2) \right) / (15d(A+2C+A \cos[2c+2dx])) + \\
 & \quad \left( 2A \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \operatorname{Sec}[c+dx])^2 \right. \\
 & \quad \left. (A+C \operatorname{Sec}[c+dx]^2) \right) / (3d(A+2C+A \cos[2c+2dx]) \operatorname{Sec}[c+dx]^{7/2}) + \\
 & \quad \left( 10C \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \operatorname{Sec}[c+dx])^2 \right. \\
 & \quad \left. (A+C \operatorname{Sec}[c+dx]^2) \right) / (21d(A+2C+A \cos[2c+2dx]) \operatorname{Sec}[c+dx]^{7/2}) + \\
 & \quad \left( \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \operatorname{Sec}[c+dx])^2 (A+C \operatorname{Sec}[c+dx]^2) \left( \frac{8(3A+2C) \cos[dx] \operatorname{Csc}[c]}{15d} + \right. \right. \\
 & \quad \left. \frac{C \operatorname{Sec}[c] \operatorname{Sec}[c+dx]^4 \operatorname{Sin}[dx]}{9d} + \frac{\operatorname{Sec}[c] \operatorname{Sec}[c+dx]^3 (7C \operatorname{Sin}[c] + 18C \operatorname{Sin}[dx])}{63d} + \right. \\
 & \quad \left. \frac{1}{315d} \operatorname{Sec}[c] \operatorname{Sec}[c+dx]^2 (90C \operatorname{Sin}[c] + 63A \operatorname{Sin}[dx] + 112C \operatorname{Sin}[dx]) + \frac{1}{315d} \right. \\
 & \quad \left. \operatorname{Sec}[c] \operatorname{Sec}[c+dx] (63A \operatorname{Sin}[c] + 112C \operatorname{Sin}[c] + 210A \operatorname{Sin}[dx] + 150C \operatorname{Sin}[dx]) + \right. \\
 & \quad \left. \left. \frac{2(7A+5C) \operatorname{Tan}[c]}{21d} \right) \right) / ((A+2C+A \cos[2c+2dx]) \operatorname{Sec}[c+dx]^{7/2})
 \end{aligned}$$

**Problem 215: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sqrt{\operatorname{Sec}[c+dx]} (a+a \operatorname{Sec}[c+dx])^2 (A+C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 4, 237 leaves, 9 steps):

$$\begin{aligned}
 & -\frac{1}{5d} 4a^2 (5A+3C) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\
 & \frac{1}{21d} 8a^2 (7A+3C) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\
 & \frac{4a^2 (5A+3C) \sqrt{\sec[c+dx]} \sin[c+dx]}{5d} + \frac{2a^2 (35A+33C) \sec[c+dx]^{3/2} \sin[c+dx]}{105d} + \\
 & \frac{2C \sec[c+dx]^{3/2} (a+a \sec[c+dx])^2 \sin[c+dx]}{7d} + \\
 & \frac{8C \sec[c+dx]^{3/2} (a^2+a^2 \sec[c+dx]) \sin[c+dx]}{35d}
 \end{aligned}$$

Result (type 5, 757 leaves):

$$\begin{aligned}
 & -\left( \left( \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^4 \operatorname{Csc}[c] \right. \right. \\
 & \quad \left. \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \right. \\
 & \quad \left. \left. \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \sec[c+dx])^2 (A+C \sec[c+dx]^2) \right) \right) / (d(A+2C+A \cos[2c+2dx])) - \\
 & \left( 3\sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^4 \operatorname{Csc}[c] \right. \\
 & \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \sec[c+dx])^2 (A+C \sec[c+dx]^2) \right) / (5d(A+2C+A \cos[2c+2dx])) + \\
 & \left( 4A \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \sec[c+dx])^2 \right. \\
 & \quad \left. (A+C \sec[c+dx]^2) \right) / (3d(A+2C+A \cos[2c+2dx]) \sec[c+dx]^{7/2}) + \\
 & \left( 4C \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \sec[c+dx])^2 \right. \\
 & \quad \left. (A+C \sec[c+dx]^2) \right) / (7d(A+2C+A \cos[2c+2dx]) \sec[c+dx]^{7/2}) + \\
 & \left( \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \sec[c+dx])^2 (A+C \sec[c+dx]^2) \left( \frac{2(5A+3C) \cos[dx] \operatorname{Csc}[c]}{5d} + \right. \right. \\
 & \quad \frac{C \operatorname{Sec}[c] \operatorname{Sec}[c+dx]^3 \sin[dx]}{7d} + \frac{\operatorname{Sec}[c] \operatorname{Sec}[c+dx]^2 (5C \sin[c] + 14C \sin[dx])}{35d} + \frac{1}{105d} \\
 & \quad \left. \left. \operatorname{Sec}[c] \operatorname{Sec}[c+dx] (42C \sin[c] + 35A \sin[dx] + 60C \sin[dx]) + \frac{(7A+12C) \operatorname{Tan}[c]}{21d} \right) \right) / \\
 & ((A+2C+A \cos[2c+2dx]) \sec[c+dx]^{7/2})
 \end{aligned}$$

**Problem 216:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(a + a \operatorname{Sec}[c + d x])^2 (A + C \operatorname{Sec}[c + d x]^2)}{\sqrt{\operatorname{Sec}[c + d x]}} dx$$

Optimal (type 4, 196 leaves, 8 steps):

$$\begin{aligned} & - \frac{16 a^2 C \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{5 d} + \\ & \frac{4 a^2 (3 A + C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{3 d} + \\ & \frac{2 a^2 (15 A + 17 C) \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{15 d} + \frac{2 C \sqrt{\operatorname{Sec}[c + d x]} (a + a \operatorname{Sec}[c + d x])^2 \operatorname{Sin}[c + d x]}{5 d} + \\ & \frac{8 C \sqrt{\operatorname{Sec}[c + d x]} (a^2 + a^2 \operatorname{Sec}[c + d x]) \operatorname{Sin}[c + d x]}{15 d} \end{aligned}$$

Result (type 5, 436 leaves):

$$\begin{aligned} & - \frac{1}{15 d (-1 + e^{2 i c}) (A + 2 C + A \operatorname{Cos}[2 c + 2 d x])} \\ & 2 i \sqrt{2} e^{-i(c+d x)} \sqrt{\frac{e^{i(c+d x)}}{1 + e^{2 i(c+d x)}}} \operatorname{Cos}[c + d x]^4 \left( 12 C (1 + e^{2 i(c+d x)}) + \right. \\ & \quad \left. 12 C (-1 + e^{2 i c}) \sqrt{1 + e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right] + \right. \\ & \quad \left. 5 (3 A + C) e^{i(c+d x)} (-1 + e^{2 i c}) \sqrt{1 + e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2 i(c+d x)}\right] \right) \\ & \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^4 (a + a \operatorname{Sec}[c + d x])^2 (A + C \operatorname{Sec}[c + d x]^2) + \\ & \left( \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^4 (a + a \operatorname{Sec}[c + d x])^2 (A + C \operatorname{Sec}[c + d x]^2) \right. \\ & \quad \left( - \frac{(-5 A - 16 C + 5 A \operatorname{Cos}[2 c]) \operatorname{Cos}[d x] \operatorname{Csc}[c]}{10 d} + \frac{A \operatorname{Cos}[c] \operatorname{Sin}[d x]}{d} + \right. \\ & \quad \left. \frac{C \operatorname{Sec}[c] \operatorname{Sec}[c + d x]^2 \operatorname{Sin}[d x]}{5 d} + \frac{\operatorname{Sec}[c] \operatorname{Sec}[c + d x] (3 C \operatorname{Sin}[c] + 10 C \operatorname{Sin}[d x])}{15 d} \right. \\ & \quad \left. \left. \frac{2 C \operatorname{Tan}[c]}{3 d} \right) \right) / \left( (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) \operatorname{Sec}[c + d x]^{7/2} \right) \end{aligned}$$

**Problem 217:** Result unnecessarily involves higher level functions.

$$\int \frac{(a + a \operatorname{Sec}[c + d x])^2 (A + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[c + d x]^{3/2}} dx$$

Optimal (type 4, 198 leaves, 8 steps):

$$\frac{4 a^2 (A-C) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{d} +$$

$$\frac{8 a^2 (A+C) \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{3 d} -$$

$$\frac{2 a^2 (A-5 C) \sqrt{\sec [c+d x]} \sin [c+d x]}{3 d} + \frac{2 A\left(a+a \sec [c+d x]\right)^2 \sin [c+d x]}{3 d \sqrt{\sec [c+d x]}} -$$

$$\frac{2(A-C) \sqrt{\sec [c+d x]}\left(a^2+a^2 \sec [c+d x]\right) \sin [c+d x]}{3 d}$$

Result (type 5, 215 leaves):

$$\frac{1}{6 d} a^2 e^{-i(2 c+d x)} \sec [c+d x]^{3 / 2}\left(-12 i A+12 i C-12 i A \cos [2(c+d x)]\right)+$$

$$12 i C \cos [2(c+d x)]+16(A+C) \cos [c+d x]^{3 / 2} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]+$$

$$12 i(A-C) e^{-2 i(c+d x)}\left(1+e^{2 i(c+d x)}\right)^{3 / 2} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4},-e^{2 i(c+d x)}\right]+$$

$$A \sin [c+d x]+4 C \sin [c+d x]+12 C \sin [2(c+d x)]+A \sin [3(c+d x)]\left)\right)$$

$$(\cos [2 c+d x]+i \sin [2 c+d x])$$

**Problem 218: Result unnecessarily involves higher level functions.**

$$\int \frac{(a+a \sec [c+d x])^2(A+C \sec [c+d x]^2)}{\sec [c+d x]^{5 / 2}} d x$$

Optimal (type 4, 196 leaves, 8 steps):

$$\frac{16 a^2 A \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{5 d} +$$

$$\frac{4 a^2 (A+3 C) \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{3 d} -$$

$$\frac{2 a^2 (7 A-15 C) \sqrt{\sec [c+d x]} \sin [c+d x]}{15 d} +$$

$$\frac{2 A\left(a+a \sec [c+d x]\right)^2 \sin [c+d x]}{5 d \sec [c+d x]^{3 / 2}} + \frac{8 A\left(a^2+a^2 \sec [c+d x]\right) \sin [c+d x]}{15 d \sqrt{\sec [c+d x]}}$$

Result (type 5, 209 leaves):

$$\left( a^2 \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} \right] + i \sin \left[ \frac{c}{2} \right] \right) \right. \\ \left( -96 i A + \frac{192 i A \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c+d x)} \right]}{\sqrt{1 + e^{2 i (c+d x)}}} - \right. \\ \left. \frac{80 i (A + 3 C) e^{i (c+d x)} \operatorname{Hypergeometric2F1} \left[ \frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2 i (c+d x)} \right]}{\sqrt{1 + e^{2 i (c+d x)}}} + 40 A \sin [c + d x] + \right. \\ \left. \left. 3 A \sec [c + d x] \sin [3 (c + d x)] + 3 A \tan [c + d x] + 60 C \tan [c + d x] \right) \right) / \left( 30 d \sqrt{\sec [c + d x]} \right)$$

**Problem 219: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + a \sec [c + d x])^2 (A + C \sec [c + d x])^2}{\sec [c + d x]^{7/2}} dx$$

Optimal (type 4, 204 leaves, 8 steps):

$$\frac{1}{5 d} 4 a^2 (3 A + 5 C) \sqrt{\cos [c + d x]} \operatorname{EllipticE} \left[ \frac{1}{2} (c + d x), 2 \right] \sqrt{\sec [c + d x]} + \\ \frac{1}{21 d} 8 a^2 (3 A + 7 C) \sqrt{\cos [c + d x]} \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right] \sqrt{\sec [c + d x]} + \\ \frac{2 a^2 (33 A + 35 C) \sin [c + d x]}{105 d \sqrt{\sec [c + d x]}} + \frac{2 A (a + a \sec [c + d x])^2 \sin [c + d x]}{7 d \sec [c + d x]^{5/2}} + \\ \frac{8 A (a^2 + a^2 \sec [c + d x]) \sin [c + d x]}{35 d \sec [c + d x]^{3/2}}$$

Result (type 5, 203 leaves):

$$\frac{1}{420 d} a^2 e^{-i (2 c + d x)} \sqrt{\sec [c + d x]} \\ \left( 160 (3 A + 7 C) \sqrt{\cos [c + d x]} \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right] + 336 i (3 A + 5 C) e^{-i (c + d x)} \right. \\ \left. \sqrt{1 + e^{2 i (c + d x)}} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c + d x)} \right] + 2 \cos [c + d x] \right. \\ \left. \left( -504 i A - 840 i C + 5 (51 A + 28 C) \sin [c + d x] + 84 A \sin [2 (c + d x)] + 15 A \sin [3 (c + d x)] \right) \right) \\ (\cos [2 c + d x] + i \sin [2 c + d x])$$

**Problem 220: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \sec [c + d x])^2 (A + C \sec [c + d x])^2}{\sec [c + d x]^{9/2}} dx$$

Optimal (type 4, 237 leaves, 9 steps):

$$\begin{aligned} & \frac{1}{15 d} 16 a^2 (2 A + 3 C) \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\sec [c + d x]} + \\ & \frac{1}{21 d} 4 a^2 (5 A + 7 C) \sqrt{\cos [c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\sec [c + d x]} + \\ & \frac{2 a^2 (19 A + 21 C) \sin [c + d x]}{105 d \sec [c + d x]^{3/2}} + \frac{4 a^2 (5 A + 7 C) \sin [c + d x]}{21 d \sqrt{\sec [c + d x]}} + \\ & \frac{2 A (a + a \sec [c + d x])^2 \sin [c + d x]}{9 d \sec [c + d x]^{7/2}} + \frac{8 A (a^2 + a^2 \sec [c + d x]) \sin [c + d x]}{63 d \sec [c + d x]^{5/2}} \end{aligned}$$

Result (type 5, 850 leaves):



$$\begin{aligned}
 & \left( 8 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^4 \operatorname{Csc}[c] \right. \\
 & \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \operatorname{Sec}[c+dx])^2 (A+C \operatorname{Sec}[c+dx]^2) \right) / (15d(A+2C+A \cos[2c+2dx])) + \\
 & \left( 4 \sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^4 \operatorname{Csc}[c] \right. \\
 & \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \operatorname{Sec}[c+dx])^2 (A+C \operatorname{Sec}[c+dx]^2) \right) / (5d(A+2C+A \cos[2c+2dx])) + \\
 & \left( 10 A \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \operatorname{Sec}[c+dx])^2 \right. \\
 & \quad \left. (A+C \operatorname{Sec}[c+dx]^2) \right) / (21d(A+2C+A \cos[2c+2dx]) \operatorname{Sec}[c+dx]^{7/2}) + \\
 & \left( 2 C \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \operatorname{Sec}[c+dx])^2 \right. \\
 & \quad \left. (A+C \operatorname{Sec}[c+dx]^2) \right) / (3d(A+2C+A \cos[2c+2dx]) \operatorname{Sec}[c+dx]^{7/2}) + \\
 & \frac{1}{(A+2C+A \cos[2c+2dx]) \operatorname{Sec}[c+dx]^{7/2}} \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \operatorname{Sec}[c+dx])^2 \\
 & \left( A+C \operatorname{Sec}[c+dx]^2 \right) \left( -\frac{1}{720d} (347A+558C+421A \cos[2c]+594C \cos[2c]) \cos[dx] \operatorname{Csc}[c] + \right. \\
 & \quad \frac{(13A+14C) \cos[2dx] \sin[2c]}{42d} + \frac{(79A+36C) \cos[3dx] \sin[3c]}{720d} + \frac{A \cos[4dx] \sin[4c]}{28d} + \\
 & \quad \frac{A \cos[5dx] \sin[5c]}{144d} + \frac{(421A+594C) \cos[c] \sin[dx]}{360d} + \frac{(13A+14C) \cos[2c] \sin[2dx]}{42d} + \\
 & \quad \left. \frac{(79A+36C) \cos[3c] \sin[3dx]}{720d} + \frac{A \cos[4c] \sin[4dx]}{28d} + \frac{A \cos[5c] \sin[5dx]}{144d} \right)
 \end{aligned}$$

**Problem 221:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(a+a \operatorname{Sec}[c+dx])^2 (A+C \operatorname{Sec}[c+dx]^2)}{\operatorname{Sec}[c+dx]^{11/2}} dx$$

Optimal (type 4, 270 leaves, 10 steps):

$$\begin{aligned} & \frac{1}{15 d} 4 a^2 (7 A+9 C) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}+ \\ & \frac{1}{231 d} 8 a^2 (25 A+33 C) \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}+ \\ & \frac{2 a^2 (89 A+99 C) \sin [c+d x]}{693 d \sec [c+d x]^{5 / 2}}+\frac{4 a^2 (7 A+9 C) \sin [c+d x]}{45 d \sec [c+d x]^{3 / 2}}+\frac{8 a^2 (25 A+33 C) \sin [c+d x]}{231 d \sqrt{\sec [c+d x]}}+ \\ & \frac{2 A\left(a+a \sec [c+d x]\right)^2 \sin [c+d x]}{11 d \sec [c+d x]^{9 / 2}}+\frac{8 A\left(a^2+a^2 \sec [c+d x]\right) \sin [c+d x]}{99 d \sec [c+d x]^{7 / 2}} \end{aligned}$$

Result (type 5, 896 leaves):

$$\begin{aligned}
 & \left( 7 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^4 \operatorname{Csc}[c] \right. \\
 & \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \operatorname{Sec}[c+dx])^2 (A+C \operatorname{Sec}[c+dx]^2) \right) / (15d(A+2C+A \cos[2c+2dx])) + \\
 & \left( 3 \sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^4 \operatorname{Csc}[c] \right. \\
 & \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \operatorname{Sec}[c+dx])^2 (A+C \operatorname{Sec}[c+dx]^2) \right) / (5d(A+2C+A \cos[2c+2dx])) + \\
 & \left( 100 A \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \operatorname{Sec}[c+dx])^2 \right. \\
 & \quad \left. (A+C \operatorname{Sec}[c+dx]^2) \right) / (231d(A+2C+A \cos[2c+2dx]) \operatorname{Sec}[c+dx]^{7/2}) + \\
 & \left( 4 C \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \operatorname{Sec}[c+dx])^2 \right. \\
 & \quad \left. (A+C \operatorname{Sec}[c+dx]^2) \right) / (7d(A+2C+A \cos[2c+2dx]) \operatorname{Sec}[c+dx]^{7/2}) + \\
 & \frac{1}{(A+2C+A \cos[2c+2dx]) \operatorname{Sec}[c+dx]^{7/2}} \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \operatorname{Sec}[c+dx])^2 \\
 & (A+C \operatorname{Sec}[c+dx]^2) \left( -\frac{1}{360d} (149A+198C+187A \cos[2c]+234C \cos[2c]) \cos[dx] \operatorname{Csc}[c] + \right. \\
 & \quad \frac{(2185A+2376C) \cos[2dx] \sin[2c]}{7392d} + \frac{(43A+36C) \cos[3dx] \sin[3c]}{360d} + \\
 & \quad \frac{(27A+11C) \cos[4dx] \sin[4c]}{616d} + \frac{A \cos[5dx] \sin[5c]}{72d} + \\
 & \quad \frac{A \cos[6dx] \sin[6c]}{352d} + \frac{(187A+234C) \cos[c] \sin[dx]}{180d} + \\
 & \quad \frac{(2185A+2376C) \cos[2c] \sin[2dx]}{7392d} + \frac{(43A+36C) \cos[3c] \sin[3dx]}{360d} + \\
 & \quad \left. \frac{(27A+11C) \cos[4c] \sin[4dx]}{616d} + \frac{A \cos[5c] \sin[5dx]}{72d} + \frac{A \cos[6c] \sin[6dx]}{352d} \right)
 \end{aligned}$$

**Problem 222: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \text{Sec}[c + dx]^{3/2} (a + a \text{Sec}[c + dx])^3 (A + C \text{Sec}[c + dx]^2) dx$$

Optimal (type 4, 319 leaves, 11 steps):

$$\begin{aligned} & -\frac{1}{5d} 4a^3 (7A + 5C) \sqrt{\text{Cos}[c + dx]} \text{EllipticE}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\text{Sec}[c + dx]} + \\ & \frac{1}{231d} 4a^3 (143A + 105C) \sqrt{\text{Cos}[c + dx]} \text{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\text{Sec}[c + dx]} + \\ & \frac{4a^3 (7A + 5C) \sqrt{\text{Sec}[c + dx]} \text{Sin}[c + dx]}{5d} + \frac{4a^3 (143A + 105C) \text{Sec}[c + dx]^{3/2} \text{Sin}[c + dx]}{231d} + \\ & \frac{8a^3 (44A + 35C) \text{Sec}[c + dx]^{5/2} \text{Sin}[c + dx]}{385d} + \frac{2C \text{Sec}[c + dx]^{5/2} (a + a \text{Sec}[c + dx])^3 \text{Sin}[c + dx]}{11d} + \\ & \frac{4C \text{Sec}[c + dx]^{5/2} (a^2 + a^2 \text{Sec}[c + dx])^2 \text{Sin}[c + dx]}{33ad} + \\ & \frac{2(33A + 35C) \text{Sec}[c + dx]^{5/2} (a^3 + a^3 \text{Sec}[c + dx]) \text{Sin}[c + dx]}{231d} \end{aligned}$$

Result (type 5, 841 leaves):

$$\begin{aligned}
 & - \left( \left( 7 A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^5 \operatorname{Csc}[c] \right. \right. \\
 & \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3 (A+C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad \left. \left( 5 \sqrt{2} d (A+2C+A \cos[2c+2dx]) \right) \right) - \\
 & \left( C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^5 \operatorname{Csc}[c] \right. \\
 & \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3 (A+C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad \left( \sqrt{2} d (A+2C+A \cos[2c+2dx]) \right) + \\
 & \left( 13 A \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \right. \\
 & \quad \left. (a+a \operatorname{Sec}[c+dx])^3 (A+C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad \left( 21 d (A+2C+A \cos[2c+2dx]) \operatorname{Sec}[c+dx]^{9/2} \right) + \\
 & \left( 5 C \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3 \right. \\
 & \quad \left. (A+C \operatorname{Sec}[c+dx]^2) \right) / \left( 11 d (A+2C+A \cos[2c+2dx]) \operatorname{Sec}[c+dx]^{9/2} \right) + \\
 & \frac{1}{(A+2C+A \cos[2c+2dx]) \operatorname{Sec}[c+dx]^{9/2}} \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3 \\
 & \quad (A+C \operatorname{Sec}[c+dx]^2) \left( \frac{(7A+5C) \cos[dx] \operatorname{Csc}[c]}{5d} + \frac{C \operatorname{Sec}[c] \operatorname{Sec}[c+dx]^5 \operatorname{Sin}[dx]}{22d} + \right. \\
 & \quad \left. \frac{\operatorname{Sec}[c] \operatorname{Sec}[c+dx]^4 (3C \operatorname{Sin}[c] + 11C \operatorname{Sin}[dx])}{66d} + \frac{1}{462d} \right. \\
 & \quad \left. \operatorname{Sec}[c] \operatorname{Sec}[c+dx]^3 (77C \operatorname{Sin}[c] + 33A \operatorname{Sin}[dx] + 126C \operatorname{Sin}[dx]) \right) + \frac{1}{2310d} \\
 & \quad \operatorname{Sec}[c] \operatorname{Sec}[c+dx]^2 (165A \operatorname{Sin}[c] + 630C \operatorname{Sin}[c] + 693A \operatorname{Sin}[dx] + 770C \operatorname{Sin}[dx]) + \frac{1}{2310d} \\
 & \quad \operatorname{Sec}[c] \operatorname{Sec}[c+dx] (693A \operatorname{Sin}[c] + 770C \operatorname{Sin}[c] + 1430A \operatorname{Sin}[dx] + 1050C \operatorname{Sin}[dx]) + \\
 & \quad \left. \frac{(143A+105C) \operatorname{Tan}[c]}{231d} \right)
 \end{aligned}$$

**Problem 223: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sqrt{\sec[c+dx]} (a+a \sec[c+dx])^3 (A+C \sec[c+dx]^2) dx$$

Optimal (type 4, 286 leaves, 10 steps):

$$\begin{aligned} & -\frac{1}{15d} 4a^3 (27A+17C) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\ & \frac{1}{21d} 4a^3 (21A+11C) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\ & \frac{4a^3 (27A+17C) \sqrt{\sec[c+dx]} \sin[c+dx]}{15d} + \frac{8a^3 (21A+16C) \sec[c+dx]^{3/2} \sin[c+dx]}{105d} + \\ & \frac{2C \sec[c+dx]^{3/2} (a+a \sec[c+dx])^3 \sin[c+dx]}{9d} + \\ & \frac{4C \sec[c+dx]^{3/2} (a^2+a^2 \sec[c+dx])^2 \sin[c+dx]}{21ad} + \\ & \frac{2(63A+73C) \sec[c+dx]^{3/2} (a^3+a^3 \sec[c+dx]) \sin[c+dx]}{315d} \end{aligned}$$

Result (type 5, 798 leaves):

$$\begin{aligned}
 & - \left( \left( 9 A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^5 \operatorname{Csc}[c] \right. \right. \\
 & \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3 (A+C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad \left. \left( 5 \sqrt{2} d (A+2C+A \cos[2c+2dx]) \right) \right) - \\
 & \left( 17 C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^5 \operatorname{Csc}[c] \right. \\
 & \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3 (A+C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad \left( 15 \sqrt{2} d (A+2C+A \cos[2c+2dx]) \right) + \\
 & \left( A \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3 \right. \\
 & \quad \left. (A+C \operatorname{Sec}[c+dx]^2) \right) / \left( d (A+2C+A \cos[2c+2dx]) \operatorname{Sec}[c+dx]^{9/2} \right) + \\
 & \left( 11 C \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3 \right. \\
 & \quad \left. (A+C \operatorname{Sec}[c+dx]^2) \right) / \left( 21 d (A+2C+A \cos[2c+2dx]) \operatorname{Sec}[c+dx]^{9/2} \right) + \\
 & \left( \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3 (A+C \operatorname{Sec}[c+dx]^2) \left( \frac{(27A+17C) \cos[dx] \operatorname{Csc}[c]}{15d} + \right. \right. \\
 & \quad \left. \frac{C \operatorname{Sec}[c] \operatorname{Sec}[c+dx]^4 \operatorname{Sin}[dx]}{18d} + \frac{\operatorname{Sec}[c] \operatorname{Sec}[c+dx]^3 (7C \operatorname{Sin}[c] + 27C \operatorname{Sin}[dx])}{126d} + \right. \\
 & \quad \left. \frac{1}{630d} \operatorname{Sec}[c] \operatorname{Sec}[c+dx]^2 (135C \operatorname{Sin}[c] + 63A \operatorname{Sin}[dx] + 238C \operatorname{Sin}[dx]) + \frac{1}{630d} \right. \\
 & \quad \left. \operatorname{Sec}[c] \operatorname{Sec}[c+dx] (63A \operatorname{Sin}[c] + 238C \operatorname{Sin}[c] + 315A \operatorname{Sin}[dx] + 330C \operatorname{Sin}[dx]) + \right. \\
 & \quad \left. \left. \frac{(21A+22C) \operatorname{Tan}[c]}{42d} \right) \right) / \left( (A+2C+A \cos[2c+2dx]) \operatorname{Sec}[c+dx]^{9/2} \right)
 \end{aligned}$$

Problem 224: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(a + a \operatorname{Sec}[c + d x])^3 (A + C \operatorname{Sec}[c + d x]^2)}{\sqrt{\operatorname{Sec}[c + d x]}} dx$$

Optimal (type 4, 253 leaves, 9 steps):

$$\begin{aligned} & -\frac{1}{5d} 4a^3 (5A + 7C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]} + \\ & \frac{1}{21d} 4a^3 (35A + 13C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]} + \\ & \frac{8a^3 (70A + 53C) \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{105d} + \frac{2C \sqrt{\operatorname{Sec}[c + d x]} (a + a \operatorname{Sec}[c + d x])^3 \operatorname{Sin}[c + d x]}{7d} + \\ & \frac{12C \sqrt{\operatorname{Sec}[c + d x]} (a^2 + a^2 \operatorname{Sec}[c + d x])^2 \operatorname{Sin}[c + d x]}{35ad} + \\ & \frac{2(5A + 7C) \sqrt{\operatorname{Sec}[c + d x]} (a^3 + a^3 \operatorname{Sec}[c + d x]) \operatorname{Sin}[c + d x]}{15d} \end{aligned}$$

Result (type 5, 778 leaves):



$$\begin{aligned}
 & - \left( \left( A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^5 \operatorname{Csc}[c] \right. \right. \\
 & \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3 (A+C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \left( \sqrt{2} d (A+2C+A \cos[2c+2dx]) \right) - \left( 7C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^5 \operatorname{Csc}[c] \right. \\
 & \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3 (A+C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \left( 5\sqrt{2} d (A+2C+A \cos[2c+2dx]) \right) + \\
 & \left( 5A \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \right. \\
 & \quad \left. (a+a \operatorname{Sec}[c+dx])^3 (A+C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \left( 3d (A+2C+A \cos[2c+2dx]) \operatorname{Sec}[c+dx]^{9/2} \right) + \\
 & \left( 13C \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3 \right. \\
 & \quad \left. (A+C \operatorname{Sec}[c+dx]^2) \right) / \left( 21d (A+2C+A \cos[2c+2dx]) \operatorname{Sec}[c+dx]^{9/2} \right) + \\
 & \left( \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3 (A+C \operatorname{Sec}[c+dx]^2) \right. \\
 & \quad \left( -\frac{(-25A-28C+5A \cos[2c]) \cos[dx] \operatorname{Csc}[c]}{20d} + \frac{A \cos[c] \sin[dx]}{2d} + \right. \\
 & \quad \frac{C \operatorname{Sec}[c] \operatorname{Sec}[c+dx]^3 \sin[dx]}{14d} + \frac{\operatorname{Sec}[c] \operatorname{Sec}[c+dx]^2 (5C \sin[c] + 21C \sin[dx])}{70d} + \frac{1}{210d} \\
 & \quad \left. \left. \operatorname{Sec}[c] \operatorname{Sec}[c+dx] (63C \sin[c] + 35A \sin[dx] + 130C \sin[dx]) + \frac{(7A+26C) \tan[c]}{42d} \right) \right) / \\
 & \left( (A+2C+A \cos[2c+2dx]) \operatorname{Sec}[c+dx]^{9/2} \right)
 \end{aligned}$$

**Problem 225: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a+a \operatorname{Sec}[c+dx])^3 (A+C \operatorname{Sec}[c+dx]^2)}{\operatorname{Sec}[c+dx]^{3/2}} dx$$

Optimal (type 4, 259 leaves, 9 steps):

$$\begin{aligned}
 & \frac{1}{5d} 4a^3 (5A - 9C) \sqrt{\cos[c + dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\sec[c + dx]} + \\
 & \frac{1}{3d} 4a^3 (5A + 3C) \sqrt{\cos[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\sec[c + dx]} + \\
 & \frac{4a^3 (5A + 21C) \sqrt{\sec[c + dx]} \sin[c + dx]}{15d} + \frac{2A (a + a \sec[c + dx])^3 \sin[c + dx]}{3d \sqrt{\sec[c + dx]}} - \\
 & \frac{2(5A - 3C) \sqrt{\sec[c + dx]} (a^2 + a^2 \sec[c + dx])^2 \sin[c + dx]}{15ad} - \\
 & \frac{2(5A - 9C) \sqrt{\sec[c + dx]} (a^3 + a^3 \sec[c + dx]) \sin[c + dx]}{15d}
 \end{aligned}$$

Result (type 5, 764 leaves):

$$\begin{aligned}
 & \left( A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^5 \csc[c] \right. \\
 & \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \sec[c+dx])^3 (A+C \sec[c+dx]^2) \right) / \\
 & \quad \left( \sqrt{2} d (A+2C+A \cos[2c+2dx]) \right) - \left( 9 C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^5 \csc[c] \right. \\
 & \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \sec[c+dx])^3 (A+C \sec[c+dx]^2) \right) / \\
 & \quad \left( 5 \sqrt{2} d (A+2C+A \cos[2c+2dx]) \right) + \\
 & \quad \left( 5 A \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \sec[c+dx])^3 \right. \\
 & \quad \left. (A+C \sec[c+dx]^2) \right) / \left( 3 d (A+2C+A \cos[2c+2dx]) \sec[c+dx]^{9/2} \right) + \\
 & \quad \left( C \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \sec[c+dx])^3 \right. \\
 & \quad \left. (A+C \sec[c+dx]^2) \right) / \left( d (A+2C+A \cos[2c+2dx]) \sec[c+dx]^{9/2} \right) + \\
 & \quad \left( \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \sec[c+dx])^3 (A+C \sec[c+dx]^2) \right. \\
 & \quad \left( -\frac{(5A-36C+15A \cos[2c]) \cos[dx] \csc[c]}{20d} + \frac{A \cos[2dx] \sin[2c]}{12d} + \frac{3A \cos[c] \sin[dx]}{2d} + \right. \\
 & \quad \frac{C \sec[c] \sec[c+dx]^2 \sin[dx]}{10d} + \frac{\sec[c] \sec[c+dx] (C \sin[c] + 5C \sin[dx])}{10d} + \\
 & \quad \left. \left. \frac{A \cos[2c] \sin[2dx]}{12d} + \frac{C \tan[c]}{2d} \right) \right) / \left( (A+2C+A \cos[2c+2dx]) \sec[c+dx]^{9/2} \right)
 \end{aligned}$$

**Problem 226: Result unnecessarily involves higher level functions.**

$$\int \frac{(a+a \sec[c+dx])^3 (A+C \sec[c+dx]^2)}{\sec[c+dx]^{5/2}} dx$$

Optimal (type 4, 253 leaves, 9 steps):

$$\begin{aligned} & \frac{1}{5d} 4a^3 (9A - 5C) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\ & \frac{1}{3d} 4a^3 (3A + 5C) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} - \\ & \frac{8a^3 (3A - 10C) \sqrt{\sec[c+dx]} \sin[c+dx]}{15d} + \\ & \frac{2A (a + a \sec[c+dx])^3 \sin[c+dx]}{5d \sec[c+dx]^{3/2}} + \frac{4A (a^2 + a^2 \sec[c+dx])^2 \sin[c+dx]}{5ad \sqrt{\sec[c+dx]}} - \\ & \frac{2(9A - 5C) \sqrt{\sec[c+dx]} (a^3 + a^3 \sec[c+dx]) \sin[c+dx]}{15d} \end{aligned}$$

Result (type 5, 245 leaves):

$$\begin{aligned} & \frac{1}{60d} a^3 e^{-i(2c+dx)} \sec[c+dx]^{3/2} \left( -216iA + 120iC - 216iA \cos[2(c+dx)] \right) + \\ & 120iC \cos[2(c+dx)] + 80(3A + 5C) \cos[c+dx]^{3/2} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] + \\ & 24i(9A - 5C) e^{-2i(c+dx)} (1 + e^{2i(c+dx)})^{3/2} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + \\ & 30A \sin[c+dx] + 40C \sin[c+dx] + 6A \sin[2(c+dx)] + 180C \sin[2(c+dx)] + \\ & 30A \sin[3(c+dx)] + 3A \sin[4(c+dx)] \left( \cos[2c+dx] + i \sin[2c+dx] \right) \end{aligned}$$

**Problem 227: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + a \sec[c+dx])^3 (A + C \sec[c+dx]^2)}{\sec[c+dx]^{7/2}} dx$$

Optimal (type 4, 253 leaves, 9 steps):

$$\begin{aligned} & \frac{1}{5d} 4a^3 (7A + 5C) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\ & \frac{1}{21d} 4a^3 (13A + 35C) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} - \\ & \frac{4a^3 (41A - 35C) \sqrt{\sec[c+dx]} \sin[c+dx]}{105d} + \frac{2A (a + a \sec[c+dx])^3 \sin[c+dx]}{7d \sec[c+dx]^{5/2}} + \\ & \frac{12A (a^2 + a^2 \sec[c+dx])^2 \sin[c+dx]}{35ad \sec[c+dx]^{3/2}} + \frac{2(7A + 5C) (a^3 + a^3 \sec[c+dx]) \sin[c+dx]}{15d \sqrt{\sec[c+dx]}} \end{aligned}$$

Result (type 5, 231 leaves):

$$\begin{aligned} & \frac{1}{420 d} a^3 e^{-i(2c+dx)} \sqrt{\sec[c+dx]} \left( -2352 i A \cos[c+dx] - \right. \\ & 1680 i C \cos[c+dx] + 80 (13 A + 35 C) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] + \\ & 336 i (7 A + 5 C) e^{-i(c+dx)} \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + \\ & 126 A \sin[c+dx] + 840 C \sin[c+dx] + 550 A \sin[2(c+dx)] + 140 C \sin[2(c+dx)] + \\ & \left. 126 A \sin[3(c+dx)] + 15 A \sin[4(c+dx)] \right) (\cos[2c+dx] + i \sin[2c+dx]) \end{aligned}$$

**Problem 228: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \sec[c+dx])^3 (A + C \sec[c+dx]^2)}{\sec[c+dx]^{9/2}} dx$$

Optimal (type 4, 253 leaves, 9 steps):

$$\begin{aligned} & \frac{1}{15 d} 4 a^3 (17 A + 27 C) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\ & \frac{1}{21 d} 4 a^3 (11 A + 21 C) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\ & \frac{8 a^3 (16 A + 21 C) \sin[c+dx]}{105 d \sqrt{\sec[c+dx]}} + \frac{2 A (a + a \sec[c+dx])^3 \sin[c+dx]}{9 d \sec[c+dx]^{7/2}} + \\ & \frac{4 A (a^2 + a^2 \sec[c+dx])^2 \sin[c+dx]}{21 a d \sec[c+dx]^{5/2}} + \frac{2 (73 A + 63 C) (a^3 + a^3 \sec[c+dx]) \sin[c+dx]}{315 d \sec[c+dx]^{3/2}} \end{aligned}$$

Result (type 5, 847 leaves):

$$\left( 17 A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos [c+dx]^5 \operatorname{Csc}[c] \right. \\ \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\ \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3 (A+C \operatorname{Sec}[c+dx]^2) \right) / \\ \left( 15 \sqrt{2} d (A+2C+A \cos [2c+2dx]) \right) + \left( 9 C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos [c+dx]^5 \operatorname{Csc}[c] \right. \\ \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\ \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3 (A+C \operatorname{Sec}[c+dx]^2) \right) / \\ \left( 5 \sqrt{2} d (A+2C+A \cos [2c+2dx]) \right) + \\ \left( 11 A \sqrt{\cos [c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3 \right. \\ \left. (A+C \operatorname{Sec}[c+dx]^2) \right) / \left( 21 d (A+2C+A \cos [2c+2dx]) \operatorname{Sec}[c+dx]^{9/2} \right) + \\ \left( C \sqrt{\cos [c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3 \right. \\ \left. (A+C \operatorname{Sec}[c+dx]^2) \right) / \left( d (A+2C+A \cos [2c+2dx]) \operatorname{Sec}[c+dx]^{9/2} \right) + \\ \frac{1}{(A+2C+A \cos [2c+2dx]) \operatorname{Sec}[c+dx]^{9/2}} \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3 \\ (A+C \operatorname{Sec}[c+dx]^2) \left( -\frac{1}{1440 d} (743 A + 1278 C + 889 A \cos [2c] + 1314 C \cos [2c]) \cos [dx] \operatorname{Csc}[c] + \right. \\ \frac{(53 A + 42 C) \cos [2 dx] \sin [2 c]}{168 d} + \frac{(151 A + 36 C) \cos [3 dx] \sin [3 c]}{1440 d} + \\ \frac{3 A \cos [4 dx] \sin [4 c]}{112 d} + \frac{A \cos [5 dx] \sin [5 c]}{288 d} + \\ \frac{(889 A + 1314 C) \cos [c] \sin [dx]}{720 d} + \frac{(53 A + 42 C) \cos [2 c] \sin [2 dx]}{168 d} + \\ \left. \frac{(151 A + 36 C) \cos [3 c] \sin [3 dx]}{1440 d} + \frac{3 A \cos [4 c] \sin [4 dx]}{112 d} + \frac{A \cos [5 c] \sin [5 dx]}{288 d} \right)$$

Problem 229: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(a + a \operatorname{Sec}[c + d x])^3 (A + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[c + d x]^{11/2}} dx$$

Optimal (type 4, 286 leaves, 10 steps):

$$\begin{aligned} & \frac{1}{5d} 4a^3 (5A + 7C) \sqrt{\operatorname{Cos}[c + dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\operatorname{Sec}[c + dx]} + \\ & \frac{1}{231d} 4a^3 (105A + 143C) \sqrt{\operatorname{Cos}[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\operatorname{Sec}[c + dx]} + \\ & \frac{8a^3 (35A + 44C) \operatorname{Sin}[c + dx]}{385d \operatorname{Sec}[c + dx]^{3/2}} + \frac{4a^3 (105A + 143C) \operatorname{Sin}[c + dx]}{231d \sqrt{\operatorname{Sec}[c + dx]}} + \\ & \frac{2A (a + a \operatorname{Sec}[c + dx])^3 \operatorname{Sin}[c + dx]}{11d \operatorname{Sec}[c + dx]^{9/2}} + \frac{4A (a^2 + a^2 \operatorname{Sec}[c + dx])^2 \operatorname{Sin}[c + dx]}{33ad \operatorname{Sec}[c + dx]^{7/2}} + \\ & \frac{2(35A + 33C) (a^3 + a^3 \operatorname{Sec}[c + dx]) \operatorname{Sin}[c + dx]}{231d \operatorname{Sec}[c + dx]^{5/2}} \end{aligned}$$

Result (type 5, 893 leaves):

$$\left( A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^5 \csc[c] \right. \\ \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\ \left. \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \sec[c+dx])^3 (A+C \sec[c+dx]^2) \right) / \\ \left( \sqrt{2} d (A+2C+A \cos[2c+2dx]) \right) + \left( 7 C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^5 \csc[c] \right. \\ \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\ \left. \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \sec[c+dx])^3 (A+C \sec[c+dx]^2) \right) / \\ \left( 5 \sqrt{2} d (A+2C+A \cos[2c+2dx]) \right) + \\ \left( 5 A \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \sec[c+dx])^3 \right. \\ \left. (A+C \sec[c+dx]^2) \right) / \left( 11 d (A+2C+A \cos[2c+2dx]) \sec[c+dx]^{9/2} \right) + \\ \left( 13 C \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \sec[c+dx])^3 \right. \\ \left. (A+C \sec[c+dx]^2) \right) / \left( 21 d (A+2C+A \cos[2c+2dx]) \sec[c+dx]^{9/2} \right) + \\ \frac{1}{(A+2C+A \cos[2c+2dx]) \sec[c+dx]^{9/2}} \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \sec[c+dx])^3 \\ (A+C \sec[c+dx]^2) \left( -\frac{1}{480 d} (215 A+318 C+265 A \cos[2c]+354 C \cos[2c]) \cos[dx] \csc[c] + \right. \\ \frac{(4473 A+4840 C) \cos[2 dx] \sin[2 c]}{14784 d} + \frac{(55 A+36 C) \cos[3 dx] \sin[3 c]}{480 d} + \\ \frac{(49 A+11 C) \cos[4 dx] \sin[4 c]}{1232 d} + \frac{A \cos[5 dx] \sin[5 c]}{96 d} + \\ \frac{A \cos[6 dx] \sin[6 c]}{704 d} + \frac{(265 A+354 C) \cos[c] \sin[dx]}{240 d} + \\ \left. \frac{(4473 A+4840 C) \cos[2 c] \sin[2 dx]}{14784 d} + \frac{(55 A+36 C) \cos[3 c] \sin[3 dx]}{480 d} + \right. \\ \left. \frac{(49 A+11 C) \cos[4 c] \sin[4 dx]}{1232 d} + \frac{A \cos[5 c] \sin[5 dx]}{96 d} + \frac{A \cos[6 c] \sin[6 dx]}{704 d} \right)$$



Problem 230: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(a + a \operatorname{Sec}[c + d x])^3 (A + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[c + d x]^{13/2}} dx$$

Optimal (type 4, 319 leaves, 11 steps):

$$\begin{aligned} & \frac{1}{195 d} 4 a^3 (175 A + 221 C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]} + \\ & \frac{1}{231 d} 4 a^3 (95 A + 121 C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]} + \\ & \frac{40 a^3 (118 A + 143 C) \operatorname{Sin}[c + d x]}{9009 d \operatorname{Sec}[c + d x]^{5/2}} + \frac{4 a^3 (175 A + 221 C) \operatorname{Sin}[c + d x]}{585 d \operatorname{Sec}[c + d x]^{3/2}} + \\ & \frac{4 a^3 (95 A + 121 C) \operatorname{Sin}[c + d x]}{231 d \sqrt{\operatorname{Sec}[c + d x]}} + \frac{2 A (a + a \operatorname{Sec}[c + d x])^3 \operatorname{Sin}[c + d x]}{13 d \operatorname{Sec}[c + d x]^{11/2}} + \\ & \frac{12 A (a^2 + a^2 \operatorname{Sec}[c + d x])^2 \operatorname{Sin}[c + d x]}{143 a d \operatorname{Sec}[c + d x]^{9/2}} + \frac{2 (145 A + 143 C) (a^3 + a^3 \operatorname{Sec}[c + d x]) \operatorname{Sin}[c + d x]}{1287 d \operatorname{Sec}[c + d x]^{7/2}} \end{aligned}$$

Result (type 5, 942 leaves):

$$\left( 35 A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^5 \operatorname{Csc}[c] \right. \\
 \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3 (A+C \operatorname{Sec}[c+dx]^2) \right) / \\
 \left( 39 \sqrt{2} d (A+2C+A \cos[2c+2dx]) \right) + \left( 17 C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^5 \operatorname{Csc}[c] \right. \\
 \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3 (A+C \operatorname{Sec}[c+dx]^2) \right) / \\
 \left( 15 \sqrt{2} d (A+2C+A \cos[2c+2dx]) \right) + \\
 \left( 95 A \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3 \right. \\
 \left. (A+C \operatorname{Sec}[c+dx]^2) \right) / \left( 231 d (A+2C+A \cos[2c+2dx]) \operatorname{Sec}[c+dx]^{9/2} \right) + \\
 \left( 11 C \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3 \right. \\
 \left. (A+C \operatorname{Sec}[c+dx]^2) \right) / \left( 21 d (A+2C+A \cos[2c+2dx]) \operatorname{Sec}[c+dx]^{9/2} \right) + \\
 \frac{1}{(A+2C+A \cos[2c+2dx]) \operatorname{Sec}[c+dx]^{9/2}} \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3 (A+C \operatorname{Sec}[c+dx]^2) \\
 \left( -\frac{1}{149760 d} (59375 A + 77272 C + 75025 A \cos[2c] + 92456 C \cos[2c]) \cos[dx] \operatorname{Csc}[c] + \right. \\
 \frac{(4267 A + 4664 C) \cos[2dx] \sin[2c]}{14784 d} + \frac{(9005 A + 7852 C) \cos[3dx] \sin[3c]}{74880 d} + \\
 \frac{(59 A + 33 C) \cos[4dx] \sin[4c]}{1232 d} + \frac{(245 A + 52 C) \cos[5dx] \sin[5c]}{14976 d} + \\
 \frac{3 A \cos[6dx] \sin[6c]}{704 d} + \frac{A \cos[7dx] \sin[7c]}{1664 d} + \\
 \frac{(75025 A + 92456 C) \cos[c] \sin[dx]}{74880 d} + \frac{(4267 A + 4664 C) \cos[2c] \sin[2dx]}{14784 d} + \\
 \frac{(9005 A + 7852 C) \cos[3c] \sin[3dx]}{74880 d} + \frac{(59 A + 33 C) \cos[4c] \sin[4dx]}{1232 d} + \\
 \left. \frac{(245 A + 52 C) \cos[5c] \sin[5dx]}{14976 d} + \frac{3 A \cos[6c] \sin[6dx]}{704 d} + \frac{A \cos[7c] \sin[7dx]}{1664 d} \right)$$

Problem 231: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\text{Sec}[c + d x]^{5/2} (A + C \text{Sec}[c + d x]^2)}{a + a \text{Sec}[c + d x]} dx$$

Optimal (type 4, 232 leaves, 9 steps):

$$\begin{aligned} & -\frac{1}{5 a d} 3 (5 A + 7 C) \sqrt{\text{Cos}[c + d x]} \text{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\text{Sec}[c + d x]} - \\ & \frac{(3 A + 5 C) \sqrt{\text{Cos}[c + d x]} \text{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\text{Sec}[c + d x]}}{3 a d} + \\ & \frac{3 (5 A + 7 C) \sqrt{\text{Sec}[c + d x]} \text{Sin}[c + d x]}{5 a d} - \frac{(3 A + 5 C) \text{Sec}[c + d x]^{3/2} \text{Sin}[c + d x]}{3 a d} + \\ & \frac{(5 A + 7 C) \text{Sec}[c + d x]^{5/2} \text{Sin}[c + d x]}{5 a d} - \frac{(A + C) \text{Sec}[c + d x]^{7/2} \text{Sin}[c + d x]}{d (a + a \text{Sec}[c + d x])} \end{aligned}$$

Result (type 5, 828 leaves):

$$\begin{aligned}
& - \left( \left( 3 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c+dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \right. \\
& \quad \left. \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \right. \\
& \quad \left. \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c+dx]^2) \right) / \left( d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c+dx]) \right) \right) - \\
& \left( 21 \sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c+dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
& \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c+dx]^2) \right) / \\
& \quad (5d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c+dx])) - \\
& \quad \left( 2A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c+dx]^2) \sin[c] \right) / \\
& \quad (d (A + 2C + A \cos[2c + 2dx]) \sqrt{\operatorname{Sec}[c+dx]} (a + a \operatorname{Sec}[c+dx])) - \\
& \quad \left( 10C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c+dx]^2) \sin[c] \right) / \\
& \quad (3d (A + 2C + A \cos[2c + 2dx]) \sqrt{\operatorname{Sec}[c+dx]} (a + a \operatorname{Sec}[c+dx])) + \\
& \quad \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 (A + C \operatorname{Sec}[c+dx]^2) \right. \\
& \quad \left( \frac{6(5A + 7C) \cos[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right]}{5d} - \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] (A \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{d} \right. \\
& \quad \left. \frac{8C \operatorname{Sec}[c] \operatorname{Sec}[c+dx]^2 \sin[dx]}{5d} + \frac{8 \operatorname{Sec}[c] \operatorname{Sec}[c+dx] (3C \sin[c] - 5C \sin[dx])}{15d} \right. \\
& \quad \left. \left. \frac{4(2C + 3A \cos[c] + 5C \cos[c]) \operatorname{Sec}[c] \operatorname{Tan}\left[\frac{c}{2}\right]}{3d} \right) \right) / \\
& \quad \left( (A + 2C + A \cos[2c + 2dx]) \sqrt{\operatorname{Sec}[c+dx]} (a + a \operatorname{Sec}[c+dx]) \right)
\end{aligned}$$

Problem 232: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\text{Sec}[c + d x]^{3/2} (A + C \text{Sec}[c + d x]^2)}{a + a \text{Sec}[c + d x]} dx$$

Optimal (type 4, 190 leaves, 8 steps):

$$\begin{aligned} & \frac{(A + 3 C) \sqrt{\text{Cos}[c + d x]} \text{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\text{Sec}[c + d x]}}{a d} + \\ & \frac{(3 A + 5 C) \sqrt{\text{Cos}[c + d x]} \text{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\text{Sec}[c + d x]}}{3 a d} - \\ & \frac{(A + 3 C) \sqrt{\text{Sec}[c + d x]} \text{Sin}[c + d x]}{a d} + \\ & \frac{(3 A + 5 C) \text{Sec}[c + d x]^{3/2} \text{Sin}[c + d x]}{3 a d} - \frac{(A + C) \text{Sec}[c + d x]^{5/2} \text{Sin}[c + d x]}{d (a + a \text{Sec}[c + d x])} \end{aligned}$$

Result (type 5, 791 leaves):

$$\left( \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c+dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\ \left. \left(1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right]\right) \right. \\ \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A+C \operatorname{Sec}[c+dx]^2) \right) / \left( d (A+2C+A \cos[2c+2dx]) (a+a \operatorname{Sec}[c+dx]) \right) + \\ \left( 3 \sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c+dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\ \left. \left(1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right]\right) \right. \\ \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A+C \operatorname{Sec}[c+dx]^2) \right) / \left( d (A+2C+A \cos[2c+2dx]) (a+a \operatorname{Sec}[c+dx]) \right) + \\ \left( 2 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2}\right] (A+C \operatorname{Sec}[c+dx]^2) \right. \\ \left. \sin[c] \right) / \left( d (A+2C+A \cos[2c+2dx]) \sqrt{\operatorname{Sec}[c+dx]} (a+a \operatorname{Sec}[c+dx]) \right) + \\ \left( 10 C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2}\right] (A+C \operatorname{Sec}[c+dx]^2) \right. \\ \left. \sin[c] \right) / \left( 3 d (A+2C+A \cos[2c+2dx]) \sqrt{\operatorname{Sec}[c+dx]} (a+a \operatorname{Sec}[c+dx]) \right) + \\ \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 (A+C \operatorname{Sec}[c+dx]^2) \right. \\ \left( -\frac{2(A+3C) \cos[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right]}{d} + \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] (A \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{d} + \right. \\ \left. \frac{8 C \operatorname{Sec}[c] \operatorname{Sec}[c+dx] \sin[dx]}{3 d} + \frac{4(2C+3A \cos[c] + 5C \cos[c]) \operatorname{Sec}[c] \operatorname{Tan}\left[\frac{c}{2}\right]}{3 d} \right) / \\ \left( (A+2C+A \cos[2c+2dx]) \sqrt{\operatorname{Sec}[c+dx]} (a+a \operatorname{Sec}[c+dx]) \right)$$

**Problem 233: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\operatorname{Sec}[c+dx]} (A+C \operatorname{Sec}[c+dx]^2)}{a+a \operatorname{Sec}[c+dx]} dx$$

Optimal (type 4, 152 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{(A+3C) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{ad} + \\
 & \frac{(A-C) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{ad} + \\
 & \frac{(A+3C) \sqrt{\sec[c+dx]} \sin[c+dx]}{ad} - \frac{(A+C) \sec[c+dx]^{3/2} \sin[c+dx]}{d(a+a \sec[c+dx])}
 \end{aligned}$$

Result (type 5, 755 leaves):

$$\begin{aligned}
 & - \left( \left( \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c+dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \right. \\
 & \quad \left. \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right]\right) \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \sec[c+dx]^2) \right) / \left( d (A + 2C + A \cos[2c + 2dx]) (a + a \sec[c+dx]) \right) \right) - \\
 & \left( 3 \sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c+dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right]\right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \sec[c+dx]^2) \right) / \left( d (A + 2C + A \cos[2c + 2dx]) (a + a \sec[c+dx]) \right) + \\
 & \left( 2 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \sec[c+dx]^2) \sin[c] \right) / \left( d (A + 2C + A \cos[2c + 2dx]) \sqrt{\sec[c+dx]} (a + a \sec[c+dx]) \right) - \\
 & \left( 2 C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \sec[c+dx]^2) \sin[c] \right) / \left( d (A + 2C + A \cos[2c + 2dx]) \sqrt{\sec[c+dx]} (a + a \sec[c+dx]) \right) + \\
 & \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 (A + C \sec[c+dx]^2) \left( \frac{2(A+3C) \cos[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right]}{d} - \right. \right. \\
 & \quad \left. \left. \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] \left( A \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right] \right)}{d} - \frac{4(A+C) \operatorname{Tan}\left[\frac{c}{2}\right]}{d} \right) \right) / \left( d (A + 2C + A \cos[2c + 2dx]) \sqrt{\sec[c+dx]} (a + a \sec[c+dx]) \right)
 \end{aligned}$$

**Problem 234:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{A + C \operatorname{Sec}[c + d x]^2}{\sqrt{\operatorname{Sec}[c + d x]} (a + a \operatorname{Sec}[c + d x])} dx$$

Optimal (type 4, 124 leaves, 6 steps):

$$\frac{(3A + C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{a d} - \frac{(A - C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{a d} - \frac{(A + C) \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{d (a + a \operatorname{Sec}[c + d x])}$$

Result (type 5, 772 leaves):



$$\begin{aligned}
 & \left( 3 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c+dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c + dx]^2) \right) / \left( d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx]) \right) + \\
 & \left( \sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c+dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c + dx]^2) \right) / \left( d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx]) \right) - \\
 & \left( 2 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c + dx]^2) \right. \\
 & \quad \left. \sin[c] \right) / \left( d (A + 2C + A \cos[2c + 2dx]) \sqrt{\operatorname{Sec}[c + dx]} (a + a \operatorname{Sec}[c + dx]) \right) + \\
 & \left( 2 C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c + dx]^2) \right. \\
 & \quad \left. \sin[c] \right) / \left( d (A + 2C + A \cos[2c + 2dx]) \sqrt{\operatorname{Sec}[c + dx]} (a + a \operatorname{Sec}[c + dx]) \right) + \\
 & \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 (A + C \operatorname{Sec}[c + dx]^2) \left( -\frac{2(2A + C + A \cos[2c]) \cos[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right]}{d} + \right. \right. \\
 & \quad \left. \left. \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] (A \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{d} + \frac{8 A \cos[c] \sin[dx]}{d} + \frac{4(A + C) \tan\left[\frac{c}{2}\right]}{d} \right) \right) / \\
 & \left( (A + 2C + A \cos[2c + 2dx]) \sqrt{\operatorname{Sec}[c + dx]} (a + a \operatorname{Sec}[c + dx]) \right)
 \end{aligned}$$

**Problem 235: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + C \operatorname{Sec}[c + dx]^2}{\operatorname{Sec}[c + dx]^{3/2} (a + a \operatorname{Sec}[c + dx])} dx$$

Optimal (type 4, 162 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{(3A + C) \sqrt{\cos[c + dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\sec[c + dx]}}{ad} + \\
 & \frac{(5A + 3C) \sqrt{\cos[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\sec[c + dx]}}{3ad} + \\
 & \frac{(5A + 3C) \sin[c + dx]}{3ad \sqrt{\sec[c + dx]}} - \frac{(A + C) \sin[c + dx]}{d \sqrt{\sec[c + dx]} (a + a \sec[c + dx])}
 \end{aligned}$$

Result (type 5, 809 leaves):

$$\begin{aligned}
 & - \left( \left( 3 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c+dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \right. \\
 & \quad \left. \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c+dx]^2) \right) / \left( d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c+dx]) \right) \right) - \\
 & \left( \sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c+dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c+dx]^2) \right) / \left( d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c+dx]) \right) + \\
 & \left( 10 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c+dx]^2) \sin[c] \right) / \\
 & \left( 3 d (A + 2C + A \cos[2c + 2dx]) \sqrt{\operatorname{Sec}[c+dx]} (a + a \operatorname{Sec}[c+dx]) \right) + \\
 & \left( 2 C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c+dx]^2) \sin[c] \right) / \\
 & \left( d (A + 2C + A \cos[2c + 2dx]) \sqrt{\operatorname{Sec}[c+dx]} (a + a \operatorname{Sec}[c+dx]) \right) + \\
 & \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 (A + C \operatorname{Sec}[c+dx]^2) \left( \frac{2(2A + C + A \cos[2c]) \cos[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right]}{d} + \right. \right. \\
 & \quad \frac{4 A \cos[2dx] \sin[2c]}{3 d} - \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] (A \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{d} - \\
 & \quad \left. \left. \frac{8 A \cos[c] \sin[dx]}{d} + \frac{4 A \cos[2c] \sin[2dx]}{3 d} - \frac{4 (A + C) \operatorname{Tan}\left[\frac{c}{2}\right]}{d} \right) \right) / \\
 & \left( (A + 2C + A \cos[2c + 2dx]) \sqrt{\operatorname{Sec}[c+dx]} (a + a \operatorname{Sec}[c+dx]) \right)
 \end{aligned}$$

**Problem 236: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + C \operatorname{Sec}[c + dx]^2}{\operatorname{Sec}[c + dx]^{5/2} (a + a \operatorname{Sec}[c + dx])} dx$$

Optimal (type 4, 199 leaves, 8 steps):

$$\frac{3 (7 A + 5 C) \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\sec [c + d x]}}{5 a d} -$$

$$\frac{(5 A + 3 C) \sqrt{\cos [c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\sec [c + d x]}}{3 a d} +$$

$$\frac{(7 A + 5 C) \sin [c + d x]}{5 a d \sec [c + d x]^{3/2}} - \frac{(5 A + 3 C) \sin [c + d x]}{3 a d \sqrt{\sec [c + d x]}} - \frac{(A + C) \sin [c + d x]}{d \sec [c + d x]^{3/2} (a + a \sec [c + d x])}$$

Result (type 5, 865 leaves):

$$\begin{aligned}
 & \left( 21 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c+dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c + dx]^2) \right) / \left( 5d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx]) \right) + \\
 & \left( 3 \sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c+dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c + dx]^2) \right) / \left( d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx]) \right) - \\
 & \left( 10 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c + dx]^2) \right. \\
 & \quad \left. \sin[c] \right) / \left( 3d (A + 2C + A \cos[2c + 2dx]) \sqrt{\operatorname{Sec}[c + dx]} (a + a \operatorname{Sec}[c + dx]) \right) - \\
 & \left( 2 C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c + dx]^2) \right. \\
 & \quad \left. \sin[c] \right) / \left( d (A + 2C + A \cos[2c + 2dx]) \sqrt{\operatorname{Sec}[c + dx]} (a + a \operatorname{Sec}[c + dx]) \right) + \\
 & \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 (A + C \operatorname{Sec}[c + dx]^2) \left( -\frac{1}{10d} (51A + 40C + 33A \cos[2c] + 20C \cos[2c]) \right. \right. \\
 & \quad \operatorname{Cos}[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] - \frac{4A \cos[2dx] \sin[2c]}{3d} + \frac{2A \cos[3dx] \sin[3c]}{5d} + \\
 & \quad \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] \left( A \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right] \right)}{d} + \frac{2(33A + 20C) \cos[c] \sin[dx]}{5d} - \\
 & \quad \left. \left. \frac{4A \cos[2c] \sin[2dx]}{3d} + \frac{2A \cos[3c] \sin[3dx]}{5d} + \frac{4(A+C) \tan\left[\frac{c}{2}\right]}{d} \right) \right) / \\
 & \left( (A + 2C + A \cos[2c + 2dx]) \sqrt{\operatorname{Sec}[c + dx]} (a + a \operatorname{Sec}[c + dx]) \right)
 \end{aligned}$$

**Problem 237: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c + dx]^{5/2} (A + C \operatorname{Sec}[c + dx]^2)}{(a + a \operatorname{Sec}[c + dx])^2} dx$$

Optimal (type 4, 229 leaves, 9 steps):

$$\begin{aligned}
 & \frac{(A+7C)\sqrt{\cos[c+dx]}\operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]\sqrt{\sec[c+dx]}}{a^2d} + \\
 & \frac{2(A+5C)\sqrt{\cos[c+dx]}\operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]\sqrt{\sec[c+dx]}}{3a^2d} - \\
 & \frac{(A+7C)\sqrt{\sec[c+dx]}\sin[c+dx]}{a^2d} + \frac{2(A+5C)\sec[c+dx]^{3/2}\sin[c+dx]}{3a^2d} - \\
 & \frac{(A+7C)\sec[c+dx]^{5/2}\sin[c+dx]}{3a^2d(1+\sec[c+dx])} - \frac{(A+C)\sec[c+dx]^{7/2}\sin[c+dx]}{3d(a+a\sec[c+dx])^2}
 \end{aligned}$$

Result (type 5, 860 leaves):

$$\begin{aligned}
 & \left( 2\sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c + dx]^2) \right) / \left( d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right) + \\
 & \left( 14\sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c + dx]^2) \right) / \left( d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right) + \\
 & \left( 8A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c + dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \operatorname{Sec}\left[\frac{c}{2}\right] \sqrt{\operatorname{Sec}[c + dx]} \right. \\
 & \quad \left. (A + C \operatorname{Sec}[c + dx]^2) \sin[c] \right) / \left( 3d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right) + \\
 & \left( 40C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c + dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \operatorname{Sec}\left[\frac{c}{2}\right] \sqrt{\operatorname{Sec}[c + dx]} \right. \\
 & \quad \left. (A + C \operatorname{Sec}[c + dx]^2) \sin[c] \right) / \left( 3d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right) + \\
 & \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\operatorname{Sec}[c + dx]} (A + C \operatorname{Sec}[c + dx]^2) \right. \\
 & \quad \left( -\frac{4(A + 7C) \cos[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right]}{d} + \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (A \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{3d} \right. \\
 & \quad \left. \frac{16 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] (A \sin\left[\frac{dx}{2}\right] + 4C \sin\left[\frac{dx}{2}\right])}{3d} + \frac{16C \operatorname{Sec}[c] \operatorname{Sec}[c + dx] \sin[dx]}{3d} \right. \\
 & \quad \left. \left. \frac{16(C + A \cos[c] + 5C \cos[c]) \operatorname{Sec}[c] \tan\left[\frac{c}{2}\right]}{3d} + \frac{4(A + C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{3d} \right) \right) / \\
 & \quad \left( (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right)
 \end{aligned}$$

**Problem 238:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Sec}[c + dx]^{3/2} (A + C \operatorname{Sec}[c + dx]^2)}{(a + a \operatorname{Sec}[c + dx])^2} dx$$

Optimal (type 4, 191 leaves, 8 steps):

$$\begin{aligned}
 & - \frac{4 C \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{a^2 d} + \\
 & \frac{(A-5 C) \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{3 a^2 d} + \frac{4 C \sqrt{\sec [c+d x]} \sin [c+d x]}{a^2 d} + \\
 & \frac{(A-5 C) \sec [c+d x]^{3 / 2} \sin [c+d x]}{3 a^2 d(1+\sec [c+d x])} - \frac{(A+C) \sec [c+d x]^{5 / 2} \sin [c+d x]}{3 d(a+a \sec [c+d x])^2}
 \end{aligned}$$

Result (type 5, 643 leaves):

$$\begin{aligned}
 & - \left( \left( 8 \sqrt{2} C e^{-i(2 c+d x)} \sqrt{\frac{e^{i(c+d x)}}{1+e^{2 i(c+d x)}}} \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \operatorname{Csc} \left[ \frac{c}{2} \right] \right. \right. \\
 & \quad \left. \left. \left( 1+e^{2 i(c+d x)} + (-1+e^{2 i c}) \sqrt{1+e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right] \right) \right. \right. \\
 & \quad \left. \left. \operatorname{Sec} \left[ \frac{c}{2} \right] (A+C \sec [c+d x]^2) \right) \right) / \left( d(A+2 C+A \cos [2 c+2 d x]) (a+a \sec [c+d x])^2 \right) + \\
 & \left( 4 A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \sqrt{\cos [c+d x]} \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \operatorname{Sec} \left[ \frac{c}{2} \right] \right. \\
 & \quad \left. \sqrt{\sec [c+d x]} (A+C \sec [c+d x]^2) \sin [c] \right) / \\
 & \left( 3 d(A+2 C+A \cos [2 c+2 d x]) (a+a \sec [c+d x])^2 \right) - \\
 & \left( 2 \theta C \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \sqrt{\cos [c+d x]} \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \right. \\
 & \quad \left. \operatorname{Sec} \left[ \frac{c}{2} \right] \sqrt{\sec [c+d x]} (A+C \sec [c+d x]^2) \sin [c] \right) / \\
 & \left( 3 d(A+2 C+A \cos [2 c+2 d x]) (a+a \sec [c+d x])^2 \right) + \\
 & \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \sqrt{\sec [c+d x]} (A+C \sec [c+d x]^2) \right. \\
 & \quad \left( \frac{16 C \cos [d x] \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} \right]}{d} + \frac{8 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right] \left( A \sin \left[ \frac{d x}{2} \right] - 5 C \sin \left[ \frac{d x}{2} \right] \right)}{3 d} \right) - \\
 & \quad \frac{4 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^3 \left( A \sin \left[ \frac{d x}{2} \right] + C \sin \left[ \frac{d x}{2} \right] \right)}{3 d} - \frac{8(-A+5 C) \operatorname{Tan} \left[ \frac{c}{2} \right]}{3 d} - \\
 & \quad \left. \left. \frac{4(A+C) \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \operatorname{Tan} \left[ \frac{c}{2} \right]}{3 d} \right) \right) / \left( (A+2 C+A \cos [2 c+2 d x]) (a+a \sec [c+d x])^2 \right)
 \end{aligned}$$



Problem 239: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{\sec [c+d x]} (A+C \sec [c+d x]^2)}{(a+a \sec [c+d x])^2} d x$$

Optimal (type 4, 165 leaves, 7 steps):

$$\begin{aligned} & - \frac{(A-C) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{a^2 d} + \\ & \frac{2(A+C) \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{3 a^2 d} + \\ & \frac{(A-C) \sqrt{\sec [c+d x]} \sin [c+d x]}{a^2 d (1+\sec [c+d x])} - \frac{(A+C) \sec [c+d x]^{3/2} \sin [c+d x]}{3 d (a+a \sec [c+d x])^2} \end{aligned}$$

Result (type 5, 835 leaves):

$$\begin{aligned}
 & - \left( \left( 2 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \right. \\
 & \quad \left. \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c + dx]^2) \right) \right) / \left( d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right) + \\
 & \left( 2 \sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c + dx]^2) \right) / \\
 & \quad \left( d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right) + \\
 & \left( 8 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c + dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] \sqrt{\operatorname{Sec}[c + dx]} (A + C \operatorname{Sec}[c + dx]^2) \sin[c] \right) / \\
 & \quad \left( 3 d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right) + \\
 & \left( 8 C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c + dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] \sqrt{\operatorname{Sec}[c + dx]} (A + C \operatorname{Sec}[c + dx]^2) \sin[c] \right) / \\
 & \quad \left( 3 d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right) + \\
 & \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\operatorname{Sec}[c + dx]} (A + C \operatorname{Sec}[c + dx]^2) \right. \\
 & \quad \left( \frac{4(A - C) \cos[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right]}{d} - \frac{16 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] (2A \sin\left[\frac{dx}{2}\right] - C \sin\left[\frac{dx}{2}\right])}{3d} \right) + \\
 & \quad \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (A \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{3d} - \frac{16(2A - C) \operatorname{Tan}\left[\frac{c}{2}\right]}{3d} + \\
 & \quad \left. \left. \frac{4(A + C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Tan}\left[\frac{c}{2}\right]}{3d} \right) \right) / \left( (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right)
 \end{aligned}$$

Problem 240: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{A + C \operatorname{Sec}[c + d x]^2}{\sqrt{\operatorname{Sec}[c + d x]} (a + a \operatorname{Sec}[c + d x])^2} dx$$

Optimal (type 4, 170 leaves, 7 steps):

$$\frac{4 A \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{a^2 d} - \frac{(5 A - C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{3 a^2 d} - \frac{(5 A - C) \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{3 a^2 d (1 + \operatorname{Sec}[c + d x])} - \frac{(A + C) \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{3 d (a + a \operatorname{Sec}[c + d x])^2}$$

Result (type 5, 659 leaves):

$$\left( 8 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\ \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\ \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c + dx]^2) \right) / \left( d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right) - \\ \left( 20 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c + dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \operatorname{Sec}\left[\frac{c}{2}\right] \sqrt{\operatorname{Sec}[c + dx]} \right. \\ \left. (A + C \operatorname{Sec}[c + dx]^2) \sin[c] \right) / \left( 3 d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right) + \\ \left( 4 C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c + dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \operatorname{Sec}\left[\frac{c}{2}\right] \sqrt{\operatorname{Sec}[c + dx]} \right. \\ \left. (A + C \operatorname{Sec}[c + dx]^2) \sin[c] \right) / \left( 3 d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right) + \\ \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\operatorname{Sec}[c + dx]} (A + C \operatorname{Sec}[c + dx]^2) \left( -\frac{4 A (3 + \cos[2c]) \cos[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right]}{d} \right. \right. \\ \left. \left. \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (A \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{3 d} \right. \right. \\ \left. \left. \frac{8 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] (7 A \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{3 d} + \frac{16 A \cos[c] \sin[dx]}{d} \right. \right. \\ \left. \left. \frac{8 (7 A + C) \tan\left[\frac{c}{2}\right]}{3 d} - \frac{4 (A + C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{3 d} \right) \right) / \left( (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right)$$

**Problem 241: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + C \operatorname{Sec}[c + dx]^2}{\operatorname{Sec}[c + dx]^{3/2} (a + a \operatorname{Sec}[c + dx])^2} dx$$

Optimal (type 4, 201 leaves, 8 steps):

$$\frac{(7A + C) \sqrt{\cos[c + dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\operatorname{Sec}[c + dx]}}{a^2 d} + \\ \frac{2(5A + C) \sqrt{\cos[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\operatorname{Sec}[c + dx]}}{3 a^2 d} + \frac{2(5A + C) \sin[c + dx]}{3 a^2 d \sqrt{\operatorname{Sec}[c + dx]}} - \\ \frac{(7A + C) \sin[c + dx]}{3 a^2 d \sqrt{\operatorname{Sec}[c + dx]} (1 + \operatorname{Sec}[c + dx])} - \frac{(A + C) \sin[c + dx]}{3 d \sqrt{\operatorname{Sec}[c + dx]} (a + a \operatorname{Sec}[c + dx])^2}$$

Result (type 5, 888 leaves):

$$\begin{aligned}
 & - \left( \left( 14 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \right. \\
 & \quad \left. \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c + dx]^2) \right) \right) / \left( d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right) - \\
 & \left( 2 \sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c + dx]^2) \right) / \\
 & \quad \left( d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right) + \\
 & \left( 40 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c + dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] \sqrt{\operatorname{Sec}[c + dx]} (A + C \operatorname{Sec}[c + dx]^2) \sin[c] \right) / \\
 & \quad \left( 3 d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right) + \\
 & \left( 8 C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c + dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] \sqrt{\operatorname{Sec}[c + dx]} (A + C \operatorname{Sec}[c + dx]^2) \sin[c] \right) / \\
 & \quad \left( 3 d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right) + \\
 & \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\operatorname{Sec}[c + dx]} (A + C \operatorname{Sec}[c + dx]^2) \right. \\
 & \quad \left. \left( \frac{4 (5A + C + 2A \cos[2c]) \cos[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right]}{d} + \right. \right. \\
 & \quad \frac{8 A \cos[2dx] \sin[2c]}{3 d} + \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (A \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{3 d} - \\
 & \quad \frac{16 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] (5A \sin\left[\frac{dx}{2}\right] + 2C \sin\left[\frac{dx}{2}\right])}{3 d} - \frac{32 A \cos[c] \sin[dx]}{d} + \\
 & \quad \left. \left. \frac{8 A \cos[2c] \sin[2dx]}{3 d} - \frac{16 (5A + 2C) \tan\left[\frac{c}{2}\right]}{3 d} + \frac{4 (A + C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{3 d} \right) \right) / \\
 & \quad \left( (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right)
 \end{aligned}$$

Problem 242: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{A + C \operatorname{Sec}[c + d x]^2}{\operatorname{Sec}[c + d x]^{5/2} (a + a \operatorname{Sec}[c + d x])^2} dx$$

Optimal (type 4, 236 leaves, 9 steps):

$$\begin{aligned} & \frac{4 (14 A + 5 C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{5 a^2 d} - \\ & \frac{5 (3 A + C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{3 a^2 d} + \\ & \frac{4 (14 A + 5 C) \operatorname{Sin}[c + d x]}{15 a^2 d \operatorname{Sec}[c + d x]^{3/2}} - \frac{5 (3 A + C) \operatorname{Sin}[c + d x]}{3 a^2 d \sqrt{\operatorname{Sec}[c + d x]}} - \\ & \frac{(3 A + C) \operatorname{Sin}[c + d x]}{a^2 d \operatorname{Sec}[c + d x]^{3/2} (1 + \operatorname{Sec}[c + d x])} - \frac{(A + C) \operatorname{Sin}[c + d x]}{3 d \operatorname{Sec}[c + d x]^{3/2} (a + a \operatorname{Sec}[c + d x])^2} \end{aligned}$$

Result (type 5, 941 leaves):

$$\begin{aligned}
 & \left( 112 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c + dx]^2) \right) / \left( 5d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right) + \\
 & \left( 8 \sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c + dx]^2) \right) / \left( d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right) - \\
 & \left( 20 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c + dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \operatorname{Sec}\left[\frac{c}{2}\right] \sqrt{\operatorname{Sec}[c + dx]} \right. \\
 & \quad \left. (A + C \operatorname{Sec}[c + dx]^2) \sin[c] \right) / \left( d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right) - \\
 & \left( 20 C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c + dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \operatorname{Sec}\left[\frac{c}{2}\right] \sqrt{\operatorname{Sec}[c + dx]} \right. \\
 & \quad \left. (A + C \operatorname{Sec}[c + dx]^2) \sin[c] \right) / \left( 3d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right) + \\
 & \frac{1}{(A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\operatorname{Sec}[c + dx]} \\
 & (A + C \operatorname{Sec}[c + dx]^2) \left( -\frac{1}{5d} (151A + 60C + 73A \cos[2c] + 20C \cos[2c]) \cos[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] - \right. \\
 & \quad \frac{16A \cos[2dx] \sin[2c]}{3d} + \frac{4A \cos[3dx] \sin[3c]}{5d} - \\
 & \quad \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (A \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{3d} + \\
 & \quad \frac{8 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] (13A \sin\left[\frac{dx}{2}\right] + 7C \sin\left[\frac{dx}{2}\right])}{3d} + \\
 & \quad \frac{4(73A + 20C) \cos[c] \sin[dx]}{5d} - \frac{16A \cos[2c] \sin[2dx]}{3d} + \\
 & \quad \left. \frac{4A \cos[3c] \sin[3dx]}{5d} + \frac{8(13A + 7C) \tan\left[\frac{c}{2}\right]}{3d} - \frac{4(A + C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{3d} \right)
 \end{aligned}$$

Problem 243: Result unnecessarily involves higher level functions and more



than twice size of optimal antiderivative.

$$\int \frac{\text{Sec}[c + dx]^{7/2} (A + C \text{Sec}[c + dx]^2)}{(a + a \text{Sec}[c + dx])^3} dx$$

Optimal (type 4, 282 leaves, 10 steps):

$$\begin{aligned} & \frac{(9A + 119C) \sqrt{\text{Cos}[c + dx]} \text{EllipticE}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\text{Sec}[c + dx]}}{10a^3d} + \\ & \frac{(A + 11C) \sqrt{\text{Cos}[c + dx]} \text{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\text{Sec}[c + dx]}}{2a^3d} - \\ & \frac{(9A + 119C) \sqrt{\text{Sec}[c + dx]} \text{Sin}[c + dx]}{10a^3d} + \\ & \frac{(A + 11C) \text{Sec}[c + dx]^{3/2} \text{Sin}[c + dx]}{2a^3d} - \frac{(A + C) \text{Sec}[c + dx]^{9/2} \text{Sin}[c + dx]}{5d(a + a \text{Sec}[c + dx])^3} - \\ & \frac{2C \text{Sec}[c + dx]^{7/2} \text{Sin}[c + dx]}{3ad(a + a \text{Sec}[c + dx])^2} - \frac{(9A + 119C) \text{Sec}[c + dx]^{5/2} \text{Sin}[c + dx]}{30d(a^3 + a^3 \text{Sec}[c + dx])} \end{aligned}$$

Result (type 5, 964 leaves):

$$\begin{aligned}
 & \left( 18 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx] (A + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad (5d(A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c+dx])^3) + \\
 & \left( 238 \sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx] (A + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad (5d(A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c+dx])^3) + \\
 & \left( 4A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^{3/2} \right. \\
 & \quad \left. (A + C \operatorname{Sec}[c+dx]^2) \sin[c] \right) / (d(A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c+dx])^3) + \\
 & \left( 44C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^{3/2} \right. \\
 & \quad \left. (A + C \operatorname{Sec}[c+dx]^2) \sin[c] \right) / (d(A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c+dx])^3) + \\
 & \frac{1}{(A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c+dx])^3} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Sec}[c+dx]^{3/2} (A + C \operatorname{Sec}[c+dx]^2) \\
 & \left( -\frac{4(9A + 119C) \cos[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right]}{5d} + \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^5 (A \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{5d} \right) + \\
 & \frac{8 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (3A \sin\left[\frac{dx}{2}\right] + 13C \sin\left[\frac{dx}{2}\right])}{15d} + \\
 & \frac{8 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] (3A \sin\left[\frac{dx}{2}\right] + 29C \sin\left[\frac{dx}{2}\right])}{3d} + \\
 & \frac{32C \operatorname{Sec}[c] \operatorname{Sec}[c+dx] \sin[dx]}{3d} + \frac{8(4C + 3A \cos[c] + 33C \cos[c]) \operatorname{Sec}[c] \operatorname{Tan}\left[\frac{c}{2}\right]}{3d} + \\
 & \frac{8(3A + 13C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Tan}\left[\frac{c}{2}\right]}{15d} + \frac{4(A + C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Tan}\left[\frac{c}{2}\right]}{5d} \Big)
 \end{aligned}$$

Problem 244: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\text{Sec}[c + d x]^{5/2} (A + C \text{Sec}[c + d x]^2)}{(a + a \text{Sec}[c + d x])^3} dx$$

Optimal (type 4, 249 leaves, 9 steps):

$$\begin{aligned} & \frac{(A - 49 C) \sqrt{\text{Cos}[c + d x]} \text{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\text{Sec}[c + d x]}}{10 a^3 d} + \\ & \frac{(A - 13 C) \sqrt{\text{Cos}[c + d x]} \text{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\text{Sec}[c + d x]}}{6 a^3 d} - \\ & \frac{(A - 49 C) \sqrt{\text{Sec}[c + d x]} \text{Sin}[c + d x]}{10 a^3 d} - \frac{(A + C) \text{Sec}[c + d x]^{7/2} \text{Sin}[c + d x]}{5 d (a + a \text{Sec}[c + d x])^3} + \\ & \frac{2 (A - 4 C) \text{Sec}[c + d x]^{5/2} \text{Sin}[c + d x]}{15 a d (a + a \text{Sec}[c + d x])^2} + \frac{(A - 13 C) \text{Sec}[c + d x]^{3/2} \text{Sin}[c + d x]}{6 d (a^3 + a^3 \text{Sec}[c + d x])} \end{aligned}$$

Result (type 5, 933 leaves):

$$\begin{aligned}
 & \left( 2\sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx] (A + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad \left( 5d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c+dx])^3 \right) - \\
 & \left( 98\sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx] (A + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad \left( 5d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c+dx])^3 \right) + \\
 & \left( 4A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^{3/2} \right. \\
 & \quad \left. (A + C \operatorname{Sec}[c+dx]^2) \sin[c] \right) / \left( 3d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c+dx])^3 \right) - \\
 & \left( 52C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^{3/2} \right. \\
 & \quad \left. (A + C \operatorname{Sec}[c+dx]^2) \sin[c] \right) / \left( 3d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c+dx])^3 \right) + \\
 & \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Sec}[c+dx]^{3/2} (A + C \operatorname{Sec}[c+dx]^2) \right. \\
 & \quad \left( -\frac{4(A-49C) \cos[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right]}{5d} + \frac{8 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] (A \sin\left[\frac{dx}{2}\right] - 13C \sin\left[\frac{dx}{2}\right])}{3d} \right) + \\
 & \quad \frac{16 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (A \sin\left[\frac{dx}{2}\right] - 4C \sin\left[\frac{dx}{2}\right])}{15d} - \\
 & \quad \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^5 (A \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{5d} - \frac{8(-A + 13C) \tan\left[\frac{c}{2}\right]}{3d} + \\
 & \quad \left. \left. \frac{16(A-4C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{15d} - \frac{4(A+C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \tan\left[\frac{c}{2}\right]}{5d} \right) \right) / \\
 & \quad \left( (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c+dx])^3 \right)
 \end{aligned}$$

Problem 245: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\text{Sec}[c + dx]^{3/2} (A + C \text{Sec}[c + dx]^2)}{(a + a \text{Sec}[c + dx])^3} dx$$

Optimal (type 4, 220 leaves, 8 steps):

$$\begin{aligned} & - \frac{(A - 9C) \sqrt{\text{Cos}[c + dx]} \text{EllipticE}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\text{Sec}[c + dx]}}{10 a^3 d} + \\ & - \frac{(A + 3C) \sqrt{\text{Cos}[c + dx]} \text{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\text{Sec}[c + dx]}}{6 a^3 d} - \\ & + \frac{(A + C) \text{Sec}[c + dx]^{5/2} \text{Sin}[c + dx]}{5 d (a + a \text{Sec}[c + dx])^3} + \\ & + \frac{2(2A - 3C) \text{Sec}[c + dx]^{3/2} \text{Sin}[c + dx]}{15 a d (a + a \text{Sec}[c + dx])^2} + \frac{(A - 9C) \sqrt{\text{Sec}[c + dx]} \text{Sin}[c + dx]}{10 d (a^3 + a^3 \text{Sec}[c + dx])} \end{aligned}$$

Result (type 5, 932 leaves):

$$\begin{aligned} & - \left( \left( 2\sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \text{Csc}\left[\frac{c}{2}\right] \right. \right. \\ & \quad \left. \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \right. \\ & \quad \left. \left. \text{Sec}\left[\frac{c}{2}\right] \text{Sec}[c + dx] (A + C \text{Sec}[c + dx]^2) \right) \right) / \\ & \quad \left. \left( 5 d (A + 2C + A \text{Cos}[2c + 2dx]) (a + a \text{Sec}[c + dx])^3 \right) \right) + \\ & \left( 18\sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \text{Csc}\left[\frac{c}{2}\right] \right. \\ & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\ & \quad \left. \text{Sec}\left[\frac{c}{2}\right] \text{Sec}[c + dx] (A + C \text{Sec}[c + dx]^2) \right) / \\ & \quad \left( 5 d (A + 2C + A \text{Cos}[2c + 2dx]) (a + a \text{Sec}[c + dx])^3 \right) + \\ & \left( 4A \text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\text{Cos}[c + dx]} \text{Csc}\left[\frac{c}{2}\right] \text{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \right) \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{\operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^{3/2} (A+C \operatorname{Sec}[c+dx]^2) \operatorname{Sin}[c]}{3d(A+2C+A \operatorname{Cos}[2c+2dx]) (a+a \operatorname{Sec}[c+dx])^3} + \right. \\
 & \left( 4C \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\operatorname{Cos}[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \\
 & \left. \frac{\operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^{3/2} (A+C \operatorname{Sec}[c+dx]^2) \operatorname{Sin}[c]}{d(A+2C+A \operatorname{Cos}[2c+2dx]) (a+a \operatorname{Sec}[c+dx])^3} + \right. \\
 & \left. \left( \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Sec}[c+dx]^{3/2} (A+C \operatorname{Sec}[c+dx]^2) \right. \right. \\
 & \left. \left. \left( \frac{4(A-9C) \operatorname{Cos}[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right]}{5d} - \frac{8 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (7A \operatorname{Sin}\left[\frac{dx}{2}\right] - 3C \operatorname{Sin}\left[\frac{dx}{2}\right])}{15d} + \right. \right. \\
 & \left. \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^5 (A \operatorname{Sin}\left[\frac{dx}{2}\right] + C \operatorname{Sin}\left[\frac{dx}{2}\right])}{5d} + \right. \\
 & \left. \frac{8 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] (A \operatorname{Sin}\left[\frac{dx}{2}\right] + 3C \operatorname{Sin}\left[\frac{dx}{2}\right])}{3d} + \frac{8(A+3C) \operatorname{Tan}\left[\frac{c}{2}\right]}{3d} - \right. \\
 & \left. \left. \left. \frac{8(7A-3C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Tan}\left[\frac{c}{2}\right]}{15d} + \frac{4(A+C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Tan}\left[\frac{c}{2}\right]}{5d} \right) \right) \right) / \\
 & \left. \left( (A+2C+A \operatorname{Cos}[2c+2dx]) (a+a \operatorname{Sec}[c+dx])^3 \right) \right)
 \end{aligned}$$

**Problem 246: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\operatorname{Sec}[c+dx]} (A+C \operatorname{Sec}[c+dx]^2)}{(a+a \operatorname{Sec}[c+dx])^3} dx$$

Optimal (type 4, 222 leaves, 8 steps):

$$\begin{aligned}
 & - \frac{(9A-C) \sqrt{\operatorname{Cos}[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\operatorname{Sec}[c+dx]}}{10a^3d} + \\
 & \frac{(3A+C) \sqrt{\operatorname{Cos}[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\operatorname{Sec}[c+dx]}}{6a^3d} - \\
 & \frac{(A+C) \operatorname{Sec}[c+dx]^{3/2} \operatorname{Sin}[c+dx]}{5d(a+a \operatorname{Sec}[c+dx])^3} + \\
 & \frac{2(3A-2C) \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{15ad(a+a \operatorname{Sec}[c+dx])^2} + \frac{(3A+C) \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{6d(a^3+a^3 \operatorname{Sec}[c+dx])}
 \end{aligned}$$

Result (type 5, 934 leaves):

$$\begin{aligned}
 & - \left( \left( 18 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx] (A + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad \left( 5d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c+dx])^3 \right) + \\
 & \left( 2 \sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx] (A + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad \left( 5d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c+dx])^3 \right) + \\
 & \left( 4A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^{3/2} (A + C \operatorname{Sec}[c+dx]^2) \sin[c] \right) / \\
 & \quad \left( d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c+dx])^3 \right) + \\
 & \left( 4C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^{3/2} (A + C \operatorname{Sec}[c+dx]^2) \sin[c] \right) / \\
 & \quad \left( 3d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c+dx])^3 \right) + \\
 & \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Sec}[c+dx]^{3/2} (A + C \operatorname{Sec}[c+dx]^2) \right. \\
 & \quad \left( \frac{4(9A - C) \cos[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right]}{5d} - \frac{8 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] (9A \sin\left[\frac{dx}{2}\right] - C \sin\left[\frac{dx}{2}\right])}{3d} \right. \\
 & \quad \left. \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^5 (A \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{5d} + \right. \\
 & \quad \left. \frac{16 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (6A \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{15d} - \frac{8(9A - C) \tan\left[\frac{c}{2}\right]}{3d} \right) +
 \end{aligned}$$

$$\left( \frac{16 (6 A + C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Tan}\left[\frac{c}{2}\right]}{15 d} - \frac{4 (A + C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Tan}\left[\frac{c}{2}\right]}{5 d} \right) / \left( (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) (a + a \operatorname{Sec}[c + d x])^3 \right)$$

**Problem 247: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + C \operatorname{Sec}[c + d x]^2}{\sqrt{\operatorname{Sec}[c + d x]} (a + a \operatorname{Sec}[c + d x])^3} dx$$

Optimal (type 4, 226 leaves, 8 steps):

$$\begin{aligned} & \frac{(49 A - C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{10 a^3 d} - \\ & \frac{(13 A - C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{6 a^3 d} - \\ & \frac{(A + C) \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{5 d (a + a \operatorname{Sec}[c + d x])^3} - \frac{2 (4 A - C) \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{15 a d (a + a \operatorname{Sec}[c + d x])^2} - \\ & \frac{(13 A - C) \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{6 d (a^3 + a^3 \operatorname{Sec}[c + d x])} \end{aligned}$$

Result (type 5, 955 leaves):



$$\begin{aligned}
 & \left( 98 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx] (A + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad \left( 5d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c+dx])^3 \right) - \\
 & \left( 2 \sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx] (A + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad \left( 5d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c+dx])^3 \right) - \\
 & \left( 52 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^{3/2} \right. \\
 & \quad \left. (A + C \operatorname{Sec}[c+dx]^2) \sin[c] \right) / \left( 3d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c+dx])^3 \right) + \\
 & \left( 4 C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^{3/2} \right. \\
 & \quad \left. (A + C \operatorname{Sec}[c+dx]^2) \sin[c] \right) / \left( 3d (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c+dx])^3 \right) + \\
 & \frac{1}{(A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c+dx])^3} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Sec}[c+dx]^{3/2} \\
 & (A + C \operatorname{Sec}[c+dx]^2) \left( -\frac{4(39A - C + 10A \cos[2c]) \cos[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right]}{5d} + \right. \\
 & \quad \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^5 (A \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{5d} + \\
 & \quad \frac{8 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] (23A \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{3d} - \\
 & \quad \frac{8 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (17A \sin\left[\frac{dx}{2}\right] + 7C \sin\left[\frac{dx}{2}\right])}{15d} + \frac{32A \cos[c] \sin[dx]}{d} + \\
 & \left. \frac{8(23A + C) \tan\left[\frac{c}{2}\right]}{3d} - \frac{8(17A + 7C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{15d} + \frac{4(A + C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \tan\left[\frac{c}{2}\right]}{5d} \right)
 \end{aligned}$$

**Problem 248: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + C \operatorname{Sec}[c + dx]^2}{\operatorname{Sec}[c + dx]^{3/2} (a + a \operatorname{Sec}[c + dx])^3} dx$$

Optimal (type 4, 249 leaves, 9 steps):

$$\begin{aligned} & -\frac{1}{10a^3d} (119A + 9C) \sqrt{\operatorname{Cos}[c + dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\operatorname{Sec}[c + dx]} + \\ & \frac{(11A + C) \sqrt{\operatorname{Cos}[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\operatorname{Sec}[c + dx]}}{2a^3d} + \\ & \frac{(11A + C) \operatorname{Sin}[c + dx]}{2a^3d \sqrt{\operatorname{Sec}[c + dx]}} - \frac{(A + C) \operatorname{Sin}[c + dx]}{5d \sqrt{\operatorname{Sec}[c + dx]} (a + a \operatorname{Sec}[c + dx])^3} - \\ & \frac{2A \operatorname{Sin}[c + dx]}{3ad \sqrt{\operatorname{Sec}[c + dx]} (a + a \operatorname{Sec}[c + dx])^2} - \frac{(119A + 9C) \operatorname{Sin}[c + dx]}{30d \sqrt{\operatorname{Sec}[c + dx]} (a^3 + a^3 \operatorname{Sec}[c + dx])} \end{aligned}$$

Result (type 5, 988 leaves):

$$\begin{aligned} & -\left( \left( 238\sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \right. \\ & \quad \left. \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \right. \\ & \quad \left. \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c + dx] (A + C \operatorname{Sec}[c + dx]^2) \right) \right) / \\ & \quad \left( 5d (A + 2C + A \operatorname{Cos}[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^3 \right) - \\ & \left( 18\sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\ & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\ & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c + dx] (A + C \operatorname{Sec}[c + dx]^2) \right) / \\ & \quad \left( 5d (A + 2C + A \operatorname{Cos}[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^3 \right) + \\ & \left( 44A \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\operatorname{Cos}[c + dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \right. \\ & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c + dx]^{3/2} (A + C \operatorname{Sec}[c + dx]^2) \operatorname{Sin}[c] \right) / \end{aligned}$$

$$\begin{aligned}
 & \left( d (A + 2C + A \cos[2c + 2dx]) (a + a \sec[c + dx])^3 \right) + \\
 & \left( 4C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c + dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c + dx]^{3/2} (A + C \operatorname{Sec}[c + dx]^2) \sin[c] \right) / \\
 & \left( d (A + 2C + A \cos[2c + 2dx]) (a + a \sec[c + dx])^3 \right) + \\
 & \frac{1}{(A + 2C + A \cos[2c + 2dx]) (a + a \sec[c + dx])^3} \\
 & \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Sec}[c + dx]^{3/2} (A + C \operatorname{Sec}[c + dx]^2) \\
 & \left( \frac{4 (89A + 9C + 30A \cos[2c]) \cos[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right]}{5d} + \right. \\
 & \quad \frac{16A \cos[2dx] \sin[2c]}{3d} - \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^5 (A \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{5d} + \\
 & \quad \frac{16 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (11A \sin\left[\frac{dx}{2}\right] + 6C \sin\left[\frac{dx}{2}\right])}{15d} - \\
 & \quad \left. \frac{8 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] (43A \sin\left[\frac{dx}{2}\right] + 9C \sin\left[\frac{dx}{2}\right])}{3d} - \right. \\
 & \quad \frac{96A \cos[c] \sin[dx]}{d} + \frac{16A \cos[2c] \sin[2dx]}{3d} - \frac{8(43A + 9C) \tan\left[\frac{c}{2}\right]}{3d} + \\
 & \quad \left. \frac{16(11A + 6C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{15d} - \frac{4(A + C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \tan\left[\frac{c}{2}\right]}{5d} \right)
 \end{aligned}$$

**Problem 249: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + C \operatorname{Sec}[c + dx]^2}{\operatorname{Sec}[c + dx]^{5/2} (a + a \operatorname{Sec}[c + dx])^3} dx$$

Optimal (type 4, 290 leaves, 10 steps):

$$\begin{aligned}
 & \frac{7(33A + 7C) \sqrt{\cos[c + dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\operatorname{Sec}[c + dx]}}{10a^3 d} - \\
 & \frac{(63A + 13C) \sqrt{\cos[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\operatorname{Sec}[c + dx]}}{6a^3 d} + \\
 & \frac{7(33A + 7C) \sin[c + dx]}{30a^3 d \operatorname{Sec}[c + dx]^{3/2}} - \frac{(63A + 13C) \sin[c + dx]}{6a^3 d \sqrt{\operatorname{Sec}[c + dx]}} - \frac{(A + C) \sin[c + dx]}{5d \operatorname{Sec}[c + dx]^{3/2} (a + a \operatorname{Sec}[c + dx])^3} - \\
 & \frac{2(6A + C) \sin[c + dx]}{15a d \operatorname{Sec}[c + dx]^{3/2} (a + a \operatorname{Sec}[c + dx])^2} - \frac{(63A + 13C) \sin[c + dx]}{10d \operatorname{Sec}[c + dx]^{3/2} (a^3 + a^3 \operatorname{Sec}[c + dx])}
 \end{aligned}$$

Result (type 5, 1032 leaves):

$$\left( 462 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\ \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\ \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx] (A + C \operatorname{Sec}[c+dx]^2) \right) / \\ (5d(A+2C+A \cos[2c+2dx]) (a+a \operatorname{Sec}[c+dx])^3) + \\ \left( 98 \sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\ \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\ \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx] (A + C \operatorname{Sec}[c+dx]^2) \right) / \\ (5d(A+2C+A \cos[2c+2dx]) (a+a \operatorname{Sec}[c+dx])^3) - \\ \left( 84 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^{3/2} \right. \\ \left. (A + C \operatorname{Sec}[c+dx]^2) \sin[c] \right) / (d(A+2C+A \cos[2c+2dx]) (a+a \operatorname{Sec}[c+dx])^3) - \\ \left( 52 C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^{3/2} \right. \\ \left. (A + C \operatorname{Sec}[c+dx]^2) \sin[c] \right) / (3d(A+2C+A \cos[2c+2dx]) (a+a \operatorname{Sec}[c+dx])^3) + \\ \frac{1}{(A+2C+A \cos[2c+2dx]) (a+a \operatorname{Sec}[c+dx])^3} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Sec}[c+dx]^{3/2} (A + C \operatorname{Sec}[c+dx]^2) \\ \left( -\frac{1}{5d} 2(329A+78C+133A \cos[2c]+20C \cos[2c]) \cos[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] - \right. \\ \frac{16A \cos[2dx] \sin[2c]}{d} + \frac{8A \cos[3dx] \sin[3c]}{5d} + \\ \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^5 (A \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{5d} + \\ \frac{184 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] (3A \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{3d} - \\ \left. \frac{8 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (27A \sin\left[\frac{dx}{2}\right] + 17C \sin\left[\frac{dx}{2}\right])}{15d} + \frac{8(133A+20C) \cos[c] \sin[dx]}{5d} \right)$$

$$\frac{16 A \cos [2 c] \sin [2 d x]}{d} + \frac{8 A \cos [3 c] \sin [3 d x]}{5 d} + \frac{184 (3 A + C) \tan \left[\frac{c}{2}\right]}{3 d} - \left. \frac{8 (27 A + 17 C) \sec \left[\frac{c}{2} + \frac{d x}{2}\right]^2 \tan \left[\frac{c}{2}\right]}{15 d} + \frac{4 (A + C) \sec \left[\frac{c}{2} + \frac{d x}{2}\right]^4 \tan \left[\frac{c}{2}\right]}{5 d} \right)$$

**Problem 261: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \sec [c + d x])^{3/2} (A + C \sec [c + d x]^2)}{\sqrt{\sec [c + d x]}} dx$$

Optimal (type 3, 171 leaves, 5 steps):

$$\frac{a^{3/2} (8 A + 7 C) \operatorname{ArcSinh} \left[ \frac{\sqrt{a} \tan [c + d x]}{\sqrt{a + a \sec [c + d x]}} \right]}{4 d} + \frac{a^2 (8 A - 5 C) \sqrt{\sec [c + d x]} \sin [c + d x]}{4 d \sqrt{a + a \sec [c + d x]}} + \frac{3 a C \sqrt{\sec [c + d x]} \sqrt{a + a \sec [c + d x]} \sin [c + d x]}{4 d} + \frac{C \sqrt{\sec [c + d x]} (a + a \sec [c + d x])^{3/2} \sin [c + d x]}{2 d}$$

Result (type 3, 378 leaves):

$$\left( (8 A + 7 C) \cos [c + d x]^3 \left( -\log [1 + \sec [c + d x]] + \log \left[ \sqrt{\sec [c + d x]} + \sec [c + d x]^{3/2} + \sqrt{1 + \sec [c + d x]} \sqrt{-1 + \sec [c + d x]^2} \right] \right) \right. \\ \left. (a (1 + \sec [c + d x]))^{3/2} \sqrt{-1 + \sec [c + d x]^2} (A + C \sec [c + d x]^2) \sin [c + d x] \right) / \\ \left( 2 d (1 - \cos [c + d x]^2) (A + 2 C + A \cos [2 c + 2 d x]) (1 + \sec [c + d x])^{3/2} + \right. \\ \left. \sqrt{(1 + \cos [c + d x]) \sec [c + d x]} (a (1 + \sec [c + d x]))^{3/2} (A + C \sec [c + d x]^2) \right. \\ \left. \left( \frac{4 A \cos [d x] \sin [c]}{d} + \frac{\sec \left[\frac{c}{2}\right] \sec \left[\frac{c}{2} + \frac{d x}{2}\right] \left( -8 A \sin \left[\frac{d x}{2}\right] + 5 C \sin \left[\frac{d x}{2}\right] \right)}{2 d} + \right. \right. \\ \left. \frac{4 A \cos [c] \sin [d x]}{d} + \frac{C \sec [c] \sec [c + d x] \sin [d x]}{d} - \right. \\ \left. \left. \frac{(-2 C + 8 A \cos [c] - 7 C \cos [c]) \sec [c] \tan \left[\frac{c}{2}\right]}{2 d} \right) \right) / \\ \left( (A + 2 C + A \cos [2 c + 2 d x]) \sec [c + d x]^{3/2} (1 + \sec [c + d x])^{3/2} \right)$$

**Problem 262: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \operatorname{Sec}[c + d x])^{3/2} (A + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[c + d x]^{3/2}} dx$$

Optimal (type 3, 169 leaves, 5 steps):

$$\frac{3 a^{3/2} C \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right]}{d} + \frac{a^2 (8 A-3 C) \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{3 d \sqrt{a+a \operatorname{Sec}[c+d x]}} - \frac{a (2 A-3 C) \sqrt{\operatorname{Sec}[c+d x]} \sqrt{a+a \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{3 d} + \frac{2 A (a+a \operatorname{Sec}[c+d x])^{3/2} \operatorname{Sin}[c+d x]}{3 d \sqrt{\operatorname{Sec}[c+d x]}}$$

Result (type 3, 382 leaves):

$$\left( 6 C \operatorname{Cos}[c+d x]^3 \left( -\operatorname{Log}[1+\operatorname{Sec}[c+d x]] + \operatorname{Log}\left[\sqrt{\operatorname{Sec}[c+d x]} + \operatorname{Sec}[c+d x]^{3/2} + \sqrt{1+\operatorname{Sec}[c+d x]} \sqrt{-1+\operatorname{Sec}[c+d x]^2}\right] \right) \right. \\ \left. (a (1+\operatorname{Sec}[c+d x]))^{3/2} \sqrt{-1+\operatorname{Sec}[c+d x]^2} (A+C \operatorname{Sec}[c+d x]^2) \operatorname{Sin}[c+d x] \right) / \\ \left( d (1-\operatorname{Cos}[c+d x]^2) (A+2 C+A \operatorname{Cos}[2 c+2 d x]) (1+\operatorname{Sec}[c+d x])^{3/2} + \sqrt{(1+\operatorname{Cos}[c+d x]) \operatorname{Sec}[c+d x]} (a (1+\operatorname{Sec}[c+d x]))^{3/2} \right. \\ \left. (A+C \operatorname{Sec}[c+d x]^2) \left( \frac{16 A \operatorname{Cos}[d x] \operatorname{Sin}[c]}{3 d} + \frac{2 A \operatorname{Cos}[2 d x] \operatorname{Sin}[2 c]}{3 d} - \frac{2 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right] \left(8 A \operatorname{Sin}\left[\frac{d x}{2}\right]-3 C \operatorname{Sin}\left[\frac{d x}{2}\right]\right)}{3 d} + \frac{16 A \operatorname{Cos}[c] \operatorname{Sin}[d x]}{3 d} + \frac{2 A \operatorname{Cos}[2 c] \operatorname{Sin}[2 d x]}{3 d} - \frac{2 (8 A-3 C) \operatorname{Tan}\left[\frac{c}{2}\right]}{3 d} \right) \right) / \\ \left( (A+2 C+A \operatorname{Cos}[2 c+2 d x]) \operatorname{Sec}[c+d x]^{3/2} (1+\operatorname{Sec}[c+d x])^{3/2} \right)$$

**Problem 263: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \operatorname{Sec}[c + d x])^{3/2} (A + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[c + d x]^{5/2}} dx$$

Optimal (type 3, 163 leaves, 5 steps):

$$\frac{2 a^{3/2} C \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right]}{d} + \frac{2 a^2 (4 A+5 C) \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{5 d \sqrt{a+a \operatorname{Sec}[c+d x]}} +$$

$$\frac{2 a A \sqrt{a+a \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{5 d \sqrt{\operatorname{Sec}[c+d x]}} + \frac{2 A (a+a \operatorname{Sec}[c+d x])^{3/2} \operatorname{Sin}[c+d x]}{5 d \operatorname{Sec}[c+d x]^{3/2}}$$

Result (type 3, 428 leaves):

$$\left(4 C \operatorname{Cos}[c+d x]^3 \left(-\operatorname{Log}[1+\operatorname{Sec}[c+d x]] + \operatorname{Log}\left[\sqrt{\operatorname{Sec}[c+d x]} + \operatorname{Sec}[c+d x]^{3/2} + \sqrt{1+\operatorname{Sec}[c+d x]} \sqrt{-1+\operatorname{Sec}[c+d x]^2}\right]\right) \right.$$

$$\left. (a(1+\operatorname{Sec}[c+d x]))^{3/2} \sqrt{-1+\operatorname{Sec}[c+d x]^2} (A+C \operatorname{Sec}[c+d x]^2) \operatorname{Sin}[c+d x]\right) /$$

$$\left(d(1-\operatorname{Cos}[c+d x]^2)(A+2 C+A \operatorname{Cos}[2 c+2 d x])(1+\operatorname{Sec}[c+d x])^{3/2} + \sqrt{(1+\operatorname{Cos}[c+d x]) \operatorname{Sec}[c+d x]} (a(1+\operatorname{Sec}[c+d x]))^{3/2} (A+C \operatorname{Sec}[c+d x]^2) \right.$$

$$\left.\left(\frac{(17 A+20 C) \operatorname{Cos}[d x] \operatorname{Sin}[c]}{5 d} + \frac{4 A \operatorname{Cos}[2 d x] \operatorname{Sin}[2 c]}{5 d} + \frac{A \operatorname{Cos}[3 d x] \operatorname{Sin}[3 c]}{5 d} - \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right] \left(4 A \operatorname{Sin}\left[\frac{d x}{2}\right] + 5 C \operatorname{Sin}\left[\frac{d x}{2}\right]\right)}{5 d} + \frac{(17 A+20 C) \operatorname{Cos}[c] \operatorname{Sin}[d x]}{5 d} + \frac{4 A \operatorname{Cos}[2 c] \operatorname{Sin}[2 d x]}{5 d} + \frac{A \operatorname{Cos}[3 c] \operatorname{Sin}[3 d x]}{5 d} - \frac{4(4 A+5 C) \operatorname{Tan}\left[\frac{c}{2}\right]}{5 d}\right)\right) /$$

$$\left((A+2 C+A \operatorname{Cos}[2 c+2 d x]) \operatorname{Sec}[c+d x]^{3/2} (1+\operatorname{Sec}[c+d x])^{3/2}\right)$$

**Problem 272: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a+a \operatorname{Sec}[c+d x])^{5/2} (A+C \operatorname{Sec}[c+d x]^2)}{\operatorname{Sec}[c+d x]^{5/2}} dx$$

Optimal (type 3, 210 leaves, 6 steps):

$$\frac{5 a^{5/2} C \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right]}{d} + \frac{a^3 (64 A+15 C) \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{15 d \sqrt{a+a \operatorname{Sec}[c+d x]}} -$$

$$\frac{a^2 (16 A-15 C) \sqrt{\operatorname{Sec}[c+d x]} \sqrt{a+a \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{15 d} +$$

$$\frac{2 a A (a+a \operatorname{Sec}[c+d x])^{3/2} \operatorname{Sin}[c+d x]}{3 d \sqrt{\operatorname{Sec}[c+d x]}} + \frac{2 A (a+a \operatorname{Sec}[c+d x])^{5/2} \operatorname{Sin}[c+d x]}{5 d \operatorname{Sec}[c+d x]^{3/2}}$$

Result (type 3, 428 leaves):

$$\begin{aligned} & \left( 10 C \cos [c+d x]^3 \left( -\operatorname{Log}[1+\operatorname{Sec}[c+d x]] + \right. \right. \\ & \quad \left. \left. \operatorname{Log}\left[\sqrt{\operatorname{Sec}[c+d x]} + \operatorname{Sec}[c+d x]^{3/2} + \sqrt{1+\operatorname{Sec}[c+d x]}} \sqrt{-1+\operatorname{Sec}[c+d x]^2}\right] \right) \right. \\ & \quad \left. (a(1+\operatorname{Sec}[c+d x]))^{5/2} \sqrt{-1+\operatorname{Sec}[c+d x]^2} (A+C \operatorname{Sec}[c+d x]^2) \operatorname{Sin}[c+d x] \right) / \\ & \quad \left( d(1-\cos [c+d x]^2) (A+2 C+A \cos [2 c+2 d x]) (1+\operatorname{Sec}[c+d x])^{5/2} \right) + \\ & \quad \left( \sqrt{(1+\cos [c+d x]) \operatorname{Sec}[c+d x]} (a(1+\operatorname{Sec}[c+d x]))^{5/2} (A+C \operatorname{Sec}[c+d x]^2) \right. \\ & \quad \left( \frac{(131 A+60 C) \cos [d x] \operatorname{Sin}[c]}{15 d} + \frac{22 A \cos [2 d x] \operatorname{Sin}[2 c]}{15 d} + \frac{A \cos [3 d x] \operatorname{Sin}[3 c]}{5 d} - \right. \\ & \quad \left. \frac{2 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right] \left(64 A \operatorname{Sin}\left[\frac{d x}{2}\right]+15 C \operatorname{Sin}\left[\frac{d x}{2}\right]\right)}{15 d} + \frac{(131 A+60 C) \cos [c] \operatorname{Sin}[d x]}{15 d} \right. \\ & \quad \left. \frac{22 A \cos [2 c] \operatorname{Sin}[2 d x]}{15 d} + \frac{A \cos [3 c] \operatorname{Sin}[3 d x]}{5 d} - \frac{2(64 A+15 C) \operatorname{Tan}\left[\frac{c}{2}\right]}{15 d} \right) \right) / \\ & \quad \left( (A+2 C+A \cos [2 c+2 d x]) \operatorname{Sec}[c+d x]^{3/2} (1+\operatorname{Sec}[c+d x])^{5/2} \right) \end{aligned}$$

**Problem 273: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a+a \operatorname{Sec}[c+d x])^{5/2} (A+C \operatorname{Sec}[c+d x]^2)}{\operatorname{Sec}[c+d x]^{7/2}} dx$$

Optimal (type 3, 210 leaves, 6 steps):

$$\begin{aligned} & \frac{2 a^{5/2} C \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right]}{d} + \frac{2 a^3 (32 A+49 C) \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{21 d \sqrt{a+a \operatorname{Sec}[c+d x]}} + \\ & \frac{2 a^2 (8 A+7 C) \sqrt{a+a \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{21 d \sqrt{\operatorname{Sec}[c+d x]}} + \\ & \frac{2 a A (a+a \operatorname{Sec}[c+d x])^{3/2} \operatorname{Sin}[c+d x]}{7 d \operatorname{Sec}[c+d x]^{3/2}} + \frac{2 A (a+a \operatorname{Sec}[c+d x])^{5/2} \operatorname{Sin}[c+d x]}{7 d \operatorname{Sec}[c+d x]^{5/2}} \end{aligned}$$

Result (type 3, 474 leaves):



$$\begin{aligned}
 & \left( 4 C \cos [c+d x]^3 \left( -\operatorname{Log} [1+\operatorname{Sec} [c+d x]] + \right. \right. \\
 & \quad \left. \left. \operatorname{Log} \left[ \sqrt{\operatorname{Sec} [c+d x]} + \operatorname{Sec} [c+d x]^{3/2} + \sqrt{1+\operatorname{Sec} [c+d x]} \sqrt{-1+\operatorname{Sec} [c+d x]^2} \right] \right) \right. \\
 & \quad \left. (a(1+\operatorname{Sec} [c+d x]))^{5/2} \sqrt{-1+\operatorname{Sec} [c+d x]^2} (A+C \operatorname{Sec} [c+d x]^2) \sin [c+d x] \right) / \\
 & \quad \left( d(1-\cos [c+d x]^2) (A+2 C+A \cos [2 c+2 d x]) (1+\operatorname{Sec} [c+d x])^{5/2} \right) + \\
 & \quad \frac{1}{(A+2 C+A \cos [2 c+2 d x]) \operatorname{Sec} [c+d x]^{3/2} (1+\operatorname{Sec} [c+d x])^{5/2}} \\
 & \quad \sqrt{(1+\cos [c+d x]) \operatorname{Sec} [c+d x]} (a(1+\operatorname{Sec} [c+d x]))^{5/2} (A+C \operatorname{Sec} [c+d x]^2) \\
 & \quad \left( \frac{(137 A+196 C) \cos [d x] \sin [c]}{21 d} + \frac{(31 A+14 C) \cos [2 d x] \sin [2 c]}{21 d} + \frac{3 A \cos [3 d x] \sin [3 c]}{7 d} + \right. \\
 & \quad \frac{A \cos [4 d x] \sin [4 c]}{14 d} - \frac{4 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right] \left( 32 A \sin \left[ \frac{d x}{2} \right] + 49 C \sin \left[ \frac{d x}{2} \right] \right)}{21 d} + \\
 & \quad \frac{(137 A+196 C) \cos [c] \sin [d x]}{21 d} + \frac{(31 A+14 C) \cos [2 c] \sin [2 d x]}{21 d} + \\
 & \quad \left. \frac{3 A \cos [3 c] \sin [3 d x]}{7 d} + \frac{A \cos [4 c] \sin [4 d x]}{14 d} - \frac{4(32 A+49 C) \operatorname{Tan} \left[ \frac{c}{2} \right]}{21 d} \right)
 \end{aligned}$$

**Problem 277: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec} [c+d x]^{5/2} (A+C \operatorname{Sec} [c+d x]^2)}{\sqrt{a+a \operatorname{Sec} [c+d x]}} dx$$

Optimal (type 3, 226 leaves, 8 steps):

$$\begin{aligned}
 & - \frac{(8 A+9 C) \operatorname{ArcSinh} \left[ \frac{\sqrt{a} \operatorname{Tan} [c+d x]}{\sqrt{a+a \operatorname{Sec} [c+d x]}} \right]}{8 \sqrt{a} d} + \\
 & \frac{\sqrt{2} (A+C) \operatorname{ArcTanh} \left[ \frac{\sqrt{a} \sqrt{\operatorname{Sec} [c+d x]} \sin [c+d x]}{\sqrt{2} \sqrt{a+a \operatorname{Sec} [c+d x]}} \right]}{\sqrt{a} d} + \frac{(8 A+7 C) \operatorname{Sec} [c+d x]^{3/2} \sin [c+d x]}{8 d \sqrt{a+a \operatorname{Sec} [c+d x]}} - \\
 & \frac{C \operatorname{Sec} [c+d x]^{5/2} \sin [c+d x]}{12 d \sqrt{a+a \operatorname{Sec} [c+d x]}} + \frac{C \operatorname{Sec} [c+d x]^{7/2} \sin [c+d x]}{3 d \sqrt{a+a \operatorname{Sec} [c+d x]}}
 \end{aligned}$$

Result (type 3, 793 leaves):

$$\begin{aligned}
 & \left( \sqrt{(1 + \cos[c + dx]) \sec[c + dx]} \sqrt{1 + \sec[c + dx]} \right. \\
 & (A + C \sec[c + dx]^2) \left( \frac{(-10C + 24A \cos[c] + 21C \cos[c]) \sin\left[\frac{c}{2}\right]}{6d \left(\cos\left[\frac{c}{2}\right] + \cos\left[\frac{3c}{2}\right]\right)} + \right. \\
 & \frac{\sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right] \left(24A \sin\left[\frac{dx}{2}\right] + 31C \sin\left[\frac{dx}{2}\right]\right)}{12d} + \\
 & \left. \frac{2C \sec[c] \sec[c + dx]^2 \sin[dx]}{3d} + \frac{\sec[c] \sec[c + dx] (4C \sin[c] - 5C \sin[dx])}{6d} \right) \Bigg) \Bigg) \Bigg) \\
 & \left( (A + 2C + A \cos[2c + 2dx]) \sec[c + dx]^{3/2} \sqrt{a(1 + \sec[c + dx])} \right) + \\
 & \frac{1}{8(A + 2C + A \cos[2c + 2dx]) \sqrt{a(1 + \sec[c + dx])}} \\
 & \cos[c + dx]^2 \sqrt{1 + \sec[c + dx]} (A + C \sec[c + dx]^2) \\
 & \left( \frac{1}{2d(1 + \cos[c + dx]) \sqrt{2 - 2\cos[c + dx]^2} \sqrt{1 - \cos[c + dx]^2}} \right. \\
 & (8A + 7C) \cos[c + dx]^2 \left( \log[1 - 2\sec[c + dx] - 3\sec[c + dx]^2 - \right. \\
 & \left. 2\sqrt{2} \sqrt{\sec[c + dx]} \sqrt{1 + \sec[c + dx]} \sqrt{-1 + \sec[c + dx]^2}] - \log[1 - 2\sec[c + dx] - \right. \\
 & \left. 3\sec[c + dx]^2 + 2\sqrt{2} \sqrt{\sec[c + dx]} \sqrt{1 + \sec[c + dx]} \sqrt{-1 + \sec[c + dx]^2}] \right) \\
 & \left. \frac{(1 + \sec[c + dx]) \sqrt{-1 + \sec[c + dx]^2} \sin[c + dx]}{4d(1 + \cos[c + dx]) (1 - \cos[c + dx]^2)} (-8A - 9C) \cos[c + dx]^2 \left( -8 \log[1 + \sec[c + dx]] + \right. \right. \\
 & \left. \left. 8 \log\left[\sqrt{\sec[c + dx]} + \sec[c + dx]^{3/2} + \sqrt{1 + \sec[c + dx]} \sqrt{-1 + \sec[c + dx]^2}\right] + \right. \right. \\
 & \left. \left. \sqrt{2} \left( -\log[1 - 2\sec[c + dx] - 3\sec[c + dx]^2 - 2\sqrt{2} \sqrt{\sec[c + dx]} \sqrt{1 + \sec[c + dx]} \right. \right. \right. \\
 & \left. \left. \left. \sqrt{-1 + \sec[c + dx]^2}\right] + \log[1 - 2\sec[c + dx] - 3\sec[c + dx]^2 + \right. \right. \right. \\
 & \left. \left. \left. 2\sqrt{2} \sqrt{\sec[c + dx]} \sqrt{1 + \sec[c + dx]} \sqrt{-1 + \sec[c + dx]^2}\right] \right) \right) \\
 & \left. (1 + \sec[c + dx]) \sqrt{-1 + \sec[c + dx]^2} \sin[c + dx] \right)
 \end{aligned}$$

**Problem 278: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec[c + dx]^{3/2} (A + C \sec[c + dx]^2)}{\sqrt{a + a \sec[c + dx]}} dx$$

Optimal (type 3, 183 leaves, 7 steps):

$$\frac{(8A+7C) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{4\sqrt{a}d} - \frac{\sqrt{2}(A+C) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{\sqrt{2} \sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{\sqrt{a}d} - \frac{C \operatorname{Sec}[c+dx]^{3/2} \operatorname{Sin}[c+dx]}{4d\sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{C \operatorname{Sec}[c+dx]^{5/2} \operatorname{Sin}[c+dx]}{2d\sqrt{a+a \operatorname{Sec}[c+dx]}}$$

Result (type 3, 730 leaves):

$$\left( \sqrt{(1+\operatorname{Cos}[c+dx]) \operatorname{Sec}[c+dx]} \right. \\ \left. \sqrt{1+\operatorname{Sec}[c+dx]} (A+C \operatorname{Sec}[c+dx]^2) \left( -\frac{C(-2+\operatorname{Cos}[c]) \operatorname{Sin}\left[\frac{c}{2}\right]}{d(\operatorname{Cos}\left[\frac{c}{2}\right]+\operatorname{Cos}\left[\frac{3c}{2}\right])} - \frac{3C \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}+\frac{dx}{2}\right] \operatorname{Sin}\left[\frac{dx}{2}\right]}{2d} + \frac{C \operatorname{Sec}[c] \operatorname{Sec}[c+dx] \operatorname{Sin}[dx]}{d} \right) \right) / \\ \left( (A+2C+A \operatorname{Cos}[2c+2dx]) \operatorname{Sec}[c+dx]^{3/2} \sqrt{a(1+\operatorname{Sec}[c+dx])} \right) + \\ \frac{1}{4(A+2C+A \operatorname{Cos}[2c+2dx]) \sqrt{a(1+\operatorname{Sec}[c+dx])} \operatorname{Cos}[c+dx]^2 \sqrt{1+\operatorname{Sec}[c+dx]} (A+C \operatorname{Sec}[c+dx]^2)} \\ \left( -\left( \left( C \operatorname{Cos}[c+dx]^2 \left( \operatorname{Log}[1-2 \operatorname{Sec}[c+dx]-3 \operatorname{Sec}[c+dx]^2-2\sqrt{2} \sqrt{\operatorname{Sec}[c+dx]} \right. \right. \right. \right. \\ \left. \left. \left. \sqrt{1+\operatorname{Sec}[c+dx]} \sqrt{-1+\operatorname{Sec}[c+dx]^2} \right) - \operatorname{Log}[1-2 \operatorname{Sec}[c+dx]-3 \operatorname{Sec}[c+dx]^2+2\sqrt{2} \sqrt{\operatorname{Sec}[c+dx]} \sqrt{1+\operatorname{Sec}[c+dx]} \sqrt{-1+\operatorname{Sec}[c+dx]^2} \right) \right) \right) \\ \left. (1+\operatorname{Sec}[c+dx]) \sqrt{-1+\operatorname{Sec}[c+dx]^2} \operatorname{Sin}[c+dx] \right) / \\ \left( 2d(1+\operatorname{Cos}[c+dx]) \sqrt{2-2 \operatorname{Cos}[c+dx]^2} \sqrt{1-\operatorname{Cos}[c+dx]^2} \right) - \\ \frac{1}{4d(1+\operatorname{Cos}[c+dx])(1-\operatorname{Cos}[c+dx]^2)} (-8A-7C) \operatorname{Cos}[c+dx]^2 \left( -8 \operatorname{Log}[1+\operatorname{Sec}[c+dx]] + \right. \\ \left. 8 \operatorname{Log}\left[\sqrt{\operatorname{Sec}[c+dx]} + \operatorname{Sec}[c+dx]^{3/2} + \sqrt{1+\operatorname{Sec}[c+dx]} \sqrt{-1+\operatorname{Sec}[c+dx]^2}\right] + \right. \\ \left. \sqrt{2} \left( -\operatorname{Log}[1-2 \operatorname{Sec}[c+dx]-3 \operatorname{Sec}[c+dx]^2-2\sqrt{2} \sqrt{\operatorname{Sec}[c+dx]} \sqrt{1+\operatorname{Sec}[c+dx]} \right. \right. \\ \left. \left. \sqrt{-1+\operatorname{Sec}[c+dx]^2} \right) + \operatorname{Log}[1-2 \operatorname{Sec}[c+dx]-3 \operatorname{Sec}[c+dx]^2+ \right. \\ \left. \left. 2\sqrt{2} \sqrt{\operatorname{Sec}[c+dx]} \sqrt{1+\operatorname{Sec}[c+dx]} \sqrt{-1+\operatorname{Sec}[c+dx]^2} \right) \right) \\ \left. (1+\operatorname{Sec}[c+dx]) \sqrt{-1+\operatorname{Sec}[c+dx]^2} \operatorname{Sin}[c+dx] \right)$$

**Problem 279: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\text{Sec}[c + d x]} (A + C \text{Sec}[c + d x]^2)}{\sqrt{a + a \text{Sec}[c + d x]}} dx$$

Optimal (type 3, 133 leaves, 6 steps):

$$-\frac{C \text{ArcSinh}\left[\frac{\sqrt{a} \text{Tan}[c + d x]}{\sqrt{a + a \text{Sec}[c + d x]}}\right]}{\sqrt{a} d} + \frac{\sqrt{2} (A + C) \text{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\text{Sec}[c + d x]} \text{Sin}[c + d x]}{\sqrt{2} \sqrt{a + a \text{Sec}[c + d x]}}\right]}{\sqrt{a} d} + \frac{C \text{Sec}[c + d x]^{3/2} \text{Sin}[c + d x]}{d \sqrt{a + a \text{Sec}[c + d x]}}$$

Result (type 3, 717 leaves):

$$\begin{aligned}
 & \left( (2A+C) \cos [c+dx]^4 \right. \\
 & \quad \left( \log [1-2 \sec [c+dx]-3 \sec [c+dx]^2-2 \sqrt{2} \sqrt{\sec [c+dx]} \sqrt{1+\sec [c+dx]} \right. \\
 & \quad \quad \left. \sqrt{-1+\sec [c+dx]^2}] - \log [1-2 \sec [c+dx]-3 \sec [c+dx]^2+ \right. \\
 & \quad \quad \left. 2 \sqrt{2} \sqrt{\sec [c+dx]} \sqrt{1+\sec [c+dx]} \sqrt{-1+\sec [c+dx]^2}] \right) \\
 & \quad \left. (1+\sec [c+dx])^{3/2} \sqrt{-1+\sec [c+dx]^2} (A+C \sec [c+dx]^2) \sin [c+dx] \right) / \\
 & \left( 2d(1+\cos [c+dx]) \sqrt{2-2 \cos [c+dx]^2} \sqrt{1-\cos [c+dx]^2} \right. \\
 & \quad \left. (A+2C+A \cos [2c+2dx]) \sqrt{a(1+\sec [c+dx])} \right) - \\
 & \left( C \cos [c+dx]^4 \left( -8 \log [1+\sec [c+dx]] + \right. \right. \\
 & \quad 8 \log [\sqrt{\sec [c+dx]} + \sec [c+dx]^{3/2} + \sqrt{1+\sec [c+dx]} \sqrt{-1+\sec [c+dx]^2}] + \\
 & \quad \sqrt{2} \left( -\log [1-2 \sec [c+dx]-3 \sec [c+dx]^2-2 \sqrt{2} \sqrt{\sec [c+dx]} \right. \\
 & \quad \quad \left. \sqrt{1+\sec [c+dx]} \sqrt{-1+\sec [c+dx]^2}] + \log [1-2 \sec [c+dx]- \right. \\
 & \quad \quad \left. \left. 3 \sec [c+dx]^2+2 \sqrt{2} \sqrt{\sec [c+dx]} \sqrt{1+\sec [c+dx]} \sqrt{-1+\sec [c+dx]^2}] \right) \right) \\
 & \quad \left. (1+\sec [c+dx])^{3/2} \sqrt{-1+\sec [c+dx]^2} (A+C \sec [c+dx]^2) \sin [c+dx] \right) / \\
 & \left( 4d(1+\cos [c+dx]) (1-\cos [c+dx]^2) (A+2C+A \cos [2c+2dx]) \right. \\
 & \quad \left. \sqrt{a(1+\sec [c+dx])} \right) + \\
 & \left( \sqrt{(1+\cos [c+dx]) \sec [c+dx]} \sqrt{1+\sec [c+dx]} (A+C \sec [c+dx]^2) \right. \\
 & \quad \left. \left( \frac{2C \sec [\frac{c}{2}] \sec [\frac{c}{2} + \frac{dx}{2}] \sin [\frac{dx}{2}]}{d} + \frac{2C \tan [\frac{c}{2}]}{d} \right) \right) / \\
 & \left( (A+2C+A \cos [2c+2dx]) \sec [c+dx]^{3/2} \sqrt{a(1+\sec [c+dx])} \right)
 \end{aligned}$$

**Problem 280: Result more than twice size of optimal antiderivative.**

$$\int \frac{A+C \sec [c+dx]^2}{\sqrt{\sec [c+dx]} \sqrt{a+a \sec [c+dx]}} dx$$

Optimal (type 3, 135 leaves, 6 steps):

$$\frac{2 C \operatorname{ArcSinh}\left[\frac{-\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right]}{\sqrt{a} d} - \frac{\sqrt{2}(A+C) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{\sqrt{2} \sqrt{a+a \operatorname{Sec}[c+d x]}}\right]}{\sqrt{a} d} + \frac{2 A \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{d \sqrt{a+a \operatorname{Sec}[c+d x]}}$$

Result (type 3, 504 leaves):

$$\frac{1}{4 d(-1+\operatorname{Sec}[c+d x]) \sqrt{1+\operatorname{Sec}[c+d x]} \sqrt{a(1+\operatorname{Sec}[c+d x])}} \operatorname{Tan}[c+d x] \left( \frac{8 A}{\sqrt{\frac{1}{1+\operatorname{Cos}[c+d x]}}} - 8 A \sqrt{\operatorname{Sec}[c+d x]} \sqrt{1+\operatorname{Sec}[c+d x]} + 8 C \operatorname{Log}[1+\operatorname{Sec}[c+d x]] \sqrt{\operatorname{Tan}[c+d x]^2} - 8 C \operatorname{Log}\left[\sqrt{\operatorname{Sec}[c+d x]} + \operatorname{Sec}[c+d x]^{3/2} + \sqrt{1+\operatorname{Sec}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]^2}\right] \sqrt{\operatorname{Tan}[c+d x]^2} + \sqrt{2} A \operatorname{Log}\left[1-2 \operatorname{Sec}[c+d x]-3 \operatorname{Sec}[c+d x]^2-2 \sqrt{2} \sqrt{\operatorname{Sec}[c+d x]} \sqrt{1+\operatorname{Sec}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]^2}\right] \sqrt{\operatorname{Tan}[c+d x]^2} + \sqrt{2} C \operatorname{Log}\left[1-2 \operatorname{Sec}[c+d x]-3 \operatorname{Sec}[c+d x]^2-2 \sqrt{2} \sqrt{\operatorname{Sec}[c+d x]} \sqrt{1+\operatorname{Sec}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]^2}\right] \sqrt{\operatorname{Tan}[c+d x]^2} - \sqrt{2} A \operatorname{Log}\left[1-2 \operatorname{Sec}[c+d x]-3 \operatorname{Sec}[c+d x]^2+2 \sqrt{2} \sqrt{\operatorname{Sec}[c+d x]} \sqrt{1+\operatorname{Sec}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]^2}\right] \sqrt{\operatorname{Tan}[c+d x]^2} - \sqrt{2} C \operatorname{Log}\left[1-2 \operatorname{Sec}[c+d x]-3 \operatorname{Sec}[c+d x]^2+2 \sqrt{2} \sqrt{\operatorname{Sec}[c+d x]} \sqrt{1+\operatorname{Sec}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]^2}\right] \sqrt{\operatorname{Tan}[c+d x]^2} \right)$$

**Problem 281: Result more than twice size of optimal antiderivative.**

$$\int \frac{A+C \operatorname{Sec}[c+d x]^2}{\operatorname{Sec}[c+d x]^{3/2} \sqrt{a+a \operatorname{Sec}[c+d x]}} dx$$

Optimal (type 3, 136 leaves, 4 steps):

$$\frac{\sqrt{2}(A+C) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{\sqrt{2} \sqrt{a+a \operatorname{Sec}[c+d x]}}\right]}{\sqrt{a} d} + \frac{2 A \operatorname{Sin}[c+d x]}{3 d \sqrt{\operatorname{Sec}[c+d x]} \sqrt{a+a \operatorname{Sec}[c+d x]}} - \frac{2 A \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{3 d \sqrt{a+a \operatorname{Sec}[c+d x]}}$$

Result (type 3, 462 leaves):

$$\begin{aligned}
 & \left( (A+C) \cos [c+d x]^4 \right. \\
 & \quad \left( \log [1-2 \sec [c+d x]-3 \sec [c+d x]^2-2 \sqrt{2} \sqrt{\sec [c+d x]} \sqrt{1+\sec [c+d x]} \right. \\
 & \quad \quad \left. \sqrt{-1+\sec [c+d x]^2}] - \log [1-2 \sec [c+d x]-3 \sec [c+d x]^2+ \right. \\
 & \quad \quad \left. 2 \sqrt{2} \sqrt{\sec [c+d x]} \sqrt{1+\sec [c+d x]} \sqrt{-1+\sec [c+d x]^2}] \right) \\
 & \quad \left( (1+\sec [c+d x])^{3/2} \sqrt{-1+\sec [c+d x]^2} (A+C \sec [c+d x]^2) \sin [c+d x] \right) / \\
 & \quad \left( d (1+\cos [c+d x]) \sqrt{2-2 \cos [c+d x]^2} \sqrt{1-\cos [c+d x]^2} \right. \\
 & \quad \left. (A+2 C+A \cos [2 c+2 d x]) \sqrt{a (1+\sec [c+d x])} \right) + \\
 & \quad \left( \sqrt{(1+\cos [c+d x]) \sec [c+d x]} \sqrt{1+\sec [c+d x]} (A+C \sec [c+d x]^2) \right. \\
 & \quad \left( -\frac{8 A \cos [d x] \sin [c]}{3 d} + \frac{2 A \cos [2 d x] \sin [2 c]}{3 d} + \frac{8 A \sec \left[\frac{c}{2}\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right] \sin \left[\frac{d x}{2}\right]}{3 d} - \right. \\
 & \quad \left. \frac{8 A \cos [c] \sin [d x]}{3 d} + \frac{2 A \cos [2 c] \sin [2 d x]}{3 d} + \frac{8 A \tan \left[\frac{c}{2}\right]}{3 d} \right) \right) / \\
 & \quad \left( (A+2 C+A \cos [2 c+2 d x]) \sec [c+d x]^{3/2} \sqrt{a (1+\sec [c+d x])} \right)
 \end{aligned}$$

**Problem 282: Result more than twice size of optimal antiderivative.**

$$\int \frac{A+C \sec [c+d x]^2}{\sec [c+d x]^{5/2} \sqrt{a+a \sec [c+d x]}} dx$$

Optimal (type 3, 181 leaves, 5 steps):

$$\begin{aligned}
 & -\frac{\sqrt{2} (A+C) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\sec [c+d x]} \sin [c+d x]}{\sqrt{2} \sqrt{a+a \sec [c+d x]}}\right]}{\sqrt{a} d} + \frac{2 A \sin [c+d x]}{5 d \sec [c+d x]^{3/2} \sqrt{a+a \sec [c+d x]}} - \\
 & \frac{2 A \sin [c+d x]}{15 d \sqrt{\sec [c+d x]} \sqrt{a+a \sec [c+d x]}} + \frac{2 (13 A+15 C) \sqrt{\sec [c+d x]} \sin [c+d x]}{15 d \sqrt{a+a \sec [c+d x]}}
 \end{aligned}$$

Result (type 3, 528 leaves):

$$\begin{aligned}
 & - \left( \left( (A+C) \cos [c+d x]^4 \left( \log [1-2 \operatorname{Sec}[c+d x]-3 \operatorname{Sec}[c+d x]^2 - \right. \right. \right. \\
 & \quad \left. \left. \left. 2 \sqrt{2} \sqrt{\operatorname{Sec}[c+d x]} \sqrt{1+\operatorname{Sec}[c+d x]} \sqrt{-1+\operatorname{Sec}[c+d x]^2} \right] - \log [1-2 \operatorname{Sec}[c+d x]- \right. \right. \\
 & \quad \left. \left. \left. 3 \operatorname{Sec}[c+d x]^2 + 2 \sqrt{2} \sqrt{\operatorname{Sec}[c+d x]} \sqrt{1+\operatorname{Sec}[c+d x]} \sqrt{-1+\operatorname{Sec}[c+d x]^2} \right] \right) \right. \\
 & \quad \left. (1+\operatorname{Sec}[c+d x])^{3/2} \sqrt{-1+\operatorname{Sec}[c+d x]^2} (A+C \operatorname{Sec}[c+d x]^2) \sin [c+d x] \right) / \\
 & \left( d (1+\cos [c+d x]) \sqrt{2-2 \cos [c+d x]^2} \sqrt{1-\cos [c+d x]^2} \right. \\
 & \quad \left. (A+2 C+A \cos [2 c+2 d x]) \sqrt{a(1+\operatorname{Sec}[c+d x])} \right) + \\
 & \left( \sqrt{(1+\cos [c+d x]) \operatorname{Sec}[c+d x]} \sqrt{1+\operatorname{Sec}[c+d x]} (A+C \operatorname{Sec}[c+d x]^2) \right. \\
 & \quad \left( \frac{(71 A+60 C) \cos [d x] \sin [c]}{15 d} - \frac{8 A \cos [2 d x] \sin [2 c]}{15 d} + \frac{A \cos [3 d x] \sin [3 c]}{5 d} - \right. \\
 & \quad \left. \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right] \left(17 A \sin \left[\frac{d x}{2}\right]+15 C \sin \left[\frac{d x}{2}\right]\right)}{15 d} + \frac{(71 A+60 C) \cos [c] \sin [d x]}{15 d} - \right. \\
 & \quad \left. \frac{8 A \cos [2 c] \sin [2 d x]}{15 d} + \frac{A \cos [3 c] \sin [3 d x]}{5 d} - \frac{4(17 A+15 C) \tan \left[\frac{c}{2}\right]}{15 d} \right) / \\
 & \left. \left( (A+2 C+A \cos [2 c+2 d x]) \operatorname{Sec}[c+d x]^{3/2} \sqrt{a(1+\operatorname{Sec}[c+d x])} \right) \right)
 \end{aligned}$$

**Problem 283: Result more than twice size of optimal antiderivative.**

$$\int \frac{A+C \operatorname{Sec}[c+d x]^2}{\operatorname{Sec}[c+d x]^{7/2} \sqrt{a+a \operatorname{Sec}[c+d x]}} dx$$

Optimal (type 3, 224 leaves, 6 steps):

$$\begin{aligned}
 & \frac{\sqrt{2} (A+C) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\operatorname{Sec}[c+d x]} \sin [c+d x]}{\sqrt{2} \sqrt{a+a \operatorname{Sec}[c+d x]}}\right]}{\sqrt{a} d} + \\
 & \frac{2 A \sin [c+d x]}{7 d \operatorname{Sec}[c+d x]^{5/2} \sqrt{a+a \operatorname{Sec}[c+d x]}} - \frac{2 A \sin [c+d x]}{35 d \operatorname{Sec}[c+d x]^{3/2} \sqrt{a+a \operatorname{Sec}[c+d x]}} + \\
 & \frac{2(31 A+35 C) \sin [c+d x]}{105 d \sqrt{\operatorname{Sec}[c+d x]} \sqrt{a+a \operatorname{Sec}[c+d x]}} - \frac{2(43 A+35 C) \sqrt{\operatorname{Sec}[c+d x]} \sin [c+d x]}{105 d \sqrt{a+a \operatorname{Sec}[c+d x]}}
 \end{aligned}$$

Result (type 3, 573 leaves):



$$\begin{aligned}
 & \left( (A + C) \cos[c + dx]^4 \right. \\
 & \left( \log\left[1 - 2 \sec[c + dx] - 3 \sec[c + dx]^2 - 2\sqrt{2} \sqrt{\sec[c + dx]} \sqrt{1 + \sec[c + dx]} \right. \right. \\
 & \left. \left. \sqrt{-1 + \sec[c + dx]^2}\right] - \log\left[1 - 2 \sec[c + dx] - 3 \sec[c + dx]^2 + \right. \right. \\
 & \left. \left. 2\sqrt{2} \sqrt{\sec[c + dx]} \sqrt{1 + \sec[c + dx]} \sqrt{-1 + \sec[c + dx]^2}\right] \right) \\
 & \left. (1 + \sec[c + dx])^{3/2} \sqrt{-1 + \sec[c + dx]^2} (A + C \sec[c + dx]^2) \sin[c + dx] \right) / \\
 & \left( d (1 + \cos[c + dx]) \sqrt{2 - 2 \cos[c + dx]^2} \sqrt{1 - \cos[c + dx]^2} \right. \\
 & \left. (A + 2C + A \cos[2c + 2dx]) \sqrt{a(1 + \sec[c + dx])} \right) + \\
 & \frac{1}{(A + 2C + A \cos[2c + 2dx]) \sec[c + dx]^{3/2} \sqrt{a(1 + \sec[c + dx])} \sqrt{(1 + \cos[c + dx]) \sec[c + dx]} \sqrt{1 + \sec[c + dx]}} \\
 & (A + C \sec[c + dx]^2) \left( -\frac{2(193A + 140C) \cos[dx] \sin[c]}{105d} + \right. \\
 & \frac{(113A + 70C) \cos[2dx] \sin[2c]}{105d} - \frac{6A \cos[3dx] \sin[3c]}{35d} + \\
 & \frac{A \cos[4dx] \sin[4c]}{14d} + \frac{8 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right] (46A \sin\left[\frac{dx}{2}\right] + 35C \sin\left[\frac{dx}{2}\right])}{105d} - \\
 & \frac{2(193A + 140C) \cos[c] \sin[dx]}{105d} + \frac{(113A + 70C) \cos[2c] \sin[2dx]}{105d} - \\
 & \left. \frac{6A \cos[3c] \sin[3dx]}{35d} + \frac{A \cos[4c] \sin[4dx]}{14d} + \frac{8(46A + 35C) \tan\left[\frac{c}{2}\right]}{105d} \right)
 \end{aligned}$$

**Problem 284: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec[c + dx]^{3/2} (A + C \sec[c + dx]^2)}{(a + a \sec[c + dx])^{3/2}} dx$$

Optimal (type 3, 188 leaves, 7 steps):

$$\begin{aligned}
 & -\frac{3C \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan[c + dx]}{\sqrt{a + a \sec[c + dx]}}\right]}{a^{3/2} d} + \frac{(A + 9C) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\sec[c + dx]} \sin[c + dx]}{\sqrt{2} \sqrt{a + a \sec[c + dx]}}\right]}{2\sqrt{2} a^{3/2} d} - \\
 & \frac{(A + C) \sec[c + dx]^{5/2} \sin[c + dx]}{2d(a + a \sec[c + dx])^{3/2}} + \frac{(A + 3C) \sec[c + dx]^{3/2} \sin[c + dx]}{2ad\sqrt{a + a \sec[c + dx]}}
 \end{aligned}$$

Result (type 3, 800 leaves):

$$\begin{aligned}
 & \frac{1}{2 (A + 2 C + A \cos [2 c + 2 d x]) (a (1 + \sec [c + d x]))^{3/2}} \\
 & \cos [c + d x]^2 (1 + \sec [c + d x])^{3/2} (A + C \sec [c + d x]^2) \\
 & \left( \frac{1}{2 d (1 + \cos [c + d x]) \sqrt{2 - 2 \cos [c + d x]^2} \sqrt{1 - \cos [c + d x]^2}} (A + 3 C) \cos [c + d x]^2 \right. \\
 & \left( \log [1 - 2 \sec [c + d x] - 3 \sec [c + d x]^2 - 2 \sqrt{2} \sqrt{\sec [c + d x]} \sqrt{1 + \sec [c + d x]} \right. \\
 & \left. \sqrt{-1 + \sec [c + d x]^2}] - \log [1 - 2 \sec [c + d x] - 3 \sec [c + d x]^2 + \right. \\
 & \left. 2 \sqrt{2} \sqrt{\sec [c + d x]} \sqrt{1 + \sec [c + d x]} \sqrt{-1 + \sec [c + d x]^2}] \right) \\
 & (1 + \sec [c + d x]) \sqrt{-1 + \sec [c + d x]^2} \sin [c + d x] - \\
 & \frac{1}{2 d (1 + \cos [c + d x]) (1 - \cos [c + d x]^2)} 3 C \cos [c + d x]^2 \left( -8 \log [1 + \sec [c + d x]] + \right. \\
 & \left. 8 \log [\sqrt{\sec [c + d x]} + \sec [c + d x]^{3/2} + \sqrt{1 + \sec [c + d x]} \sqrt{-1 + \sec [c + d x]^2}] + \right. \\
 & \left. \sqrt{2} \left( -\log [1 - 2 \sec [c + d x] - 3 \sec [c + d x]^2 - 2 \sqrt{2} \sqrt{\sec [c + d x]} \sqrt{1 + \sec [c + d x]} \right. \right. \\
 & \left. \left. \sqrt{-1 + \sec [c + d x]^2}] + \log [1 - 2 \sec [c + d x] - 3 \sec [c + d x]^2 + \right. \right. \\
 & \left. \left. 2 \sqrt{2} \sqrt{\sec [c + d x]} \sqrt{1 + \sec [c + d x]} \sqrt{-1 + \sec [c + d x]^2}] \right) \right) \\
 & (1 + \sec [c + d x]) \sqrt{-1 + \sec [c + d x]^2} \sin [c + d x] \Big) + \\
 & \left( \sqrt{(1 + \cos [c + d x]) \sec [c + d x]} (1 + \sec [c + d x])^{3/2} \right. \\
 & (A + C \sec [c + d x]^2) \\
 & \left( \frac{\sec [\frac{c}{2}] \sec [\frac{c}{2} + \frac{dx}{2}]^2 (-A \sin [\frac{c}{2}] - C \sin [\frac{c}{2}])}{2 d} + \right. \\
 & \frac{\sec [\frac{c}{2}] \sec [\frac{c}{2} + \frac{dx}{2}]^3 (-A \sin [\frac{dx}{2}] - C \sin [\frac{dx}{2}])}{2 d} + \\
 & \left. \frac{\sec [\frac{c}{2}] \sec [\frac{c}{2} + \frac{dx}{2}] (A \sin [\frac{dx}{2}] + 3 C \sin [\frac{dx}{2}])}{d} + \frac{(A + 3 C) \tan [\frac{c}{2}]}{d} \right) \Big) / \\
 & \left( (A + 2 C + A \cos [2 c + 2 d x]) \sec [c + d x]^{3/2} (a (1 + \sec [c + d x]))^{3/2} \right)
 \end{aligned}$$

**Problem 285: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\sec [c + d x]} (A + C \sec [c + d x]^2)}{(a + a \sec [c + d x])^{3/2}} dx$$

Optimal (type 3, 145 leaves, 6 steps):

$$\frac{2 C \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right]}{a^{3/2} d} + \frac{(3 A - 5 C) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{\sqrt{2} \sqrt{a+a \operatorname{Sec}[c+d x]}}\right]}{2 \sqrt{2} a^{3/2} d} - \frac{(A + C) \operatorname{Sec}[c+d x]^{3/2} \operatorname{Sin}[c+d x]}{2 d (a + a \operatorname{Sec}[c+d x])^{3/2}}$$

Result (type 3, 795 leaves):

$$\begin{aligned}
 & \frac{1}{2 (A + 2 C + A \cos [2 c + 2 d x]) (a (1 + \sec [c + d x]))^{3/2}} \\
 & \cos [c + d x]^2 (1 + \sec [c + d x])^{3/2} (A + C \sec [c + d x]^2) \\
 & \left( \frac{1}{2 d (1 + \cos [c + d x]) \sqrt{2 - 2 \cos [c + d x]^2} \sqrt{1 - \cos [c + d x]^2}} (3 A - C) \cos [c + d x]^2 \right. \\
 & \left( \log [1 - 2 \sec [c + d x] - 3 \sec [c + d x]^2 - 2 \sqrt{2} \sqrt{\sec [c + d x]} \sqrt{1 + \sec [c + d x]} \right. \\
 & \left. \sqrt{-1 + \sec [c + d x]^2}] - \log [1 - 2 \sec [c + d x] - 3 \sec [c + d x]^2 + \right. \\
 & \left. 2 \sqrt{2} \sqrt{\sec [c + d x]} \sqrt{1 + \sec [c + d x]} \sqrt{-1 + \sec [c + d x]^2}] \right) \\
 & (1 + \sec [c + d x]) \sqrt{-1 + \sec [c + d x]^2} \sin [c + d x] + \\
 & \frac{1}{d (1 + \cos [c + d x]) (1 - \cos [c + d x]^2)} C \cos [c + d x]^2 \left( -8 \log [1 + \sec [c + d x]] + \right. \\
 & \left. 8 \log [\sqrt{\sec [c + d x]} + \sec [c + d x]^{3/2} + \sqrt{1 + \sec [c + d x]} \sqrt{-1 + \sec [c + d x]^2}] + \right. \\
 & \left. \sqrt{2} \left( -\log [1 - 2 \sec [c + d x] - 3 \sec [c + d x]^2 - 2 \sqrt{2} \sqrt{\sec [c + d x]} \sqrt{1 + \sec [c + d x]} \right. \right. \\
 & \left. \left. \sqrt{-1 + \sec [c + d x]^2}] + \log [1 - 2 \sec [c + d x] - 3 \sec [c + d x]^2 + \right. \right. \\
 & \left. \left. 2 \sqrt{2} \sqrt{\sec [c + d x]} \sqrt{1 + \sec [c + d x]} \sqrt{-1 + \sec [c + d x]^2}] \right) \right) \\
 & (1 + \sec [c + d x]) \sqrt{-1 + \sec [c + d x]^2} \sin [c + d x] \Big) + \\
 & \left( \sqrt{(1 + \cos [c + d x]) \sec [c + d x]} (1 + \sec [c + d x])^{3/2} \right. \\
 & (A + C \sec [c + d x]^2) \\
 & \left( \frac{\sec [\frac{c}{2}] \sec [\frac{c}{2} + \frac{dx}{2}]^2 (A \sin [\frac{c}{2}] + C \sin [\frac{c}{2}])}{2 d} + \right. \\
 & \frac{\sec [\frac{c}{2}] \sec [\frac{c}{2} + \frac{dx}{2}] (-A \sin [\frac{dx}{2}] - C \sin [\frac{dx}{2}])}{d} + \\
 & \left. \left. \frac{\sec [\frac{c}{2}] \sec [\frac{c}{2} + \frac{dx}{2}]^3 (A \sin [\frac{dx}{2}] + C \sin [\frac{dx}{2}])}{2 d} - \frac{(A + C) \tan [\frac{c}{2}]}{d} \right) \right) \Big) / \\
 & \left( (A + 2 C + A \cos [2 c + 2 d x]) \sec [c + d x]^{3/2} (a (1 + \sec [c + d x]))^{3/2} \right)
 \end{aligned}$$

**Problem 288: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + C \sec [c + d x]^2}{\sec [c + d x]^{5/2} (a + a \sec [c + d x])^{3/2}} dx$$

Optimal (type 3, 248 leaves, 6 steps):

$$\frac{(15A + 7C) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\sec[c+dx]} \sin[c+dx]}{\sqrt{2} \sqrt{a+a \sec[c+dx]}}\right]}{2\sqrt{2} a^{3/2} d} - \frac{(A+C) \sin[c+dx]}{2d \sec[c+dx]^{3/2} (a+a \sec[c+dx])^{3/2}} + \frac{(9A+5C) \sin[c+dx]}{10ad \sec[c+dx]^{3/2} \sqrt{a+a \sec[c+dx]}} - \frac{(13A+5C) \sin[c+dx]}{10ad \sqrt{\sec[c+dx]} \sqrt{a+a \sec[c+dx]}} + \frac{(49A+25C) \sqrt{\sec[c+dx]} \sin[c+dx]}{10ad \sqrt{a+a \sec[c+dx]}}$$

Result (type 3, 630 leaves):

$$\begin{aligned}
 & - \left( \left( (15A + 7C) \cos[c+dx]^4 \left( \log[1 - 2 \sec[c+dx] - 3 \sec[c+dx]^2 - \right. \right. \right. \\
 & \quad \left. \left. \left. 2\sqrt{2} \sqrt{\sec[c+dx]} \sqrt{1 + \sec[c+dx]} \sqrt{-1 + \sec[c+dx]^2} \right) - \log[1 - 2 \sec[c+dx] - \right. \right. \\
 & \quad \left. \left. 3 \sec[c+dx]^2 + 2\sqrt{2} \sqrt{\sec[c+dx]} \sqrt{1 + \sec[c+dx]} \sqrt{-1 + \sec[c+dx]^2} \right) \right) \\
 & \quad \left. \left. \left. (1 + \sec[c+dx])^{5/2} \sqrt{-1 + \sec[c+dx]^2} (A + C \sec[c+dx]^2) \sin[c+dx] \right) \right) / \\
 & \quad \left( 4d (1 + \cos[c+dx]) \sqrt{2 - 2 \cos[c+dx]^2} \sqrt{1 - \cos[c+dx]^2} \right. \\
 & \quad \left. (A + 2C + A \cos[2c + 2dx]) (a (1 + \sec[c+dx]))^{3/2} \right) + \\
 & \quad \frac{1}{(A + 2C + A \cos[2c + 2dx]) \sec[c+dx]^{3/2} (a (1 + \sec[c+dx]))^{3/2}} \\
 & \quad \sqrt{\frac{(1 + \cos[c+dx]) \sec[c+dx]}{(1 + \sec[c+dx])^{3/2} (A + C \sec[c+dx]^2)}} \\
 & \quad \left( \frac{\sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 (-A \sin\left[\frac{c}{2}\right] - C \sin\left[\frac{c}{2}\right])}{2d} + \right. \\
 & \quad \frac{(57A + 20C) \cos[dx] \sin[c]}{5d} - \frac{6A \cos[2dx] \sin[2c]}{5d} + \\
 & \quad \frac{A \cos[3dx] \sin[3c]}{5d} + \frac{\sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (-A \sin\left[\frac{dx}{2}\right] - C \sin\left[\frac{dx}{2}\right])}{2d} - \\
 & \quad \frac{3 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right] (17A \sin\left[\frac{dx}{2}\right] + 5C \sin\left[\frac{dx}{2}\right])}{5d} + \frac{(57A + 20C) \cos[c] \sin[dx]}{5d} - \\
 & \quad \left. \frac{6A \cos[2c] \sin[2dx]}{5d} + \frac{A \cos[3c] \sin[3dx]}{5d} - \frac{3(17A + 5C) \tan\left[\frac{c}{2}\right]}{5d} \right)
 \end{aligned}$$

**Problem 289: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec[c+dx]^{5/2} (A + C \sec[c+dx]^2)}{(a + a \sec[c+dx])^{5/2}} dx$$

Optimal (type 3, 237 leaves, 8 steps):

$$\begin{aligned}
 & - \frac{5 C \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right]}{a^{5/2} d} + \\
 & \frac{(3 A+115 C) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{\sqrt{2} \sqrt{a+a \operatorname{Sec}[c+d x]}}\right]}{16 \sqrt{2} a^{5/2} d} - \frac{(A+C) \operatorname{Sec}[c+d x]^{7/2} \operatorname{Sin}[c+d x]}{4 d (a+a \operatorname{Sec}[c+d x])^{5/2}} + \\
 & \frac{(A-15 C) \operatorname{Sec}[c+d x]^{5/2} \operatorname{Sin}[c+d x]}{16 a d (a+a \operatorname{Sec}[c+d x])^{3/2}} + \frac{(3 A+35 C) \operatorname{Sec}[c+d x]^{3/2} \operatorname{Sin}[c+d x]}{16 a^2 d \sqrt{a+a \operatorname{Sec}[c+d x]}}
 \end{aligned}$$

Result (type 3, 903 leaves):

$$\begin{aligned}
 & \frac{1}{16 (A + 2C + A \cos [2c + 2dx]) (a (1 + \sec [c + dx]))^{5/2}} \\
 & \cos [c + dx]^2 (1 + \sec [c + dx])^{5/2} (A + C \sec [c + dx]^2) \\
 & \left( \frac{1}{2d (1 + \cos [c + dx]) \sqrt{2 - 2 \cos [c + dx]^2} \sqrt{1 - \cos [c + dx]^2}} (3A + 35C) \cos [c + dx]^2 \right. \\
 & \left( \log [1 - 2 \sec [c + dx] - 3 \sec [c + dx]^2 - 2\sqrt{2} \sqrt{\sec [c + dx]} \sqrt{1 + \sec [c + dx]} \right. \\
 & \left. \sqrt{-1 + \sec [c + dx]^2}] - \log [1 - 2 \sec [c + dx] - 3 \sec [c + dx]^2 + \right. \\
 & \left. 2\sqrt{2} \sqrt{\sec [c + dx]} \sqrt{1 + \sec [c + dx]} \sqrt{-1 + \sec [c + dx]^2}] \right) \\
 & (1 + \sec [c + dx]) \sqrt{-1 + \sec [c + dx]^2} \sin [c + dx] - \\
 & \frac{1}{d (1 + \cos [c + dx]) (1 - \cos [c + dx]^2)} 20C \cos [c + dx]^2 \left( -8 \log [1 + \sec [c + dx]] + \right. \\
 & \left. 8 \log [\sqrt{\sec [c + dx]} + \sec [c + dx]^{3/2} + \sqrt{1 + \sec [c + dx]} \sqrt{-1 + \sec [c + dx]^2}] + \right. \\
 & \left. \sqrt{2} \left( -\log [1 - 2 \sec [c + dx] - 3 \sec [c + dx]^2 - 2\sqrt{2} \sqrt{\sec [c + dx]} \sqrt{1 + \sec [c + dx]} \right. \right. \\
 & \left. \left. \sqrt{-1 + \sec [c + dx]^2}] + \log [1 - 2 \sec [c + dx] - 3 \sec [c + dx]^2 + \right. \right. \\
 & \left. \left. 2\sqrt{2} \sqrt{\sec [c + dx]} \sqrt{1 + \sec [c + dx]} \sqrt{-1 + \sec [c + dx]^2}] \right) \right) \\
 & (1 + \sec [c + dx]) \sqrt{-1 + \sec [c + dx]^2} \sin [c + dx] \Big) + \\
 & \left( \sqrt{(1 + \cos [c + dx]) \sec [c + dx]} (1 + \sec [c + dx])^{5/2} \right. \\
 & (A + C \sec [c + dx]^2) \\
 & \left( \frac{\sec [\frac{c}{2}] \sec [\frac{c}{2} + \frac{dx}{2}]^2 (A \sin [\frac{c}{2}] - 15C \sin [\frac{c}{2}])}{16d} + \right. \\
 & \frac{\sec [\frac{c}{2}] \sec [\frac{c}{2} + \frac{dx}{2}]^4 (-A \sin [\frac{c}{2}] - C \sin [\frac{c}{2}])}{8d} + \\
 & \frac{\sec [\frac{c}{2}] \sec [\frac{c}{2} + \frac{dx}{2}]^3 (A \sin [\frac{dx}{2}] - 15C \sin [\frac{dx}{2}])}{16d} + \\
 & \frac{\sec [\frac{c}{2}] \sec [\frac{c}{2} + \frac{dx}{2}]^5 (-A \sin [\frac{dx}{2}] - C \sin [\frac{dx}{2}])}{8d} + \\
 & \left. \frac{\sec [\frac{c}{2}] \sec [\frac{c}{2} + \frac{dx}{2}] (3A \sin [\frac{dx}{2}] + 35C \sin [\frac{dx}{2}])}{8d} + \frac{(3A + 35C) \tan [\frac{c}{2}]}{8d} \right) \Big) / \\
 & ((A + 2C + A \cos [2c + 2dx]) \sec [c + dx]^{3/2} (a (1 + \sec [c + dx]))^{5/2})
 \end{aligned}$$

Problem 290: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Sec}[c + d x]^{3/2} (A + C \text{Sec}[c + d x]^2)}{(a + a \text{Sec}[c + d x])^{5/2}} dx$$

Optimal (type 3, 192 leaves, 7 steps):

$$\frac{2 C \text{ArcSinh}\left[\frac{\sqrt{a} \text{Tan}[c+d x]}{\sqrt{a+a \text{Sec}[c+d x]}}\right]}{a^{5/2} d} + \frac{(5 A - 43 C) \text{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\text{Sec}[c+d x]} \text{Sin}[c+d x]}{\sqrt{2} \sqrt{a+a \text{Sec}[c+d x]}}\right]}{16 \sqrt{2} a^{5/2} d} - \frac{(A + C) \text{Sec}[c + d x]^{5/2} \text{Sin}[c + d x]}{4 d (a + a \text{Sec}[c + d x])^{5/2}} + \frac{(5 A - 11 C) \text{Sec}[c + d x]^{3/2} \text{Sin}[c + d x]}{16 a d (a + a \text{Sec}[c + d x])^{3/2}}$$

Result (type 3, 901 leaves):



$$\begin{aligned}
 & \frac{1}{16 (A + 2C + A \cos [2c + 2dx]) (a (1 + \sec [c + dx]))^{5/2}} \\
 & \cos [c + dx]^2 (1 + \sec [c + dx])^{5/2} (A + C \sec [c + dx]^2) \\
 & \left( \frac{1}{2d (1 + \cos [c + dx]) \sqrt{2 - 2 \cos [c + dx]^2} \sqrt{1 - \cos [c + dx]^2}} (5A - 11C) \cos [c + dx]^2 \right. \\
 & \left( \log [1 - 2 \sec [c + dx] - 3 \sec [c + dx]^2 - 2\sqrt{2} \sqrt{\sec [c + dx]} \sqrt{1 + \sec [c + dx]} \right. \\
 & \left. \sqrt{-1 + \sec [c + dx]^2}] - \log [1 - 2 \sec [c + dx] - 3 \sec [c + dx]^2 + \right. \\
 & \left. 2\sqrt{2} \sqrt{\sec [c + dx]} \sqrt{1 + \sec [c + dx]} \sqrt{-1 + \sec [c + dx]^2}] \right) \\
 & (1 + \sec [c + dx]) \sqrt{-1 + \sec [c + dx]^2} \sin [c + dx] + \\
 & \frac{1}{d (1 + \cos [c + dx]) (1 - \cos [c + dx]^2)} 8C \cos [c + dx]^2 \left( -8 \log [1 + \sec [c + dx]] + \right. \\
 & \left. 8 \log [\sqrt{\sec [c + dx]} + \sec [c + dx]^{3/2} + \sqrt{1 + \sec [c + dx]} \sqrt{-1 + \sec [c + dx]^2}] + \right. \\
 & \left. \sqrt{2} \left( -\log [1 - 2 \sec [c + dx] - 3 \sec [c + dx]^2 - 2\sqrt{2} \sqrt{\sec [c + dx]} \sqrt{1 + \sec [c + dx]} \right. \right. \\
 & \left. \left. \sqrt{-1 + \sec [c + dx]^2}] + \log [1 - 2 \sec [c + dx] - 3 \sec [c + dx]^2 + \right. \right. \\
 & \left. \left. 2\sqrt{2} \sqrt{\sec [c + dx]} \sqrt{1 + \sec [c + dx]} \sqrt{-1 + \sec [c + dx]^2}] \right) \right) \\
 & (1 + \sec [c + dx]) \sqrt{-1 + \sec [c + dx]^2} \sin [c + dx] \Big) + \\
 & \left( \sqrt{(1 + \cos [c + dx]) \sec [c + dx]} (1 + \sec [c + dx])^{5/2} \right. \\
 & (A + C \sec [c + dx]^2) \\
 & \left( \frac{\sec [\frac{c}{2}] \sec [\frac{c}{2} + \frac{dx}{2}]^4 (A \sin [\frac{c}{2}] + C \sin [\frac{c}{2}])}{8d} + \right. \\
 & \frac{\sec [\frac{c}{2}] \sec [\frac{c}{2} + \frac{dx}{2}]^2 (-9A \sin [\frac{c}{2}] + 7C \sin [\frac{c}{2}])}{16d} + \\
 & \frac{\sec [\frac{c}{2}] \sec [\frac{c}{2} + \frac{dx}{2}] (5A \sin [\frac{dx}{2}] - 11C \sin [\frac{dx}{2}])}{8d} + \\
 & \frac{\sec [\frac{c}{2}] \sec [\frac{c}{2} + \frac{dx}{2}]^5 (A \sin [\frac{dx}{2}] + C \sin [\frac{dx}{2}])}{8d} + \\
 & \left. \left. \frac{\sec [\frac{c}{2}] \sec [\frac{c}{2} + \frac{dx}{2}]^3 (-9A \sin [\frac{dx}{2}] + 7C \sin [\frac{dx}{2}])}{16d} + \frac{(5A - 11C) \tan [\frac{c}{2}]}{8d} \right) \right) / \\
 & \left( (A + 2C + A \cos [2c + 2dx]) \sec [c + dx]^{3/2} (a (1 + \sec [c + dx]))^{5/2} \right)
 \end{aligned}$$

**Problem 294: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + C \operatorname{Sec}[c + d x]^2}{\operatorname{Sec}[c + d x]^{5/2} (a + a \operatorname{Sec}[c + d x])^{5/2}} dx$$

Optimal (type 3, 295 leaves, 7 steps):

$$\begin{aligned} & - \frac{(283 A + 75 C) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{\sqrt{2} \sqrt{a+a \operatorname{Sec}[c+d x]}}\right]}{16 \sqrt{2} a^{5/2} d} - \frac{(A + C) \operatorname{Sin}[c + d x]}{4 d \operatorname{Sec}[c + d x]^{3/2} (a + a \operatorname{Sec}[c + d x])^{5/2}} \\ & + \frac{(21 A + 5 C) \operatorname{Sin}[c + d x]}{16 a d \operatorname{Sec}[c + d x]^{3/2} (a + a \operatorname{Sec}[c + d x])^{3/2}} + \frac{(157 A + 45 C) \operatorname{Sin}[c + d x]}{80 a^2 d \operatorname{Sec}[c + d x]^{3/2} \sqrt{a + a \operatorname{Sec}[c + d x]}} \\ & + \frac{(787 A + 195 C) \operatorname{Sin}[c + d x]}{240 a^2 d \sqrt{\operatorname{Sec}[c + d x]} \sqrt{a + a \operatorname{Sec}[c + d x]}} + \frac{(2671 A + 735 C) \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{240 a^2 d \sqrt{a + a \operatorname{Sec}[c + d x]}} \end{aligned}$$

Result (type 3, 722 leaves):

$$\begin{aligned}
 & - \left( \left( (283 A + 75 C) \cos [c + d x]^4 \left( \log [1 - 2 \sec [c + d x] - 3 \sec [c + d x]^2 - \right. \right. \right. \\
 & \quad \left. \left. \left. 2 \sqrt{2} \sqrt{\sec [c + d x]} \sqrt{1 + \sec [c + d x]} \sqrt{-1 + \sec [c + d x]^2} \right) - \log [1 - 2 \sec [c + d x] - \right. \right. \\
 & \quad \left. \left. 3 \sec [c + d x]^2 + 2 \sqrt{2} \sqrt{\sec [c + d x]} \sqrt{1 + \sec [c + d x]} \sqrt{-1 + \sec [c + d x]^2} \right) \right) \\
 & \quad \left. \left. \left. (1 + \sec [c + d x])^{7/2} \sqrt{-1 + \sec [c + d x]^2} (A + C \sec [c + d x]^2) \sin [c + d x] \right) \right) / \\
 & \left( 32 d (1 + \cos [c + d x]) \sqrt{2 - 2 \cos [c + d x]^2} \sqrt{1 - \cos [c + d x]^2} \right. \\
 & \quad \left. (A + 2 C + A \cos [2 c + 2 d x]) (a (1 + \sec [c + d x]))^{5/2} \right) + \\
 & \frac{1}{(A + 2 C + A \cos [2 c + 2 d x]) \sec [c + d x]^{3/2} (a (1 + \sec [c + d x]))^{5/2}} \\
 & \sqrt{(1 + \cos [c + d x]) \sec [c + d x]} \\
 & (1 + \sec [c + d x])^{5/2} \\
 & (A + C \sec [c + d x]^2) \\
 & \left( \frac{\sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \left( -41 A \sin \left[ \frac{c}{2} \right] - 25 C \sin \left[ \frac{c}{2} \right] \right)}{16 d} + \right. \\
 & \quad \frac{\sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \left( A \sin \left[ \frac{c}{2} \right] + C \sin \left[ \frac{c}{2} \right] \right)}{8 d} + \frac{(331 A + 60 C) \cos [d x] \sin [c]}{15 d} - \\
 & \quad \frac{28 A \cos [2 d x] \sin [2 c]}{15 d} + \frac{A \cos [3 d x] \sin [3 c]}{5 d} + \\
 & \quad \frac{\sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right] \left( -2069 A \sin \left[ \frac{d x}{2} \right] - 165 C \sin \left[ \frac{d x}{2} \right] \right)}{120 d} + \\
 & \quad \frac{\sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^3 \left( -41 A \sin \left[ \frac{d x}{2} \right] - 25 C \sin \left[ \frac{d x}{2} \right] \right)}{16 d} + \\
 & \quad \left. \frac{\sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^5 \left( A \sin \left[ \frac{d x}{2} \right] + C \sin \left[ \frac{d x}{2} \right] \right)}{8 d} + \frac{(331 A + 60 C) \cos [c] \sin [d x]}{15 d} - \right. \\
 & \quad \left. \frac{28 A \cos [2 c] \sin [2 d x]}{15 d} + \frac{A \cos [3 c] \sin [3 d x]}{5 d} - \frac{(2069 A + 165 C) \tan \left[ \frac{c}{2} \right]}{120 d} \right)
 \end{aligned}$$

**Problem 295: Unable to integrate problem.**

$$\int (a + a \sec [c + d x])^{2/3} (A + C \sec [c + d x]^2) dx$$

Optimal (type 6, 434 leaves, 10 steps):

$$\frac{3 C (a + a \operatorname{Sec}[c + d x])^{2/3} \operatorname{Tan}[c + d x]}{5 d} + \left( 3 \sqrt{2} \operatorname{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \frac{1}{2} (1 + \operatorname{Sec}[c + d x]), 1 + \operatorname{Sec}[c + d x]\right] (a + a \operatorname{Sec}[c + d x])^{2/3} \operatorname{Tan}[c + d x] \right) / \left( 7 d \sqrt{1 - \operatorname{Sec}[c + d x]} \right) + \frac{3 C (a + a \operatorname{Sec}[c + d x])^{2/3} \operatorname{Tan}[c + d x]}{5 d (1 + \operatorname{Sec}[c + d x])} - \left( 3^{3/4} C \operatorname{EllipticF}\left[\operatorname{ArcCos}\left[\frac{2^{1/3} - (1 - \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}\right], \frac{1}{4} (2 + \sqrt{3})\right] (a + a \operatorname{Sec}[c + d x])^{2/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3}) \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \operatorname{Sec}[c + d x])^{1/3} + (1 + \operatorname{Sec}[c + d x])^{2/3}}{(2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3})^2}} \operatorname{Tan}[c + d x] \right) / \left( 5 \times 2^{1/3} d (1 - \operatorname{Sec}[c + d x]) (1 + \operatorname{Sec}[c + d x]) \sqrt{-\frac{(1 + \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3})}{(2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3})^2}} \right)$$

Result (type 8, 29 leaves):

$$\int (a + a \operatorname{Sec}[c + d x])^{2/3} (A + C \operatorname{Sec}[c + d x]^2) dx$$

**Problem 296: Unable to integrate problem.**

$$\int \frac{A + C \operatorname{Sec}[c + d x]^2}{(a + a \operatorname{Sec}[c + d x])^{1/3}} dx$$

Optimal (type 6, 384 leaves, 9 steps):

$$\begin{aligned}
 & \frac{3 C \operatorname{Tan}[c+d x]}{2 d (a+a \operatorname{Sec}[c+d x])^{1/3}} + \\
 & \left( 3 \sqrt{2} \operatorname{AppellF1}\left[\frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \frac{1}{2} (1+\operatorname{Sec}[c+d x]), 1+\operatorname{Sec}[c+d x]\right] \operatorname{Tan}[c+d x] \right) / \\
 & \left( d \sqrt{1-\operatorname{Sec}[c+d x]} (a+a \operatorname{Sec}[c+d x])^{1/3} \right) + \\
 & \left( 3^{3/4} C \operatorname{EllipticF}\left[\operatorname{ArcCos}\left[\frac{2^{1/3}-(1-\sqrt{3})(1+\operatorname{Sec}[c+d x])^{1/3}}{2^{1/3}-(1+\sqrt{3})(1+\operatorname{Sec}[c+d x])^{1/3}}\right], \frac{1}{4} (2+\sqrt{3})\right] \right. \\
 & \left. \left( 2^{1/3}-(1+\operatorname{Sec}[c+d x])^{1/3} \right) \sqrt{\frac{2^{2/3}+2^{1/3}(1+\operatorname{Sec}[c+d x])^{1/3}+(1+\operatorname{Sec}[c+d x])^{2/3}}{(2^{1/3}-(1+\sqrt{3})(1+\operatorname{Sec}[c+d x])^{1/3})^2}} \right. \\
 & \left. \operatorname{Tan}[c+d x] \right) / \left( 2 \times 2^{1/3} d (1-\operatorname{Sec}[c+d x]) (a+a \operatorname{Sec}[c+d x])^{1/3} \right. \\
 & \left. \sqrt{-\frac{(1+\operatorname{Sec}[c+d x])^{1/3} (2^{1/3}-(1+\operatorname{Sec}[c+d x])^{1/3})}{(2^{1/3}-(1+\sqrt{3})(1+\operatorname{Sec}[c+d x])^{1/3})^2}} \right)
 \end{aligned}$$

Result (type 8, 29 leaves):

$$\int \frac{A+C \operatorname{Sec}[c+d x]^2}{(a+a \operatorname{Sec}[c+d x])^{1/3}} dx$$

**Problem 297: Unable to integrate problem.**

$$\int \frac{A+C \operatorname{Sec}[c+d x]^2}{(a+a \operatorname{Sec}[c+d x])^{4/3}} dx$$

Optimal (type 6, 396 leaves, 9 steps):

$$\begin{aligned}
 & - \frac{3 (A + C) \operatorname{Tan}[c + d x]}{5 d (a + a \operatorname{Sec}[c + d x])^{4/3}} + \\
 & \left( 3 \sqrt{2} \operatorname{AppellF1}\left[\frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \frac{1}{2} (1 + \operatorname{Sec}[c + d x]), 1 + \operatorname{Sec}[c + d x]\right] \operatorname{Tan}[c + d x] \right) / \\
 & \left( a d \sqrt{1 - \operatorname{Sec}[c + d x]} (a + a \operatorname{Sec}[c + d x])^{1/3} \right) + \\
 & \left( 3^{3/4} (A - 4 C) \operatorname{EllipticF}\left[\operatorname{ArcCos}\left[\frac{2^{1/3} - (1 - \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}\right], \frac{1}{4} (2 + \sqrt{3})\right] \right. \\
 & \left. \left( 2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3} \right) \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \operatorname{Sec}[c + d x])^{1/3} + (1 + \operatorname{Sec}[c + d x])^{2/3}}{(2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3})^2}} \right. \\
 & \left. \operatorname{Tan}[c + d x] \right) / \left( 5 \times 2^{1/3} a d (1 - \operatorname{Sec}[c + d x]) (a + a \operatorname{Sec}[c + d x])^{1/3} \right. \\
 & \left. \sqrt{-\frac{(1 + \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3})}{(2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3})^2}} \right)
 \end{aligned}$$

Result(type 8, 29 leaves):

$$\int \frac{A + C \operatorname{Sec}[c + d x]^2}{(a + a \operatorname{Sec}[c + d x])^{4/3}} dx$$

Problem 298: Unable to integrate problem.

$$\int \frac{A + C \operatorname{Sec}[c + d x]^2}{(a + a \operatorname{Sec}[c + d x])^{7/3}} dx$$

Optimal (type 6, 457 leaves, 10 steps):

$$\begin{aligned}
 & - \frac{3 (A + C) \operatorname{Tan}[c + d x]}{11 d (a + a \operatorname{Sec}[c + d x])^{7/3}} - \frac{3 (4 A - 7 C) \operatorname{Tan}[c + d x]}{55 a^2 d (1 + \operatorname{Sec}[c + d x]) (a + a \operatorname{Sec}[c + d x])^{1/3}} - \\
 & \left( 3 \sqrt{2} A \operatorname{AppellF1}\left[-\frac{5}{6}, \frac{1}{2}, 1, \frac{1}{6}, \frac{1}{2} (1 + \operatorname{Sec}[c + d x]), 1 + \operatorname{Sec}[c + d x]\right] \operatorname{Tan}[c + d x] \right) / \\
 & \left( 5 a^2 d \sqrt{1 - \operatorname{Sec}[c + d x]} (1 + \operatorname{Sec}[c + d x]) (a + a \operatorname{Sec}[c + d x])^{1/3} \right) + \\
 & \left( 3^{3/4} (4 A - 7 C) \operatorname{EllipticF}\left[\operatorname{ArcCos}\left[\frac{2^{1/3} - (1 - \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}\right], \frac{1}{4} (2 + \sqrt{3})\right] \right. \\
 & \left. \left( 2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3} \right) \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \operatorname{Sec}[c + d x])^{1/3} + (1 + \operatorname{Sec}[c + d x])^{2/3}}{(2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3})^2}} \right. \\
 & \left. \operatorname{Tan}[c + d x] \right) / \left( 55 \times 2^{1/3} a^2 d (1 - \operatorname{Sec}[c + d x]) (a + a \operatorname{Sec}[c + d x])^{1/3} \right. \\
 & \left. \sqrt{-\frac{(1 + \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3})}{(2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3})^2}} \right)
 \end{aligned}$$

Result(type 8, 29 leaves):

$$\int \frac{A + C \operatorname{Sec}[c + d x]^2}{(a + a \operatorname{Sec}[c + d x])^{7/3}} dx$$

**Problem 299: Unable to integrate problem.**

$$\int (a + a \operatorname{Sec}[c + d x])^{4/3} (A + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 6, 815 leaves, 12 steps):

$$\begin{aligned}
 & \frac{3 a C (a + a \operatorname{Sec}[c + d x])^{1/3} \operatorname{Tan}[c + d x]}{7 d} + \\
 & \left( 3 \sqrt{2} a \operatorname{AppellF1}\left[\frac{11}{6}, \frac{1}{2}, 1, \frac{17}{6}, \frac{1}{2} (1 + \operatorname{Sec}[c + d x]), 1 + \operatorname{Sec}[c + d x]\right] \right. \\
 & \quad \left. (1 + \operatorname{Sec}[c + d x]) (a + a \operatorname{Sec}[c + d x])^{1/3} \operatorname{Tan}[c + d x] \right) / \\
 & \left( 11 d \sqrt{1 - \operatorname{Sec}[c + d x]} \right) + \frac{3 C (a + a \operatorname{Sec}[c + d x])^{4/3} \operatorname{Tan}[c + d x]}{7 d} - \\
 & \frac{15 (1 + \sqrt{3}) a C (a + a \operatorname{Sec}[c + d x])^{1/3} \operatorname{Tan}[c + d x]}{7 d (1 + \operatorname{Sec}[c + d x])^{2/3} (2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3})} + \\
 & \left( 15 \times 2^{1/3} \times 3^{1/4} a C \operatorname{EllipticE}\left[\operatorname{ArcCos}\left[\frac{2^{1/3} - (1 - \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}\right], \frac{1}{4} (2 + \sqrt{3})\right] \right) \\
 & \quad (a + a \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3}) \\
 & \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \operatorname{Sec}[c + d x])^{1/3} + (1 + \operatorname{Sec}[c + d x])^{2/3}}{(2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3})^2} \operatorname{Tan}[c + d x]} \Bigg/ \left( 7 d (1 - \operatorname{Sec}[c + d x]) \right) \\
 & (1 + \operatorname{Sec}[c + d x])^{2/3} \sqrt{-\frac{(1 + \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3})}{(2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3})^2}} + \\
 & \left( 5 \times 3^{3/4} (1 - \sqrt{3}) a C \operatorname{EllipticF}\left[\operatorname{ArcCos}\left[\frac{2^{1/3} - (1 - \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}\right], \frac{1}{4} (2 + \sqrt{3})\right] \right) \\
 & \quad (a + a \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3}) \\
 & \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \operatorname{Sec}[c + d x])^{1/3} + (1 + \operatorname{Sec}[c + d x])^{2/3}}{(2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3})^2} \operatorname{Tan}[c + d x]} \Bigg/ \left( 7 \times 2^{2/3} d \right) \\
 & (1 - \operatorname{Sec}[c + d x]) (1 + \operatorname{Sec}[c + d x])^{2/3} \sqrt{-\frac{(1 + \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3})}{(2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3})^2}}
 \end{aligned}$$

Result (type 8, 29 leaves):

$$\int (a + a \operatorname{Sec}[c + d x])^{4/3} (A + C \operatorname{Sec}[c + d x]^2) dx$$

Problem 300: Unable to integrate problem.

$$\int (a + a \operatorname{Sec}[c + d x])^{1/3} (A + C \operatorname{Sec}[c + d x]^2) dx$$



Optimal (type 6, 774 leaves, 11 steps):

$$\begin{aligned}
 & \frac{3 C (a + a \operatorname{Sec}[c + d x])^{1/3} \operatorname{Tan}[c + d x]}{4 d} + \\
 & \left( 3 \sqrt{2} \operatorname{AppellF1}\left[\frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \frac{1}{2} (1 + \operatorname{Sec}[c + d x]), 1 + \operatorname{Sec}[c + d x]\right] \right. \\
 & \quad \left. (a + a \operatorname{Sec}[c + d x])^{1/3} \operatorname{Tan}[c + d x] \right) / \left( 5 d \sqrt{1 - \operatorname{Sec}[c + d x]} \right) - \\
 & \frac{3 (1 + \sqrt{3}) C (a + a \operatorname{Sec}[c + d x])^{1/3} \operatorname{Tan}[c + d x]}{4 d (1 + \operatorname{Sec}[c + d x])^{2/3} (2^{1/3} - (1 + \sqrt{3})) (1 + \operatorname{Sec}[c + d x])^{1/3}} + \\
 & \left( 3 \times 3^{1/4} C \operatorname{EllipticE}\left[\operatorname{ArcCos}\left[\frac{2^{1/3} - (1 - \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}\right], \frac{1}{4} (2 + \sqrt{3})\right] \right) \\
 & \quad (a + a \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3}) \\
 & \quad \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \operatorname{Sec}[c + d x])^{1/3} + (1 + \operatorname{Sec}[c + d x])^{2/3}}{(2^{1/3} - (1 + \sqrt{3})) (1 + \operatorname{Sec}[c + d x])^{1/3}} \operatorname{Tan}[c + d x]} \Bigg/ \left( 2 \times 2^{2/3} d \right. \\
 & \quad \left. (1 - \operatorname{Sec}[c + d x]) (1 + \operatorname{Sec}[c + d x])^{2/3} \sqrt{-\frac{(1 + \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3})}{(2^{1/3} - (1 + \sqrt{3})) (1 + \operatorname{Sec}[c + d x])^{1/3}}}} \right) + \\
 & \left( 3^{3/4} (1 - \sqrt{3}) C \operatorname{EllipticF}\left[\operatorname{ArcCos}\left[\frac{2^{1/3} - (1 - \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}\right], \frac{1}{4} (2 + \sqrt{3})\right] \right) \\
 & \quad (a + a \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3}) \\
 & \quad \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \operatorname{Sec}[c + d x])^{1/3} + (1 + \operatorname{Sec}[c + d x])^{2/3}}{(2^{1/3} - (1 + \sqrt{3})) (1 + \operatorname{Sec}[c + d x])^{1/3}} \operatorname{Tan}[c + d x]} \Bigg/ \left( 4 \times 2^{2/3} d \right. \\
 & \quad \left. (1 - \operatorname{Sec}[c + d x]) (1 + \operatorname{Sec}[c + d x])^{2/3} \sqrt{-\frac{(1 + \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3})}{(2^{1/3} - (1 + \sqrt{3})) (1 + \operatorname{Sec}[c + d x])^{1/3}}}} \right)
 \end{aligned}$$

Result (type 8, 29 leaves):

$$\int (a + a \operatorname{Sec}[c + d x])^{1/3} (A + C \operatorname{Sec}[c + d x]^2) dx$$

**Problem 301: Unable to integrate problem.**

$$\int \frac{A + C \operatorname{Sec}[c + d x]^2}{(a + a \operatorname{Sec}[c + d x])^{2/3}} dx$$

Optimal (type 6, 791 leaves, 11 steps):

$$\begin{aligned}
& - \frac{3 (A + C) \operatorname{Tan}[c + d x]}{d (a + a \operatorname{Sec}[c + d x])^{2/3}} + \\
& \left( 3 \sqrt{2} \operatorname{AppellF1}\left[\frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \frac{1}{2} (1 + \operatorname{Sec}[c + d x]), 1 + \operatorname{Sec}[c + d x]\right] (a + a \operatorname{Sec}[c + d x])^{1/3} \right. \\
& \quad \left. \operatorname{Tan}[c + d x] \right) / \left( 5 a d \sqrt{1 - \operatorname{Sec}[c + d x]} \right) - \\
& \frac{3 (1 + \sqrt{3}) (A + 2 C) (a + a \operatorname{Sec}[c + d x])^{1/3} \operatorname{Tan}[c + d x]}{a d (1 + \operatorname{Sec}[c + d x])^{2/3} (2^{1/3} - (1 + \sqrt{3})) (1 + \operatorname{Sec}[c + d x])^{1/3}} + \\
& \left( 3 \times 2^{1/3} \times 3^{1/4} (A + 2 C) \operatorname{EllipticE}\left[\operatorname{ArcCos}\left[\frac{2^{1/3} - (1 - \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}\right], \frac{1}{4} (2 + \sqrt{3})\right] \right. \\
& \quad \left. (a + a \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3}) \right. \\
& \quad \left. \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \operatorname{Sec}[c + d x])^{1/3} + (1 + \operatorname{Sec}[c + d x])^{2/3}}{(2^{1/3} - (1 + \sqrt{3})) (1 + \operatorname{Sec}[c + d x])^{1/3}} \operatorname{Tan}[c + d x]} \right) / \left( a d (1 - \operatorname{Sec}[c + d x]) \right) \\
& (1 + \operatorname{Sec}[c + d x])^{2/3} \sqrt{-\frac{(1 + \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3})}{(2^{1/3} - (1 + \sqrt{3})) (1 + \operatorname{Sec}[c + d x])^{1/3}} \operatorname{Tan}[c + d x]} + \\
& \left( 3^{3/4} (1 - \sqrt{3}) (A + 2 C) \operatorname{EllipticF}\left[\operatorname{ArcCos}\left[\frac{2^{1/3} - (1 - \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}\right], \frac{1}{4} (2 + \sqrt{3})\right] \right. \\
& \quad \left. (a + a \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3}) \right. \\
& \quad \left. \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \operatorname{Sec}[c + d x])^{1/3} + (1 + \operatorname{Sec}[c + d x])^{2/3}}{(2^{1/3} - (1 + \sqrt{3})) (1 + \operatorname{Sec}[c + d x])^{1/3}} \operatorname{Tan}[c + d x]} \right) / \left( 2^{2/3} a d \right. \\
& \quad \left. (1 - \operatorname{Sec}[c + d x]) (1 + \operatorname{Sec}[c + d x])^{2/3} \sqrt{-\frac{(1 + \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3})}{(2^{1/3} - (1 + \sqrt{3})) (1 + \operatorname{Sec}[c + d x])^{1/3}} \operatorname{Tan}[c + d x]} \right)
\end{aligned}$$

Result (type 8, 29 leaves):

$$\int \frac{A + C \operatorname{Sec}[c + d x]^2}{(a + a \operatorname{Sec}[c + d x])^{2/3}} dx$$

Problem 302: Unable to integrate problem.

$$\int \frac{A + C \operatorname{Sec}[c + d x]^2}{(a + a \operatorname{Sec}[c + d x])^{5/3}} dx$$

Optimal (type 6, 841 leaves, 12 steps):

$$\begin{aligned}
 & - \frac{3(A+C) \operatorname{Tan}[c+dx]}{7d(a+a \operatorname{Sec}[c+dx])^{5/3}} - \frac{3(2A-5C) \operatorname{Tan}[c+dx]}{7ad(a+a \operatorname{Sec}[c+dx])^{2/3}} - \\
 & \left( 3\sqrt{2} \operatorname{AppellF1}\left[-\frac{1}{6}, \frac{1}{2}, 1, \frac{5}{6}, \frac{1}{2}(1+\operatorname{Sec}[c+dx]), 1+\operatorname{Sec}[c+dx]\right] \operatorname{Tan}[c+dx] \right) / \\
 & \left( ad\sqrt{1-\operatorname{Sec}[c+dx]}(a+a \operatorname{Sec}[c+dx])^{2/3} - \right. \\
 & \left. \frac{3(1+\sqrt{3})(2A-5C)(1+\operatorname{Sec}[c+dx])^{1/3} \operatorname{Tan}[c+dx]}{7ad(a+a \operatorname{Sec}[c+dx])^{2/3}(2^{1/3}-(1+\sqrt{3}))(1+\operatorname{Sec}[c+dx])^{1/3}} \right) + \\
 & \left( 3 \times 2^{1/3} \times 3^{1/4} (2A-5C) \operatorname{EllipticE}\left[\operatorname{ArcCos}\left[\frac{2^{1/3}-(1-\sqrt{3})(1+\operatorname{Sec}[c+dx])^{1/3}}{2^{1/3}-(1+\sqrt{3})(1+\operatorname{Sec}[c+dx])^{1/3}}\right], \frac{1}{4}(2+\sqrt{3})\right] \right) \\
 & (1+\operatorname{Sec}[c+dx])^{1/3}(2^{1/3}-(1+\operatorname{Sec}[c+dx])^{1/3}) \\
 & \sqrt{\frac{2^{2/3}+2^{1/3}(1+\operatorname{Sec}[c+dx])^{1/3}+(1+\operatorname{Sec}[c+dx])^{2/3}}{(2^{1/3}-(1+\sqrt{3}))(1+\operatorname{Sec}[c+dx])^{1/3}} \operatorname{Tan}[c+dx]} \Bigg) / \left( 7ad(1-\operatorname{Sec}[c+dx]) \right) \\
 & (a+a \operatorname{Sec}[c+dx])^{2/3} \sqrt{-\frac{(1+\operatorname{Sec}[c+dx])^{1/3}(2^{1/3}-(1+\operatorname{Sec}[c+dx])^{1/3})}{(2^{1/3}-(1+\sqrt{3}))(1+\operatorname{Sec}[c+dx])^{1/3}} \Bigg) + \\
 & \left( 3^{3/4}(1-\sqrt{3})(2A-5C) \operatorname{EllipticF}\left[\operatorname{ArcCos}\left[\frac{2^{1/3}-(1-\sqrt{3})(1+\operatorname{Sec}[c+dx])^{1/3}}{2^{1/3}-(1+\sqrt{3})(1+\operatorname{Sec}[c+dx])^{1/3}}\right], \frac{1}{4}(2+\sqrt{3})\right] \right) \\
 & (1+\operatorname{Sec}[c+dx])^{1/3}(2^{1/3}-(1+\operatorname{Sec}[c+dx])^{1/3}) \\
 & \sqrt{\frac{2^{2/3}+2^{1/3}(1+\operatorname{Sec}[c+dx])^{1/3}+(1+\operatorname{Sec}[c+dx])^{2/3}}{(2^{1/3}-(1+\sqrt{3}))(1+\operatorname{Sec}[c+dx])^{1/3}} \operatorname{Tan}[c+dx]} \Bigg) / \left( 7 \times 2^{2/3} ad \right) \\
 & (1-\operatorname{Sec}[c+dx])(a+a \operatorname{Sec}[c+dx])^{2/3} \sqrt{-\frac{(1+\operatorname{Sec}[c+dx])^{1/3}(2^{1/3}-(1+\operatorname{Sec}[c+dx])^{1/3})}{(2^{1/3}-(1+\sqrt{3}))(1+\operatorname{Sec}[c+dx])^{1/3}} \Bigg)
 \end{aligned}$$

Result (type 8, 29 leaves):

$$\int \frac{A+C \operatorname{Sec}[c+dx]^2}{(a+a \operatorname{Sec}[c+dx])^{5/3}} dx$$

**Problem 303: Unable to integrate problem.**

$$\int \operatorname{Sec}[c+dx]^m (a+a \operatorname{Sec}[c+dx])^n (A+C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 6, 244 leaves, 8 steps):

$$\frac{C \operatorname{Sec}[c+dx]^{1+m} (a+a \operatorname{Sec}[c+dx])^n \operatorname{Sin}[c+dx]}{d(1+m+n)} + \frac{1}{d(1+m+n)}$$

$$2^{\frac{3}{2}+n} C n \operatorname{AppellF1}\left[\frac{1}{2}, 1-m, -\frac{1}{2}-n, \frac{3}{2}, 1-\operatorname{Sec}[c+dx], \frac{1}{2}(1-\operatorname{Sec}[c+dx])\right]$$

$$(1+\operatorname{Sec}[c+dx])^{-\frac{1}{2}-n} (a+a \operatorname{Sec}[c+dx])^n \operatorname{Tan}[c+dx] + \frac{1}{d(1+m+n)}$$

$$2^{\frac{1}{2}+n} (C(m-n)+A(1+m+n)) \operatorname{AppellF1}\left[\frac{1}{2}, 1-m, \frac{1}{2}-n, \frac{3}{2}, 1-\operatorname{Sec}[c+dx], \frac{1}{2}(1-\operatorname{Sec}[c+dx])\right]$$

$$(1+\operatorname{Sec}[c+dx])^{-\frac{1}{2}-n} (a+a \operatorname{Sec}[c+dx])^n \operatorname{Tan}[c+dx]$$

Result (type 8, 35 leaves):

$$\int \operatorname{Sec}[c+dx]^m (a+a \operatorname{Sec}[c+dx])^n (A+C \operatorname{Sec}[c+dx]^2) dx$$

### Problem 304: Unable to integrate problem.

$$\int \operatorname{Sec}[c+dx]^{-1-n} (a+a \operatorname{Sec}[c+dx])^n (A+C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 6, 253 leaves, 8 steps):

$$\frac{A \operatorname{Sec}[c+dx]^{-n} (a+a \operatorname{Sec}[c+dx])^n \operatorname{Sin}[c+dx]}{d(1+n)}$$

$$\left( (C-A n+C n) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}-n, -n, 1-n, -\frac{2 \operatorname{Sec}[c+dx]}{1-\operatorname{Sec}[c+dx]}\right] \operatorname{Sec}[c+dx]^{1-n} \right. \\ \left. \left( \frac{1+\operatorname{Sec}[c+dx]}{1-\operatorname{Sec}[c+dx]} \right)^{\frac{1}{2}-n} (a+a \operatorname{Sec}[c+dx])^n \operatorname{Sin}[c+dx] \right) / (d n(1+n)(1+\operatorname{Sec}[c+dx])) +$$

$$\frac{1}{d} 2^{\frac{3}{2}+n} C \operatorname{AppellF1}\left[\frac{1}{2}, 1+n, -\frac{1}{2}-n, \frac{3}{2}, 1-\operatorname{Sec}[c+dx], \frac{1}{2}(1-\operatorname{Sec}[c+dx])\right]$$

$$(1+\operatorname{Sec}[c+dx])^{-\frac{1}{2}-n} (a+a \operatorname{Sec}[c+dx])^n \operatorname{Tan}[c+dx]$$

Result (type 8, 39 leaves):

$$\int \operatorname{Sec}[c+dx]^{-1-n} (a+a \operatorname{Sec}[c+dx])^n (A+C \operatorname{Sec}[c+dx]^2) dx$$

### Problem 306: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[c+dx]^2 (a+a \operatorname{Sec}[c+dx]) (B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 3, 106 leaves, 7 steps):

$$\frac{a(4B+3C) \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{8d} + \frac{a(B+C) \operatorname{Tan}[c+dx]}{d} +$$

$$\frac{a(4B+3C) \operatorname{Sec}[c+dx] \operatorname{Tan}[c+dx]}{8d} + \frac{aC \operatorname{Sec}[c+dx]^3 \operatorname{Tan}[c+dx]}{4d} + \frac{a(B+C) \operatorname{Tan}[c+dx]^3}{3d}$$

Result (type 3, 337 leaves):

$$\begin{aligned}
 & -\frac{1}{192 d} a \operatorname{Sec}[c+d x]^4 \\
 & \left( 36 B \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]+27 C \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]+ \right. \\
 & \quad 12(4 B+3 C) \operatorname{Cos}[2(c+d x)]\left(\operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]- \right. \\
 & \quad \quad \left. \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]\right)+3(4 B+3 C) \operatorname{Cos}[4(c+d x)] \\
 & \quad \left. \left(\operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]-\operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]\right)- \right. \\
 & \quad 36 B \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]-27 C \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]- \\
 & \quad 24 B \operatorname{Sin}[c+d x]-66 C \operatorname{Sin}[c+d x]-64 B \operatorname{Sin}[2(c+d x)]-64 C \operatorname{Sin}[2(c+d x)]- \\
 & \quad \left. 24 B \operatorname{Sin}[3(c+d x)]-18 C \operatorname{Sin}[3(c+d x)]-16 B \operatorname{Sin}[4(c+d x)]-16 C \operatorname{Sin}[4(c+d x)]\right)
 \end{aligned}$$

**Problem 307: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c+d x](a+a \operatorname{Sec}[c+d x])(B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) dx$$

Optimal (type 3, 86 leaves, 7 steps):

$$\begin{aligned}
 & \frac{a(B+C) \operatorname{ArcTanh}[\operatorname{Sin}[c+d x]]}{2 d} + \frac{a(3 B+2 C) \operatorname{Tan}[c+d x]}{3 d} + \\
 & \frac{a(B+C) \operatorname{Sec}[c+d x] \operatorname{Tan}[c+d x]}{2 d} + \frac{a C \operatorname{Sec}[c+d x]^2 \operatorname{Tan}[c+d x]}{3 d}
 \end{aligned}$$

Result (type 3, 181 leaves):

$$\begin{aligned}
 & -\frac{1}{24 d} a \operatorname{Sec}[c+d x]^3\left(9(B+C) \operatorname{Cos}[c+d x]\left(\operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]- \right. \right. \\
 & \quad \left. \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]\right)+3(B+C) \operatorname{Cos}[3(c+d x)] \\
 & \quad \left. \left(\operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]-\operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]\right)- \right. \\
 & \quad \left. 4(3 B+4 C+3(B+C) \operatorname{Cos}[c+d x]+(3 B+2 C) \operatorname{Cos}[2(c+d x)]) \operatorname{Sin}[c+d x]\right)
 \end{aligned}$$

**Problem 308: Result more than twice size of optimal antiderivative.**

$$\int (a+a \operatorname{Sec}[c+d x])(B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) dx$$

Optimal (type 3, 56 leaves, 5 steps):

$$\frac{a(2 B+C) \operatorname{ArcTanh}[\operatorname{Sin}[c+d x]]}{2 d} + \frac{a(B+C) \operatorname{Tan}[c+d x]}{d} + \frac{a C \operatorname{Sec}[c+d x] \operatorname{Tan}[c+d x]}{2 d}$$

Result (type 3, 154 leaves):

$$\frac{1}{4d} a \left( -2(2B+C) \operatorname{Log} \left[ \cos \left[ \frac{1}{2}(c+dx) \right] - \sin \left[ \frac{1}{2}(c+dx) \right] \right] + \right. \\ \left. 4B \operatorname{Log} \left[ \cos \left[ \frac{1}{2}(c+dx) \right] + \sin \left[ \frac{1}{2}(c+dx) \right] \right] + \right. \\ \left. 2C \operatorname{Log} \left[ \cos \left[ \frac{1}{2}(c+dx) \right] + \sin \left[ \frac{1}{2}(c+dx) \right] \right] + \frac{C}{\left( \cos \left[ \frac{1}{2}(c+dx) \right] - \sin \left[ \frac{1}{2}(c+dx) \right] \right)^2} - \right. \\ \left. \frac{C}{\left( \cos \left[ \frac{1}{2}(c+dx) \right] + \sin \left[ \frac{1}{2}(c+dx) \right] \right)^2} + 4(B+C) \operatorname{Tan}[c+dx] \right)$$

**Problem 309: Result more than twice size of optimal antiderivative.**

$$\int \cos[c+dx] (a+a \sec[c+dx]) (B \sec[c+dx]+C \sec[c+dx]^2) dx$$

Optimal (type 3, 32 leaves, 5 steps):

$$aBx + \frac{a(B+C) \operatorname{ArcTanh}[\sin[c+dx]]}{d} + \frac{aC \operatorname{Tan}[c+dx]}{d}$$

Result (type 3, 159 leaves):

$$aBx - \frac{aB \operatorname{Log} \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] - \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right]}{d} - \frac{aC \operatorname{Log} \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] - \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right]}{d} + \\ \frac{aB \operatorname{Log} \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] + \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right]}{d} + \frac{aC \operatorname{Log} \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] + \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right]}{d} + \frac{aC \operatorname{Tan}[c+dx]}{d}$$

**Problem 310: Result more than twice size of optimal antiderivative.**

$$\int \cos[c+dx]^2 (a+a \sec[c+dx]) (B \sec[c+dx]+C \sec[c+dx]^2) dx$$

Optimal (type 3, 32 leaves, 4 steps):

$$a(B+C)x + \frac{aC \operatorname{ArcTanh}[\sin[c+dx]]}{d} + \frac{aB \sin[c+dx]}{d}$$

Result (type 3, 104 leaves):

$$aBx + aCx - \frac{aC \operatorname{Log} \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] - \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right]}{d} + \\ \frac{aC \operatorname{Log} \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] + \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right]}{d} + \frac{aB \cos[dx] \sin[c]}{d} + \frac{aB \cos[c] \sin[dx]}{d}$$

### Problem 314: Result more than twice size of optimal antiderivative.

$$\int \sec [c + d x]^2 (a + a \sec [c + d x])^2 (B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 3, 169 leaves, 8 steps):

$$\frac{a^2 (7 B + 6 C) \operatorname{ArcTanh}[\sin [c + d x]]}{8 d} + \frac{a^2 (10 B + 9 C) \tan [c + d x]}{5 d} +$$

$$\frac{a^2 (7 B + 6 C) \sec [c + d x] \tan [c + d x]}{8 d} + \frac{a^2 (5 B + 6 C) \sec [c + d x]^3 \tan [c + d x]}{20 d} +$$

$$\frac{C \sec [c + d x]^3 (a^2 + a^2 \sec [c + d x]) \tan [c + d x]}{5 d} + \frac{a^2 (10 B + 9 C) \tan [c + d x]^3}{15 d}$$

Result (type 3, 391 leaves):

$$-\frac{1}{1920 d} a^2 \sec [c + d x]^5 \left( 105 B \cos [5 (c + d x)] \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] \right) +$$

$$90 C \cos [5 (c + d x)] \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] +$$

$$150 (7 B + 6 C) \cos [c + d x] \left( \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] - \right.$$

$$\left. \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] \right) + 75 (7 B + 6 C) \cos [3 (c + d x)]$$

$$\left( \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] - \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] \right) -$$

$$105 B \cos [5 (c + d x)] \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] -$$

$$90 C \cos [5 (c + d x)] \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] - 640 B \sin [c + d x] -$$

$$960 C \sin [c + d x] - 660 B \sin [2 (c + d x)] - 840 C \sin [2 (c + d x)] -$$

$$800 B \sin [3 (c + d x)] - 720 C \sin [3 (c + d x)] - 210 B \sin [4 (c + d x)] -$$

$$180 C \sin [4 (c + d x)] - 160 B \sin [5 (c + d x)] - 144 C \sin [5 (c + d x)] \Big)$$

### Problem 315: Result more than twice size of optimal antiderivative.

$$\int \sec [c + d x] (a + a \sec [c + d x])^2 (B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 3, 138 leaves, 8 steps):

$$\frac{a^2 (8 B + 7 C) \operatorname{ArcTanh}[\sin [c + d x]]}{8 d} +$$

$$\frac{a^2 (8 B + 7 C) \tan [c + d x]}{6 d} + \frac{a^2 (8 B + 7 C) \sec [c + d x] \tan [c + d x]}{24 d} +$$

$$\frac{(4 B - C) (a + a \sec [c + d x])^2 \tan [c + d x]}{12 d} + \frac{C (a + a \sec [c + d x])^3 \tan [c + d x]}{4 a d}$$

Result (type 3, 339 leaves):

$$\begin{aligned}
 & -\frac{1}{192 d} a^2 \operatorname{Sec}[c+d x]^4 \\
 & \left( 72 B \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]+63 C \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]+ \right. \\
 & \quad 12(8 B+7 C) \operatorname{Cos}[2(c+d x)]\left(\operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]- \right. \\
 & \quad \quad \left. \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]\right)+3(8 B+7 C) \operatorname{Cos}[4(c+d x)] \\
 & \quad \left. \left(\operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]-\operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]\right)- \right. \\
 & \quad 72 B \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]-63 C \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]- \\
 & \quad 48 B \operatorname{Sin}[c+d x]-90 C \operatorname{Sin}[c+d x]-112 B \operatorname{Sin}[2(c+d x)]-128 C \operatorname{Sin}[2(c+d x)]- \\
 & \quad \left. 48 B \operatorname{Sin}[3(c+d x)]-42 C \operatorname{Sin}[3(c+d x)]-40 B \operatorname{Sin}[4(c+d x)]-32 C \operatorname{Sin}[4(c+d x)]\right)
 \end{aligned}$$

### Problem 317: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cos}[c+d x] (a+a \operatorname{Sec}[c+d x])^2 (B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) dx$$

Optimal (type 3, 82 leaves, 6 steps):

$$\begin{aligned}
 & a^2 B x + \frac{a^2(4 B+3 C) \operatorname{ArcTanh}[\operatorname{Sin}[c+d x]]}{2 d} + \\
 & \frac{a^2(2 B+3 C) \operatorname{Tan}[c+d x]}{2 d} + \frac{C(a^2+a^2 \operatorname{Sec}[c+d x]) \operatorname{Tan}[c+d x]}{2 d}
 \end{aligned}$$

Result (type 3, 277 leaves):

$$\begin{aligned}
 & \frac{1}{16} a^2 (1+\operatorname{Cos}[c+d x])^2 \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^4 \\
 & \left( 4 B x - \frac{2(4 B+3 C) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]}{d} + \right. \\
 & \quad \frac{2(4 B+3 C) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]}{d} + \frac{C}{d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^2} + \\
 & \quad \frac{4(B+2 C) \operatorname{Sin}\left[\frac{d x}{2}\right]}{d\left(\operatorname{Cos}\left[\frac{c}{2}\right]-\operatorname{Sin}\left[\frac{c}{2}\right]\right)\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)} - \\
 & \quad \frac{C}{d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^2} + \\
 & \quad \left. \frac{4(B+2 C) \operatorname{Sin}\left[\frac{d x}{2}\right]}{d\left(\operatorname{Cos}\left[\frac{c}{2}\right]+\operatorname{Sin}\left[\frac{c}{2}\right]\right)\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)} \right)
 \end{aligned}$$



### Problem 323: Result more than twice size of optimal antiderivative.

$$\int \sec [c + d x] (a + a \sec [c + d x])^3 (B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 3, 163 leaves, 12 steps):

$$\frac{a^3 (15 B + 13 C) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{8 d} + \frac{a^3 (15 B + 13 C) \operatorname{Tan}[c + d x]}{5 d} +$$

$$\frac{3 a^3 (15 B + 13 C) \sec [c + d x] \operatorname{Tan}[c + d x]}{40 d} + \frac{(5 B - C) (a + a \sec [c + d x])^3 \operatorname{Tan}[c + d x]}{20 d} +$$

$$\frac{C (a + a \sec [c + d x])^4 \operatorname{Tan}[c + d x]}{5 a d} + \frac{a^3 (15 B + 13 C) \operatorname{Tan}[c + d x]^3}{60 d}$$

Result (type 3, 391 leaves):

$$-\frac{1}{1920 d} a^3 \sec [c + d x]^5 \left( 225 B \operatorname{Cos}[5 (c + d x)] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2} (c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]\right] + \right.$$

$$195 C \operatorname{Cos}[5 (c + d x)] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2} (c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]\right] + 150 (15 B + 13 C) \operatorname{Cos}[c + d x]$$

$$\left. \left( \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2} (c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]\right] - \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2} (c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]\right] \right) + \right.$$

$$75 (15 B + 13 C) \operatorname{Cos}[3 (c + d x)]$$

$$\left. \left( \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2} (c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]\right] - \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2} (c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]\right] \right) - \right.$$

$$225 B \operatorname{Cos}[5 (c + d x)] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2} (c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]\right] -$$

$$195 C \operatorname{Cos}[5 (c + d x)] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2} (c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]\right] - 1200 B \operatorname{Sin}[c + d x] -$$

$$1600 C \operatorname{Sin}[c + d x] - 1140 B \operatorname{Sin}[2 (c + d x)] - 1500 C \operatorname{Sin}[2 (c + d x)] -$$

$$1560 B \operatorname{Sin}[3 (c + d x)] - 1520 C \operatorname{Sin}[3 (c + d x)] - 450 B \operatorname{Sin}[4 (c + d x)] -$$

$$\left. 390 C \operatorname{Sin}[4 (c + d x)] - 360 B \operatorname{Sin}[5 (c + d x)] - 304 C \operatorname{Sin}[5 (c + d x)] \right)$$

### Problem 324: Result more than twice size of optimal antiderivative.

$$\int (a + a \sec [c + d x])^3 (B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 3, 125 leaves, 11 steps):

$$\frac{5 a^3 (4 B + 3 C) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{8 d} +$$

$$\frac{a^3 (4 B + 3 C) \operatorname{Tan}[c + d x]}{d} + \frac{3 a^3 (4 B + 3 C) \sec [c + d x] \operatorname{Tan}[c + d x]}{8 d} +$$

$$\frac{C (a + a \sec [c + d x])^3 \operatorname{Tan}[c + d x]}{4 d} + \frac{a^3 (4 B + 3 C) \operatorname{Tan}[c + d x]^3}{12 d}$$

Result (type 3, 339 leaves):

$$\begin{aligned}
& \frac{1}{192 d} a^3 \operatorname{Sec}[c+d x]^4 \left( -180 B \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] - \right. \\
& \quad 135 C \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] - 60(4 B+3 C) \operatorname{Cos}[2(c+d x)] \\
& \quad \left. \left( \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] - \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] \right) - \right. \\
& \quad 15(4 B+3 C) \operatorname{Cos}[4(c+d x)] \\
& \quad \left. \left( \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] - \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] \right) \right) + \\
& \quad 180 B \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] + \\
& \quad 135 C \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] + 72 B \operatorname{Sin}[c+d x] + 138 C \operatorname{Sin}[c+d x] + \\
& \quad 208 B \operatorname{Sin}[2(c+d x)] + 240 C \operatorname{Sin}[2(c+d x)] + 72 B \operatorname{Sin}[3(c+d x)] + \\
& \quad 90 C \operatorname{Sin}[3(c+d x)] + 88 B \operatorname{Sin}[4(c+d x)] + 72 C \operatorname{Sin}[4(c+d x)] \Big)
\end{aligned}$$

### Problem 325: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cos}[c+d x] (a+a \operatorname{Sec}[c+d x])^3 (B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) dx$$

Optimal (type 3, 111 leaves, 7 steps):

$$\begin{aligned}
& a^3 B x + \frac{a^3 (7 B+5 C) \operatorname{ArcTanh}[\operatorname{Sin}[c+d x]]}{2 d} + \frac{5 a^3 (B+C) \operatorname{Tan}[c+d x]}{2 d} + \\
& \frac{a C (a+a \operatorname{Sec}[c+d x])^2 \operatorname{Tan}[c+d x]}{3 d} + \frac{(3 B+5 C) (a^3+a^3 \operatorname{Sec}[c+d x]) \operatorname{Tan}[c+d x]}{6 d}
\end{aligned}$$

Result (type 3, 772 leaves):

$$\begin{aligned}
 & a^3 \left( \frac{1}{8} B x (1 + \cos [c + d x])^3 \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 + \frac{1}{16 d} \right. \\
 & \quad (-7 B - 5 C) (1 + \cos [c + d x])^3 \operatorname{Log} \left[ \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 + \\
 & \quad \frac{1}{16 d} (7 B + 5 C) (1 + \cos [c + d x])^3 \operatorname{Log} \left[ \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 + \\
 & \quad \frac{C (1 + \cos [c + d x])^3 \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \sin \left[ \frac{d x}{2} \right]}{48 d \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right)^3} + \\
 & \quad \left( (1 + \cos [c + d x])^3 \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \left( 3 B \cos \left[ \frac{c}{2} \right] + 10 C \cos \left[ \frac{c}{2} \right] - 3 B \sin \left[ \frac{c}{2} \right] - 8 C \sin \left[ \frac{c}{2} \right] \right) \right) / \\
 & \quad \left( 96 d \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right)^2 \right) + \\
 & \quad \frac{(1 + \cos [c + d x])^3 \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \left( 9 B \sin \left[ \frac{d x}{2} \right] + 11 C \sin \left[ \frac{d x}{2} \right] \right)}{24 d \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right)} + \\
 & \quad \frac{C (1 + \cos [c + d x])^3 \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \sin \left[ \frac{d x}{2} \right]}{48 d \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right)^3} + \\
 & \quad \left( (1 + \cos [c + d x])^3 \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \left( -3 B \cos \left[ \frac{c}{2} \right] - 10 C \cos \left[ \frac{c}{2} \right] - 3 B \sin \left[ \frac{c}{2} \right] - 8 C \sin \left[ \frac{c}{2} \right] \right) \right) / \\
 & \quad \left( 96 d \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right)^2 \right) + \\
 & \quad \frac{(1 + \cos [c + d x])^3 \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \left( 9 B \sin \left[ \frac{d x}{2} \right] + 11 C \sin \left[ \frac{d x}{2} \right] \right)}{24 d \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right)} \Big)
 \end{aligned}$$

**Problem 327: Result more than twice size of optimal antiderivative.**

$$\int \cos [c + d x]^3 (a + a \operatorname{Sec} [c + d x])^3 (B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) dx$$

Optimal (type 3, 117 leaves, 6 steps):

$$\begin{aligned}
 & \frac{1}{2} a^3 (7 B + 6 C) x + \frac{a^3 (B + 3 C) \operatorname{ArcTanh} [\sin [c + d x]]}{d} + \frac{5 a^3 B \sin [c + d x]}{2 d} + \\
 & \frac{a B \cos [c + d x] (a + a \operatorname{Sec} [c + d x])^2 \sin [c + d x]}{2 d} - \frac{(B - 2 C) (a^3 + a^3 \operatorname{Sec} [c + d x]) \sin [c + d x]}{2 d}
 \end{aligned}$$

Result (type 3, 272 leaves):

$$\frac{1}{32} a^3 (1 + \cos [c + d x])^3 \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^6$$

$$\left( 2(7B + 6C)x - \frac{4(B + 3C) \operatorname{Log}\left[\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right]\right]}{d} + \right.$$

$$\frac{4(B + 3C) \operatorname{Log}\left[\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right]}{d} + \frac{4(3B + C) \cos [d x] \sin [c]}{d} +$$

$$\frac{B \cos [2 d x] \sin [2 c]}{d} + \frac{4(3B + C) \cos [c] \sin [d x]}{d} + \frac{B \cos [2 c] \sin [2 d x]}{d} +$$

$$\frac{4C \sin\left[\frac{d x}{2}\right]}{d \left(\cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right]\right) \left(\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right]\right)} +$$

$$\left. \frac{4C \sin\left[\frac{d x}{2}\right]}{d \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right]\right) \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right)} \right)$$

**Problem 332: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c + d x]^3 (B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{a + a \operatorname{Sec}[c + d x]} dx$$

Optimal (type 3, 131 leaves, 7 steps):

$$\frac{3(B - C) \operatorname{ArcTanh}[\sin [c + d x]]}{2 a d} - \frac{(3 B - 4 C) \tan [c + d x]}{a d} +$$

$$\frac{3(B - C) \operatorname{Sec}[c + d x] \tan [c + d x]}{2 a d} + \frac{(B - C) \operatorname{Sec}[c + d x]^3 \tan [c + d x]}{d(a + a \operatorname{Sec}[c + d x])} - \frac{(3 B - 4 C) \tan [c + d x]^3}{3 a d}$$

Result (type 3, 550 leaves):

$$\begin{aligned}
 & \frac{1}{24 a d (1 + \cos [c + d x])} \\
 & \cos \left[ \frac{1}{2} (c + d x) \right] \sec [c + d x]^3 \left( 9 B \cos \left[ \frac{5}{2} (c + d x) \right] \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] - \right. \\
 & \quad 9 C \cos \left[ \frac{5}{2} (c + d x) \right] \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] + \\
 & \quad 9 B \cos \left[ \frac{7}{2} (c + d x) \right] \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] - \\
 & \quad 9 C \cos \left[ \frac{7}{2} (c + d x) \right] \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] + \\
 & \quad 27 (B - C) \cos \left[ \frac{1}{2} (c + d x) \right] \left( \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] - \right. \\
 & \quad \quad \left. \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] \right) + 27 (B - C) \cos \left[ \frac{3}{2} (c + d x) \right] \\
 & \quad \left( \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] - \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] \right) - \\
 & \quad 9 B \cos \left[ \frac{5}{2} (c + d x) \right] \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] + \\
 & \quad 9 C \cos \left[ \frac{5}{2} (c + d x) \right] \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] - \\
 & \quad 9 B \cos \left[ \frac{7}{2} (c + d x) \right] \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] + \\
 & \quad 9 C \cos \left[ \frac{7}{2} (c + d x) \right] \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] - 12 B \sin \left[ \frac{1}{2} (c + d x) \right] + \\
 & \quad 18 B \sin \left[ \frac{3}{2} (c + d x) \right] - 30 C \sin \left[ \frac{3}{2} (c + d x) \right] - 6 B \sin \left[ \frac{5}{2} (c + d x) \right] + \\
 & \quad 2 C \sin \left[ \frac{5}{2} (c + d x) \right] + 12 B \sin \left[ \frac{7}{2} (c + d x) \right] - 16 C \sin \left[ \frac{7}{2} (c + d x) \right] \left. \right)
 \end{aligned}$$

**Problem 333: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c + d x]^2 (B \sec [c + d x] + C \sec [c + d x]^2)}{a + a \sec [c + d x]} dx$$

Optimal (type 3, 108 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{(2 B - 3 C) \operatorname{ArcTanh}[\sin [c + d x]]}{2 a d} + \frac{2 (B - C) \tan [c + d x]}{a d} - \\
 & \frac{(2 B - 3 C) \sec [c + d x] \tan [c + d x]}{2 a d} + \frac{(B - C) \sec [c + d x]^2 \tan [c + d x]}{d (a + a \sec [c + d x])}
 \end{aligned}$$

Result (type 3, 383 leaves):

$$\frac{1}{4 a d (1 + \cos [c + d x])} \cos \left[ \frac{1}{2} (c + d x) \right] \sec [c + d x]^2 \left( 2 B \cos \left[ \frac{5}{2} (c + d x) \right] \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] - \right. \\ \left. 3 C \cos \left[ \frac{5}{2} (c + d x) \right] \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] + \right. \\ \left. 2 (2 B - 3 C) \cos \left[ \frac{1}{2} (c + d x) \right] \left( \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] - \right. \right. \\ \left. \left. \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] \right) + (2 B - 3 C) \cos \left[ \frac{3}{2} (c + d x) \right] \right. \\ \left. \left( \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] - \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] \right) - \right. \\ \left. 2 B \cos \left[ \frac{5}{2} (c + d x) \right] \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] + \right. \\ \left. 3 C \cos \left[ \frac{5}{2} (c + d x) \right] \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] + 4 B \sin \left[ \frac{1}{2} (c + d x) \right] - \right. \\ \left. 2 C \sin \left[ \frac{1}{2} (c + d x) \right] + 2 C \sin \left[ \frac{3}{2} (c + d x) \right] + 4 B \sin \left[ \frac{5}{2} (c + d x) \right] - 4 C \sin \left[ \frac{5}{2} (c + d x) \right] \right)$$

**Problem 334: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c + d x] (B \sec [c + d x] + C \sec [c + d x]^2)}{a + a \sec [c + d x]} dx$$

Optimal (type 3, 62 leaves, 6 steps):

$$\frac{(B - C) \operatorname{ArcTanh}[\sin [c + d x]]}{a d} + \frac{C \tan [c + d x]}{a d} - \frac{(B - C) \tan [c + d x]}{d (a + a \sec [c + d x])}$$

Result (type 3, 234 leaves):

$$- \left( \left( \cos \left[ \frac{1}{2} (c + d x) \right] \left( (B - C) \cos \left[ \frac{1}{2} (c + d x) \right] \left( \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] - \right. \right. \right. \right. \\ \left. \left. \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] \right) + (B - C) \cos \left[ \frac{3}{2} (c + d x) \right] \right. \right. \\ \left. \left. \left( \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] - \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] \right) - \right. \right. \\ \left. \left. 2 (C - (B - 2 C) \cos [c + d x]) \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) / \\ \left( a d (1 + \cos [c + d x]) \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right. \\ \left. \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right)$$

**Problem 335: Result more than twice size of optimal antiderivative.**

$$\int \frac{B \sec [c + d x] + C \sec [c + d x]^2}{a + a \sec [c + d x]} dx$$

Optimal (type 3, 44 leaves, 4 steps):

$$\frac{C \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{a d} + \frac{(B - C) \operatorname{Tan}[c + d x]}{a d (1 + \operatorname{Sec}[c + d x])}$$

Result (type 3, 106 leaves):

$$\left( 2 \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] \left( C \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] \right. \right. \\ \left. \left. \left( -\operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right) \right) + \right. \\ \left. (B - C) \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) / (a d (1 + \operatorname{Cos}[c + d x]))$$

**Problem 336: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Cos}[c + d x] (B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{a + a \operatorname{Sec}[c + d x]} dx$$

Optimal (type 3, 35 leaves, 3 steps):

$$\frac{B x}{a} - \frac{(B - C) \operatorname{Tan}[c + d x]}{d (a + a \operatorname{Sec}[c + d x])}$$

Result (type 3, 72 leaves):

$$\left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] \operatorname{Sec}\left[\frac{c}{2}\right] \left( B d x \operatorname{Cos}\left[\frac{d x}{2}\right] + B d x \operatorname{Cos}\left[c + \frac{d x}{2}\right] + 2(-B + C) \operatorname{Sin}\left[\frac{d x}{2}\right] \right) \right) / (a d (1 + \operatorname{Cos}[c + d x]))$$

**Problem 338: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Cos}[c + d x]^3 (B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{a + a \operatorname{Sec}[c + d x]} dx$$

Optimal (type 3, 98 leaves, 6 steps):

$$\frac{(3B - 2C)x}{2a} - \frac{2(B - C) \operatorname{Sin}[c + d x]}{a d} + \\ \frac{(3B - 2C) \operatorname{Cos}[c + d x] \operatorname{Sin}[c + d x]}{2 a d} - \frac{(B - C) \operatorname{Cos}[c + d x] \operatorname{Sin}[c + d x]}{d (a + a \operatorname{Sec}[c + d x])}$$

Result (type 3, 197 leaves):

$$\left( \cos\left[\frac{1}{2}(c+dx)\right] \sec\left[\frac{c}{2}\right] \left( 4(3B-2C)dx \cos\left[\frac{dx}{2}\right] + 4(3B-2C)dx \cos\left[c+\frac{dx}{2}\right] - 20B \sin\left[\frac{dx}{2}\right] + 20C \sin\left[\frac{dx}{2}\right] - 4B \sin\left[c+\frac{dx}{2}\right] + 4C \sin\left[c+\frac{dx}{2}\right] - 3B \sin\left[c+\frac{3dx}{2}\right] + 4C \sin\left[c+\frac{3dx}{2}\right] - 3B \sin\left[2c+\frac{3dx}{2}\right] + 4C \sin\left[2c+\frac{3dx}{2}\right] + B \sin\left[2c+\frac{5dx}{2}\right] + B \sin\left[3c+\frac{5dx}{2}\right] \right) \right) / (8ad(1+\cos[c+dx]))$$

**Problem 339: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c+dx]^4 (B \sec[c+dx] + C \sec[c+dx]^2)}{a + a \sec[c+dx]} dx$$

Optimal (type 3, 122 leaves, 7 steps):

$$-\frac{3(B-C)x}{2a} + \frac{(4B-3C)\sin[c+dx]}{ad} - \frac{3(B-C)\cos[c+dx]\sin[c+dx]}{2ad} - \frac{(B-C)\cos[c+dx]^2\sin[c+dx]}{d(a+a\sec[c+dx])} - \frac{(4B-3C)\sin[c+dx]^3}{3ad}$$

Result (type 3, 249 leaves):

$$\frac{1}{24ad(1+\cos[c+dx])} \cos\left[\frac{1}{2}(c+dx)\right] \sec\left[\frac{c}{2}\right] \left( -36(B-C)dx \cos\left[\frac{dx}{2}\right] - 36(B-C)dx \cos\left[c+\frac{dx}{2}\right] + 69B \sin\left[\frac{dx}{2}\right] - 60C \sin\left[\frac{dx}{2}\right] + 21B \sin\left[c+\frac{dx}{2}\right] - 12C \sin\left[c+\frac{dx}{2}\right] + 18B \sin\left[c+\frac{3dx}{2}\right] - 9C \sin\left[c+\frac{3dx}{2}\right] + 18B \sin\left[2c+\frac{3dx}{2}\right] - 9C \sin\left[2c+\frac{3dx}{2}\right] - 2B \sin\left[2c+\frac{5dx}{2}\right] + 3C \sin\left[2c+\frac{5dx}{2}\right] - 2B \sin\left[3c+\frac{5dx}{2}\right] + 3C \sin\left[3c+\frac{5dx}{2}\right] + B \sin\left[3c+\frac{7dx}{2}\right] + B \sin\left[4c+\frac{7dx}{2}\right] \right)$$

**Problem 340: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec[c+dx]^3 (B \sec[c+dx] + C \sec[c+dx]^2)}{(a + a \sec[c+dx])^2} dx$$

Optimal (type 3, 156 leaves, 8 steps):

$$-\frac{(4B-7C)\operatorname{ArcTanh}[\sin[c+dx]]}{2a^2d} + \frac{2(5B-8C)\tan[c+dx]}{3a^2d} - \frac{(4B-7C)\sec[c+dx]\tan[c+dx]}{2a^2d} + \frac{(5B-8C)\sec[c+dx]^2\tan[c+dx]}{3a^2d(1+\sec[c+dx])} + \frac{(B-C)\sec[c+dx]^3\tan[c+dx]}{3d(a+a\sec[c+dx])^2}$$

Result (type 3, 379 leaves):



$$\begin{aligned} & \frac{1}{6 a^2 d} \cos \left[ \frac{1}{2} (c+d x) \right]^4 \sec [c+d x]^2 \left( 3 (4 B-7 C) \right. \\ & \quad \left. \left( \log \left[ \cos \left[ \frac{1}{2} (c+d x) \right] - \sin \left[ \frac{1}{2} (c+d x) \right] \right] - \log \left[ \cos \left[ \frac{1}{2} (c+d x) \right] + \sin \left[ \frac{1}{2} (c+d x) \right] \right] \right) \right) + \\ & 8 (B+5 C) \csc [c+d x]^3 \sin \left[ \frac{1}{2} (c+d x) \right]^4 - 64 (B-C) \csc [c+d x]^5 \sin \left[ \frac{1}{2} (c+d x) \right]^8 - \\ & 128 C \csc [c+d x]^7 \sin \left[ \frac{1}{2} (c+d x) \right]^{12} + (26 B-44 C) \tan \left[ \frac{1}{2} (c+d x) \right] - 6 (4 B-7 C) \\ & \quad \left( \log \left[ \cos \left[ \frac{1}{2} (c+d x) \right] - \sin \left[ \frac{1}{2} (c+d x) \right] \right] - \log \left[ \cos \left[ \frac{1}{2} (c+d x) \right] + \sin \left[ \frac{1}{2} (c+d x) \right] \right] \right) \\ & \tan \left[ \frac{1}{2} (c+d x) \right]^2 - 8 (5 B-8 C) \tan \left[ \frac{1}{2} (c+d x) \right]^3 + 3 (4 B-7 C) \\ & \quad \left( \log \left[ \cos \left[ \frac{1}{2} (c+d x) \right] - \sin \left[ \frac{1}{2} (c+d x) \right] \right] - \log \left[ \cos \left[ \frac{1}{2} (c+d x) \right] + \sin \left[ \frac{1}{2} (c+d x) \right] \right] \right) \\ & \tan \left[ \frac{1}{2} (c+d x) \right]^4 + \left( 14 B-20 C+B \sec \left[ \frac{1}{2} (c+d x) \right]^2 \right) \tan \left[ \frac{1}{2} (c+d x) \right]^5 \end{aligned}$$

### Problem 341: Result more than twice size of optimal antiderivative.

$$\int \frac{\sec [c+d x]^2 (B \sec [c+d x]+C \sec [c+d x]^2)}{(a+a \sec [c+d x])^2} dx$$

Optimal (type 3, 108 leaves, 7 steps):

$$\begin{aligned} & \frac{(B-2 C) \operatorname{ArcTanh}[\sin [c+d x]]}{a^2 d} - \frac{(B-4 C) \tan [c+d x]}{3 a^2 d} - \\ & \frac{(B-2 C) \tan [c+d x]}{a^2 d (1+\sec [c+d x])} + \frac{(B-C) \sec [c+d x]^2 \tan [c+d x]}{3 d (a+a \sec [c+d x])^2} \end{aligned}$$

Result (type 3, 245 leaves):

$$\begin{aligned} & \frac{1}{3 a^2 d} \cos \left[ \frac{1}{2} (c+d x) \right]^2 \sec [c+d x] \left( -3 (B-2 C) \right. \\ & \quad \left. \left( \log \left[ \cos \left[ \frac{1}{2} (c+d x) \right] - \sin \left[ \frac{1}{2} (c+d x) \right] \right] - \log \left[ \cos \left[ \frac{1}{2} (c+d x) \right] + \sin \left[ \frac{1}{2} (c+d x) \right] \right] \right) \right) - \\ & 4 (B-C) \csc [c+d x]^3 \sin \left[ \frac{1}{2} (c+d x) \right]^4 + 16 (B-C) \csc [c+d x]^5 \sin \left[ \frac{1}{2} (c+d x) \right]^8 + \\ & (-4 B+13 C) \tan \left[ \frac{1}{2} (c+d x) \right] + 3 (B-2 C) \\ & \quad \left( \log \left[ \cos \left[ \frac{1}{2} (c+d x) \right] - \sin \left[ \frac{1}{2} (c+d x) \right] \right] - \log \left[ \cos \left[ \frac{1}{2} (c+d x) \right] + \sin \left[ \frac{1}{2} (c+d x) \right] \right] \right) \\ & \tan \left[ \frac{1}{2} (c+d x) \right]^2 + (4 B-7 C) \tan \left[ \frac{1}{2} (c+d x) \right]^3 \end{aligned}$$

### Problem 344: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x] \left( B \sec [c+d x]+C \sec [c+d x]^2 \right)}{\left( a+a \sec [c+d x] \right)^2} d x$$

Optimal (type 3, 70 leaves, 4 steps):

$$\frac{B x}{a^2} - \frac{(4 B-C) \tan [c+d x]}{3 a^2 d \left( 1+\sec [c+d x] \right)} - \frac{(B-C) \tan [c+d x]}{3 d \left( a+a \sec [c+d x] \right)^2}$$

Result (type 3, 153 leaves):

$$\begin{aligned} & \frac{1}{24 a^2 d} \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{1}{2} (c+d x) \right]^3 \\ & \left( 9 B d x \cos \left[ \frac{d x}{2} \right] + 9 B d x \cos \left[ c+\frac{d x}{2} \right] + 3 B d x \cos \left[ c+\frac{3 d x}{2} \right] + 3 B d x \cos \left[ 2 c+\frac{3 d x}{2} \right] - \right. \\ & 18 B \sin \left[ \frac{d x}{2} \right] + 6 C \sin \left[ \frac{d x}{2} \right] + 12 B \sin \left[ c+\frac{d x}{2} \right] - \\ & \left. 6 C \sin \left[ c+\frac{d x}{2} \right] - 10 B \sin \left[ c+\frac{3 d x}{2} \right] + 4 C \sin \left[ c+\frac{3 d x}{2} \right] \right) \end{aligned}$$

### Problem 345: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^2 \left( B \sec [c+d x]+C \sec [c+d x]^2 \right)}{\left( a+a \sec [c+d x] \right)^2} d x$$

Optimal (type 3, 98 leaves, 6 steps):

$$-\frac{(2 B-C) x}{a^2} + \frac{2(5 B-2 C) \sin [c+d x]}{3 a^2 d} - \frac{(2 B-C) \sin [c+d x]}{a^2 d \left( 1+\sec [c+d x] \right)} - \frac{(B-C) \sin [c+d x]}{3 d \left( a+a \sec [c+d x] \right)^2}$$

Result (type 3, 245 leaves):

$$\begin{aligned} & \frac{1}{12 a^2 d \left( 1+\cos [c+d x] \right)^2} \\ & \cos \left[ \frac{1}{2} (c+d x) \right] \sec \left[ \frac{c}{2} \right] \left( -18(2 B-C) d x \cos \left[ \frac{d x}{2} \right] - 18(2 B-C) d x \cos \left[ c+\frac{d x}{2} \right] - \right. \\ & 12 B d x \cos \left[ c+\frac{3 d x}{2} \right] + 6 C d x \cos \left[ c+\frac{3 d x}{2} \right] - 12 B d x \cos \left[ 2 c+\frac{3 d x}{2} \right] + 6 C d x \cos \left[ 2 c+\frac{3 d x}{2} \right] + \\ & 66 B \sin \left[ \frac{d x}{2} \right] - 36 C \sin \left[ \frac{d x}{2} \right] - 30 B \sin \left[ c+\frac{d x}{2} \right] + 24 C \sin \left[ c+\frac{d x}{2} \right] + 41 B \sin \left[ c+\frac{3 d x}{2} \right] - \\ & \left. 20 C \sin \left[ c+\frac{3 d x}{2} \right] + 9 B \sin \left[ 2 c+\frac{3 d x}{2} \right] + 3 B \sin \left[ 2 c+\frac{5 d x}{2} \right] + 3 B \sin \left[ 3 c+\frac{5 d x}{2} \right] \right) \end{aligned}$$

### Problem 346: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^3 \left( B \sec [c+d x]+C \sec [c+d x]^2 \right)}{\left( a+a \sec [c+d x] \right)^2} d x$$

Optimal (type 3, 143 leaves, 7 steps):

$$\frac{(7B-4C)x}{2a^2} - \frac{2(8B-5C)\sin[c+dx]}{3a^2d} + \frac{(7B-4C)\cos[c+dx]\sin[c+dx]}{2a^2d} - \frac{(8B-5C)\cos[c+dx]\sin[c+dx]}{3a^2d(1+\sec[c+dx])} - \frac{(B-C)\cos[c+dx]\sin[c+dx]}{3d(a+a\sec[c+dx])^2}$$

Result (type 3, 315 leaves):

$$\frac{1}{48a^2d(1+\cos[c+dx])^2} \cos\left[\frac{1}{2}(c+dx)\right] \sec\left[\frac{c}{2}\right] \left( 36(7B-4C)dx \cos\left[\frac{dx}{2}\right] + 36(7B-4C)dx \cos\left[c+\frac{dx}{2}\right] + 84Bdx \cos\left[c+\frac{3dx}{2}\right] - 48Cdx \cos\left[c+\frac{3dx}{2}\right] + 84Bdx \cos\left[2c+\frac{3dx}{2}\right] - 48Cdx \cos\left[2c+\frac{3dx}{2}\right] - 381B \sin\left[\frac{dx}{2}\right] + 264C \sin\left[\frac{dx}{2}\right] + 147B \sin\left[c+\frac{dx}{2}\right] - 120C \sin\left[c+\frac{dx}{2}\right] - 239B \sin\left[c+\frac{3dx}{2}\right] + 164C \sin\left[c+\frac{3dx}{2}\right] - 63B \sin\left[2c+\frac{3dx}{2}\right] + 36C \sin\left[2c+\frac{3dx}{2}\right] - 15B \sin\left[2c+\frac{5dx}{2}\right] + 12C \sin\left[2c+\frac{5dx}{2}\right] - 15B \sin\left[3c+\frac{5dx}{2}\right] + 12C \sin\left[3c+\frac{5dx}{2}\right] + 3B \sin\left[3c+\frac{7dx}{2}\right] + 3B \sin\left[4c+\frac{7dx}{2}\right] \right)$$

**Problem 347: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c+dx]^4 (B \sec[c+dx] + C \sec[c+dx]^2)}{(a+a\sec[c+dx])^2} dx$$

Optimal (type 3, 170 leaves, 8 steps):

$$-\frac{(10B-7C)x}{2a^2} + \frac{4(3B-2C)\sin[c+dx]}{a^2d} - \frac{(10B-7C)\cos[c+dx]\sin[c+dx]}{2a^2d} - \frac{(10B-7C)\cos[c+dx]^2\sin[c+dx]}{3a^2d(1+\sec[c+dx])} - \frac{(B-C)\cos[c+dx]^2\sin[c+dx]}{3d(a+a\sec[c+dx])^2} - \frac{4(3B-2C)\sin[c+dx]^3}{3a^2d}$$

Result (type 3, 369 leaves):

$$\frac{1}{48 a^2 d \left(1 + \cos [c + d x]\right)^2} \cos \left[\frac{1}{2}(c + d x)\right] \sec \left[\frac{c}{2}\right] \left(-36(10 B - 7 C) d x \cos \left[\frac{d x}{2}\right] - 36(10 B - 7 C) d x \cos \left[c + \frac{d x}{2}\right] - 120 B d x \cos \left[c + \frac{3 d x}{2}\right] + 84 C d x \cos \left[c + \frac{3 d x}{2}\right] - 120 B d x \cos \left[2 c + \frac{3 d x}{2}\right] + 84 C d x \cos \left[2 c + \frac{3 d x}{2}\right] + 516 B \sin \left[\frac{d x}{2}\right] - 381 C \sin \left[\frac{d x}{2}\right] - 156 B \sin \left[c + \frac{d x}{2}\right] + 147 C \sin \left[c + \frac{d x}{2}\right] + 342 B \sin \left[c + \frac{3 d x}{2}\right] - 239 C \sin \left[c + \frac{3 d x}{2}\right] + 118 B \sin \left[2 c + \frac{3 d x}{2}\right] - 63 C \sin \left[2 c + \frac{3 d x}{2}\right] + 30 B \sin \left[2 c + \frac{5 d x}{2}\right] - 15 C \sin \left[2 c + \frac{5 d x}{2}\right] + 30 B \sin \left[3 c + \frac{5 d x}{2}\right] - 15 C \sin \left[3 c + \frac{5 d x}{2}\right] - 3 B \sin \left[3 c + \frac{7 d x}{2}\right] + 3 C \sin \left[3 c + \frac{7 d x}{2}\right] - 3 B \sin \left[4 c + \frac{7 d x}{2}\right] + 3 C \sin \left[4 c + \frac{7 d x}{2}\right] + B \sin \left[4 c + \frac{9 d x}{2}\right] + B \sin \left[5 c + \frac{9 d x}{2}\right]\right)$$

**Problem 348: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c + d x]^4 \left(B \sec [c + d x] + C \sec [c + d x]^2\right)}{\left(a + a \sec [c + d x]\right)^3} d x$$

Optimal (type 3, 202 leaves, 9 steps):

$$\begin{aligned} & - \frac{(6 B - 13 C) \operatorname{ArcTanh}[\sin [c + d x]]}{2 a^3 d} + \frac{8(9 B - 19 C) \tan [c + d x]}{15 a^3 d} - \\ & \frac{(6 B - 13 C) \sec [c + d x] \tan [c + d x]}{2 a^3 d} + \frac{(B - C) \sec [c + d x]^4 \tan [c + d x]}{5 d \left(a + a \sec [c + d x]\right)^3} + \\ & \frac{(6 B - 11 C) \sec [c + d x]^3 \tan [c + d x]}{15 a d \left(a + a \sec [c + d x]\right)^2} + \frac{4(9 B - 19 C) \sec [c + d x]^2 \tan [c + d x]}{15 d \left(a^3 + a^3 \sec [c + d x]\right)} \end{aligned}$$

Result (type 3, 428 leaves):

$$\begin{aligned} & \frac{1}{60 a^3 d} \cos \left[ \frac{1}{2} (c+d x) \right]^4 \sec [c+d x]^2 \left( 30 (6 B-13 C) \right. \\ & \quad \left. \left( \log \left[ \cos \left[ \frac{1}{2} (c+d x) \right] - \sin \left[ \frac{1}{2} (c+d x) \right] \right] - \log \left[ \cos \left[ \frac{1}{2} (c+d x) \right] + \sin \left[ \frac{1}{2} (c+d x) \right] \right] \right) \right) + \\ & 16 (12 B+13 C) \csc [c+d x]^3 \sin \left[ \frac{1}{2} (c+d x) \right]^4 + 4 (87 B-197 C) \tan \left[ \frac{1}{2} (c+d x) \right] + \\ & (-21 B+31 C+(24 B-34 C) \cos [c+d x]) \sec \left[ \frac{1}{2} (c+d x) \right]^4 \tan \left[ \frac{1}{2} (c+d x) \right] - 60 (6 B-13 C) \\ & \quad \left( \log \left[ \cos \left[ \frac{1}{2} (c+d x) \right] - \sin \left[ \frac{1}{2} (c+d x) \right] \right] - \log \left[ \cos \left[ \frac{1}{2} (c+d x) \right] + \sin \left[ \frac{1}{2} (c+d x) \right] \right] \right) \\ & \tan \left[ \frac{1}{2} (c+d x) \right]^2 - 64 (9 B-19 C) \tan \left[ \frac{1}{2} (c+d x) \right]^3 - \\ & (-6 B+11 C+(12 B-17 C) \cos [c+d x]) \sec \left[ \frac{1}{2} (c+d x) \right]^4 \tan \left[ \frac{1}{2} (c+d x) \right]^3 + 30 (6 B-13 C) \\ & \quad \left( \log \left[ \cos \left[ \frac{1}{2} (c+d x) \right] - \sin \left[ \frac{1}{2} (c+d x) \right] \right] - \log \left[ \cos \left[ \frac{1}{2} (c+d x) \right] + \sin \left[ \frac{1}{2} (c+d x) \right] \right] \right) \\ & \tan \left[ \frac{1}{2} (c+d x) \right]^4 + \left( 228 B-428 C+3 (B-C) \sec \left[ \frac{1}{2} (c+d x) \right]^4 \right) \tan \left[ \frac{1}{2} (c+d x) \right]^5 \end{aligned}$$

**Problem 353: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos [c+d x] (B \sec [c+d x]+C \sec [c+d x]^2)}{(a+a \sec [c+d x])^3} dx$$

Optimal (type 3, 108 leaves, 5 steps):

$$\frac{B x}{a^3} - \frac{(B-C) \tan [c+d x]}{5 d (a+a \sec [c+d x])^3} - \frac{(7 B-2 C) \tan [c+d x]}{15 a d (a+a \sec [c+d x])^2} - \frac{2 (11 B-C) \tan [c+d x]}{15 d (a^3+a^3 \sec [c+d x])}$$

Result (type 3, 241 leaves):

$$\begin{aligned} & \frac{1}{480 a^3 d} \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{1}{2} (c+d x) \right]^5 \\ & \left( 150 B d x \cos \left[ \frac{d x}{2} \right] + 150 B d x \cos \left[ c + \frac{d x}{2} \right] + 75 B d x \cos \left[ c + \frac{3 d x}{2} \right] + 75 B d x \cos \left[ 2 c + \frac{3 d x}{2} \right] + \right. \\ & 15 B d x \cos \left[ 2 c + \frac{5 d x}{2} \right] + 15 B d x \cos \left[ 3 c + \frac{5 d x}{2} \right] - 370 B \sin \left[ \frac{d x}{2} \right] + 80 C \sin \left[ \frac{d x}{2} \right] + \\ & 270 B \sin \left[ c + \frac{d x}{2} \right] - 60 C \sin \left[ c + \frac{d x}{2} \right] - 230 B \sin \left[ c + \frac{3 d x}{2} \right] + 40 C \sin \left[ c + \frac{3 d x}{2} \right] + \\ & \left. 90 B \sin \left[ 2 c + \frac{3 d x}{2} \right] - 30 C \sin \left[ 2 c + \frac{3 d x}{2} \right] - 64 B \sin \left[ 2 c + \frac{5 d x}{2} \right] + 14 C \sin \left[ 2 c + \frac{5 d x}{2} \right] \right) \end{aligned}$$

**Problem 354: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos [c+d x]^2 (B \sec [c+d x]+C \sec [c+d x]^2)}{(a+a \sec [c+d x])^3} dx$$

Optimal (type 3, 136 leaves, 7 steps):

$$-\frac{(3B-C)x}{a^3} + \frac{2(36B-11C)\sin[c+dx]}{15a^3d} - \frac{(B-C)\sin[c+dx]}{5d(a+a\sec[c+dx])^3} - \frac{(9B-4C)\sin[c+dx]}{15ad(a+a\sec[c+dx])^2} - \frac{(3B-C)\sin[c+dx]}{d(a^3+a^3\sec[c+dx])}$$

Result (type 3, 365 leaves):

$$\frac{1}{120a^3d(1+\cos[c+dx])^3} \cos\left[\frac{1}{2}(c+dx)\right] \sec\left[\frac{c}{2}\right] \left( -300(3B-C)dx \cos\left[\frac{dx}{2}\right] - 300(3B-C)dx \cos\left[c+\frac{dx}{2}\right] - 450Bdx \cos\left[c+\frac{3dx}{2}\right] + 150Cdx \cos\left[c+\frac{3dx}{2}\right] - 450Bdx \cos\left[2c+\frac{3dx}{2}\right] + 150Cdx \cos\left[2c+\frac{3dx}{2}\right] - 90Bdx \cos\left[2c+\frac{5dx}{2}\right] + 30Cdx \cos\left[2c+\frac{5dx}{2}\right] - 90Bdx \cos\left[3c+\frac{5dx}{2}\right] + 30Cdx \cos\left[3c+\frac{5dx}{2}\right] + 1755B \sin\left[\frac{dx}{2}\right] - 740C \sin\left[\frac{dx}{2}\right] - 1125B \sin\left[c+\frac{dx}{2}\right] + 540C \sin\left[c+\frac{dx}{2}\right] + 1215B \sin\left[c+\frac{3dx}{2}\right] - 460C \sin\left[c+\frac{3dx}{2}\right] - 225B \sin\left[2c+\frac{3dx}{2}\right] + 180C \sin\left[2c+\frac{3dx}{2}\right] + 363B \sin\left[2c+\frac{5dx}{2}\right] - 128C \sin\left[2c+\frac{5dx}{2}\right] + 75B \sin\left[3c+\frac{5dx}{2}\right] + 15B \sin\left[3c+\frac{7dx}{2}\right] + 15B \sin\left[4c+\frac{7dx}{2}\right] \right)$$

**Problem 355: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c+dx]^3 (B \sec[c+dx] + C \sec[c+dx]^2)}{(a+a\sec[c+dx])^3} dx$$

Optimal (type 3, 187 leaves, 8 steps):

$$\frac{(13B-6C)x}{2a^3} - \frac{8(19B-9C)\sin[c+dx]}{15a^3d} + \frac{(13B-6C)\cos[c+dx]\sin[c+dx]}{2a^3d} - \frac{(B-C)\cos[c+dx]\sin[c+dx]}{5d(a+a\sec[c+dx])^3} - \frac{(11B-6C)\cos[c+dx]\sin[c+dx]}{15ad(a+a\sec[c+dx])^2} - \frac{4(19B-9C)\cos[c+dx]\sin[c+dx]}{15d(a^3+a^3\sec[c+dx])}$$

Result (type 3, 435 leaves):

$$\frac{1}{480 a^3 d (1 + \cos [c + d x])^3} \cos \left[ \frac{1}{2} (c + d x) \right] \sec \left[ \frac{c}{2} \right] \left( 600 (13 B - 6 C) d x \cos \left[ \frac{d x}{2} \right] + 600 (13 B - 6 C) d x \cos \left[ c + \frac{d x}{2} \right] + 3900 B d x \cos \left[ c + \frac{3 d x}{2} \right] - 1800 C d x \cos \left[ c + \frac{3 d x}{2} \right] + 3900 B d x \cos \left[ 2 c + \frac{3 d x}{2} \right] - 1800 C d x \cos \left[ 2 c + \frac{3 d x}{2} \right] + 780 B d x \cos \left[ 2 c + \frac{5 d x}{2} \right] - 360 C d x \cos \left[ 2 c + \frac{5 d x}{2} \right] + 780 B d x \cos \left[ 3 c + \frac{5 d x}{2} \right] - 360 C d x \cos \left[ 3 c + \frac{5 d x}{2} \right] - 12760 B \sin \left[ \frac{d x}{2} \right] + 7020 C \sin \left[ \frac{d x}{2} \right] + 7560 B \sin \left[ c + \frac{d x}{2} \right] - 4500 C \sin \left[ c + \frac{d x}{2} \right] - 9230 B \sin \left[ c + \frac{3 d x}{2} \right] + 4860 C \sin \left[ c + \frac{3 d x}{2} \right] + 930 B \sin \left[ 2 c + \frac{3 d x}{2} \right] - 900 C \sin \left[ 2 c + \frac{3 d x}{2} \right] - 2782 B \sin \left[ 2 c + \frac{5 d x}{2} \right] + 1452 C \sin \left[ 2 c + \frac{5 d x}{2} \right] - 750 B \sin \left[ 3 c + \frac{5 d x}{2} \right] + 300 C \sin \left[ 3 c + \frac{5 d x}{2} \right] - 105 B \sin \left[ 3 c + \frac{7 d x}{2} \right] + 60 C \sin \left[ 3 c + \frac{7 d x}{2} \right] - 105 B \sin \left[ 4 c + \frac{7 d x}{2} \right] + 60 C \sin \left[ 4 c + \frac{7 d x}{2} \right] + 15 B \sin \left[ 4 c + \frac{9 d x}{2} \right] + 15 B \sin \left[ 5 c + \frac{9 d x}{2} \right] \right)$$

**Problem 361: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c + d x] \sqrt{a + a \sec [c + d x]} (B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 3, 66 leaves, 5 steps):

$$\frac{2 \sqrt{a} B \operatorname{ArcTan} \left[ \frac{\sqrt{a} \tan [c + d x]}{\sqrt{a + a \sec [c + d x]}} \right]}{d} + \frac{2 a C \tan [c + d x]}{d \sqrt{a + a \sec [c + d x]}}$$

Result (type 4, 363 leaves):

$$\begin{aligned}
 & -\frac{1}{d} 8 (-3 - 2\sqrt{2}) B \cos\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7 - 5\sqrt{2} + (10 - 7\sqrt{2}) \cos\left[\frac{1}{2}(c+dx)\right]}{1 + \cos\left[\frac{1}{2}(c+dx)\right]}} \\
 & \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c+dx)\right]}{1 + \cos\left[\frac{1}{2}(c+dx)\right]}} \left(1 - \sqrt{2} + (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c+dx)\right]\right) \\
 & \left( \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] + \right. \\
 & \quad \left. 2 \text{EllipticPi}\left[-3 + 2\sqrt{2}, -\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \right) \\
 & \sqrt{\left(-1 - \sqrt{2} + (2 + \sqrt{2}) \cos\left[\frac{1}{2}(c+dx)\right]\right) \sec\left[\frac{1}{4}(c+dx)\right]^2 \sec\left[\frac{1}{2}(c+dx)\right]} \\
 & \sec[c+dx] \sqrt{a(1 + \sec[c+dx])} \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c+dx)\right]^2} + \\
 & \frac{2C \sqrt{a(1 + \sec[c+dx])} \tan\left[\frac{1}{2}(c+dx)\right]}{d}
 \end{aligned}$$

**Problem 362:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \cos[c+dx]^2 \sqrt{a + a \sec[c+dx]} (B \sec[c+dx] + C \sec[c+dx]^2) dx$$

Optimal (type 3, 68 leaves, 4 steps):

$$\frac{\sqrt{a} (B + 2C) \text{ArcTan}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{a + a \sec[c+dx]}}\right]}{d} + \frac{a B \sin[c+dx]}{d \sqrt{a + a \sec[c+dx]}}$$

Result (type 4, 396 leaves):



$$\begin{aligned}
 & \frac{1}{d} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1+\operatorname{Sec}[c+dx])} \left(-\frac{1}{2} B \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + \frac{1}{2} B \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right]\right) - \\
 & \frac{1}{d} 4(-3-2\sqrt{2})(B+2C) \operatorname{Cos}\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7-5\sqrt{2}+(10-7\sqrt{2})\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}{1+\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}} \\
 & \sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2})\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}{1+\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}} \left(1-\sqrt{2}+(-2+\sqrt{2})\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \\
 & \left( \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] + \right. \\
 & \left. 2 \operatorname{EllipticPi}\left[-3+2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \right) \\
 & \sqrt{\left(-1-\sqrt{2}+(2+\sqrt{2})\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]} \\
 & \operatorname{Sec}[c+dx] \sqrt{a(1+\operatorname{Sec}[c+dx])} \sqrt{3-2\sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}
 \end{aligned}$$

**Problem 363: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \operatorname{Cos}[c+dx]^3 \sqrt{a+a \operatorname{Sec}[c+dx]} (B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 3, 117 leaves, 5 steps):

$$\frac{\sqrt{a} (3B+4C) \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{4d} + \frac{a(3B+4C) \operatorname{Sin}[c+dx]}{4d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{aB \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx]}{2d \sqrt{a+a \operatorname{Sec}[c+dx]}}$$

Result (type 4, 418 leaves):

$$\begin{aligned} & \frac{1}{d} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1+\operatorname{Sec}[c+dx])} \\ & \left(-\frac{1}{8}(B+4C) \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + \frac{1}{4}(B+2C) \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right] + \frac{1}{8}B \operatorname{Sin}\left[\frac{5}{2}(c+dx)\right]\right) + \\ & \frac{1}{d} \left(2 + \frac{3}{\sqrt{2}}\right) (3B+4C) \operatorname{Cos}\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7-5\sqrt{2} + (10-7\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}{1+\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}} \\ & \left(1-\sqrt{2} + (-2+\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \left(\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] + \right. \\ & \left. 2 \operatorname{EllipticPi}\left[-3+2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right]\right) \\ & \sqrt{\left(-1+\sqrt{2} - (-2+\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2} \\ & \sqrt{\left(-1-\sqrt{2} + (2+\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]} \\ & \operatorname{Sec}[c+dx] \sqrt{a(1+\operatorname{Sec}[c+dx])} \sqrt{3-2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \end{aligned}$$

**Problem 364: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \operatorname{Cos}[c+dx]^4 \sqrt{a+a \operatorname{Sec}[c+dx]} (B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 3, 160 leaves, 6 steps):

$$\begin{aligned} & \frac{\sqrt{a} (5B+6C) \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{8d} + \frac{a (5B+6C) \operatorname{Sin}[c+dx]}{8d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \\ & \frac{a (5B+6C) \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx]}{12d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{aB \operatorname{Cos}[c+dx]^2 \operatorname{Sin}[c+dx]}{3d \sqrt{a+a \operatorname{Sec}[c+dx]}} \end{aligned}$$

Result (type 4, 443 leaves):

$$\begin{aligned}
 & \frac{1}{d} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1+\operatorname{Sec}[c+dx])} \left( -\frac{1}{48}(11B+6C) \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \frac{1}{12}(4B+3C) \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right] + \frac{1}{16}(B+2C) \operatorname{Sin}\left[\frac{5}{2}(c+dx)\right] + \frac{1}{24}B \operatorname{Sin}\left[\frac{7}{2}(c+dx)\right] \right) + \\
 & \frac{1}{d} \left( 1 + \frac{3}{2\sqrt{2}} \right) (5B+6C) \operatorname{Cos}\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7-5\sqrt{2}+(10-7\sqrt{2})\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}{1+\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}} \\
 & \left( 1 - \sqrt{2} + (-2+\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \right) \left( \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] + \right. \\
 & \quad \left. 2 \operatorname{EllipticPi}\left[-3+2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \right) \\
 & \sqrt{\left( -1 + \sqrt{2} - (-2+\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \sqrt{\left( -1 - \sqrt{2} + (2+\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]} \\
 & \operatorname{Sec}[c+dx] \sqrt{a(1+\operatorname{Sec}[c+dx])} \sqrt{3-2\sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}
 \end{aligned}$$

**Problem 369: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \operatorname{Cos}[c+dx] (a+a \operatorname{Sec}[c+dx])^{3/2} (B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 3, 105 leaves, 6 steps):

$$\frac{2 a^{3/2} B \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{d} + \frac{2 a^2 (3 B + 4 C) \operatorname{Tan}[c+dx]}{3 d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{2 a C \sqrt{a+a \operatorname{Sec}[c+dx]} \operatorname{Tan}[c+dx]}{3 d}$$

Result (type 4, 408 leaves):

$$\begin{aligned} & \frac{1}{d} \cos [c+d x] \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^3 (a(1+\operatorname{Sec}[c+d x]))^{3/2} \\ & \left(\frac{1}{3}(3 B+5 C) \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]+\frac{1}{3} C \operatorname{Sec}[c+d x] \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)- \\ & \frac{1}{d} 4(-3-2 \sqrt{2}) B \operatorname{Cos}\left[\frac{1}{4}(c+d x)\right]^4 \sqrt{\frac{7-5 \sqrt{2}+(10-7 \sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]}{1+\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]}} \\ & \sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]}{1+\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]}}\left(1-\sqrt{2}+(-2+\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]\right) \\ & \left(\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right]+ \right. \\ & \left. 2 \operatorname{EllipticPi}\left[-3+2 \sqrt{2},-\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right]\right) \\ & \sqrt{\left(-1-\sqrt{2}+(2+\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]\right) \operatorname{Sec}\left[\frac{1}{4}(c+d x)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^3} \\ & (a(1+\operatorname{Sec}[c+d x]))^{3/2} \sqrt{3-2 \sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+d x)\right]^2} \end{aligned}$$

**Problem 370: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c+d x]^2 (a+a \operatorname{Sec}[c+d x])^{3/2} (B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) d x$$

Optimal (type 3, 103 leaves, 5 steps):

$$\begin{aligned} & \frac{a^{3/2}(3 B+2 C) \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right]}{d}+ \\ & \frac{a^2(B-2 C) \operatorname{Sin}[c+d x]}{d \sqrt{a+a \operatorname{Sec}[c+d x]}}+\frac{2 a C \sqrt{a+a \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{d} \end{aligned}$$

Result (type 4, 408 leaves):

$$\begin{aligned} & \frac{1}{d} \cos[c + dx] \sec\left[\frac{1}{2}(c + dx)\right]^3 (a(1 + \sec[c + dx]))^{3/2} \\ & \left( \frac{1}{4}(-B + 4C) \sin\left[\frac{1}{2}(c + dx)\right] + \frac{1}{4}B \sin\left[\frac{3}{2}(c + dx)\right] \right) - \\ & \frac{1}{d} 2(-3 - 2\sqrt{2})(3B + 2C) \cos\left[\frac{1}{4}(c + dx)\right]^4 \sqrt{\frac{7 - 5\sqrt{2} + (10 - 7\sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \\ & \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \left(1 - \sqrt{2} + (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]\right) \\ & \left( \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] + \right. \\ & \left. 2 \text{EllipticPi}\left[-3 + 2\sqrt{2}, -\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \right) \\ & \sqrt{\left(-1 - \sqrt{2} + (2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]\right) \sec\left[\frac{1}{4}(c + dx)\right]^2 \sec\left[\frac{1}{2}(c + dx)\right]^3} \\ & (a(1 + \sec[c + dx]))^{3/2} \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \end{aligned}$$

**Problem 372: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c + dx]^4 (a + a \sec[c + dx])^{3/2} (B \sec[c + dx] + C \sec[c + dx]^2) dx$$

Optimal (type 3, 164 leaves, 6 steps):

$$\begin{aligned} & \frac{a^{3/2} (11B + 14C) \text{ArcTan}\left[\frac{\sqrt{a} \tan[c + dx]}{\sqrt{a + a \sec[c + dx]}}\right]}{8d} + \frac{a^2 (11B + 14C) \sin[c + dx]}{8d \sqrt{a + a \sec[c + dx]}} + \\ & \frac{a^2 (7B + 6C) \cos[c + dx] \sin[c + dx]}{12d \sqrt{a + a \sec[c + dx]}} + \frac{aB \cos[c + dx]^2 \sqrt{a + a \sec[c + dx]} \sin[c + dx]}{3d} \end{aligned}$$

Result (type 4, 3073 leaves):

$$a \left( -\frac{1}{d} 2(-3 - 2\sqrt{2}) C \cos\left[\frac{1}{4}(c + dx)\right]^4 \sqrt{\frac{7 - 5\sqrt{2} + (10 - 7\sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \right.$$

$$\begin{aligned}
 & \sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \left(1-\sqrt{2}+(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]\right) \\
 & (1+\cos[c+dx]) \left( \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] + \right. \\
 & \quad \left. 2 \text{EllipticPi}\left[-3+2\sqrt{2}, -\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \right) \\
 & \sec\left[\frac{c}{2}+\frac{dx}{2}\right]^2 \sqrt{\left(-1-\sqrt{2}+(2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]\right) \sec\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \sec\left[\frac{1}{2}(c+dx)\right] \sec[c+dx] \sqrt{a(1+\sec[c+dx])} \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} + \\
 & \frac{1}{4\sqrt{1+\sec[c+dx]}} B (1+\cos[c+dx]) \sec\left[\frac{c}{2}+\frac{dx}{2}\right]^2 \sqrt{a(1+\sec[c+dx])} \\
 & \left( \frac{1}{d} \sec\left[\frac{1}{2}(c+dx)\right] \sqrt{1+\sec[c+dx]} \left(-\frac{1}{2}\sin\left[\frac{1}{2}(c+dx)\right] + \frac{1}{2}\sin\left[\frac{3}{2}(c+dx)\right]\right) - \right. \\
 & \quad \left. \frac{1}{d} 4(-3-2\sqrt{2})\cos\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7-5\sqrt{2}+(10-7\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \right. \\
 & \quad \left. \sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \left(1-\sqrt{2}+(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]\right) \right. \\
 & \quad \left( \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] + \right. \\
 & \quad \left. 2 \text{EllipticPi}\left[-3+2\sqrt{2}, -\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \right) \\
 & \quad \left. \sqrt{\left(\left(-1-\sqrt{2}+(2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]\right) \sec\left[\frac{1}{4}(c+dx)\right]^2\right) \sec\left[\frac{1}{2}(c+dx)\right]} \right. \\
 & \quad \left. \sec[c+dx] \sqrt{1+\sec[c+dx]} \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \right) + \\
 & \frac{1}{2\sqrt{1+\sec[c+dx]}} C (1+\cos[c+dx]) \sec\left[\frac{c}{2}+\frac{dx}{2}\right]^2 \sqrt{a(1+\sec[c+dx])}
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{1}{d} \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right] \sqrt{1+\operatorname{Sec}[c+dx]} \left( -\frac{1}{2} \operatorname{Sin} \left[ \frac{1}{2} (c+dx) \right] + \frac{1}{2} \operatorname{Sin} \left[ \frac{3}{2} (c+dx) \right] \right) - \right. \\
 & \frac{1}{d} 4 (-3-2\sqrt{2}) \operatorname{Cos} \left[ \frac{1}{4} (c+dx) \right]^4 \sqrt{\frac{7-5\sqrt{2}+(10-7\sqrt{2}) \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right]}{1+\operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right]}} \\
 & \sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2}) \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right]}{1+\operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right]}} \left( 1-\sqrt{2}+(-2+\sqrt{2}) \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right] \right) \\
 & \left( \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\operatorname{Tan} \left[ \frac{1}{4} (c+dx) \right]}{\sqrt{3-2\sqrt{2}}} \right], 17-12\sqrt{2} \right] + \right. \\
 & \left. 2 \operatorname{EllipticPi} \left[ -3+2\sqrt{2}, -\operatorname{ArcSin} \left[ \frac{\operatorname{Tan} \left[ \frac{1}{4} (c+dx) \right]}{\sqrt{3-2\sqrt{2}}} \right], 17-12\sqrt{2} \right] \right) \\
 & \sqrt{\left( (-1-\sqrt{2}+(2+\sqrt{2}) \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right]) \operatorname{Sec} \left[ \frac{1}{4} (c+dx) \right]^2 \right) \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]} \\
 & \left. \operatorname{Sec}[c+dx] \sqrt{1+\operatorname{Sec}[c+dx]} \sqrt{3-2\sqrt{2}-\operatorname{Tan} \left[ \frac{1}{4} (c+dx) \right]^2} \right) + \\
 & \frac{1}{2\sqrt{1+\operatorname{Sec}[c+dx]}} B (1+\operatorname{Cos}[c+dx]) \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \sqrt{a(1+\operatorname{Sec}[c+dx])} \\
 & \left( \frac{1}{d} \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right] \sqrt{1+\operatorname{Sec}[c+dx]} \right. \\
 & \left. \left( -\frac{1}{8} \operatorname{Sin} \left[ \frac{1}{2} (c+dx) \right] + \frac{1}{4} \operatorname{Sin} \left[ \frac{3}{2} (c+dx) \right] + \frac{1}{8} \operatorname{Sin} \left[ \frac{5}{2} (c+dx) \right] \right) + \right. \\
 & \frac{1}{d} 3 \left( 2 + \frac{3}{\sqrt{2}} \right) \operatorname{Cos} \left[ \frac{1}{4} (c+dx) \right]^4 \sqrt{\frac{7-5\sqrt{2}+(10-7\sqrt{2}) \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right]}{1+\operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right]}} \\
 & \left( 1-\sqrt{2}+(-2+\sqrt{2}) \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right] \right) \left( \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\operatorname{Tan} \left[ \frac{1}{4} (c+dx) \right]}{\sqrt{3-2\sqrt{2}}} \right], \right. \right. \\
 & \left. \left. 17-12\sqrt{2} \right] + 2 \operatorname{EllipticPi} \left[ -3+2\sqrt{2}, -\operatorname{ArcSin} \left[ \frac{\operatorname{Tan} \left[ \frac{1}{4} (c+dx) \right]}{\sqrt{3-2\sqrt{2}}} \right], 17-12\sqrt{2} \right] \right) \\
 & \left. \sqrt{\left( (-1+\sqrt{2}-(-2+\sqrt{2}) \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right]) \operatorname{Sec} \left[ \frac{1}{4} (c+dx) \right]^2 \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\left( \left( -1 - \sqrt{2} + (2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + dx) \right] \right) \sec \left[ \frac{1}{4} (c + dx) \right]^2 \right) \sec \left[ \frac{1}{2} (c + dx) \right]} \\
 & \sec [c + dx] \sqrt{1 + \sec [c + dx]} \sqrt{3 - 2\sqrt{2} - \tan \left[ \frac{1}{4} (c + dx) \right]^2} \Bigg) + \\
 & \frac{1}{4 \sqrt{1 + \sec [c + dx]}} C (1 + \cos [c + dx]) \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \sqrt{a (1 + \sec [c + dx])} \\
 & \left( \frac{1}{2d} \sec \left[ \frac{1}{2} (c + dx) \right] \sqrt{1 + \sec [c + dx]} \left( -\sin \left[ \frac{1}{2} (c + dx) \right] + \sin \left[ \frac{3}{2} (c + dx) \right] \right) + \right. \\
 & \left. \frac{1}{2d \sqrt{\sec [c + dx]}} \sec \left[ \frac{1}{2} (c + dx) \right] \sqrt{1 + \sec [c + dx]} \left( \frac{1}{2} \sqrt{\sec [c + dx]} \right. \right. \\
 & \left. \left( \sin \left[ \frac{1}{2} (c + dx) \right] + \sin \left[ \frac{5}{2} (c + dx) \right] \right) + 4 (-3 - 2\sqrt{2}) \cos \left[ \frac{1}{4} (c + dx) \right]^4 \right. \\
 & \left. \sqrt{\frac{7 - 5\sqrt{2} + (10 - 7\sqrt{2}) \cos \left[ \frac{1}{2} (c + dx) \right]}{1 + \cos \left[ \frac{1}{2} (c + dx) \right]}} \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + dx) \right]}{1 + \cos \left[ \frac{1}{2} (c + dx) \right]}} \right. \\
 & \left. \left( 1 - \sqrt{2} + (-2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + dx) \right] \right) \left( \text{EllipticF} \left[ \text{ArcSin} \left[ \frac{\tan \left[ \frac{1}{4} (c + dx) \right]}{\sqrt{3 - 2\sqrt{2}}} \right], 17 - \right. \right. \right. \\
 & \left. \left. 12\sqrt{2} \right] + 2 \text{EllipticPi} \left[ -3 + 2\sqrt{2}, -\text{ArcSin} \left[ \frac{\tan \left[ \frac{1}{4} (c + dx) \right]}{\sqrt{3 - 2\sqrt{2}}} \right], 17 - 12\sqrt{2} \right] \right) \Bigg) \\
 & \sqrt{\left( \left( -1 - \sqrt{2} + (2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + dx) \right] \right) \sec \left[ \frac{1}{4} (c + dx) \right]^2 \right) \sec [c + dx]^{3/2} \sqrt{3 - 2\sqrt{2} - \tan \left[ \frac{1}{4} (c + dx) \right]^2} \Bigg) \Bigg) + \\
 & \frac{1}{4 \sqrt{1 + \sec [c + dx]}} B (1 + \cos [c + dx]) \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \sqrt{a (1 + \sec [c + dx])} \\
 & \left( \frac{1}{2} \left( \frac{1}{d} \sec \left[ \frac{1}{2} (c + dx) \right] \sqrt{1 + \sec [c + dx]} \left( -\frac{1}{2} \sin \left[ \frac{1}{2} (c + dx) \right] + \frac{1}{2} \sin \left[ \frac{3}{2} (c + dx) \right] \right) - \right. \\
 & \left. \frac{1}{d} 4 (-3 - 2\sqrt{2}) \cos \left[ \frac{1}{4} (c + dx) \right]^4 \sqrt{\frac{7 - 5\sqrt{2} + (10 - 7\sqrt{2}) \cos \left[ \frac{1}{2} (c + dx) \right]}{1 + \cos \left[ \frac{1}{2} (c + dx) \right]}} \right)
 \end{aligned}$$



$$\begin{aligned}
 & \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \left(1 - \sqrt{2} + (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]\right) \\
 & \left( \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] + \right. \\
 & \quad \left. 2 \text{EllipticPi}\left[-3 + 2\sqrt{2}, -\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right]\right) \\
 & \sqrt{\left(\left(-1 - \sqrt{2} + (2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]\right) \sec\left[\frac{1}{4}(c + dx)\right]^2\right) \sec\left[\frac{1}{2}(c + dx)\right]} \\
 & \sec[c + dx] \sqrt{1 + \sec[c + dx]} \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \Bigg) + \\
 & \frac{1}{2} \left( \frac{1}{6d} \sec\left[\frac{1}{2}(c + dx)\right] \sqrt{1 + \sec[c + dx]} \left(2 \sin\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{3}{2}(c + dx)\right] + \right. \right. \\
 & \quad \left. \left. \sin\left[\frac{7}{2}(c + dx)\right]\right) + \frac{1}{2d \sqrt{\sec[c + dx]}} \sec\left[\frac{1}{2}(c + dx)\right] \right. \\
 & \quad \left. \sqrt{1 + \sec[c + dx]} \left(\frac{1}{2} \sqrt{\sec[c + dx]} \left(\sin\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{5}{2}(c + dx)\right]\right) + \right. \right. \\
 & \quad \left. \left. 4(-3 - 2\sqrt{2}) \cos\left[\frac{1}{4}(c + dx)\right]^4 \sqrt{\frac{7 - 5\sqrt{2} + (10 - 7\sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \right. \right. \\
 & \quad \left. \left. \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \left(1 - \sqrt{2} + (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]\right) \right. \right. \\
 & \quad \left. \left( \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] + \right. \right. \\
 & \quad \left. \left. 2 \text{EllipticPi}\left[-3 + 2\sqrt{2}, -\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right]\right) \right. \\
 & \quad \left. \sqrt{\left(\left(-1 - \sqrt{2} + (2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]\right) \sec\left[\frac{1}{4}(c + dx)\right]^2\right) \right)
 \end{aligned}$$



$$\begin{aligned}
 & \left( \frac{1}{d} \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right] \sqrt{1+\operatorname{Sec}[c+dx]} \left( -\frac{1}{2} \operatorname{Sin} \left[ \frac{1}{2} (c+dx) \right] + \frac{1}{2} \operatorname{Sin} \left[ \frac{3}{2} (c+dx) \right] \right) - \right. \\
 & \frac{1}{d} 4 (-3-2\sqrt{2}) \operatorname{Cos} \left[ \frac{1}{4} (c+dx) \right]^4 \sqrt{\frac{7-5\sqrt{2}+(10-7\sqrt{2}) \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right]}{1+\operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right]}} \\
 & \sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2}) \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right]}{1+\operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right]}} \left( 1-\sqrt{2}+(-2+\sqrt{2}) \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right] \right) \\
 & \left( \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\operatorname{Tan} \left[ \frac{1}{4} (c+dx) \right]}{\sqrt{3-2\sqrt{2}}} \right], 17-12\sqrt{2} \right] + \right. \\
 & \left. 2 \operatorname{EllipticPi} \left[ -3+2\sqrt{2}, -\operatorname{ArcSin} \left[ \frac{\operatorname{Tan} \left[ \frac{1}{4} (c+dx) \right]}{\sqrt{3-2\sqrt{2}}} \right], 17-12\sqrt{2} \right] \right) \\
 & \sqrt{\left( \left( -1-\sqrt{2}+(2+\sqrt{2}) \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right] \right) \operatorname{Sec} \left[ \frac{1}{4} (c+dx) \right]^2 \right) \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]} \\
 & \left. \operatorname{Sec}[c+dx] \sqrt{1+\operatorname{Sec}[c+dx]} \sqrt{3-2\sqrt{2}-\operatorname{Tan} \left[ \frac{1}{4} (c+dx) \right]^2} \right) + \\
 & \frac{1}{8\sqrt{1+\operatorname{Sec}[c+dx]}} 3C \left( 1+\operatorname{Cos}[c+dx] \right) \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \sqrt{a \left( 1+\operatorname{Sec}[c+dx] \right)} \\
 & \left( \frac{1}{d} \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right] \sqrt{1+\operatorname{Sec}[c+dx]} \left( -\frac{1}{2} \operatorname{Sin} \left[ \frac{1}{2} (c+dx) \right] + \frac{1}{2} \operatorname{Sin} \left[ \frac{3}{2} (c+dx) \right] \right) - \right. \\
 & \frac{1}{d} 4 (-3-2\sqrt{2}) \operatorname{Cos} \left[ \frac{1}{4} (c+dx) \right]^4 \sqrt{\frac{7-5\sqrt{2}+(10-7\sqrt{2}) \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right]}{1+\operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right]}} \\
 & \sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2}) \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right]}{1+\operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right]}} \left( 1-\sqrt{2}+(-2+\sqrt{2}) \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right] \right) \\
 & \left( \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\operatorname{Tan} \left[ \frac{1}{4} (c+dx) \right]}{\sqrt{3-2\sqrt{2}}} \right], 17-12\sqrt{2} \right] + \right. \\
 & \left. 2 \operatorname{EllipticPi} \left[ -3+2\sqrt{2}, -\operatorname{ArcSin} \left[ \frac{\operatorname{Tan} \left[ \frac{1}{4} (c+dx) \right]}{\sqrt{3-2\sqrt{2}}} \right], 17-12\sqrt{2} \right] \right)
 \end{aligned}$$

$$\begin{aligned}
& \sqrt{\left( \left( -1 - \sqrt{2} + (2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + dx) \right] \right) \sec \left[ \frac{1}{4} (c + dx) \right]^2 \right) \sec \left[ \frac{1}{2} (c + dx) \right]} \\
& \sec [c + dx] \sqrt{1 + \sec [c + dx]} \sqrt{3 - 2\sqrt{2} - \tan \left[ \frac{1}{4} (c + dx) \right]^2} \Bigg) + \\
& \frac{1}{8\sqrt{1 + \sec [c + dx]}} 3B (1 + \cos [c + dx]) \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \sqrt{a (1 + \sec [c + dx])} \\
& \left( \frac{1}{d} \sec \left[ \frac{1}{2} (c + dx) \right] \sqrt{1 + \sec [c + dx]} \right. \\
& \left. \left( -\frac{1}{8} \sin \left[ \frac{1}{2} (c + dx) \right] + \frac{1}{4} \sin \left[ \frac{3}{2} (c + dx) \right] + \frac{1}{8} \sin \left[ \frac{5}{2} (c + dx) \right] \right) \right) + \\
& \frac{1}{d} 3 \left( 2 + \frac{3}{\sqrt{2}} \right) \cos \left[ \frac{1}{4} (c + dx) \right]^4 \sqrt{\frac{7 - 5\sqrt{2} + (10 - 7\sqrt{2}) \cos \left[ \frac{1}{2} (c + dx) \right]}{1 + \cos \left[ \frac{1}{2} (c + dx) \right]}} \\
& \left( 1 - \sqrt{2} + (-2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + dx) \right] \right) \left( \text{EllipticF} \left[ \text{ArcSin} \left[ \frac{\tan \left[ \frac{1}{4} (c + dx) \right]}{\sqrt{3 - 2\sqrt{2}}} \right] \right], \right. \\
& \left. 17 - 12\sqrt{2} \right] + 2 \text{EllipticPi} \left[ -3 + 2\sqrt{2}, -\text{ArcSin} \left[ \frac{\tan \left[ \frac{1}{4} (c + dx) \right]}{\sqrt{3 - 2\sqrt{2}}} \right], 17 - 12\sqrt{2} \right] \Bigg) \\
& \sqrt{\left( \left( -1 + \sqrt{2} - (-2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + dx) \right] \right) \sec \left[ \frac{1}{4} (c + dx) \right]^2 \right)} \\
& \sqrt{\left( \left( -1 - \sqrt{2} + (2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + dx) \right] \right) \sec \left[ \frac{1}{4} (c + dx) \right]^2 \right) \sec \left[ \frac{1}{2} (c + dx) \right]} \\
& \sec [c + dx] \sqrt{1 + \sec [c + dx]} \sqrt{3 - 2\sqrt{2} - \tan \left[ \frac{1}{4} (c + dx) \right]^2} \Bigg) + \\
& \frac{1}{4\sqrt{1 + \sec [c + dx]}} C (1 + \cos [c + dx]) \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \sqrt{a (1 + \sec [c + dx])} \\
& \left( \frac{1}{2d} \sec \left[ \frac{1}{2} (c + dx) \right] \sqrt{1 + \sec [c + dx]} \left( -\sin \left[ \frac{1}{2} (c + dx) \right] + \sin \left[ \frac{3}{2} (c + dx) \right] \right) \right) + \\
& \frac{1}{2d\sqrt{\sec [c + dx]}} \sec \left[ \frac{1}{2} (c + dx) \right] \sqrt{1 + \sec [c + dx]} \left( \frac{1}{2} \sqrt{\sec [c + dx]} \right. \\
& \left. \left( \sin \left[ \frac{1}{2} (c + dx) \right] + \sin \left[ \frac{5}{2} (c + dx) \right] \right) + 4 (-3 - 2\sqrt{2}) \cos \left[ \frac{1}{4} (c + dx) \right]^4 \right)
\end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{7-5\sqrt{2}+(10-7\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \\
 & \left(1-\sqrt{2}+(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]\right) \left(\text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right]+2\text{EllipticPi}\left[-3+2\sqrt{2}, -\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right]\right) \\
 & \sqrt{\left(\left(-1-\sqrt{2}+(2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]\right)\sec\left[\frac{1}{4}(c+dx)\right]^2\right)} \\
 & \left.\sec[c+dx]^{3/2} \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2}\right) + \\
 & \frac{1}{8\sqrt{1+\sec[c+dx]}} C(1+\cos[c+dx]) \sec\left[\frac{c}{2}+\frac{dx}{2}\right]^2 \sqrt{a(1+\sec[c+dx])} \\
 & \left(\frac{1}{6d}\sec\left[\frac{1}{2}(c+dx)\right] \sqrt{1+\sec[c+dx]}\right. \\
 & \left. \left(2\sin\left[\frac{1}{2}(c+dx)\right]-\sin\left[\frac{3}{2}(c+dx)\right]+\sin\left[\frac{7}{2}(c+dx)\right]\right) + \right. \\
 & \left. \frac{1}{2d\sqrt{\sec[c+dx]}} \sec\left[\frac{1}{2}(c+dx)\right] \sqrt{1+\sec[c+dx]}\left(\frac{1}{2}\sqrt{\sec[c+dx]}\right.\right. \\
 & \left. \left. \left(\sin\left[\frac{1}{2}(c+dx)\right]+\sin\left[\frac{5}{2}(c+dx)\right]\right)+4(-3-2\sqrt{2})\cos\left[\frac{1}{4}(c+dx)\right]^4\right.\right. \\
 & \left. \left. \sqrt{\frac{7-5\sqrt{2}+(10-7\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}}\right.\right. \\
 & \left. \left. \left(1-\sqrt{2}+(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]\right)\left(\text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right]+2\text{EllipticPi}\left[-3+2\sqrt{2}, -\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right]\right)\right. \\
 & \left. \left. \sqrt{\left(\left(-1-\sqrt{2}+(2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]\right)\sec\left[\frac{1}{4}(c+dx)\right]^2\right)}\right)
 \end{aligned}$$



$$\begin{aligned}
 & \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \left(1 - \sqrt{2} + (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]\right) \\
 & \left( \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] + \right. \\
 & \quad \left. 2 \text{EllipticPi}\left[-3 + 2\sqrt{2}, -\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \right) \\
 & \sqrt{\left(\left(-1 - \sqrt{2} + (2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]\right) \sec\left[\frac{1}{4}(c + dx)\right]^2\right)} \\
 & \sec[c + dx]^{3/2} \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \Bigg) \Bigg) + \\
 & \frac{1}{8\sqrt{1 + \sec[c + dx]}} B (1 + \cos[c + dx]) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sqrt{a(1 + \sec[c + dx])} \\
 & \left(\frac{1}{2} \left(\frac{1}{2d} \sec\left[\frac{1}{2}(c + dx)\right] \sqrt{1 + \sec[c + dx]} \left(-\sin\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{3}{2}(c + dx)\right]\right) + \right. \right. \\
 & \quad \frac{1}{2d\sqrt{\sec[c + dx]}} \sec\left[\frac{1}{2}(c + dx)\right] \sqrt{1 + \sec[c + dx]} \\
 & \quad \left. \left(\frac{1}{2} \sqrt{\sec[c + dx]} \left(\sin\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{5}{2}(c + dx)\right]\right) + \right. \right. \\
 & \quad \left. 4(-3 - 2\sqrt{2}) \cos\left[\frac{1}{4}(c + dx)\right]^4 \sqrt{\frac{7 - 5\sqrt{2} + (10 - 7\sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \right. \\
 & \quad \left. \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \left(1 - \sqrt{2} + (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]\right) \right. \\
 & \quad \left( \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] + \right. \\
 & \quad \left. 2 \text{EllipticPi}\left[-3 + 2\sqrt{2}, -\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \right) \\
 & \left. \sqrt{\left(\left(-1 - \sqrt{2} + (2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]\right) \sec\left[\frac{1}{4}(c + dx)\right]^2\right)} \right)
 \end{aligned}$$





$$\frac{2 a^{5/2} B \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right]}{d} + \frac{2 a^3 (35 B + 32 C) \operatorname{Tan}[c+d x]}{15 d \sqrt{a+a \operatorname{Sec}[c+d x]}} + \frac{2 a^2 (5 B + 8 C) \sqrt{a+a \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x]}{15 d} + \frac{2 a C (a+a \operatorname{Sec}[c+d x])^{3/2} \operatorname{Tan}[c+d x]}{5 d}$$

Result (type 4, 455 leaves):

$$\begin{aligned} & \frac{1}{d} \operatorname{Cos}[c+d x]^2 \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^5 (a(1+\operatorname{Sec}[c+d x]))^{5/2} \\ & \left( \frac{1}{30} (40 B + 43 C) \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] + \frac{1}{10} C \operatorname{Sec}[c+d x]^2 \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] + \right. \\ & \quad \left. \frac{1}{30} \operatorname{Sec}[c+d x] \left( 5 B \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] + 14 C \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right) \right) - \\ & \frac{1}{d} 2 (-3 - 2\sqrt{2}) B \operatorname{Cos}\left[\frac{1}{4}(c+d x)\right]^4 \sqrt{\frac{7 - 5\sqrt{2} + (10 - 7\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]}{1 + \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]}} \\ & \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]}{1 + \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]}} \left( 1 - \sqrt{2} + (-2 + \sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] \right) \\ & \operatorname{Cos}[c+d x] \left( \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+d x)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] + \right. \\ & \quad \left. 2 \operatorname{EllipticPi}\left[-3 + 2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+d x)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \right) \\ & \sqrt{\left( -1 - \sqrt{2} + (2 + \sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] \right) \operatorname{Sec}\left[\frac{1}{4}(c+d x)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^5} \\ & (a(1+\operatorname{Sec}[c+d x]))^{5/2} \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c+d x)\right]^2} \end{aligned}$$

**Problem 379: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \operatorname{Cos}[c+d x]^2 (a+a \operatorname{Sec}[c+d x])^{5/2} (B \operatorname{Sec}[c+d x] + C \operatorname{Sec}[c+d x]^2) dx$$

Optimal (type 3, 143 leaves, 6 steps):

$$\frac{a^{5/2} (5B + 2C) \operatorname{ArcTan}\left[\frac{-\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{d} - \frac{a^3 (3B + 14C) \operatorname{Sin}[c+dx]}{3d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{2a^2 (B + 2C) \sqrt{a+a \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{d} + \frac{2aC (a+a \operatorname{Sec}[c+dx])^{3/2} \operatorname{Sin}[c+dx]}{3d}$$

Result (type 4, 434 leaves):

$$\begin{aligned} & \frac{1}{d} \operatorname{Cos}[c+dx]^2 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\operatorname{Sec}[c+dx]))^{5/2} \\ & \left( \frac{1}{24} (9B + 32C) \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + \frac{1}{6} C \operatorname{Sec}[c+dx] \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + \frac{1}{8} B \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right] \right) + \\ & \frac{1}{d} \left( 2 + \frac{3}{\sqrt{2}} \right) (5B + 2C) \operatorname{Cos}\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7 - 5\sqrt{2} + (10 - 7\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}{1 + \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}} \\ & \left( 1 - \sqrt{2} + (-2 + \sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \right) \operatorname{Cos}[c+dx] \\ & \left( \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] + \right. \\ & \left. 2 \operatorname{EllipticPi}\left[-3 + 2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \right) \\ & \sqrt{\left( -1 + \sqrt{2} - (-2 + \sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2} \\ & \sqrt{\left( -1 - \sqrt{2} + (2 + \sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2} \\ & \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\operatorname{Sec}[c+dx]))^{5/2} \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \end{aligned}$$

**Problem 380: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \operatorname{Cos}[c+dx]^3 (a+a \operatorname{Sec}[c+dx])^{5/2} (B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 3, 154 leaves, 6 steps):

$$\frac{a^{5/2} (19B + 20C) \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{4d} + \frac{a^3 (9B - 4C) \operatorname{Sin}[c+dx]}{4d \sqrt{a+a \operatorname{Sec}[c+dx]}} - \frac{a^2 (B - 4C) \sqrt{a+a \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{2d} + \frac{aB \operatorname{Cos}[c+dx] (a+a \operatorname{Sec}[c+dx])^{3/2} \operatorname{Sin}[c+dx]}{2d}$$

Result (type 4, 437 leaves):

$$\begin{aligned} & \frac{1}{d} \operatorname{Cos}[c+dx]^2 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\operatorname{Sec}[c+dx]))^{5/2} \\ & \left( \frac{3}{32} (-3B+4C) \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + \frac{1}{16} (5B+2C) \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right] + \frac{1}{32} B \operatorname{Sin}\left[\frac{5}{2}(c+dx)\right] \right) + \\ & \frac{1}{8d} (4+3\sqrt{2}) (19B+20C) \operatorname{Cos}\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7-5\sqrt{2}+(10-7\sqrt{2})\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}{1+\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}} \\ & \left( (1-\sqrt{2}+(-2+\sqrt{2})\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]) \operatorname{Cos}[c+dx] \right. \\ & \left. \left( \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] + \right. \right. \\ & \left. \left. 2 \operatorname{EllipticPi}\left[-3+2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \right) \right) \\ & \sqrt{\left(-1+\sqrt{2}-(-2+\sqrt{2})\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2} \\ & \sqrt{\left(-1-\sqrt{2}+(2+\sqrt{2})\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2} \\ & \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\operatorname{Sec}[c+dx]))^{5/2} \sqrt{3-2\sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \end{aligned}$$

**Problem 382: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \operatorname{Cos}[c+dx]^5 (a+a \operatorname{Sec}[c+dx])^{5/2} (B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 3, 209 leaves, 7 steps):

$$\frac{a^{5/2} (163 B + 200 C) \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{64 d} +$$

$$\frac{a^3 (163 B + 200 C) \operatorname{Sin}[c+dx]}{64 d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{a^3 (95 B + 104 C) \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx]}{96 d \sqrt{a+a \operatorname{Sec}[c+dx]}} +$$

$$\frac{a^2 (11 B + 8 C) \operatorname{Cos}[c+dx]^2 \sqrt{a+a \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{24 d} +$$

$$\frac{a B \operatorname{Cos}[c+dx]^3 (a+a \operatorname{Sec}[c+dx])^{3/2} \operatorname{Sin}[c+dx]}{4 d}$$

Result (type 4, 479 leaves):

$$\frac{1}{d} \operatorname{Cos}[c+dx]^2 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\operatorname{Sec}[c+dx]))^{5/2}$$

$$\left( -\frac{(265 B + 376 C) \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]}{1536} + \frac{1}{192} (55 B + 64 C) \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right] + \right.$$

$$\left. \frac{1}{512} (47 B + 40 C) \operatorname{Sin}\left[\frac{5}{2}(c+dx)\right] + \frac{1}{192} (5 B + 2 C) \operatorname{Sin}\left[\frac{7}{2}(c+dx)\right] + \frac{1}{256} B \operatorname{Sin}\left[\frac{9}{2}(c+dx)\right] \right) +$$

$$\frac{1}{64 d} \left( 2 + \frac{3}{\sqrt{2}} \right) (163 B + 200 C) \operatorname{Cos}\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7 - 5\sqrt{2} + (10 - 7\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}{1 + \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}}$$

$$\left( 1 - \sqrt{2} + (-2 + \sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \right) \operatorname{Cos}[c+dx]$$

$$\left( \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] + \right.$$

$$\left. 2 \operatorname{EllipticPi}\left[-3 + 2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \right)$$

$$\sqrt{\left( -1 + \sqrt{2} - (-2 + \sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2}$$

$$\sqrt{\left( -1 - \sqrt{2} + (2 + \sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2}$$

$$\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\operatorname{Sec}[c+dx]))^{5/2} \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}$$

### Problem 383: Result unnecessarily involves higher level functions.

$$\int \cos [c + d x]^6 (a + a \sec [c + d x])^{5/2} (B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 3, 254 leaves, 8 steps):

$$\begin{aligned} & \frac{a^{5/2} (283 B + 326 C) \operatorname{ArcTan} \left[ \frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \sec [c+dx]}} \right]}{128 d} + \frac{a^3 (283 B + 326 C) \operatorname{Sin}[c + d x]}{128 d \sqrt{a + a \sec [c + d x]}} + \\ & \frac{a^3 (283 B + 326 C) \operatorname{Cos}[c + d x] \operatorname{Sin}[c + d x]}{192 d \sqrt{a + a \sec [c + d x]}} + \frac{a^3 (157 B + 170 C) \operatorname{Cos}[c + d x]^2 \operatorname{Sin}[c + d x]}{240 d \sqrt{a + a \sec [c + d x]}} + \\ & \frac{a^2 (13 B + 10 C) \operatorname{Cos}[c + d x]^3 \sqrt{a + a \sec [c + d x]} \operatorname{Sin}[c + d x]}{40 d} + \\ & \frac{a B \operatorname{Cos}[c + d x]^4 (a + a \sec [c + d x])^{3/2} \operatorname{Sin}[c + d x]}{5 d} \end{aligned}$$

Result (type 4, 500 leaves):

$$\frac{1}{d} \text{Cos}[c + d x]^2 \text{Sec}\left[\frac{1}{2}(c + d x)\right]^5 \left(a(1 + \text{Sec}[c + d x])\right)^{5/2}$$

$$\left( -\frac{(2309 B + 2650 C) \text{Sin}\left[\frac{1}{2}(c + d x)\right]}{15360} + \frac{(509 B + 550 C) \text{Sin}\left[\frac{3}{2}(c + d x)\right]}{1920} + \right.$$

$$\frac{(95 B + 94 C) \text{Sin}\left[\frac{5}{2}(c + d x)\right]}{1024} + \frac{1}{960} (32 B + 25 C) \text{Sin}\left[\frac{7}{2}(c + d x)\right] +$$

$$\left. \frac{1}{512} (5 B + 2 C) \text{Sin}\left[\frac{9}{2}(c + d x)\right] + \frac{1}{640} B \text{Sin}\left[\frac{11}{2}(c + d x)\right] \right) +$$

$$\frac{1}{256 d} (4 + 3\sqrt{2}) (283 B + 326 C) \text{Cos}\left[\frac{1}{4}(c + d x)\right]^4 \sqrt{\frac{7 - 5\sqrt{2} + (10 - 7\sqrt{2}) \text{Cos}\left[\frac{1}{2}(c + d x)\right]}{1 + \text{Cos}\left[\frac{1}{2}(c + d x)\right]}}$$

$$\left( (1 - \sqrt{2} + (-2 + \sqrt{2}) \text{Cos}\left[\frac{1}{2}(c + d x)\right]) \text{Cos}[c + d x] \right.$$

$$\left( \text{EllipticF}\left[\text{ArcSin}\left[\frac{\text{Tan}\left[\frac{1}{4}(c + d x)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] + \right.$$

$$\left. 2 \text{EllipticPi}\left[-3 + 2\sqrt{2}, -\text{ArcSin}\left[\frac{\text{Tan}\left[\frac{1}{4}(c + d x)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \right)$$

$$\sqrt{\left(-1 + \sqrt{2} - (-2 + \sqrt{2}) \text{Cos}\left[\frac{1}{2}(c + d x)\right]\right) \text{Sec}\left[\frac{1}{4}(c + d x)\right]^2}$$

$$\sqrt{\left(-1 - \sqrt{2} + (2 + \sqrt{2}) \text{Cos}\left[\frac{1}{2}(c + d x)\right]\right) \text{Sec}\left[\frac{1}{4}(c + d x)\right]^2}$$

$$\text{Sec}\left[\frac{1}{2}(c + d x)\right]^5 \left(a(1 + \text{Sec}[c + d x])\right)^{5/2} \sqrt{3 - 2\sqrt{2} - \text{Tan}\left[\frac{1}{4}(c + d x)\right]^2}$$

**Problem 404: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Sec}[c + d x] (B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2)}{(a + a \text{Sec}[c + d x])^{5/2}} dx$$

Optimal (type 3, 126 leaves, 5 steps):

$$\frac{(5 B + 19 C) \text{ArcTan}\left[\frac{\sqrt{a} \text{Tan}[c + d x]}{\sqrt{2} \sqrt{a + a \text{Sec}[c + d x]}}\right]}{16 \sqrt{2} a^{5/2} d} - \frac{(B - C) \text{Tan}[c + d x]}{4 d (a + a \text{Sec}[c + d x])^{5/2}} + \frac{(5 B - 13 C) \text{Tan}[c + d x]}{16 a d (a + a \text{Sec}[c + d x])^{3/2}}$$

Result (type 3, 256 leaves):

$$\left( (5B + 19C) \operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]\right] \cos\left[\frac{1}{2}(c + dx)\right]^4 \sqrt{\frac{\cos[c + dx]}{1 + \cos[c + dx]}} \operatorname{Sec}[c + dx]^{5/2} \right. \\ \left. \sqrt{1 + \operatorname{Sec}[c + dx]} \right) / \left( 4d \sqrt{\operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 (a(1 + \operatorname{Sec}[c + dx]))^{5/2}} \right) + \\ \left( \cos\left[\frac{1}{2}(c + dx)\right]^5 \operatorname{Sec}[c + dx]^3 \left( -\frac{1}{2}(-B + 9C) \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right] + \right. \right. \\ \left. \frac{1}{2} \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^4 \left( -B \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right] + C \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right] \right) + \frac{1}{4} \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right. \\ \left. \left. \left( 3B \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right] + 5C \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right] \right) \right) \right) / (d(a(1 + \operatorname{Sec}[c + dx]))^{5/2})$$

**Problem 405: Result more than twice size of optimal antiderivative.**

$$\int \frac{B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2}{(a + a \operatorname{Sec}[c + dx])^{5/2}} dx$$

Optimal (type 3, 126 leaves, 5 steps):

$$\frac{(3B + 5C) \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c + dx]}{\sqrt{2} \sqrt{a + a \operatorname{Sec}[c + dx]}}\right]}{16\sqrt{2} a^{5/2} d} + \frac{(B - C) \operatorname{Tan}[c + dx]}{4d(a + a \operatorname{Sec}[c + dx])^{5/2}} + \frac{(3B + 5C) \operatorname{Tan}[c + dx]}{16ad(a + a \operatorname{Sec}[c + dx])^{3/2}}$$

Result (type 3, 298 leaves):

$$\left( (3B + 5C) \operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]\right] \cos\left[\frac{1}{2}(c + dx)\right]^4 \right. \\ \left. \sqrt{\frac{\cos[c + dx]}{1 + \cos[c + dx]}} \operatorname{Sec}[c + dx]^{3/2} \sqrt{1 + \operatorname{Sec}[c + dx]} (B + C \operatorname{Sec}[c + dx]) \right) / \\ \left( 4d(C + B \cos[c + dx]) \sqrt{\operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 (a(1 + \operatorname{Sec}[c + dx]))^{5/2}} \right) + \\ \left( \cos\left[\frac{1}{2}(c + dx)\right]^5 \operatorname{Sec}[c + dx]^2 (B + C \operatorname{Sec}[c + dx]) \right. \\ \left( \frac{1}{2}(7B + C) \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right] + \frac{1}{2} \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^4 \left( B \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right] - C \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right] \right) + \right. \\ \left. \frac{1}{4} \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \left( -11B \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right] + 3C \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right] \right) \right) / \\ (d(C + B \cos[c + dx]) (a(1 + \operatorname{Sec}[c + dx]))^{5/2})$$

### Problem 408: Result more than twice size of optimal antiderivative.

$$\int \sec [c+d x]^3 (a+a \sec [c+d x]) (A+B \sec [c+d x]+C \sec [c+d x]^2) d x$$

Optimal (type 3, 152 leaves, 7 steps):

$$\frac{a(4A+3(B+C)) \operatorname{ArcTanh}[\sin [c+d x]]}{8 d} + \frac{a(5A+5B+4C) \tan [c+d x]}{5 d} +$$

$$\frac{a(4A+3(B+C)) \sec [c+d x] \tan [c+d x]}{8 d} + \frac{a(B+C) \sec [c+d x]^3 \tan [c+d x]}{4 d} +$$

$$\frac{a C \sec [c+d x]^4 \tan [c+d x]}{5 d} + \frac{a(5A+5B+4C) \tan [c+d x]^3}{15 d}$$

Result (type 3, 660 leaves):

$$\frac{a A \operatorname{Log}\left[\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right]}{2 d} - \frac{3 a B \operatorname{Log}\left[\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right]}{8 d} -$$

$$\frac{3 a C \operatorname{Log}\left[\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right]}{8 d} + \frac{a A \operatorname{Log}\left[\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right]}{2 d} +$$

$$\frac{3 a B \operatorname{Log}\left[\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right]}{8 d} + \frac{3 a C \operatorname{Log}\left[\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right]}{8 d} +$$

$$\frac{16 d\left(\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right)^4}{a A} + \frac{16 d\left(\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right)^4}{3 a B} +$$

$$\frac{4 d\left(\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right)^2}{3 a C} + \frac{16 d\left(\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right)^2}{a B} -$$

$$\frac{16 d\left(\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right)^2}{a C} - \frac{16 d\left(\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right)^4}{a A} -$$

$$\frac{16 d\left(\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right)^4}{3 a B} - \frac{16 d\left(\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right)^2}{3 a C} +$$

$$\frac{2 a A \tan [c+d x]}{3 d} + \frac{2 a B \tan [c+d x]}{3 d} + \frac{8 a C \tan [c+d x]}{15 d} + \frac{a A \sec [c+d x]^2 \tan [c+d x]}{3 d} +$$

$$\frac{a B \sec [c+d x]^2 \tan [c+d x]}{3 d} + \frac{4 a C \sec [c+d x]^2 \tan [c+d x]}{15 d} + \frac{a C \sec [c+d x]^4 \tan [c+d x]}{5 d}$$

### Problem 409: Result more than twice size of optimal antiderivative.

$$\int \sec [c+d x]^2 (a+a \sec [c+d x]) (A+B \sec [c+d x]+C \sec [c+d x]^2) d x$$

Optimal (type 3, 127 leaves, 7 steps):



$$\frac{a (4 A + 4 B + 3 C) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{8 d} +$$

$$\frac{a (3 A + 2 (B + C)) \operatorname{Tan}[c + d x]}{3 d} + \frac{a (4 A + 4 B + 3 C) \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x]}{8 d} +$$

$$\frac{a (B + C) \operatorname{Sec}[c + d x]^2 \operatorname{Tan}[c + d x]}{3 d} + \frac{a C \operatorname{Sec}[c + d x]^3 \operatorname{Tan}[c + d x]}{4 d}$$

Result (type 3, 545 leaves):

$$\frac{a A \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right]}{2 d} -$$

$$\frac{a B \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right]}{2 d} - \frac{3 a C \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right]}{8 d} +$$

$$\frac{a A \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right]}{2 d} + \frac{a B \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right]}{2 d} +$$

$$\frac{3 a C \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right]}{8 d} + \frac{a C}{16 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^4} +$$

$$\frac{a A}{4 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} + \frac{a B}{4 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} +$$

$$\frac{3 a C}{16 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} - \frac{a B}{16 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^4} -$$

$$\frac{a A}{4 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} - \frac{a B}{4 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} -$$

$$\frac{3 a C}{16 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} + \frac{a A \operatorname{Tan}[c + d x]}{d} + \frac{2 a B \operatorname{Tan}[c + d x]}{3 d} +$$

$$\frac{2 a C \operatorname{Tan}[c + d x]}{3 d} + \frac{a B \operatorname{Sec}[c + d x]^2 \operatorname{Tan}[c + d x]}{3 d} + \frac{a C \operatorname{Sec}[c + d x]^2 \operatorname{Tan}[c + d x]}{3 d}$$

**Problem 410: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c + d x] (a + a \operatorname{Sec}[c + d x]) (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 3, 92 leaves, 6 steps):

$$\frac{a (2 A + B + C) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{2 d} + \frac{a (3 A + 3 B + 2 C) \operatorname{Tan}[c + d x]}{3 d} +$$

$$\frac{a (B + C) \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x]}{2 d} + \frac{a C \operatorname{Sec}[c + d x]^2 \operatorname{Tan}[c + d x]}{3 d}$$

Result (type 3, 995 leaves):

$$\begin{aligned}
& a \left( \left( (-2A - B - C) \cos[c + dx]^2 \operatorname{Log} \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] - \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right] \right. \right. \\
& \quad \left. \left. (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right) \right) / (d(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\
& \left( (2A + B + C) \cos[c + dx]^2 \operatorname{Log} \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] + \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right] \right. \\
& \quad \left. (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right) / (d(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\
& \left( C \cos[c + dx]^2 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \sin \left[ \frac{dx}{2} \right] \right) / \\
& \left( 3d(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \right. \\
& \quad \left. \left( \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] - \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right)^3 \right) + \left( \cos[c + dx]^2 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right. \\
& \quad \left. \left( 3B \cos \left[ \frac{c}{2} \right] + 4C \cos \left[ \frac{c}{2} \right] - 3B \sin \left[ \frac{c}{2} \right] - 2C \sin \left[ \frac{c}{2} \right] \right) \right) / \\
& \left( 6d(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \right. \\
& \quad \left. \left( \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] - \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right)^2 \right) + \left( 2 \cos[c + dx]^2 \right. \\
& \quad \left. (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \left( 3A \sin \left[ \frac{dx}{2} \right] + 3B \sin \left[ \frac{dx}{2} \right] + 2C \sin \left[ \frac{dx}{2} \right] \right) \right) / \\
& \left( 3d(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \right. \\
& \quad \left. \left( \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] - \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right) \right) + \\
& \left( C \cos[c + dx]^2 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \sin \left[ \frac{dx}{2} \right] \right) / \\
& \left( 3d(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \right. \\
& \quad \left. \left( \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] + \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right)^3 \right) + \left( \cos[c + dx]^2 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right. \\
& \quad \left. \left( -3B \cos \left[ \frac{c}{2} \right] - 4C \cos \left[ \frac{c}{2} \right] - 3B \sin \left[ \frac{c}{2} \right] - 2C \sin \left[ \frac{c}{2} \right] \right) \right) / \\
& \left( 6d(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \right. \\
& \quad \left. \left( \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] + \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right)^2 \right) + \left( 2 \cos[c + dx]^2 \right. \\
& \quad \left. (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \left( 3A \sin \left[ \frac{dx}{2} \right] + 3B \sin \left[ \frac{dx}{2} \right] + 2C \sin \left[ \frac{dx}{2} \right] \right) \right) / \\
& \left( 3d(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \right. \\
& \quad \left. \left( \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] + \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right) \right)
\end{aligned}$$

**Problem 411: Result more than twice size of optimal antiderivative.**

$$\int (a + a \sec [c + d x]) (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 3, 63 leaves, 5 steps):

$$a A x + \frac{a (2 A + 2 B + C) \operatorname{ArcTanh}[\sin [c + d x]]}{2 d} + \frac{a (B + C) \tan [c + d x]}{d} + \frac{a C \sec [c + d x] \tan [c + d x]}{2 d}$$

Result (type 3, 305 leaves):

$$\left( a \cos [c + d x]^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\ \left. \left( 4 A x - \frac{2 (2 A + 2 B + C) \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right]}{d} + \right. \right. \\ \left. \frac{2 (2 A + 2 B + C) \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right]}{d} + \right. \\ \left. \frac{C}{d \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2} + \right. \\ \left. \frac{4 (B + C) \sin \left[ \frac{d x}{2} \right]}{d \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)} - \right. \\ \left. \frac{C}{d \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2} + \right. \\ \left. \frac{4 (B + C) \sin \left[ \frac{d x}{2} \right]}{d \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)} \right) \Bigg/ \\ \left( 2 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 (c + d x)]) \right)$$

**Problem 412: Result more than twice size of optimal antiderivative.**

$$\int \cos [c + d x] (a + a \sec [c + d x]) (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 3, 46 leaves, 5 steps):

$$a (A + B) x + \frac{a (B + C) \operatorname{ArcTanh}[\sin [c + d x]]}{d} + \frac{a A \sin [c + d x]}{d} + \frac{a C \tan [c + d x]}{d}$$

Result (type 3, 187 leaves):

$$\begin{aligned}
 & a A x + a B x - \frac{a B \operatorname{Log}\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d} - \frac{a C \operatorname{Log}\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d} + \\
 & \frac{a B \operatorname{Log}\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d} + \frac{a C \operatorname{Log}\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d} + \\
 & \frac{a A \cos[dx] \sin[c]}{d} + \frac{a A \cos[c] \sin[dx]}{d} + \frac{a C \tan[c+dx]}{d}
 \end{aligned}$$

**Problem 417: Result more than twice size of optimal antiderivative.**

$$\int \sec[c+dx]^3 (a+a \sec[c+dx])^2 (A+B \sec[c+dx]+C \sec[c+dx]^2) dx$$

Optimal (type 3, 222 leaves, 8 steps):

$$\begin{aligned}
 & \frac{a^2 (14 A + 12 B + 11 C) \operatorname{ArcTanh}[\sin[c+dx]]}{16 d} + \\
 & \frac{a^2 (10 A + 9 B + 8 C) \tan[c+dx]}{5 d} + \frac{a^2 (14 A + 12 B + 11 C) \sec[c+dx] \tan[c+dx]}{16 d} + \\
 & \frac{a^2 (10 A + 12 B + 9 C) \sec[c+dx]^3 \tan[c+dx]}{40 d} + \frac{C \sec[c+dx]^3 (a+a \sec[c+dx])^2 \tan[c+dx]}{6 d} + \\
 & \frac{(3 B + C) \sec[c+dx]^3 (a^2 + a^2 \sec[c+dx]) \tan[c+dx]}{15 d} + \frac{a^2 (10 A + 9 B + 8 C) \tan[c+dx]^3}{15 d}
 \end{aligned}$$

Result (type 3, 959 leaves):

$$\begin{aligned}
 & \left( (-14A - 12B - 11C) \cos[c + dx]^4 \operatorname{Log}\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \right. \\
 & \quad \left. \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a + a \sec[c + dx])^2 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right) / \\
 & (32d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\
 & \left( (14A + 12B + 11C) \cos[c + dx]^4 \operatorname{Log}\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \right. \\
 & \quad \left. \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a + a \sec[c + dx])^2 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right) / \\
 & (32d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\
 & \left( C \sec[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sec[c + dx]^2 (a + a \sec[c + dx])^2 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\
 & \quad \left. \sin[dx] \right) / (12d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\
 & \left( \sec[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sec[c + dx] (a + a \sec[c + dx])^2 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\
 & \quad \left. (5C \sin[c] + 6B \sin[dx] + 12C \sin[dx]) \right) / \\
 & (60d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\
 & \left( \sec[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a + a \sec[c + dx])^2 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\
 & \quad \left. (24B \sin[c] + 48C \sin[c] + 30A \sin[dx] + 60B \sin[dx] + 55C \sin[dx]) \right) / \\
 & (240d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\
 & \left( \cos[c + dx] \sec[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a + a \sec[c + dx])^2 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\
 & \quad \left. (30A \sin[c] + 60B \sin[c] + 55C \sin[c] + 80A \sin[dx] + 72B \sin[dx] + 64C \sin[dx]) \right) / \\
 & (240d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\
 & \left( \cos[c + dx]^2 \sec[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a + a \sec[c + dx])^2 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\
 & \quad \left. (160A \sin[c] + 144B \sin[c] + 128C \sin[c] + 210A \sin[dx] + 180B \sin[dx] + 165C \sin[dx]) \right) / \\
 & (480d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\
 & \left( \cos[c + dx]^3 \sec[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a + a \sec[c + dx])^2 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\
 & \quad \left. (210A \sin[c] + 180B \sin[c] + 165C \sin[c] + 320A \sin[dx] + 288B \sin[dx] + 256C \sin[dx]) \right) / \\
 & (480d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]))
 \end{aligned}$$

**Problem 418: Result more than twice size of optimal antiderivative.**

$$\int \sec[c + dx]^2 (a + a \sec[c + dx])^2 (A + B \sec[c + dx] + C \sec[c + dx]^2) dx$$

Optimal (type 3, 190 leaves, 8 steps):

$$\frac{a^2 (8A + 7B + 6C) \operatorname{ArcTanh}[\operatorname{Sin}[c + dx]]}{8d} + \frac{a^2 (8A + 7B + 6C) \operatorname{Tan}[c + dx]}{6d} +$$

$$\frac{a^2 (8A + 7B + 6C) \operatorname{Sec}[c + dx] \operatorname{Tan}[c + dx]}{24d} + \frac{(20A - 5B + 6C) (a + a \operatorname{Sec}[c + dx])^2 \operatorname{Tan}[c + dx]}{60d} +$$

$$\frac{C \operatorname{Sec}[c + dx]^2 (a + a \operatorname{Sec}[c + dx])^2 \operatorname{Tan}[c + dx]}{5d} + \frac{(5B + 2C) (a + a \operatorname{Sec}[c + dx])^3 \operatorname{Tan}[c + dx]}{20ad}$$

Result (type 3, 417 leaves):

$$\frac{1}{3840d (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2(c + dx)])}$$

$$a^2 (1 + \operatorname{Cos}[c + dx])^2 (C + B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[c + dx]^2)$$

$$\operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^4 \operatorname{Sec}[c + dx]^5 \left(240(8A + 7B + 6C) \operatorname{Cos}[c + dx]^5 \right.$$

$$\left. \left(\operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right] - \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right]\right) -$$

$$\operatorname{Sec}[c] \left(80(16A + 14B + 15C) \operatorname{Sin}[dx] - 240(3A + 2B + C) \operatorname{Sin}[2c + dx] + \right.$$

$$240A \operatorname{Sin}[c + 2dx] + 330B \operatorname{Sin}[c + 2dx] + 420C \operatorname{Sin}[c + 2dx] + 240A \operatorname{Sin}[3c + 2dx] +$$

$$330B \operatorname{Sin}[3c + 2dx] + 420C \operatorname{Sin}[3c + 2dx] + 880A \operatorname{Sin}[2c + 3dx] + 800B \operatorname{Sin}[2c + 3dx] +$$

$$720C \operatorname{Sin}[2c + 3dx] - 120A \operatorname{Sin}[4c + 3dx] + 120A \operatorname{Sin}[3c + 4dx] + 105B \operatorname{Sin}[3c + 4dx] +$$

$$90C \operatorname{Sin}[3c + 4dx] + 120A \operatorname{Sin}[5c + 4dx] + 105B \operatorname{Sin}[5c + 4dx] + 90C \operatorname{Sin}[5c + 4dx] +$$

$$\left. 200A \operatorname{Sin}[4c + 5dx] + 160B \operatorname{Sin}[4c + 5dx] + 144C \operatorname{Sin}[4c + 5dx]\right)$$

### Problem 419: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[c + dx] (a + a \operatorname{Sec}[c + dx])^2 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) dx$$

Optimal (type 3, 147 leaves, 7 steps):

$$\frac{a^2 (12A + 8B + 7C) \operatorname{ArcTanh}[\operatorname{Sin}[c + dx]]}{8d} +$$

$$\frac{a^2 (12A + 8B + 7C) \operatorname{Tan}[c + dx]}{6d} + \frac{a^2 (12A + 8B + 7C) \operatorname{Sec}[c + dx] \operatorname{Tan}[c + dx]}{24d} +$$

$$\frac{(4B - C) (a + a \operatorname{Sec}[c + dx])^2 \operatorname{Tan}[c + dx]}{12d} + \frac{C (a + a \operatorname{Sec}[c + dx])^3 \operatorname{Tan}[c + dx]}{4ad}$$

Result (type 3, 386 leaves):

1

$$\begin{aligned}
 & 384 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 (c + d x)]) \\
 & a^2 (1 + \cos [c + d x])^2 (C + B \cos [c + d x] + A \cos [c + d x]^2) \\
 & \sec \left[ \frac{1}{2} (c + d x) \right]^4 \sec [c + d x]^4 \left( 24 (12 A + 8 B + 7 C) \cos [c + d x]^4 \right. \\
 & \quad \left. \left( \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] - \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] \right) - \right. \\
 & \quad \sec [c] \left( -24 (6 A + 5 B + 4 C) \sin [c] + 3 (4 A + 8 B + 15 C) \sin [d x] + 12 A \sin [2 c + d x] + \right. \\
 & \quad 24 B \sin [2 c + d x] + 45 C \sin [2 c + d x] + 144 A \sin [c + 2 d x] + 136 B \sin [c + 2 d x] + \\
 & \quad 128 C \sin [c + 2 d x] - 48 A \sin [3 c + 2 d x] - 24 B \sin [3 c + 2 d x] + 12 A \sin [2 c + 3 d x] + \\
 & \quad 24 B \sin [2 c + 3 d x] + 21 C \sin [2 c + 3 d x] + 12 A \sin [4 c + 3 d x] + 24 B \sin [4 c + 3 d x] + \\
 & \quad \left. \left. 21 C \sin [4 c + 3 d x] + 48 A \sin [3 c + 4 d x] + 40 B \sin [3 c + 4 d x] + 32 C \sin [3 c + 4 d x] \right) \right)
 \end{aligned}$$

### Problem 420: Result more than twice size of optimal antiderivative.

$$\int (a + a \sec [c + d x])^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 3, 120 leaves, 6 steps):

$$\begin{aligned}
 & a^2 A x + \frac{a^2 (4 A + 3 B + 2 C) \operatorname{ArcTanh}[\sin [c + d x]]}{2 d} + \frac{a^2 (2 A + 3 B + 2 C) \tan [c + d x]}{2 d} + \\
 & \frac{C (a + a \sec [c + d x])^2 \tan [c + d x]}{3 d} + \frac{(3 B + 2 C) (a^2 + a^2 \sec [c + d x]) \tan [c + d x]}{6 d}
 \end{aligned}$$

Result (type 3, 1307 leaves):

$$\begin{aligned}
 & \left( A x \cos [c + d x]^4 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a + a \sec [c + d x])^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \\
 & \quad (2 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) + \\
 & \quad \left( (-4 A - 3 B - 2 C) \cos [c + d x]^4 \log \left[ \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right] \right. \\
 & \quad \left. \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a + a \sec [c + d x])^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \\
 & \quad (4 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) + \\
 & \quad \left( (4 A + 3 B + 2 C) \cos [c + d x]^4 \log \left[ \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a + a \sec [c + d x])^2 \right. \\
 & \quad \left. (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / (4 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) + \\
 & \quad \left( C \cos [c + d x]^4 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a + a \sec [c + d x])^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \sin \left[ \frac{d x}{2} \right] \right) / \\
 & \quad (12 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) \\
 & \quad \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right)^3 + \\
 & \quad \left( \cos [c + d x]^4 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a + a \sec [c + d x])^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right)
 \end{aligned}$$

$$\begin{aligned}
& \left( 3 B \cos \left[ \frac{c}{2} \right] + 7 C \cos \left[ \frac{c}{2} \right] - 3 B \sin \left[ \frac{c}{2} \right] - 5 C \sin \left[ \frac{c}{2} \right] \right) / \\
& \left( 24 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \right. \\
& \quad \left. \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right)^2 \right) + \\
& \left( \cos [c + d x]^4 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a + a \sec [c + d x])^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
& \quad \left. \left( 3 A \sin \left[ \frac{d x}{2} \right] + 6 B \sin \left[ \frac{d x}{2} \right] + 5 C \sin \left[ \frac{d x}{2} \right] \right) \right) / \\
& \left( 6 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \right. \\
& \quad \left. \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right) \right) + \\
& \left( C \cos [c + d x]^4 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a + a \sec [c + d x])^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \sin \left[ \frac{d x}{2} \right] \right) / \\
& \left( 12 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
& \quad \left. \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right)^3 \right) + \\
& \left( \cos [c + d x]^4 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a + a \sec [c + d x])^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
& \quad \left. \left( -3 B \cos \left[ \frac{c}{2} \right] - 7 C \cos \left[ \frac{c}{2} \right] - 3 B \sin \left[ \frac{c}{2} \right] - 5 C \sin \left[ \frac{c}{2} \right] \right) \right) / \\
& \left( 24 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \right. \\
& \quad \left. \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right)^2 \right) + \\
& \left( \cos [c + d x]^4 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a + a \sec [c + d x])^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
& \quad \left. \left( 3 A \sin \left[ \frac{d x}{2} \right] + 6 B \sin \left[ \frac{d x}{2} \right] + 5 C \sin \left[ \frac{d x}{2} \right] \right) \right) / \\
& \left( 6 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \right. \\
& \quad \left. \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right) \right)
\end{aligned}$$

**Problem 421: Result more than twice size of optimal antiderivative.**

$$\int \cos [c + d x] (a + a \sec [c + d x])^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 3, 121 leaves, 6 steps):



$$a^2 (2A+B) x + \frac{a^2 (2A+4B+3C) \operatorname{ArcTanh}[\sin[c+dx]]}{2d} + \frac{A(a+a \sec[c+dx])^2 \sin[c+dx]}{d} - \frac{a^2 (2A-2B-3C) \tan[c+dx]}{2d} - \frac{(2A-C)(a^2+a^2 \sec[c+dx]) \tan[c+dx]}{2d}$$

Result (type 3, 1091 leaves):

$$\begin{aligned} & \left( (2A+B) x \cos[c+dx]^4 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \sec[c+dx])^2 (A+B \sec[c+dx] + C \sec[c+dx]^2) \right) / \\ & \left( 2(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right) + \\ & \left( (-2A-4B-3C) \cos[c+dx]^4 \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \right. \\ & \left. \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \sec[c+dx])^2 (A+B \sec[c+dx] + C \sec[c+dx]^2) \right) / \\ & \left( 4d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right) + \\ & \left( (2A+4B+3C) \cos[c+dx]^4 \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \sec[c+dx])^2 \right. \\ & \left. (A+B \sec[c+dx] + C \sec[c+dx]^2) \right) / \left( 4d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right) + \\ & \left( A \cos[dx] \cos[c+dx]^4 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \sec[c+dx])^2 (A+B \sec[c+dx] + C \sec[c+dx]^2) \right. \\ & \left. \sin[c] \right) / \left( 2d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right) + \\ & \left( A \cos[c] \cos[c+dx]^4 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \sec[c+dx])^2 (A+B \sec[c+dx] + C \sec[c+dx]^2) \right. \\ & \left. \sin[dx] \right) / \left( 2d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right) + \\ & \left( C \cos[c+dx]^4 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \sec[c+dx])^2 (A+B \sec[c+dx] + C \sec[c+dx]^2) \right) / \\ & \left( 8d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right)^2 \right) + \\ & \left( \cos[c+dx]^4 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \sec[c+dx])^2 (A+B \sec[c+dx] + C \sec[c+dx]^2) \right. \\ & \left. \left( B \sin\left[\frac{dx}{2}\right] + 2C \sin\left[\frac{dx}{2}\right] \right) \right) / \left( 2d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right. \\ & \left. \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right) \right) - \\ & \left( C \cos[c+dx]^4 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \sec[c+dx])^2 (A+B \sec[c+dx] + C \sec[c+dx]^2) \right) / \\ & \left( 8d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right)^2 \right) + \\ & \left( \cos[c+dx]^4 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \sec[c+dx])^2 (A+B \sec[c+dx] + C \sec[c+dx]^2) \right. \\ & \left. \left( B \sin\left[\frac{dx}{2}\right] + 2C \sin\left[\frac{dx}{2}\right] \right) \right) / \left( 2d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right. \\ & \left. \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right) \right) \end{aligned}$$

**Problem 422: Result more than twice size of optimal antiderivative.**

$$\int \cos [c + d x]^2 (a + a \operatorname{Sec} [c + d x])^2 (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) dx$$

Optimal (type 3, 128 leaves, 5 steps):

$$\frac{1}{2} a^2 (3 A + 4 B + 2 C) x + \frac{a^2 (B + 2 C) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{d} + \frac{a^2 (3 A + 2 B - 2 C) \operatorname{Sin}[c + d x]}{2 d} + \frac{A \operatorname{Cos}[c + d x] (a + a \operatorname{Sec}[c + d x])^2 \operatorname{Sin}[c + d x]}{2 d} - \frac{(A - 2 C) (a^2 + a^2 \operatorname{Sec}[c + d x]) \operatorname{Sin}[c + d x]}{2 d}$$

Result (type 3, 1016 leaves):

$$\begin{aligned}
 & a^2 \left( \left( (3A + 4B + 2C) x \cos [c + dx]^2 (1 + \cos [c + dx])^2 \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 \right. \right. \\
 & \quad \left. \left. (A + B \operatorname{Sec} [c + dx] + C \operatorname{Sec} [c + dx]^2) \right) / (4 (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx])) \right) + \\
 & \left( (-B - 2C) \cos [c + dx]^2 (1 + \cos [c + dx])^2 \operatorname{Log} \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] - \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 \right. \\
 & \quad \left. (A + B \operatorname{Sec} [c + dx] + C \operatorname{Sec} [c + dx]^2) \right) / (2d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx])) + \\
 & \left( (B + 2C) \cos [c + dx]^2 (1 + \cos [c + dx])^2 \operatorname{Log} \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] + \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 \right. \\
 & \quad \left. (A + B \operatorname{Sec} [c + dx] + C \operatorname{Sec} [c + dx]^2) \right) / (2d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx])) + \\
 & \left( (2A + B) \cos [dx] \cos [c + dx]^2 (1 + \cos [c + dx])^2 \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 \right. \\
 & \quad \left. (A + B \operatorname{Sec} [c + dx] + C \operatorname{Sec} [c + dx]^2) \sin [c] \right) / \\
 & \quad (2d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx])) + \\
 & \left( A \cos [2dx] \cos [c + dx]^2 (1 + \cos [c + dx])^2 \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 (A + B \operatorname{Sec} [c + dx] + C \operatorname{Sec} [c + dx]^2) \right. \\
 & \quad \left. \sin [2c] \right) / (8d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx])) + \\
 & \left( (2A + B) \cos [c] \cos [c + dx]^2 (1 + \cos [c + dx])^2 \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 \right. \\
 & \quad \left. (A + B \operatorname{Sec} [c + dx] + C \operatorname{Sec} [c + dx]^2) \sin [dx] \right) / \\
 & \quad (2d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx])) + \\
 & \left( A \cos [2c] \cos [c + dx]^2 (1 + \cos [c + dx])^2 \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 (A + B \operatorname{Sec} [c + dx] + C \operatorname{Sec} [c + dx]^2) \right. \\
 & \quad \left. \sin [2dx] \right) / (8d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx])) + \\
 & \left( C \cos [c + dx]^2 (1 + \cos [c + dx])^2 \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 (A + B \operatorname{Sec} [c + dx] + C \operatorname{Sec} [c + dx]^2) \right. \\
 & \quad \left. \sin \left[ \frac{dx}{2} \right] \right) / (2d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx])) \\
 & \quad \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] - \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right) + \\
 & \left( C \cos [c + dx]^2 (1 + \cos [c + dx])^2 \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 (A + B \operatorname{Sec} [c + dx] + C \operatorname{Sec} [c + dx]^2) \right. \\
 & \quad \left. \sin \left[ \frac{dx}{2} \right] \right) / (2d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx])) \\
 & \quad \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] + \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right)
 \end{aligned}$$

**Problem 427: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec} [c + dx]^3 (a + a \operatorname{Sec} [c + dx])^3 (A + B \operatorname{Sec} [c + dx] + C \operatorname{Sec} [c + dx]^2) dx$$

Optimal (type 3, 274 leaves, 9 steps):

$$\begin{aligned}
 & \frac{a^3 (26 A + 23 B + 21 C) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{16 d} + \\
 & \frac{a^3 (133 A + 119 B + 108 C) \operatorname{Tan}[c + d x]}{35 d} + \frac{a^3 (26 A + 23 B + 21 C) \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x]}{16 d} + \\
 & \frac{a^3 (154 A + 147 B + 129 C) \operatorname{Sec}[c + d x]^3 \operatorname{Tan}[c + d x]}{280 d} + \\
 & \frac{C \operatorname{Sec}[c + d x]^3 (a + a \operatorname{Sec}[c + d x])^3 \operatorname{Tan}[c + d x]}{7 d} + \\
 & \frac{(7 B + 3 C) \operatorname{Sec}[c + d x]^3 (a^2 + a^2 \operatorname{Sec}[c + d x])^2 \operatorname{Tan}[c + d x]}{42 a d} + \\
 & \frac{(3 A + 4 B + 3 C) \operatorname{Sec}[c + d x]^3 (a^3 + a^3 \operatorname{Sec}[c + d x]) \operatorname{Tan}[c + d x]}{15 d} + \\
 & \frac{a^3 (133 A + 119 B + 108 C) \operatorname{Tan}[c + d x]^3}{105 d}
 \end{aligned}$$

Result (type 3, 1087 leaves):

$$\begin{aligned}
 & \left( (-26A - 23B - 21C) \cos[c + dx]^5 \operatorname{Log}\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \right. \\
 & \quad \left. \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right) / \\
 & (64d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\
 & \left( (26A + 23B + 21C) \cos[c + dx]^5 \operatorname{Log}\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \right. \\
 & \quad \left. \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right) / \\
 & (64d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\
 & \left( C \sec[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sec[c + dx]^2 (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\
 & \quad \left. \sin[dx] \right) / (28d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\
 & \left( \sec[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sec[c + dx] (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\
 & \quad \left. (6C \sin[c] + 7B \sin[dx] + 21C \sin[dx]) \right) / \\
 & (168d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\
 & \left( \sec[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\
 & \quad \left. (35B \sin[c] + 105C \sin[c] + 42A \sin[dx] + 126B \sin[dx] + 162C \sin[dx]) \right) / \\
 & (840d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\
 & \left( \cos[c + dx] \sec[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\
 & \quad \left. (168A \sin[c] + 504B \sin[c] + 648C \sin[c] + 630A \sin[dx] + 805B \sin[dx] + 735C \sin[dx]) \right) / \\
 & (3360d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\
 & \left( \cos[c + dx]^2 \sec[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\
 & \quad \left. (630A \sin[c] + 805B \sin[c] + 735C \sin[c] + 1064A \sin[dx] + 952B \sin[dx] + \right. \\
 & \quad \left. 864C \sin[dx]) \right) / (3360d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\
 & \left( \cos[c + dx]^3 \sec[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\
 & \quad \left. (2128A \sin[c] + 1904B \sin[c] + 1728C \sin[c] + 2730A \sin[dx] + 2415B \sin[dx] + \right. \\
 & \quad \left. 2205C \sin[dx]) \right) / (6720d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\
 & \left( \cos[c + dx]^4 \sec[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\
 & \quad \left. (2730A \sin[c] + 2415B \sin[c] + 2205C \sin[c] + 4256A \sin[dx] + 3808B \sin[dx] + \right. \\
 & \quad \left. 3456C \sin[dx]) \right) / (6720d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]))
 \end{aligned}$$

**Problem 428: Result more than twice size of optimal antiderivative.**

$$\int \text{Sec}[c + d x]^2 (a + a \text{Sec}[c + d x])^3 (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) dx$$

Optimal (type 3, 216 leaves, 12 steps):

$$\begin{aligned} & \frac{a^3 (30 A + 26 B + 23 C) \text{ArcTanh}[\text{Sin}[c + d x]]}{16 d} + \\ & \frac{a^3 (30 A + 26 B + 23 C) \text{Tan}[c + d x]}{10 d} + \frac{3 a^3 (30 A + 26 B + 23 C) \text{Sec}[c + d x] \text{Tan}[c + d x]}{80 d} + \\ & \frac{(30 A - 6 B + 7 C) (a + a \text{Sec}[c + d x])^3 \text{Tan}[c + d x]}{120 d} + \\ & \frac{C \text{Sec}[c + d x]^2 (a + a \text{Sec}[c + d x])^3 \text{Tan}[c + d x]}{6 d} + \\ & \frac{(2 B + C) (a + a \text{Sec}[c + d x])^4 \text{Tan}[c + d x]}{10 a d} + \frac{a^3 (30 A + 26 B + 23 C) \text{Tan}[c + d x]^3}{120 d} \end{aligned}$$

Result (type 3, 959 leaves):

$$\begin{aligned}
 & \left( (-30A - 26B - 23C) \cos[c + dx]^5 \operatorname{Log}\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \right. \\
 & \quad \left. \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right) / \\
 & (64d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\
 & \left( (30A + 26B + 23C) \cos[c + dx]^5 \operatorname{Log}\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \right. \\
 & \quad \left. \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right) / \\
 & (64d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\
 & \left( C \sec[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sec[c + dx] (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\
 & \quad \left. \sin[dx] \right) / (24d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\
 & \left( \sec[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\
 & \quad \left. (5C \sin[c] + 6B \sin[dx] + 18C \sin[dx]) \right) / \\
 & (120d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\
 & \left( \cos[c + dx] \sec[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\
 & \quad \left. (24B \sin[c] + 72C \sin[c] + 30A \sin[dx] + 90B \sin[dx] + 115C \sin[dx]) \right) / \\
 & (480d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\
 & \left( \cos[c + dx]^2 \sec[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\
 & \quad \left. (30A \sin[c] + 90B \sin[c] + 115C \sin[c] + 120A \sin[dx] + 152B \sin[dx] + 136C \sin[dx]) \right) / \\
 & (480d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\
 & \left( \cos[c + dx]^3 \sec[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\
 & \quad \left. (240A \sin[c] + 304B \sin[c] + 272C \sin[c] + 450A \sin[dx] + 390B \sin[dx] + 345C \sin[dx]) \right) / \\
 & (960d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\
 & \left( \cos[c + dx]^4 \sec[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\
 & \quad \left. (450A \sin[c] + 390B \sin[c] + 345C \sin[c] + 720A \sin[dx] + 608B \sin[dx] + 544C \sin[dx]) \right) / \\
 & (960d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]))
 \end{aligned}$$

**Problem 429: Result more than twice size of optimal antiderivative.**

$$\int \sec[c + dx] (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) dx$$

Optimal (type 3, 175 leaves, 11 steps):

$$\frac{a^3 (20A + 15B + 13C) \operatorname{ArcTanh}[\operatorname{Sin}[c + dx]]}{8d} + \frac{a^3 (20A + 15B + 13C) \operatorname{Tan}[c + dx]}{5d} +$$

$$\frac{3a^3 (20A + 15B + 13C) \operatorname{Sec}[c + dx] \operatorname{Tan}[c + dx]}{40d} + \frac{(5B - C) (a + a \operatorname{Sec}[c + dx])^3 \operatorname{Tan}[c + dx]}{20d} +$$

$$\frac{C (a + a \operatorname{Sec}[c + dx])^4 \operatorname{Tan}[c + dx]}{5ad} + \frac{a^3 (20A + 15B + 13C) \operatorname{Tan}[c + dx]^3}{60d}$$

Result (type 3, 629 leaves):

$$\left( (-20A - 15B - 13C) \operatorname{Cos}[c + dx]^5 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] - \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \right. \\ \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \operatorname{Sec}[c + dx])^3 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right) / \\ (32d (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx])) +$$

$$\left( (20A + 15B + 13C) \operatorname{Cos}[c + dx]^5 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \right. \\ \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \operatorname{Sec}[c + dx])^3 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right) / \\ (32d (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx])) +$$

$$\frac{1}{7680d (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx])}$$

$$\operatorname{Sec}[c] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \operatorname{Sec}[c + dx])^3 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \\ (2720A \operatorname{Sin}[dx] + 2400B \operatorname{Sin}[dx] + 2320C \operatorname{Sin}[dx] - 1680A \operatorname{Sin}[2c + dx] - \\ 1200B \operatorname{Sin}[2c + dx] - 720C \operatorname{Sin}[2c + dx] + 360A \operatorname{Sin}[c + 2dx] + 570B \operatorname{Sin}[c + 2dx] + \\ 750C \operatorname{Sin}[c + 2dx] + 360A \operatorname{Sin}[3c + 2dx] + 570B \operatorname{Sin}[3c + 2dx] + 750C \operatorname{Sin}[3c + 2dx] + \\ 1840A \operatorname{Sin}[2c + 3dx] + 1680B \operatorname{Sin}[2c + 3dx] + 1520C \operatorname{Sin}[2c + 3dx] - \\ 360A \operatorname{Sin}[4c + 3dx] - 120B \operatorname{Sin}[4c + 3dx] + 180A \operatorname{Sin}[3c + 4dx] + \\ 225B \operatorname{Sin}[3c + 4dx] + 195C \operatorname{Sin}[3c + 4dx] + 180A \operatorname{Sin}[5c + 4dx] + 225B \operatorname{Sin}[5c + 4dx] + \\ 195C \operatorname{Sin}[5c + 4dx] + 440A \operatorname{Sin}[4c + 5dx] + 360B \operatorname{Sin}[4c + 5dx] + 304C \operatorname{Sin}[4c + 5dx])$$

**Problem 430: Result more than twice size of optimal antiderivative.**

$$\int (a + a \operatorname{Sec}[c + dx])^3 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) dx$$

Optimal (type 3, 162 leaves, 7 steps):

$$a^3 Ax + \frac{a^3 (28A + 20B + 15C) \operatorname{ArcTanh}[\operatorname{Sin}[c + dx]]}{8d} + \frac{5a^3 (4A + 4B + 3C) \operatorname{Tan}[c + dx]}{8d} +$$

$$\frac{C (a + a \operatorname{Sec}[c + dx])^3 \operatorname{Tan}[c + dx]}{4d} + \frac{(4B + 3C) (a^2 + a^2 \operatorname{Sec}[c + dx])^2 \operatorname{Tan}[c + dx]}{12ad} +$$

$$\frac{(12A + 20B + 15C) (a^3 + a^3 \operatorname{Sec}[c + dx]) \operatorname{Tan}[c + dx]}{24d}$$

Result (type 3, 464 leaves):



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$$\begin{aligned}
 & 768 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 (c + d x)]) \\
 & a^3 (1 + \cos [c + d x])^3 (C + B \cos [c + d x] + A \cos [c + d x]^2) \\
 & \sec \left[ \frac{1}{2} (c + d x) \right]^6 \sec [c + d x]^4 \left( -24 (28 A + 20 B + 15 C) \cos [c + d x]^4 \right. \\
 & \quad \left. \left( \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] - \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] \right) + \right. \\
 & \quad \left. \sec [c] (72 A d x \cos [c] + 48 A d x \cos [c + 2 d x] + 48 A d x \cos [3 c + 2 d x] + 12 A d x \right. \\
 & \quad \quad \cos [3 c + 4 d x] + 12 A d x \cos [5 c + 4 d x] - 216 A \sin [c] - 264 B \sin [c] - 216 C \sin [c] + \\
 & \quad \quad 12 A \sin [d x] + 36 B \sin [d x] + 69 C \sin [d x] + 12 A \sin [2 c + d x] + 36 B \sin [2 c + d x] + \\
 & \quad \quad 69 C \sin [2 c + d x] + 216 A \sin [c + 2 d x] + 280 B \sin [c + 2 d x] + 264 C \sin [c + 2 d x] - \\
 & \quad \quad 72 A \sin [3 c + 2 d x] - 72 B \sin [3 c + 2 d x] - 24 C \sin [3 c + 2 d x] + 12 A \sin [2 c + 3 d x] + \\
 & \quad \quad 36 B \sin [2 c + 3 d x] + 45 C \sin [2 c + 3 d x] + 12 A \sin [4 c + 3 d x] + 36 B \sin [4 c + 3 d x] + \\
 & \quad \quad \left. \left. 45 C \sin [4 c + 3 d x] + 72 A \sin [3 c + 4 d x] + 88 B \sin [3 c + 4 d x] + 72 C \sin [3 c + 4 d x] \right) \right)
 \end{aligned}$$

### Problem 431: Result more than twice size of optimal antiderivative.

$$\int \cos [c + d x] (a + a \sec [c + d x])^3 (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 3, 156 leaves, 7 steps):

$$\begin{aligned}
 & a^3 (3 A + B) x + \frac{a^3 (6 A + 7 B + 5 C) \operatorname{ArcTanh}[\sin [c + d x]]}{2 d} + \\
 & \frac{A (a + a \sec [c + d x])^3 \sin [c + d x]}{d} + \frac{5 a^3 (B + C) \tan [c + d x]}{2 d} - \\
 & \frac{(3 A - C) (a^2 + a^2 \sec [c + d x])^2 \tan [c + d x]}{3 a d} - \frac{(6 A - 3 B - 5 C) (a^3 + a^3 \sec [c + d x]) \tan [c + d x]}{6 d}
 \end{aligned}$$

Result (type 3, 1503 leaves):

$$\begin{aligned}
 & \left( (3 A + B) x \cos [c + d x]^5 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 (a + a \sec [c + d x])^3 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \\
 & (4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) + \\
 & \left( (-6 A - 7 B - 5 C) \cos [c + d x]^5 \log \left[ \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right] \right. \\
 & \quad \left. \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 (a + a \sec [c + d x])^3 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \\
 & (8 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) + \\
 & \left( (6 A + 7 B + 5 C) \cos [c + d x]^5 \log \left[ \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 (a + a \sec [c + d x])^3 \right. \\
 & \quad \left. (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / (8 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) + \\
 & \left( A \cos [d x] \cos [c + d x]^5 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 (a + a \sec [c + d x])^3 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left. \sin [c] \right) / (4 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) +
 \end{aligned}$$

$$\begin{aligned}
& \left( A \cos [c] \cos [c+d x]^5 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 (a+a \sec [c+d x])^3 (A+B \sec [c+d x]+C \sec [c+d x]^2) \right. \\
& \quad \left. \sin [d x] \right) / \left( 4 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right) + \\
& \left( C \cos [c+d x]^5 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 (a+a \sec [c+d x])^3 (A+B \sec [c+d x]+C \sec [c+d x]^2) \sin \left[ \frac{d x}{2} \right] \right) / \\
& \left( 24 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right. \\
& \quad \left. \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right)^3 \right) + \\
& \left( \cos [c+d x]^5 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 (a+a \sec [c+d x])^3 (A+B \sec [c+d x]+C \sec [c+d x]^2) \right. \\
& \quad \left. \left( 3 B \cos \left[ \frac{c}{2} \right] + 10 C \cos \left[ \frac{c}{2} \right] - 3 B \sin \left[ \frac{c}{2} \right] - 8 C \sin \left[ \frac{c}{2} \right] \right) \right) / \\
& \left( 48 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \right. \\
& \quad \left. \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right)^2 \right) + \\
& \left( \cos [c+d x]^5 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 (a+a \sec [c+d x])^3 (A+B \sec [c+d x]+C \sec [c+d x]^2) \right. \\
& \quad \left. \left( 3 A \sin \left[ \frac{d x}{2} \right] + 9 B \sin \left[ \frac{d x}{2} \right] + 11 C \sin \left[ \frac{d x}{2} \right] \right) \right) / \\
& \left( 12 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \right. \\
& \quad \left. \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right) \right) + \\
& \left( C \cos [c+d x]^5 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 (a+a \sec [c+d x])^3 (A+B \sec [c+d x]+C \sec [c+d x]^2) \sin \left[ \frac{d x}{2} \right] \right) / \\
& \left( 24 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right. \\
& \quad \left. \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right)^3 \right) + \\
& \left( \cos [c+d x]^5 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 (a+a \sec [c+d x])^3 (A+B \sec [c+d x]+C \sec [c+d x]^2) \right. \\
& \quad \left. \left( -3 B \cos \left[ \frac{c}{2} \right] - 10 C \cos \left[ \frac{c}{2} \right] - 3 B \sin \left[ \frac{c}{2} \right] - 8 C \sin \left[ \frac{c}{2} \right] \right) \right) / \\
& \left( 48 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \right. \\
& \quad \left. \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right)^2 \right) + \\
& \left( \cos [c+d x]^5 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 (a+a \sec [c+d x])^3 (A+B \sec [c+d x]+C \sec [c+d x]^2) \right. \\
& \quad \left. \left( 3 A \sin \left[ \frac{d x}{2} \right] + 9 B \sin \left[ \frac{d x}{2} \right] + 11 C \sin \left[ \frac{d x}{2} \right] \right) \right) / \\
& \left( 12 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \right)
\end{aligned}$$

$$\left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right)$$

### Problem 432: Result more than twice size of optimal antiderivative.

$$\int \cos[c + dx]^2 (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) dx$$

Optimal (type 3, 171 leaves, 6 steps):

$$\begin{aligned} & \frac{1}{2} a^3 (7A + 6B + 2C) x + \frac{a^3 (2A + 6B + 7C) \operatorname{ArcTanh}[\sin[c + dx]]}{2d} + \\ & \frac{5a^3 (A - C) \sin[c + dx]}{2d} + \frac{A \cos[c + dx] (a + a \sec[c + dx])^3 \sin[c + dx]}{2d} - \\ & \frac{(A - C) (a^2 + a^2 \sec[c + dx])^2 \sin[c + dx]}{2ad} - \frac{(A - 2B - 4C) (a^3 + a^3 \sec[c + dx]) \sin[c + dx]}{2d} \end{aligned}$$

Result (type 3, 1302 leaves):

$$\begin{aligned} & \left( (7A + 6B + 2C) x \cos[c + dx]^5 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 \right. \\ & \quad \left. (A + B \sec[c + dx] + C \sec[c + dx]^2) \right) / (8(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\ & \left( (-2A - 6B - 7C) \cos[c + dx]^5 \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \right. \\ & \quad \left. (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right) / \\ & \quad (8d(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\ & \left( (2A + 6B + 7C) \cos[c + dx]^5 \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 \right. \\ & \quad \left. (A + B \sec[c + dx] + C \sec[c + dx]^2) \right) / (8d(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\ & \left( (3A + B) \cos[dx] \cos[c + dx]^5 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 \right. \\ & \quad \left. (A + B \sec[c + dx] + C \sec[c + dx]^2) \sin[c] \right) / \\ & \quad (4d(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\ & \left( A \cos[2dx] \cos[c + dx]^5 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\ & \quad \left. \sin[2c] \right) / (16d(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\ & \left( (3A + B) \cos[c] \cos[c + dx]^5 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 \right. \\ & \quad \left. (A + B \sec[c + dx] + C \sec[c + dx]^2) \sin[dx] \right) / \\ & \quad (4d(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\ & \left( A \cos[2c] \cos[c + dx]^5 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \end{aligned}$$

$$\begin{aligned}
 & \left. \sin[2dx] \right) / \left( 16d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \right) + \\
 & \left( C \cos[c + dx]^5 \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \operatorname{Sec}[c + dx])^3 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right) / \\
 & \left( 16d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right)^2 \right) + \\
 & \left( \cos[c + dx]^5 \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \operatorname{Sec}[c + dx])^3 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right. \\
 & \quad \left. \left( B \sin\left[\frac{dx}{2}\right] + 3C \sin\left[\frac{dx}{2}\right] \right) \right) / \left( 4d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \right. \\
 & \quad \left. \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right) \right) - \\
 & \left( C \cos[c + dx]^5 \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \operatorname{Sec}[c + dx])^3 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right) / \\
 & \left( 16d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right)^2 \right) + \\
 & \left( \cos[c + dx]^5 \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \operatorname{Sec}[c + dx])^3 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right. \\
 & \quad \left. \left( B \sin\left[\frac{dx}{2}\right] + 3C \sin\left[\frac{dx}{2}\right] \right) \right) / \left( 4d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \right. \\
 & \quad \left. \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right) \right)
 \end{aligned}$$

**Problem 433: Result more than twice size of optimal antiderivative.**

$$\int \cos[c + dx]^3 (a + a \operatorname{Sec}[c + dx])^3 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) dx$$

Optimal (type 3, 169 leaves, 6 steps):

$$\begin{aligned}
 & \frac{1}{2} a^3 (5A + 7B + 6C) x + \frac{a^3 (B + 3C) \operatorname{ArcTanh}[\sin[c + dx]]}{d} + \\
 & \frac{5 a^3 (A + B) \sin[c + dx]}{2d} + \frac{A \cos[c + dx]^2 (a + a \operatorname{Sec}[c + dx])^3 \sin[c + dx]}{3d} + \\
 & \frac{(A + B) \cos[c + dx] (a^2 + a^2 \operatorname{Sec}[c + dx])^2 \sin[c + dx]}{2ad} - \\
 & \frac{(5A + 3B - 6C) (a^3 + a^3 \operatorname{Sec}[c + dx]) \sin[c + dx]}{6d}
 \end{aligned}$$

Result (type 3, 379 leaves):

$$\frac{1}{48 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 (c + d x)])} \\
 a^3 \cos [c + d x]^2 (1 + \cos [c + d x])^3 \sec \left[ \frac{1}{2} (c + d x) \right]^6 (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 \left( 6 (5 A + 7 B + 6 C) x - \frac{12 (B + 3 C) \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right]}{d} + \right. \\
 \frac{12 (B + 3 C) \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right]}{d} + \frac{3 (15 A + 4 (3 B + C)) \cos [d x] \sin [c]}{d} + \\
 \frac{3 (3 A + B) \cos [2 d x] \sin [2 c]}{d} + \frac{A \cos [3 d x] \sin [3 c]}{d} + \\
 \frac{3 (15 A + 4 (3 B + C)) \cos [c] \sin [d x]}{d} + \frac{3 (3 A + B) \cos [2 c] \sin [2 d x]}{d} + \\
 \frac{A \cos [3 c] \sin [3 d x]}{d} + \frac{12 C \sin \left[ \frac{d x}{2} \right]}{d \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)} + \\
 \left. \frac{12 C \sin \left[ \frac{d x}{2} \right]}{d \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)} \right)$$

**Problem 438: Result more than twice size of optimal antiderivative.**

$$\int \sec [c + d x]^2 (a + a \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 3, 252 leaves, 15 steps):

$$\frac{a^4 (56 A + 49 B + 44 C) \operatorname{ArcTanh} [\sin [c + d x]]}{16 d} + \frac{4 a^4 (56 A + 49 B + 44 C) \tan [c + d x]}{35 d} + \\
 \frac{27 a^4 (56 A + 49 B + 44 C) \sec [c + d x] \tan [c + d x]}{560 d} + \frac{a^4 (56 A + 49 B + 44 C) \sec [c + d x]^3 \tan [c + d x]}{280 d} + \\
 \frac{(42 A - 7 B + 8 C) (a + a \sec [c + d x])^4 \tan [c + d x]}{210 d} + \\
 \frac{C \sec [c + d x]^2 (a + a \sec [c + d x])^4 \tan [c + d x]}{7 d} + \\
 \frac{(7 B + 4 C) (a + a \sec [c + d x])^5 \tan [c + d x]}{42 a d} + \frac{2 a^4 (56 A + 49 B + 44 C) \tan [c + d x]^3}{105 d}$$

Result (type 3, 1087 leaves):

$$\begin{aligned}
& \left( (-56A - 49B - 44C) \cos[c + dx]^6 \operatorname{Log}\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \right. \\
& \quad \left. \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \sec[c + dx])^4 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right) / \\
& (128d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\
& \left( (56A + 49B + 44C) \cos[c + dx]^6 \operatorname{Log}\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \right. \\
& \quad \left. \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \sec[c + dx])^4 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right) / \\
& (128d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\
& \left( C \sec[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^8 \sec[c + dx] (a + a \sec[c + dx])^4 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\
& \quad \left. \sin[dx] \right) / (56d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\
& \left( \sec[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \sec[c + dx])^4 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\
& \quad \left. (6C \sin[c] + 7B \sin[dx] + 28C \sin[dx]) \right) / \\
& (336d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\
& \left( \cos[c + dx] \sec[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \sec[c + dx])^4 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\
& \quad \left. (35B \sin[c] + 140C \sin[c] + 42A \sin[dx] + 168B \sin[dx] + 288C \sin[dx]) \right) / \\
& (1680d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\
& \left( \cos[c + dx]^2 \sec[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \sec[c + dx])^4 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\
& \quad \left. (168A \sin[c] + 672B \sin[c] + 1152C \sin[c] + 840A \sin[dx] + 1435B \sin[dx] + \right. \\
& \quad \left. 1540C \sin[dx]) \right) / (6720d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\
& \left( \cos[c + dx]^3 \sec[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \sec[c + dx])^4 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\
& \quad \left. (840A \sin[c] + 1435B \sin[c] + 1540C \sin[c] + 1904A \sin[dx] + 2016B \sin[dx] + \right. \\
& \quad \left. 1816C \sin[dx]) \right) / (6720d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\
& \left( \cos[c + dx]^4 \sec[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \sec[c + dx])^4 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\
& \quad \left. (3808A \sin[c] + 4032B \sin[c] + 3632C \sin[c] + 5880A \sin[dx] + 5145B \sin[dx] + \right. \\
& \quad \left. 4620C \sin[dx]) \right) / (13440d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\
& \left( \cos[c + dx]^5 \sec[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \sec[c + dx])^4 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\
& \quad \left. (5880A \sin[c] + 5145B \sin[c] + 4620C \sin[c] + 9296A \sin[dx] + 8064B \sin[dx] + \right. \\
& \quad \left. 7264C \sin[dx]) \right) / (13440d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]))
\end{aligned}$$

**Problem 439: Result more than twice size of optimal antiderivative.**

$$\int \text{Sec}[c + d x] (a + a \text{Sec}[c + d x])^4 (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) dx$$

Optimal (type 3, 209 leaves, 14 steps):

$$\begin{aligned} & \frac{7 a^4 (10 A + 8 B + 7 C) \text{ArcTanh}[\text{Sin}[c + d x]]}{16 d} + \\ & \frac{4 a^4 (10 A + 8 B + 7 C) \text{Tan}[c + d x]}{5 d} + \frac{27 a^4 (10 A + 8 B + 7 C) \text{Sec}[c + d x] \text{Tan}[c + d x]}{80 d} + \\ & \frac{a^4 (10 A + 8 B + 7 C) \text{Sec}[c + d x]^3 \text{Tan}[c + d x]}{40 d} + \frac{(6 B - C) (a + a \text{Sec}[c + d x])^4 \text{Tan}[c + d x]}{30 d} + \\ & \frac{C (a + a \text{Sec}[c + d x])^5 \text{Tan}[c + d x]}{6 a d} + \frac{2 a^4 (10 A + 8 B + 7 C) \text{Tan}[c + d x]^3}{15 d} \end{aligned}$$

Result (type 3, 961 leaves):

$$\begin{aligned}
& - \left( \left( 7 (10A + 8B + 7C) \cos [c + dx]^6 \log \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] - \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right] \right. \right. \\
& \quad \left. \left. \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^8 (a + a \sec [c + dx])^4 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) \right) / \\
& \quad (128d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx])) + \\
& \left( 7 (10A + 8B + 7C) \cos [c + dx]^6 \log \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] + \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right] \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^8 \right. \\
& \quad \left. (a + a \sec [c + dx])^4 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) / \\
& \quad (128d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx])) + \\
& \left( C \sec [c] \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^8 (a + a \sec [c + dx])^4 (A + B \sec [c + dx] + C \sec [c + dx]^2) \sin [dx] \right) / \\
& \quad (48d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx])) + \\
& \left( \cos [c + dx] \sec [c] \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^8 (a + a \sec [c + dx])^4 \right. \\
& \quad \left. (A + B \sec [c + dx] + C \sec [c + dx]^2) (5C \sin [c] + 6B \sin [dx] + 24C \sin [dx]) \right) / \\
& \quad (240d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx])) + \\
& \left( \cos [c + dx]^2 \sec [c] \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^8 (a + a \sec [c + dx])^4 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right. \\
& \quad \left. (24B \sin [c] + 96C \sin [c] + 30A \sin [dx] + 120B \sin [dx] + 205C \sin [dx]) \right) / \\
& \quad (960d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx])) + \\
& \left( \cos [c + dx]^3 \sec [c] \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^8 (a + a \sec [c + dx])^4 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right. \\
& \quad \left. (30A \sin [c] + 120B \sin [c] + 205C \sin [c] + 160A \sin [dx] + 272B \sin [dx] + 288C \sin [dx]) \right) / \\
& \quad (960d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx])) + \\
& \left( \cos [c + dx]^4 \sec [c] \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^8 (a + a \sec [c + dx])^4 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right. \\
& \quad \left. (320A \sin [c] + 544B \sin [c] + 576C \sin [c] + 810A \sin [dx] + 840B \sin [dx] + 735C \sin [dx]) \right) / \\
& \quad (1920d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx])) + \\
& \left( \cos [c + dx]^5 \sec [c] \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^8 (a + a \sec [c + dx])^4 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right. \\
& \quad \left. (810A \sin [c] + 840B \sin [c] + 735C \sin [c] + 1600A \sin [dx] + 1328B \sin [dx] + \right. \\
& \quad \left. 1152C \sin [dx]) \right) / (1920d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]))
\end{aligned}$$

**Problem 440: Result more than twice size of optimal antiderivative.**

$$\int (a + a \sec [c + dx])^4 (A + B \sec [c + dx] + C \sec [c + dx]^2) dx$$

Optimal (type 3, 195 leaves, 8 steps):



$$\begin{aligned}
 & a^4 A x + \frac{a^4 (48 A + 35 B + 28 C) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{8 d} + \\
 & \frac{a^4 (40 A + 35 B + 28 C) \operatorname{Tan}[c + d x]}{8 d} + \frac{a (5 B + 4 C) (a + a \operatorname{Sec}[c + d x])^3 \operatorname{Tan}[c + d x]}{20 d} + \\
 & \frac{C (a + a \operatorname{Sec}[c + d x])^4 \operatorname{Tan}[c + d x]}{5 d} + \frac{(20 A + 35 B + 28 C) (a^2 + a^2 \operatorname{Sec}[c + d x])^2 \operatorname{Tan}[c + d x]}{60 d} + \\
 & \frac{(32 A + 35 B + 28 C) (a^4 + a^4 \operatorname{Sec}[c + d x]) \operatorname{Tan}[c + d x]}{24 d}
 \end{aligned}$$

Result (type 3, 725 leaves):

$$\begin{aligned}
 & \left( (-48 A - 35 B - 28 C) \operatorname{Cos}[c + d x]^6 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right] - \operatorname{Sin}\left[\frac{c}{2} + \frac{d x}{2}\right]\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^8 (a + a \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) / \\
 & (64 d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x])) + \\
 & \left( (48 A + 35 B + 28 C) \operatorname{Cos}[c + d x]^6 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{d x}{2}\right]\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^8 (a + a \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) / \\
 & (64 d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x])) + \\
 & \frac{1}{15360 d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x])} \\
 & \operatorname{Cos}[c + d x] \operatorname{Sec}[c] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^8 (a + a \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\
 & (600 A d x \operatorname{Cos}[d x] + 600 A d x \operatorname{Cos}[2 c + d x] + 300 A d x \operatorname{Cos}[2 c + 3 d x] + \\
 & 300 A d x \operatorname{Cos}[4 c + 3 d x] + 60 A d x \operatorname{Cos}[4 c + 5 d x] + 60 A d x \operatorname{Cos}[6 c + 5 d x] + \\
 & 4880 A \operatorname{Sin}[d x] + 5120 B \operatorname{Sin}[d x] + 4720 C \operatorname{Sin}[d x] - 3120 A \operatorname{Sin}[2 c + d x] - \\
 & 2880 B \operatorname{Sin}[2 c + d x] - 1920 C \operatorname{Sin}[2 c + d x] + 480 A \operatorname{Sin}[c + 2 d x] + 930 B \operatorname{Sin}[c + 2 d x] + \\
 & 1320 C \operatorname{Sin}[c + 2 d x] + 480 A \operatorname{Sin}[3 c + 2 d x] + 930 B \operatorname{Sin}[3 c + 2 d x] + 1320 C \operatorname{Sin}[3 c + 2 d x] + \\
 & 3280 A \operatorname{Sin}[2 c + 3 d x] + 3520 B \operatorname{Sin}[2 c + 3 d x] + 3200 C \operatorname{Sin}[2 c + 3 d x] - \\
 & 720 A \operatorname{Sin}[4 c + 3 d x] - 480 B \operatorname{Sin}[4 c + 3 d x] - 120 C \operatorname{Sin}[4 c + 3 d x] + 240 A \operatorname{Sin}[3 c + 4 d x] + \\
 & 405 B \operatorname{Sin}[3 c + 4 d x] + 420 C \operatorname{Sin}[3 c + 4 d x] + 240 A \operatorname{Sin}[5 c + 4 d x] + 405 B \operatorname{Sin}[5 c + 4 d x] + \\
 & 420 C \operatorname{Sin}[5 c + 4 d x] + 800 A \operatorname{Sin}[4 c + 5 d x] + 800 B \operatorname{Sin}[4 c + 5 d x] + 664 C \operatorname{Sin}[4 c + 5 d x])
 \end{aligned}$$

**Problem 441: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Cos}[c + d x] (a + a \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 3, 196 leaves, 8 steps):

$$\begin{aligned}
 & a^4 (4A + B) x + \frac{a^4 (52A + 48B + 35C) \operatorname{ArcTanh}[\operatorname{Sin}[c + dx]]}{8d} + \\
 & \frac{A (a + a \operatorname{Sec}[c + dx])^4 \operatorname{Sin}[c + dx]}{d} + \frac{5a^4 (4A + 8B + 7C) \operatorname{Tan}[c + dx]}{8d} - \\
 & \frac{a (4A - C) (a + a \operatorname{Sec}[c + dx])^3 \operatorname{Tan}[c + dx]}{4d} - \frac{(12A - 4B - 7C) (a^2 + a^2 \operatorname{Sec}[c + dx])^2 \operatorname{Tan}[c + dx]}{12d} - \\
 & \frac{(12A - 32B - 35C) (a^4 + a^4 \operatorname{Sec}[c + dx]) \operatorname{Tan}[c + dx]}{24d}
 \end{aligned}$$

Result (type 3, 738 leaves):

$$\begin{aligned}
 & \left( (-52A - 48B - 35C) \operatorname{Cos}[c + dx]^6 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] - \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \operatorname{Sec}[c + dx])^4 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right) / \\
 & (64d (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx])) + \\
 & \left( (52A + 48B + 35C) \operatorname{Cos}[c + dx]^6 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \operatorname{Sec}[c + dx])^4 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right) / \\
 & (64d (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx])) + \\
 & \frac{1}{1536d (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx])} \\
 & \operatorname{Cos}[c + dx]^2 \operatorname{Sec}[c] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \operatorname{Sec}[c + dx])^4 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \\
 & (288A dx \operatorname{Cos}[c] + 72B dx \operatorname{Cos}[c] + 192A dx \operatorname{Cos}[c + 2dx] + 48B dx \operatorname{Cos}[c + 2dx] + \\
 & 192A dx \operatorname{Cos}[3c + 2dx] + 48B dx \operatorname{Cos}[3c + 2dx] + 48A dx \operatorname{Cos}[3c + 4dx] + \\
 & 12B dx \operatorname{Cos}[3c + 4dx] + 48A dx \operatorname{Cos}[5c + 4dx] + 12B dx \operatorname{Cos}[5c + 4dx] - 288A \operatorname{Sin}[c] - \\
 & 480B \operatorname{Sin}[c] - 480C \operatorname{Sin}[c] + 24A \operatorname{Sin}[dx] + 48B \operatorname{Sin}[dx] + 105C \operatorname{Sin}[dx] + \\
 & 24A \operatorname{Sin}[2c + dx] + 48B \operatorname{Sin}[2c + dx] + 105C \operatorname{Sin}[2c + dx] + 288A \operatorname{Sin}[c + 2dx] + \\
 & 496B \operatorname{Sin}[c + 2dx] + 544C \operatorname{Sin}[c + 2dx] - 96A \operatorname{Sin}[3c + 2dx] - 144B \operatorname{Sin}[3c + 2dx] - \\
 & 96C \operatorname{Sin}[3c + 2dx] + 30A \operatorname{Sin}[2c + 3dx] + 48B \operatorname{Sin}[2c + 3dx] + 81C \operatorname{Sin}[2c + 3dx] + \\
 & 30A \operatorname{Sin}[4c + 3dx] + 48B \operatorname{Sin}[4c + 3dx] + 81C \operatorname{Sin}[4c + 3dx] + 96A \operatorname{Sin}[3c + 4dx] + \\
 & 160B \operatorname{Sin}[3c + 4dx] + 160C \operatorname{Sin}[3c + 4dx] + 6A \operatorname{Sin}[4c + 5dx] + 6A \operatorname{Sin}[6c + 5dx])
 \end{aligned}$$

Problem 442: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cos}[c + dx]^2 (a + a \operatorname{Sec}[c + dx])^4 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) dx$$

Optimal (type 3, 209 leaves, 7 steps):

$$\frac{1}{2} a^4 (13 A + 8 B + 2 C) x + \frac{a^4 (8 A + 13 B + 12 C) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{2 d} +$$

$$\frac{5 a^4 (A - B - 2 C) \operatorname{Sin}[c + d x]}{2 d} - \frac{a (3 A - 2 C) (a + a \operatorname{Sec}[c + d x])^3 \operatorname{Sin}[c + d x]}{6 d} +$$

$$\frac{A \operatorname{Cos}[c + d x] (a + a \operatorname{Sec}[c + d x])^4 \operatorname{Sin}[c + d x]}{2 d} - \frac{(A - B - 2 C) (a^2 + a^2 \operatorname{Sec}[c + d x])^2 \operatorname{Sin}[c + d x]}{2 d} +$$

$$\frac{(3 A + 18 B + 22 C) (a^4 + a^4 \operatorname{Sec}[c + d x]) \operatorname{Sin}[c + d x]}{6 d}$$

Result (type 3, 739 leaves):

$$\left( (-8 A - 13 B - 12 C) \operatorname{Cos}[c + d x]^6 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right] - \operatorname{Sin}\left[\frac{c}{2} + \frac{d x}{2}\right]\right] \right. \\ \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^8 (a + a \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) / \\ (16 d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x])) +$$

$$\left( (8 A + 13 B + 12 C) \operatorname{Cos}[c + d x]^6 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{d x}{2}\right]\right] \right. \\ \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^8 (a + a \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) / \\ (16 d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x])) +$$


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$$1536 d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x])$$

$$\operatorname{Cos}[c + d x]^3 \operatorname{Sec}[c] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^8 (a + a \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)$$

$$(468 A d x \operatorname{Cos}[d x] + 288 B d x \operatorname{Cos}[d x] + 72 C d x \operatorname{Cos}[d x] + 468 A d x \operatorname{Cos}[2 c + d x] +$$

$$288 B d x \operatorname{Cos}[2 c + d x] + 72 C d x \operatorname{Cos}[2 c + d x] + 156 A d x \operatorname{Cos}[2 c + 3 d x] +$$

$$96 B d x \operatorname{Cos}[2 c + 3 d x] + 24 C d x \operatorname{Cos}[2 c + 3 d x] + 156 A d x \operatorname{Cos}[4 c + 3 d x] +$$

$$96 B d x \operatorname{Cos}[4 c + 3 d x] + 24 C d x \operatorname{Cos}[4 c + 3 d x] + 102 A \operatorname{Sin}[d x] + 384 B \operatorname{Sin}[d x] +$$

$$672 C \operatorname{Sin}[d x] - 42 A \operatorname{Sin}[2 c + d x] - 192 B \operatorname{Sin}[2 c + d x] - 288 C \operatorname{Sin}[2 c + d x] +$$

$$96 A \operatorname{Sin}[c + 2 d x] + 48 B \operatorname{Sin}[c + 2 d x] + 96 C \operatorname{Sin}[c + 2 d x] + 96 A \operatorname{Sin}[3 c + 2 d x] +$$

$$48 B \operatorname{Sin}[3 c + 2 d x] + 96 C \operatorname{Sin}[3 c + 2 d x] + 57 A \operatorname{Sin}[2 c + 3 d x] + 192 B \operatorname{Sin}[2 c + 3 d x] +$$

$$320 C \operatorname{Sin}[2 c + 3 d x] + 9 A \operatorname{Sin}[4 c + 3 d x] + 48 A \operatorname{Sin}[3 c + 4 d x] + 12 B \operatorname{Sin}[3 c + 4 d x] +$$

$$48 A \operatorname{Sin}[5 c + 4 d x] + 12 B \operatorname{Sin}[5 c + 4 d x] + 3 A \operatorname{Sin}[4 c + 5 d x] + 3 A \operatorname{Sin}[6 c + 5 d x])$$

**Problem 443: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Cos}[c + d x]^3 (a + a \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 3, 217 leaves, 7 steps):

$$\frac{1}{2} a^4 (12 A + 13 B + 8 C) x + \frac{a^4 (2 A + 8 B + 13 C) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{2 d} +$$

$$\frac{5 a^4 (2 A + B - C) \operatorname{Sin}[c + d x]}{2 d} + \frac{a (4 A + 3 B) \operatorname{Cos}[c + d x] (a + a \operatorname{Sec}[c + d x])^3 \operatorname{Sin}[c + d x]}{6 d} +$$

$$\frac{A \operatorname{Cos}[c + d x]^2 (a + a \operatorname{Sec}[c + d x])^4 \operatorname{Sin}[c + d x]}{3 d} - \frac{(2 A + B - C) (a^2 + a^2 \operatorname{Sec}[c + d x])^2 \operatorname{Sin}[c + d x]}{2 d} -$$

$$\frac{(8 A - 3 B - 18 C) (a^4 + a^4 \operatorname{Sec}[c + d x]) \operatorname{Sin}[c + d x]}{6 d}$$

Result (type 3, 1518 leaves):

$$\left( (12 A + 13 B + 8 C) x \operatorname{Cos}[c + d x]^6 \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^8 (a + a \operatorname{Sec}[c + d x])^4 \right. \\ \left. (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) / \left( 16 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \right) +$$

$$\left( (-2 A - 8 B - 13 C) \operatorname{Cos}[c + d x]^6 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right] - \operatorname{Sin}\left[\frac{c}{2} + \frac{d x}{2}\right]\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^8 \right. \\ \left. (a + a \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) /$$

$$\left( 16 d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \right) +$$

$$\left( (2 A + 8 B + 13 C) \operatorname{Cos}[c + d x]^6 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{d x}{2}\right]\right] \right. \\ \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^8 (a + a \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) /$$

$$\left( 16 d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \right) +$$

$$\left( (27 A + 16 B + 4 C) \operatorname{Cos}[d x] \operatorname{Cos}[c + d x]^6 \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^8 \right. \\ \left. (a + a \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \operatorname{Sin}[c] \right) /$$

$$\left( 32 d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \right) +$$

$$\left( (4 A + B) \operatorname{Cos}[2 d x] \operatorname{Cos}[c + d x]^6 \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^8 (a + a \operatorname{Sec}[c + d x])^4 \right. \\ \left. (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \operatorname{Sin}[2 c] \right) /$$

$$\left( 32 d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \right) +$$

$$\left( A \operatorname{Cos}[3 d x] \operatorname{Cos}[c + d x]^6 \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^8 (a + a \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\ \left. \operatorname{Sin}[3 c] \right) / \left( 96 d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \right) +$$

$$\left( (27 A + 16 B + 4 C) \operatorname{Cos}[c] \operatorname{Cos}[c + d x]^6 \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^8 (a + a \operatorname{Sec}[c + d x])^4 \right. \\ \left. (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \operatorname{Sin}[d x] \right) /$$

$$\left( 32 d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \right) +$$

$$\left( (4 A + B) \operatorname{Cos}[2 c] \operatorname{Cos}[c + d x]^6 \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^8 (a + a \operatorname{Sec}[c + d x])^4 \right. \\ \left. (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \operatorname{Sin}[2 d x] \right) /$$

$$\begin{aligned}
 & \left( 32 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right) + \\
 & \left( A \cos [3 c] \cos [c + d x]^6 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 (a + a \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left. \sin [3 d x] \right) / \left( 96 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right) + \\
 & \left( C \cos [c + d x]^6 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 (a + a \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \\
 & \left( 32 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right)^2 \right) + \\
 & \left( \cos [c + d x]^6 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 (a + a \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left. \left( B \sin \left[ \frac{d x}{2} \right] + 4 C \sin \left[ \frac{d x}{2} \right] \right) \right) / \left( 8 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right) \right) - \\
 & \left( C \cos [c + d x]^6 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 (a + a \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \\
 & \left( 32 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right)^2 \right) + \\
 & \left( \cos [c + d x]^6 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 (a + a \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left. \left( B \sin \left[ \frac{d x}{2} \right] + 4 C \sin \left[ \frac{d x}{2} \right] \right) \right) / \left( 8 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right) \right)
 \end{aligned}$$

### Problem 444: Result more than twice size of optimal antiderivative.

$$\int \cos [c + d x]^4 (a + a \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 3, 217 leaves, 7 steps):

$$\begin{aligned}
 & \frac{1}{8} a^4 (35 A + 48 B + 52 C) x + \frac{a^4 (B + 4 C) \operatorname{ArcTanh}[\sin [c + d x]]}{d} + \\
 & \frac{5 a^4 (7 A + 8 B + 4 C) \sin [c + d x]}{8 d} + \frac{a (A + B) \cos [c + d x]^2 (a + a \sec [c + d x])^3 \sin [c + d x]}{3 d} + \\
 & \frac{A \cos [c + d x]^3 (a + a \sec [c + d x])^4 \sin [c + d x]}{4 d} + \\
 & \frac{(7 A + 8 B + 4 C) \cos [c + d x] (a^2 + a^2 \sec [c + d x])^2 \sin [c + d x]}{8 d} - \\
 & \frac{(35 A + 32 B - 12 C) (a^4 + a^4 \sec [c + d x]) \sin [c + d x]}{24 d}
 \end{aligned}$$

Result (type 3, 1436 leaves):

$$a^4 \left( \left( (35 A + 48 B + 52 C) x \cos [c + d x]^2 (1 + \cos [c + d x])^4 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 \right. \right.$$

$$\begin{aligned}
& \left. (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / (64 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) + \\
& \left( (-B - 4 C) \cos [c + d x]^2 (1 + \cos [c + d x])^4 \log \left[ \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 \right. \\
& \left. (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / (8 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) + \\
& \left( (B + 4 C) \cos [c + d x]^2 (1 + \cos [c + d x])^4 \log \left[ \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 \right. \\
& \left. (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / (8 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) + \\
& \left( (28 A + 27 B + 16 C) \cos [d x] \cos [c + d x]^2 (1 + \cos [c + d x])^4 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 \right. \\
& \left. (A + B \sec [c + d x] + C \sec [c + d x]^2) \sin [c] \right) / \\
& (32 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) + \\
& \left( (7 A + 4 B + C) \cos [2 d x] \cos [c + d x]^2 (1 + \cos [c + d x])^4 \right. \\
& \left. \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 (A + B \sec [c + d x] + C \sec [c + d x]^2) \sin [2 c] \right) / \\
& (32 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) + \\
& \left( (4 A + B) \cos [3 d x] \cos [c + d x]^2 (1 + \cos [c + d x])^4 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 \right. \\
& \left. (A + B \sec [c + d x] + C \sec [c + d x]^2) \sin [3 c] \right) / \\
& (96 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) + \\
& \left( A \cos [4 d x] \cos [c + d x]^2 (1 + \cos [c + d x])^4 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
& \left. \sin [4 c] \right) / (256 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) + \\
& \left( (28 A + 27 B + 16 C) \cos [c] \cos [c + d x]^2 (1 + \cos [c + d x])^4 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 \right. \\
& \left. (A + B \sec [c + d x] + C \sec [c + d x]^2) \sin [d x] \right) / \\
& (32 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) + \\
& \left( (7 A + 4 B + C) \cos [2 c] \cos [c + d x]^2 (1 + \cos [c + d x])^4 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 \right. \\
& \left. (A + B \sec [c + d x] + C \sec [c + d x]^2) \sin [2 d x] \right) / \\
& (32 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) + \\
& \left( (4 A + B) \cos [3 c] \cos [c + d x]^2 (1 + \cos [c + d x])^4 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 \right. \\
& \left. (A + B \sec [c + d x] + C \sec [c + d x]^2) \sin [3 d x] \right) / \\
& (96 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) + \\
& \left( A \cos [4 c] \cos [c + d x]^2 (1 + \cos [c + d x])^4 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
& \left. \sin [4 d x] \right) / (256 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) +
\end{aligned}$$

$$\begin{aligned} & \left( C \cos [c+d x]^2 (1+\cos [c+d x])^4 \sec \left[ \frac{c}{2}+\frac{d x}{2} \right]^8 (A+B \sec [c+d x]+C \sec [c+d x]^2) \right. \\ & \quad \left. \sin \left[ \frac{d x}{2} \right] \right) / \left( 8 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right. \\ & \quad \left. \left( \cos \left[ \frac{c}{2} \right]-\sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2}+\frac{d x}{2} \right]-\sin \left[ \frac{c}{2}+\frac{d x}{2} \right] \right) \right) + \\ & \left( C \cos [c+d x]^2 (1+\cos [c+d x])^4 \sec \left[ \frac{c}{2}+\frac{d x}{2} \right]^8 (A+B \sec [c+d x]+C \sec [c+d x]^2) \right. \\ & \quad \left. \sin \left[ \frac{d x}{2} \right] \right) / \left( 8 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right. \\ & \quad \left. \left( \cos \left[ \frac{c}{2} \right]+\sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2}+\frac{d x}{2} \right]+\sin \left[ \frac{c}{2}+\frac{d x}{2} \right] \right) \right) \end{aligned}$$

**Problem 449: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c+d x]^4 (A+B \sec [c+d x]+C \sec [c+d x]^2)}{a+a \sec [c+d x]} dx$$

Optimal (type 3, 183 leaves, 7 steps):

$$\begin{aligned} & \frac{3(4 A-4 B+5 C) \operatorname{ArcTanh}[\sin [c+d x]]}{8 a d}-\frac{(3 A-4 B+4 C) \tan [c+d x]}{a d}+ \\ & \frac{3(4 A-4 B+5 C) \sec [c+d x] \tan [c+d x]}{8 a d}+\frac{(4 A-4 B+5 C) \sec [c+d x]^3 \tan [c+d x]}{4 a d}- \\ & \frac{(A-B+C) \sec [c+d x]^4 \tan [c+d x]}{d(a+a \sec [c+d x])}-\frac{(3 A-4 B+4 C) \tan [c+d x]^3}{3 a d} \end{aligned}$$

Result (type 3, 1099 leaves):

$$\begin{aligned}
& - \left( \left( 3 (4A - 4B + 5C) \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \cos [c + dx] \right. \right. \\
& \quad \left. \left. \log \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] - \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right] (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) \right) / \\
& \quad \left( 2d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) (a + a \sec [c + dx]) \right) + \\
& \left( 3 (4A - 4B + 5C) \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \cos [c + dx] \log \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] + \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right] \right. \\
& \quad \left. (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) / \\
& \quad \left( 2d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) (a + a \sec [c + dx]) \right) + \\
& \left( 1 / (192d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) (a + a \sec [c + dx])) \right) \\
& \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] \sec \left[ \frac{c}{2} \right] \sec [c] \sec [c + dx]^3 (A + B \sec [c + dx] + C \sec [c + dx]^2) \\
& \left( -60A \sin \left[ \frac{dx}{2} \right] + 108B \sin \left[ \frac{dx}{2} \right] - 75C \sin \left[ \frac{dx}{2} \right] - 60A \sin \left[ \frac{3dx}{2} \right] + 124B \sin \left[ \frac{3dx}{2} \right] - \right. \\
& \quad 91C \sin \left[ \frac{3dx}{2} \right] + 204A \sin \left[ c - \frac{dx}{2} \right] - 252B \sin \left[ c - \frac{dx}{2} \right] + 219C \sin \left[ c - \frac{dx}{2} \right] - \\
& \quad 60A \sin \left[ c + \frac{dx}{2} \right] + 12B \sin \left[ c + \frac{dx}{2} \right] + 21C \sin \left[ c + \frac{dx}{2} \right] + 84A \sin \left[ 2c + \frac{dx}{2} \right] - \\
& \quad 132B \sin \left[ 2c + \frac{dx}{2} \right] + 165C \sin \left[ 2c + \frac{dx}{2} \right] + 36A \sin \left[ c + \frac{3dx}{2} \right] + 28B \sin \left[ c + \frac{3dx}{2} \right] + \\
& \quad 5C \sin \left[ c + \frac{3dx}{2} \right] + 36A \sin \left[ 2c + \frac{3dx}{2} \right] - 36B \sin \left[ 2c + \frac{3dx}{2} \right] + 69C \sin \left[ 2c + \frac{3dx}{2} \right] + \\
& \quad 132A \sin \left[ 3c + \frac{3dx}{2} \right] - 132B \sin \left[ 3c + \frac{3dx}{2} \right] + 165C \sin \left[ 3c + \frac{3dx}{2} \right] - 156A \sin \left[ c + \frac{5dx}{2} \right] + \\
& \quad 220B \sin \left[ c + \frac{5dx}{2} \right] - 211C \sin \left[ c + \frac{5dx}{2} \right] - 60A \sin \left[ 2c + \frac{5dx}{2} \right] + 124B \sin \left[ 2c + \frac{5dx}{2} \right] - \\
& \quad 115C \sin \left[ 2c + \frac{5dx}{2} \right] - 60A \sin \left[ 3c + \frac{5dx}{2} \right] + 60B \sin \left[ 3c + \frac{5dx}{2} \right] - 51C \sin \left[ 3c + \frac{5dx}{2} \right] + \\
& \quad 36A \sin \left[ 4c + \frac{5dx}{2} \right] - 36B \sin \left[ 4c + \frac{5dx}{2} \right] + 45C \sin \left[ 4c + \frac{5dx}{2} \right] - 12A \sin \left[ 2c + \frac{7dx}{2} \right] + \\
& \quad 28B \sin \left[ 2c + \frac{7dx}{2} \right] - 19C \sin \left[ 2c + \frac{7dx}{2} \right] + 12A \sin \left[ 3c + \frac{7dx}{2} \right] + 4B \sin \left[ 3c + \frac{7dx}{2} \right] + \\
& \quad 5C \sin \left[ 3c + \frac{7dx}{2} \right] + 12A \sin \left[ 4c + \frac{7dx}{2} \right] - 12B \sin \left[ 4c + \frac{7dx}{2} \right] + 21C \sin \left[ 4c + \frac{7dx}{2} \right] + \\
& \quad 36A \sin \left[ 5c + \frac{7dx}{2} \right] - 36B \sin \left[ 5c + \frac{7dx}{2} \right] + 45C \sin \left[ 5c + \frac{7dx}{2} \right] - 48A \sin \left[ 3c + \frac{9dx}{2} \right] + \\
& \quad 64B \sin \left[ 3c + \frac{9dx}{2} \right] - 64C \sin \left[ 3c + \frac{9dx}{2} \right] - 24A \sin \left[ 4c + \frac{9dx}{2} \right] + 40B \sin \left[ 4c + \frac{9dx}{2} \right] - \\
& \quad \left. 40C \sin \left[ 4c + \frac{9dx}{2} \right] - 24A \sin \left[ 5c + \frac{9dx}{2} \right] + 24B \sin \left[ 5c + \frac{9dx}{2} \right] - 24C \sin \left[ 5c + \frac{9dx}{2} \right] \right)
\end{aligned}$$

**Problem 450: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c + dx]^3 (A + B \sec [c + dx] + C \sec [c + dx]^2)}{a + a \sec [c + dx]} dx$$



Optimal (type 3, 148 leaves, 6 steps):

$$\begin{aligned}
 & - \frac{(2A - 3B + 3C) \operatorname{ArcTanh}[\operatorname{Sin}[c + dx]]}{2ad} + \\
 & \frac{(3A - 3B + 4C) \operatorname{Tan}[c + dx]}{ad} - \frac{(2A - 3B + 3C) \operatorname{Sec}[c + dx] \operatorname{Tan}[c + dx]}{2ad} - \\
 & \frac{(A - B + C) \operatorname{Sec}[c + dx]^3 \operatorname{Tan}[c + dx]}{d(a + a \operatorname{Sec}[c + dx])} + \frac{(3A - 3B + 4C) \operatorname{Tan}[c + dx]^3}{3ad}
 \end{aligned}$$

Result (type 3, 898 leaves):

$$\begin{aligned}
 & \left( 2(2A - 3B + 3C) \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Cos}[c + dx] \right. \\
 & \quad \left. \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] - \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right) / \\
 & \quad (d(A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])) - \\
 & \left( 2(2A - 3B + 3C) \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Cos}[c + dx] \right. \\
 & \quad \left. \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right) / \\
 & \quad (d(A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])) + \\
 & \quad \frac{1}{24d(A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])} \\
 & \quad \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c] \operatorname{Sec}[c + dx]^2 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \\
 & \quad \left( -6A \operatorname{Sin}\left[\frac{dx}{2}\right] + 6B \operatorname{Sin}\left[\frac{dx}{2}\right] + 6C \operatorname{Sin}\left[\frac{dx}{2}\right] + 30A \operatorname{Sin}\left[\frac{3dx}{2}\right] - 27B \operatorname{Sin}\left[\frac{3dx}{2}\right] + \right. \\
 & \quad 39C \operatorname{Sin}\left[\frac{3dx}{2}\right] - 12A \operatorname{Sin}\left[c - \frac{dx}{2}\right] + 12B \operatorname{Sin}\left[c - \frac{dx}{2}\right] - 24C \operatorname{Sin}\left[c - \frac{dx}{2}\right] - \\
 & \quad 6A \operatorname{Sin}\left[c + \frac{dx}{2}\right] + 6B \operatorname{Sin}\left[c + \frac{dx}{2}\right] - 6C \operatorname{Sin}\left[c + \frac{dx}{2}\right] - 24A \operatorname{Sin}\left[2c + \frac{dx}{2}\right] + \\
 & \quad 24B \operatorname{Sin}\left[2c + \frac{dx}{2}\right] - 24C \operatorname{Sin}\left[2c + \frac{dx}{2}\right] + 12A \operatorname{Sin}\left[c + \frac{3dx}{2}\right] - 9B \operatorname{Sin}\left[c + \frac{3dx}{2}\right] + \\
 & \quad 21C \operatorname{Sin}\left[c + \frac{3dx}{2}\right] + 12A \operatorname{Sin}\left[2c + \frac{3dx}{2}\right] - 9B \operatorname{Sin}\left[2c + \frac{3dx}{2}\right] + 9C \operatorname{Sin}\left[2c + \frac{3dx}{2}\right] - \\
 & \quad 6A \operatorname{Sin}\left[3c + \frac{3dx}{2}\right] + 9B \operatorname{Sin}\left[3c + \frac{3dx}{2}\right] - 9C \operatorname{Sin}\left[3c + \frac{3dx}{2}\right] + 6A \operatorname{Sin}\left[c + \frac{5dx}{2}\right] - \\
 & \quad 3B \operatorname{Sin}\left[c + \frac{5dx}{2}\right] + 7C \operatorname{Sin}\left[c + \frac{5dx}{2}\right] + 3B \operatorname{Sin}\left[2c + \frac{5dx}{2}\right] + C \operatorname{Sin}\left[2c + \frac{5dx}{2}\right] + \\
 & \quad 3B \operatorname{Sin}\left[3c + \frac{5dx}{2}\right] - 3C \operatorname{Sin}\left[3c + \frac{5dx}{2}\right] - 6A \operatorname{Sin}\left[4c + \frac{5dx}{2}\right] + 9B \operatorname{Sin}\left[4c + \frac{5dx}{2}\right] - \\
 & \quad 9C \operatorname{Sin}\left[4c + \frac{5dx}{2}\right] + 12A \operatorname{Sin}\left[2c + \frac{7dx}{2}\right] - 12B \operatorname{Sin}\left[2c + \frac{7dx}{2}\right] + \\
 & \quad 16C \operatorname{Sin}\left[2c + \frac{7dx}{2}\right] + 6A \operatorname{Sin}\left[3c + \frac{7dx}{2}\right] - 6B \operatorname{Sin}\left[3c + \frac{7dx}{2}\right] + \\
 & \quad \left. 10C \operatorname{Sin}\left[3c + \frac{7dx}{2}\right] + 6A \operatorname{Sin}\left[4c + \frac{7dx}{2}\right] - 6B \operatorname{Sin}\left[4c + \frac{7dx}{2}\right] + 6C \operatorname{Sin}\left[4c + \frac{7dx}{2}\right] \right)
 \end{aligned}$$

**Problem 451: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Sec}[c + d x]^2 (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2)}{a + a \text{Sec}[c + d x]} dx$$

Optimal (type 3, 119 leaves, 6 steps):

$$\frac{(2 A - 2 B + 3 C) \text{ArcTanh}[\text{Sin}[c + d x]]}{2 a d} - \frac{(A - 2 B + 2 C) \text{Tan}[c + d x]}{a d} + \frac{(2 A - 2 B + 3 C) \text{Sec}[c + d x] \text{Tan}[c + d x]}{2 a d} - \frac{(A - B + C) \text{Sec}[c + d x]^2 \text{Tan}[c + d x]}{d (a + a \text{Sec}[c + d x])}$$

Result (type 3, 900 leaves):

$$\begin{aligned}
 & - \left( \left( 2 (2A - 2B + 3C) \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \cos [c + dx] \right. \right. \\
 & \quad \left. \left. \log \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] - \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right] (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) \right) / \\
 & \quad \left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) (a + a \sec [c + dx]) \right) + \\
 & \left( 2 (2A - 2B + 3C) \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \cos [c + dx] \log \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] + \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right] \right. \\
 & \quad \left. (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) / \\
 & \quad \left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) (a + a \sec [c + dx]) \right) - \\
 & \left( 4 \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] \cos [c + dx] \sec \left[ \frac{c}{2} \right] (A + B \sec [c + dx] + C \sec [c + dx]^2) \right. \\
 & \quad \left. \left( A \sin \left[ \frac{dx}{2} \right] - B \sin \left[ \frac{dx}{2} \right] + C \sin \left[ \frac{dx}{2} \right] \right) \right) / \\
 & \quad \left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) (a + a \sec [c + dx]) \right) + \\
 & \left( C \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \cos [c + dx] (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) / \\
 & \quad \left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \right. \\
 & \quad \left. (a + a \sec [c + dx]) \left( \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] - \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right)^2 \right) - \\
 & \left( 4 \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \cos [c + dx] (A + B \sec [c + dx] + C \sec [c + dx]^2) \left( -B \sin \left[ \frac{dx}{2} \right] + C \sin \left[ \frac{dx}{2} \right] \right) \right) / \\
 & \quad \left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) (a + a \sec [c + dx]) \right. \\
 & \quad \left. \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] - \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right) \right) - \\
 & \left( C \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \cos [c + dx] (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) / \\
 & \quad \left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \right. \\
 & \quad \left. (a + a \sec [c + dx]) \left( \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] + \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right)^2 \right) - \\
 & \left( 4 \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \cos [c + dx] (A + B \sec [c + dx] + C \sec [c + dx]^2) \left( -B \sin \left[ \frac{dx}{2} \right] + C \sin \left[ \frac{dx}{2} \right] \right) \right) / \\
 & \quad \left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \right. \\
 & \quad \left. (a + a \sec [c + dx]) \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] + \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right) \right)
 \end{aligned}$$

**Problem 452: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c + dx] (A + B \sec [c + dx] + C \sec [c + dx]^2)}{a + a \sec [c + dx]} dx$$

Optimal (type 3, 63 leaves, 4 steps):

$$\frac{(B-C) \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{ad} + \frac{C \operatorname{Tan}[c+dx]}{ad} + \frac{(A-B+C) \operatorname{Tan}[c+dx]}{ad(1+\operatorname{Sec}[c+dx])}$$

Result (type 3, 255 leaves):

$$\frac{1}{ad(A+2C+2B \cos[c+dx]+A \cos[2(c+dx)])(1+\operatorname{Sec}[c+dx])} \\ 4 \cos\left[\frac{1}{2}(c+dx)\right] \cos[c+dx] (A+B \operatorname{Sec}[c+dx]+C \operatorname{Sec}[c+dx]^2) \left( (A-B+C) \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sin}\left[\frac{dx}{2}\right] + \right. \\ \left. \cos\left[\frac{1}{2}(c+dx)\right] \left( -(B-C) \left( \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right]\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) - \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] + \right. \right. \right. \\ \left. \left. \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right] \right) + (C \operatorname{Sin}[dx]) \right) / \left( \left( \cos\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right] \right) \right. \\ \left. \left( \cos\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \left( \cos\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \right) \right)$$

**Problem 453: Result more than twice size of optimal antiderivative.**

$$\int \frac{A+B \operatorname{Sec}[c+dx]+C \operatorname{Sec}[c+dx]^2}{a+a \operatorname{Sec}[c+dx]} dx$$

Optimal (type 3, 52 leaves, 4 steps):

$$\frac{Ax}{a} + \frac{C \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{ad} - \frac{(A-B+C) \operatorname{Tan}[c+dx]}{ad(1+\operatorname{Sec}[c+dx])}$$

Result (type 3, 163 leaves):

$$\left( 4 \cos\left[\frac{1}{2}(c+dx)\right] (C+B \cos[c+dx]+A \cos[c+dx]^2) \right. \\ \left( \cos\left[\frac{1}{2}(c+dx)\right] \left( Adx - C \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right] + \right. \right. \\ \left. \left. C \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right] \right) - (A-B+C) \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sin}\left[\frac{dx}{2}\right] \right) \right) / \\ (ad(1+\cos[c+dx])(A+2C+2B \cos[c+dx]+A \cos[2(c+dx)]))$$

**Problem 456: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c+dx]^3 (A+B \operatorname{Sec}[c+dx]+C \operatorname{Sec}[c+dx]^2)}{a+a \operatorname{Sec}[c+dx]} dx$$

Optimal (type 3, 139 leaves, 6 steps):

$$-\frac{(3A-3B+2C)x}{2a} + \frac{(4A-3B+3C) \operatorname{Sin}[c+dx]}{ad} - \frac{(3A-3B+2C) \cos[c+dx] \operatorname{Sin}[c+dx]}{2ad} - \\ \frac{(A-B+C) \cos[c+dx]^2 \operatorname{Sin}[c+dx]}{d(a+a \operatorname{Sec}[c+dx])} - \frac{(4A-3B+3C) \operatorname{Sin}[c+dx]^3}{3ad}$$

Result (type 3, 307 leaves):

$$\frac{1}{24 a d (1 + \cos [c + d x])} \cos \left[ \frac{1}{2} (c + d x) \right] \sec \left[ \frac{c}{2} \right]$$

$$\left( -12 (3 A - 3 B + 2 C) d x \cos \left[ \frac{d x}{2} \right] - 12 (3 A - 3 B + 2 C) d x \cos \left[ c + \frac{d x}{2} \right] + 69 A \sin \left[ \frac{d x}{2} \right] - \right.$$

$$60 B \sin \left[ \frac{d x}{2} \right] + 60 C \sin \left[ \frac{d x}{2} \right] + 21 A \sin \left[ c + \frac{d x}{2} \right] - 12 B \sin \left[ c + \frac{d x}{2} \right] + 12 C \sin \left[ c + \frac{d x}{2} \right] +$$

$$18 A \sin \left[ c + \frac{3 d x}{2} \right] - 9 B \sin \left[ c + \frac{3 d x}{2} \right] + 12 C \sin \left[ c + \frac{3 d x}{2} \right] + 18 A \sin \left[ 2 c + \frac{3 d x}{2} \right] -$$

$$9 B \sin \left[ 2 c + \frac{3 d x}{2} \right] + 12 C \sin \left[ 2 c + \frac{3 d x}{2} \right] - 2 A \sin \left[ 2 c + \frac{5 d x}{2} \right] + 3 B \sin \left[ 2 c + \frac{5 d x}{2} \right] -$$

$$\left. 2 A \sin \left[ 3 c + \frac{5 d x}{2} \right] + 3 B \sin \left[ 3 c + \frac{5 d x}{2} \right] + A \sin \left[ 3 c + \frac{7 d x}{2} \right] + A \sin \left[ 4 c + \frac{7 d x}{2} \right] \right)$$

**Problem 457: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos [c + d x]^4 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{a + a \sec [c + d x]} dx$$

Optimal (type 3, 174 leaves, 7 steps):

$$\frac{3 (5 A - 4 B + 4 C) x}{8 a} - \frac{(4 A - 4 B + 3 C) \sin [c + d x]}{a d} +$$

$$\frac{3 (5 A - 4 B + 4 C) \cos [c + d x] \sin [c + d x]}{8 a d} + \frac{(5 A - 4 B + 4 C) \cos [c + d x]^3 \sin [c + d x]}{4 a d} -$$

$$\frac{(A - B + C) \cos [c + d x]^3 \sin [c + d x]}{d (a + a \sec [c + d x])} + \frac{(4 A - 4 B + 3 C) \sin [c + d x]^3}{3 a d}$$

Result (type 3, 393 leaves):

$$\frac{1}{192 a d (1 + \cos [c + d x])}$$

$$\cos \left[ \frac{1}{2} (c + d x) \right] \sec \left[ \frac{c}{2} \right] \left( 72 (5 A - 4 B + 4 C) d x \cos \left[ \frac{d x}{2} \right] + 72 (5 A - 4 B + 4 C) d x \cos \left[ c + \frac{d x}{2} \right] - \right.$$

$$552 A \sin \left[ \frac{d x}{2} \right] + 552 B \sin \left[ \frac{d x}{2} \right] - 480 C \sin \left[ \frac{d x}{2} \right] - 168 A \sin \left[ c + \frac{d x}{2} \right] +$$

$$168 B \sin \left[ c + \frac{d x}{2} \right] - 96 C \sin \left[ c + \frac{d x}{2} \right] - 120 A \sin \left[ c + \frac{3 d x}{2} \right] + 144 B \sin \left[ c + \frac{3 d x}{2} \right] -$$

$$72 C \sin \left[ c + \frac{3 d x}{2} \right] - 120 A \sin \left[ 2 c + \frac{3 d x}{2} \right] + 144 B \sin \left[ 2 c + \frac{3 d x}{2} \right] - 72 C \sin \left[ 2 c + \frac{3 d x}{2} \right] +$$

$$40 A \sin \left[ 2 c + \frac{5 d x}{2} \right] - 16 B \sin \left[ 2 c + \frac{5 d x}{2} \right] + 24 C \sin \left[ 2 c + \frac{5 d x}{2} \right] + 40 A \sin \left[ 3 c + \frac{5 d x}{2} \right] -$$

$$16 B \sin \left[ 3 c + \frac{5 d x}{2} \right] + 24 C \sin \left[ 3 c + \frac{5 d x}{2} \right] - 5 A \sin \left[ 3 c + \frac{7 d x}{2} \right] + 8 B \sin \left[ 3 c + \frac{7 d x}{2} \right] -$$

$$\left. 5 A \sin \left[ 4 c + \frac{7 d x}{2} \right] + 8 B \sin \left[ 4 c + \frac{7 d x}{2} \right] + 3 A \sin \left[ 4 c + \frac{9 d x}{2} \right] + 3 A \sin \left[ 5 c + \frac{9 d x}{2} \right] \right)$$

**Problem 458: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Sec}[c + dx]^4 (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2)}{(a + a \text{Sec}[c + dx])^2} dx$$

Optimal (type 3, 194 leaves, 7 steps):

$$\begin{aligned} & - \frac{(4A - 7B + 10C) \text{ArcTanh}[\text{Sin}[c + dx]]}{2a^2d} + \frac{(5A - 8B + 12C) \text{Tan}[c + dx]}{a^2d} - \\ & \frac{(4A - 7B + 10C) \text{Sec}[c + dx] \text{Tan}[c + dx]}{2a^2d} - \frac{(4A - 7B + 10C) \text{Sec}[c + dx]^3 \text{Tan}[c + dx]}{3a^2d(1 + \text{Sec}[c + dx])} - \\ & \frac{(A - B + C) \text{Sec}[c + dx]^4 \text{Tan}[c + dx]}{3d(a + a \text{Sec}[c + dx])^2} + \frac{(5A - 8B + 12C) \text{Tan}[c + dx]^3}{3a^2d} \end{aligned}$$

Result (type 3, 1069 leaves):

$$\begin{aligned}
 & \left( 4 (4A - 7B + 10C) \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \right. \\
 & \quad \left. \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] (A + B \sec[c + dx] + C \sec[c + dx]^2) \right) / \\
 & \quad \left( d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) (a + a \sec[c + dx])^2 \right) - \\
 & \left( 4 (4A - 7B + 10C) \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \right. \\
 & \quad \left. (A + B \sec[c + dx] + C \sec[c + dx]^2) \right) / \\
 & \quad \left( d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) (a + a \sec[c + dx])^2 \right) + \\
 & \left( 1 / \left( 48d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) (a + a \sec[c + dx])^2 \right) \right) \\
 & \cos\left[\frac{c}{2} + \frac{dx}{2}\right] \sec\left[\frac{c}{2}\right] \sec[c] \sec[c + dx]^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \\
 & \left( -48A \sin\left[\frac{dx}{2}\right] + 45B \sin\left[\frac{dx}{2}\right] - 6C \sin\left[\frac{dx}{2}\right] + 132A \sin\left[\frac{3dx}{2}\right] - 201B \sin\left[\frac{3dx}{2}\right] + \right. \\
 & \quad 310C \sin\left[\frac{3dx}{2}\right] - 120A \sin\left[c - \frac{dx}{2}\right] + 195B \sin\left[c - \frac{dx}{2}\right] - 306C \sin\left[c - \frac{dx}{2}\right] + \\
 & \quad 48A \sin\left[c + \frac{dx}{2}\right] - 51B \sin\left[c + \frac{dx}{2}\right] + 42C \sin\left[c + \frac{dx}{2}\right] - 120A \sin\left[2c + \frac{dx}{2}\right] + \\
 & \quad 189B \sin\left[2c + \frac{dx}{2}\right] - 270C \sin\left[2c + \frac{dx}{2}\right] - 8A \sin\left[c + \frac{3dx}{2}\right] - B \sin\left[c + \frac{3dx}{2}\right] + \\
 & \quad 50C \sin\left[c + \frac{3dx}{2}\right] + 72A \sin\left[2c + \frac{3dx}{2}\right] - 81B \sin\left[2c + \frac{3dx}{2}\right] + 90C \sin\left[2c + \frac{3dx}{2}\right] - \\
 & \quad 68A \sin\left[3c + \frac{3dx}{2}\right] + 119B \sin\left[3c + \frac{3dx}{2}\right] - 170C \sin\left[3c + \frac{3dx}{2}\right] + \\
 & \quad 84A \sin\left[c + \frac{5dx}{2}\right] - 129B \sin\left[c + \frac{5dx}{2}\right] + 198C \sin\left[c + \frac{5dx}{2}\right] - 9B \sin\left[2c + \frac{5dx}{2}\right] + \\
 & \quad 42C \sin\left[2c + \frac{5dx}{2}\right] + 48A \sin\left[3c + \frac{5dx}{2}\right] - 57B \sin\left[3c + \frac{5dx}{2}\right] + 66C \sin\left[3c + \frac{5dx}{2}\right] - \\
 & \quad 36A \sin\left[4c + \frac{5dx}{2}\right] + 63B \sin\left[4c + \frac{5dx}{2}\right] - 90C \sin\left[4c + \frac{5dx}{2}\right] + 48A \sin\left[2c + \frac{7dx}{2}\right] - \\
 & \quad 75B \sin\left[2c + \frac{7dx}{2}\right] + 114C \sin\left[2c + \frac{7dx}{2}\right] + 6A \sin\left[3c + \frac{7dx}{2}\right] - 15B \sin\left[3c + \frac{7dx}{2}\right] + \\
 & \quad 36C \sin\left[3c + \frac{7dx}{2}\right] + 30A \sin\left[4c + \frac{7dx}{2}\right] - 39B \sin\left[4c + \frac{7dx}{2}\right] + 48C \sin\left[4c + \frac{7dx}{2}\right] - \\
 & \quad 12A \sin\left[5c + \frac{7dx}{2}\right] + 21B \sin\left[5c + \frac{7dx}{2}\right] - 30C \sin\left[5c + \frac{7dx}{2}\right] + 20A \sin\left[3c + \frac{9dx}{2}\right] - \\
 & \quad 32B \sin\left[3c + \frac{9dx}{2}\right] + 48C \sin\left[3c + \frac{9dx}{2}\right] + 6A \sin\left[4c + \frac{9dx}{2}\right] - 12B \sin\left[4c + \frac{9dx}{2}\right] + \\
 & \quad \left. 22C \sin\left[4c + \frac{9dx}{2}\right] + 14A \sin\left[5c + \frac{9dx}{2}\right] - 20B \sin\left[5c + \frac{9dx}{2}\right] + 26C \sin\left[5c + \frac{9dx}{2}\right] \right)
 \end{aligned}$$

**Problem 459: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Sec}[c + dx]^3 (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2)}{(a + a \text{Sec}[c + dx])^2} dx$$

Optimal (type 3, 169 leaves, 7 steps):

$$\frac{(2A - 4B + 7C) \text{ArcTanh}[\text{Sin}[c + dx]]}{2a^2d} - \frac{2(2A - 5B + 8C) \text{Tan}[c + dx]}{3a^2d} + \frac{(2A - 4B + 7C) \text{Sec}[c + dx] \text{Tan}[c + dx]}{2a^2d} - \frac{(2A - 5B + 8C) \text{Sec}[c + dx]^2 \text{Tan}[c + dx]}{3a^2d(1 + \text{Sec}[c + dx])} - \frac{(A - B + C) \text{Sec}[c + dx]^3 \text{Tan}[c + dx]}{3d(a + a \text{Sec}[c + dx])^2}$$

Result (type 3, 901 leaves):



$$\begin{aligned}
 & - \left( \left( 4 (2A - 4B + 7C) \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \right. \right. \\
 & \quad \left. \left. \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] (A + B \sec[c + dx] + C \sec[c + dx]^2) \right) \right) / \\
 & \quad \left( d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) (a + a \sec[c + dx])^2 \right) + \\
 & \left( 4 (2A - 4B + 7C) \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \right. \\
 & \quad \left. (A + B \sec[c + dx] + C \sec[c + dx]^2) \right) / \\
 & \quad \left( d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) (a + a \sec[c + dx])^2 \right) + \\
 & \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right] \sec\left[\frac{c}{2}\right] \sec[c] \sec[c + dx]^2 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\
 & \quad \left( 20A \sin\left[\frac{dx}{2}\right] - 14B \sin\left[\frac{dx}{2}\right] + 14C \sin\left[\frac{dx}{2}\right] - 22A \sin\left[\frac{3dx}{2}\right] + 64B \sin\left[\frac{3dx}{2}\right] - \right. \\
 & \quad 97C \sin\left[\frac{3dx}{2}\right] + 36A \sin\left[c - \frac{dx}{2}\right] - 84B \sin\left[c - \frac{dx}{2}\right] + 126C \sin\left[c - \frac{dx}{2}\right] - \\
 & \quad 36A \sin\left[c + \frac{dx}{2}\right] + 42B \sin\left[c + \frac{dx}{2}\right] - 42C \sin\left[c + \frac{dx}{2}\right] + 20A \sin\left[2c + \frac{dx}{2}\right] - \\
 & \quad 56B \sin\left[2c + \frac{dx}{2}\right] + 98C \sin\left[2c + \frac{dx}{2}\right] + 18A \sin\left[c + \frac{3dx}{2}\right] - 6B \sin\left[c + \frac{3dx}{2}\right] + \\
 & \quad 3C \sin\left[c + \frac{3dx}{2}\right] - 22A \sin\left[2c + \frac{3dx}{2}\right] + 34B \sin\left[2c + \frac{3dx}{2}\right] - 37C \sin\left[2c + \frac{3dx}{2}\right] + \\
 & \quad 18A \sin\left[3c + \frac{3dx}{2}\right] - 36B \sin\left[3c + \frac{3dx}{2}\right] + 63C \sin\left[3c + \frac{3dx}{2}\right] - 18A \sin\left[c + \frac{5dx}{2}\right] + \\
 & \quad 48B \sin\left[c + \frac{5dx}{2}\right] - 75C \sin\left[c + \frac{5dx}{2}\right] + 6A \sin\left[2c + \frac{5dx}{2}\right] + 6B \sin\left[2c + \frac{5dx}{2}\right] - \\
 & \quad 15C \sin\left[2c + \frac{5dx}{2}\right] - 18A \sin\left[3c + \frac{5dx}{2}\right] + 30B \sin\left[3c + \frac{5dx}{2}\right] - 39C \sin\left[3c + \frac{5dx}{2}\right] + \\
 & \quad 6A \sin\left[4c + \frac{5dx}{2}\right] - 12B \sin\left[4c + \frac{5dx}{2}\right] + 21C \sin\left[4c + \frac{5dx}{2}\right] - 8A \sin\left[2c + \frac{7dx}{2}\right] + \\
 & \quad 20B \sin\left[2c + \frac{7dx}{2}\right] - 32C \sin\left[2c + \frac{7dx}{2}\right] + 6B \sin\left[3c + \frac{7dx}{2}\right] - 12C \sin\left[3c + \frac{7dx}{2}\right] - \\
 & \quad \left. \left. 8A \sin\left[4c + \frac{7dx}{2}\right] + 14B \sin\left[4c + \frac{7dx}{2}\right] - 20C \sin\left[4c + \frac{7dx}{2}\right] \right) \right) / \\
 & \quad \left( 24d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) (a + a \sec[c + dx])^2 \right)
 \end{aligned}$$

**Problem 460: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec[c + dx]^2 (A + B \sec[c + dx] + C \sec[c + dx]^2)}{(a + a \sec[c + dx])^2} dx$$

Optimal (type 3, 112 leaves, 6 steps):

$$\frac{(B-2C) \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{a^2 d} + \frac{(A-B+4C) \operatorname{Tan}[c+dx]}{3 a^2 d} - \frac{(B-2C) \operatorname{Tan}[c+dx]}{a^2 d (1+\operatorname{Sec}[c+dx])} - \frac{(A-B+C) \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx]}{3 d (a+a \operatorname{Sec}[c+dx])^2}$$

Result (type 3, 312 leaves):

$$\begin{aligned} & \left( 4 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right. \\ & \left( (A-B+C) \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sin}\left[\frac{dx}{2}\right] + 2(A-4B+7C) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sin}\left[\frac{dx}{2}\right] + \right. \\ & \left. \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^3 \left( -6(B-2C) \left( \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - \right. \right. \right. \\ & \left. \left. \left. \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \right) + (6C \operatorname{Sin}[dx]) \right) / \right. \\ & \left. \left( \left( \operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \right) \right. \\ & \left. \left( \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) + (A-B+C) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \operatorname{Tan}\left[\frac{c}{2}\right] \Big) / \\ & \left( 3 a^2 d (A+2C+2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2(c+dx)]) (1+\operatorname{Sec}[c+dx])^2 \right) \end{aligned}$$

**Problem 461: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c+dx] (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2)}{(a+a \operatorname{Sec}[c+dx])^2} dx$$

Optimal (type 3, 81 leaves, 4 steps):

$$\frac{C \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{a^2 d} + \frac{(A+2B-5C) \operatorname{Tan}[c+dx]}{3 a^2 d (1+\operatorname{Sec}[c+dx])} + \frac{(A-B+C) \operatorname{Tan}[c+dx]}{3 d (a+a \operatorname{Sec}[c+dx])^2}$$

Result (type 3, 219 leaves):

$$\begin{aligned} & - \left( \left( 4 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] (C+B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[c+dx]^2) \left( 6C \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^3 \right. \right. \right. \\ & \left. \left. \left. \left( \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \right) \right) + \right. \\ & (A-B+C) \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sin}\left[\frac{dx}{2}\right] - 2(2A+B-4C) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sin}\left[\frac{dx}{2}\right] + \\ & \left. (A-B+C) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \operatorname{Tan}\left[\frac{c}{2}\right] \right) \Big) / \\ & \left( 3 a^2 d (1+\operatorname{Cos}[c+dx])^2 (A+2C+2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2(c+dx)]) \right) \end{aligned}$$

**Problem 462: Result more than twice size of optimal antiderivative.**

$$\int \frac{A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2}{(a+a \operatorname{Sec}[c+dx])^2} dx$$

Optimal (type 3, 74 leaves, 3 steps):

$$\frac{A x}{a^2} - \frac{(4A - B - 2C) \operatorname{Tan}[c + dx]}{3 a^2 d (1 + \operatorname{Sec}[c + dx])} - \frac{(A - B + C) \operatorname{Tan}[c + dx]}{3 d (a + a \operatorname{Sec}[c + dx])^2}$$

Result (type 3, 175 leaves):

$$\begin{aligned} & \frac{1}{24 a^2 d} \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^3 \\ & \left( 9 A dx \operatorname{Cos}\left[\frac{dx}{2}\right] + 9 A dx \operatorname{Cos}\left[c + \frac{dx}{2}\right] + 3 A dx \operatorname{Cos}\left[c + \frac{3 dx}{2}\right] + 3 A dx \operatorname{Cos}\left[2c + \frac{3 dx}{2}\right] - \right. \\ & \quad 18 A \operatorname{Sin}\left[\frac{dx}{2}\right] + 6 B \operatorname{Sin}\left[\frac{dx}{2}\right] + 6 C \operatorname{Sin}\left[\frac{dx}{2}\right] + 12 A \operatorname{Sin}\left[c + \frac{dx}{2}\right] - \\ & \quad \left. 6 B \operatorname{Sin}\left[c + \frac{dx}{2}\right] - 10 A \operatorname{Sin}\left[c + \frac{3 dx}{2}\right] + 4 B \operatorname{Sin}\left[c + \frac{3 dx}{2}\right] + 2 C \operatorname{Sin}\left[c + \frac{3 dx}{2}\right] \right) \end{aligned}$$

**Problem 463: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Cos}[c + dx] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2)}{(a + a \operatorname{Sec}[c + dx])^2} dx$$

Optimal (type 3, 100 leaves, 5 steps):

$$-\frac{(2A - B)x}{a^2} + \frac{(10A - 4B + C) \operatorname{Sin}[c + dx]}{3 a^2 d} - \frac{(2A - B) \operatorname{Sin}[c + dx]}{a^2 d (1 + \operatorname{Sec}[c + dx])} - \frac{(A - B + C) \operatorname{Sin}[c + dx]}{3 d (a + a \operatorname{Sec}[c + dx])^2}$$

Result (type 3, 279 leaves):

$$\begin{aligned} & \frac{1}{12 a^2 d (1 + \operatorname{Cos}[c + dx])^2} \\ & \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] \operatorname{Sec}\left[\frac{c}{2}\right] \left( -18 (2A - B) dx \operatorname{Cos}\left[\frac{dx}{2}\right] - 18 (2A - B) dx \operatorname{Cos}\left[c + \frac{dx}{2}\right] - \right. \\ & \quad 12 A dx \operatorname{Cos}\left[c + \frac{3 dx}{2}\right] + 6 B dx \operatorname{Cos}\left[c + \frac{3 dx}{2}\right] - 12 A dx \operatorname{Cos}\left[2c + \frac{3 dx}{2}\right] + \\ & \quad 6 B dx \operatorname{Cos}\left[2c + \frac{3 dx}{2}\right] + 66 A \operatorname{Sin}\left[\frac{dx}{2}\right] - 36 B \operatorname{Sin}\left[\frac{dx}{2}\right] + 12 C \operatorname{Sin}\left[\frac{dx}{2}\right] - 30 A \operatorname{Sin}\left[c + \frac{dx}{2}\right] + \\ & \quad 24 B \operatorname{Sin}\left[c + \frac{dx}{2}\right] - 12 C \operatorname{Sin}\left[c + \frac{dx}{2}\right] + 41 A \operatorname{Sin}\left[c + \frac{3 dx}{2}\right] - 20 B \operatorname{Sin}\left[c + \frac{3 dx}{2}\right] + \\ & \quad \left. 8 C \operatorname{Sin}\left[c + \frac{3 dx}{2}\right] + 9 A \operatorname{Sin}\left[2c + \frac{3 dx}{2}\right] + 3 A \operatorname{Sin}\left[2c + \frac{5 dx}{2}\right] + 3 A \operatorname{Sin}\left[3c + \frac{5 dx}{2}\right] \right) \end{aligned}$$

**Problem 464: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Cos}[c + dx]^2 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2)}{(a + a \operatorname{Sec}[c + dx])^2} dx$$

Optimal (type 3, 156 leaves, 6 steps):

$$\frac{(7A - 4B + 2C)x}{2a^2} - \frac{2(8A - 5B + 2C)\sin[c + dx]}{3a^2d} + \frac{(7A - 4B + 2C)\cos[c + dx]\sin[c + dx]}{2a^2d} - \frac{(8A - 5B + 2C)\cos[c + dx]\sin[c + dx]}{3a^2d(1 + \sec[c + dx])} - \frac{(A - B + C)\cos[c + dx]\sin[c + dx]}{3d(a + a\sec[c + dx])^2}$$

Result (type 3, 377 leaves):

$$\frac{1}{192a^2d} \sec\left[\frac{c}{2}\right] \sec\left[\frac{1}{2}(c + dx)\right]^3 \left( 36(7A - 4B + 2C)dx \cos\left[\frac{dx}{2}\right] + 36(7A - 4B + 2C)dx \cos\left[c + \frac{dx}{2}\right] + 84Adx \cos\left[c + \frac{3dx}{2}\right] - 48Bdx \cos\left[c + \frac{3dx}{2}\right] + 24Cdx \cos\left[c + \frac{3dx}{2}\right] + 84Adx \cos\left[2c + \frac{3dx}{2}\right] - 48Bdx \cos\left[2c + \frac{3dx}{2}\right] + 24Cdx \cos\left[2c + \frac{3dx}{2}\right] - 381A \sin\left[\frac{dx}{2}\right] + 264B \sin\left[\frac{dx}{2}\right] - 144C \sin\left[\frac{dx}{2}\right] + 147A \sin\left[c + \frac{dx}{2}\right] - 120B \sin\left[c + \frac{dx}{2}\right] + 96C \sin\left[c + \frac{dx}{2}\right] - 239A \sin\left[c + \frac{3dx}{2}\right] + 164B \sin\left[c + \frac{3dx}{2}\right] - 80C \sin\left[c + \frac{3dx}{2}\right] - 63A \sin\left[2c + \frac{3dx}{2}\right] + 36B \sin\left[2c + \frac{3dx}{2}\right] - 15A \sin\left[2c + \frac{5dx}{2}\right] + 12B \sin\left[2c + \frac{5dx}{2}\right] - 15A \sin\left[3c + \frac{5dx}{2}\right] + 12B \sin\left[3c + \frac{5dx}{2}\right] + 3A \sin\left[3c + \frac{7dx}{2}\right] + 3A \sin\left[4c + \frac{7dx}{2}\right] \right)$$

**Problem 465: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c + dx]^3 (A + B \sec[c + dx] + C \sec[c + dx]^2)}{(a + a \sec[c + dx])^2} dx$$

Optimal (type 3, 185 leaves, 7 steps):

$$-\frac{(10A - 7B + 4C)x}{2a^2} + \frac{(12A - 8B + 5C)\sin[c + dx]}{a^2d} - \frac{(10A - 7B + 4C)\cos[c + dx]\sin[c + dx]}{2a^2d} - \frac{(10A - 7B + 4C)\cos[c + dx]^2\sin[c + dx]}{3a^2d(1 + \sec[c + dx])} - \frac{(A - B + C)\cos[c + dx]^2\sin[c + dx]}{3d(a + a\sec[c + dx])^2} - \frac{(12A - 8B + 5C)\sin[c + dx]^3}{3a^2d}$$

Result (type 3, 473 leaves):

$$\frac{1}{192 a^2 d} \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^3 \left( -36(10 A-7 B+4 C) d x \cos\left[\frac{d x}{2}\right] - 36(10 A-7 B+4 C) d x \cos\left[c+\frac{d x}{2}\right] - \right. \\
 120 A d x \cos\left[c+\frac{3 d x}{2}\right] + 84 B d x \cos\left[c+\frac{3 d x}{2}\right] - 48 C d x \cos\left[c+\frac{3 d x}{2}\right] - \\
 120 A d x \cos\left[2 c+\frac{3 d x}{2}\right] + 84 B d x \cos\left[2 c+\frac{3 d x}{2}\right] - 48 C d x \cos\left[2 c+\frac{3 d x}{2}\right] + \\
 516 A \sin\left[\frac{d x}{2}\right] - 381 B \sin\left[\frac{d x}{2}\right] + 264 C \sin\left[\frac{d x}{2}\right] - 156 A \sin\left[c+\frac{d x}{2}\right] + \\
 147 B \sin\left[c+\frac{d x}{2}\right] - 120 C \sin\left[c+\frac{d x}{2}\right] + 342 A \sin\left[c+\frac{3 d x}{2}\right] - 239 B \sin\left[c+\frac{3 d x}{2}\right] + \\
 164 C \sin\left[c+\frac{3 d x}{2}\right] + 118 A \sin\left[2 c+\frac{3 d x}{2}\right] - 63 B \sin\left[2 c+\frac{3 d x}{2}\right] + 36 C \sin\left[2 c+\frac{3 d x}{2}\right] + \\
 30 A \sin\left[2 c+\frac{5 d x}{2}\right] - 15 B \sin\left[2 c+\frac{5 d x}{2}\right] + 12 C \sin\left[2 c+\frac{5 d x}{2}\right] + 30 A \sin\left[3 c+\frac{5 d x}{2}\right] - \\
 15 B \sin\left[3 c+\frac{5 d x}{2}\right] + 12 C \sin\left[3 c+\frac{5 d x}{2}\right] - 3 A \sin\left[3 c+\frac{7 d x}{2}\right] + 3 B \sin\left[3 c+\frac{7 d x}{2}\right] - \\
 \left. 3 A \sin\left[4 c+\frac{7 d x}{2}\right] + 3 B \sin\left[4 c+\frac{7 d x}{2}\right] + A \sin\left[4 c+\frac{9 d x}{2}\right] + A \sin\left[5 c+\frac{9 d x}{2}\right] \right)$$

**Problem 466: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c+d x]^4 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2)}{(a+a \operatorname{Sec}[c+d x])^3} d x$$

Optimal (type 3, 216 leaves, 8 steps):

$$\frac{(2 A-6 B+13 C) \operatorname{ArcTanh}[\operatorname{Sin}[c+d x]]}{2 a^3 d} - \frac{2(11 A-36 B+76 C) \operatorname{Tan}[c+d x]}{15 a^3 d} + \\
 \frac{(2 A-6 B+13 C) \operatorname{Sec}[c+d x] \operatorname{Tan}[c+d x]}{2 a^3 d} - \frac{(A-B+C) \operatorname{Sec}[c+d x]^4 \operatorname{Tan}[c+d x]}{5 d (a+a \operatorname{Sec}[c+d x])^3} - \\
 \frac{(A-6 B+11 C) \operatorname{Sec}[c+d x]^3 \operatorname{Tan}[c+d x]}{15 a d (a+a \operatorname{Sec}[c+d x])^2} - \frac{(11 A-36 B+76 C) \operatorname{Sec}[c+d x]^2 \operatorname{Tan}[c+d x]}{15 d (a^3+a^3 \operatorname{Sec}[c+d x])}$$

Result (type 3, 1081 leaves):

$$\begin{aligned}
 & - \left( \left( 8 (2A - 6B + 13C) \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \right. \right. \\
 & \quad \left. \left. \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \sec[c + dx] (A + B \sec[c + dx] + C \sec^2[c + dx]^2) \right) \right) / \\
 & \quad \left( d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) (a + a \sec[c + dx])^3 \right) + \\
 & \left( 8 (2A - 6B + 13C) \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \right. \\
 & \quad \left. \sec[c + dx] (A + B \sec[c + dx] + C \sec^2[c + dx]^2) \right) / \\
 & \quad \left( d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) (a + a \sec[c + dx])^3 \right) + \\
 & \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right] \sec\left[\frac{c}{2}\right] \sec[c] \sec^3[c + dx] (A + B \sec[c + dx] + C \sec^2[c + dx]^2) \right. \\
 & \quad \left( 490A \sin\left[\frac{dx}{2}\right] - 870B \sin\left[\frac{dx}{2}\right] + 1235C \sin\left[\frac{dx}{2}\right] - 530A \sin\left[\frac{3dx}{2}\right] + 1830B \sin\left[\frac{3dx}{2}\right] - \right. \\
 & \quad 3805C \sin\left[\frac{3dx}{2}\right] + 654A \sin\left[c - \frac{dx}{2}\right] - 2094B \sin\left[c - \frac{dx}{2}\right] + 4329C \sin\left[c - \frac{dx}{2}\right] - \\
 & \quad 654A \sin\left[c + \frac{dx}{2}\right] + 1314B \sin\left[c + \frac{dx}{2}\right] - 1989C \sin\left[c + \frac{dx}{2}\right] + 490A \sin\left[2c + \frac{dx}{2}\right] - \\
 & \quad 1650B \sin\left[2c + \frac{dx}{2}\right] + 3575C \sin\left[2c + \frac{dx}{2}\right] + 350A \sin\left[c + \frac{3dx}{2}\right] - 450B \sin\left[c + \frac{3dx}{2}\right] + \\
 & \quad 475C \sin\left[c + \frac{3dx}{2}\right] - 530A \sin\left[2c + \frac{3dx}{2}\right] + 1230B \sin\left[2c + \frac{3dx}{2}\right] - 2005C \sin\left[2c + \frac{3dx}{2}\right] + \\
 & \quad 350A \sin\left[3c + \frac{3dx}{2}\right] - 1050B \sin\left[3c + \frac{3dx}{2}\right] + 2275C \sin\left[3c + \frac{3dx}{2}\right] - \\
 & \quad 378A \sin\left[c + \frac{5dx}{2}\right] + 1278B \sin\left[c + \frac{5dx}{2}\right] - 2673C \sin\left[c + \frac{5dx}{2}\right] + 150A \sin\left[2c + \frac{5dx}{2}\right] - \\
 & \quad 90B \sin\left[2c + \frac{5dx}{2}\right] - 105C \sin\left[2c + \frac{5dx}{2}\right] - 378A \sin\left[3c + \frac{5dx}{2}\right] + 918B \sin\left[3c + \frac{5dx}{2}\right] - \\
 & \quad 1593C \sin\left[3c + \frac{5dx}{2}\right] + 150A \sin\left[4c + \frac{5dx}{2}\right] - 450B \sin\left[4c + \frac{5dx}{2}\right] + \\
 & \quad 975C \sin\left[4c + \frac{5dx}{2}\right] - 190A \sin\left[2c + \frac{7dx}{2}\right] + 630B \sin\left[2c + \frac{7dx}{2}\right] - \\
 & \quad 1325C \sin\left[2c + \frac{7dx}{2}\right] + 30A \sin\left[3c + \frac{7dx}{2}\right] + 60B \sin\left[3c + \frac{7dx}{2}\right] - 255C \sin\left[3c + \frac{7dx}{2}\right] - \\
 & \quad 190A \sin\left[4c + \frac{7dx}{2}\right] + 480B \sin\left[4c + \frac{7dx}{2}\right] - 875C \sin\left[4c + \frac{7dx}{2}\right] + \\
 & \quad 30A \sin\left[5c + \frac{7dx}{2}\right] - 90B \sin\left[5c + \frac{7dx}{2}\right] + 195C \sin\left[5c + \frac{7dx}{2}\right] - 44A \sin\left[3c + \frac{9dx}{2}\right] + \\
 & \quad 144B \sin\left[3c + \frac{9dx}{2}\right] - 304C \sin\left[3c + \frac{9dx}{2}\right] + 30B \sin\left[4c + \frac{9dx}{2}\right] - 90C \sin\left[4c + \frac{9dx}{2}\right] - \\
 & \quad \left. \left. 44A \sin\left[5c + \frac{9dx}{2}\right] + 114B \sin\left[5c + \frac{9dx}{2}\right] - 214C \sin\left[5c + \frac{9dx}{2}\right] \right) \right) / \\
 & \quad \left( 240d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) (a + a \sec[c + dx])^3 \right)
 \end{aligned}$$

**Problem 467: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Sec}[c + d x]^3 (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2)}{(a + a \text{Sec}[c + d x])^3} dx$$

Optimal (type 3, 161 leaves, 7 steps):

$$\frac{(B - 3 C) \text{ArcTanh}[\text{Sin}[c + d x]]}{a^3 d} + \frac{(2 A - 7 B + 27 C) \text{Tan}[c + d x]}{15 a^3 d} - \frac{(A - B + C) \text{Sec}[c + d x]^3 \text{Tan}[c + d x]}{5 d (a + a \text{Sec}[c + d x])^3} + \frac{(A + 4 B - 9 C) \text{Sec}[c + d x]^2 \text{Tan}[c + d x]}{15 a d (a + a \text{Sec}[c + d x])^2} - \frac{(B - 3 C) \text{Tan}[c + d x]}{d (a^3 + a^3 \text{Sec}[c + d x])}$$

Result (type 3, 839 leaves):

$$\begin{aligned} & \left( 16 (-B + 3 C) \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^6 \right. \\ & \quad \left. \log \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] - \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right] \sec [c + dx] (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) / \\ & \left( d (A + 2 C + 2 B \cos [c + dx] + A \cos [2 c + 2 dx]) (a + a \sec [c + dx])^3 \right) - \\ & \left( 16 (-B + 3 C) \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^6 \log \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] + \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right] \right. \\ & \quad \left. \sec [c + dx] (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) / \\ & \left( d (A + 2 C + 2 B \cos [c + dx] + A \cos [2 c + 2 dx]) (a + a \sec [c + dx])^3 \right) + \\ & \left( \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] \sec \left[ \frac{c}{2} \right] \sec [c] \sec [c + dx]^2 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right. \\ & \quad \left( -20 A \sin \left[ \frac{dx}{2} \right] + 160 B \sin \left[ \frac{dx}{2} \right] - 255 C \sin \left[ \frac{dx}{2} \right] + 22 A \sin \left[ \frac{3 dx}{2} \right] - 167 B \sin \left[ \frac{3 dx}{2} \right] + \right. \\ & \quad 567 C \sin \left[ \frac{3 dx}{2} \right] - 10 A \sin \left[ c - \frac{dx}{2} \right] + 170 B \sin \left[ c - \frac{dx}{2} \right] - 600 C \sin \left[ c - \frac{dx}{2} \right] + \\ & \quad 10 A \sin \left[ c + \frac{dx}{2} \right] - 170 B \sin \left[ c + \frac{dx}{2} \right] + 375 C \sin \left[ c + \frac{dx}{2} \right] - 20 A \sin \left[ 2 c + \frac{dx}{2} \right] + \\ & \quad 160 B \sin \left[ 2 c + \frac{dx}{2} \right] - 480 C \sin \left[ 2 c + \frac{dx}{2} \right] + 75 B \sin \left[ c + \frac{3 dx}{2} \right] - 60 C \sin \left[ c + \frac{3 dx}{2} \right] + \\ & \quad 22 A \sin \left[ 2 c + \frac{3 dx}{2} \right] - 167 B \sin \left[ 2 c + \frac{3 dx}{2} \right] + 402 C \sin \left[ 2 c + \frac{3 dx}{2} \right] + \\ & \quad 75 B \sin \left[ 3 c + \frac{3 dx}{2} \right] - 225 C \sin \left[ 3 c + \frac{3 dx}{2} \right] + 10 A \sin \left[ c + \frac{5 dx}{2} \right] - 95 B \sin \left[ c + \frac{5 dx}{2} \right] + \\ & \quad 315 C \sin \left[ c + \frac{5 dx}{2} \right] + 15 B \sin \left[ 2 c + \frac{5 dx}{2} \right] + 30 C \sin \left[ 2 c + \frac{5 dx}{2} \right] + 10 A \sin \left[ 3 c + \frac{5 dx}{2} \right] - \\ & \quad 95 B \sin \left[ 3 c + \frac{5 dx}{2} \right] + 240 C \sin \left[ 3 c + \frac{5 dx}{2} \right] + 15 B \sin \left[ 4 c + \frac{5 dx}{2} \right] - 45 C \sin \left[ 4 c + \frac{5 dx}{2} \right] + \\ & \quad 2 A \sin \left[ 2 c + \frac{7 dx}{2} \right] - 22 B \sin \left[ 2 c + \frac{7 dx}{2} \right] + 72 C \sin \left[ 2 c + \frac{7 dx}{2} \right] + 15 C \sin \left[ 3 c + \frac{7 dx}{2} \right] + \\ & \quad \left. \left. 2 A \sin \left[ 4 c + \frac{7 dx}{2} \right] - 22 B \sin \left[ 4 c + \frac{7 dx}{2} \right] + 57 C \sin \left[ 4 c + \frac{7 dx}{2} \right] \right) \right) / \\ & \left( 60 d (A + 2 C + 2 B \cos [c + dx] + A \cos [2 c + 2 dx]) (a + a \sec [c + dx])^3 \right) \end{aligned}$$

**Problem 468: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c + dx]^2 (A + B \sec [c + dx] + C \sec [c + dx]^2)}{(a + a \sec [c + dx])^3} dx$$

Optimal (type 3, 132 leaves, 5 steps):

$$\begin{aligned} & \frac{C \operatorname{ArcTanh}[\sin [c + dx]]}{a^3 d} - \frac{(A - B + C) \sec [c + dx]^2 \tan [c + dx]}{5 d (a + a \sec [c + dx])^3} - \\ & \frac{(3 A + 2 B - 7 C) \tan [c + dx]}{15 a d (a + a \sec [c + dx])^2} + \frac{(6 A + 4 B - 29 C) \tan [c + dx]}{15 d (a^3 + a^3 \sec [c + dx])} \end{aligned}$$



Result (type 3, 277 leaves):

$$\begin{aligned}
 & - \left( \left( (C + B \cos [c + dx] + A \cos [c + dx]^2) \left( 240 C \cos \left[ \frac{1}{2} (c + dx) \right]^6 \right. \right. \right. \\
 & \quad \left. \left. \left( \log \left[ \cos \left[ \frac{1}{2} (c + dx) \right] - \sin \left[ \frac{1}{2} (c + dx) \right] \right] - \log \left[ \cos \left[ \frac{1}{2} (c + dx) \right] + \sin \left[ \frac{1}{2} (c + dx) \right] \right] \right) - \right. \right. \\
 & \quad \left. \cos \left[ \frac{1}{2} (c + dx) \right] \sec \left[ \frac{c}{2} \right] \left( 5 (3A + 4B - 29C) \sin \left[ \frac{dx}{2} \right] - 15 (A - 5C) \sin \left[ c + \frac{dx}{2} \right] + \right. \right. \\
 & \quad \left. 15A \sin \left[ c + \frac{3dx}{2} \right] + 10B \sin \left[ c + \frac{3dx}{2} \right] - 95C \sin \left[ c + \frac{3dx}{2} \right] + 15C \sin \left[ 2c + \frac{3dx}{2} \right] + \right. \\
 & \quad \left. \left. \left. 3A \sin \left[ 2c + \frac{5dx}{2} \right] + 2B \sin \left[ 2c + \frac{5dx}{2} \right] - 22C \sin \left[ 2c + \frac{5dx}{2} \right] \right) \right) \right) / \\
 & \left( 15 a^3 d (1 + \cos [c + dx])^3 (A + 2C + 2B \cos [c + dx] + A \cos [2(c + dx)]) \right)
 \end{aligned}$$

**Problem 470: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec [c + dx] + C \sec [c + dx]^2}{(a + a \sec [c + dx])^3} dx$$

Optimal (type 3, 115 leaves, 4 steps):

$$\frac{Ax}{a^3} - \frac{(A - B + C) \tan [c + dx]}{5d (a + a \sec [c + dx])^3} - \frac{(7A - 2B - 3C) \tan [c + dx]}{15ad (a + a \sec [c + dx])^2} - \frac{(22A - 2B - 3C) \tan [c + dx]}{15d (a^3 + a^3 \sec [c + dx])}$$

Result (type 3, 289 leaves):

$$\begin{aligned}
 & \frac{1}{480 a^3 d} \\
 & \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{1}{2} (c + dx) \right]^5 \left( 150 A dx \cos \left[ \frac{dx}{2} \right] + 150 A dx \cos \left[ c + \frac{dx}{2} \right] + 75 A dx \cos \left[ c + \frac{3dx}{2} \right] + \right. \\
 & \quad 75 A dx \cos \left[ 2c + \frac{3dx}{2} \right] + 15 A dx \cos \left[ 2c + \frac{5dx}{2} \right] + 15 A dx \cos \left[ 3c + \frac{5dx}{2} \right] - 370 A \sin \left[ \frac{dx}{2} \right] + \\
 & \quad 80 B \sin \left[ \frac{dx}{2} \right] + 30 C \sin \left[ \frac{dx}{2} \right] + 270 A \sin \left[ c + \frac{dx}{2} \right] - 60 B \sin \left[ c + \frac{dx}{2} \right] - 30 C \sin \left[ c + \frac{dx}{2} \right] - \\
 & \quad 230 A \sin \left[ c + \frac{3dx}{2} \right] + 40 B \sin \left[ c + \frac{3dx}{2} \right] + 30 C \sin \left[ c + \frac{3dx}{2} \right] + 90 A \sin \left[ 2c + \frac{3dx}{2} \right] - \\
 & \quad \left. 30 B \sin \left[ 2c + \frac{3dx}{2} \right] - 64 A \sin \left[ 2c + \frac{5dx}{2} \right] + 14 B \sin \left[ 2c + \frac{5dx}{2} \right] + 6 C \sin \left[ 2c + \frac{5dx}{2} \right] \right)
 \end{aligned}$$

**Problem 471: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos [c + dx] (A + B \sec [c + dx] + C \sec [c + dx]^2)}{(a + a \sec [c + dx])^3} dx$$

Optimal (type 3, 141 leaves, 6 steps):

$$-\frac{(3A-B)x}{a^3} + \frac{2(36A-11B+C)\sin[c+dx]}{15a^3d} - \frac{(A-B+C)\sin[c+dx]}{5d(a+a\sec[c+dx])^3} - \frac{(9A-4B-C)\sin[c+dx]}{15ad(a+a\sec[c+dx])^2} - \frac{(3A-B)\sin[c+dx]}{d(a^3+a^3\sec[c+dx])}$$

Result (type 3, 419 leaves):

$$\frac{1}{960a^3d} \sec\left[\frac{c}{2}\right] \sec\left[\frac{1}{2}(c+dx)\right]^5 \left( -300(3A-B)dx \cos\left[\frac{dx}{2}\right] - 300(3A-B)dx \cos\left[c+\frac{dx}{2}\right] - 450Adx \cos\left[c+\frac{3dx}{2}\right] + 150Bdx \cos\left[c+\frac{3dx}{2}\right] - 450Adx \cos\left[2c+\frac{3dx}{2}\right] + 150Bdx \cos\left[2c+\frac{3dx}{2}\right] - 90Adx \cos\left[2c+\frac{5dx}{2}\right] + 30Bdx \cos\left[2c+\frac{5dx}{2}\right] - 90Adx \cos\left[3c+\frac{5dx}{2}\right] + 30Bdx \cos\left[3c+\frac{5dx}{2}\right] + 1755A \sin\left[\frac{dx}{2}\right] - 740B \sin\left[\frac{dx}{2}\right] + 160C \sin\left[\frac{dx}{2}\right] - 1125A \sin\left[c+\frac{dx}{2}\right] + 540B \sin\left[c+\frac{dx}{2}\right] - 120C \sin\left[c+\frac{dx}{2}\right] + 1215A \sin\left[c+\frac{3dx}{2}\right] - 460B \sin\left[c+\frac{3dx}{2}\right] + 80C \sin\left[c+\frac{3dx}{2}\right] - 225A \sin\left[2c+\frac{3dx}{2}\right] + 180B \sin\left[2c+\frac{3dx}{2}\right] - 60C \sin\left[2c+\frac{3dx}{2}\right] + 363A \sin\left[2c+\frac{5dx}{2}\right] - 128B \sin\left[2c+\frac{5dx}{2}\right] + 28C \sin\left[2c+\frac{5dx}{2}\right] + 75A \sin\left[3c+\frac{5dx}{2}\right] + 15A \sin\left[3c+\frac{7dx}{2}\right] + 15A \sin\left[4c+\frac{7dx}{2}\right] \right)$$

**Problem 472: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c+dx]^2 (A+B \sec[c+dx] + C \sec[c+dx]^2)}{(a+a \sec[c+dx])^3} dx$$

Optimal (type 3, 201 leaves, 7 steps):

$$\frac{(13A-6B+2C)x}{2a^3} - \frac{2(76A-36B+11C)\sin[c+dx]}{15a^3d} + \frac{(13A-6B+2C)\cos[c+dx]\sin[c+dx]}{2a^3d} - \frac{(A-B+C)\cos[c+dx]\sin[c+dx]}{5d(a+a\sec[c+dx])^3} - \frac{(11A-6B+C)\cos[c+dx]\sin[c+dx]}{15ad(a+a\sec[c+dx])^2} - \frac{(76A-36B+11C)\cos[c+dx]\sin[c+dx]}{15d(a^3+a^3\sec[c+dx])}$$

Result (type 3, 557 leaves):

$$\frac{1}{3840 a^3 d} \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^5$$

$$\left(600(13A-6B+2C)dx \operatorname{Cos}\left[\frac{dx}{2}\right] + 600(13A-6B+2C)dx \operatorname{Cos}\left[c+\frac{dx}{2}\right] +\right.$$

$$3900A dx \operatorname{Cos}\left[c+\frac{3dx}{2}\right] - 1800B dx \operatorname{Cos}\left[c+\frac{3dx}{2}\right] + 600C dx \operatorname{Cos}\left[c+\frac{3dx}{2}\right] +$$

$$3900A dx \operatorname{Cos}\left[2c+\frac{3dx}{2}\right] - 1800B dx \operatorname{Cos}\left[2c+\frac{3dx}{2}\right] + 600C dx \operatorname{Cos}\left[2c+\frac{3dx}{2}\right] +$$

$$780A dx \operatorname{Cos}\left[2c+\frac{5dx}{2}\right] - 360B dx \operatorname{Cos}\left[2c+\frac{5dx}{2}\right] + 120C dx \operatorname{Cos}\left[2c+\frac{5dx}{2}\right] +$$

$$780A dx \operatorname{Cos}\left[3c+\frac{5dx}{2}\right] - 360B dx \operatorname{Cos}\left[3c+\frac{5dx}{2}\right] + 120C dx \operatorname{Cos}\left[3c+\frac{5dx}{2}\right] -$$

$$12760A \operatorname{Sin}\left[\frac{dx}{2}\right] + 7020B \operatorname{Sin}\left[\frac{dx}{2}\right] - 2960C \operatorname{Sin}\left[\frac{dx}{2}\right] + 7560A \operatorname{Sin}\left[c+\frac{dx}{2}\right] -$$

$$4500B \operatorname{Sin}\left[c+\frac{dx}{2}\right] + 2160C \operatorname{Sin}\left[c+\frac{dx}{2}\right] - 9230A \operatorname{Sin}\left[c+\frac{3dx}{2}\right] + 4860B \operatorname{Sin}\left[c+\frac{3dx}{2}\right] -$$

$$1840C \operatorname{Sin}\left[c+\frac{3dx}{2}\right] + 930A \operatorname{Sin}\left[2c+\frac{3dx}{2}\right] - 900B \operatorname{Sin}\left[2c+\frac{3dx}{2}\right] + 720C \operatorname{Sin}\left[2c+\frac{3dx}{2}\right] -$$

$$2782A \operatorname{Sin}\left[2c+\frac{5dx}{2}\right] + 1452B \operatorname{Sin}\left[2c+\frac{5dx}{2}\right] - 512C \operatorname{Sin}\left[2c+\frac{5dx}{2}\right] -$$

$$750A \operatorname{Sin}\left[3c+\frac{5dx}{2}\right] + 300B \operatorname{Sin}\left[3c+\frac{5dx}{2}\right] - 105A \operatorname{Sin}\left[3c+\frac{7dx}{2}\right] + 60B \operatorname{Sin}\left[3c+\frac{7dx}{2}\right] -$$

$$105A \operatorname{Sin}\left[4c+\frac{7dx}{2}\right] + 60B \operatorname{Sin}\left[4c+\frac{7dx}{2}\right] + 15A \operatorname{Sin}\left[4c+\frac{9dx}{2}\right] + 15A \operatorname{Sin}\left[5c+\frac{9dx}{2}\right] \left.)\right)$$

**Problem 473: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Cos}[c+dx]^3 (A+B \operatorname{Sec}[c+dx]+C \operatorname{Sec}[c+dx]^2)}{(a+a \operatorname{Sec}[c+dx])^3} dx$$

Optimal (type 3, 237 leaves, 8 steps):

$$-\frac{(23A-13B+6C)x}{2a^3} + \frac{4(34A-19B+9C)\operatorname{Sin}[c+dx]}{5a^3d} - \frac{(23A-13B+6C)\operatorname{Cos}[c+dx]\operatorname{Sin}[c+dx]}{2a^3d}$$

$$\frac{(A-B+C)\operatorname{Cos}[c+dx]^2\operatorname{Sin}[c+dx]}{5d(a+a \operatorname{Sec}[c+dx])^3} - \frac{(13A-8B+3C)\operatorname{Cos}[c+dx]^2\operatorname{Sin}[c+dx]}{15ad(a+a \operatorname{Sec}[c+dx])^2}$$

$$\frac{(23A-13B+6C)\operatorname{Cos}[c+dx]^2\operatorname{Sin}[c+dx]}{3d(a^3+a^3 \operatorname{Sec}[c+dx])} - \frac{4(34A-19B+9C)\operatorname{Sin}[c+dx]^3}{15a^3d}$$

Result (type 3, 655 leaves):

$$\frac{1}{3840 a^3 d} \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^5$$

$$\left(-600(23 A-13 B+6 C) d x \operatorname{Cos}\left[\frac{d x}{2}\right]-600(23 A-13 B+6 C) d x \operatorname{Cos}\left[c+\frac{d x}{2}\right]-\right.$$

$$6900 A d x \operatorname{Cos}\left[c+\frac{3 d x}{2}\right]+3900 B d x \operatorname{Cos}\left[c+\frac{3 d x}{2}\right]-1800 C d x \operatorname{Cos}\left[c+\frac{3 d x}{2}\right]-$$

$$6900 A d x \operatorname{Cos}\left[2 c+\frac{3 d x}{2}\right]+3900 B d x \operatorname{Cos}\left[2 c+\frac{3 d x}{2}\right]-1800 C d x \operatorname{Cos}\left[2 c+\frac{3 d x}{2}\right]-$$

$$1380 A d x \operatorname{Cos}\left[2 c+\frac{5 d x}{2}\right]+780 B d x \operatorname{Cos}\left[2 c+\frac{5 d x}{2}\right]-360 C d x \operatorname{Cos}\left[2 c+\frac{5 d x}{2}\right]-$$

$$1380 A d x \operatorname{Cos}\left[3 c+\frac{5 d x}{2}\right]+780 B d x \operatorname{Cos}\left[3 c+\frac{5 d x}{2}\right]-360 C d x \operatorname{Cos}\left[3 c+\frac{5 d x}{2}\right]+$$

$$20410 A \operatorname{Sin}\left[\frac{d x}{2}\right]-12760 B \operatorname{Sin}\left[\frac{d x}{2}\right]+7020 C \operatorname{Sin}\left[\frac{d x}{2}\right]-11110 A \operatorname{Sin}\left[c+\frac{d x}{2}\right]+$$

$$7560 B \operatorname{Sin}\left[c+\frac{d x}{2}\right]-4500 C \operatorname{Sin}\left[c+\frac{d x}{2}\right]+15380 A \operatorname{Sin}\left[c+\frac{3 d x}{2}\right]-9230 B \operatorname{Sin}\left[c+\frac{3 d x}{2}\right]+$$

$$4860 C \operatorname{Sin}\left[c+\frac{3 d x}{2}\right]-380 A \operatorname{Sin}\left[2 c+\frac{3 d x}{2}\right]+930 B \operatorname{Sin}\left[2 c+\frac{3 d x}{2}\right]-900 C \operatorname{Sin}\left[2 c+\frac{3 d x}{2}\right]+$$

$$4777 A \operatorname{Sin}\left[2 c+\frac{5 d x}{2}\right]-2782 B \operatorname{Sin}\left[2 c+\frac{5 d x}{2}\right]+1452 C \operatorname{Sin}\left[2 c+\frac{5 d x}{2}\right]+$$

$$1625 A \operatorname{Sin}\left[3 c+\frac{5 d x}{2}\right]-750 B \operatorname{Sin}\left[3 c+\frac{5 d x}{2}\right]+300 C \operatorname{Sin}\left[3 c+\frac{5 d x}{2}\right]+$$

$$230 A \operatorname{Sin}\left[3 c+\frac{7 d x}{2}\right]-105 B \operatorname{Sin}\left[3 c+\frac{7 d x}{2}\right]+60 C \operatorname{Sin}\left[3 c+\frac{7 d x}{2}\right]+230 A \operatorname{Sin}\left[4 c+\frac{7 d x}{2}\right]-$$

$$105 B \operatorname{Sin}\left[4 c+\frac{7 d x}{2}\right]+60 C \operatorname{Sin}\left[4 c+\frac{7 d x}{2}\right]-20 A \operatorname{Sin}\left[4 c+\frac{9 d x}{2}\right]+15 B \operatorname{Sin}\left[4 c+\frac{9 d x}{2}\right]-$$

$$20 A \operatorname{Sin}\left[5 c+\frac{9 d x}{2}\right]+15 B \operatorname{Sin}\left[5 c+\frac{9 d x}{2}\right]+5 A \operatorname{Sin}\left[5 c+\frac{11 d x}{2}\right]+5 A \operatorname{Sin}\left[6 c+\frac{11 d x}{2}\right]\left.)\right)$$

**Problem 474: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c+d x]^5 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2)}{(a+a \operatorname{Sec}[c+d x])^4} d x$$

Optimal (type 3, 254 leaves, 9 steps):

$$\frac{(2 A-8 B+21 C) \operatorname{ArcTanh}[\operatorname{Sin}[c+d x]]}{2 a^4 d}$$

$$+\frac{8(20 A-83 B+216 C) \operatorname{Tan}[c+d x]}{105 a^4 d}+\frac{(2 A-8 B+21 C) \operatorname{Sec}[c+d x] \operatorname{Tan}[c+d x]}{2 a^4 d}$$

$$-\frac{(10 A-52 B+129 C) \operatorname{Sec}[c+d x]^3 \operatorname{Tan}[c+d x]}{105 a^4 d(1+\operatorname{Sec}[c+d x])^2}-\frac{4(20 A-83 B+216 C) \operatorname{Sec}[c+d x]^2 \operatorname{Tan}[c+d x]}{105 a^4 d(1+\operatorname{Sec}[c+d x])}$$

$$+\frac{(A-B+C) \operatorname{Sec}[c+d x]^5 \operatorname{Tan}[c+d x]}{7 d(a+a \operatorname{Sec}[c+d x])^4}+\frac{(B-2 C) \operatorname{Sec}[c+d x]^4 \operatorname{Tan}[c+d x]}{5 a d(a+a \operatorname{Sec}[c+d x])^3}$$

Result (type 3, 1322 leaves):

$$\begin{aligned}
 & - \left( \left( 16 (2A - 8B + 21C) \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^8 \right. \right. \\
 & \quad \left. \left. \log \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] - \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right] \sec [c + dx]^2 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) \right) / \\
 & \quad \left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) (a + a \sec [c + dx])^4 \right) + \\
 & \left( 16 (2A - 8B + 21C) \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^8 \log \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] + \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right] \right. \\
 & \quad \left. \sec [c + dx]^2 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) / \\
 & \quad \left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) (a + a \sec [c + dx])^4 \right) - \\
 & \left( 4 \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \sec \left[ \frac{c}{2} \right] \sec [c + dx]^2 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right. \\
 & \quad \left. \left( A \sin \left[ \frac{c}{2} \right] - B \sin \left[ \frac{c}{2} \right] + C \sin \left[ \frac{c}{2} \right] \right) \right) / \\
 & \quad \left( 7d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) (a + a \sec [c + dx])^4 \right) - \\
 & \left( 8 \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 \sec \left[ \frac{c}{2} \right] \sec [c + dx]^2 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right. \\
 & \quad \left. \left( 10A \sin \left[ \frac{c}{2} \right] - 17B \sin \left[ \frac{c}{2} \right] + 24C \sin \left[ \frac{c}{2} \right] \right) \right) / \\
 & \quad \left( 35d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) (a + a \sec [c + dx])^4 \right) - \\
 & \left( 16 \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^6 \sec \left[ \frac{c}{2} \right] \sec [c + dx]^2 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right. \\
 & \quad \left. \left( 55A \sin \left[ \frac{c}{2} \right] - 139B \sin \left[ \frac{c}{2} \right] + 258C \sin \left[ \frac{c}{2} \right] \right) \right) / \\
 & \quad \left( 105d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) (a + a \sec [c + dx])^4 \right) - \\
 & \left( 4 \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] \sec \left[ \frac{c}{2} \right] \sec [c + dx]^2 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right. \\
 & \quad \left. \left( A \sin \left[ \frac{dx}{2} \right] - B \sin \left[ \frac{dx}{2} \right] + C \sin \left[ \frac{dx}{2} \right] \right) \right) / \\
 & \quad \left( 7d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) (a + a \sec [c + dx])^4 \right) - \\
 & \left( 8 \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^3 \sec \left[ \frac{c}{2} \right] \sec [c + dx]^2 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right. \\
 & \quad \left. \left( 10A \sin \left[ \frac{dx}{2} \right] - 17B \sin \left[ \frac{dx}{2} \right] + 24C \sin \left[ \frac{dx}{2} \right] \right) \right) / \\
 & \quad \left( 35d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) (a + a \sec [c + dx])^4 \right) - \\
 & \left( 16 \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^5 \sec \left[ \frac{c}{2} \right] \sec [c + dx]^2 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right. \\
 & \quad \left. \left( 55A \sin \left[ \frac{dx}{2} \right] - 139B \sin \left[ \frac{dx}{2} \right] + 258C \sin \left[ \frac{dx}{2} \right] \right) \right) / \\
 & \quad \left( 105d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) (a + a \sec [c + dx])^4 \right) - \\
 & \left( 32 \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^7 \sec \left[ \frac{c}{2} \right] \sec [c + dx]^2 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right. \\
 & \quad \left. \left( 160A \sin \left[ \frac{dx}{2} \right] - 559B \sin \left[ \frac{dx}{2} \right] + 1308C \sin \left[ \frac{dx}{2} \right] \right) \right) /
 \end{aligned}$$

$$\begin{aligned} & \left( 105 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^4 \right) + \\ & \left( 16 C \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 \sec [c] \sec [c + d x]^4 (A + B \sec [c + d x] + C \sec [c + d x]^2) \sin [d x] \right) / \\ & \left( d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^4 \right) + \\ & \left( 16 \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 \sec [c] \sec [c + d x]^3 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\ & \quad \left. (C \sin [c] + 2 B \sin [d x] - 8 C \sin [d x]) \right) / \\ & \left( d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^4 \right) \end{aligned}$$

### Problem 475: Result more than twice size of optimal antiderivative.

$$\int \frac{\sec [c + d x]^4 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{(a + a \sec [c + d x])^4} dx$$

Optimal (type 3, 204 leaves, 8 steps):

$$\begin{aligned} & \frac{(B - 4 C) \operatorname{ArcTanh}[\sin [c + d x]]}{a^4 d} + \frac{(6 A - 55 B + 244 C) \tan [c + d x]}{105 a^4 d} + \\ & \frac{(3 A + 25 B - 88 C) \sec [c + d x]^2 \tan [c + d x]}{105 a^4 d (1 + \sec [c + d x])^2} - \frac{(B - 4 C) \tan [c + d x]}{a^4 d (1 + \sec [c + d x])} - \\ & \frac{(A - B + C) \sec [c + d x]^4 \tan [c + d x]}{7 d (a + a \sec [c + d x])^4} + \frac{(2 A + 5 B - 12 C) \sec [c + d x]^3 \tan [c + d x]}{35 a d (a + a \sec [c + d x])^3} \end{aligned}$$

Result (type 3, 1208 leaves):

$$\begin{aligned} & \left( 32 (-B + 4 C) \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 \log \left[ \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right] \right. \\ & \quad \left. \sec [c + d x]^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \\ & \left( d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^4 \right) - \\ & \left( 32 (-B + 4 C) \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 \log \left[ \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right] \right. \\ & \quad \left. \sec [c + d x]^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \\ & \left( d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^4 \right) + \\ & \left( 4 \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \sec \left[ \frac{c}{2} \right] \sec [c + d x]^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\ & \quad \left. \left( A \sin \left[ \frac{c}{2} \right] - B \sin \left[ \frac{c}{2} \right] + C \sin \left[ \frac{c}{2} \right] \right) \right) / \\ & \left( 7 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^4 \right) + \\ & \left( 8 \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \sec \left[ \frac{c}{2} \right] \sec [c + d x]^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\ & \quad \left. \left( 3 A \sin \left[ \frac{c}{2} \right] - 10 B \sin \left[ \frac{c}{2} \right] + 17 C \sin \left[ \frac{c}{2} \right] \right) \right) / \\ & \left( 35 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^4 \right) + \end{aligned}$$

$$\begin{aligned}
 & \left( 16 \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sec\left[\frac{c}{2}\right] \sec[c+dx]^2 (A+B \sec[c+dx] + C \sec[c+dx]^2) \right. \\
 & \quad \left. \left( 6A \sin\left[\frac{c}{2}\right] - 55B \sin\left[\frac{c}{2}\right] + 139C \sin\left[\frac{c}{2}\right] \right) \right) / \\
 & \left( 105d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) (a+a \sec[c+dx])^4 \right) + \\
 & \left( 4 \cos\left[\frac{c}{2} + \frac{dx}{2}\right] \sec\left[\frac{c}{2}\right] \sec[c+dx]^2 (A+B \sec[c+dx] + C \sec[c+dx]^2) \right. \\
 & \quad \left. \left( A \sin\left[\frac{dx}{2}\right] - B \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right] \right) \right) / \\
 & \left( 7d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) (a+a \sec[c+dx])^4 \right) + \\
 & \left( 8 \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^3 \sec\left[\frac{c}{2}\right] \sec[c+dx]^2 (A+B \sec[c+dx] + C \sec[c+dx]^2) \right. \\
 & \quad \left. \left( 3A \sin\left[\frac{dx}{2}\right] - 10B \sin\left[\frac{dx}{2}\right] + 17C \sin\left[\frac{dx}{2}\right] \right) \right) / \\
 & \left( 35d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) (a+a \sec[c+dx])^4 \right) + \\
 & \left( 16 \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^5 \sec\left[\frac{c}{2}\right] \sec[c+dx]^2 (A+B \sec[c+dx] + C \sec[c+dx]^2) \right. \\
 & \quad \left. \left( 6A \sin\left[\frac{dx}{2}\right] - 55B \sin\left[\frac{dx}{2}\right] + 139C \sin\left[\frac{dx}{2}\right] \right) \right) / \\
 & \left( 105d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) (a+a \sec[c+dx])^4 \right) + \\
 & \left( 32 \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^7 \sec\left[\frac{c}{2}\right] \sec[c+dx]^2 (A+B \sec[c+dx] + C \sec[c+dx]^2) \right. \\
 & \quad \left. \left( 6A \sin\left[\frac{dx}{2}\right] - 160B \sin\left[\frac{dx}{2}\right] + 559C \sin\left[\frac{dx}{2}\right] \right) \right) / \\
 & \left( 105d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) (a+a \sec[c+dx])^4 \right) + \\
 & \left( 32C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^8 \sec[c] \sec[c+dx]^3 (A+B \sec[c+dx] + C \sec[c+dx]^2) \sin[dx] \right) / \\
 & \left( d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) (a+a \sec[c+dx])^4 \right)
 \end{aligned}$$

**Problem 479: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec[c+dx] + C \sec[c+dx]^2}{(a + a \sec[c+dx])^4} dx$$

Optimal (type 3, 148 leaves, 5 steps):

$$\begin{aligned}
 & \frac{Ax}{a^4} - \frac{(55A - 6B - 8C) \tan[c+dx]}{105a^4 d (1 + \sec[c+dx])^2} - \frac{2(80A - 3B - 4C) \tan[c+dx]}{105a^4 d (1 + \sec[c+dx])} \\
 & \frac{(A - B + C) \tan[c+dx]}{7d (a + a \sec[c+dx])^4} - \frac{(10A - 3B - 4C) \tan[c+dx]}{35a d (a + a \sec[c+dx])^3}
 \end{aligned}$$

Result (type 3, 405 leaves):

$$\frac{1}{13440 a^4 d} \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^7 \left( 3675 A dx \operatorname{Cos}\left[\frac{dx}{2}\right] + 3675 A dx \operatorname{Cos}\left[c + \frac{dx}{2}\right] + 2205 A dx \operatorname{Cos}\left[c + \frac{3dx}{2}\right] + 2205 A dx \operatorname{Cos}\left[2c + \frac{3dx}{2}\right] + 735 A dx \operatorname{Cos}\left[2c + \frac{5dx}{2}\right] + 735 A dx \operatorname{Cos}\left[3c + \frac{5dx}{2}\right] + 105 A dx \operatorname{Cos}\left[3c + \frac{7dx}{2}\right] + 105 A dx \operatorname{Cos}\left[4c + \frac{7dx}{2}\right] - 9940 A \operatorname{Sin}\left[\frac{dx}{2}\right] + 1260 B \operatorname{Sin}\left[\frac{dx}{2}\right] + 560 C \operatorname{Sin}\left[\frac{dx}{2}\right] + 8260 A \operatorname{Sin}\left[c + \frac{dx}{2}\right] - 1260 B \operatorname{Sin}\left[c + \frac{dx}{2}\right] - 350 C \operatorname{Sin}\left[c + \frac{dx}{2}\right] - 7140 A \operatorname{Sin}\left[c + \frac{3dx}{2}\right] + 882 B \operatorname{Sin}\left[c + \frac{3dx}{2}\right] + 336 C \operatorname{Sin}\left[c + \frac{3dx}{2}\right] + 3780 A \operatorname{Sin}\left[2c + \frac{3dx}{2}\right] - 630 B \operatorname{Sin}\left[2c + \frac{3dx}{2}\right] - 210 C \operatorname{Sin}\left[2c + \frac{3dx}{2}\right] - 2800 A \operatorname{Sin}\left[2c + \frac{5dx}{2}\right] + 294 B \operatorname{Sin}\left[2c + \frac{5dx}{2}\right] + 182 C \operatorname{Sin}\left[2c + \frac{5dx}{2}\right] + 840 A \operatorname{Sin}\left[3c + \frac{5dx}{2}\right] - 210 B \operatorname{Sin}\left[3c + \frac{5dx}{2}\right] - 520 A \operatorname{Sin}\left[3c + \frac{7dx}{2}\right] + 72 B \operatorname{Sin}\left[3c + \frac{7dx}{2}\right] + 26 C \operatorname{Sin}\left[3c + \frac{7dx}{2}\right] \right)$$

**Problem 480: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Cos}[c+dx] (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2)}{(a+a \operatorname{Sec}[c+dx])^4} dx$$

Optimal (type 3, 176 leaves, 7 steps):

$$-\frac{(4A-B)x}{a^4} + \frac{2(332A-80B+3C)\operatorname{Sin}[c+dx]}{105a^4d} - \frac{(88A-25B-3C)\operatorname{Sin}[c+dx]}{105a^4d(1+\operatorname{Sec}[c+dx])^2} - \frac{(4A-B)\operatorname{Sin}[c+dx]}{a^4d(1+\operatorname{Sec}[c+dx])} - \frac{(A-B+C)\operatorname{Sin}[c+dx]}{7d(a+a \operatorname{Sec}[c+dx])^4} - \frac{(12A-5B-2C)\operatorname{Sin}[c+dx]}{35ad(a+a \operatorname{Sec}[c+dx])^3}$$

Result (type 3, 567 leaves):



$$\frac{1}{26880 a^4 d} \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^7$$

$$\left(-7350(4A-B)dx \operatorname{Cos}\left[\frac{dx}{2}\right] - 7350(4A-B)dx \operatorname{Cos}\left[c + \frac{dx}{2}\right] - 17640Adx \operatorname{Cos}\left[c + \frac{3dx}{2}\right] +\right.$$

$$4410Bdx \operatorname{Cos}\left[c + \frac{3dx}{2}\right] - 17640Adx \operatorname{Cos}\left[2c + \frac{3dx}{2}\right] + 4410Bdx \operatorname{Cos}\left[2c + \frac{3dx}{2}\right] -$$

$$5880Adx \operatorname{Cos}\left[2c + \frac{5dx}{2}\right] + 1470Bdx \operatorname{Cos}\left[2c + \frac{5dx}{2}\right] - 5880Adx \operatorname{Cos}\left[3c + \frac{5dx}{2}\right] +$$

$$1470Bdx \operatorname{Cos}\left[3c + \frac{5dx}{2}\right] - 840Adx \operatorname{Cos}\left[3c + \frac{7dx}{2}\right] + 210Bdx \operatorname{Cos}\left[3c + \frac{7dx}{2}\right] -$$

$$840Adx \operatorname{Cos}\left[4c + \frac{7dx}{2}\right] + 210Bdx \operatorname{Cos}\left[4c + \frac{7dx}{2}\right] + 60830A \operatorname{Sin}\left[\frac{dx}{2}\right] -$$

$$19880B \operatorname{Sin}\left[\frac{dx}{2}\right] + 2520C \operatorname{Sin}\left[\frac{dx}{2}\right] - 46130A \operatorname{Sin}\left[c + \frac{dx}{2}\right] + 16520B \operatorname{Sin}\left[c + \frac{dx}{2}\right] -$$

$$2520C \operatorname{Sin}\left[c + \frac{dx}{2}\right] + 46116A \operatorname{Sin}\left[c + \frac{3dx}{2}\right] - 14280B \operatorname{Sin}\left[c + \frac{3dx}{2}\right] + 1764C \operatorname{Sin}\left[c + \frac{3dx}{2}\right] -$$

$$18060A \operatorname{Sin}\left[2c + \frac{3dx}{2}\right] + 7560B \operatorname{Sin}\left[2c + \frac{3dx}{2}\right] - 1260C \operatorname{Sin}\left[2c + \frac{3dx}{2}\right] +$$

$$19292A \operatorname{Sin}\left[2c + \frac{5dx}{2}\right] - 5600B \operatorname{Sin}\left[2c + \frac{5dx}{2}\right] + 588C \operatorname{Sin}\left[2c + \frac{5dx}{2}\right] -$$

$$2100A \operatorname{Sin}\left[3c + \frac{5dx}{2}\right] + 1680B \operatorname{Sin}\left[3c + \frac{5dx}{2}\right] - 420C \operatorname{Sin}\left[3c + \frac{5dx}{2}\right] +$$

$$3791A \operatorname{Sin}\left[3c + \frac{7dx}{2}\right] - 1040B \operatorname{Sin}\left[3c + \frac{7dx}{2}\right] + 144C \operatorname{Sin}\left[3c + \frac{7dx}{2}\right] +$$

$$\left.735A \operatorname{Sin}\left[4c + \frac{7dx}{2}\right] + 105A \operatorname{Sin}\left[4c + \frac{9dx}{2}\right] + 105A \operatorname{Sin}\left[5c + \frac{9dx}{2}\right]\right)$$

**Problem 481: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Cos}[c+dx]^2 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2)}{(a+a \operatorname{Sec}[c+dx])^4} dx$$

Optimal (type 3, 239 leaves, 8 steps):

$$\frac{(21A-8B+2C)x}{2a^4} - \frac{8(216A-83B+20C) \operatorname{Sin}[c+dx]}{105a^4 d} + \frac{(21A-8B+2C) \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx]}{2a^4 d}$$

$$\frac{(129A-52B+10C) \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx]}{105a^4 d (1+\operatorname{Sec}[c+dx])^2} - \frac{4(216A-83B+20C) \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx]}{105a^4 d (1+\operatorname{Sec}[c+dx])}$$

$$\frac{(A-B+C) \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx]}{7d(a+a \operatorname{Sec}[c+dx])^4} - \frac{(2A-B) \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx]}{5ad(a+a \operatorname{Sec}[c+dx])^3}$$

Result (type 3, 1290 leaves):

$$\left(16(21A-8B+2C)x \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^8 \operatorname{Sec}[c+dx]^2 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2)\right) /$$

$$\left((A+2C+2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) (a+a \operatorname{Sec}[c+dx])^4\right) +$$

$$\begin{aligned}
& \left( 4 \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \sec \left[ \frac{c}{2} \right] \sec [c + dx]^2 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right. \\
& \quad \left. \left( A \sin \left[ \frac{c}{2} \right] - B \sin \left[ \frac{c}{2} \right] + C \sin \left[ \frac{c}{2} \right] \right) \right) / \\
& \left( 7 d (A + 2 C + 2 B \cos [c + dx] + A \cos [2 c + 2 dx]) (a + a \sec [c + dx])^4 \right) - \\
& \left( 8 \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 \sec \left[ \frac{c}{2} \right] \sec [c + dx]^2 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right. \\
& \quad \left. \left( 39 A \sin \left[ \frac{c}{2} \right] - 32 B \sin \left[ \frac{c}{2} \right] + 25 C \sin \left[ \frac{c}{2} \right] \right) \right) / \\
& \left( 35 d (A + 2 C + 2 B \cos [c + dx] + A \cos [2 c + 2 dx]) (a + a \sec [c + dx])^4 \right) + \\
& \left( 16 \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^6 \sec \left[ \frac{c}{2} \right] \sec [c + dx]^2 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right. \\
& \quad \left. \left( 447 A \sin \left[ \frac{c}{2} \right] - 286 B \sin \left[ \frac{c}{2} \right] + 160 C \sin \left[ \frac{c}{2} \right] \right) \right) / \\
& \left( 105 d (A + 2 C + 2 B \cos [c + dx] + A \cos [2 c + 2 dx]) (a + a \sec [c + dx])^4 \right) + \\
& \left( 4 \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] \sec \left[ \frac{c}{2} \right] \sec [c + dx]^2 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right. \\
& \quad \left. \left( A \sin \left[ \frac{dx}{2} \right] - B \sin \left[ \frac{dx}{2} \right] + C \sin \left[ \frac{dx}{2} \right] \right) \right) / \\
& \left( 7 d (A + 2 C + 2 B \cos [c + dx] + A \cos [2 c + 2 dx]) (a + a \sec [c + dx])^4 \right) - \\
& \left( 8 \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^3 \sec \left[ \frac{c}{2} \right] \sec [c + dx]^2 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right. \\
& \quad \left. \left( 39 A \sin \left[ \frac{dx}{2} \right] - 32 B \sin \left[ \frac{dx}{2} \right] + 25 C \sin \left[ \frac{dx}{2} \right] \right) \right) / \\
& \left( 35 d (A + 2 C + 2 B \cos [c + dx] + A \cos [2 c + 2 dx]) (a + a \sec [c + dx])^4 \right) + \\
& \left( 16 \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^5 \sec \left[ \frac{c}{2} \right] \sec [c + dx]^2 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right. \\
& \quad \left. \left( 447 A \sin \left[ \frac{dx}{2} \right] - 286 B \sin \left[ \frac{dx}{2} \right] + 160 C \sin \left[ \frac{dx}{2} \right] \right) \right) / \\
& \left( 105 d (A + 2 C + 2 B \cos [c + dx] + A \cos [2 c + 2 dx]) (a + a \sec [c + dx])^4 \right) - \\
& \left( 32 \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^7 \sec \left[ \frac{c}{2} \right] \sec [c + dx]^2 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right. \\
& \quad \left. \left( 1653 A \sin \left[ \frac{dx}{2} \right] - 764 B \sin \left[ \frac{dx}{2} \right] + 260 C \sin \left[ \frac{dx}{2} \right] \right) \right) / \\
& \left( 105 d (A + 2 C + 2 B \cos [c + dx] + A \cos [2 c + 2 dx]) (a + a \sec [c + dx])^4 \right) + \\
& \left( (4 A - B) \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^8 \sec [c + dx]^2 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right. \\
& \quad \left. \left( -\frac{16 i \cos [c + dx]}{d} - \frac{16 \sin [c + dx]}{d} \right) \right) / \\
& \left( (A + 2 C + 2 B \cos [c + dx] + A \cos [2 c + 2 dx]) (a + a \sec [c + dx])^4 \right) + \\
& \left( (4 A - B) \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^8 \sec [c + dx]^2 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right. \\
& \quad \left. \left( \frac{16 i \cos [c + dx]}{d} - \frac{16 \sin [c + dx]}{d} \right) \right) / \\
& \left( (A + 2 C + 2 B \cos [c + dx] + A \cos [2 c + 2 dx]) (a + a \sec [c + dx])^4 \right) +
\end{aligned}$$

$$\left( 8 A \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^8 \sec [c + dx]^2 (A + B \sec [c + dx] + C \sec [c + dx]^2) \sin [2c + 2dx] \right) / \left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) (a + a \sec [c + dx])^4 \right)$$

**Problem 486: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sqrt{a + a \sec [c + dx]} (A + B \sec [c + dx] + C \sec [c + dx]^2) dx$$

Optimal (type 3, 100 leaves, 5 steps):

$$\frac{2 \sqrt{a} A \operatorname{ArcTan} \left[ \frac{\sqrt{a} \tan [c + dx]}{\sqrt{a + a \sec [c + dx]}} \right]}{d} + \frac{2 a (3 B + C) \tan [c + dx]}{3 d \sqrt{a + a \sec [c + dx]}} + \frac{2 C \sqrt{a + a \sec [c + dx]} \tan [c + dx]}{3 d}$$

Result (type 4, 506 leaves):

$$\left( \cos [c + dx]^2 \sec \left[ \frac{1}{2} (c + dx) \right] \sqrt{a (1 + \sec [c + dx])} (A + B \sec [c + dx] + C \sec [c + dx]^2) \left( \frac{4}{3} (3 B + 2 C) \sin \left[ \frac{1}{2} (c + dx) \right] + \frac{4}{3} C \sec [c + dx] \sin \left[ \frac{1}{2} (c + dx) \right] \right) \right) / \left( d (A + 2 C + 2 B \cos [c + dx] + A \cos [2 c + 2 d x]) \right) - \frac{1}{d (A + 2 C + 2 B \cos [c + dx] + A \cos [2 c + 2 d x])}$$

$$16 (-3 - 2 \sqrt{2}) A \cos \left[ \frac{1}{4} (c + dx) \right]^4 \sqrt{\frac{7 - 5 \sqrt{2} + (10 - 7 \sqrt{2}) \cos \left[ \frac{1}{2} (c + dx) \right]}{1 + \cos \left[ \frac{1}{2} (c + dx) \right]}}$$

$$\sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + dx) \right]}{1 + \cos \left[ \frac{1}{2} (c + dx) \right]}} \left( 1 - \sqrt{2} + (-2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + dx) \right] \right)$$

$$\cos [c + dx] \left( \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\tan \left[ \frac{1}{4} (c + dx) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] + 2 \operatorname{EllipticPi} \left[ -3 + 2 \sqrt{2}, -\operatorname{ArcSin} \left[ \frac{\tan \left[ \frac{1}{4} (c + dx) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \right)$$

$$\sqrt{\left( -1 - \sqrt{2} + (2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + dx) \right] \right) \sec \left[ \frac{1}{4} (c + dx) \right]^2 \sec \left[ \frac{1}{2} (c + dx) \right]}$$

$$\sqrt{a (1 + \sec [c + dx])} (A + B \sec [c + dx] + C \sec [c + dx]^2) \sqrt{3 - 2 \sqrt{2} - \tan \left[ \frac{1}{4} (c + dx) \right]^2}$$

**Problem 487: Result unnecessarily involves higher level functions and more**

than twice size of optimal antiderivative.

$$\int \cos [c + d x] \sqrt{a + a \sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 3, 98 leaves, 5 steps):

$$\frac{\sqrt{a} (A + 2 B) \operatorname{ArcTan} \left[ \frac{\sqrt{a} \tan [c + d x]}{\sqrt{a + a \sec [c + d x]}} \right]}{d} + \frac{A \sqrt{a + a \sec [c + d x]} \sin [c + d x]}{d} - \frac{a (A - 2 C) \tan [c + d x]}{d \sqrt{a + a \sec [c + d x]}}$$

Result (type 4, 402 leaves):

$$\begin{aligned} & \frac{1}{d} \sec \left[ \frac{1}{2} (c + d x) \right] \sqrt{a (1 + \sec [c + d x])} \left( \frac{1}{2} (-A + 4 C) \sin \left[ \frac{1}{2} (c + d x) \right] + \frac{1}{2} A \sin \left[ \frac{3}{2} (c + d x) \right] \right) - \\ & \frac{1}{d} 4 (-3 - 2 \sqrt{2}) (A + 2 B) \cos \left[ \frac{1}{4} (c + d x) \right]^4 \sqrt{\frac{7 - 5 \sqrt{2} + (10 - 7 \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right]}{1 + \cos \left[ \frac{1}{2} (c + d x) \right]}} \\ & \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right]}{1 + \cos \left[ \frac{1}{2} (c + d x) \right]}} \left( 1 - \sqrt{2} + (-2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right] \right) \\ & \left( \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\tan \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] + \right. \\ & \left. 2 \operatorname{EllipticPi} \left[ -3 + 2 \sqrt{2}, -\operatorname{ArcSin} \left[ \frac{\tan \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \right) \\ & \sqrt{\left( -1 - \sqrt{2} + (2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right] \right) \sec \left[ \frac{1}{4} (c + d x) \right]^2 \sec \left[ \frac{1}{2} (c + d x) \right]} \\ & \sec [c + d x] \sqrt{a (1 + \sec [c + d x])} \sqrt{3 - 2 \sqrt{2} - \tan \left[ \frac{1}{4} (c + d x) \right]^2} \end{aligned}$$

Problem 488: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \cos [c + d x]^2 \sqrt{a + a \sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 3, 117 leaves, 4 steps):

$$\frac{\sqrt{a} (3A + 4B + 8C) \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{4d} + \frac{a(A + 4B) \operatorname{Sin}[c+dx]}{4d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{A \operatorname{Cos}[c+dx] \sqrt{a+a \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{2d}$$

Result (type 4, 421 leaves):

$$\begin{aligned} & \frac{1}{d} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1+\operatorname{Sec}[c+dx])} \\ & \left(-\frac{1}{8}(A+4B) \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + \frac{1}{4}(A+2B) \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right] + \frac{1}{8}A \operatorname{Sin}\left[\frac{5}{2}(c+dx)\right]\right) + \\ & \frac{1}{d} \left(2 + \frac{3}{\sqrt{2}}\right) (3A + 4B + 8C) \operatorname{Cos}\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7 - 5\sqrt{2} + (10 - 7\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}{1 + \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}} \\ & \left(1 - \sqrt{2} + (-2 + \sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \left(\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] + \right. \\ & \left. 2 \operatorname{EllipticPi}\left[-3 + 2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right]\right) \\ & \sqrt{\left(-1 + \sqrt{2} - (-2 + \sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2} \\ & \sqrt{\left(-1 - \sqrt{2} + (2 + \sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]} \\ & \operatorname{Sec}[c+dx] \sqrt{a(1+\operatorname{Sec}[c+dx])} \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \end{aligned}$$

**Problem 489: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \operatorname{Cos}[c+dx]^3 \sqrt{a+a \operatorname{Sec}[c+dx]} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 3, 163 leaves, 5 steps):

$$\frac{\sqrt{a} (5A + 6B + 8C) \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{8d} + \frac{a(5A + 6B + 8C) \operatorname{Sin}[c+dx]}{8d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{a(A + 6B) \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx]}{12d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{A \operatorname{Cos}[c+dx]^2 \sqrt{a+a \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{3d}$$

Result (type 4, 452 leaves):

$$\begin{aligned} & \frac{1}{d} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1+\operatorname{Sec}[c+dx])} \\ & \left(-\frac{1}{48}(11A+6B+24C) \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + \frac{1}{12}(4A+3B+6C) \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right] + \right. \\ & \quad \left. \frac{1}{16}(A+2B) \operatorname{Sin}\left[\frac{5}{2}(c+dx)\right] + \frac{1}{24}A \operatorname{Sin}\left[\frac{7}{2}(c+dx)\right]\right) + \\ & \frac{1}{d} \left(1 + \frac{3}{2\sqrt{2}}\right) (5A+6B+8C) \operatorname{Cos}\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7-5\sqrt{2} + (10-7\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}{1+\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}} \\ & \left((1-\sqrt{2} + (-2+\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]) \left(\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] + \right. \right. \\ & \quad \left. \left. 2 \operatorname{EllipticPi}\left[-3+2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right]\right)\right) \\ & \sqrt{\left(-1+\sqrt{2} - (-2+\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2} \\ & \sqrt{\left(-1-\sqrt{2} + (2+\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]} \\ & \operatorname{Sec}[c+dx] \sqrt{a(1+\operatorname{Sec}[c+dx])} \sqrt{3-2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \end{aligned}$$

**Problem 490: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \operatorname{Cos}[c+dx]^4 \sqrt{a+a \operatorname{Sec}[c+dx]} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 3, 209 leaves, 6 steps):

$$\begin{aligned} & \frac{\sqrt{a} (35A+40B+48C) \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{64d} + \\ & \frac{a(35A+40B+48C) \operatorname{Sin}[c+dx]}{64d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{a(35A+40B+48C) \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx]}{96d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \\ & \frac{a(A+8B) \operatorname{Cos}[c+dx]^2 \operatorname{Sin}[c+dx]}{24d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{A \operatorname{Cos}[c+dx]^3 \sqrt{a+a \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{4d} \end{aligned}$$

Result (type 4, 476 leaves):

$$\begin{aligned}
 & \frac{1}{d} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1+\operatorname{Sec}[c+dx])} \\
 & \left(-\frac{1}{384}(41A+88B+48C) \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + \frac{1}{48}(11A+16B+12C) \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right] + \frac{1}{128}\right. \\
 & \quad \left.(15A+8B+16C) \operatorname{Sin}\left[\frac{5}{2}(c+dx)\right] + \frac{1}{48}(A+2B) \operatorname{Sin}\left[\frac{7}{2}(c+dx)\right] + \frac{1}{64}A \operatorname{Sin}\left[\frac{9}{2}(c+dx)\right]\right) + \\
 & \frac{1}{(-64+48\sqrt{2})d} (35A+40B+48C) \operatorname{Cos}\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7-5\sqrt{2}+(10-7\sqrt{2})\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}{1+\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}} \\
 & \left(1-\sqrt{2}+(-2+\sqrt{2})\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \left(\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] + \right. \\
 & \quad \left. 2 \operatorname{EllipticPi}\left[-3+2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right]\right) \\
 & \sqrt{\left(-1+\sqrt{2}-(-2+\sqrt{2})\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \sqrt{\left(-1-\sqrt{2}+(2+\sqrt{2})\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]} \\
 & \operatorname{Sec}[c+dx] \sqrt{a(1+\operatorname{Sec}[c+dx])} \sqrt{3-2\sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}
 \end{aligned}$$

**Problem 494: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int (a+a \operatorname{Sec}[c+dx])^{3/2} (A+B \operatorname{Sec}[c+dx]+C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 3, 142 leaves, 6 steps):

$$\begin{aligned}
 & \frac{2a^{3/2}A \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{d} + \frac{2a^2(15A+20B+12C) \operatorname{Tan}[c+dx]}{15d\sqrt{a+a \operatorname{Sec}[c+dx]}} + \\
 & \frac{2a(5B+3C)\sqrt{a+a \operatorname{Sec}[c+dx]}\operatorname{Tan}[c+dx]}{15d} + \frac{2C(a+a \operatorname{Sec}[c+dx])^{3/2}\operatorname{Tan}[c+dx]}{5d}
 \end{aligned}$$

Result (type 4, 554 leaves):

$$\begin{aligned} & \left( \cos [c+d x]^3 \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^3 (a(1+\operatorname{Sec}[c+d x]))^{3/2} (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \right. \\ & \quad \left( \frac{2}{15}(15 A+25 B+18 C) \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] + \frac{2}{5} C \operatorname{Sec}[c+d x]^2 \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] + \right. \\ & \quad \left. \left. \frac{2}{15} \operatorname{Sec}[c+d x] \left( 5 B \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] + 9 C \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right) \right) \right) / \\ & \quad \left( d(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right) - \\ & \quad \frac{1}{d(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])} \\ & \quad 8(-3-2 \sqrt{2}) A \cos \left[\frac{1}{4}(c+d x)\right]^4 \sqrt{\frac{7-5 \sqrt{2}+(10-7 \sqrt{2}) \cos \left[\frac{1}{2}(c+d x)\right]}{1+\cos \left[\frac{1}{2}(c+d x)\right]}} \\ & \quad \sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2}) \cos \left[\frac{1}{2}(c+d x)\right]}{1+\cos \left[\frac{1}{2}(c+d x)\right]}} \left( 1-\sqrt{2}+(-2+\sqrt{2}) \cos \left[\frac{1}{2}(c+d x)\right] \right) \\ & \quad \cos [c+d x]^2 \left( \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right] + \right. \\ & \quad \left. 2 \operatorname{EllipticPi}\left[-3+2 \sqrt{2},-\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right] \right) \\ & \quad \sqrt{\left(-1-\sqrt{2}+(2+\sqrt{2}) \cos \left[\frac{1}{2}(c+d x)\right]\right) \operatorname{Sec}\left[\frac{1}{4}(c+d x)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^3} \\ & \quad (a(1+\operatorname{Sec}[c+d x]))^{3/2} (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \sqrt{3-2 \sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+d x)\right]^2} \end{aligned}$$

**Problem 496: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c+d x]^2 (a+a \operatorname{Sec}[c+d x])^{3/2} (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) dx$$

Optimal (type 3, 157 leaves, 5 steps):

$$\begin{aligned} & \frac{a^{3/2}(7 A+12 B+8 C) \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right]}{4 d} + \frac{a^2(5 A+4 B-8 C) \operatorname{Sin}[c+d x]}{4 d \sqrt{a+a \operatorname{Sec}[c+d x]}} - \\ & \frac{a(A-4 C) \sqrt{a+a \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{2 d} + \frac{A \cos [c+d x](a+a \operatorname{Sec}[c+d x])^{3/2} \operatorname{Sin}[c+d x]}{2 d} \end{aligned}$$

Result (type 4, 436 leaves):



$$\begin{aligned}
 & \frac{1}{2} \left( \frac{1}{d} \cos [c+d x] \operatorname{Sec} \left[ \frac{1}{2} (c+d x) \right]^3 (a (1+\operatorname{Sec} [c+d x]))^{3/2} \right. \\
 & \quad \left. \left( -\frac{1}{8} (5 A+4 B-16 C) \sin \left[ \frac{1}{2} (c+d x) \right] + \frac{1}{4} (3 A+2 B) \sin \left[ \frac{3}{2} (c+d x) \right] + \frac{1}{8} A \sin \left[ \frac{5}{2} (c+d x) \right] \right) \right. \\
 & \quad \frac{1}{d} \left( 2 + \frac{3}{\sqrt{2}} \right) (7 A+12 B+8 C) \cos \left[ \frac{1}{4} (c+d x) \right]^4 \sqrt{\frac{7-5 \sqrt{2}+(10-7 \sqrt{2}) \cos \left[ \frac{1}{2} (c+d x) \right]}{1+\cos \left[ \frac{1}{2} (c+d x) \right]}} \\
 & \quad \left( 1-\sqrt{2}+(-2+\sqrt{2}) \cos \left[ \frac{1}{2} (c+d x) \right] \right) \left( \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\tan \left[ \frac{1}{4} (c+d x) \right]}{\sqrt{3-2 \sqrt{2}}} \right], 17-12 \sqrt{2} \right] + \right. \\
 & \quad \left. 2 \operatorname{EllipticPi} \left[ -3+2 \sqrt{2}, -\operatorname{ArcSin} \left[ \frac{\tan \left[ \frac{1}{4} (c+d x) \right]}{\sqrt{3-2 \sqrt{2}}} \right], 17-12 \sqrt{2} \right] \right) \\
 & \quad \sqrt{\left( -1+\sqrt{2}-(-2+\sqrt{2}) \cos \left[ \frac{1}{2} (c+d x) \right] \right) \operatorname{Sec} \left[ \frac{1}{4} (c+d x) \right]^2} \\
 & \quad \sqrt{\left( -1-\sqrt{2}+(2+\sqrt{2}) \cos \left[ \frac{1}{2} (c+d x) \right] \right) \operatorname{Sec} \left[ \frac{1}{4} (c+d x) \right]^2} \\
 & \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c+d x) \right]^3 (a (1+\operatorname{Sec} [c+d x]))^{3/2} \sqrt{3-2 \sqrt{2}-\tan \left[ \frac{1}{4} (c+d x) \right]^2} \right)
 \end{aligned}$$

**Problem 498: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c+d x]^4 (a+a \operatorname{Sec} [c+d x])^{3/2} (A+B \operatorname{Sec} [c+d x]+C \operatorname{Sec} [c+d x]^2) dx$$

Optimal (type 3, 215 leaves, 6 steps):

$$\begin{aligned}
 & \frac{a^{3/2} (75 A+88 B+112 C) \operatorname{ArcTan} \left[ \frac{\sqrt{a} \tan [c+d x]}{\sqrt{a+a \operatorname{Sec} [c+d x]}} \right]}{64 d} + \\
 & \frac{a^2 (75 A+88 B+112 C) \sin [c+d x]}{64 d \sqrt{a+a \operatorname{Sec} [c+d x]}} + \frac{a^2 (39 A+56 B+48 C) \cos [c+d x] \sin [c+d x]}{96 d \sqrt{a+a \operatorname{Sec} [c+d x]}} + \\
 & \frac{a (3 A+8 B) \cos [c+d x]^2 \sqrt{a+a \operatorname{Sec} [c+d x]} \sin [c+d x]}{24 d} + \\
 & \frac{A \cos [c+d x]^3 (a+a \operatorname{Sec} [c+d x])^{3/2} \sin [c+d x]}{4 d}
 \end{aligned}$$

Result (type 4, 586 leaves):

$$\begin{aligned}
& \left( \cos [c+d x]^3 \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^3 (a(1+\operatorname{Sec}[c+d x]))^{3/2} \right. \\
& \quad \left. (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \left( -\frac{1}{384}(129 A+136 B+240 C) \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] + \right. \right. \\
& \quad \left. \frac{1}{48}(27 A+28 B+36 C) \operatorname{Sin}\left[\frac{3}{2}(c+d x)\right] + \frac{1}{128}(23 A+24 B+16 C) \operatorname{Sin}\left[\frac{5}{2}(c+d x)\right] + \right. \\
& \quad \left. \left. \frac{1}{48}(3 A+2 B) \operatorname{Sin}\left[\frac{7}{2}(c+d x)\right] + \frac{1}{64} A \operatorname{Sin}\left[\frac{9}{2}(c+d x)\right] \right) \right) / \\
& \quad \left( d(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right) + \\
& \quad \frac{1}{(-64+48 \sqrt{2}) d(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])} \\
& \quad (75 A+88 B+112 C) \cos \left[\frac{1}{4}(c+d x)\right]^4 \sqrt{\frac{7-5 \sqrt{2}+(10-7 \sqrt{2}) \cos \left[\frac{1}{2}(c+d x)\right]}{1+\cos \left[\frac{1}{2}(c+d x)\right]}} \\
& \quad \left(1-\sqrt{2}+(-2+\sqrt{2}) \cos \left[\frac{1}{2}(c+d x)\right]\right) \cos [c+d x]^2 \\
& \quad \left( \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4}(c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right] + \right. \\
& \quad \left. 2 \operatorname{EllipticPi}\left[-3+2 \sqrt{2}, -\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4}(c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right] \right) \\
& \quad \sqrt{\left(-1+\sqrt{2}-(-2+\sqrt{2}) \cos \left[\frac{1}{2}(c+d x)\right]\right) \operatorname{Sec}\left[\frac{1}{4}(c+d x)\right]^2} \\
& \quad \sqrt{\left(-1-\sqrt{2}+(2+\sqrt{2}) \cos \left[\frac{1}{2}(c+d x)\right]\right) \operatorname{Sec}\left[\frac{1}{4}(c+d x)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^3} \\
& \quad (a(1+\operatorname{Sec}[c+d x]))^{3/2} (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \sqrt{3-2 \sqrt{2}-\tan \left[\frac{1}{4}(c+d x)\right]^2}
\end{aligned}$$

**Problem 499:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \cos [c+d x]^5 (a+a \operatorname{Sec}[c+d x])^{3/2} (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) dx$$

Optimal (type 3, 263 leaves, 7 steps):

$$\begin{aligned}
 & \frac{a^{3/2} (133 A + 150 B + 176 C) \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{128 d} + \\
 & \frac{a^2 (133 A + 150 B + 176 C) \operatorname{Sin}[c+dx]}{128 d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{a^2 (133 A + 150 B + 176 C) \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx]}{192 d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \\
 & \frac{a^2 (67 A + 90 B + 80 C) \operatorname{Cos}[c+dx]^2 \operatorname{Sin}[c+dx]}{240 d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \\
 & \frac{a (3 A + 10 B) \operatorname{Cos}[c+dx]^3 \sqrt{a+a \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{40 d} + \\
 & \frac{A \operatorname{Cos}[c+dx]^4 (a+a \operatorname{Sec}[c+dx])^{3/2} \operatorname{Sin}[c+dx]}{5 d}
 \end{aligned}$$

Result (type 4, 611 leaves):

$$\begin{aligned}
& \frac{1}{d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])} \\
& \cos [c + d x]^3 \sec \left[ \frac{1}{2} (c + d x) \right]^3 (a (1 + \sec [c + d x]))^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
& \left( -\frac{(1019 A + 1290 B + 1360 C) \sin \left[ \frac{1}{2} (c + d x) \right]}{3840} + \frac{1}{480} (239 A + 270 B + 280 C) \sin \left[ \frac{3}{2} (c + d x) \right] + \right. \\
& \quad \frac{1}{256} (49 A + 46 B + 48 C) \sin \left[ \frac{5}{2} (c + d x) \right] + \frac{1}{240} (17 A + 15 B + 10 C) \sin \left[ \frac{7}{2} (c + d x) \right] + \\
& \quad \left. \frac{1}{128} (3 A + 2 B) \sin \left[ \frac{9}{2} (c + d x) \right] + \frac{1}{160} A \sin \left[ \frac{11}{2} (c + d x) \right] \right) + \\
& \frac{1}{64 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])} (4 + 3 \sqrt{2}) (133 A + 150 B + 176 C) \\
& \cos \left[ \frac{1}{4} (c + d x) \right]^4 \sqrt{\frac{7 - 5 \sqrt{2} + (10 - 7 \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right]}{1 + \cos \left[ \frac{1}{2} (c + d x) \right]}} \\
& \left( 1 - \sqrt{2} + (-2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right] \right) \cos [c + d x]^2 \\
& \left( \text{EllipticF} \left[ \text{ArcSin} \left[ \frac{\tan \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] + \right. \\
& \quad \left. 2 \text{EllipticPi} \left[ -3 + 2 \sqrt{2}, -\text{ArcSin} \left[ \frac{\tan \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \right) \\
& \sqrt{\left( -1 + \sqrt{2} - (-2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right] \right) \sec \left[ \frac{1}{4} (c + d x) \right]^2} \\
& \sqrt{\left( -1 - \sqrt{2} + (2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right] \right) \sec \left[ \frac{1}{4} (c + d x) \right]^2 \sec \left[ \frac{1}{2} (c + d x) \right]^3} \\
& (a (1 + \sec [c + d x]))^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \sqrt{3 - 2 \sqrt{2} - \tan \left[ \frac{1}{4} (c + d x) \right]^2}
\end{aligned}$$

**Problem 503: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int (a + a \sec [c + d x])^{5/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 3, 182 leaves, 7 steps):

$$\frac{2 a^{5/2} A \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right]}{d} + \frac{2 a^3 (245 A + 224 B + 160 C) \operatorname{Tan}[c+d x]}{105 d \sqrt{a+a \operatorname{Sec}[c+d x]}} +$$

$$\frac{2 a^2 (35 A + 56 B + 40 C) \sqrt{a+a \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x]}{105 d} +$$

$$\frac{2 a (7 B + 5 C) (a+a \operatorname{Sec}[c+d x])^{3/2} \operatorname{Tan}[c+d x]}{35 d} + \frac{2 C (a+a \operatorname{Sec}[c+d x])^{5/2} \operatorname{Tan}[c+d x]}{7 d}$$

Result (type 4, 606 leaves):

$$\frac{1}{d (A + 2 C + 2 B \operatorname{Cos}[c+d x] + A \operatorname{Cos}[2 c + 2 d x])}$$

$$\operatorname{Cos}[c+d x]^4 \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^5 (a (1 + \operatorname{Sec}[c+d x]))^{5/2} (A + B \operatorname{Sec}[c+d x] + C \operatorname{Sec}[c+d x]^2)$$

$$\left( \frac{1}{105} (280 A + 301 B + 230 C) \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] + \frac{1}{7} C \operatorname{Sec}[c+d x]^3 \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] + \right.$$

$$\frac{1}{35} \operatorname{Sec}[c+d x]^2 \left( 7 B \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] + 20 C \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right) +$$

$$\left. \frac{1}{105} \operatorname{Sec}[c+d x] \left( 35 A \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] + 98 B \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] + 115 C \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right) \right) -$$

$$\frac{1}{d (A + 2 C + 2 B \operatorname{Cos}[c+d x] + A \operatorname{Cos}[2 c + 2 d x])} 4 (-3 - 2 \sqrt{2}) A \operatorname{Cos}\left[\frac{1}{4}(c+d x)\right]^4$$

$$\sqrt{\frac{7 - 5 \sqrt{2} + (10 - 7 \sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]}{1 + \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]}} \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]}{1 + \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]}}$$

$$\left( 1 - \sqrt{2} + (-2 + \sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] \right) \operatorname{Cos}[c+d x]^3$$

$$\left( \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+d x)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}\right] + \right.$$

$$\left. 2 \operatorname{EllipticPi}\left[-3 + 2 \sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+d x)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}\right] \right)$$

$$\sqrt{\left( -1 - \sqrt{2} + (2 + \sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] \right) \operatorname{Sec}\left[\frac{1}{4}(c+d x)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^5}$$

$$(a (1 + \operatorname{Sec}[c+d x]))^{5/2} (A + B \operatorname{Sec}[c+d x] + C \operatorname{Sec}[c+d x]^2) \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c+d x)\right]^2}$$

Problem 505: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \cos [c + d x]^2 (a + a \operatorname{Sec} [c + d x])^{5/2} (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) dx$$

Optimal (type 3, 197 leaves, 6 steps):

$$\frac{a^{5/2} (19 A + 20 B + 8 C) \operatorname{ArcTan} \left[ \frac{\sqrt{a} \operatorname{Tan} [c + d x]}{\sqrt{a + a \operatorname{Sec} [c + d x]}} \right]}{4 d} + \frac{a^3 (27 A - 12 B - 56 C) \operatorname{Sin} [c + d x]}{12 d \sqrt{a + a \operatorname{Sec} [c + d x]}} - \frac{a^2 (A - 4 B - 8 C) \sqrt{a + a \operatorname{Sec} [c + d x]} \operatorname{Sin} [c + d x]}{2 d} - \frac{a (3 A - 4 C) (a + a \operatorname{Sec} [c + d x])^{3/2} \operatorname{Sin} [c + d x]}{6 d} + \frac{A \operatorname{Cos} [c + d x] (a + a \operatorname{Sec} [c + d x])^{5/2} \operatorname{Sin} [c + d x]}{2 d}$$

Result (type 4, 467 leaves):

$$\begin{aligned}
 & \frac{1}{2} \left( \frac{1}{d} \cos [c+d x]^2 \sec \left[ \frac{1}{2} (c+d x) \right]^5 (a (1+\sec [c+d x]))^{5/2} \right. \\
 & \quad \left( -\frac{1}{48} (27 A-36 B-128 C) \sin \left[ \frac{1}{2} (c+d x) \right] + \frac{1}{3} C \sec [c+d x] \sin \left[ \frac{1}{2} (c+d x) \right] + \right. \\
 & \quad \left. \frac{1}{8} (5 A+2 B) \sin \left[ \frac{3}{2} (c+d x) \right] + \frac{1}{16} A \sin \left[ \frac{5}{2} (c+d x) \right] \right) + \\
 & \frac{1}{d} \left( 1 + \frac{3}{2 \sqrt{2}} \right) (19 A+20 B+8 C) \cos \left[ \frac{1}{4} (c+d x) \right]^4 \sqrt{\frac{7-5 \sqrt{2}+(10-7 \sqrt{2}) \cos \left[ \frac{1}{2} (c+d x) \right]}{1+\cos \left[ \frac{1}{2} (c+d x) \right]}} \\
 & \quad \left( 1-\sqrt{2}+(-2+\sqrt{2}) \cos \left[ \frac{1}{2} (c+d x) \right] \right) \cos [c+d x] \\
 & \quad \left( \text{EllipticF} \left[ \text{ArcSin} \left[ \frac{\tan \left[ \frac{1}{4} (c+d x) \right]}{\sqrt{3-2 \sqrt{2}}} \right], 17-12 \sqrt{2} \right] + \right. \\
 & \quad \left. 2 \text{EllipticPi} \left[ -3+2 \sqrt{2}, -\text{ArcSin} \left[ \frac{\tan \left[ \frac{1}{4} (c+d x) \right]}{\sqrt{3-2 \sqrt{2}}} \right], 17-12 \sqrt{2} \right] \right) \\
 & \quad \sqrt{\left( -1+\sqrt{2}-(-2+\sqrt{2}) \cos \left[ \frac{1}{2} (c+d x) \right] \right) \sec \left[ \frac{1}{4} (c+d x) \right]^2} \\
 & \quad \sqrt{\left( -1-\sqrt{2}+(2+\sqrt{2}) \cos \left[ \frac{1}{2} (c+d x) \right] \right) \sec \left[ \frac{1}{4} (c+d x) \right]^2} \\
 & \quad \left. \sec \left[ \frac{1}{2} (c+d x) \right]^5 (a (1+\sec [c+d x]))^{5/2} \sqrt{3-2 \sqrt{2}-\tan \left[ \frac{1}{4} (c+d x) \right]^2} \right)
 \end{aligned}$$

**Problem 507: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c+d x]^4 (a+a \sec [c+d x])^{5/2} (A+B \sec [c+d x]+C \sec [c+d x]^2) dx$$

Optimal (type 3, 215 leaves, 6 steps):

$$\frac{a^{5/2} (163 A + 200 B + 304 C) \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{64 d} + \frac{a^3 (299 A + 392 B + 432 C) \operatorname{Sin}[c+dx]}{192 d \sqrt{a+a \operatorname{Sec}[c+dx]}} +$$

$$\frac{a^2 (17 A + 24 B + 16 C) \operatorname{Cos}[c+dx] \sqrt{a+a \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{32 d} +$$

$$\frac{a (5 A + 8 B) \operatorname{Cos}[c+dx]^2 (a+a \operatorname{Sec}[c+dx])^{3/2} \operatorname{Sin}[c+dx]}{24 d} +$$

$$\frac{A \operatorname{Cos}[c+dx]^3 (a+a \operatorname{Sec}[c+dx])^{5/2} \operatorname{Sin}[c+dx]}{4 d}$$

Result (type 4, 587 leaves):

$$\left( \operatorname{Cos}[c+dx]^4 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\operatorname{Sec}[c+dx]))^{5/2} \right.$$

$$\left. (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \left( -\frac{1}{768} (265 A + 376 B + 432 C) \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + \right. \right.$$

$$\left. \frac{1}{96} (55 A + 64 B + 60 C) \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right] + \frac{1}{256} (47 A + 40 B + 16 C) \operatorname{Sin}\left[\frac{5}{2}(c+dx)\right] + \right.$$

$$\left. \frac{1}{96} (5 A + 2 B) \operatorname{Sin}\left[\frac{7}{2}(c+dx)\right] + \frac{1}{128} A \operatorname{Sin}\left[\frac{9}{2}(c+dx)\right] \right) \Big/$$

$$\left( d (A + 2 C + 2 B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) \right) +$$

$$\frac{1}{64 d (A + 2 C + 2 B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx])}$$

$$(4 + 3\sqrt{2}) (163 A + 200 B + 304 C) \operatorname{Cos}\left[\frac{1}{4}(c+dx)\right]^4$$

$$\sqrt{\frac{7 - 5\sqrt{2} + (10 - 7\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}{1 + \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}} \left( 1 - \sqrt{2} + (-2 + \sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \right)$$

$$\operatorname{Cos}[c+dx]^3 \left( \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] + \right.$$

$$\left. 2 \operatorname{EllipticPi}\left[-3 + 2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \right)$$

$$\sqrt{\left( -1 + \sqrt{2} - (-2 + \sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2}$$

$$\sqrt{\left( -1 - \sqrt{2} + (2 + \sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^5}$$

$$(a(1+\operatorname{Sec}[c+dx]))^{5/2} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}$$



Problem 508: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \cos [c + d x]^5 (a + a \sec [c + d x])^{5/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 3, 261 leaves, 7 steps):

$$\frac{a^{5/2} (283 A + 326 B + 400 C) \operatorname{ArcTan} \left[ \frac{\sqrt{a} \tan [c + d x]}{\sqrt{a + a \sec [c + d x]}} \right]}{128 d} +$$

$$\frac{a^3 (283 A + 326 B + 400 C) \sin [c + d x]}{128 d \sqrt{a + a \sec [c + d x]}} + \frac{a^3 (787 A + 950 B + 1040 C) \cos [c + d x] \sin [c + d x]}{960 d \sqrt{a + a \sec [c + d x]}} +$$

$$\frac{a^2 (79 A + 110 B + 80 C) \cos [c + d x]^2 \sqrt{a + a \sec [c + d x]} \sin [c + d x]}{240 d} +$$

$$\frac{a (A + 2 B) \cos [c + d x]^3 (a + a \sec [c + d x])^{3/2} \sin [c + d x]}{8 d} +$$

$$\frac{A \cos [c + d x]^4 (a + a \sec [c + d x])^{5/2} \sin [c + d x]}{5 d}$$

Result (type 4, 611 leaves):

$$\begin{aligned}
& \frac{1}{d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])} \\
& \cos [c + d x]^4 \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^5 (a (1 + \operatorname{Sec} [c + d x]))^{5/2} (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) \\
& \left( -\frac{(2309 A + 2650 B + 3760 C) \sin \left[ \frac{1}{2} (c + d x) \right]}{7680} + \frac{1}{960} (509 A + 550 B + 640 C) \sin \left[ \frac{3}{2} (c + d x) \right] + \right. \\
& \quad \frac{1}{512} (95 A + 94 B + 80 C) \sin \left[ \frac{5}{2} (c + d x) \right] + \frac{1}{480} (32 A + 25 B + 10 C) \sin \left[ \frac{7}{2} (c + d x) \right] + \\
& \quad \left. \frac{1}{256} (5 A + 2 B) \sin \left[ \frac{9}{2} (c + d x) \right] + \frac{1}{320} A \sin \left[ \frac{11}{2} (c + d x) \right] \right) + \\
& \frac{1}{64 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])} \left( 2 + \frac{3}{\sqrt{2}} \right) (283 A + 326 B + 400 C) \\
& \cos \left[ \frac{1}{4} (c + d x) \right]^4 \sqrt{\frac{7 - 5 \sqrt{2} + (10 - 7 \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right]}{1 + \cos \left[ \frac{1}{2} (c + d x) \right]}} \\
& \left( 1 - \sqrt{2} + (-2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right] \right) \cos [c + d x]^3 \\
& \left( \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\tan \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] + \right. \\
& \quad \left. 2 \operatorname{EllipticPi} \left[ -3 + 2 \sqrt{2}, -\operatorname{ArcSin} \left[ \frac{\tan \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \right) \\
& \sqrt{\left( -1 + \sqrt{2} - (-2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right] \right) \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2} \\
& \sqrt{\left( -1 - \sqrt{2} + (2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right] \right) \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^5} \\
& (a (1 + \operatorname{Sec} [c + d x]))^{5/2} (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) \sqrt{3 - 2 \sqrt{2} - \tan \left[ \frac{1}{4} (c + d x) \right]^2}
\end{aligned}$$

**Problem 509: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c + d x]^6 (a + a \operatorname{Sec} [c + d x])^{5/2} (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) dx$$

Optimal (type 3, 311 leaves, 8 steps):

$$\begin{aligned}
 & \frac{a^{5/2} (1015 A + 1132 B + 1304 C) \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{512 d} + \\
 & \frac{a^3 (1015 A + 1132 B + 1304 C) \operatorname{Sin}[c+dx]}{512 d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{a^3 (1015 A + 1132 B + 1304 C) \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx]}{768 d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \\
 & \frac{a^3 (545 A + 628 B + 680 C) \operatorname{Cos}[c+dx]^2 \operatorname{Sin}[c+dx]}{960 d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{1}{480 d} + \\
 & \frac{a^2 (115 A + 156 B + 120 C) \operatorname{Cos}[c+dx]^3 \sqrt{a+a \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{60 d} + \\
 & \frac{a (5 A + 12 B) \operatorname{Cos}[c+dx]^4 (a+a \operatorname{Sec}[c+dx])^{3/2} \operatorname{Sin}[c+dx]}{6 d} + \\
 & \frac{A \operatorname{Cos}[c+dx]^5 (a+a \operatorname{Sec}[c+dx])^{5/2} \operatorname{Sin}[c+dx]}{6 d}
 \end{aligned}$$

Result (type 4, 635 leaves):

$$\begin{aligned}
& \frac{1}{d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])} \\
& \cos [c + d x]^4 \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^5 (a (1 + \operatorname{Sec} [c + d x]))^{5/2} \\
& (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) \left( -\frac{(7945 A + 9236 B + 10600 C) \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right]}{30720} + \right. \\
& \frac{(935 A + 1018 B + 1100 C) \operatorname{Sin} \left[ \frac{3}{2} (c + d x) \right]}{1920} + \frac{(1145 A + 1140 B + 1128 C) \operatorname{Sin} \left[ \frac{5}{2} (c + d x) \right]}{6144} + \\
& \frac{(145 A + 128 B + 100 C) \operatorname{Sin} \left[ \frac{7}{2} (c + d x) \right]}{1920} + \frac{(83 A + 60 B + 24 C) \operatorname{Sin} \left[ \frac{9}{2} (c + d x) \right]}{3072} + \\
& \left. \frac{1}{640} (5 A + 2 B) \operatorname{Sin} \left[ \frac{11}{2} (c + d x) \right] + \frac{1}{768} A \operatorname{Sin} \left[ \frac{13}{2} (c + d x) \right] \right) + \\
& \frac{1}{512 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])} \\
& (4 + 3 \sqrt{2}) (1015 A + 1132 B + 1304 C) \cos \left[ \frac{1}{4} (c + d x) \right]^4 \\
& \sqrt{\frac{7 - 5 \sqrt{2} + (10 - 7 \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right]}{1 + \cos \left[ \frac{1}{2} (c + d x) \right]}} \left( 1 - \sqrt{2} + (-2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right] \right) \\
& \cos [c + d x]^3 \left( \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] + \right. \\
& \left. 2 \operatorname{EllipticPi} \left[ -3 + 2 \sqrt{2}, -\operatorname{ArcSin} \left[ \frac{\operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \right) \\
& \sqrt{\left( -1 + \sqrt{2} - (-2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right] \right) \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2} \\
& \sqrt{\left( -1 - \sqrt{2} + (2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right] \right) \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^5} \\
& (a (1 + \operatorname{Sec} [c + d x]))^{5/2} (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}
\end{aligned}$$

**Problem 522: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec} [c + d x] (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2)}{(a + a \operatorname{Sec} [c + d x])^{3/2}} dx$$

Optimal (type 3, 120 leaves, 4 steps):

$$\frac{(A+3B-7C) \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{2} \sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{2\sqrt{2} a^{3/2} d} + \frac{(A-B+C) \operatorname{Tan}[c+dx]}{2d(a+a \operatorname{Sec}[c+dx])^{3/2}} + \frac{2C \operatorname{Tan}[c+dx]}{ad \sqrt{a+a \operatorname{Sec}[c+dx]}}$$

Result (type 3, 307 leaves):

$$\left( 2(A+3B-7C) \operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\ \left. \sqrt{\frac{\operatorname{Cos}[c+dx]}{1+\operatorname{Cos}[c+dx]}} \sqrt{1+\operatorname{Sec}[c+dx]} (A+B \operatorname{Sec}[c+dx]+C \operatorname{Sec}[c+dx]^2)} \right) / \\ \left( d(A+2C+2B \operatorname{Cos}[c+dx]+A \operatorname{Cos}[2c+2dx]) \sqrt{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2} \right. \\ \left. \sqrt{\operatorname{Sec}[c+dx]} (a(1+\operatorname{Sec}[c+dx]))^{3/2} \right) + \\ \left( \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^3 (A+B \operatorname{Sec}[c+dx]+C \operatorname{Sec}[c+dx]^2) \left( 4(A-B+5C) \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] - \right. \right. \\ \left. \left. 2 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left( A \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] - B \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + C \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) / \\ \left( d(A+2C+2B \operatorname{Cos}[c+dx]+A \operatorname{Cos}[2c+2dx]) (a(1+\operatorname{Sec}[c+dx]))^{3/2} \right)$$

**Problem 526: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Cos}[c+dx]^3 (A+B \operatorname{Sec}[c+dx]+C \operatorname{Sec}[c+dx]^2)}{(a+a \operatorname{Sec}[c+dx])^{3/2}} dx$$

Optimal (type 3, 284 leaves, 9 steps):

$$-\frac{(47A-38B+24C) \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{8a^{3/2}d} + \frac{(17A-13B+9C) \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{2} \sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{2\sqrt{2} a^{3/2}d} - \\ \frac{(A-B+C) \operatorname{Cos}[c+dx]^2 \operatorname{Sin}[c+dx]}{2d(a+a \operatorname{Sec}[c+dx])^{3/2}} + \frac{(21A-14B+12C) \operatorname{Sin}[c+dx]}{8ad \sqrt{a+a \operatorname{Sec}[c+dx]}} - \\ \frac{(13A-12B+6C) \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx]}{12ad \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{(5A-3B+3C) \operatorname{Cos}[c+dx]^2 \operatorname{Sin}[c+dx]}{6ad \sqrt{a+a \operatorname{Sec}[c+dx]}}$$

Result (type 3, 831 leaves):

$$\begin{aligned}
 & \left( \cos [c+d x]^2 (1+\sec [c+d x])^{3 / 2} (A+B \sec [c+d x]+C \sec [c+d x]^2) \right. \\
 & \left. \left( \left( \sqrt{2}(-21 A+14 B-12 C) \operatorname{ArcTan}\left[\frac{\sqrt{2}}{\sqrt{-1+\sec [c+d x]}}\right] \cos [c+d x]^2 \right. \right. \right. \\
 & \left. \left. \left. \sqrt{-1+\sec [c+d x]}(1+\sec [c+d x])^{3 / 2} \sin [c+d x] \right) \right) / \left( d(1+\cos [c+d x]) \right. \right. \\
 & \left. \left. \sqrt{1-\cos [c+d x]^2} \sqrt{\cos [c+d x]^2(-1+\sec [c+d x])(1+\sec [c+d x])} \right) - \right. \\
 & \left. \left( (47 A-38 B+24 C) \left( \sqrt{2} \operatorname{ArcTan}\left[\frac{\sqrt{2}}{\sqrt{-1+\sec [c+d x]}}\right] + \operatorname{ArcTan}\left[\frac{-2+\sqrt{1+\sec [c+d x]}}{\sqrt{-1+\sec [c+d x]}}\right] \right) - \right. \right. \\
 & \left. \left. \operatorname{ArcTan}\left[\frac{2+\sqrt{1+\sec [c+d x]}}{\sqrt{-1+\sec [c+d x]}}\right] \right) \cos [c+d x]^2 \sqrt{-1+\sec [c+d x]} \right. \\
 & \left. (1+\sec [c+d x])^{3 / 2} \sin [c+d x] \right) / \left( d(1+\cos [c+d x]) \sqrt{1-\cos [c+d x]^2} \right. \\
 & \left. \left. \left. \left. \left. \sqrt{\cos [c+d x]^2(-1+\sec [c+d x])(1+\sec [c+d x])} \right) \right) \right) \right) / \\
 & \left( 8(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])(a(1+\sec [c+d x]))^{3 / 2} \right) + \\
 & \left( 1 / \left( (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])(a(1+\sec [c+d x]))^{3 / 2} \right) \right) \\
 & \cos [c+d x]^2 \\
 & \sqrt{(1+\cos [c+d x]) \sec [c+d x]} \\
 & (1+\sec [c+d x])^{3 / 2} \\
 & (A+B \sec [c+d x]+C \sec [c+d x]^2) \\
 & \left( \frac{\sec \left[\frac{c}{2}\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^2\left(-A \sin \left[\frac{c}{2}\right]+B \sin \left[\frac{c}{2}\right]-C \sin \left[\frac{c}{2}\right]\right)}{2 d} + \frac{(25 A-14 B+8 C) \cos [d x] \sin [c]}{4 d} - \right. \\
 & \frac{(11 A-6 B) \cos [2 d x] \sin [2 c]}{12 d} + \frac{A \cos [3 d x] \sin [3 c]}{6 d} + \frac{1}{12 d} \\
 & \left. \sec \left[\frac{c}{2}\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]\left(-61 A \sin \left[\frac{d x}{2}\right]+30 B \sin \left[\frac{d x}{2}\right]-12 C \sin \left[\frac{d x}{2}\right]\right) + \right. \\
 & \left. \frac{\sec \left[\frac{c}{2}\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^3\left(-A \sin \left[\frac{d x}{2}\right]+B \sin \left[\frac{d x}{2}\right]-C \sin \left[\frac{d x}{2}\right]\right)}{2 d} + \right. \\
 & \left. \frac{(25 A-14 B+8 C) \cos [c] \sin [d x]}{4 d} - \frac{(11 A-6 B) \cos [2 c] \sin [2 d x]}{12 d} + \right. \\
 & \left. \frac{A \cos [3 c] \sin [3 d x]}{6 d} - \frac{(61 A-30 B+12 C) \tan \left[\frac{c}{2}\right]}{12 d} \right)
 \end{aligned}$$

**Problem 529: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c + d x]^2 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{(a + a \sec [c + d x])^{5/2}} dx$$

Optimal (type 3, 179 leaves, 5 steps):

$$\frac{(5 A + 19 B - 75 C) \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c + d x]}{\sqrt{2} \sqrt{a + a \sec [c + d x]}}\right]}{16 \sqrt{2} a^{5/2} d} - \frac{(A - B + C) \sec [c + d x]^2 \operatorname{Tan}[c + d x]}{4 d (a + a \sec [c + d x])^{5/2}} - \frac{(3 A + 5 B - 13 C) \operatorname{Tan}[c + d x]}{16 a d (a + a \sec [c + d x])^{3/2}} + \frac{(A - B + 9 C) \operatorname{Tan}[c + d x]}{4 a^2 d \sqrt{a + a \sec [c + d x]}}$$

Result (type 3, 372 leaves):

$$\left( (5 A + 19 B - 75 C) \operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right] \cos\left[\frac{1}{2}(c + d x)\right]^4 \sqrt{\frac{\cos [c + d x]}{1 + \cos [c + d x]}} \right. \\ \left. \sqrt{\sec [c + d x]} \sqrt{1 + \sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \\ \left( 2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{\sec \left[\frac{1}{2}(c + d x)\right]^2 (a (1 + \sec [c + d x]))^{5/2}} \right) + \\ \left( \cos \left[\frac{1}{2}(c + d x)\right]^5 \sec [c + d x] (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\ \left. \left( (A - 9 B + 49 C) \sin \left[\frac{1}{2}(c + d x)\right] + \right. \right. \\ \left. \frac{1}{2} \sec \left[\frac{1}{2}(c + d x)\right]^2 \left( 3 A \sin \left[\frac{1}{2}(c + d x)\right] + 5 B \sin \left[\frac{1}{2}(c + d x)\right] - 13 C \sin \left[\frac{1}{2}(c + d x)\right] \right) \right. \\ \left. \left. \sec \left[\frac{1}{2}(c + d x)\right]^4 \left( -A \sin \left[\frac{1}{2}(c + d x)\right] + B \sin \left[\frac{1}{2}(c + d x)\right] - C \sin \left[\frac{1}{2}(c + d x)\right] \right) \right) \right) / \\ \left( d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a (1 + \sec [c + d x]))^{5/2} \right)$$

**Problem 530: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c + d x] (A + B \sec [c + d x] + C \sec [c + d x]^2)}{(a + a \sec [c + d x])^{5/2}} dx$$

Optimal (type 3, 137 leaves, 4 steps):

$$\frac{(3A + 5B + 19C) \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{2} \sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{16 \sqrt{2} a^{5/2} d} - \frac{(A - B + C) \operatorname{Sec}[c+dx] \operatorname{Tan}[c+dx]}{4d (a + a \operatorname{Sec}[c+dx])^{5/2}} + \frac{(7A + B - 9C) \operatorname{Tan}[c+dx]}{16ad (a + a \operatorname{Sec}[c+dx])^{3/2}}$$

Result (type 3, 371 leaves):

$$\left( (3A + 5B + 19C) \operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^4 \sqrt{\frac{\operatorname{Cos}[c+dx]}{1 + \operatorname{Cos}[c+dx]}} \right. \\ \left. \sqrt{\operatorname{Sec}[c+dx]} \sqrt{1 + \operatorname{Sec}[c+dx]} (A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\ \left( 2d (A + 2C + 2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c + 2dx]) \sqrt{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 (a (1 + \operatorname{Sec}[c+dx]))^{5/2}} \right) + \\ \left( \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^5 \operatorname{Sec}[c+dx] (A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right. \\ \left. \left( (7A + B - 9C) \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4 \left( A \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] - B \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + C \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \right. \right. \\ \left. \left. + \frac{1}{2} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left( -11A \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + 3B \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + 5C \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) / \\ \left( d (A + 2C + 2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c + 2dx]) (a (1 + \operatorname{Sec}[c+dx]))^{5/2} \right)$$

### Problem 531: Result more than twice size of optimal antiderivative.

$$\int \frac{A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2}{(a + a \operatorname{Sec}[c+dx])^{5/2}} dx$$

Optimal (type 3, 171 leaves, 7 steps):

$$\frac{2A \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{a^{5/2} d} - \frac{(43A - 3B - 5C) \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{2} \sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{16 \sqrt{2} a^{5/2} d} - \frac{(A - B + C) \operatorname{Tan}[c+dx]}{4d (a + a \operatorname{Sec}[c+dx])^{5/2}} - \frac{(11A - 3B - 5C) \operatorname{Tan}[c+dx]}{16ad (a + a \operatorname{Sec}[c+dx])^{3/2}}$$

Result (type 3, 418 leaves):



$$\left( \left( (-43A + 3B + 5C) \operatorname{ArcSin} \left[ \operatorname{Tan} \left[ \frac{1}{2} (c + dx) \right] \right] + 32 \sqrt{2} A \operatorname{ArcTan} \left[ \frac{\operatorname{Tan} \left[ \frac{1}{2} (c + dx) \right]}{\sqrt{\frac{\operatorname{Cos}[c+dx]}{1+\operatorname{Cos}[c+dx]}}} \right] \right) \right. \\ \left. \operatorname{Cos} \left[ \frac{1}{2} (c + dx) \right]^4 \sqrt{\frac{\operatorname{Cos}[c+dx]}{1+\operatorname{Cos}[c+dx]}} \sqrt{\operatorname{Sec}[c+dx]} \right. \\ \left. \sqrt{1+\operatorname{Sec}[c+dx]} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\ \left( 2d (A+2C+2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) \sqrt{\operatorname{Sec} \left[ \frac{1}{2} (c + dx) \right]^2 (a(1+\operatorname{Sec}[c+dx]))^{5/2}} \right) + \\ \left( \operatorname{Cos} \left[ \frac{1}{2} (c + dx) \right]^5 \operatorname{Sec}[c+dx] (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right. \\ \left. \left( - (15A - 7B - C) \operatorname{Sin} \left[ \frac{1}{2} (c + dx) \right] + \right. \right. \\ \left. \left. \operatorname{Sec} \left[ \frac{1}{2} (c + dx) \right]^4 \left( -A \operatorname{Sin} \left[ \frac{1}{2} (c + dx) \right] + B \operatorname{Sin} \left[ \frac{1}{2} (c + dx) \right] - C \operatorname{Sin} \left[ \frac{1}{2} (c + dx) \right] \right) + \right. \right. \\ \left. \left. \frac{1}{2} \operatorname{Sec} \left[ \frac{1}{2} (c + dx) \right]^2 \left( 19A \operatorname{Sin} \left[ \frac{1}{2} (c + dx) \right] - 11B \operatorname{Sin} \left[ \frac{1}{2} (c + dx) \right] + 3C \operatorname{Sin} \left[ \frac{1}{2} (c + dx) \right] \right) \right) \right) / \\ \left( d (A+2C+2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) (a(1+\operatorname{Sec}[c+dx]))^{5/2} \right)$$

**Problem 532: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Cos}[c+dx] (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2)}{(a+a \operatorname{Sec}[c+dx])^{5/2}} dx$$

Optimal (type 3, 217 leaves, 8 steps):

$$- \frac{(5A - 2B) \operatorname{ArcTan} \left[ \frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}} \right]}{a^{5/2} d} + \frac{(115A - 43B + 3C) \operatorname{ArcTan} \left[ \frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{2} \sqrt{a+a \operatorname{Sec}[c+dx]}} \right]}{16 \sqrt{2} a^{5/2} d} - \\ \frac{(A - B + C) \operatorname{Sin}[c+dx]}{4d (a+a \operatorname{Sec}[c+dx])^{5/2}} - \frac{(15A - 7B - C) \operatorname{Sin}[c+dx]}{16ad (a+a \operatorname{Sec}[c+dx])^{3/2}} + \frac{(35A - 11B + 3C) \operatorname{Sin}[c+dx]}{16a^2 d \sqrt{a+a \operatorname{Sec}[c+dx]}}$$

Result (type 3, 839 leaves):

$$\begin{aligned}
 & \left( \cos [c+d x]^2 (1+\sec [c+d x])^{5 / 2} (A+B \sec [c+d x]+C \sec [c+d x]^2) \right. \\
 & \left. \left( \left( \sqrt{2}(-35 A+11 B-3 C) \operatorname{ArcTan}\left[\frac{\sqrt{2}}{\sqrt{-1+\sec [c+d x]}}\right] \cos [c+d x]^2 \right. \right. \right. \\
 & \left. \left. \left. \sqrt{-1+\sec [c+d x]}(1+\sec [c+d x])^{3 / 2} \sin [c+d x] \right) \right) / \left( d(1+\cos [c+d x]) \right. \right. \\
 & \left. \left. \sqrt{1-\cos [c+d x]^2} \sqrt{\cos [c+d x]^2(-1+\sec [c+d x])(1+\sec [c+d x])} \right) - \right. \\
 & \left. \left( (80 A-32 B) \left( \sqrt{2} \operatorname{ArcTan}\left[\frac{\sqrt{2}}{\sqrt{-1+\sec [c+d x]}}\right] + \operatorname{ArcTan}\left[\frac{-2+\sqrt{1+\sec [c+d x]}}{\sqrt{-1+\sec [c+d x]}}\right] \right) - \right. \right. \\
 & \left. \left. \operatorname{ArcTan}\left[\frac{2+\sqrt{1+\sec [c+d x]}}{\sqrt{-1+\sec [c+d x]}}\right] \right) \cos [c+d x]^2 \sqrt{-1+\sec [c+d x]} \right. \\
 & \left. \left. (1+\sec [c+d x])^{3 / 2} \sin [c+d x] \right) \right) / \left( d(1+\cos [c+d x]) \sqrt{1-\cos [c+d x]^2} \right. \\
 & \left. \left. \sqrt{\cos [c+d x]^2(-1+\sec [c+d x])(1+\sec [c+d x])} \right) \right) \left. \right) / \\
 & \left( 16(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])(a(1+\sec [c+d x]))^{5 / 2} \right) + \\
 & \left( 1 / \left( (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])(a(1+\sec [c+d x]))^{5 / 2} \right) \right) \\
 & \cos [c+d x]^2 \\
 & \sqrt{(1+\cos [c+d x]) \sec [c+d x]} \\
 & (1+\sec [c+d x])^{5 / 2} \\
 & (A+B \sec [c+d x]+C \sec [c+d x]^2) \\
 & \left( \frac{\sec \left[\frac{c}{2}\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^2\left(-27 A \sin \left[\frac{c}{2}\right]+19 B \sin \left[\frac{c}{2}\right]-11 C \sin \left[\frac{c}{2}\right]\right)}{16 d} + \right. \\
 & \frac{\sec \left[\frac{c}{2}\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4\left(A \sin \left[\frac{c}{2}\right]-B \sin \left[\frac{c}{2}\right]+C \sin \left[\frac{c}{2}\right]\right)}{8 d} + \frac{2 A \cos [d x] \sin [c]}{d} + \\
 & \frac{1}{16 d} \sec \left[\frac{c}{2}\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^3\left(-27 A \sin \left[\frac{d x}{2}\right]+19 B \sin \left[\frac{d x}{2}\right]-11 C \sin \left[\frac{d x}{2}\right]\right) + \\
 & \frac{\sec \left[\frac{c}{2}\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^5\left(A \sin \left[\frac{d x}{2}\right]-B \sin \left[\frac{d x}{2}\right]+C \sin \left[\frac{d x}{2}\right]\right)}{8 d} + \\
 & \frac{\sec \left[\frac{c}{2}\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]\left(7 A \sin \left[\frac{d x}{2}\right]-15 B \sin \left[\frac{d x}{2}\right]+7 C \sin \left[\frac{d x}{2}\right]\right)}{8 d} + \\
 & \left. \frac{2 A \cos [c] \sin [d x]}{d} + \frac{(7 A-15 B+7 C) \tan \left[\frac{c}{2}\right]}{8 d} \right)
 \end{aligned}$$

**Problem 534: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \text{Sec}[c+dx]^{3/2} (a+a \text{Sec}[c+dx]) (A+B \text{Sec}[c+dx]+C \text{Sec}[c+dx]^2) dx$$

Optimal (type 4, 217 leaves, 9 steps):

$$\begin{aligned} & -\frac{1}{5d} 2a(5A+3(B+C)) \sqrt{\text{Cos}[c+dx]} \text{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\text{Sec}[c+dx]} + \\ & \frac{1}{21d} 2a(7A+7B+5C) \sqrt{\text{Cos}[c+dx]} \text{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\text{Sec}[c+dx]} + \\ & \frac{2a(5A+3(B+C)) \sqrt{\text{Sec}[c+dx]} \text{Sin}[c+dx]}{5d} + \frac{2a(7A+7B+5C) \text{Sec}[c+dx]^{3/2} \text{Sin}[c+dx]}{21d} + \\ & \frac{2a(B+C) \text{Sec}[c+dx]^{5/2} \text{Sin}[c+dx]}{5d} + \frac{2aC \text{Sec}[c+dx]^{7/2} \text{Sin}[c+dx]}{7d} \end{aligned}$$

Result (type 5, 997 leaves):

$$\begin{aligned} & a \left( - \left( \left( 2\sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \text{Cos}[c+dx]^2 \text{Csc}[c] \right. \right. \right. \\ & \quad \left. \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \right. \\ & \quad \left. \left. (A+B \text{Sec}[c+dx]+C \text{Sec}[c+dx]^2) \right) / (d(A+2C+2B \text{Cos}[c+dx]+A \text{Cos}[2c+2dx])) \right) - \\ & \left( 6\sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \text{Cos}[c+dx]^2 \text{Csc}[c] \right. \\ & \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\ & \quad \left. (A+B \text{Sec}[c+dx]+C \text{Sec}[c+dx]^2) \right) / \\ & \quad (5d(A+2C+2B \text{Cos}[c+dx]+A \text{Cos}[2c+2dx])) - \\ & \left( 6\sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \text{Cos}[c+dx]^2 \text{Csc}[c] \right. \\ & \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\ & \quad \left. (A+B \text{Sec}[c+dx]+C \text{Sec}[c+dx]^2) \right) / (5d(A+2C+2B \text{Cos}[c+dx]+A \text{Cos}[2c+2dx])) + \end{aligned}$$

$$\left( \begin{aligned} & \left( 4 A \cos [c+d x]^{5 / 2} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]} \right. \\ & \quad \left. (A+B \sec [c+d x]+C \sec [c+d x]^2) \right) / \left( 3 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right) + \\ & \left( 4 B \cos [c+d x]^{5 / 2} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]} \right. \\ & \quad \left. (A+B \sec [c+d x]+C \sec [c+d x]^2) \right) / \left( 3 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right) + \\ & \left( 20 C \cos [c+d x]^{5 / 2} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]} \right. \\ & \quad \left. (A+B \sec [c+d x]+C \sec [c+d x]^2) \right) / \left( 21 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right) + \\ & \left( (A+B \sec [c+d x]+C \sec [c+d x]^2) \left( \frac{4(5 A+3 B+3 C) \cos [d x] \operatorname{Csc}[c]}{5 d} + \right. \right. \\ & \quad \left. \frac{4 C \sec [c] \sec [c+d x]^3 \sin [d x]}{7 d} + \frac{1}{35 d} 4 \sec [c] \sec [c+d x]^2 \right. \\ & \quad \left. (5 C \sin [c]+7 B \sin [d x]+7 C \sin [d x]) + \frac{1}{105 d} 4 \sec [c] \sec [c+d x] (21 B \sin [c]+21 C \right. \\ & \quad \left. \sin [c]+35 A \sin [d x]+35 B \sin [d x]+25 C \sin [d x]) + \frac{4(7 A+7 B+5 C) \tan [c]}{21 d} \right) \Big) / \\ & \left. \left( (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sec [c+d x]^{3 / 2} \right) \right) \end{aligned} \right)$$

**Problem 535: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sqrt{\sec [c+d x]} (a+a \sec [c+d x]) (A+B \sec [c+d x]+C \sec [c+d x]^2) dx$$

Optimal (type 4, 181 leaves, 8 steps):

$$\begin{aligned} & -\frac{1}{5 d} 2 a (5 A+5 B+3 C) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]} + \\ & \frac{1}{3 d} 2 a (3 A+B+C) \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]} + \\ & \frac{2 a (5 A+5 B+3 C) \sqrt{\sec [c+d x]} \sin [c+d x]}{5 d} + \\ & \frac{2 a (B+C) \sec [c+d x]^{3 / 2} \sin [c+d x]}{3 d} + \frac{2 a C \sec [c+d x]^{5 / 2} \sin [c+d x]}{5 d} \end{aligned}$$

Result (type 5, 937 leaves):

$$a \left( - \left( \left( 2 \sqrt{2} A e^{-i(2 c+d x)} \sqrt{\frac{e^{i(c+d x)}}{1+e^{2 i(c+d x)}}} \cos [c+d x]^2 \operatorname{Csc}[c] \right) \right) \right)$$

$$\begin{aligned}
 & \left( \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)} \right] \right) \right. \\
 & \left. (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right) / \left( d (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) \right) - \\
 & \left( 2\sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}}} \operatorname{Cos}[c + dx]^2 \operatorname{Csc}[c] \right. \\
 & \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)} \right] \right) \right. \\
 & \left. (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right) / \left( d (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) \right) - \\
 & \left( 6\sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}}} \operatorname{Cos}[c + dx]^2 \operatorname{Csc}[c] \right. \\
 & \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)} \right] \right) \right. \\
 & \left. (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right) / \left( 5d (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) \right) + \\
 & \left( 4A \operatorname{Cos}[c + dx]^{5/2} \operatorname{EllipticF} \left[ \frac{1}{2}(c + dx), 2 \right] \sqrt{\operatorname{Sec}[c + dx]} \right. \\
 & \left. (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right) / \left( d (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) \right) + \\
 & \left( 4B \operatorname{Cos}[c + dx]^{5/2} \operatorname{EllipticF} \left[ \frac{1}{2}(c + dx), 2 \right] \sqrt{\operatorname{Sec}[c + dx]} \right. \\
 & \left. (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right) / \left( 3d (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) \right) + \\
 & \left( 4C \operatorname{Cos}[c + dx]^{5/2} \operatorname{EllipticF} \left[ \frac{1}{2}(c + dx), 2 \right] \sqrt{\operatorname{Sec}[c + dx]} \right. \\
 & \left. (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right) / \\
 & \left( 3d (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) \right) + \left( (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right. \\
 & \left. \left( \frac{4(5A + 5B + 3C) \operatorname{Cos}[dx] \operatorname{Csc}[c]}{5d} + \frac{4C \operatorname{Sec}[c] \operatorname{Sec}[c + dx]^2 \operatorname{Sin}[dx]}{5d} + \frac{1}{15d} \right. \right. \\
 & \left. \left. 4 \operatorname{Sec}[c] \operatorname{Sec}[c + dx] (3C \operatorname{Sin}[c] + 5B \operatorname{Sin}[dx] + 5C \operatorname{Sin}[dx]) + \frac{4(B + C) \operatorname{Tan}[c]}{3d} \right) \right) / \\
 & \left. \left( (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) \operatorname{Sec}[c + dx]^{3/2} \right) \right)
 \end{aligned}$$

**Problem 536: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \operatorname{Sec}[c + d x]) (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\sqrt{\operatorname{Sec}[c + d x]}} dx$$

Optimal (type 4, 143 leaves, 7 steps):

$$\frac{2 a (A - B - C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{d} +$$

$$\frac{1}{3 d} 2 a (3 A + 3 B + C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]} +$$

$$\frac{2 a (B + C) \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{d} + \frac{2 a C \operatorname{Sec}[c + d x]^{3/2} \operatorname{Sin}[c + d x]}{3 d}$$

Result (type 5, 908 leaves):

$$a \left( \left( 2 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \operatorname{Cos}[c+dx]^2 \operatorname{Csc}[c] \right. \right.$$

$$\left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right.$$

$$\left. (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) / (d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x])) -$$

$$\left( 2 \sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \operatorname{Cos}[c+dx]^2 \operatorname{Csc}[c] \right.$$

$$\left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right.$$

$$\left. (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) / (d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x])) -$$

$$\left( 2 \sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \operatorname{Cos}[c+dx]^2 \operatorname{Csc}[c] \right.$$

$$\left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right.$$

$$\left. (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) / (d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x])) +$$

$$\left( 4 A \operatorname{Cos}[c + d x]^{5/2} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]} \right)$$

$$\begin{aligned}
 & \left. \left( (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) / \left( d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \right) \right) + \\
 & \left( 4 B \operatorname{Cos}[c + d x]^{5/2} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]} \right. \\
 & \left. (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) / \left( d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \right) + \\
 & \left( 4 C \operatorname{Cos}[c + d x]^{5/2} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]} \right. \\
 & \left. (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) / \left( 3 d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \right) + \\
 & \left( (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \left( -\frac{2(A - 2 B - 2 C + A \operatorname{Cos}[2 c]) \operatorname{Cos}[d x] \operatorname{Csc}[c]}{d} + \right. \right. \\
 & \left. \left. \frac{4 A \operatorname{Cos}[c] \operatorname{Sin}[d x]}{d} + \frac{4 C \operatorname{Sec}[c] \operatorname{Sec}[c + d x] \operatorname{Sin}[d x]}{3 d} + \frac{4 C \operatorname{Tan}[c]}{3 d} \right) \right) / \\
 & \left. \left( (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \operatorname{Sec}[c + d x]^{3/2} \right) \right)
 \end{aligned}$$

**Problem 537: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + a \operatorname{Sec}[c + d x]) (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[c + d x]^{3/2}} dx$$

Optimal (type 4, 138 leaves, 7 steps):

$$\begin{aligned}
 & \frac{2 a (A + B - C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{d} + \\
 & \frac{1}{3 d} 2 a (A + 3 (B + C)) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]} + \\
 & \frac{2 a A \operatorname{Sin}[c + d x]}{3 d \sqrt{\operatorname{Sec}[c + d x]}} + \frac{2 a C \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{d}
 \end{aligned}$$

Result (type 5, 162 leaves):

$$\begin{aligned}
 & \frac{1}{3 d} a \sqrt{\operatorname{Sec}[c + d x]} \left( -6 i A \operatorname{Cos}[c + d x] - 6 i B \operatorname{Cos}[c + d x] + \right. \\
 & \left. 6 i C \operatorname{Cos}[c + d x] + 2 (A + 3 (B + C)) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] + \right. \\
 & \left. 6 i (A + B - C) e^{-i(c + d x)} \sqrt{1 + e^{2 i(c + d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c + d x)}\right] + \right. \\
 & \left. 6 C \operatorname{Sin}[c + d x] + A \operatorname{Sin}[2(c + d x)] \right)
 \end{aligned}$$

**Problem 538: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + a \operatorname{Sec}[c + d x]) (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[c + d x]^{5/2}} dx$$

Optimal (type 4, 146 leaves, 7 steps):

$$\begin{aligned} & \frac{1}{5d} 2a (3A + 5(B+C)) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\ & \frac{1}{3d} 2a (A+B+3C) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\ & \frac{2aA \sin[c+dx]}{5d \sec[c+dx]^{3/2}} + \frac{2a(A+B) \sin[c+dx]}{3d \sqrt{\sec[c+dx]}} \end{aligned}$$

Result (type 5, 156 leaves):

$$\begin{aligned} & \frac{1}{30d} a \sqrt{\sec[c+dx]} \left( 20(A+B+3C) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] + \right. \\ & \quad \left. 12i(3A+5(B+C)) e^{-i(c+dx)} \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + \right. \\ & \quad \left. 2 \cos[c+dx] (-6i(3A+5(B+C)) + 10(A+B) \sin[c+dx] + 3A \sin[2(c+dx)]) \right) \end{aligned}$$

**Problem 539: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + a \sec[c+dx]) (A + B \sec[c+dx] + C \sec[c+dx]^2)}{\sec[c+dx]^{7/2}} dx$$

Optimal (type 4, 182 leaves, 8 steps):

$$\begin{aligned} & \frac{1}{5d} 2a (3(A+B) + 5C) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\ & \frac{1}{21d} 2a (5A+7(B+C)) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\ & \frac{2aA \sin[c+dx]}{7d \sec[c+dx]^{5/2}} + \frac{2a(A+B) \sin[c+dx]}{5d \sec[c+dx]^{3/2}} + \frac{2a(5A+7(B+C)) \sin[c+dx]}{21d \sqrt{\sec[c+dx]}} \end{aligned}$$

Result (type 5, 180 leaves):

$$\begin{aligned} & \frac{1}{420d} a \sqrt{\sec[c+dx]} \left( 40(5A+7(B+C)) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] + \right. \\ & \quad \left. 168i(3A+3B+5C) e^{-i(c+dx)} \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + \right. \\ & \quad \left. 2 \cos[c+dx] (-84i(3A+3B+5C) + 5(23A+28(B+C)) \sin[c+dx] + \right. \\ & \quad \left. 42(A+B) \sin[2(c+dx)] + 15A \sin[3(c+dx)]) \right) \end{aligned}$$

**Problem 540: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + a \sec[c+dx]) (A + B \sec[c+dx] + C \sec[c+dx]^2)}{\sec[c+dx]^{9/2}} dx$$

Optimal (type 4, 215 leaves, 9 steps):



$$\begin{aligned} & \frac{1}{15d} 2a(7A+9(B+C)) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \frac{1}{21d} \\ & 2a(5(A+B)+7C) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \frac{2aA \sin[c+dx]}{9d \sec[c+dx]^{7/2}} + \\ & \frac{2a(A+B) \sin[c+dx]}{7d \sec[c+dx]^{5/2}} + \frac{2a(7A+9(B+C)) \sin[c+dx]}{45d \sec[c+dx]^{3/2}} + \frac{2a(5(A+B)+7C) \sin[c+dx]}{21d \sqrt{\sec[c+dx]}} \end{aligned}$$

Result (type 5, 210 leaves):

$$\begin{aligned} & \frac{1}{2520d} a \sqrt{\sec[c+dx]} \\ & \left( 240(5A+5B+7C) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] + 336i(7A+9(B+C)) \right. \\ & \quad e^{-i(c+dx)} \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + 2 \cos[c+dx] \\ & \quad \left. (-1176iA - 1512iB - 1512iC + 30(23A+23B+28C) \sin[c+dx] + 14(19A+18(B+C)) \right. \\ & \quad \left. \sin[2(c+dx)] + 90A \sin[3(c+dx)] + 90B \sin[3(c+dx)] + 35A \sin[4(c+dx)] \right) \end{aligned}$$

**Problem 541: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sec[c+dx]^{3/2} (a+a \sec[c+dx])^2 (A+B \sec[c+dx]+C \sec[c+dx]^2) dx$$

Optimal (type 4, 291 leaves, 10 steps):

$$\begin{aligned} & -\frac{1}{15d} 4a^2(12A+9B+8C) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\ & \frac{1}{21d} 4a^2(7A+6B+5C) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\ & \frac{4a^2(12A+9B+8C) \sqrt{\sec[c+dx]} \sin[c+dx]}{15d} + \frac{4a^2(7A+6B+5C) \sec[c+dx]^{3/2} \sin[c+dx]}{21d} + \\ & \frac{2a^2(21A+27B+19C) \sec[c+dx]^{5/2} \sin[c+dx]}{105d} + \\ & \frac{2C \sec[c+dx]^{5/2} (a+a \sec[c+dx])^2 \sin[c+dx]}{9d} + \\ & \frac{2(9B+4C) \sec[c+dx]^{5/2} (a^2+a^2 \sec[c+dx]) \sin[c+dx]}{63d} \end{aligned}$$

Result (type 5, 1240 leaves):

$$\begin{aligned} & -\left( \left( 4\sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^4 \operatorname{Csc}[c] \right. \right. \\ & \quad \left. \left. (1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}}) \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right) \end{aligned}$$

$$\begin{aligned}
 & \left. \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a + a \sec[c + dx])^2 (A + B \sec[c + dx] + C \sec[c + dx]^2)\right) / \\
 & \left. (5d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) \right) - \\
 & \left( 3\sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}}} \cos[c + dx]^4 \operatorname{Csc}[c] \right. \\
 & \left. (1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right]) \right) \\
 & \left. \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a + a \sec[c + dx])^2 (A + B \sec[c + dx] + C \sec[c + dx]^2)\right) / \\
 & (5d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) - \\
 & \left( 8\sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}}} \cos[c + dx]^4 \operatorname{Csc}[c] \right. \\
 & \left. (1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right]) \right) \\
 & \left. \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a + a \sec[c + dx])^2 (A + B \sec[c + dx] + C \sec[c + dx]^2)\right) / \\
 & (15d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])) + \\
 & \left( 2A \sqrt{\cos[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \right. \\
 & \left. (a + a \sec[c + dx])^2 (A + B \sec[c + dx] + C \sec[c + dx]^2)\right) / \\
 & (3d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sec[c + dx]^{7/2}) + \\
 & \left( 4B \sqrt{\cos[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \right. \\
 & \left. (a + a \sec[c + dx])^2 (A + B \sec[c + dx] + C \sec[c + dx]^2)\right) / \\
 & (7d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sec[c + dx]^{7/2}) + \\
 & \left( 10C \sqrt{\cos[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \right. \\
 & \left. (a + a \sec[c + dx])^2 (A + B \sec[c + dx] + C \sec[c + dx]^2)\right) / \\
 & (21d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sec[c + dx]^{7/2}) + \\
 & \frac{1}{(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sec[c + dx]^{7/2}} \\
 & \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a + a \sec[c + dx])^2 (A + B \sec[c + dx] + C \sec[c + dx]^2)
 \end{aligned}$$

$$\left( \frac{2 (12 A + 9 B + 8 C) \cos [d x] \operatorname{Csc}[c]}{15 d} + \frac{C \operatorname{Sec}[c] \operatorname{Sec}[c+d x]^4 \sin [d x]}{9 d} + \frac{\operatorname{Sec}[c] \operatorname{Sec}[c+d x]^3 (7 C \sin [c] + 9 B \sin [d x] + 18 C \sin [d x])}{63 d} + \frac{1}{315 d} \operatorname{Sec}[c] \operatorname{Sec}[c+d x]^2 (45 B \sin [c] + 90 C \sin [c] + 63 A \sin [d x] + 126 B \sin [d x] + 112 C \sin [d x]) + \frac{1}{315 d} \operatorname{Sec}[c] \operatorname{Sec}[c+d x] (63 A \sin [c] + 126 B \sin [c] + 112 C \sin [c] + 210 A \sin [d x] + 180 B \sin [d x] + 150 C \sin [d x]) + \frac{2 (7 A + 6 B + 5 C) \operatorname{Tan}[c]}{21 d} \right)$$

**Problem 542: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sqrt{\operatorname{Sec}[c+d x]} (a+a \operatorname{Sec}[c+d x])^2 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) dx$$

Optimal (type 4, 255 leaves, 9 steps):

$$\begin{aligned} & -\frac{1}{5 d} 4 a^2 (5 A+4 B+3 C) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\operatorname{Sec}[c+d x]} + \\ & \frac{1}{21 d} 4 a^2 (14 A+7 B+6 C) \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\operatorname{Sec}[c+d x]} + \\ & \frac{4 a^2 (5 A+4 B+3 C) \sqrt{\operatorname{Sec}[c+d x]} \sin [c+d x]}{5 d} + \\ & \frac{2 a^2 (35 A+49 B+33 C) \operatorname{Sec}[c+d x]^{3 / 2} \sin [c+d x]}{105 d} + \\ & \frac{2 C \operatorname{Sec}[c+d x]^{3 / 2} (a+a \operatorname{Sec}[c+d x])^2 \sin [c+d x]}{7 d} + \\ & \frac{2 (7 B+4 C) \operatorname{Sec}[c+d x]^{3 / 2} (a^2+a^2 \operatorname{Sec}[c+d x]) \sin [c+d x]}{35 d} \end{aligned}$$

Result (type 5, 1184 leaves):

$$\begin{aligned} & -\left( \left( \sqrt{2} A e^{-i(2 c+d x)} \sqrt{\frac{e^{i(c+d x)}}{1+e^{2 i(c+d x)}}} \cos [c+d x]^4 \operatorname{Csc}[c] \right. \right. \\ & \left. \left. \left( 1+e^{2 i(c+d x)} + (-1+e^{2 i c}) \sqrt{1+e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right] \right) \right. \right. \\ & \left. \left. \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \right) \right) / \\ & \left. \left( d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right) \right) - \end{aligned}$$

$$\begin{aligned}
 & \left( 4 \sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^4 \operatorname{Csc}[c] \right. \\
 & \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \operatorname{Sec}[c+dx])^2 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & (5d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx])) - \\
 & \left( 3 \sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^4 \operatorname{Csc}[c] \right. \\
 & \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \operatorname{Sec}[c+dx])^2 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & (5d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx])) + \\
 & \left( 4A \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \right. \\
 & \quad \left. (a+a \operatorname{Sec}[c+dx])^2 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & (3d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \operatorname{Sec}[c+dx]^{7/2}) + \\
 & \left( 2B \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \right. \\
 & \quad \left. (a+a \operatorname{Sec}[c+dx])^2 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & (3d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \operatorname{Sec}[c+dx]^{7/2}) + \\
 & \left( 4C \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \right. \\
 & \quad \left. (a+a \operatorname{Sec}[c+dx])^2 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & (7d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \operatorname{Sec}[c+dx]^{7/2}) + \\
 & \left( \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \operatorname{Sec}[c+dx])^2 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right. \\
 & \quad \left( \frac{2(5A+4B+3C) \cos[dx] \operatorname{Csc}[c]}{5d} + \frac{C \operatorname{Sec}[c] \operatorname{Sec}[c+dx]^3 \operatorname{Sin}[dx]}{7d} + \right. \\
 & \quad \left. \frac{\operatorname{Sec}[c] \operatorname{Sec}[c+dx]^2 (5C \operatorname{Sin}[c] + 7B \operatorname{Sin}[dx] + 14C \operatorname{Sin}[dx])}{35d} + \frac{1}{105d} \right. \\
 & \quad \left. \operatorname{Sec}[c] \operatorname{Sec}[c+dx] (21B \operatorname{Sin}[c] + 42C \operatorname{Sin}[c] + 35A \operatorname{Sin}[dx] + 70B \operatorname{Sin}[dx] + 60C \operatorname{Sin}[dx]) + \right. \\
 & \quad \left. \left. \frac{(7A+14B+12C) \operatorname{Tan}[c]}{21d} \right) \right) / ((A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \operatorname{Sec}[c+dx]^{7/2})
 \end{aligned}$$

Problem 543: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(a + a \sec [c + d x])^2 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sqrt{\sec [c + d x]}} dx$$

Optimal (type 4, 214 leaves, 8 steps):

$$\begin{aligned} & -\frac{1}{5d} 4a^2 (5B + 4C) \sqrt{\cos [c + dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\sec [c + dx]} + \\ & \frac{1}{3d} 4a^2 (3A + 2B + C) \sqrt{\cos [c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\sec [c + dx]} + \\ & \frac{2a^2 (15A + 25B + 17C) \sqrt{\sec [c + dx]} \sin [c + dx]}{15d} + \\ & \frac{2C \sqrt{\sec [c + dx]} (a + a \sec [c + dx])^2 \sin [c + dx]}{5d} + \\ & \frac{2(5B + 4C) \sqrt{\sec [c + dx]} (a^2 + a^2 \sec [c + dx]) \sin [c + dx]}{15d} \end{aligned}$$

Result (type 5, 942 leaves):

$$\begin{aligned} & -\left( \left( \sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos [c + dx]^4 \operatorname{Csc}[c] \right. \right. \\ & \quad \left. \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \right. \\ & \quad \left. \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a + a \sec [c + dx])^2 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) \right) / \\ & \quad \left. \left. \left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \right) \right) - \right. \\ & \left( 4\sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos [c + dx]^4 \operatorname{Csc}[c] \right. \\ & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right) / \\ & \quad \left. \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a + a \sec [c + dx])^2 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) \right) / \\ & \quad \left( 5d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \right) + \\ & \quad \left( 2A \sqrt{\cos [c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \right) \end{aligned}$$

$$\begin{aligned}
 & \left( (a + a \operatorname{Sec}[c + d x])^2 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) / \\
 & \left( d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \operatorname{Sec}[c + d x]^{7/2} \right) + \\
 & \left( 4 B \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^4 \right. \\
 & \left. (a + a \operatorname{Sec}[c + d x])^2 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) / \\
 & \left( 3 d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \operatorname{Sec}[c + d x]^{7/2} \right) + \\
 & \left( 2 C \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^4 \right. \\
 & \left. (a + a \operatorname{Sec}[c + d x])^2 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) / \\
 & \left( 3 d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \operatorname{Sec}[c + d x]^{7/2} \right) + \\
 & \left( \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^4 (a + a \operatorname{Sec}[c + d x])^2 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \left( -\frac{(-5 A - 20 B - 16 C + 5 A \operatorname{Cos}[2 c]) \operatorname{Cos}[d x] \operatorname{Csc}[c]}{10 d} + \right. \\
 & \frac{A \operatorname{Cos}[c] \operatorname{Sin}[d x]}{d} + \frac{C \operatorname{Sec}[c] \operatorname{Sec}[c + d x]^2 \operatorname{Sin}[d x]}{5 d} + \\
 & \left. \left. \frac{\operatorname{Sec}[c] \operatorname{Sec}[c + d x] (3 C \operatorname{Sin}[c] + 5 B \operatorname{Sin}[d x] + 10 C \operatorname{Sin}[d x])}{15 d} + \frac{(B + 2 C) \operatorname{Tan}[c]}{3 d} \right) \right) / \\
 & \left( (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \operatorname{Sec}[c + d x]^{7/2} \right)
 \end{aligned}$$

**Problem 544: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + a \operatorname{Sec}[c + d x])^2 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[c + d x]^{3/2}} dx$$

Optimal (type 4, 208 leaves, 8 steps):

$$\begin{aligned}
 & \frac{4 a^2 (A - C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{d} + \frac{1}{3 d} \\
 & - \frac{4 a^2 (2 A + 3 B + 2 C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{2} - \\
 & \frac{2 a^2 (A - 3 B - 5 C) \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{3 d} + \frac{2 A (a + a \operatorname{Sec}[c + d x])^2 \operatorname{Sin}[c + d x]}{3 d \sqrt{\operatorname{Sec}[c + d x]}} - \\
 & \frac{2 (A - C) \sqrt{\operatorname{Sec}[c + d x]} (a^2 + a^2 \operatorname{Sec}[c + d x]) \operatorname{Sin}[c + d x]}{3 d}
 \end{aligned}$$

Result (type 5, 233 leaves):

$$\begin{aligned} & \frac{1}{6d} a^2 e^{-i(2c+dx)} \operatorname{Sec}[c+dx]^{3/2} \left( -12iA + 12iC - 12iA \operatorname{Cos}[2(c+dx)] + \right. \\ & \quad 12iC \operatorname{Cos}[2(c+dx)] + 8(2A+3B+2C) \operatorname{Cos}[c+dx]^{3/2} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] + \\ & \quad 12i(A-C) e^{-2i(c+dx)} (1+e^{2i(c+dx)})^{3/2} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + \\ & \quad A \operatorname{Sin}[c+dx] + 4C \operatorname{Sin}[c+dx] + 6B \operatorname{Sin}[2(c+dx)] + \\ & \quad \left. 12C \operatorname{Sin}[2(c+dx)] + A \operatorname{Sin}[3(c+dx)] \right) (\operatorname{Cos}[2c+dx] + i \operatorname{Sin}[2c+dx]) \end{aligned}$$

**Problem 545: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + a \operatorname{Sec}[c+dx])^2 (A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2)}{\operatorname{Sec}[c+dx]^{5/2}} dx$$

Optimal (type 4, 214 leaves, 8 steps):

$$\begin{aligned} & \frac{1}{5d} 4a^2 (4A+5B) \sqrt{\operatorname{Cos}[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\operatorname{Sec}[c+dx]} + \\ & \frac{1}{3d} 4a^2 (A+2B+3C) \sqrt{\operatorname{Cos}[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\operatorname{Sec}[c+dx]} - \\ & \frac{2a^2 (7A+5B-15C) \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{15d} + \\ & \frac{2A(a+a \operatorname{Sec}[c+dx])^2 \operatorname{Sin}[c+dx]}{5d \operatorname{Sec}[c+dx]^{3/2}} + \frac{2(4A+5B)(a^2+a^2 \operatorname{Sec}[c+dx]) \operatorname{Sin}[c+dx]}{15d \sqrt{\operatorname{Sec}[c+dx]}} \end{aligned}$$

Result (type 5, 187 leaves):

$$\begin{aligned} & \frac{1}{30d} a^2 \sqrt{\operatorname{Sec}[c+dx]} \left( -96iA \operatorname{Cos}[c+dx] - 120iB \operatorname{Cos}[c+dx] + \right. \\ & \quad 40(A+2B+3C) \sqrt{\operatorname{Cos}[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] + 24i(4A+5B) e^{-i(c+dx)} \\ & \quad \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + 3A \operatorname{Sin}[c+dx] + \\ & \quad \left. 60C \operatorname{Sin}[c+dx] + 20A \operatorname{Sin}[2(c+dx)] + 10B \operatorname{Sin}[2(c+dx)] + 3A \operatorname{Sin}[3(c+dx)] \right) \end{aligned}$$

**Problem 546: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + a \operatorname{Sec}[c+dx])^2 (A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2)}{\operatorname{Sec}[c+dx]^{7/2}} dx$$

Optimal (type 4, 219 leaves, 8 steps):

$$\begin{aligned} & \frac{1}{5d} 4a^2 (3A+4B+5C) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\ & \frac{1}{21d} 4a^2 (6A+7B+14C) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\ & \frac{2a^2 (33A+49B+35C) \sin[c+dx]}{105d \sqrt{\sec[c+dx]}} + \frac{2A (a+a \sec[c+dx])^2 \sin[c+dx]}{7d \sec[c+dx]^{5/2}} + \\ & \frac{2(4A+7B) (a^2+a^2 \sec[c+dx]) \sin[c+dx]}{35d \sec[c+dx]^{3/2}} \end{aligned}$$

Result (type 5, 189 leaves):

$$\begin{aligned} & \frac{1}{420d} a^2 \sqrt{\sec[c+dx]} \left( 80(6A+7(B+2C)) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] + \right. \\ & \quad 336i(3A+4B+5C) e^{-i(c+dx)} \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + \\ & \quad \left. 2 \cos[c+dx] (-504iA - 672iB - 840iC + 5(51A+28(2B+C)) \sin[c+dx] + \right. \\ & \quad \left. 42(2A+B) \sin[2(c+dx)] + 15A \sin[3(c+dx)] \right) \end{aligned}$$

**Problem 547: Result unnecessarily involves higher level functions.**

$$\int \frac{(a+a \sec[c+dx])^2 (A+B \sec[c+dx] + C \sec[c+dx]^2)}{\sec[c+dx]^{9/2}} dx$$

Optimal (type 4, 255 leaves, 9 steps):

$$\begin{aligned} & \frac{1}{15d} 4a^2 (8A+9B+12C) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\ & \frac{1}{21d} 4a^2 (5A+6B+7C) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\ & \frac{2a^2 (19A+27B+21C) \sin[c+dx]}{105d \sec[c+dx]^{3/2}} + \frac{4a^2 (5A+6B+7C) \sin[c+dx]}{21d \sqrt{\sec[c+dx]}} + \\ & \frac{2A (a+a \sec[c+dx])^2 \sin[c+dx]}{9d \sec[c+dx]^{7/2}} + \frac{2(4A+9B) (a^2+a^2 \sec[c+dx]) \sin[c+dx]}{63d \sec[c+dx]^{5/2}} \end{aligned}$$

Result (type 5, 248 leaves):

$$\begin{aligned} & \frac{1}{2520d} a^2 e^{-i(2c+dx)} \sqrt{\sec[c+dx]} \left( 480(5A+6B+7C) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] + \right. \\ & \quad 672i(8A+9B+12C) e^{-i(c+dx)} \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + \\ & \quad \left. 2 \cos[c+dx] (-2688iA - 3024iB - 4032iC + 30(46A+51B+56C) \sin[c+dx] + \right. \\ & \quad \left. 14(37A+36B+18C) \sin[2(c+dx)] + 180A \sin[3(c+dx)] + \right. \\ & \quad \left. 90B \sin[3(c+dx)] + 35A \sin[4(c+dx)] \right) (\cos[2c+dx] + i \sin[2c+dx]) \end{aligned}$$

**Problem 548: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**



$$\int \frac{(a + a \operatorname{Sec}[c + d x])^2 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[c + d x]^{11/2}} dx$$

Optimal (type 4, 291 leaves, 10 steps):

$$\begin{aligned} & \frac{1}{15 d} 4 a^2 (7 A + 8 B + 9 C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]} + \\ & \frac{1}{231 d} 4 a^2 (50 A + 55 B + 66 C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]} + \\ & \frac{2 a^2 (89 A + 121 B + 99 C) \operatorname{Sin}[c + d x]}{693 d \operatorname{Sec}[c + d x]^{5/2}} + \frac{4 a^2 (7 A + 8 B + 9 C) \operatorname{Sin}[c + d x]}{45 d \operatorname{Sec}[c + d x]^{3/2}} + \\ & \frac{4 a^2 (50 A + 55 B + 66 C) \operatorname{Sin}[c + d x]}{231 d \sqrt{\operatorname{Sec}[c + d x]}} + \frac{2 A (a + a \operatorname{Sec}[c + d x])^2 \operatorname{Sin}[c + d x]}{11 d \operatorname{Sec}[c + d x]^{9/2}} + \\ & \frac{2 (4 A + 11 B) (a^2 + a^2 \operatorname{Sec}[c + d x]) \operatorname{Sin}[c + d x]}{99 d \operatorname{Sec}[c + d x]^{7/2}} \end{aligned}$$

Result (type 5, 1337 leaves):

$$\begin{aligned} & \left( 7 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \operatorname{Cos}[c+dx]^4 \operatorname{Csc}[c] \right. \\ & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\ & \quad \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a + a \operatorname{Sec}[c + d x])^2 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) / \\ & (15 d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x])) + \\ & \left( 8 \sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \operatorname{Cos}[c+dx]^4 \operatorname{Csc}[c] \right. \\ & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\ & \quad \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a + a \operatorname{Sec}[c + d x])^2 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) / \\ & (15 d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x])) + \\ & \left( 3 \sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \operatorname{Cos}[c+dx]^4 \operatorname{Csc}[c] \right. \\ & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\ & \quad \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a + a \operatorname{Sec}[c + d x])^2 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) / \end{aligned}$$

$$\begin{aligned}
 & \left( 5 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right) + \\
 & \left( 100 A \sqrt{\cos [c + d x]} \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \right. \\
 & \quad \left. (a + a \operatorname{Sec} [c + d x])^2 (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) \right) / \\
 & \left( 231 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \operatorname{Sec} [c + d x]^{7/2} \right) + \\
 & \left( 10 B \sqrt{\cos [c + d x]} \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \right. \\
 & \quad \left. (a + a \operatorname{Sec} [c + d x])^2 (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) \right) / \\
 & \left( 21 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \operatorname{Sec} [c + d x]^{7/2} \right) + \\
 & \left( 4 C \sqrt{\cos [c + d x]} \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \right. \\
 & \quad \left. (a + a \operatorname{Sec} [c + d x])^2 (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) \right) / \\
 & \left( 7 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \operatorname{Sec} [c + d x]^{7/2} \right) + \\
 & \quad \frac{1}{(A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \operatorname{Sec} [c + d x]^{7/2}} \\
 & \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a + a \operatorname{Sec} [c + d x])^2 (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) \\
 & \left( - \frac{1}{720 d} (298 A + 347 B + 396 C + 374 A \cos [2 c] + 421 B \cos [2 c] + 468 C \cos [2 c]) \cos [d x] \operatorname{Csc} [c] + \right. \\
 & \quad \frac{(2185 A + 2288 B + 2376 C) \cos [2 d x] \sin [2 c]}{7392 d} + \frac{(86 A + 79 B + 72 C) \cos [3 d x] \sin [3 c]}{720 d} + \\
 & \quad \frac{(27 A + 22 B + 11 C) \cos [4 d x] \sin [4 c]}{616 d} + \frac{(2 A + B) \cos [5 d x] \sin [5 c]}{144 d} + \\
 & \quad \frac{A \cos [6 d x] \sin [6 c]}{352 d} + \frac{(374 A + 421 B + 468 C) \cos [c] \sin [d x]}{360 d} + \\
 & \quad \frac{(2185 A + 2288 B + 2376 C) \cos [2 c] \sin [2 d x]}{7392 d} + \frac{(86 A + 79 B + 72 C) \cos [3 c] \sin [3 d x]}{720 d} \\
 & \quad \left. \frac{(27 A + 22 B + 11 C) \cos [4 c] \sin [4 d x]}{616 d} + \frac{(2 A + B) \cos [5 c] \sin [5 d x]}{144 d} + \frac{A \cos [6 c] \sin [6 d x]}{352 d} \right)
 \end{aligned}$$

**Problem 549: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec} [c + d x]^{3/2} (a + a \operatorname{Sec} [c + d x])^3 (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) dx$$

Optimal (type 4, 343 leaves, 11 steps):

$$\begin{aligned}
 & -\frac{1}{15d} 4a^3 (21A + 17B + 15C) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \frac{1}{231d} \\
 & 4a^3 (143A + 121B + 105C) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\
 & \frac{4a^3 (21A + 17B + 15C) \sqrt{\sec[c+dx]} \sin[c+dx]}{15d} + \\
 & \frac{4a^3 (143A + 121B + 105C) \sec[c+dx]^{3/2} \sin[c+dx]}{231d} + \\
 & \frac{4a^3 (264A + 253B + 210C) \sec[c+dx]^{5/2} \sin[c+dx]}{1155d} + \\
 & \frac{2C \sec[c+dx]^{5/2} (a+a \sec[c+dx])^3 \sin[c+dx]}{11d} + \\
 & \frac{2(11B + 6C) \sec[c+dx]^{5/2} (a^2 + a^2 \sec[c+dx])^2 \sin[c+dx]}{99ad} + \frac{1}{693d} \\
 & 2(99A + 143B + 105C) \sec[c+dx]^{5/2} (a^3 + a^3 \sec[c+dx]) \sin[c+dx]
 \end{aligned}$$

Result (type 5, 1292 leaves):

$$\begin{aligned}
 & -\left( \left( 7A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^5 \operatorname{Csc}[c] \right. \right. \\
 & \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \left. \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \sec[c+dx])^3 (A+B \sec[c+dx] + C \sec[c+dx]^2) \right) \right) / \\
 & \quad \left( 5\sqrt{2} d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right) - \\
 & \left( 17B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^5 \operatorname{Csc}[c] \right. \\
 & \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \left. \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \sec[c+dx])^3 (A+B \sec[c+dx] + C \sec[c+dx]^2) \right) \right) / \\
 & \quad \left( 15\sqrt{2} d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right) - \\
 & \left( C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^5 \operatorname{Csc}[c] \right. \\
 & \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right) / \\
 & \left( \sqrt{2} d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \right) + \\
 & \left( 13A \sqrt{\cos[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \right. \\
 & \quad \left. (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right) / \\
 & (21d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sec[c + dx]^{9/2}) + \\
 & \left( 11B \sqrt{\cos[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \right. \\
 & \quad \left. (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right) / \\
 & (21d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sec[c + dx]^{9/2}) + \\
 & \left( 5C \sqrt{\cos[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \right. \\
 & \quad \left. (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right) / \\
 & (11d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sec[c + dx]^{9/2}) + \\
 & \frac{1}{(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sec[c + dx]^{9/2}} \\
 & \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \\
 & \left( \frac{(21A + 17B + 15C) \cos[dx] \operatorname{Csc}[c]}{15d} + \frac{C \sec[c] \sec[c + dx]^5 \sin[dx]}{22d} + \right. \\
 & \quad \left. \frac{\sec[c] \sec[c + dx]^4 (9C \sin[c] + 11B \sin[dx] + 33C \sin[dx])}{198d} + \frac{1}{1386d} \sec[c] \right. \\
 & \quad \left. \sec[c + dx]^3 (77B \sin[c] + 231C \sin[c] + 99A \sin[dx] + 297B \sin[dx] + 378C \sin[dx]) + \right. \\
 & \quad \left. \frac{1}{6930d} \sec[c] \sec[c + dx]^2 (495A \sin[c] + 1485B \sin[c] + 1890C \sin[c] + \right. \\
 & \quad \left. 2079A \sin[dx] + 2618B \sin[dx] + 2310C \sin[dx]) + \frac{1}{6930d} \right. \\
 & \quad \left. \sec[c] \sec[c + dx] (2079A \sin[c] + 2618B \sin[c] + 2310C \sin[c] + 4290A \sin[dx] + \right. \\
 & \quad \left. 3630B \sin[dx] + 3150C \sin[dx]) + \frac{(143A + 121B + 105C) \operatorname{Tan}[c]}{231d} \right)
 \end{aligned}$$

**Problem 550: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sqrt{\sec[c + dx]} (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) dx$$

Optimal (type 4, 307 leaves, 10 steps):

$$\begin{aligned}
 & -\frac{1}{15d} 4a^3 (27A + 21B + 17C) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\
 & \frac{1}{21d} 4a^3 (21A + 13B + 11C) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\
 & \frac{4a^3 (27A + 21B + 17C) \sqrt{\sec[c+dx]} \sin[c+dx]}{15d} + \\
 & \frac{4a^3 (42A + 41B + 32C) \sec[c+dx]^{3/2} \sin[c+dx]}{105d} + \\
 & \frac{2C \sec[c+dx]^{3/2} (a + a \sec[c+dx])^3 \sin[c+dx]}{9d} + \\
 & \frac{2(3B + 2C) \sec[c+dx]^{3/2} (a^2 + a^2 \sec[c+dx])^2 \sin[c+dx]}{21ad} + \\
 & \frac{2(63A + 99B + 73C) \sec[c+dx]^{3/2} (a^3 + a^3 \sec[c+dx]) \sin[c+dx]}{315d}
 \end{aligned}$$

Result (type 5, 1237 leaves):

$$\begin{aligned}
 & -\left( \left( 9A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^5 \operatorname{Csc}[c] \right. \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c+dx])^3 (A + B \sec[c+dx] + C \sec[c+dx]^2) \right) \right) / \\
 & \quad \left( 5\sqrt{2} d (A + 2C + 2B \cos[c+dx] + A \cos[2c + 2dx]) \right) - \\
 & \left( 7B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^5 \operatorname{Csc}[c] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c+dx])^3 (A + B \sec[c+dx] + C \sec[c+dx]^2) \right) \right) / \\
 & \quad \left( 5\sqrt{2} d (A + 2C + 2B \cos[c+dx] + A \cos[2c + 2dx]) \right) - \\
 & \left( 17C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^5 \operatorname{Csc}[c] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right) / \\
 & \left( 15\sqrt{2} d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \right) + \\
 & \left( A \sqrt{\cos[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \right. \\
 & \quad \left. (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right) / \\
 & \left( d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sec[c + dx]^{9/2} \right) + \\
 & \left( 13B \sqrt{\cos[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \right. \\
 & \quad \left. (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right) / \\
 & \left( 21d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sec[c + dx]^{9/2} \right) + \\
 & \left( 11C \sqrt{\cos[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \right. \\
 & \quad \left. (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right) / \\
 & \left( 21d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sec[c + dx]^{9/2} \right) + \\
 & \frac{1}{(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sec[c + dx]^{9/2}} \\
 & \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \\
 & \left( \frac{(27A + 21B + 17C) \cos[dx] \operatorname{Csc}[c]}{15d} + \frac{C \sec[c] \sec[c + dx]^4 \sin[dx]}{18d} + \right. \\
 & \quad \left. \frac{\sec[c] \sec[c + dx]^3 (7C \sin[c] + 9B \sin[dx] + 27C \sin[dx])}{126d} + \frac{1}{630d} \sec[c] \sec[c + dx]^2 \right. \\
 & \quad \left. (45B \sin[c] + 135C \sin[c] + 63A \sin[dx] + 189B \sin[dx] + 238C \sin[dx]) + \right. \\
 & \quad \left. \frac{1}{630d} \sec[c] \sec[c + dx] (63A \sin[c] + 189B \sin[c] + 238C \sin[c] + \right. \\
 & \quad \left. 315A \sin[dx] + 390B \sin[dx] + 330C \sin[dx]) + \frac{(21A + 26B + 22C) \tan[c]}{42d} \right)
 \end{aligned}$$

**Problem 551: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2)}{\sqrt{\sec[c + dx]}} dx$$

Optimal (type 4, 271 leaves, 9 steps):

$$\begin{aligned}
 & -\frac{1}{5d} 4a^3 (5A+9B+7C) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\
 & \frac{1}{21d} 4a^3 (35A+21B+13C) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\
 & \frac{4a^3 (140A+147B+106C) \sqrt{\sec[c+dx]} \sin[c+dx]}{105d} + \\
 & \frac{2C \sqrt{\sec[c+dx]} (a+a \sec[c+dx])^3 \sin[c+dx]}{7d} + \\
 & \frac{2(7B+6C) \sqrt{\sec[c+dx]} (a^2+a^2 \sec[c+dx])^2 \sin[c+dx]}{35ad} + \\
 & \frac{2(5A+9B+7C) \sqrt{\sec[c+dx]} (a^3+a^3 \sec[c+dx]) \sin[c+dx]}{15d}
 \end{aligned}$$

Result (type 5, 1202 leaves):

$$\begin{aligned}
 & -\left( \left( A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^5 \operatorname{Csc}[c] \right. \right. \\
 & \quad \left. \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \sec[c+dx])^3 (A+B \sec[c+dx] + C \sec[c+dx]^2) \right) \right) / \\
 & \quad \left. \left( \sqrt{2} d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right) \right) - \\
 & \left( 9B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^5 \operatorname{Csc}[c] \right. \\
 & \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \sec[c+dx])^3 (A+B \sec[c+dx] + C \sec[c+dx]^2) \right) / \\
 & \quad \left( 5\sqrt{2} d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right) - \\
 & \left( 7C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^5 \operatorname{Csc}[c] \right. \\
 & \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right)
 \end{aligned}$$

$$\left. \begin{aligned} & \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \Bigg/ \\ & \left( 5\sqrt{2} d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \right) + \\ & \left( 5A \sqrt{\cos[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \right. \\ & \quad \left. (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right) \Bigg/ \\ & \left( 3d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sec[c + dx]^{9/2} \right) + \\ & \left( B \sqrt{\cos[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \right. \\ & \quad \left. (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right) \Bigg/ \\ & \left( d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sec[c + dx]^{9/2} \right) + \\ & \left( 13C \sqrt{\cos[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \right. \\ & \quad \left. (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right) \Bigg/ \\ & \left( 21d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sec[c + dx]^{9/2} \right) + \\ & \left( \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\ & \quad \left( -\frac{(-25A - 36B - 28C + 5A \cos[2c]) \cos[dx] \operatorname{Csc}[c]}{20d} + \right. \\ & \quad \frac{A \cos[c] \sin[dx]}{2d} + \frac{C \sec[c] \sec[c + dx]^3 \sin[dx]}{14d} + \\ & \quad \frac{\sec[c] \sec[c + dx]^2 (5C \sin[c] + 7B \sin[dx] + 21C \sin[dx])}{70d} + \frac{1}{210d} \sec[c] \\ & \quad \left. \left. \sec[c + dx] (21B \sin[c] + 63C \sin[c] + 35A \sin[dx] + 105B \sin[dx] + 130C \sin[dx]) + \right. \right. \\ & \quad \left. \left. \frac{(7A + 21B + 26C) \tan[c]}{42d} \right) \right) \Bigg/ \left( (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sec[c + dx]^{9/2} \right) \end{aligned} \right)$$

**Problem 552: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2)}{\sec[c + dx]^{3/2}} dx$$

Optimal (type 4, 271 leaves, 9 steps):



$$\begin{aligned}
 & \frac{1}{5d} 4a^3 (5A - 5B - 9C) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\
 & \frac{1}{3d} 4a^3 (5A + 5B + 3C) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\
 & \frac{4a^3 (5A + 20B + 21C) \sqrt{\sec[c+dx]} \sin[c+dx]}{15d} + \frac{2A (a + a \sec[c+dx])^3 \sin[c+dx]}{3d \sqrt{\sec[c+dx]}} - \\
 & \frac{2(5A - 3C) \sqrt{\sec[c+dx]} (a^2 + a^2 \sec[c+dx])^2 \sin[c+dx]}{15ad} - \\
 & \frac{2(5A - 5B - 9C) \sqrt{\sec[c+dx]} (a^3 + a^3 \sec[c+dx]) \sin[c+dx]}{15d}
 \end{aligned}$$

Result (type 5, 1190 leaves):

$$\begin{aligned}
 & \left( A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^5 \operatorname{Csc}[c] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c+dx])^3 (A + B \sec[c+dx] + C \sec[c+dx]^2) \right) / \\
 & \quad \left( \sqrt{2} d (A + 2C + 2B \cos[c+dx] + A \cos[2c + 2dx]) \right) - \\
 & \left( B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^5 \operatorname{Csc}[c] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c+dx])^3 (A + B \sec[c+dx] + C \sec[c+dx]^2) \right) / \\
 & \quad \left( \sqrt{2} d (A + 2C + 2B \cos[c+dx] + A \cos[2c + 2dx]) \right) - \\
 & \left( 9C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^5 \operatorname{Csc}[c] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c+dx])^3 (A + B \sec[c+dx] + C \sec[c+dx]^2) \right) / \\
 & \quad \left( 5\sqrt{2} d (A + 2C + 2B \cos[c+dx] + A \cos[2c + 2dx]) \right) + \\
 & \left( 5A \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \right)
 \end{aligned}$$

$$\begin{aligned} & \left( (a + a \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) / \\ & (3 d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \operatorname{Sec}[c + d x]^{9/2}) + \\ & \left( 5 B \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 \right. \\ & \left. (a + a \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) / \\ & (3 d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \operatorname{Sec}[c + d x]^{9/2}) + \\ & \left( C \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 \right. \\ & \left. (a + a \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) / \\ & (d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \operatorname{Sec}[c + d x]^{9/2}) + \\ & \left( \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\ & \left. \left( -\frac{1}{20 d} (5 A - 25 B - 36 C + 15 A \operatorname{Cos}[2 c] + 5 B \operatorname{Cos}[2 c]) \operatorname{Cos}[d x] \operatorname{Csc}[c] + \right. \right. \\ & \left. \frac{A \operatorname{Cos}[2 d x] \operatorname{Sin}[2 c]}{12 d} + \frac{(3 A + B) \operatorname{Cos}[c] \operatorname{Sin}[d x]}{2 d} + \frac{C \operatorname{Sec}[c] \operatorname{Sec}[c + d x]^2 \operatorname{Sin}[d x]}{10 d} + \right. \\ & \left. \frac{\operatorname{Sec}[c] \operatorname{Sec}[c + d x] (3 C \operatorname{Sin}[c] + 5 B \operatorname{Sin}[d x] + 15 C \operatorname{Sin}[d x])}{30 d} + \frac{A \operatorname{Cos}[2 c] \operatorname{Sin}[2 d x]}{12 d} + \right. \\ & \left. \left. \frac{(B + 3 C) \operatorname{Tan}[c]}{6 d} \right) \right) / \left( (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \operatorname{Sec}[c + d x]^{9/2} \right) \end{aligned}$$

**Problem 553: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[c + d x]^{5/2}} dx$$

Optimal (type 4, 270 leaves, 9 steps):

$$\begin{aligned} & \frac{1}{5 d} 4 a^3 (9 A + 5 B - 5 C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]} + \\ & \frac{1}{3 d} 4 a^3 (3 A + 5 (B + C)) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]} - \\ & \frac{4 a^3 (6 A - 5 B - 20 C) \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{15 d} + \\ & \frac{2 A (a + a \operatorname{Sec}[c + d x])^3 \operatorname{Sin}[c + d x]}{5 d \operatorname{Sec}[c + d x]^{3/2}} + \frac{2 (6 A + 5 B) (a^2 + a^2 \operatorname{Sec}[c + d x])^2 \operatorname{Sin}[c + d x]}{15 a d \sqrt{\operatorname{Sec}[c + d x]}} - \\ & \frac{2 (9 A + 5 B - 5 C) \sqrt{\operatorname{Sec}[c + d x]} (a^3 + a^3 \operatorname{Sec}[c + d x]) \operatorname{Sin}[c + d x]}{15 d} \end{aligned}$$

Result (type 5, 1203 leaves):

$$\begin{aligned}
 & \left( 9 A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos [c+dx]^5 \operatorname{Csc}[c] \right. \\
 & \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad \left( 5 \sqrt{2} d (A+2C+2B \cos [c+dx] + A \cos [2c+2dx]) \right) + \\
 & \left( B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos [c+dx]^5 \operatorname{Csc}[c] \right. \\
 & \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad \left( \sqrt{2} d (A+2C+2B \cos [c+dx] + A \cos [2c+2dx]) \right) - \\
 & \left( C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos [c+dx]^5 \operatorname{Csc}[c] \right. \\
 & \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad \left( \sqrt{2} d (A+2C+2B \cos [c+dx] + A \cos [2c+2dx]) \right) + \\
 & \left( A \sqrt{\cos [c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \right. \\
 & \quad \left. (a+a \operatorname{Sec}[c+dx])^3 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad \left( d (A+2C+2B \cos [c+dx] + A \cos [2c+2dx]) \operatorname{Sec}[c+dx]^{9/2} \right) + \\
 & \left( 5 B \sqrt{\cos [c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \right. \\
 & \quad \left. (a+a \operatorname{Sec}[c+dx])^3 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad \left( 3 d (A+2C+2B \cos [c+dx] + A \cos [2c+2dx]) \operatorname{Sec}[c+dx]^{9/2} \right) + \\
 & \left( 5 C \sqrt{\cos [c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \right. \\
 & \quad \left. (a+a \operatorname{Sec}[c+dx])^3 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad \left( 3 d (A+2C+2B \cos [c+dx] + A \cos [2c+2dx]) \operatorname{Sec}[c+dx]^{9/2} \right) +
 \end{aligned}$$

$$\left( \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\ \left. \left( -\frac{1}{80d} (71A + 20B - 100C + 73A \cos[2c] + 60B \cos[2c] + 20C \cos[2c]) \cos[dx] \operatorname{Csc}[c] + \right. \right. \\ \left. \frac{(3A + B) \cos[2dx] \sin[2c]}{12d} + \frac{A \cos[3dx] \sin[3c]}{40d} + \right. \\ \left. \frac{(73A + 60B + 20C) \cos[c] \sin[dx]}{40d} + \frac{C \sec[c] \sec[c + dx] \sin[dx]}{6d} + \right. \\ \left. \left. \frac{(3A + B) \cos[2c] \sin[2dx]}{12d} + \frac{A \cos[3c] \sin[3dx]}{40d} + \frac{C \tan[c]}{6d} \right) \right) / \\ \left( (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sec[c + dx]^{9/2} \right)$$

**Problem 554: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + a \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2)}{\sec[c + dx]^{7/2}} dx$$

Optimal (type 4, 271 leaves, 9 steps):

$$\frac{1}{5d} 4a^3 (7A + 9B + 5C) \sqrt{\cos[c + dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\sec[c + dx]} + \\ \frac{1}{21d} 4a^3 (13A + 21B + 35C) \sqrt{\cos[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\sec[c + dx]} - \\ \frac{4a^3 (41A + 42B - 35C) \sqrt{\sec[c + dx]} \sin[c + dx]}{105d} + \frac{2A (a + a \sec[c + dx])^3 \sin[c + dx]}{7d \sec[c + dx]^{5/2}} + \\ \frac{2(6A + 7B) (a^2 + a^2 \sec[c + dx])^2 \sin[c + dx]}{35ad \sec[c + dx]^{3/2}} + \frac{2(7A + 9B + 5C) (a^3 + a^3 \sec[c + dx]) \sin[c + dx]}{15d \sqrt{\sec[c + dx]}}$$

Result (type 5, 279 leaves):

$$\frac{1}{420d} \\ a^3 e^{-i(2c+dx)} \sqrt{\sec[c + dx]} \left( -2352i A \cos[c + dx] - 3024i B \cos[c + dx] - 1680i C \cos[c + dx] + \right. \\ \left. 80(13A + 21B + 35C) \sqrt{\cos[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] + \right. \\ \left. 336i (7A + 9B + 5C) e^{-i(c+dx)} \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + \right. \\ \left. 126A \sin[c + dx] + 42B \sin[2(c + dx)] + 840C \sin[3(c + dx)] + 550A \sin[2(c + dx)] + \right. \\ \left. 420B \sin[2(c + dx)] + 140C \sin[2(c + dx)] + 126A \sin[3(c + dx)] + \right. \\ \left. 42B \sin[3(c + dx)] + 15A \sin[4(c + dx)] \right) (\cos[2c + dx] + i \sin[2c + dx])$$

**Problem 555: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + a \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[c + d x]^{9/2}} dx$$

Optimal (type 4, 271 leaves, 9 steps):

$$\begin{aligned} & \frac{1}{15 d} 4 a^3 (17 A + 21 B + 27 C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]} + \\ & \frac{1}{21 d} 4 a^3 (11 A + 13 B + 21 C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]} + \\ & \frac{4 a^3 (32 A + 41 B + 42 C) \operatorname{Sin}[c + d x]}{105 d \sqrt{\operatorname{Sec}[c + d x]}} + \frac{2 A (a + a \operatorname{Sec}[c + d x])^3 \operatorname{Sin}[c + d x]}{9 d \operatorname{Sec}[c + d x]^{7/2}} + \\ & \frac{2 (2 A + 3 B) (a^2 + a^2 \operatorname{Sec}[c + d x])^2 \operatorname{Sin}[c + d x]}{21 a d \operatorname{Sec}[c + d x]^{5/2}} + \\ & \frac{2 (73 A + 99 B + 63 C) (a^3 + a^3 \operatorname{Sec}[c + d x]) \operatorname{Sin}[c + d x]}{315 d \operatorname{Sec}[c + d x]^{3/2}} \end{aligned}$$

Result (type 5, 214 leaves):

$$\begin{aligned} & \frac{1}{2520 d} a^3 \sqrt{\operatorname{Sec}[c + d x]} \\ & \left( 480 (11 A + 13 B + 21 C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] + 672 i (17 A + 21 B + 27 C) \right. \\ & \quad e^{-i(c+d x)} \sqrt{1 + e^{2i(c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+d x)}\right] + 2 \operatorname{Cos}[c + d x] \\ & \quad \left. (-5712 i A - 7056 i B - 9072 i C + 30 (97 A + 107 B + 84 C) \operatorname{Sin}[c + d x] + 14 (73 A + 54 B + 18 C) \right. \\ & \quad \left. \operatorname{Sin}[2(c + d x)] + 270 A \operatorname{Sin}[3(c + d x)] + 90 B \operatorname{Sin}[3(c + d x)] + 35 A \operatorname{Sin}[4(c + d x)] \right) \end{aligned}$$

**Problem 556: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + a \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[c + d x]^{11/2}} dx$$

Optimal (type 4, 307 leaves, 10 steps):

$$\begin{aligned} & \frac{1}{15d} 4a^3 (15A + 17B + 21C) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \frac{1}{231d} \\ & 4a^3 (105A + 121B + 143C) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\ & \frac{4a^3 (210A + 253B + 264C) \sin[c+dx]}{1155d \sec[c+dx]^{3/2}} + \frac{4a^3 (105A + 121B + 143C) \sin[c+dx]}{231d \sqrt{\sec[c+dx]}} + \\ & \frac{2A (a + a \sec[c+dx])^3 \sin[c+dx]}{11d \sec[c+dx]^{9/2}} + \frac{2(6A + 11B) (a^2 + a^2 \sec[c+dx])^2 \sin[c+dx]}{99ad \sec[c+dx]^{7/2}} + \\ & \frac{2(105A + 143B + 99C) (a^3 + a^3 \sec[c+dx]) \sin[c+dx]}{693d \sec[c+dx]^{5/2}} \end{aligned}$$

Result (type 5, 247 leaves):

$$\begin{aligned} & \frac{1}{55440d} \\ & a^3 \sqrt{\sec[c+dx]} \left( 960 (105A + 121B + 143C) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] + 14784i \right. \\ & \quad \left. (15A + 17B + 21C) e^{-i(c+dx)} \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + \right. \\ & \quad \left. 2 \cos[c+dx] (-110880iA - 125664iB - 155232iC + \right. \\ & \quad \left. 30(1953A + 2134B + 2354C) \sin[c+dx] + 308(75A + 73B + 54C) \sin[2(c+dx)] + \right. \\ & \quad \left. 8505A \sin[3(c+dx)] + 5940B \sin[3(c+dx)] + 1980C \sin[3(c+dx)] + \right. \\ & \quad \left. 2310A \sin[4(c+dx)] + 770B \sin[4(c+dx)] + 315A \sin[5(c+dx)] \right) \end{aligned}$$

**Problem 557: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \sec[c+dx])^3 (A + B \sec[c+dx] + C \sec[c+dx]^2)}{\sec[c+dx]^{13/2}} dx$$

Optimal (type 4, 343 leaves, 11 steps):

$$\begin{aligned} & \frac{1}{195d} 4a^3 (175A + 195B + 221C) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\ & \frac{1}{231d} 4a^3 (95A + 105B + 121C) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\ & \frac{20a^3 (236A + 273B + 286C) \sin[c+dx]}{9009d \sec[c+dx]^{5/2}} + \frac{4a^3 (175A + 195B + 221C) \sin[c+dx]}{585d \sec[c+dx]^{3/2}} + \\ & \frac{4a^3 (95A + 105B + 121C) \sin[c+dx]}{231d \sqrt{\sec[c+dx]}} + \frac{2A (a + a \sec[c+dx])^3 \sin[c+dx]}{13d \sec[c+dx]^{11/2}} + \\ & \frac{2(6A + 13B) (a^2 + a^2 \sec[c+dx])^2 \sin[c+dx]}{143ad \sec[c+dx]^{9/2}} + \\ & \frac{2(145A + 195B + 143C) (a^3 + a^3 \sec[c+dx]) \sin[c+dx]}{1287d \sec[c+dx]^{7/2}} \end{aligned}$$

Result (type 5, 1386 leaves):

$$\begin{aligned}
 & \left( 35 A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^5 \operatorname{Csc}[c] \right. \\
 & \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad \left( 39 \sqrt{2} d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right) + \\
 & \left( B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^5 \operatorname{Csc}[c] \right. \\
 & \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad \left( \sqrt{2} d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right) + \\
 & \left( 17 C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^5 \operatorname{Csc}[c] \right. \\
 & \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad \left( 15 \sqrt{2} d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right) + \\
 & \left( 95 A \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \right. \\
 & \quad \left. (a+a \operatorname{Sec}[c+dx])^3 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad \left( 231 d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \operatorname{Sec}[c+dx]^{9/2} \right) + \\
 & \left( 5 B \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \right. \\
 & \quad \left. (a+a \operatorname{Sec}[c+dx])^3 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad \left( 11 d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \operatorname{Sec}[c+dx]^{9/2} \right) + \\
 & \left( 11 C \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \right. \\
 & \quad \left. (a+a \operatorname{Sec}[c+dx])^3 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) /
 \end{aligned}$$

$$\frac{(21 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \operatorname{Sec}[c + d x]^{9/2}) + 1}{(A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \operatorname{Sec}[c + d x]^{9/2}} \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \left(-\frac{1}{149760 d} (59375 A + 67080 B + 77272 C + 75025 A \cos [2 c] + 82680 B \cos [2 c] + 92456 C \cos [2 c]) \cos [d x] \operatorname{Csc}[c] + \frac{(4267 A + 4473 B + 4664 C) \cos [2 d x] \sin [2 c]}{14784 d} + \frac{(9005 A + 8580 B + 7852 C) \cos [3 d x] \sin [3 c]}{74880 d} + \frac{(59 A + 49 B + 33 C) \cos [4 d x] \sin [4 c]}{1232 d} + \frac{(245 A + 156 B + 52 C) \cos [5 d x] \sin [5 c]}{14976 d} + \frac{(3 A + B) \cos [6 d x] \sin [6 c]}{704 d} + \frac{A \cos [7 d x] \sin [7 c]}{1664 d} + \frac{(75025 A + 82680 B + 92456 C) \cos [c] \sin [d x]}{74880 d} + \frac{(4267 A + 4473 B + 4664 C) \cos [2 c] \sin [2 d x]}{14784 d} + \frac{(9005 A + 8580 B + 7852 C) \cos [3 c] \sin [3 d x]}{74880 d} + \frac{(59 A + 49 B + 33 C) \cos [4 c] \sin [4 d x]}{1232 d} + \frac{(245 A + 156 B + 52 C) \cos [5 c] \sin [5 d x]}{14976 d} + \frac{(3 A + B) \cos [6 c] \sin [6 d x]}{704 d} + \frac{A \cos [7 c] \sin [7 d x]}{1664 d}\right)$$

**Problem 558: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c + d x]^{5/2} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{a + a \operatorname{Sec}[c + d x]} dx$$

Optimal (type 4, 250 leaves, 9 steps):

$$-\frac{1}{5 a d} 3 (5 A - 5 B + 7 C) \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]} - \frac{1}{3 a d} (3 A - 5 B + 5 C) \sqrt{\cos [c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]} + \frac{3 (5 A - 5 B + 7 C) \sqrt{\operatorname{Sec}[c + d x]} \sin [c + d x]}{5 a d} - \frac{(3 A - 5 B + 5 C) \operatorname{Sec}[c + d x]^{3/2} \sin [c + d x]}{3 a d} + \frac{(5 A - 5 B + 7 C) \operatorname{Sec}[c + d x]^{5/2} \sin [c + d x]}{5 a d} - \frac{(A - B + C) \operatorname{Sec}[c + d x]^{7/2} \sin [c + d x]}{d (a + a \operatorname{Sec}[c + d x])}$$

Result (type 5, 1278 leaves):

$$-\left(\left(3 \sqrt{2} A e^{-i(2 c+d x)} \sqrt{\frac{e^{i(c+d x)}}{1+e^{2 i(c+d x)}}}\right) \cos \left[\frac{c}{2} + \frac{d x}{2}\right]^2 \cos [c + d x] \operatorname{Csc}\left[\frac{c}{2}\right]\right)$$



$$\begin{aligned}
 & \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \\
 & \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \Bigg/ \\
 & \left( d (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) (a + a \operatorname{Sec}[c + dx]) \right) \Bigg) + \\
 & \left( 3\sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}}} \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Cos}[c + dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \left. (1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right]) \right) \\
 & \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \Bigg/ \\
 & \left( d (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) (a + a \operatorname{Sec}[c + dx]) \right) - \\
 & \left( 21\sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}}} \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Cos}[c + dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \left. (1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right]) \right) \\
 & \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \Bigg/ \\
 & \left( 5d (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) (a + a \operatorname{Sec}[c + dx]) \right) - \\
 & \left( 2A \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sqrt{\operatorname{Cos}[c + dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \operatorname{Sin}[c] \right) \Bigg/ \\
 & \left( d (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) \sqrt{\operatorname{Sec}[c + dx]} (a + a \operatorname{Sec}[c + dx]) \right) + \\
 & \left( 10B \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sqrt{\operatorname{Cos}[c + dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \operatorname{Sin}[c] \right) \Bigg/ \\
 & \left( 3d (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) \sqrt{\operatorname{Sec}[c + dx]} (a + a \operatorname{Sec}[c + dx]) \right) - \\
 & \left( 10C \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sqrt{\operatorname{Cos}[c + dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \operatorname{Sin}[c] \right) \Bigg/ \\
 & \left( 3d (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) \sqrt{\operatorname{Sec}[c + dx]} (a + a \operatorname{Sec}[c + dx]) \right) +
 \end{aligned}$$

$$\left( \frac{\cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 (A + B \sec[c + dx] + C \sec[c + dx]^2) \left( \frac{6(5A - 5B + 7C) \cos[dx] \csc\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right]}{5d} - \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right] (A \sin\left[\frac{dx}{2}\right] - B \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{d} + \frac{8C \sec[c] \sec[c + dx]^2 \sin[dx]}{5d} + \frac{8 \sec[c] \sec[c + dx] (3C \sin[c] + 5B \sin[dx] - 5C \sin[dx])}{15d} - \frac{1}{3d} \right)}{4(-2B + 2C + 3A \cos[c] - 5B \cos[c] + 5C \cos[c]) \sec[c] \tan\left[\frac{c}{2}\right]} \right) / \left( (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{\sec[c + dx]} (a + a \sec[c + dx]) \right)$$

**Problem 559: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\sec[c + dx]^{3/2} (A + B \sec[c + dx] + C \sec[c + dx]^2)}{a + a \sec[c + dx]} dx$$

Optimal (type 4, 205 leaves, 8 steps):

$$\frac{(A - 3B + 3C) \sqrt{\cos[c + dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\sec[c + dx]}}{ad} + \frac{1}{3ad} (3A - 3B + 5C) \sqrt{\cos[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\sec[c + dx]} - \frac{(A - 3B + 3C) \sqrt{\sec[c + dx]} \sin[c + dx]}{ad} + \frac{(3A - 3B + 5C) \sec[c + dx]^{3/2} \sin[c + dx]}{3ad} - \frac{(A - B + C) \sec[c + dx]^{5/2} \sin[c + dx]}{d(a + a \sec[c + dx])}$$

Result (type 5, 1229 leaves):

$$\left( \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c + dx] \csc\left[\frac{c}{2}\right] \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \sec\left[\frac{c}{2}\right] (A + B \sec[c + dx] + C \sec[c + dx]^2) \right) / \left( d(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) (a + a \sec[c + dx]) \right) -$$

$$\begin{aligned}
 & \left( 3 \sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c+dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & (d(A + 2C + 2B \cos[c+dx] + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c+dx])) + \\
 & \left( 3 \sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c+dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & (d(A + 2C + 2B \cos[c+dx] + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c+dx])) + \\
 & \left( 2A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \sin[c] \right) / \\
 & (d(A + 2C + 2B \cos[c+dx] + A \cos[2c + 2dx]) \sqrt{\operatorname{Sec}[c+dx]} (a + a \operatorname{Sec}[c+dx])) - \\
 & \left( 2B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \sin[c] \right) / \\
 & (d(A + 2C + 2B \cos[c+dx] + A \cos[2c + 2dx]) \sqrt{\operatorname{Sec}[c+dx]} (a + a \operatorname{Sec}[c+dx])) + \\
 & \left( 10C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \sin[c] \right) / \\
 & (3d(A + 2C + 2B \cos[c+dx] + A \cos[2c + 2dx]) \sqrt{\operatorname{Sec}[c+dx]} (a + a \operatorname{Sec}[c+dx])) + \\
 & \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 (A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \left( -\frac{2(A - 3B + 3C) \cos[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right]}{d} + \right. \right. \\
 & \quad \left. \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] (A \sin\left[\frac{dx}{2}\right] - B \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{d} + \right. \\
 & \quad \left. \frac{8C \operatorname{Sec}[c] \operatorname{Sec}[c+dx] \sin[dx]}{3d} + \right. \\
 & \quad \left. \left. \frac{4(2C + 3A \cos[c] - 3B \cos[c] + 5C \cos[c]) \operatorname{Sec}[c] \operatorname{Tan}\left[\frac{c}{2}\right]}{3d} \right) \right) /
 \end{aligned}$$

$$\left( (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{\sec[c + dx]} (a + a \sec[c + dx]) \right)$$

**Problem 560: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\sec[c + dx]} (A + B \sec[c + dx] + C \sec[c + dx]^2)}{a + a \sec[c + dx]} dx$$

Optimal (type 4, 162 leaves, 7 steps):

$$-\frac{1}{ad} (A - B + 3C) \sqrt{\cos[c + dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\sec[c + dx]} +$$

$$\frac{(A + B - C) \sqrt{\cos[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\sec[c + dx]}}{ad} +$$

$$\frac{(A - B + 3C) \sqrt{\sec[c + dx]} \sin[c + dx]}{ad} - \frac{(A - B + C) \sec[c + dx]^{3/2} \sin[c + dx]}{d(a + a \sec[c + dx])}$$

Result (type 5, 1190 leaves):

$$-\left( \left( \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c + dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \right.$$

$$\left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right.$$

$$\left. \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \sec[c + dx] + C \sec[c + dx]^2) \right) / \right.$$

$$\left. (d(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) (a + a \sec[c + dx])) \right) +$$

$$\left( \sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c + dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right.$$

$$\left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right.$$

$$\left. \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \sec[c + dx] + C \sec[c + dx]^2) \right) / \right.$$

$$\left. (d(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) (a + a \sec[c + dx])) - \right.$$

$$\left( 3\sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c + dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right)$$

$$\begin{aligned}
 & \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \\
 & \operatorname{Sec}\left[\frac{c}{2}\right] \left( A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2 \right) \Bigg/ \\
 & \left( d \left( A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx] \right) \left( a + a \operatorname{Sec}[c + dx] \right) \right) + \\
 & \left( 2A \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sqrt{\operatorname{Cos}[c + dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{c}{2}\right] \left( A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2 \right) \operatorname{Sin}[c] \right) \Bigg/ \\
 & \left( d \left( A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx] \right) \sqrt{\operatorname{Sec}[c + dx]} \left( a + a \operatorname{Sec}[c + dx] \right) \right) + \\
 & \left( 2B \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sqrt{\operatorname{Cos}[c + dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{c}{2}\right] \left( A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2 \right) \operatorname{Sin}[c] \right) \Bigg/ \\
 & \left( d \left( A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx] \right) \sqrt{\operatorname{Sec}[c + dx]} \left( a + a \operatorname{Sec}[c + dx] \right) \right) - \\
 & \left( 2C \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sqrt{\operatorname{Cos}[c + dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{c}{2}\right] \left( A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2 \right) \operatorname{Sin}[c] \right) \Bigg/ \\
 & \left( d \left( A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx] \right) \sqrt{\operatorname{Sec}[c + dx]} \left( a + a \operatorname{Sec}[c + dx] \right) \right) + \\
 & \left( \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \left( A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2 \right) \left( \frac{2(A - B + 3C) \operatorname{Cos}[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right]}{d} - \right. \right. \\
 & \left. \left. \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] \left( A \operatorname{Sin}\left[\frac{dx}{2}\right] - B \operatorname{Sin}\left[\frac{dx}{2}\right] + C \operatorname{Sin}\left[\frac{dx}{2}\right] \right)}{d} - \frac{4(A - B + C) \operatorname{Tan}\left[\frac{c}{2}\right]}{d} \right) \right) \Bigg/ \\
 & \left( \left( A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx] \right) \sqrt{\operatorname{Sec}[c + dx]} \left( a + a \operatorname{Sec}[c + dx] \right) \right)
 \end{aligned}$$

**Problem 561:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2}{\sqrt{\operatorname{Sec}[c + dx]} (a + a \operatorname{Sec}[c + dx])} dx$$

Optimal (type 4, 133 leaves, 6 steps):

$$\begin{aligned}
 & \frac{(3A - B + C) \sqrt{\operatorname{Cos}[c + dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\operatorname{Sec}[c + dx]}}{ad} - \\
 & \frac{(A - B - C) \sqrt{\operatorname{Cos}[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\operatorname{Sec}[c + dx]}}{ad} - \\
 & \frac{(A - B + C) \sqrt{\operatorname{Sec}[c + dx]} \operatorname{Sin}[c + dx]}{d(a + a \operatorname{Sec}[c + dx])}
 \end{aligned}$$

Result (type 5, 1208 leaves):

$$\begin{aligned}
& \left( 3 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c+dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
& \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
& \quad (d(A + 2C + 2B \cos[c+dx] + A \cos[2c+2dx]) (a + a \operatorname{Sec}[c+dx])) - \\
& \left( \sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c+dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
& \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
& \quad (d(A + 2C + 2B \cos[c+dx] + A \cos[2c+2dx]) (a + a \operatorname{Sec}[c+dx])) + \\
& \left( \sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c+dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
& \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
& \quad (d(A + 2C + 2B \cos[c+dx] + A \cos[2c+2dx]) (a + a \operatorname{Sec}[c+dx])) - \\
& \left( 2 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \sin[c] \right) / \\
& \quad (d(A + 2C + 2B \cos[c+dx] + A \cos[2c+2dx]) \sqrt{\operatorname{Sec}[c+dx]} (a + a \operatorname{Sec}[c+dx])) + \\
& \left( 2 B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \sin[c] \right) / \\
& \quad (d(A + 2C + 2B \cos[c+dx] + A \cos[2c+2dx]) \sqrt{\operatorname{Sec}[c+dx]} (a + a \operatorname{Sec}[c+dx])) + \\
& \left( 2 C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \sin[c] \right) /
\end{aligned}$$

$$\left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sqrt{\sec [c + dx]} (a + a \sec [c + dx]) \right) +$$

$$\left( \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right.$$

$$\left( - \frac{2 (2A - B + C + A \cos [2c]) \cos [dx] \operatorname{Csc} \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} \right]}{d} + \right.$$

$$\left. \frac{4 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{dx}{2} \right] (A \sin \left[ \frac{dx}{2} \right] - B \sin \left[ \frac{dx}{2} \right] + C \sin \left[ \frac{dx}{2} \right])}{d} + \right.$$

$$\left. \frac{8A \cos [c] \sin [dx]}{d} + \frac{4 (A - B + C) \tan \left[ \frac{c}{2} \right]}{d} \right) \Bigg/$$

$$\left( (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sqrt{\sec [c + dx]} (a + a \sec [c + dx]) \right)$$

**Problem 562: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec [c + dx] + C \sec [c + dx]^2}{\sec [c + dx]^{3/2} (a + a \sec [c + dx])} dx$$

Optimal (type 4, 174 leaves, 7 steps):

$$-\frac{1}{ad} (3A - 3B + C) \sqrt{\cos [c + dx]} \operatorname{EllipticE} \left[ \frac{1}{2} (c + dx), 2 \right] \sqrt{\sec [c + dx]} +$$

$$\frac{1}{3ad} (5A - 3B + 3C) \sqrt{\cos [c + dx]} \operatorname{EllipticF} \left[ \frac{1}{2} (c + dx), 2 \right] \sqrt{\sec [c + dx]} +$$

$$\frac{(5A - 3B + 3C) \sin [c + dx]}{3ad \sqrt{\sec [c + dx]}} - \frac{(A - B + C) \sin [c + dx]}{d \sqrt{\sec [c + dx]} (a + a \sec [c + dx])}$$

Result (type 5, 1256 leaves):

$$-\left( \left( 3 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \cos [c + dx] \operatorname{Csc} \left[ \frac{c}{2} \right] \right. \right.$$

$$\left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)} \right] \right) \right.$$

$$\left. \sec \left[ \frac{c}{2} \right] (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) \Bigg/$$

$$\left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) (a + a \sec [c + dx]) \right) \Bigg)$$

$$\begin{aligned}
& \left( 3 \sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c+dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
& \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
& (d(A + 2C + 2B \cos[c+dx] + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c+dx])) - \\
& \left( \sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c+dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
& \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
& (d(A + 2C + 2B \cos[c+dx] + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c+dx])) + \\
& \left( 10 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \sin[c] \right) / \\
& \left( 3 d (A + 2C + 2B \cos[c+dx] + A \cos[2c + 2dx]) \sqrt{\operatorname{Sec}[c+dx]} (a + a \operatorname{Sec}[c+dx]) \right) - \\
& \left( 2 B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \sin[c] \right) / \\
& \left( d (A + 2C + 2B \cos[c+dx] + A \cos[2c + 2dx]) \sqrt{\operatorname{Sec}[c+dx]} (a + a \operatorname{Sec}[c+dx]) \right) + \\
& \left( 2 C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \sin[c] \right) / \\
& \left( d (A + 2C + 2B \cos[c+dx] + A \cos[2c + 2dx]) \sqrt{\operatorname{Sec}[c+dx]} (a + a \operatorname{Sec}[c+dx]) \right) + \\
& \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 (A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right. \\
& \quad \left. \left( \frac{1}{d} (2A - 2B + C + A \cos[2c] - B \cos[2c]) \cos[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] + \right. \right. \\
& \quad \left. \left. \frac{4 A \cos[2dx] \sin[2c]}{3d} - \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] (A \sin\left[\frac{dx}{2}\right] - B \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{d} \right) \right) -
\end{aligned}$$



$$\left( \frac{8(A-B) \cos[c] \sin[dx]}{d} + \frac{4A \cos[2c] \sin[2dx]}{3d} - \frac{4(A-B+C) \tan\left[\frac{c}{2}\right]}{d} \right) \Bigg/ \left( (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \sqrt{\sec[c+dx]} (a+a \sec[c+dx]) \right)$$

**Problem 563: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A+B \sec[c+dx] + C \sec[c+dx]^2}{\sec[c+dx]^{5/2} (a+a \sec[c+dx])} dx$$

Optimal (type 4, 214 leaves, 8 steps):

$$\frac{1}{5ad} 3(7A-5B+5C) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} - \frac{1}{3ad} (5A-5B+3C) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \frac{(7A-5B+5C) \sin[c+dx]}{5ad \sec[c+dx]^{3/2}} - \frac{(5A-5B+3C) \sin[c+dx]}{3ad \sqrt{\sec[c+dx]}} - \frac{(A-B+C) \sin[c+dx]}{d \sec[c+dx]^{3/2} (a+a \sec[c+dx])}$$

Result (type 5, 1321 leaves):

$$\left( 21\sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c+dx] \operatorname{Csc}\left[\frac{c}{2}\right] \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \operatorname{Sec}\left[\frac{c}{2}\right] (A+B \sec[c+dx] + C \sec[c+dx]^2) \right) \Bigg/ \left( 5d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) (a+a \sec[c+dx]) \right) - \left( 3\sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c+dx] \operatorname{Csc}\left[\frac{c}{2}\right] \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \operatorname{Sec}\left[\frac{c}{2}\right] (A+B \sec[c+dx] + C \sec[c+dx]^2) \right) \Bigg/ \left( d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) (a+a \sec[c+dx]) \right) + \left( 3\sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c+dx] \operatorname{Csc}\left[\frac{c}{2}\right] \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right)$$

$$\begin{aligned} & \left. \operatorname{Sec}\left[\frac{c}{2}\right] \left(A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2\right)\right\} / \\ & \left(d\left(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]\right)\left(a+a \operatorname{Sec}[c+d x]\right)\right)- \\ & \left(10 A \cos \left[\frac{c}{2}+\frac{d x}{2}\right]^2 \sqrt{\cos [c+d x]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]\right. \\ & \left.\operatorname{Sec}\left[\frac{c}{2}\right] \left(A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2\right) \sin [c]\right\} / \\ & \left(3 d\left(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]\right) \sqrt{\operatorname{Sec}[c+d x]} \left(a+a \operatorname{Sec}[c+d x]\right)\right)+ \\ & \left(10 B \cos \left[\frac{c}{2}+\frac{d x}{2}\right]^2 \sqrt{\cos [c+d x]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]\right. \\ & \left.\operatorname{Sec}\left[\frac{c}{2}\right] \left(A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2\right) \sin [c]\right\} / \\ & \left(3 d\left(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]\right) \sqrt{\operatorname{Sec}[c+d x]} \left(a+a \operatorname{Sec}[c+d x]\right)\right)- \\ & \left(2 C \cos \left[\frac{c}{2}+\frac{d x}{2}\right]^2 \sqrt{\cos [c+d x]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]\right. \\ & \left.\operatorname{Sec}\left[\frac{c}{2}\right] \left(A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2\right) \sin [c]\right\} / \\ & \left(d\left(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]\right) \sqrt{\operatorname{Sec}[c+d x]} \left(a+a \operatorname{Sec}[c+d x]\right)\right)+ \\ & \left(\cos \left[\frac{c}{2}+\frac{d x}{2}\right]^2\left(A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2\right)\right. \\ & \left(-\frac{1}{10 d}\left(51 A-40 B+40 C+33 A \cos [2 c]-20 B \cos [2 c]+20 C \cos [2 c]\right)\right. \\ & \left.\cos [d x] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right]-\frac{4(A-B) \cos [2 d x] \sin [2 c]}{3 d}+\right. \\ & \left.\frac{2 A \cos [3 d x] \sin [3 c]}{5 d}+\frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]\left(A \sin \left[\frac{d x}{2}\right]-B \sin \left[\frac{d x}{2}\right]+C \sin \left[\frac{d x}{2}\right]\right)}{d}+\right. \\ & \left.\frac{2\left(33 A-20 B+20 C\right) \cos [c] \sin [d x]}{5 d}-\frac{4(A-B) \cos [2 c] \sin [2 d x]}{3 d}+\right. \\ & \left.\frac{2 A \cos [3 c] \sin [3 d x]}{5 d}+\frac{4(A-B+C) \tan \left[\frac{c}{2}\right]}{d}\right)\left.\right\} / \\ & \left(\left(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]\right) \sqrt{\operatorname{Sec}[c+d x]} \left(a+a \operatorname{Sec}[c+d x]\right)\right) \end{aligned}$$

**Problem 564:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2}{\operatorname{Sec}[c+d x]^{7/2}\left(a+a \operatorname{Sec}[c+d x]\right)} d x$$

Optimal (type 4, 250 leaves, 9 steps):

$$\begin{aligned}
 & -\frac{1}{5ad} 3(7A-7B+5C) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\
 & \frac{1}{21ad} 5(9A-7B+7C) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\
 & \frac{(9A-7B+7C) \sin[c+dx]}{7ad \sec[c+dx]^{5/2}} - \frac{(7A-7B+5C) \sin[c+dx]}{5ad \sec[c+dx]^{3/2}} + \\
 & \frac{5(9A-7B+7C) \sin[c+dx]}{21ad \sqrt{\sec[c+dx]}} - \frac{(A-B+C) \sin[c+dx]}{d \sec[c+dx]^{5/2} (a+a \sec[c+dx])}
 \end{aligned}$$

Result(type 5, 1377 leaves):

$$\begin{aligned}
 & -\left( \left( 21\sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c+dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \sec[c+dx] + C \sec[c+dx]^2) \right) / \\
 & \quad \left. (5d(A + 2C + 2B \cos[c+dx] + A \cos[2c + 2dx]) (a + a \sec[c+dx])) \right) + \\
 & \left( 21\sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c+dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \sec[c+dx] + C \sec[c+dx]^2) \right) / \\
 & \quad \left. (5d(A + 2C + 2B \cos[c+dx] + A \cos[2c + 2dx]) (a + a \sec[c+dx])) - \right. \\
 & \left( 3\sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c+dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \sec[c+dx] + C \sec[c+dx]^2) \right) / \\
 & \quad \left. (d(A + 2C + 2B \cos[c+dx] + A \cos[2c + 2dx]) (a + a \sec[c+dx])) + \right. \\
 & \left( 30A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \sec[c+dx] + C \sec[c+dx]^2) \sin[c] \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( 7 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{\sec [c + d x]} (a + a \sec [c + d x]) \right) - \\
 & \left( 10 B \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \sqrt{\cos [c + d x]} \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[ \frac{c}{2} \right] (A + B \sec [c + d x] + C \sec [c + d x]^2) \sin [c] \right) / \\
 & \left( 3 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{\sec [c + d x]} (a + a \sec [c + d x]) \right) + \\
 & \left( 10 C \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \sqrt{\cos [c + d x]} \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[ \frac{c}{2} \right] (A + B \sec [c + d x] + C \sec [c + d x]^2) \sin [c] \right) / \\
 & \left( 3 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{\sec [c + d x]} (a + a \sec [c + d x]) \right) + \\
 & \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left( \frac{1}{10 d} (51 A - 51 B + 40 C + 33 A \cos [2 c] - 33 B \cos [2 c] + 20 C \cos [2 c]) \cos [d x] \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} \right] + \right. \\
 & \quad \frac{2 (27 A - 14 B + 14 C) \cos [2 d x] \sin [2 c]}{21 d} - \frac{2 (A - B) \cos [3 d x] \sin [3 c]}{5 d} + \\
 & \quad \frac{A \cos [4 d x] \sin [4 c]}{7 d} - \frac{4 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right] (A \sin \left[ \frac{d x}{2} \right] - B \sin \left[ \frac{d x}{2} \right] + C \sin \left[ \frac{d x}{2} \right])}{d} - \\
 & \quad \frac{2 (33 A - 33 B + 20 C) \cos [c] \sin [d x]}{5 d} + \frac{2 (27 A - 14 B + 14 C) \cos [2 c] \sin [2 d x]}{21 d} - \\
 & \quad \left. \left. \frac{2 (A - B) \cos [3 c] \sin [3 d x]}{5 d} + \frac{A \cos [4 c] \sin [4 d x]}{7 d} - \frac{4 (A - B + C) \tan \left[ \frac{c}{2} \right]}{d} \right) \right) / \\
 & \left( (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{\sec [c + d x]} (a + a \sec [c + d x]) \right)
 \end{aligned}$$

**Problem 565: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c + d x]^{5/2} (A + B \sec [c + d x] + C \sec [c + d x]^2)}{(a + a \sec [c + d x])^2} dx$$

Optimal (type 4, 251 leaves, 9 steps):

$$\frac{(A-4B+7C) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{a^2 d} +$$

$$\frac{1}{3a^2 d} (2A-5B+10C) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} -$$

$$\frac{(A-4B+7C) \sqrt{\sec[c+dx]} \sin[c+dx]}{a^2 d} + \frac{(2A-5B+10C) \sec[c+dx]^{3/2} \sin[c+dx]}{3a^2 d} -$$

$$\frac{(A-4B+7C) \sec[c+dx]^{5/2} \sin[c+dx]}{3a^2 d (1+\sec[c+dx])} - \frac{(A-B+C) \sec[c+dx]^{7/2} \sin[c+dx]}{3d (a+a \sec[c+dx])^2}$$

Result (type 5, 1311 leaves):

$$\left( 2\sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \right.$$

$$\left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right.$$

$$\left. \operatorname{Sec}\left[\frac{c}{2}\right] (A+B \sec[c+dx] + C \sec[c+dx]^2) \right) /$$

$$\left( d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) (a+a \sec[c+dx])^2 \right) -$$

$$\left( 8\sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \right.$$

$$\left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right.$$

$$\left. \operatorname{Sec}\left[\frac{c}{2}\right] (A+B \sec[c+dx] + C \sec[c+dx]^2) \right) /$$

$$\left( d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) (a+a \sec[c+dx])^2 \right) +$$

$$\left( 14\sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \right.$$

$$\left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right.$$

$$\left. \operatorname{Sec}\left[\frac{c}{2}\right] (A+B \sec[c+dx] + C \sec[c+dx]^2) \right) /$$

$$\left( d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) (a+a \sec[c+dx])^2 \right) +$$

$$\left( 8A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right.$$

$$\left. \operatorname{Sec}\left[\frac{c}{2}\right] \sqrt{\sec[c+dx]} (A+B \sec[c+dx] + C \sec[c+dx]^2) \sin[c] \right) /$$

$$\begin{aligned}
 & \left( 3 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^2 \right) - \\
 & \left( 20 B \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \sqrt{\cos [c + d x]} \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[ \frac{c}{2} \right] \sqrt{\operatorname{Sec} [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) \sin [c] \right) / \\
 & \left( 3 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^2 \right) + \\
 & \left( 40 C \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \sqrt{\cos [c + d x]} \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[ \frac{c}{2} \right] \sqrt{\operatorname{Sec} [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) \sin [c] \right) / \\
 & \left( 3 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^2 \right) + \\
 & \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \sqrt{\operatorname{Sec} [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left( - \frac{4 (A - 4 B + 7 C) \cos [d x] \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} \right]}{d} + \right. \\
 & \quad \frac{4 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^3 (A \sin \left[ \frac{d x}{2} \right] - B \sin \left[ \frac{d x}{2} \right] + C \sin \left[ \frac{d x}{2} \right])}{3 d} + \frac{1}{3 d} 8 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right] \\
 & \quad \left( 2 A \sin \left[ \frac{d x}{2} \right] - 5 B \sin \left[ \frac{d x}{2} \right] + 8 C \sin \left[ \frac{d x}{2} \right] \right) + \frac{16 C \operatorname{Sec} [c] \operatorname{Sec} [c + d x] \sin [d x]}{3 d} + \\
 & \quad \left. \frac{8 (2 C + 2 A \cos [c] - 5 B \cos [c] + 10 C \cos [c]) \operatorname{Sec} [c] \operatorname{Tan} \left[ \frac{c}{2} \right]}{3 d} + \right. \\
 & \quad \left. \left. \frac{4 (A - B + C) \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \operatorname{Tan} \left[ \frac{c}{2} \right]}{3 d} \right) \right) / \\
 & \left( (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^2 \right)
 \end{aligned}$$

**Problem 566: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec} [c + d x]^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2)}{(a + a \sec [c + d x])^2} dx$$

Optimal (type 4, 207 leaves, 8 steps):

$$\frac{(B-4C) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{a^2 d} +$$

$$\frac{1}{3a^2 d} (A+2B-5C) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} -$$

$$\frac{(B-4C) \sqrt{\sec[c+dx]} \sin[c+dx]}{a^2 d} +$$

$$\frac{(A+2B-5C) \sec[c+dx]^{3/2} \sin[c+dx]}{3a^2 d (1+\sec[c+dx])} - \frac{(A-B+C) \sec[c+dx]^{5/2} \sin[c+dx]}{3d (a+a\sec[c+dx])^2}$$

Result (type 5, 1072 leaves):

$$\left( 2\sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \right.$$

$$\left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right.$$

$$\left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \sec[c+dx] + C \sec[c+dx]^2) \right) /$$

$$\left( d (A + 2C + 2B \cos[c+dx] + A \cos[2c+2dx]) (a + a \sec[c+dx])^2 \right) -$$

$$\left( 8\sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \right.$$

$$\left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right.$$

$$\left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \sec[c+dx] + C \sec[c+dx]^2) \right) /$$

$$\left( d (A + 2C + 2B \cos[c+dx] + A \cos[2c+2dx]) (a + a \sec[c+dx])^2 \right) +$$

$$\left( 4A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right.$$

$$\left. \operatorname{Sec}\left[\frac{c}{2}\right] \sqrt{\sec[c+dx]} (A + B \sec[c+dx] + C \sec[c+dx]^2) \sin[c] \right) /$$

$$\left( 3d (A + 2C + 2B \cos[c+dx] + A \cos[2c+2dx]) (a + a \sec[c+dx])^2 \right) +$$

$$\left( 8B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right.$$

$$\left. \operatorname{Sec}\left[\frac{c}{2}\right] \sqrt{\sec[c+dx]} (A + B \sec[c+dx] + C \sec[c+dx]^2) \sin[c] \right) /$$

$$\left( 3d (A + 2C + 2B \cos[c+dx] + A \cos[2c+2dx]) (a + a \sec[c+dx])^2 \right) -$$

$$\left( 20C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right.$$

$$\left. \operatorname{Sec}\left[\frac{c}{2}\right] \sqrt{\sec[c+dx]} (A + B \sec[c+dx] + C \sec[c+dx]^2) \sin[c] \right) /$$

$$\left( 3 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^2 \right) +$$

$$\left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \sqrt{\sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right.$$

$$\left( \frac{4 (-B + 4 C) \cos [d x] \operatorname{Csc} \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} \right]}{d} + \right.$$

$$\frac{8 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right] (A \sin \left[ \frac{d x}{2} \right] + 2 B \sin \left[ \frac{d x}{2} \right] - 5 C \sin \left[ \frac{d x}{2} \right])}{3 d} -$$

$$\frac{4 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^3 (A \sin \left[ \frac{d x}{2} \right] - B \sin \left[ \frac{d x}{2} \right] + C \sin \left[ \frac{d x}{2} \right])}{3 d} +$$

$$\left. \left. \frac{8 (A + 2 B - 5 C) \tan \left[ \frac{c}{2} \right]}{3 d} - \frac{4 (A - B + C) \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \tan \left[ \frac{c}{2} \right]}{3 d} \right) \right) /$$

$$\left( (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^2 \right)$$

**Problem 567: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2)}{(a + a \sec [c + d x])^2} dx$$

Optimal (type 4, 173 leaves, 7 steps):

$$- \frac{(A - C) \sqrt{\cos [c + d x]} \operatorname{EllipticE} \left[ \frac{1}{2} (c + d x), 2 \right] \sqrt{\sec [c + d x]}}{a^2 d} +$$

$$\frac{1}{3 a^2 d} (2 A + B + 2 C) \sqrt{\cos [c + d x]} \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right] \sqrt{\sec [c + d x]} +$$

$$\frac{(A - C) \sqrt{\sec [c + d x]} \sin [c + d x]}{a^2 d (1 + \sec [c + d x])} - \frac{(A - B + C) \sec [c + d x]^{3/2} \sin [c + d x]}{3 d (a + a \sec [c + d x])^2}$$

Result (type 5, 1073 leaves):

$$- \left( \left( 2 \sqrt{2} A e^{-i (2 c + d x)} \sqrt{\frac{e^{i (c + d x)}}{1 + e^{2 i (c + d x)}}} \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \operatorname{Csc} \left[ \frac{c}{2} \right] \right. \right.$$

$$\left. \left( 1 + e^{2 i (c + d x)} + (-1 + e^{2 i c}) \sqrt{1 + e^{2 i (c + d x)}} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c + d x)} \right] \right) \right.$$

$$\left. \left. \sec \left[ \frac{c}{2} \right] (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) \right) /$$



$$\begin{aligned}
 & \left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) (a + a \sec [c + dx])^2 \right) + \\
 & \left( 2\sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 \operatorname{Csc} \left[ \frac{c}{2} \right] \right. \\
 & \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)} \right] \right) \right. \\
 & \left. \operatorname{Sec} \left[ \frac{c}{2} \right] (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) / \\
 & \left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) (a + a \sec [c + dx])^2 \right) + \\
 & \left( 8A \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 \sqrt{\cos [c + dx]} \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{EllipticF} \left[ \frac{1}{2} (c + dx), 2 \right] \right. \\
 & \left. \operatorname{Sec} \left[ \frac{c}{2} \right] \sqrt{\sec [c + dx]} (A + B \sec [c + dx] + C \sec [c + dx]^2) \sin [c] \right) / \\
 & \left( 3d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) (a + a \sec [c + dx])^2 \right) + \\
 & \left( 4B \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 \sqrt{\cos [c + dx]} \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{EllipticF} \left[ \frac{1}{2} (c + dx), 2 \right] \right. \\
 & \left. \operatorname{Sec} \left[ \frac{c}{2} \right] \sqrt{\sec [c + dx]} (A + B \sec [c + dx] + C \sec [c + dx]^2) \sin [c] \right) / \\
 & \left( 3d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) (a + a \sec [c + dx])^2 \right) + \\
 & \left( 8C \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 \sqrt{\cos [c + dx]} \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{EllipticF} \left[ \frac{1}{2} (c + dx), 2 \right] \right. \\
 & \left. \operatorname{Sec} \left[ \frac{c}{2} \right] \sqrt{\sec [c + dx]} (A + B \sec [c + dx] + C \sec [c + dx]^2) \sin [c] \right) / \\
 & \left( 3d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) (a + a \sec [c + dx])^2 \right) + \\
 & \left( \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 \sqrt{\sec [c + dx]} (A + B \sec [c + dx] + C \sec [c + dx]^2) \right. \\
 & \left. \left( \frac{4(A - C) \cos [dx] \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} \right]}{d} - \right. \right. \\
 & \left. \frac{8 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right] \left( 4A \sin \left[ \frac{dx}{2} \right] - B \sin \left[ \frac{dx}{2} \right] - 2C \sin \left[ \frac{dx}{2} \right] \right)}{3d} + \right. \\
 & \left. \frac{4 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right]^3 \left( A \sin \left[ \frac{dx}{2} \right] - B \sin \left[ \frac{dx}{2} \right] + C \sin \left[ \frac{dx}{2} \right] \right)}{3d} - \right. \\
 & \left. \left. \frac{8(4A - B - 2C) \tan \left[ \frac{c}{2} \right]}{3d} + \frac{4(A - B + C) \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \tan \left[ \frac{c}{2} \right]}{3d} \right) \right) / \\
 & \left( (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) (a + a \sec [c + dx])^2 \right)
 \end{aligned}$$

**Problem 568: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2}{\sqrt{\operatorname{Sec}[c + dx]} (a + a \operatorname{Sec}[c + dx])^2} dx$$

Optimal (type 4, 184 leaves, 7 steps):

$$\frac{(4A - B) \sqrt{\operatorname{Cos}[c + dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\operatorname{Sec}[c + dx]}}{a^2 d} - \frac{1}{3a^2 d} (5A - 2B - C) \sqrt{\operatorname{Cos}[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\operatorname{Sec}[c + dx]} - \frac{(5A - 2B - C) \sqrt{\operatorname{Sec}[c + dx]} \operatorname{Sin}[c + dx]}{3a^2 d (1 + \operatorname{Sec}[c + dx])} - \frac{(A - B + C) \sqrt{\operatorname{Sec}[c + dx]} \operatorname{Sin}[c + dx]}{3d (a + a \operatorname{Sec}[c + dx])^2}$$

Result (type 5, 1090 leaves):

$$\left( 8\sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right) / \left( d (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right) - \left( 2\sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right) / \left( d (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right) - \left( 20A \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\operatorname{Cos}[c + dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \operatorname{Sec}\left[\frac{c}{2}\right] \sqrt{\operatorname{Sec}[c + dx]} (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \operatorname{Sin}[c] \right) / \left( 3d (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right) + \left( 8B \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\operatorname{Cos}[c + dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \operatorname{Sec}\left[\frac{c}{2}\right] \sqrt{\operatorname{Sec}[c + dx]} (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \operatorname{Sin}[c] \right) / \left( 3d (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right)$$

$$\begin{aligned}
 & \left( 3 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^2 \right) + \\
 & \left( 4 C \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \sqrt{\cos [c + d x]} \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[ \frac{c}{2} \right] \sqrt{\operatorname{Sec} [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) \sin [c] \right) / \\
 & \left( 3 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^2 \right) + \\
 & \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \sqrt{\operatorname{Sec} [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left( - \frac{4 (3 A - B + A \cos [2 c]) \cos [d x] \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} \right]}{d} + \right. \\
 & \quad \frac{8 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right] (7 A \sin \left[ \frac{d x}{2} \right] - 4 B \sin \left[ \frac{d x}{2} \right] + C \sin \left[ \frac{d x}{2} \right])}{3 d} - \\
 & \quad \frac{4 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^3 (A \sin \left[ \frac{d x}{2} \right] - B \sin \left[ \frac{d x}{2} \right] + C \sin \left[ \frac{d x}{2} \right])}{3 d} + \frac{16 A \cos [c] \sin [d x]}{d} + \\
 & \quad \left. \left. \frac{8 (7 A - 4 B + C) \tan \left[ \frac{c}{2} \right]}{3 d} - \frac{4 (A - B + C) \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \tan \left[ \frac{c}{2} \right]}{3 d} \right) \right) / \\
 & \left( (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^2 \right)
 \end{aligned}$$

**Problem 569: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec [c + d x] + C \sec [c + d x]^2}{\operatorname{Sec} [c + d x]^{3/2} (a + a \sec [c + d x])^2} dx$$

Optimal (type 4, 220 leaves, 8 steps):

$$\begin{aligned}
 & - \frac{1}{a^2 d} (7 A - 4 B + C) \sqrt{\cos [c + d x]} \operatorname{EllipticE} \left[ \frac{1}{2} (c + d x), 2 \right] \sqrt{\operatorname{Sec} [c + d x]} + \\
 & \frac{1}{3 a^2 d} (10 A - 5 B + 2 C) \sqrt{\cos [c + d x]} \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right] \sqrt{\operatorname{Sec} [c + d x]} + \\
 & \frac{(10 A - 5 B + 2 C) \sin [c + d x]}{3 a^2 d \sqrt{\operatorname{Sec} [c + d x]}} - \frac{(7 A - 4 B + C) \sin [c + d x]}{3 a^2 d \sqrt{\operatorname{Sec} [c + d x]} (1 + \operatorname{Sec} [c + d x])} - \\
 & \frac{(A - B + C) \sin [c + d x]}{3 d \sqrt{\operatorname{Sec} [c + d x]} (a + a \sec [c + d x])^2}
 \end{aligned}$$

Result (type 5, 1346 leaves):

$$- \left( \left( 14 \sqrt{2} A e^{-i (2 c + d x)} \sqrt{\frac{e^{i (c + d x)}}{1 + e^{2 i (c + d x)}}} \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \operatorname{Csc} \left[ \frac{c}{2} \right] \right. \right.$$

$$\begin{aligned}
 & \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \\
 & \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \Bigg/ \\
 & \left( d (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right) + \\
 & \left( 8\sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}}} \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right) \Bigg/ \\
 & \left( d (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right) - \\
 & \left( 2\sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}}} \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right) \Bigg/ \\
 & \left( d (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right) + \\
 & \left( 40A \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\operatorname{Cos}[c + dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{c}{2}\right] \sqrt{\operatorname{Sec}[c + dx]} (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \operatorname{Sin}[c] \right) \Bigg/ \\
 & \left( 3d (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right) - \\
 & \left( 20B \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\operatorname{Cos}[c + dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{c}{2}\right] \sqrt{\operatorname{Sec}[c + dx]} (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \operatorname{Sin}[c] \right) \Bigg/ \\
 & \left( 3d (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right) + \\
 & \left( 8C \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\operatorname{Cos}[c + dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{c}{2}\right] \sqrt{\operatorname{Sec}[c + dx]} (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \operatorname{Sin}[c] \right) \Bigg/ \\
 & \left( 3d (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right) +
 \end{aligned}$$

$$\frac{1}{(A+2C+2B \cos[c+dx]+A \cos[2c+2dx]) (a+a \sec[c+dx])^2} \cos\left[\frac{c}{2}+\frac{dx}{2}\right]^4 \sqrt{\sec[c+dx]} (A+B \sec[c+dx]+C \sec[c+dx]^2) \left(\frac{1}{d} 4(5A-3B+C+2A \cos[2c]-B \cos[2c]) \cos[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right] + \frac{8A \cos[2dx] \sin[2c]}{3d} + \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}+\frac{dx}{2}\right]^3 (A \sin\left[\frac{dx}{2}\right]-B \sin\left[\frac{dx}{2}\right]+C \sin\left[\frac{dx}{2}\right])}{3d} - \frac{1}{3d} 8 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}+\frac{dx}{2}\right] \left(10A \sin\left[\frac{dx}{2}\right]-7B \sin\left[\frac{dx}{2}\right]+4C \sin\left[\frac{dx}{2}\right]\right) - \frac{16(2A-B) \cos[c] \sin[dx]}{d} + \frac{8A \cos[2c] \sin[2dx]}{3d} - \frac{8(10A-7B+4C) \tan\left[\frac{c}{2}\right]}{3d} + \frac{4(A-B+C) \sec\left[\frac{c}{2}+\frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{3d}\right)$$

**Problem 570: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A+B \sec[c+dx]+C \sec[c+dx]^2}{\sec[c+dx]^{5/2} (a+a \sec[c+dx])^2} dx$$

Optimal (type 4, 254 leaves, 9 steps):

$$\frac{1}{5a^2d} (56A-35B+20C) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} - \frac{1}{3a^2d} 5(3A-2B+C) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \frac{(56A-35B+20C) \sin[c+dx]}{15a^2d \sec[c+dx]^{3/2}} - \frac{5(3A-2B+C) \sin[c+dx]}{3a^2d \sqrt{\sec[c+dx]}} - \frac{(3A-2B+C) \sin[c+dx]}{a^2d \sec[c+dx]^{3/2} (1+\sec[c+dx])} - \frac{(A-B+C) \sin[c+dx]}{3d \sec[c+dx]^{3/2} (a+a \sec[c+dx])^2}$$

Result (type 5, 1408 leaves):

$$\left(112\sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2}+\frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \left(1+e^{2i(c+dx)}+(-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right]\right) \sec\left[\frac{c}{2}\right] (A+B \sec[c+dx]+C \sec[c+dx]^2)\right) / \left(5d (A+2C+2B \cos[c+dx]+A \cos[2c+2dx]) (a+a \sec[c+dx])^2\right) -$$

$$\begin{aligned}
 & \left( 14 \sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right) / \\
 & \quad \left( d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right) + \\
 & \left( 8 \sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right) / \\
 & \quad \left( d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right) - \\
 & \left( 20 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c + dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] \sqrt{\operatorname{Sec}[c + dx]} (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \sin[c] \right) / \\
 & \quad \left( d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right) + \\
 & \left( 40 B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c + dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] \sqrt{\operatorname{Sec}[c + dx]} (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \sin[c] \right) / \\
 & \quad \left( 3 d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right) - \\
 & \left( 20 C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c + dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] \sqrt{\operatorname{Sec}[c + dx]} (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \sin[c] \right) / \\
 & \quad \left( 3 d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right) + \\
 & \quad \frac{1}{(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2} \\
 & \quad \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\operatorname{Sec}[c + dx]} (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \\
 & \quad \left( -\frac{1}{5d} (151A - 100B + 60C + 73A \cos[2c] - 40B \cos[2c] + 20C \cos[2c]) \cos[dx] \right. \\
 & \quad \left. \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] - \frac{8(2A - B) \cos[2dx] \sin[2c]}{3d} + \frac{4A \cos[3dx] \sin[3c]}{5d} - \right.
 \end{aligned}$$

$$\frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 \left(A \operatorname{Sin}\left[\frac{dx}{2}\right] - B \operatorname{Sin}\left[\frac{dx}{2}\right] + C \operatorname{Sin}\left[\frac{dx}{2}\right]\right)}{3 d} + \frac{1}{3 d}$$

$$8 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] \left(13 A \operatorname{Sin}\left[\frac{dx}{2}\right] - 10 B \operatorname{Sin}\left[\frac{dx}{2}\right] + 7 C \operatorname{Sin}\left[\frac{dx}{2}\right]\right) +$$

$$\frac{4 (73 A - 40 B + 20 C) \operatorname{Cos}[c] \operatorname{Sin}[dx]}{5 d} - \frac{8 (2 A - B) \operatorname{Cos}[2 c] \operatorname{Sin}[2 dx]}{3 d} +$$

$$\frac{4 A \operatorname{Cos}[3 c] \operatorname{Sin}[3 dx]}{5 d} + \frac{8 (13 A - 10 B + 7 C) \operatorname{Tan}\left[\frac{c}{2}\right]}{3 d} - \frac{4 (A - B + C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Tan}\left[\frac{c}{2}\right]}{3 d}$$

**Problem 571: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c + dx]^{7/2} (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2)}{(a + a \operatorname{Sec}[c + dx])^3} dx$$

Optimal (type 4, 308 leaves, 10 steps):

$$\frac{1}{10 a^3 d} (9 A - 49 B + 119 C) \sqrt{\operatorname{Cos}[c + dx]} \operatorname{EllipticE}\left[\frac{1}{2} (c + dx), 2\right] \sqrt{\operatorname{Sec}[c + dx]} +$$

$$\frac{1}{6 a^3 d} (3 A - 13 B + 33 C) \sqrt{\operatorname{Cos}[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2} (c + dx), 2\right] \sqrt{\operatorname{Sec}[c + dx]} -$$

$$\frac{(9 A - 49 B + 119 C) \sqrt{\operatorname{Sec}[c + dx]} \operatorname{Sin}[c + dx]}{10 a^3 d} +$$

$$\frac{(3 A - 13 B + 33 C) \operatorname{Sec}[c + dx]^{3/2} \operatorname{Sin}[c + dx]}{6 a^3 d} - \frac{(A - B + C) \operatorname{Sec}[c + dx]^{9/2} \operatorname{Sin}[c + dx]}{5 d (a + a \operatorname{Sec}[c + dx])^3} +$$

$$\frac{(B - 2 C) \operatorname{Sec}[c + dx]^{7/2} \operatorname{Sin}[c + dx]}{3 a d (a + a \operatorname{Sec}[c + dx])^2} - \frac{(9 A - 49 B + 119 C) \operatorname{Sec}[c + dx]^{5/2} \operatorname{Sin}[c + dx]}{30 d (a^3 + a^3 \operatorname{Sec}[c + dx])}$$

Result (type 5, 1432 leaves):

$$\left( 18 \sqrt{2} A e^{-i (2 c + dx)} \sqrt{\frac{e^{i (c + dx)}}{1 + e^{2 i (c + dx)}}} \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \right.$$

$$\left. \left( 1 + e^{2 i (c + dx)} + (-1 + e^{2 i c}) \sqrt{1 + e^{2 i (c + dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c + dx)}\right] \right) \right.$$

$$\left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c + dx] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right) /$$

$$(5 d (A + 2 C + 2 B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2 c + 2 dx]) (a + a \operatorname{Sec}[c + dx])^3) -$$

$$\left( 98 \sqrt{2} B e^{-i (2 c + dx)} \sqrt{\frac{e^{i (c + dx)}}{1 + e^{2 i (c + dx)}}} \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \right.$$

$$\begin{aligned}
& \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \\
& \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx] \left( A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2 \right) \Big/ \\
& \left( 5d \left( A + 2C + 2B \cos[c+dx] + A \cos[2c+2dx] \right) \left( a + a \operatorname{Sec}[c+dx] \right)^3 \right) + \\
& \left( 238 \sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
& \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right) \\
& \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx] \left( A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2 \right) \Big/ \\
& \left( 5d \left( A + 2C + 2B \cos[c+dx] + A \cos[2c+2dx] \right) \left( a + a \operatorname{Sec}[c+dx] \right)^3 \right) + \\
& \left( 4A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \\
& \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^{3/2} \left( A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2 \right) \sin[c] \right) \Big/ \\
& \left( d \left( A + 2C + 2B \cos[c+dx] + A \cos[2c+2dx] \right) \left( a + a \operatorname{Sec}[c+dx] \right)^3 \right) - \\
& \left( 52B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \\
& \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^{3/2} \left( A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2 \right) \sin[c] \right) \Big/ \\
& \left( 3d \left( A + 2C + 2B \cos[c+dx] + A \cos[2c+2dx] \right) \left( a + a \operatorname{Sec}[c+dx] \right)^3 \right) + \\
& \left( 44C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \\
& \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^{3/2} \left( A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2 \right) \sin[c] \right) \Big/ \\
& \left( d \left( A + 2C + 2B \cos[c+dx] + A \cos[2c+2dx] \right) \left( a + a \operatorname{Sec}[c+dx] \right)^3 \right) + \\
& \frac{1}{\left( A + 2C + 2B \cos[c+dx] + A \cos[2c+2dx] \right) \left( a + a \operatorname{Sec}[c+dx] \right)^3} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Sec}[c+dx]^{3/2} \\
& \left( A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2 \right) \left( -\frac{4(9A - 49B + 119C) \cos[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right]}{5d} + \right. \\
& \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^5 \left( A \sin\left[\frac{dx}{2}\right] - B \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right] \right)}{5d} + \frac{1}{15d} 8 \operatorname{Sec}\left[\frac{c}{2}\right] \\
& \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 \left( 3A \sin\left[\frac{dx}{2}\right] - 8B \sin\left[\frac{dx}{2}\right] + 13C \sin\left[\frac{dx}{2}\right] \right) + \frac{1}{3d} 8 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] \\
& \left. \left( 3A \sin\left[\frac{dx}{2}\right] - 13B \sin\left[\frac{dx}{2}\right] + 29C \sin\left[\frac{dx}{2}\right] \right) + \frac{32C \operatorname{Sec}[c] \operatorname{Sec}[c+dx] \sin[dx]}{3d} + \right.
\end{aligned}$$



$$\frac{8 (4 C + 3 A \cos [c] - 13 B \cos [c] + 33 C \cos [c]) \sec [c] \tan \left[ \frac{c}{2} \right]}{3 d} + \frac{8 (3 A - 8 B + 13 C) \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \tan \left[ \frac{c}{2} \right]}{15 d} + \frac{4 (A - B + C) \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \tan \left[ \frac{c}{2} \right]}{5 d}$$

**Problem 572: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c+d x]^{5/2} (A+B \sec [c+d x]+C \sec [c+d x]^2)}{(a+a \sec [c+d x])^3} d x$$

Optimal (type 4, 269 leaves, 9 steps):

$$\frac{1}{10 a^3 d} (A+9 B-49 C) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]} + \frac{1}{6 a^3 d} (A+3 B-13 C) \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]} - \frac{(A+9 B-49 C) \sqrt{\sec [c+d x]} \sin [c+d x]}{10 a^3 d} - \frac{(A-B+C) \sec [c+d x]^{7/2} \sin [c+d x]}{5 d (a+a \sec [c+d x])^3} + \frac{(2 A+3 B-8 C) \sec [c+d x]^{5/2} \sin [c+d x]}{15 a d (a+a \sec [c+d x])^2} + \frac{(A+3 B-13 C) \sec [c+d x]^{3/2} \sin [c+d x]}{6 d (a^3+a^3 \sec [c+d x])}$$

Result (type 5, 1400 leaves):

$$\left( 2 \sqrt{2} A e^{-i(2 c+d x)} \sqrt{\frac{e^{i(c+d x)}}{1+e^{2 i(c+d x)}}} \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \operatorname{Csc} \left[ \frac{c}{2} \right] \right. \\ \left. \left( 1+e^{2 i(c+d x)} + (-1+e^{2 i c}) \sqrt{1+e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right] \right) \right. \\ \left. \sec \left[ \frac{c}{2} \right] \sec [c+d x] (A+B \sec [c+d x]+C \sec [c+d x]^2) \right) / \\ \left( 5 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) (a+a \sec [c+d x])^3 \right) + \\ \left( 18 \sqrt{2} B e^{-i(2 c+d x)} \sqrt{\frac{e^{i(c+d x)}}{1+e^{2 i(c+d x)}}} \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \operatorname{Csc} \left[ \frac{c}{2} \right] \right. \\ \left. \left( 1+e^{2 i(c+d x)} + (-1+e^{2 i c}) \sqrt{1+e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right] \right) \right. \\ \left. \sec \left[ \frac{c}{2} \right] \sec [c+d x] (A+B \sec [c+d x]+C \sec [c+d x]^2) \right) / \\ \left( 5 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) (a+a \sec [c+d x])^3 \right) -$$

$$\begin{aligned}
& \left( 98 \sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
& \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2i c}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx] (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
& \quad \left( 5d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) (a+a \operatorname{Sec}[c+dx])^3 \right) + \\
& \quad \left( 4A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^{3/2} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \sin[c] \right) / \\
& \quad \left( 3d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) (a+a \operatorname{Sec}[c+dx])^3 \right) + \\
& \quad \left( 4B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^{3/2} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \sin[c] \right) / \\
& \quad \left( d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) (a+a \operatorname{Sec}[c+dx])^3 \right) - \\
& \quad \left( 52C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^{3/2} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \sin[c] \right) / \\
& \quad \left( 3d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) (a+a \operatorname{Sec}[c+dx])^3 \right) + \\
& \quad \frac{1}{(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) (a+a \operatorname{Sec}[c+dx])^3} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Sec}[c+dx]^{3/2} \\
& \quad (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \left( -\frac{4(A+9B-49C) \cos[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right]}{5d} + \right. \\
& \quad \frac{8 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] (A \sin\left[\frac{dx}{2}\right] + 3B \sin\left[\frac{dx}{2}\right] - 13C \sin\left[\frac{dx}{2}\right])}{3d} + \frac{1}{15d} \\
& \quad 8 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (2A \sin\left[\frac{dx}{2}\right] + 3B \sin\left[\frac{dx}{2}\right] - 8C \sin\left[\frac{dx}{2}\right]) - \\
& \quad \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^5 (A \sin\left[\frac{dx}{2}\right] - B \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{5d} - \frac{8(-A-3B+13C) \tan\left[\frac{c}{2}\right]}{3d} + \\
& \quad \left. \frac{8(2A+3B-8C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{15d} - \frac{4(A-B+C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \tan\left[\frac{c}{2}\right]}{5d} \right)
\end{aligned}$$

**Problem 573:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\text{Sec}[c+dx]^{3/2} (A+B \text{Sec}[c+dx] + C \text{Sec}[c+dx]^2)}{(a+a \text{Sec}[c+dx])^3} dx$$

Optimal (type 4, 231 leaves, 8 steps):

$$-\frac{1}{10a^3d} (A-B-9C) \sqrt{\text{Cos}[c+dx]} \text{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\text{Sec}[c+dx]} +$$

$$\frac{(A+B+3C) \sqrt{\text{Cos}[c+dx]} \text{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\text{Sec}[c+dx]}}{6a^3d} -$$

$$\frac{(A-B+C) \text{Sec}[c+dx]^{5/2} \text{Sin}[c+dx]}{5d(a+a \text{Sec}[c+dx])^3} +$$

$$\frac{(4A+B-6C) \text{Sec}[c+dx]^{3/2} \text{Sin}[c+dx]}{15ad(a+a \text{Sec}[c+dx])^2} + \frac{(A-B-9C) \sqrt{\text{Sec}[c+dx]} \text{Sin}[c+dx]}{10d(a^3+a^3 \text{Sec}[c+dx])}$$

Result (type 5, 1395 leaves):

$$-\left( \left( 2\sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \text{Csc}\left[\frac{c}{2}\right] \right. \right.$$

$$\left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right.$$

$$\left. \left. \text{Sec}\left[\frac{c}{2}\right] \text{Sec}[c+dx] (A+B \text{Sec}[c+dx] + C \text{Sec}[c+dx]^2) \right) / \right.$$

$$\left. \left( 5d (A+2C+2B \text{Cos}[c+dx] + A \text{Cos}[2c+2dx]) (a+a \text{Sec}[c+dx])^3 \right) \right) +$$

$$\left( 2\sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \text{Csc}\left[\frac{c}{2}\right] \right.$$

$$\left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right.$$

$$\left. \left. \text{Sec}\left[\frac{c}{2}\right] \text{Sec}[c+dx] (A+B \text{Sec}[c+dx] + C \text{Sec}[c+dx]^2) \right) / \right.$$

$$\left. \left( 5d (A+2C+2B \text{Cos}[c+dx] + A \text{Cos}[2c+2dx]) (a+a \text{Sec}[c+dx])^3 \right) +$$

$$\left( 18\sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \text{Csc}\left[\frac{c}{2}\right] \right.$$

$$\left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right)$$

$$\begin{aligned} & \left. \sec\left[\frac{c}{2}\right] \sec[c+dx] \left(A+B \sec[c+dx]+C \sec[c+dx]^2\right)\right) / \\ & \left(5 d\left(A+2 C+2 B \cos [c+dx]+A \cos [2 c+2 dx]\right)\left(a+a \sec [c+dx]\right)^3\right)+ \\ & \left(4 A \cos \left[\frac{c}{2}+\frac{dx}{2}\right]^6 \sqrt{\cos [c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]\right. \\ & \left.\sec\left[\frac{c}{2}\right] \sec [c+dx]^{3 / 2}\left(A+B \sec [c+dx]+C \sec [c+dx]^2\right) \sin [c]\right) / \\ & \left(3 d\left(A+2 C+2 B \cos [c+dx]+A \cos [2 c+2 dx]\right)\left(a+a \sec [c+dx]\right)^3\right)+ \\ & \left(4 B \cos \left[\frac{c}{2}+\frac{dx}{2}\right]^6 \sqrt{\cos [c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]\right. \\ & \left.\sec\left[\frac{c}{2}\right] \sec [c+dx]^{3 / 2}\left(A+B \sec [c+dx]+C \sec [c+dx]^2\right) \sin [c]\right) / \\ & \left(3 d\left(A+2 C+2 B \cos [c+dx]+A \cos [2 c+2 dx]\right)\left(a+a \sec [c+dx]\right)^3\right)+ \\ & \left(4 C \cos \left[\frac{c}{2}+\frac{dx}{2}\right]^6 \sqrt{\cos [c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]\right. \\ & \left.\sec\left[\frac{c}{2}\right] \sec [c+dx]^{3 / 2}\left(A+B \sec [c+dx]+C \sec [c+dx]^2\right) \sin [c]\right) / \\ & \left(d\left(A+2 C+2 B \cos [c+dx]+A \cos [2 c+2 dx]\right)\left(a+a \sec [c+dx]\right)^3\right)+ \\ & \frac{1}{\left(A+2 C+2 B \cos [c+dx]+A \cos [2 c+2 dx]\right)\left(a+a \sec [c+dx]\right)^3} \\ & \cos \left[\frac{c}{2}+\frac{dx}{2}\right]^6 \sec [c+dx]^{3 / 2}\left(A+B \sec [c+dx]+C \sec [c+dx]^2\right) \\ & \left(\frac{4(A-B-9 C) \cos [dx] \operatorname{Csc}\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right]}{5 d}-\frac{1}{15 d}\right. \\ & \left.8 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}+\frac{dx}{2}\right]^3\left(7 A \sin\left[\frac{dx}{2}\right]-2 B \sin\left[\frac{dx}{2}\right]-3 C \sin\left[\frac{dx}{2}\right]\right)+\right. \\ & \left.\frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}+\frac{dx}{2}\right]^5\left(A \sin\left[\frac{dx}{2}\right]-B \sin\left[\frac{dx}{2}\right]+C \sin\left[\frac{dx}{2}\right]\right)}{5 d}+\right. \\ & \left.\frac{8 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}+\frac{dx}{2}\right]\left(A \sin\left[\frac{dx}{2}\right]+B \sin\left[\frac{dx}{2}\right]+3 C \sin\left[\frac{dx}{2}\right]\right)}{3 d}+\frac{8(A+B+3 C) \tan\left[\frac{c}{2}\right]}{3 d}-\right. \\ & \left.\frac{8(7 A-2 B-3 C) \sec\left[\frac{c}{2}+\frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{15 d}+\frac{4(A-B+C) \sec\left[\frac{c}{2}+\frac{dx}{2}\right]^4 \tan\left[\frac{c}{2}\right]}{5 d}\right) \end{aligned}$$

**Problem 574:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{\sec [c+dx]}\left(A+B \sec [c+dx]+C \sec [c+dx]^2\right)}{\left(a+a \sec [c+dx]\right)^3} dx$$

Optimal (type 4, 231 leaves, 8 steps):

$$\begin{aligned}
 & - \frac{1}{10 a^3 d} (9 A + B - C) \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\sec [c + d x]} + \\
 & \frac{(3 A + B + C) \sqrt{\cos [c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\sec [c + d x]}}{6 a^3 d} - \\
 & \frac{(A - B + C) \sec [c + d x]^{3/2} \sin [c + d x]}{5 d (a + a \sec [c + d x])^3} + \\
 & \frac{(6 A - B - 4 C) \sqrt{\sec [c + d x]} \sin [c + d x]}{15 a d (a + a \sec [c + d x])^2} + \frac{(3 A + B + C) \sqrt{\sec [c + d x]} \sin [c + d x]}{6 d (a^3 + a^3 \sec [c + d x])}
 \end{aligned}$$

Result (type 5, 1401 leaves):

$$\begin{aligned}
 & - \left( \left( 18 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \right. \\
 & \quad \left. \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{c}{2}\right] \sec [c + d x] (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) \right) / \\
 & \quad \left. \left( 5 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^3 \right) \right) - \\
 & \left( 2 \sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] \sec [c + d x] (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \\
 & \quad \left. \left( 5 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^3 \right) \right) + \\
 & \left( 2 \sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] \sec [c + d x] (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \\
 & \quad \left. \left( 5 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^3 \right) \right) + \\
 & \left( 4 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos [c + d x]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{\operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^{3/2} (A+B \operatorname{Sec}[c+dx]+C \operatorname{Sec}[c+dx]^2) \operatorname{Sin}[c]}{d(A+2C+2B \operatorname{Cos}[c+dx]+A \operatorname{Cos}[2c+2dx]) (a+a \operatorname{Sec}[c+dx])^3} + \right. \\
 & \left. \frac{4B \operatorname{Cos}\left[\frac{c}{2}+\frac{dx}{2}\right]^6 \sqrt{\operatorname{Cos}[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{\operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^{3/2} (A+B \operatorname{Sec}[c+dx]+C \operatorname{Sec}[c+dx]^2) \operatorname{Sin}[c]} \right. \\
 & \left. \frac{3d(A+2C+2B \operatorname{Cos}[c+dx]+A \operatorname{Cos}[2c+2dx]) (a+a \operatorname{Sec}[c+dx])^3}{4C \operatorname{Cos}\left[\frac{c}{2}+\frac{dx}{2}\right]^6 \sqrt{\operatorname{Cos}[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]} + \right. \\
 & \left. \frac{\operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^{3/2} (A+B \operatorname{Sec}[c+dx]+C \operatorname{Sec}[c+dx]^2) \operatorname{Sin}[c]}{3d(A+2C+2B \operatorname{Cos}[c+dx]+A \operatorname{Cos}[2c+2dx]) (a+a \operatorname{Sec}[c+dx])^3} + \right. \\
 & \left. \frac{1}{(A+2C+2B \operatorname{Cos}[c+dx]+A \operatorname{Cos}[2c+2dx]) (a+a \operatorname{Sec}[c+dx])^3} \operatorname{Cos}\left[\frac{c}{2}+\frac{dx}{2}\right]^6 \right. \\
 & \left. \operatorname{Sec}[c+dx]^{3/2} (A+B \operatorname{Sec}[c+dx]+C \operatorname{Sec}[c+dx]^2) \left( \frac{4(9A+B-C) \operatorname{Cos}[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right]}{5d} - \right. \right. \\
 & \left. \frac{8 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}+\frac{dx}{2}\right] (9A \operatorname{Sin}\left[\frac{dx}{2}\right] - B \operatorname{Sin}\left[\frac{dx}{2}\right] - C \operatorname{Sin}\left[\frac{dx}{2}\right])}{3d} - \right. \\
 & \left. \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}+\frac{dx}{2}\right]^5 (A \operatorname{Sin}\left[\frac{dx}{2}\right] - B \operatorname{Sin}\left[\frac{dx}{2}\right] + C \operatorname{Sin}\left[\frac{dx}{2}\right])}{5d} + \frac{1}{15d} 8 \operatorname{Sec}\left[\frac{c}{2}\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{c}{2}+\frac{dx}{2}\right]^3 (12A \operatorname{Sin}\left[\frac{dx}{2}\right] - 7B \operatorname{Sin}\left[\frac{dx}{2}\right] + 2C \operatorname{Sin}\left[\frac{dx}{2}\right]) - \frac{8(9A-B-C) \operatorname{Tan}\left[\frac{c}{2}\right]}{3d} + \right. \\
 & \left. \frac{8(12A-7B+2C) \operatorname{Sec}\left[\frac{c}{2}+\frac{dx}{2}\right]^2 \operatorname{Tan}\left[\frac{c}{2}\right]}{15d} - \frac{4(A-B+C) \operatorname{Sec}\left[\frac{c}{2}+\frac{dx}{2}\right]^4 \operatorname{Tan}\left[\frac{c}{2}\right]}{5d} \right) \left. \right)
 \end{aligned}$$

**Problem 575: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A+B \operatorname{Sec}[c+dx]+C \operatorname{Sec}[c+dx]^2}{\sqrt{\operatorname{Sec}[c+dx]} (a+a \operatorname{Sec}[c+dx])^3} dx$$

Optimal (type 4, 241 leaves, 8 steps):

$$\frac{1}{10 a^3 d} (49 A - 9 B - C) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]} -$$

$$\frac{1}{6 a^3 d} (13 A - 3 B - C) \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]} -$$

$$\frac{(A-B+C) \sqrt{\sec [c+d x]} \sin [c+d x]}{5 d (a+a \sec [c+d x])^3} - \frac{(8 A-3 B-2 C) \sqrt{\sec [c+d x]} \sin [c+d x]}{15 a d (a+a \sec [c+d x])^2} -$$

$$\frac{(13 A-3 B-C) \sqrt{\sec [c+d x]} \sin [c+d x]}{6 d (a^3+a^3 \sec [c+d x])}$$

Result (type 5, 1419 leaves):

$$\left( 98 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \right.$$

$$\left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right.$$

$$\left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx] (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) /$$

$$(5 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) (a+a \sec [c+d x])^3) -$$

$$\left( 18 \sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \right.$$

$$\left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right.$$

$$\left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx] (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) /$$

$$(5 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) (a+a \sec [c+d x])^3) -$$

$$\left( 2 \sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \right.$$

$$\left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right.$$

$$\left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx] (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) /$$

$$(5 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) (a+a \sec [c+d x])^3) -$$

$$\left( 52 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos [c+d x]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \right.$$

$$\left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^{3/2} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \sin [c] \right) /$$

$$\begin{aligned}
 & \left( 3 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \operatorname{Sec}[c + d x])^3 \right) + \\
 & \left( 4 B \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \sqrt{\cos [c + d x]} \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec}[c + d x]^{3/2} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \sin [c] \right) / \\
 & \left( d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \operatorname{Sec}[c + d x])^3 \right) + \\
 & \left( 4 C \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \sqrt{\cos [c + d x]} \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec}[c + d x]^{3/2} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \sin [c] \right) / \\
 & \left( 3 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \operatorname{Sec}[c + d x])^3 \right) + \\
 & \frac{1}{(A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \operatorname{Sec}[c + d x])^3} \\
 & \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \operatorname{Sec}[c + d x]^{3/2} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\
 & \left( - \frac{4 (39 A - 9 B - C + 10 A \cos [2 c]) \cos [d x] \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} \right]}{5 d} + \right. \\
 & \quad \frac{8 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right] (23 A \sin \left[ \frac{d x}{2} \right] - 9 B \sin \left[ \frac{d x}{2} \right] + C \sin \left[ \frac{d x}{2} \right])}{3 d} + \\
 & \quad \frac{4 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^5 (A \sin \left[ \frac{d x}{2} \right] - B \sin \left[ \frac{d x}{2} \right] + C \sin \left[ \frac{d x}{2} \right])}{5 d} - \frac{1}{15 d} \\
 & \quad \left. 8 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^3 (17 A \sin \left[ \frac{d x}{2} \right] - 12 B \sin \left[ \frac{d x}{2} \right] + 7 C \sin \left[ \frac{d x}{2} \right]) \right) + \\
 & \quad \frac{32 A \cos [c] \sin [d x]}{d} + \frac{8 (23 A - 9 B + C) \operatorname{Tan} \left[ \frac{c}{2} \right]}{3 d} - \\
 & \quad \left. \frac{8 (17 A - 12 B + 7 C) \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \operatorname{Tan} \left[ \frac{c}{2} \right]}{15 d} + \frac{4 (A - B + C) \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \operatorname{Tan} \left[ \frac{c}{2} \right]}{5 d} \right)
 \end{aligned}$$

**Problem 576:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2}{\operatorname{Sec}[c + d x]^{3/2} (a + a \operatorname{Sec}[c + d x])^3} dx$$

Optimal (type 4, 274 leaves, 9 steps):



$$\begin{aligned}
 & -\frac{1}{10 a^3 d} (119 A - 49 B + 9 C) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]} + \\
 & \frac{1}{6 a^3 d} (33 A - 13 B + 3 C) \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]} + \\
 & \frac{(33 A - 13 B + 3 C) \sin [c+d x]}{6 a^3 d \sqrt{\sec [c+d x]}} - \frac{(A - B + C) \sin [c+d x]}{5 d \sqrt{\sec [c+d x]} (a + a \sec [c+d x])^3} - \\
 & \frac{(2 A - B) \sin [c+d x]}{3 a d \sqrt{\sec [c+d x]} (a + a \sec [c+d x])^2} - \frac{(119 A - 49 B + 9 C) \sin [c+d x]}{30 d \sqrt{\sec [c+d x]} (a^3 + a^3 \sec [c+d x])}
 \end{aligned}$$

Result (type 5, 1467 leaves):

$$\begin{aligned}
 & -\left( \left( 238 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \right. \\
 & \quad \left. \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right]\right) \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx] (A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) \right) / \\
 & \quad \left. \left( 5 d (A + 2 C + 2 B \cos [c+d x] + A \cos [2 c+2 d x]) (a + a \operatorname{Sec}[c+d x])^3 \right) \right) + \\
 & \left( 98 \sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right]\right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx] (A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad \left. \left( 5 d (A + 2 C + 2 B \cos [c+d x] + A \cos [2 c+2 d x]) (a + a \operatorname{Sec}[c+d x])^3 \right) \right) - \\
 & \left( 18 \sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right]\right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx] (A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad \left. \left( 5 d (A + 2 C + 2 B \cos [c+d x] + A \cos [2 c+2 d x]) (a + a \operatorname{Sec}[c+d x])^3 \right) \right) + \\
 & \left( 44 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos [c+d x]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{\operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^{3/2} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \operatorname{Sin}[c]}{d (A+2C+2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) (a+a \operatorname{Sec}[c+dx])^3} - \right. \\
 & \left. \left( 52B \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\operatorname{Cos}[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \right. \\
 & \left. \left. \frac{\operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^{3/2} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \operatorname{Sin}[c]}{3d (A+2C+2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) (a+a \operatorname{Sec}[c+dx])^3} + \right. \right. \\
 & \left. \left. \left( 4C \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\operatorname{Cos}[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \right. \right. \\
 & \left. \left. \left. \frac{\operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^{3/2} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \operatorname{Sin}[c]}{d (A+2C+2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) (a+a \operatorname{Sec}[c+dx])^3} + \right. \right. \right. \\
 & \left. \left. \left. \frac{1}{(A+2C+2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) (a+a \operatorname{Sec}[c+dx])^3} \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Sec}[c+dx]^{3/2} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right. \right. \right. \\
 & \left. \left. \left. \left( \frac{1}{5d} 4 (89A - 39B + 9C + 30A \operatorname{Cos}[2c] - 10B \operatorname{Cos}[2c]) \operatorname{Cos}[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] + \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{16A \operatorname{Cos}[2dx] \operatorname{Sin}[2c]}{3d} - \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^5 (A \operatorname{Sin}\left[\frac{dx}{2}\right] - B \operatorname{Sin}\left[\frac{dx}{2}\right] + C \operatorname{Sin}\left[\frac{dx}{2}\right])}{5d} \right. \right. \right. \\
 & \left. \left. \left. \frac{1}{3d} 8 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] (43A \operatorname{Sin}\left[\frac{dx}{2}\right] - 23B \operatorname{Sin}\left[\frac{dx}{2}\right] + 9C \operatorname{Sin}\left[\frac{dx}{2}\right]) + \right. \right. \right. \\
 & \left. \left. \left. \frac{1}{15d} 8 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (22A \operatorname{Sin}\left[\frac{dx}{2}\right] - 17B \operatorname{Sin}\left[\frac{dx}{2}\right] + 12C \operatorname{Sin}\left[\frac{dx}{2}\right]) - \right. \right. \right. \\
 & \left. \left. \left. \frac{32(3A-B) \operatorname{Cos}[c] \operatorname{Sin}[dx]}{d} + \frac{16A \operatorname{Cos}[2c] \operatorname{Sin}[2dx]}{3d} - \frac{8(43A-23B+9C) \operatorname{Tan}\left[\frac{c}{2}\right]}{3d} + \right. \right. \right. \\
 & \left. \left. \left. \frac{8(22A-17B+12C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Tan}\left[\frac{c}{2}\right]}{15d} - \frac{4(A-B+C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Tan}\left[\frac{c}{2}\right]}{5d} \right) \right) \right)
 \end{aligned}$$

**Problem 577: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2}{\operatorname{Sec}[c+dx]^{5/2} (a+a \operatorname{Sec}[c+dx])^3} dx$$

Optimal (type 4, 313 leaves, 10 steps):

$$\frac{1}{10 a^3 d} 7 (33 A - 17 B + 7 C) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]} -$$

$$\frac{1}{6 a^3 d} (63 A - 33 B + 13 C) \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]} +$$

$$\frac{7 (33 A - 17 B + 7 C) \sin [c+d x]}{30 a^3 d \sec [c+d x]^{3/2}} - \frac{(63 A - 33 B + 13 C) \sin [c+d x]}{6 a^3 d \sqrt{\sec [c+d x]}} -$$

$$\frac{(A - B + C) \sin [c+d x]}{5 d \sec [c+d x]^{3/2} (a + a \sec [c+d x])^3} - \frac{(12 A - 7 B + 2 C) \sin [c+d x]}{15 a d \sec [c+d x]^{3/2} (a + a \sec [c+d x])^2} -$$

$$\frac{(63 A - 33 B + 13 C) \sin [c+d x]}{10 d \sec [c+d x]^{3/2} (a^3 + a^3 \sec [c+d x])}$$

Result (type 5, 1525 leaves):

$$\left( 462 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \right.$$

$$\left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right.$$

$$\left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx] (A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) /$$

$$\left( 5 d (A + 2 C + 2 B \cos [c+d x] + A \cos [2 c+2 d x]) (a + a \operatorname{Sec}[c+d x])^3 \right) -$$

$$\left( 238 \sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \right.$$

$$\left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right.$$

$$\left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx] (A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) /$$

$$\left( 5 d (A + 2 C + 2 B \cos [c+d x] + A \cos [2 c+2 d x]) (a + a \operatorname{Sec}[c+d x])^3 \right) +$$

$$\left( 98 \sqrt{2} C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \right.$$

$$\left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right.$$

$$\left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx] (A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) /$$

$$\left( 5 d (A + 2 C + 2 B \cos [c+d x] + A \cos [2 c+2 d x]) (a + a \operatorname{Sec}[c+d x])^3 \right) -$$

$$\left( 84 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos [c+d x]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \right.$$

$$\begin{aligned}
& \left( \frac{\operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^{3/2} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \operatorname{Sin}[c]}{d (A+2C+2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) (a+a \operatorname{Sec}[c+dx])^3} + \right. \\
& \left( 44B \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\operatorname{Cos}[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \\
& \left. \frac{\operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^{3/2} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \operatorname{Sin}[c]}{d (A+2C+2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) (a+a \operatorname{Sec}[c+dx])^3} - \right. \\
& \left. \left( 52C \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\operatorname{Cos}[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \right. \\
& \left. \left. \frac{\operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^{3/2} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \operatorname{Sin}[c]}{3d (A+2C+2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) (a+a \operatorname{Sec}[c+dx])^3} + \right. \right. \\
& \left. \left. \frac{1}{(A+2C+2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) (a+a \operatorname{Sec}[c+dx])^3} \right. \right. \\
& \left. \left. \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Sec}[c+dx]^{3/2} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right. \right. \\
& \left. \left. \left( -\frac{1}{5d} 2 (329A - 178B + 78C + 133A \operatorname{Cos}[2c] - 60B \operatorname{Cos}[2c] + 20C \operatorname{Cos}[2c]) \operatorname{Cos}[dx] \right. \right. \right. \\
& \left. \left. \left. \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] - \frac{16(3A-B) \operatorname{Cos}[2dx] \operatorname{Sin}[2c]}{3d} + \frac{8A \operatorname{Cos}[3dx] \operatorname{Sin}[3c]}{5d} + \right. \right. \\
& \left. \left. \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^5 (A \operatorname{Sin}\left[\frac{dx}{2}\right] - B \operatorname{Sin}\left[\frac{dx}{2}\right] + C \operatorname{Sin}\left[\frac{dx}{2}\right])}{5d} - \frac{1}{15d} 8 \operatorname{Sec}\left[\frac{c}{2}\right] \right. \right. \\
& \left. \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (27A \operatorname{Sin}\left[\frac{dx}{2}\right] - 22B \operatorname{Sin}\left[\frac{dx}{2}\right] + 17C \operatorname{Sin}\left[\frac{dx}{2}\right]) + \frac{1}{3d} 8 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] \right. \right. \\
& \left. \left. (69A \operatorname{Sin}\left[\frac{dx}{2}\right] - 43B \operatorname{Sin}\left[\frac{dx}{2}\right] + 23C \operatorname{Sin}\left[\frac{dx}{2}\right]) + \frac{8(133A - 60B + 20C) \operatorname{Cos}[c] \operatorname{Sin}[dx]}{5d} - \right. \right. \\
& \left. \left. \frac{16(3A-B) \operatorname{Cos}[2c] \operatorname{Sin}[2dx]}{3d} + \frac{8A \operatorname{Cos}[3c] \operatorname{Sin}[3dx]}{5d} + \frac{8(69A - 43B + 23C) \operatorname{Tan}\left[\frac{c}{2}\right]}{3d} - \right. \right. \\
& \left. \left. \frac{8(27A - 22B + 17C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Tan}\left[\frac{c}{2}\right]}{15d} + \frac{4(A-B+C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Tan}\left[\frac{c}{2}\right]}{5d} \right) \right)
\end{aligned}$$

**Problem 578: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c+dx]^{5/2} \sqrt{a+a \operatorname{Sec}[c+dx]} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 3, 227 leaves, 6 steps):

$$\frac{\sqrt{a} (48 A + 40 B + 35 C) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{64 d} +$$

$$\frac{a (48 A + 40 B + 35 C) \operatorname{Sec}[c+dx]^{3/2} \operatorname{Sin}[c+dx]}{64 d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{a (48 A + 40 B + 35 C) \operatorname{Sec}[c+dx]^{5/2} \operatorname{Sin}[c+dx]}{96 d \sqrt{a+a \operatorname{Sec}[c+dx]}} +$$

$$\frac{a (8 B + C) \operatorname{Sec}[c+dx]^{7/2} \operatorname{Sin}[c+dx]}{24 d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{C \operatorname{Sec}[c+dx]^{7/2} \sqrt{a+a \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{4 d}$$

Result (type 3, 2038 leaves):

$$- \left( \left( \frac{1}{256} + \frac{i}{256} \right) \left( (-1+i) + \sqrt{2} \right) \right.$$

$$\left. \left( (144 + 48 i) A + 48 \sqrt{2} A + (120 + 40 i) B + 40 \sqrt{2} B + (105 + 35 i) C + 35 \sqrt{2} C \right) \right.$$

$$\operatorname{ArcTan}\left[ \frac{\operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right] - \sqrt{2} \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right]}{-\operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] + \sqrt{2} \operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right]} \right]$$

$$\left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1+\operatorname{Sec}[c+dx])} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right] /$$

$$\left( \sqrt{2} (i + \sqrt{2}) d (A + 2C + 2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) \operatorname{Sec}[c+dx]^{5/2} \right) -$$

$$\left( \left( \frac{1}{256} - \frac{i}{256} \right) \left( (1+i) + \sqrt{2} \right) \left( (-144 + 48 i) A + 48 \sqrt{2} A - (120 - 40 i) B + 40 \sqrt{2} B - \right. \right.$$

$$\left. (105 - 35 i) C + 35 \sqrt{2} C \right) \operatorname{ArcTan}\left[ \frac{\operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right] - \sqrt{2} \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right]}{\operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] + \sqrt{2} \operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right]} \right]$$

$$\left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1+\operatorname{Sec}[c+dx])} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right] /$$

$$\left( \sqrt{2} (i + \sqrt{2}) d (A + 2C + 2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) \operatorname{Sec}[c+dx]^{5/2} \right) +$$

$$\left( (96A + 48i\sqrt{2}A + 80B + 40i\sqrt{2}B + 70C + 35i\sqrt{2}C) \operatorname{Log}\left[\sqrt{2} + 2 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \right.$$

$$\left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1+\operatorname{Sec}[c+dx])} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right] /$$

$$\left( (128 (i + \sqrt{2}) d (A + 2C + 2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) \operatorname{Sec}[c+dx]^{5/2} \right) -$$

$$\left( \left( \frac{1}{512} - \frac{i}{512} \right) \left( (-1+i) + \sqrt{2} \right) \right.$$

$$\left. \left( (144 + 48 i) A + 48 \sqrt{2} A + (120 + 40 i) B + 40 \sqrt{2} B + (105 + 35 i) C + 35 \sqrt{2} C \right) \right.$$

$$\operatorname{Log}\left[ 2 - \sqrt{2} \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]$$

$$\left. \sqrt{a(1+\operatorname{Sec}[c+dx])} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right] /$$

$$\begin{aligned}
& \left( \sqrt{2} (\mathbf{i} + \sqrt{2}) d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sec [c + dx]^{5/2} \right) + \\
& \left( \left( \frac{1}{512} + \frac{\mathbf{i}}{512} \right) \left( (1 + \mathbf{i}) + \sqrt{2} \right) \right. \\
& \quad \left( (-144 + 48 \mathbf{i}) A + 48 \sqrt{2} A - (120 - 40 \mathbf{i}) B + 40 \sqrt{2} B - (105 - 35 \mathbf{i}) C + 35 \sqrt{2} C \right) \\
& \quad \left. \log \left[ 2 + \sqrt{2} \cos \left[ \frac{1}{2} (c + dx) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c + dx) \right] \right] \sec \left[ \frac{1}{2} (c + dx) \right] \right. \\
& \quad \left. \sqrt{a (1 + \sec [c + dx]) (A + B \sec [c + dx] + C \sec [c + dx]^2)} \right) / \\
& \left( \sqrt{2} (\mathbf{i} + \sqrt{2}) d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sec [c + dx]^{5/2} \right) + \\
& \left( (8B + 7C) \sec \left[ \frac{1}{2} (c + dx) \right] \sqrt{a (1 + \sec [c + dx]) (A + B \sec [c + dx] + C \sec [c + dx]^2)} \right) / \\
& \left( 48d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \right. \\
& \quad \left. \sec [c + dx]^{5/2} \left( \cos \left[ \frac{1}{2} (c + dx) \right] - \sin \left[ \frac{1}{2} (c + dx) \right] \right)^3 \right) + \\
& \left( (48A + 40B + 35C) \sec \left[ \frac{1}{2} (c + dx) \right] \sqrt{a (1 + \sec [c + dx]) (A + B \sec [c + dx] + C \sec [c + dx]^2)} \right) / \\
& \left( 64d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \right. \\
& \quad \left. \sec [c + dx]^{5/2} \left( \cos \left[ \frac{1}{2} (c + dx) \right] - \sin \left[ \frac{1}{2} (c + dx) \right] \right) \right) + \\
& \left( (-8B - 7C) \sec \left[ \frac{1}{2} (c + dx) \right] \sqrt{a (1 + \sec [c + dx]) (A + B \sec [c + dx] + C \sec [c + dx]^2)} \right) / \\
& \left( 48d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \right. \\
& \quad \left. \sec [c + dx]^{5/2} \left( \cos \left[ \frac{1}{2} (c + dx) \right] + \sin \left[ \frac{1}{2} (c + dx) \right] \right)^3 \right) + \\
& \left( (-48A - 40B - 35C) \sec \left[ \frac{1}{2} (c + dx) \right] \sqrt{a (1 + \sec [c + dx]) (A + B \sec [c + dx] + C \sec [c + dx]^2)} \right) / \\
& \left( 64d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \right. \\
& \quad \left. \sec [c + dx]^{5/2} \left( \cos \left[ \frac{1}{2} (c + dx) \right] + \sin \left[ \frac{1}{2} (c + dx) \right] \right) \right) + \\
& \left( \sec \left[ \frac{1}{2} (c + dx) \right] \sqrt{a (1 + \sec [c + dx]) (A + B \sec [c + dx] + C \sec [c + dx]^2)} \right. \\
& \quad \left. \left( 16A \sin \left[ \frac{1}{2} (c + dx) \right] + 8B \sin \left[ \frac{1}{2} (c + dx) \right] + 11C \sin \left[ \frac{1}{2} (c + dx) \right] \right) \right) / \\
& \left( 32d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sec [c + dx]^{5/2} \right. \\
& \quad \left. \left( \cos \left[ \frac{1}{2} (c + dx) \right] - \sin \left[ \frac{1}{2} (c + dx) \right] \right)^2 \right) + \\
& \left( \sec \left[ \frac{1}{2} (c + dx) \right] \sqrt{a (1 + \sec [c + dx]) (A + B \sec [c + dx] + C \sec [c + dx]^2)} \right. \\
& \quad \left. \left( 16A \sin \left[ \frac{1}{2} (c + dx) \right] + 8B \sin \left[ \frac{1}{2} (c + dx) \right] + 11C \sin \left[ \frac{1}{2} (c + dx) \right] \right) \right) /
\end{aligned}$$

$$\begin{aligned}
 & \left( 32 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sec [c + d x]^{5/2} \right. \\
 & \quad \left. \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right) + \\
 & \left( C \sqrt{a (1 + \sec [c + d x])} (A + B \sec [c + d x] + C \sec [c + d x]^2) \tan \left[ \frac{1}{2} (c + d x) \right] \right) / \\
 & \left( 8 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. \sec [c + d x]^{5/2} \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^4 \right) + \\
 & \left( C \sqrt{a (1 + \sec [c + d x])} (A + B \sec [c + d x] + C \sec [c + d x]^2) \tan \left[ \frac{1}{2} (c + d x) \right] \right) / \\
 & \left( 8 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. \sec [c + d x]^{5/2} \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^4 \right)
 \end{aligned}$$

**Problem 579: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \sec [c + d x]^{3/2} \sqrt{a + a \sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 3, 179 leaves, 5 steps):

$$\begin{aligned}
 & \frac{\sqrt{a} (8 A + 6 B + 5 C) \operatorname{ArcSinh} \left[ \frac{\sqrt{a} \tan [c + d x]}{\sqrt{a + a \sec [c + d x]}} \right]}{8 d} + \frac{a (8 A + 6 B + 5 C) \sec [c + d x]^{3/2} \sin [c + d x]}{8 d \sqrt{a + a \sec [c + d x]}} + \\
 & \frac{a (6 B + C) \sec [c + d x]^{5/2} \sin [c + d x]}{12 d \sqrt{a + a \sec [c + d x]}} + \frac{C \sec [c + d x]^{5/2} \sqrt{a + a \sec [c + d x]} \sin [c + d x]}{3 d}
 \end{aligned}$$

Result (type 3, 1772 leaves):

$$\begin{aligned}
 & - \left( \left( \frac{1}{32} + \frac{i}{32} \right) \left( (-1 + i) + \sqrt{2} \right) \left( (24 + 8 i) A + 8 \sqrt{2} A + (18 + 6 i) B + 6 \sqrt{2} B + (15 + 5 i) C + 5 \sqrt{2} C \right) \right. \\
 & \quad \left. \operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{4} (c + d x) \right]}{-\cos \left[ \frac{1}{4} (c + d x) \right] + \sqrt{2} \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right]} \right] \right. \\
 & \quad \left. \sec \left[ \frac{1}{2} (c + d x) \right] \sqrt{a (1 + \sec [c + d x])} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \\
 & \left( \sqrt{2} (i + \sqrt{2}) d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sec [c + d x]^{5/2} \right) -
 \end{aligned}$$

$$\begin{aligned}
& \left( \left( \frac{1}{32} - \frac{i}{32} \right) \left( (1+i) + \sqrt{2} \right) \left( (-24+8i) A + 8\sqrt{2} A - (18-6i) B + 6\sqrt{2} B - (15-5i) C + 5\sqrt{2} C \right) \right. \\
& \quad \text{ArcTan} \left[ \frac{\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{4}(c+dx)\right]}{\cos\left[\frac{1}{4}(c+dx)\right] + \sqrt{2} \cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]} \right] \\
& \quad \left. \text{Sec} \left[ \frac{1}{2}(c+dx) \right] \sqrt{a(1+\text{Sec}[c+dx])} (A+B\text{Sec}[c+dx] + C\text{Sec}[c+dx]^2) \right] / \\
& \quad \left( \sqrt{2} (i + \sqrt{2}) d (A+2C+2B\cos[c+dx] + A\cos[2c+2dx]) \text{Sec}[c+dx]^{5/2} \right) + \\
& \quad \left( (16A+8i\sqrt{2}A+12B+6i\sqrt{2}B+10C+5i\sqrt{2}C) \text{Log}[\sqrt{2}+2\sin\left[\frac{1}{2}(c+dx)\right]] \right. \\
& \quad \left. \text{Sec} \left[ \frac{1}{2}(c+dx) \right] \sqrt{a(1+\text{Sec}[c+dx])} (A+B\text{Sec}[c+dx] + C\text{Sec}[c+dx]^2) \right] / \\
& \quad \left( 16(i+\sqrt{2}) d (A+2C+2B\cos[c+dx] + A\cos[2c+2dx]) \text{Sec}[c+dx]^{5/2} \right) - \\
& \quad \left( \left( \frac{1}{64} - \frac{i}{64} \right) \left( (-1+i) + \sqrt{2} \right) \left( (24+8i) A + 8\sqrt{2} A + (18+6i) B + 6\sqrt{2} B + (15+5i) C + 5\sqrt{2} C \right) \right. \\
& \quad \left. \text{Log} \left[ 2 - \sqrt{2} \cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{2}(c+dx)\right] \right] \text{Sec} \left[ \frac{1}{2}(c+dx) \right] \right. \\
& \quad \left. \sqrt{a(1+\text{Sec}[c+dx])} (A+B\text{Sec}[c+dx] + C\text{Sec}[c+dx]^2) \right] / \\
& \quad \left( \sqrt{2} (i + \sqrt{2}) d (A+2C+2B\cos[c+dx] + A\cos[2c+2dx]) \text{Sec}[c+dx]^{5/2} \right) + \\
& \quad \left( \left( \frac{1}{64} + \frac{i}{64} \right) \left( (1+i) + \sqrt{2} \right) \left( (-24+8i) A + 8\sqrt{2} A - (18-6i) B + 6\sqrt{2} B - (15-5i) C + 5\sqrt{2} C \right) \right. \\
& \quad \left. \text{Log} \left[ 2 + \sqrt{2} \cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{2}(c+dx)\right] \right] \text{Sec} \left[ \frac{1}{2}(c+dx) \right] \right. \\
& \quad \left. \sqrt{a(1+\text{Sec}[c+dx])} (A+B\text{Sec}[c+dx] + C\text{Sec}[c+dx]^2) \right] / \\
& \quad \left( \sqrt{2} (i + \sqrt{2}) d (A+2C+2B\cos[c+dx] + A\cos[2c+2dx]) \text{Sec}[c+dx]^{5/2} \right) + \\
& \quad \left( C \text{Sec} \left[ \frac{1}{2}(c+dx) \right] \sqrt{a(1+\text{Sec}[c+dx])} (A+B\text{Sec}[c+dx] + C\text{Sec}[c+dx]^2) \right) / \\
& \quad \left( 6d (A+2C+2B\cos[c+dx] + A\cos[2c+2dx]) \right. \\
& \quad \left. \text{Sec}[c+dx]^{5/2} \left( \cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right] \right)^3 \right) + \\
& \quad \left( (8A+6B+5C) \text{Sec} \left[ \frac{1}{2}(c+dx) \right] \sqrt{a(1+\text{Sec}[c+dx])} (A+B\text{Sec}[c+dx] + C\text{Sec}[c+dx]^2) \right) / \\
& \quad \left( 8d (A+2C+2B\cos[c+dx] + A\cos[2c+2dx]) \right. \\
& \quad \left. \text{Sec}[c+dx]^{5/2} \left( \cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) - \\
& \quad \left( C \text{Sec} \left[ \frac{1}{2}(c+dx) \right] \sqrt{a(1+\text{Sec}[c+dx])} (A+B\text{Sec}[c+dx] + C\text{Sec}[c+dx]^2) \right) / \\
& \quad \left( 6d (A+2C+2B\cos[c+dx] + A\cos[2c+2dx]) \right)
\end{aligned}$$



$$\begin{aligned}
 & \operatorname{Sec}[c+dx]^{5/2} \left( \cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3 + \\
 & \left( (-8A - 6B - 5C) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1+\operatorname{Sec}[c+dx])} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \left( 8d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right) \\
 & \operatorname{Sec}[c+dx]^{5/2} \left( \cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right) + \\
 & \left( \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1+\operatorname{Sec}[c+dx])} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right. \\
 & \left. \left( 2B \sin\left[\frac{1}{2}(c+dx)\right] + C \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) / \left( 4d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right) \\
 & \operatorname{Sec}[c+dx]^{5/2} \left( \cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right] \right)^2 + \\
 & \left( \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1+\operatorname{Sec}[c+dx])} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right. \\
 & \left. \left( 2B \sin\left[\frac{1}{2}(c+dx)\right] + C \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) / \left( 4d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right) \\
 & \operatorname{Sec}[c+dx]^{5/2} \left( \cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^2
 \end{aligned}$$

**Problem 580: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \sqrt{\operatorname{Sec}[c+dx]} \sqrt{a+a \operatorname{Sec}[c+dx]} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 3, 131 leaves, 4 steps):

$$\frac{\sqrt{a} (8A+4B+3C) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{4d} + \\
 \frac{a(4B+C) \operatorname{Sec}[c+dx]^{3/2} \operatorname{Sin}[c+dx]}{4d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{C \operatorname{Sec}[c+dx]^{3/2} \sqrt{a+a \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{2d}$$

Result (type 3, 1490 leaves):

$$\begin{aligned}
 & - \left( \left( \frac{1}{16} + \frac{i}{16} \right) \left( (-1+i) + \sqrt{2} \right) \left( (24+8i)A + 8\sqrt{2}A + (12+4i)B + 4\sqrt{2}B + (9+3i)C + 3\sqrt{2}C \right) \right. \\
 & \left. \operatorname{ArcTan}\left[ \frac{\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{4}(c+dx)\right]}{-\cos\left[\frac{1}{4}(c+dx)\right] + \sqrt{2} \cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]} \right] \right) \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1+\operatorname{Sec}[c+dx])} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) /
 \end{aligned}$$

$$\begin{aligned}
& \left( \sqrt{2} \left( i + \sqrt{2} \right) d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \sec [c + d x]^{5/2} \right) - \\
& \left( \left( \frac{1}{16} - \frac{i}{16} \right) \left( (1 + i) + \sqrt{2} \right) \left( (-24 + 8 i) A + 8 \sqrt{2} A - (12 - 4 i) B + 4 \sqrt{2} B - (9 - 3 i) C + 3 \sqrt{2} C \right) \right. \\
& \quad \text{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c + d x) \right] + \sin \left[ \frac{1}{4} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{4} (c + d x) \right]}{\cos \left[ \frac{1}{4} (c + d x) \right] + \sqrt{2} \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right]} \right] \\
& \quad \left. \sec \left[ \frac{1}{2} (c + d x) \right] \sqrt{a \left( 1 + \sec [c + d x] \right)} \left( A + B \sec [c + d x] + C \sec [c + d x]^2 \right) \right) / \\
& \left( \sqrt{2} \left( i + \sqrt{2} \right) d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \sec [c + d x]^{5/2} \right) + \\
& \left( (16 A + 8 i \sqrt{2} A + 8 B + 4 i \sqrt{2} B + 6 C + 3 i \sqrt{2} C) \log \left[ \sqrt{2} + 2 \sin \left[ \frac{1}{2} (c + d x) \right] \right] \right. \\
& \quad \left. \sec \left[ \frac{1}{2} (c + d x) \right] \sqrt{a \left( 1 + \sec [c + d x] \right)} \left( A + B \sec [c + d x] + C \sec [c + d x]^2 \right) \right) / \\
& \left( 8 \left( i + \sqrt{2} \right) d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \sec [c + d x]^{5/2} \right) - \\
& \left( \left( \frac{1}{32} - \frac{i}{32} \right) \left( (-1 + i) + \sqrt{2} \right) \left( (24 + 8 i) A + 8 \sqrt{2} A + (12 + 4 i) B + 4 \sqrt{2} B + (9 + 3 i) C + 3 \sqrt{2} C \right) \right. \\
& \quad \left. \log \left[ 2 - \sqrt{2} \cos \left[ \frac{1}{2} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c + d x) \right] \right] \sec \left[ \frac{1}{2} (c + d x) \right] \right. \\
& \quad \left. \sqrt{a \left( 1 + \sec [c + d x] \right)} \left( A + B \sec [c + d x] + C \sec [c + d x]^2 \right) \right) / \\
& \left( \sqrt{2} \left( i + \sqrt{2} \right) d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \sec [c + d x]^{5/2} \right) + \\
& \left( \left( \frac{1}{32} + \frac{i}{32} \right) \left( (1 + i) + \sqrt{2} \right) \left( (-24 + 8 i) A + 8 \sqrt{2} A - (12 - 4 i) B + 4 \sqrt{2} B - (9 - 3 i) C + 3 \sqrt{2} C \right) \right. \\
& \quad \left. \log \left[ 2 + \sqrt{2} \cos \left[ \frac{1}{2} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c + d x) \right] \right] \sec \left[ \frac{1}{2} (c + d x) \right] \right. \\
& \quad \left. \sqrt{a \left( 1 + \sec [c + d x] \right)} \left( A + B \sec [c + d x] + C \sec [c + d x]^2 \right) \right) / \\
& \left( \sqrt{2} \left( i + \sqrt{2} \right) d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \sec [c + d x]^{5/2} \right) + \\
& \left( (4 B + 3 C) \sec \left[ \frac{1}{2} (c + d x) \right] \sqrt{a \left( 1 + \sec [c + d x] \right)} \left( A + B \sec [c + d x] + C \sec [c + d x]^2 \right) \right) / \\
& \left( 4 d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \right. \\
& \quad \left. \sec [c + d x]^{5/2} \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) + \\
& \left( (-4 B - 3 C) \sec \left[ \frac{1}{2} (c + d x) \right] \sqrt{a \left( 1 + \sec [c + d x] \right)} \left( A + B \sec [c + d x] + C \sec [c + d x]^2 \right) \right) / \\
& \left( 4 d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \right. \\
& \quad \left. \sec [c + d x]^{5/2} \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) +
\end{aligned}$$

$$\left( C \sqrt{a (1 + \sec [c + d x])} (A + B \sec [c + d x] + C \sec [c + d x]^2) \tan \left[ \frac{1}{2} (c + d x) \right] \right) /$$

$$\left( 2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right.$$

$$\left. \sec [c + d x]^{5/2} \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right) +$$

$$\left( C \sqrt{a (1 + \sec [c + d x])} (A + B \sec [c + d x] + C \sec [c + d x]^2) \tan \left[ \frac{1}{2} (c + d x) \right] \right) /$$

$$\left( 2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right.$$

$$\left. \sec [c + d x]^{5/2} \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right)$$

**Problem 581: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{a + a \sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sqrt{\sec [c + d x]}} dx$$

Optimal (type 3, 119 leaves, 4 steps):

$$\frac{\sqrt{a} (2 B + C) \operatorname{ArcSinh} \left[ \frac{\sqrt{a} \tan [c + d x]}{\sqrt{a + a \sec [c + d x]}} \right]}{d} +$$

$$\frac{a (2 A - C) \sqrt{\sec [c + d x]} \sin [c + d x]}{d \sqrt{a + a \sec [c + d x]}} + \frac{C \sqrt{\sec [c + d x]} \sqrt{a + a \sec [c + d x]} \sin [c + d x]}{d}$$

Result (type 3, 627 leaves):

$$\frac{1}{d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 (c + d x)]) \sec [c + d x]^{5/2} \left( \frac{1}{16} + \frac{i}{16} \right) \sqrt{a (1 + \sec [c + d x])}}$$

$$(A + B \sec [c + d x] + C \sec [c + d x]^2) \left( \frac{1}{i + \sqrt{2}} 2 i \sqrt{2} \left( (-3 + i) + \sqrt{2} \right) \left( (1 + i) + \sqrt{2} \right) \right.$$

$$(2 B + C) \operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c + d x) \right] - (-1 + \sqrt{2}) \sin \left[ \frac{1}{4} (c + d x) \right]}{(1 + \sqrt{2}) \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right]} \right] \sec \left[ \frac{1}{2} (c + d x) \right] -$$

$$\frac{1}{i + \sqrt{2}} 2 \sqrt{2} \left( (-1 + i) + \sqrt{2} \right) \left( (3 + i) + \sqrt{2} \right) (2 B + C)$$

$$\operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c + d x) \right] - (1 + \sqrt{2}) \sin \left[ \frac{1}{4} (c + d x) \right]}{(-1 + \sqrt{2}) \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right]} \right] \sec \left[ \frac{1}{2} (c + d x) \right] + \frac{1}{i + \sqrt{2}}$$

$$(4 + 4 i) \left( -2 i + \sqrt{2} \right) (2 B + C) \operatorname{Log} \left[ \sqrt{2} + 2 \sin \left[ \frac{1}{2} (c + d x) \right] \right] \sec \left[ \frac{1}{2} (c + d x) \right] +$$

$$\frac{1}{i + \sqrt{2}} i \sqrt{2} \left( (-1 + i) + \sqrt{2} \right) \left( (3 + i) + \sqrt{2} \right) (2 B + C)$$

$$\operatorname{Log} \left[ 2 - \sqrt{2} \cos \left[ \frac{1}{2} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c + d x) \right] \right] \sec \left[ \frac{1}{2} (c + d x) \right] +$$

$$\frac{1}{i + \sqrt{2}} \sqrt{2} \left( (-3 + i) + \sqrt{2} \right) \left( (1 + i) + \sqrt{2} \right) (2 B + C)$$

$$\operatorname{Log} \left[ 2 + \sqrt{2} \cos \left[ \frac{1}{2} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c + d x) \right] \right] \sec \left[ \frac{1}{2} (c + d x) \right] -$$

$$\left. \frac{(8 - 8 i) C \sec \left[ \frac{1}{2} (c + d x) \right]^2}{-1 + \tan \left[ \frac{1}{2} (c + d x) \right]} + (32 - 32 i) A \tan \left[ \frac{1}{2} (c + d x) \right] - \frac{(8 - 8 i) C \sec \left[ \frac{1}{2} (c + d x) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + d x) \right]} \right)$$

**Problem 582: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{a + a \sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sec [c + d x]^{3/2}} dx$$

Optimal (type 3, 120 leaves, 4 steps):

$$\frac{2 \sqrt{a} C \operatorname{ArcSinh} \left[ \frac{\sqrt{a} \tan [c + d x]}{\sqrt{a + a \sec [c + d x]}} \right]}{d} +$$

$$\frac{2 a (A + 3 B) \sqrt{\sec [c + d x]} \sin [c + d x]}{3 d \sqrt{a + a \sec [c + d x]}} + \frac{2 A \sqrt{a + a \sec [c + d x]} \sin [c + d x]}{3 d \sqrt{\sec [c + d x]}}$$

Result (type 3, 347 leaves):

$$\frac{1}{12 d \sqrt{\sec [c+d x]}} \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right] \sqrt{a\left(1+\operatorname{Sec}[c+d x]\right)} \left( -6 i \sqrt{2} C \operatorname{ArcTan}\left[\frac{\cos\left[\frac{1}{4}(c+d x)\right]-(-1+\sqrt{2}) \sin\left[\frac{1}{4}(c+d x)\right]}{(1+\sqrt{2}) \cos\left[\frac{1}{4}(c+d x)\right]-\sin\left[\frac{1}{4}(c+d x)\right]}\right] - 6 i \sqrt{2} C \operatorname{ArcTan}\left[\frac{\cos\left[\frac{1}{4}(c+d x)\right]-\left(1+\sqrt{2}\right) \sin\left[\frac{1}{4}(c+d x)\right]}{\left(-1+\sqrt{2}\right) \cos\left[\frac{1}{4}(c+d x)\right]-\sin\left[\frac{1}{4}(c+d x)\right]}\right] + 6 \sqrt{2} C \operatorname{Log}\left[\sqrt{2}+2 \sin\left[\frac{1}{2}(c+d x)\right]\right] - 3 \sqrt{2} C \operatorname{Log}\left[2-\sqrt{2} \cos\left[\frac{1}{2}(c+d x)\right]-\sqrt{2} \sin\left[\frac{1}{2}(c+d x)\right]\right] - 3 \sqrt{2} C \operatorname{Log}\left[2+\sqrt{2} \cos\left[\frac{1}{2}(c+d x)\right]-\sqrt{2} \sin\left[\frac{1}{2}(c+d x)\right]\right] + 12 A \sin\left[\frac{1}{2}(c+d x)\right] + 24 B \sin\left[\frac{1}{2}(c+d x)\right] + 4 A \sin\left[\frac{3}{2}(c+d x)\right] \right)$$

**Problem 586: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c+d x]^{5/2} (a+a \operatorname{Sec}[c+d x])^{3/2} (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) dx$$

Optimal (type 3, 283 leaves, 7 steps):

$$\frac{a^{3/2} (176 A + 150 B + 133 C) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right]}{128 d} + \frac{a^2 (176 A + 150 B + 133 C) \operatorname{Sec}[c+d x]^{3/2} \sin[c+d x]}{128 d \sqrt{a+a \operatorname{Sec}[c+d x]}} + \frac{a^2 (176 A + 150 B + 133 C) \operatorname{Sec}[c+d x]^{5/2} \sin[c+d x]}{192 d \sqrt{a+a \operatorname{Sec}[c+d x]}} + \frac{a^2 (80 A + 90 B + 67 C) \operatorname{Sec}[c+d x]^{7/2} \sin[c+d x]}{240 d \sqrt{a+a \operatorname{Sec}[c+d x]}} + \frac{a (10 B + 3 C) \operatorname{Sec}[c+d x]^{7/2} \sqrt{a+a \operatorname{Sec}[c+d x]} \sin[c+d x]}{40 d} + \frac{C \operatorname{Sec}[c+d x]^{7/2} (a+a \operatorname{Sec}[c+d x])^{3/2} \sin[c+d x]}{5 d}$$

Result (type 3, 2352 leaves):

$$-\left(\left(\frac{1}{1024} + \frac{i}{1024}\right) \left((-1+i) + \sqrt{2}\right) \left((528+176 i) A + 176 \sqrt{2} A + (450+150 i) B + 150 \sqrt{2} B + (399+133 i) C + 133 \sqrt{2} C\right)\right)$$

$$\begin{aligned}
 & \text{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{4} (c + d x) \right]}{-\cos \left[ \frac{1}{4} (c + d x) \right] + \sqrt{2} \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right]} \right] \\
 & \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^3 \left( a \left( 1 + \text{Sec} [c + d x] \right) \right)^{3/2} \left( A + B \text{Sec} [c + d x] + C \text{Sec} [c + d x]^2 \right) \Bigg/ \\
 & \left( \sqrt{2} \left( i + \sqrt{2} \right) d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \text{Sec} [c + d x]^{7/2} \right) - \\
 & \left( \left( \frac{1}{1024} - \frac{i}{1024} \right) \left( (1 + i) + \sqrt{2} \right) \left( (-528 + 176 i) A + 176 \sqrt{2} A - \right. \right. \\
 & \quad \left. \left. (450 - 150 i) B + 150 \sqrt{2} B - (399 - 133 i) C + 133 \sqrt{2} C \right) \right. \\
 & \text{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c + d x) \right] + \sin \left[ \frac{1}{4} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{4} (c + d x) \right]}{\cos \left[ \frac{1}{4} (c + d x) \right] + \sqrt{2} \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right]} \right] \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^3 \\
 & \left. \left( a \left( 1 + \text{Sec} [c + d x] \right) \right)^{3/2} \left( A + B \text{Sec} [c + d x] + C \text{Sec} [c + d x]^2 \right) \right) \Bigg/ \\
 & \left( \sqrt{2} \left( i + \sqrt{2} \right) d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \text{Sec} [c + d x]^{7/2} \right) + \\
 & \left( (352 A + 176 i \sqrt{2} A + 300 B + 150 i \sqrt{2} B + 266 C + 133 i \sqrt{2} C) \log \left[ \sqrt{2} + 2 \sin \left[ \frac{1}{2} (c + d x) \right] \right] \right) \\
 & \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^3 \left( a \left( 1 + \text{Sec} [c + d x] \right) \right)^{3/2} \left( A + B \text{Sec} [c + d x] + C \text{Sec} [c + d x]^2 \right) \Bigg/ \\
 & \left( 512 \left( i + \sqrt{2} \right) d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \text{Sec} [c + d x]^{7/2} \right) - \\
 & \left( \left( \frac{1}{2048} - \frac{i}{2048} \right) \left( (-1 + i) + \sqrt{2} \right) \right. \\
 & \quad \left. \left( (528 + 176 i) A + 176 \sqrt{2} A + (450 + 150 i) B + 150 \sqrt{2} B + (399 + 133 i) C + 133 \sqrt{2} C \right) \right. \\
 & \left. \log \left[ 2 - \sqrt{2} \cos \left[ \frac{1}{2} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c + d x) \right] \right] \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^3 \right. \\
 & \quad \left. \left( a \left( 1 + \text{Sec} [c + d x] \right) \right)^{3/2} \left( A + B \text{Sec} [c + d x] + C \text{Sec} [c + d x]^2 \right) \right) \Bigg/ \\
 & \left( \sqrt{2} \left( i + \sqrt{2} \right) d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \text{Sec} [c + d x]^{7/2} \right) + \\
 & \left( \left( \frac{1}{2048} + \frac{i}{2048} \right) \left( (1 + i) + \sqrt{2} \right) \right. \\
 & \quad \left. \left( (-528 + 176 i) A + 176 \sqrt{2} A - (450 - 150 i) B + 150 \sqrt{2} B - (399 - 133 i) C + 133 \sqrt{2} C \right) \right. \\
 & \left. \log \left[ 2 + \sqrt{2} \cos \left[ \frac{1}{2} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c + d x) \right] \right] \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^3 \right. \\
 & \quad \left. \left( a \left( 1 + \text{Sec} [c + d x] \right) \right)^{3/2} \left( A + B \text{Sec} [c + d x] + C \text{Sec} [c + d x]^2 \right) \right) \Bigg/ \\
 & \left( \sqrt{2} \left( i + \sqrt{2} \right) d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \text{Sec} [c + d x]^{7/2} \right) + \\
 & \left( C \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^3 \left( a \left( 1 + \text{Sec} [c + d x] \right) \right)^{3/2} \left( A + B \text{Sec} [c + d x] + C \text{Sec} [c + d x]^2 \right) \right) \Bigg/
 \end{aligned}$$

$$\begin{aligned}
 & \left( 40 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. \sec [c + d x]^{7/2} \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^5 \right) + \\
 & \left( (16 A + 30 B + 29 C) \sec \left[ \frac{1}{2} (c + d x) \right]^3 (a (1 + \sec [c + d x]))^{3/2} \right. \\
 & \quad \left. (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \left( 192 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. \sec [c + d x]^{7/2} \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^3 \right) + \\
 & \left( (176 A + 150 B + 133 C) \sec \left[ \frac{1}{2} (c + d x) \right]^3 (a (1 + \sec [c + d x]))^{3/2} \right. \\
 & \quad \left. (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \left( 256 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. \sec [c + d x]^{7/2} \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) - \\
 & \left( C \sec \left[ \frac{1}{2} (c + d x) \right]^3 (a (1 + \sec [c + d x]))^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \\
 & \left( 40 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. \sec [c + d x]^{7/2} \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^5 \right) + \\
 & \left( (-16 A - 30 B - 29 C) \sec \left[ \frac{1}{2} (c + d x) \right]^3 (a (1 + \sec [c + d x]))^{3/2} \right. \\
 & \quad \left. (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \left( 192 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. \sec [c + d x]^{7/2} \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^3 \right) + \\
 & \left( (-176 A - 150 B - 133 C) \sec \left[ \frac{1}{2} (c + d x) \right]^3 (a (1 + \sec [c + d x]))^{3/2} \right. \\
 & \quad \left. (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \left( 256 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. \sec [c + d x]^{7/2} \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) + \\
 & \left( \sec \left[ \frac{1}{2} (c + d x) \right]^3 (a (1 + \sec [c + d x]))^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left. \left( 2 B \sin \left[ \frac{1}{2} (c + d x) \right] + 3 C \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) / \\
 & \left( 32 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sec [c + d x]^{7/2} \right. \\
 & \quad \left. \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^4 \right) + \\
 & \left( \sec \left[ \frac{1}{2} (c + d x) \right]^3 (a (1 + \sec [c + d x]))^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left. \left( 2 B \sin \left[ \frac{1}{2} (c + d x) \right] + 3 C \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
& \left( 32 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sec [c + d x]^{7/2} \right. \\
& \quad \left. \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^4 \right) + \\
& \left( \sec \left[ \frac{1}{2} (c + d x) \right]^3 (a (1 + \sec [c + d x]))^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
& \quad \left. \left( 48 A \sin \left[ \frac{1}{2} (c + d x) \right] + 38 B \sin \left[ \frac{1}{2} (c + d x) \right] + 37 C \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) / \\
& \left( 128 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sec [c + d x]^{7/2} \right. \\
& \quad \left. \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right) + \\
& \left( \sec \left[ \frac{1}{2} (c + d x) \right]^3 (a (1 + \sec [c + d x]))^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
& \quad \left. \left( 48 A \sin \left[ \frac{1}{2} (c + d x) \right] + 38 B \sin \left[ \frac{1}{2} (c + d x) \right] + 37 C \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) / \\
& \left( 128 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sec [c + d x]^{7/2} \right. \\
& \quad \left. \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right)
\end{aligned}$$

**Problem 587: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \sec [c + d x]^{3/2} (a + a \sec [c + d x])^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 3, 233 leaves, 6 steps):

$$\begin{aligned}
& \frac{a^{3/2} (112 A + 88 B + 75 C) \operatorname{ArcSinh} \left[ \frac{\sqrt{a} \tan [c + d x]}{\sqrt{a + a \sec [c + d x]}} \right]}{64 d} + \\
& \frac{a^2 (112 A + 88 B + 75 C) \sec [c + d x]^{3/2} \sin [c + d x]}{64 d \sqrt{a + a \sec [c + d x]}} + \\
& \frac{a^2 (48 A + 56 B + 39 C) \sec [c + d x]^{5/2} \sin [c + d x]}{96 d \sqrt{a + a \sec [c + d x]}} + \\
& \frac{a (8 B + 3 C) \sec [c + d x]^{5/2} \sqrt{a + a \sec [c + d x]} \sin [c + d x]}{24 d} + \\
& \frac{C \sec [c + d x]^{5/2} (a + a \sec [c + d x])^{3/2} \sin [c + d x]}{4 d}
\end{aligned}$$

Result (type 3, 2084 leaves):

$$- \left( \left( \frac{1}{512} + \frac{i}{512} \right) \left( (-1 + i) + \sqrt{2} \right) \right)$$



$$\begin{aligned}
 & \left( (336 + 112 i) A + 112 \sqrt{2} A + (264 + 88 i) B + 88 \sqrt{2} B + (225 + 75 i) C + 75 \sqrt{2} C \right) \\
 & \text{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{4} (c + d x) \right]}{-\cos \left[ \frac{1}{4} (c + d x) \right] + \sqrt{2} \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right]} \right] \\
 & \left. \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^3 (a (1 + \text{Sec} [c + d x]))^{3/2} (A + B \text{Sec} [c + d x] + C \text{Sec} [c + d x]^2) \right] / \\
 & \left( \sqrt{2} (i + \sqrt{2}) d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \text{Sec} [c + d x]^{7/2} \right) - \\
 & \left( \left( \frac{1}{512} - \frac{i}{512} \right) ((1 + i) + \sqrt{2}) ((-336 + 112 i) A + 112 \sqrt{2} A - (264 - 88 i) B + 88 \sqrt{2} B - \right. \\
 & \left. (225 - 75 i) C + 75 \sqrt{2} C) \text{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c + d x) \right] + \sin \left[ \frac{1}{4} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{4} (c + d x) \right]}{\cos \left[ \frac{1}{4} (c + d x) \right] + \sqrt{2} \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right]} \right] \right. \\
 & \left. \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^3 (a (1 + \text{Sec} [c + d x]))^{3/2} (A + B \text{Sec} [c + d x] + C \text{Sec} [c + d x]^2) \right] / \\
 & \left( \sqrt{2} (i + \sqrt{2}) d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \text{Sec} [c + d x]^{7/2} \right) + \\
 & \left( (224 A + 112 i \sqrt{2} A + 176 B + 88 i \sqrt{2} B + 150 C + 75 i \sqrt{2} C) \text{Log} \left[ \sqrt{2} + 2 \sin \left[ \frac{1}{2} (c + d x) \right] \right] \right) \\
 & \left. \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^3 (a (1 + \text{Sec} [c + d x]))^{3/2} (A + B \text{Sec} [c + d x] + C \text{Sec} [c + d x]^2) \right] / \\
 & \left( 256 (i + \sqrt{2}) d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \text{Sec} [c + d x]^{7/2} \right) - \\
 & \left( \left( \frac{1}{1024} - \frac{i}{1024} \right) ((-1 + i) + \sqrt{2}) \right. \\
 & \left. ((336 + 112 i) A + 112 \sqrt{2} A + (264 + 88 i) B + 88 \sqrt{2} B + (225 + 75 i) C + 75 \sqrt{2} C) \right. \\
 & \left. \text{Log} \left[ 2 - \sqrt{2} \cos \left[ \frac{1}{2} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c + d x) \right] \right] \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^3 \right. \\
 & \left. (a (1 + \text{Sec} [c + d x]))^{3/2} (A + B \text{Sec} [c + d x] + C \text{Sec} [c + d x]^2) \right] / \\
 & \left( \sqrt{2} (i + \sqrt{2}) d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \text{Sec} [c + d x]^{7/2} \right) + \\
 & \left( \left( \frac{1}{1024} + \frac{i}{1024} \right) ((1 + i) + \sqrt{2}) \right. \\
 & \left. ((-336 + 112 i) A + 112 \sqrt{2} A - (264 - 88 i) B + 88 \sqrt{2} B - (225 - 75 i) C + 75 \sqrt{2} C) \right. \\
 & \left. \text{Log} \left[ 2 + \sqrt{2} \cos \left[ \frac{1}{2} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c + d x) \right] \right] \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^3 \right. \\
 & \left. (a (1 + \text{Sec} [c + d x]))^{3/2} (A + B \text{Sec} [c + d x] + C \text{Sec} [c + d x]^2) \right] / \\
 & \left( \sqrt{2} (i + \sqrt{2}) d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \text{Sec} [c + d x]^{7/2} \right) + \\
 & \left( (8 B + 15 C) \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^3 (a (1 + \text{Sec} [c + d x]))^{3/2} (A + B \text{Sec} [c + d x] + C \text{Sec} [c + d x]^2) \right) /
 \end{aligned}$$

$$\begin{aligned}
& \left( 96 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
& \quad \left. \sec [c + d x]^{7/2} \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^3 \right) + \\
& \left( (112 A + 88 B + 75 C) \sec \left[ \frac{1}{2} (c + d x) \right]^3 (a (1 + \sec [c + d x]))^{3/2} \right. \\
& \quad \left. (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \left( 128 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
& \quad \left. \sec [c + d x]^{7/2} \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) + \\
& \left( (-8 B - 15 C) \sec \left[ \frac{1}{2} (c + d x) \right]^3 (a (1 + \sec [c + d x]))^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \\
& \left( 96 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
& \quad \left. \sec [c + d x]^{7/2} \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^3 \right) + \\
& \left( (-112 A - 88 B - 75 C) \sec \left[ \frac{1}{2} (c + d x) \right]^3 (a (1 + \sec [c + d x]))^{3/2} \right. \\
& \quad \left. (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \left( 128 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
& \quad \left. \sec [c + d x]^{7/2} \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) + \\
& \left( \sec \left[ \frac{1}{2} (c + d x) \right]^3 (a (1 + \sec [c + d x]))^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
& \quad \left. \left( 16 A \sin \left[ \frac{1}{2} (c + d x) \right] + 24 B \sin \left[ \frac{1}{2} (c + d x) \right] + 19 C \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) / \\
& \left( 64 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sec [c + d x]^{7/2} \right. \\
& \quad \left. \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right) + \\
& \left( \sec \left[ \frac{1}{2} (c + d x) \right]^3 (a (1 + \sec [c + d x]))^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
& \quad \left. \left( 16 A \sin \left[ \frac{1}{2} (c + d x) \right] + 24 B \sin \left[ \frac{1}{2} (c + d x) \right] + 19 C \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) / \\
& \left( 64 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sec [c + d x]^{7/2} \right. \\
& \quad \left. \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right) + \\
& \left( C \sec \left[ \frac{1}{2} (c + d x) \right]^2 (a (1 + \sec [c + d x]))^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
& \quad \left. \tan \left[ \frac{1}{2} (c + d x) \right] \right) / \left( 16 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
& \quad \left. \sec [c + d x]^{7/2} \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^4 \right) + \\
& \left( C \sec \left[ \frac{1}{2} (c + d x) \right]^2 (a (1 + \sec [c + d x]))^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right.
\end{aligned}$$

$$\frac{\tan\left[\frac{1}{2}(c+dx)\right]}{\sec[c+dx]^{7/2} \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^4} \left(16d(A+2C+2B\cos[c+dx]+A\cos[2c+2dx])\right)$$

**Problem 588: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \sqrt{\sec[c+dx]} (a+a\sec[c+dx])^{3/2} (A+B\sec[c+dx]+C\sec[c+dx]^2) dx$$

Optimal (type 3, 181 leaves, 5 steps):

$$\frac{a^{3/2} (24A+14B+11C) \operatorname{ArcSinh}\left[\frac{-\sqrt{a}\tan[c+dx]}{\sqrt{a+a\sec[c+dx]}}\right]}{8d} + \frac{a^2 (24A+30B+19C) \sec[c+dx]^{3/2} \sin[c+dx]}{24d\sqrt{a+a\sec[c+dx]}} + \frac{a(2B+C) \sec[c+dx]^{3/2} \sqrt{a+a\sec[c+dx]} \sin[c+dx]}{4d} + \frac{C \sec[c+dx]^{3/2} (a+a\sec[c+dx])^{3/2} \sin[c+dx]}{3d}$$

Result (type 3, 1796 leaves):

$$\begin{aligned} & - \left( \left( \frac{1}{64} + \frac{i}{64} \right) \left( (-1+i) + \sqrt{2} \right) \right. \\ & \quad \left( (72+24i)A + 24\sqrt{2}A + (42+14i)B + 14\sqrt{2}B + (33+11i)C + 11\sqrt{2}C \right) \\ & \quad \operatorname{ArcTan}\left[ \frac{\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right] - \sqrt{2}\sin\left[\frac{1}{4}(c+dx)\right]}{-\cos\left[\frac{1}{4}(c+dx)\right] + \sqrt{2}\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]} \right] \\ & \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^3 (a(1+\sec[c+dx]))^{3/2} (A+B\sec[c+dx]+C\sec[c+dx]^2) \right] \Bigg/ \\ & \quad \left( \sqrt{2} (i+\sqrt{2}) d (A+2C+2B\cos[c+dx]+A\cos[2c+2dx]) \sec[c+dx]^{7/2} \right) - \\ & \quad \left( \left( \frac{1}{64} - \frac{i}{64} \right) \left( (1+i) + \sqrt{2} \right) \left( (-72+24i)A + 24\sqrt{2}A - (42-14i)B + 14\sqrt{2}B - (33-11i)C + \right. \right. \\ & \quad \left. \left. 11\sqrt{2}C \right) \operatorname{ArcTan}\left[ \frac{\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right] - \sqrt{2}\sin\left[\frac{1}{4}(c+dx)\right]}{\cos\left[\frac{1}{4}(c+dx)\right] + \sqrt{2}\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]} \right] \right. \\ & \quad \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^3 (a(1+\sec[c+dx]))^{3/2} (A+B\sec[c+dx]+C\sec[c+dx]^2) \right] \right) \Bigg/ \\ & \quad \left( \sqrt{2} (i+\sqrt{2}) d (A+2C+2B\cos[c+dx]+A\cos[2c+2dx]) \sec[c+dx]^{7/2} \right) + \end{aligned}$$

$$\begin{aligned}
& \left( (48A + 24i\sqrt{2}A + 28B + 14i\sqrt{2}B + 22C + 11i\sqrt{2}C) \operatorname{Log}[\sqrt{2} + 2\operatorname{Sin}[\frac{1}{2}(c+dx)]] \right. \\
& \quad \left. \operatorname{Sec}[\frac{1}{2}(c+dx)]^3 (a(1+\operatorname{Sec}[c+dx]))^{3/2} (A+B\operatorname{Sec}[c+dx] + C\operatorname{Sec}[c+dx]^2) \right) / \\
& \left( 32(i+\sqrt{2})d(A+2C+2B\operatorname{Cos}[c+dx] + A\operatorname{Cos}[2c+2dx]) \operatorname{Sec}[c+dx]^{7/2} \right) - \\
& \left( \left( \frac{1}{128} - \frac{i}{128} \right) ((-1+i) + \sqrt{2}) \right. \\
& \quad \left( (72+24i)A + 24\sqrt{2}A + (42+14i)B + 14\sqrt{2}B + (33+11i)C + 11\sqrt{2}C \right) \\
& \quad \left. \operatorname{Log}[2 - \sqrt{2}\operatorname{Cos}[\frac{1}{2}(c+dx)] - \sqrt{2}\operatorname{Sin}[\frac{1}{2}(c+dx)]] \operatorname{Sec}[\frac{1}{2}(c+dx)]^3 \right. \\
& \quad \left. (a(1+\operatorname{Sec}[c+dx]))^{3/2} (A+B\operatorname{Sec}[c+dx] + C\operatorname{Sec}[c+dx]^2) \right) / \\
& \left( \sqrt{2}(i+\sqrt{2})d(A+2C+2B\operatorname{Cos}[c+dx] + A\operatorname{Cos}[2c+2dx]) \operatorname{Sec}[c+dx]^{7/2} \right) + \\
& \left( \left( \frac{1}{128} + \frac{i}{128} \right) ((1+i) + \sqrt{2}) \right. \\
& \quad \left( (-72+24i)A + 24\sqrt{2}A - (42-14i)B + 14\sqrt{2}B - (33-11i)C + 11\sqrt{2}C \right) \\
& \quad \left. \operatorname{Log}[2 + \sqrt{2}\operatorname{Cos}[\frac{1}{2}(c+dx)] - \sqrt{2}\operatorname{Sin}[\frac{1}{2}(c+dx)]] \operatorname{Sec}[\frac{1}{2}(c+dx)]^3 \right. \\
& \quad \left. (a(1+\operatorname{Sec}[c+dx]))^{3/2} (A+B\operatorname{Sec}[c+dx] + C\operatorname{Sec}[c+dx]^2) \right) / \\
& \left( \sqrt{2}(i+\sqrt{2})d(A+2C+2B\operatorname{Cos}[c+dx] + A\operatorname{Cos}[2c+2dx]) \operatorname{Sec}[c+dx]^{7/2} \right) + \\
& \left( C\operatorname{Sec}[\frac{1}{2}(c+dx)]^3 (a(1+\operatorname{Sec}[c+dx]))^{3/2} (A+B\operatorname{Sec}[c+dx] + C\operatorname{Sec}[c+dx]^2) \right) / \\
& \left( 12d(A+2C+2B\operatorname{Cos}[c+dx] + A\operatorname{Cos}[2c+2dx]) \right. \\
& \quad \left. \operatorname{Sec}[c+dx]^{7/2} \left( \operatorname{Cos}[\frac{1}{2}(c+dx)] - \operatorname{Sin}[\frac{1}{2}(c+dx)] \right)^3 \right) + \\
& \left( (8A+14B+11C) \operatorname{Sec}[\frac{1}{2}(c+dx)]^3 (a(1+\operatorname{Sec}[c+dx]))^{3/2} \right. \\
& \quad \left. (A+B\operatorname{Sec}[c+dx] + C\operatorname{Sec}[c+dx]^2) \right) / \left( 16d(A+2C+2B\operatorname{Cos}[c+dx] + A\operatorname{Cos}[2c+2dx]) \right. \\
& \quad \left. \operatorname{Sec}[c+dx]^{7/2} \left( \operatorname{Cos}[\frac{1}{2}(c+dx)] - \operatorname{Sin}[\frac{1}{2}(c+dx)] \right) \right) - \\
& \left( C\operatorname{Sec}[\frac{1}{2}(c+dx)]^3 (a(1+\operatorname{Sec}[c+dx]))^{3/2} (A+B\operatorname{Sec}[c+dx] + C\operatorname{Sec}[c+dx]^2) \right) / \\
& \left( 12d(A+2C+2B\operatorname{Cos}[c+dx] + A\operatorname{Cos}[2c+2dx]) \right. \\
& \quad \left. \operatorname{Sec}[c+dx]^{7/2} \left( \operatorname{Cos}[\frac{1}{2}(c+dx)] + \operatorname{Sin}[\frac{1}{2}(c+dx)] \right)^3 \right) + \\
& \left( (-8A-14B-11C) \operatorname{Sec}[\frac{1}{2}(c+dx)]^3 (a(1+\operatorname{Sec}[c+dx]))^{3/2} \right. \\
& \quad \left. (A+B\operatorname{Sec}[c+dx] + C\operatorname{Sec}[c+dx]^2) \right) / \left( 16d(A+2C+2B\operatorname{Cos}[c+dx] + A\operatorname{Cos}[2c+2dx]) \right. \\
& \quad \left. \operatorname{Sec}[c+dx]^{7/2} \left( \operatorname{Cos}[\frac{1}{2}(c+dx)] + \operatorname{Sin}[\frac{1}{2}(c+dx)] \right) \right) +
\end{aligned}$$

$$\begin{aligned}
 & \left( \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^3 (a(1+\operatorname{Sec}[c+dx]))^{3/2} (A+B\operatorname{Sec}[c+dx]+C\operatorname{Sec}[c+dx]^2) \right. \\
 & \quad \left. \left( 2B\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + 3C\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \right) / \\
 & \left( 8d(A+2C+2B\operatorname{Cos}[c+dx]+A\operatorname{Cos}[2c+2dx]) \operatorname{Sec}[c+dx]^{7/2} \right. \\
 & \quad \left. \left( \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^2 \right) + \\
 & \left( \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^3 (a(1+\operatorname{Sec}[c+dx]))^{3/2} (A+B\operatorname{Sec}[c+dx]+C\operatorname{Sec}[c+dx]^2) \right. \\
 & \quad \left. \left( 2B\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + 3C\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \right) / \\
 & \left( 8d(A+2C+2B\operatorname{Cos}[c+dx]+A\operatorname{Cos}[2c+2dx]) \operatorname{Sec}[c+dx]^{7/2} \right. \\
 & \quad \left. \left( \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^2 \right)
 \end{aligned}$$

**Problem 589: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(a+a\operatorname{Sec}[c+dx])^{3/2} (A+B\operatorname{Sec}[c+dx]+C\operatorname{Sec}[c+dx]^2)}{\sqrt{\operatorname{Sec}[c+dx]}} dx$$

Optimal (type 3, 183 leaves, 5 steps):

$$\begin{aligned}
 & \frac{a^{3/2} (8A+12B+7C) \operatorname{ArcSinh}\left[\frac{\sqrt{a}\operatorname{Tan}[c+dx]}{\sqrt{a+a\operatorname{Sec}[c+dx]}}\right]}{4d} + \frac{a^2 (8A-4B-5C) \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{4d\sqrt{a+a\operatorname{Sec}[c+dx]}} + \\
 & \frac{a(4B+3C) \sqrt{\operatorname{Sec}[c+dx]} \sqrt{a+a\operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{4d} + \\
 & \frac{C\sqrt{\operatorname{Sec}[c+dx]} (a+a\operatorname{Sec}[c+dx])^{3/2} \operatorname{Sin}[c+dx]}{2d}
 \end{aligned}$$

Result (type 3, 1627 leaves):

$$\begin{aligned}
 & - \left( \left( \frac{1}{32} + \frac{i}{32} \right) \left( (-1+i) + \sqrt{2} \right) \right. \\
 & \quad \left( (24+8i)A + 8\sqrt{2}A + (36+12i)B + 12\sqrt{2}B + (21+7i)C + 7\sqrt{2}C \right) \\
 & \quad \operatorname{ArcTan}\left[ \frac{\operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right] - \sqrt{2}\operatorname{Sin}\left[\frac{1}{4}(c+dx)\right]}{-\operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] + \sqrt{2}\operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right]} \right] \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^3 (a(1+\operatorname{Sec}[c+dx]))^{3/2} (A+B\operatorname{Sec}[c+dx]+C\operatorname{Sec}[c+dx]^2) \right) /
 \end{aligned}$$

$$\begin{aligned}
& \left( \sqrt{2} \left( i + \sqrt{2} \right) d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \sec [c + d x]^{7/2} \right) - \\
& \left( \left( \frac{1}{32} - \frac{i}{32} \right) \left( (1 + i) + \sqrt{2} \right) \left( (-24 + 8 i) A + 8 \sqrt{2} A - (36 - 12 i) B + 12 \sqrt{2} B - (21 - 7 i) C + 7 \sqrt{2} C \right) \right. \\
& \quad \text{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c + d x) \right] + \sin \left[ \frac{1}{4} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{4} (c + d x) \right]}{\cos \left[ \frac{1}{4} (c + d x) \right] + \sqrt{2} \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right]} \right] \\
& \quad \left. \sec \left[ \frac{1}{2} (c + d x) \right]^3 \left( a \left( 1 + \sec [c + d x] \right) \right)^{3/2} \left( A + B \sec [c + d x] + C \sec [c + d x]^2 \right) \right) / \\
& \left( \sqrt{2} \left( i + \sqrt{2} \right) d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \sec [c + d x]^{7/2} \right) + \\
& \left( (16 A + 8 i \sqrt{2} A + 24 B + 12 i \sqrt{2} B + 14 C + 7 i \sqrt{2} C) \log \left[ \sqrt{2} + 2 \sin \left[ \frac{1}{2} (c + d x) \right] \right] \right. \\
& \quad \left. \sec \left[ \frac{1}{2} (c + d x) \right]^3 \left( a \left( 1 + \sec [c + d x] \right) \right)^{3/2} \left( A + B \sec [c + d x] + C \sec [c + d x]^2 \right) \right) / \\
& \left( 16 \left( i + \sqrt{2} \right) d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \sec [c + d x]^{7/2} \right) - \\
& \left( \left( \frac{1}{64} - \frac{i}{64} \right) \left( (-1 + i) + \sqrt{2} \right) \left( (24 + 8 i) A + 8 \sqrt{2} A + (36 + 12 i) B + 12 \sqrt{2} B + (21 + 7 i) C + 7 \sqrt{2} C \right) \right. \\
& \quad \left. \log \left[ 2 - \sqrt{2} \cos \left[ \frac{1}{2} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c + d x) \right] \right] \sec \left[ \frac{1}{2} (c + d x) \right]^3 \right. \\
& \quad \left. \left( a \left( 1 + \sec [c + d x] \right) \right)^{3/2} \left( A + B \sec [c + d x] + C \sec [c + d x]^2 \right) \right) / \\
& \left( \sqrt{2} \left( i + \sqrt{2} \right) d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \sec [c + d x]^{7/2} \right) + \\
& \left( \left( \frac{1}{64} + \frac{i}{64} \right) \left( (1 + i) + \sqrt{2} \right) \left( (-24 + 8 i) A + 8 \sqrt{2} A - (36 - 12 i) B + 12 \sqrt{2} B - (21 - 7 i) C + 7 \sqrt{2} C \right) \right. \\
& \quad \left. \log \left[ 2 + \sqrt{2} \cos \left[ \frac{1}{2} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c + d x) \right] \right] \sec \left[ \frac{1}{2} (c + d x) \right]^3 \right. \\
& \quad \left. \left( a \left( 1 + \sec [c + d x] \right) \right)^{3/2} \left( A + B \sec [c + d x] + C \sec [c + d x]^2 \right) \right) / \\
& \left( \sqrt{2} \left( i + \sqrt{2} \right) d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \sec [c + d x]^{7/2} \right) + \\
& \left( (4 B + 7 C) \sec \left[ \frac{1}{2} (c + d x) \right]^3 \left( a \left( 1 + \sec [c + d x] \right) \right)^{3/2} \left( A + B \sec [c + d x] + C \sec [c + d x]^2 \right) \right) / \\
& \left( 8 d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \right. \\
& \quad \left. \sec [c + d x]^{7/2} \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) + \\
& \left( (-4 B - 7 C) \sec \left[ \frac{1}{2} (c + d x) \right]^3 \left( a \left( 1 + \sec [c + d x] \right) \right)^{3/2} \left( A + B \sec [c + d x] + C \sec [c + d x]^2 \right) \right) / \\
& \left( 8 d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \right. \\
& \quad \left. \sec [c + d x]^{7/2} \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) +
\end{aligned}$$

$$\begin{aligned}
 & \left( 2 A \operatorname{Sec} \left[ \frac{1}{2} (c+d x) \right]^2 (a (1+\operatorname{Sec}[c+d x]))^{3/2} (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \right. \\
 & \quad \left. \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right] \right) / \left( d (A+2 C+2 B \operatorname{Cos}[c+d x]+A \operatorname{Cos}[2 c+2 d x]) \operatorname{Sec}[c+d x]^{7/2} \right) + \\
 & \left( C \operatorname{Sec} \left[ \frac{1}{2} (c+d x) \right]^2 (a (1+\operatorname{Sec}[c+d x]))^{3/2} (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \right. \\
 & \quad \left. \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right] \right) / \left( 4 d (A+2 C+2 B \operatorname{Cos}[c+d x]+A \operatorname{Cos}[2 c+2 d x]) \right. \\
 & \quad \left. \operatorname{Sec}[c+d x]^{7/2} \left( \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right] - \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right] \right)^2 \right) + \\
 & \left( C \operatorname{Sec} \left[ \frac{1}{2} (c+d x) \right]^2 (a (1+\operatorname{Sec}[c+d x]))^{3/2} (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \right. \\
 & \quad \left. \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right] \right) / \left( 4 d (A+2 C+2 B \operatorname{Cos}[c+d x]+A \operatorname{Cos}[2 c+2 d x]) \right. \\
 & \quad \left. \operatorname{Sec}[c+d x]^{7/2} \left( \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right] + \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right] \right)^2 \right)
 \end{aligned}$$

**Problem 590: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(a+a \operatorname{Sec}[c+d x])^{3/2} (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2)}{\operatorname{Sec}[c+d x]^{3/2}} dx$$

Optimal (type 3, 177 leaves, 5 steps):

$$\begin{aligned}
 & \frac{a^{3/2} (2 B+3 C) \operatorname{ArcSinh} \left[ \frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}} \right]}{d} + \frac{a^2 (8 A+6 B-3 C) \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{3 d \sqrt{a+a \operatorname{Sec}[c+d x]}} - \\
 & \frac{a (2 A-3 C) \sqrt{\operatorname{Sec}[c+d x]} \sqrt{a+a \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{3 d} + \frac{2 A (a+a \operatorname{Sec}[c+d x])^{3/2} \operatorname{Sin}[c+d x]}{3 d \sqrt{\operatorname{Sec}[c+d x]}}
 \end{aligned}$$

Result (type 3, 1406 leaves):

$$\begin{aligned}
 & - \left( \left( \left( \frac{1}{8} + \frac{i}{8} \right) \left( (-1+i) + \sqrt{2} \right) \left( (6+2 i) B + 2 \sqrt{2} B + (9+3 i) C + 3 \sqrt{2} C \right) \right. \right. \\
 & \quad \left. \operatorname{ArcTan} \left[ \frac{\operatorname{Cos} \left[ \frac{1}{4} (c+d x) \right] - \operatorname{Sin} \left[ \frac{1}{4} (c+d x) \right] - \sqrt{2} \operatorname{Sin} \left[ \frac{1}{4} (c+d x) \right]}{-\operatorname{Cos} \left[ \frac{1}{4} (c+d x) \right] + \sqrt{2} \operatorname{Cos} \left[ \frac{1}{4} (c+d x) \right] - \operatorname{Sin} \left[ \frac{1}{4} (c+d x) \right]} \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c+d x) \right]^3 (a (1+\operatorname{Sec}[c+d x]))^{3/2} (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \right) / \\
 & \quad \left( \sqrt{2} (i+\sqrt{2}) d (A+2 C+2 B \operatorname{Cos}[c+d x]+A \operatorname{Cos}[2 c+2 d x]) \operatorname{Sec}[c+d x]^{7/2} \right) -
 \end{aligned}$$

$$\begin{aligned}
& \left( \left( \frac{1}{8} - \frac{i}{8} \right) \left( (1+i) + \sqrt{2} \right) \left( (-6+2i) B + 2\sqrt{2} B - (9-3i) C + 3\sqrt{2} C \right) \right. \\
& \quad \text{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c+dx) \right] + \sin \left[ \frac{1}{4} (c+dx) \right] - \sqrt{2} \sin \left[ \frac{1}{4} (c+dx) \right]}{\cos \left[ \frac{1}{4} (c+dx) \right] + \sqrt{2} \cos \left[ \frac{1}{4} (c+dx) \right] - \sin \left[ \frac{1}{4} (c+dx) \right]} \right] \\
& \quad \left. \text{Sec} \left[ \frac{1}{2} (c+dx) \right]^3 \left( a (1 + \text{Sec} [c+dx]) \right)^{3/2} (A + B \text{Sec} [c+dx] + C \text{Sec} [c+dx]^2) \right) / \\
& \quad \left( \sqrt{2} (i + \sqrt{2}) d (A + 2C + 2B \cos [c+dx] + A \cos [2c+2dx]) \text{Sec} [c+dx]^{7/2} \right) + \\
& \quad \left( (4B + 2i\sqrt{2} B + 6C + 3i\sqrt{2} C) \text{Log} [\sqrt{2} + 2 \sin \left[ \frac{1}{2} (c+dx) \right]] \text{Sec} \left[ \frac{1}{2} (c+dx) \right]^3 \right. \\
& \quad \left. (a (1 + \text{Sec} [c+dx]))^{3/2} (A + B \text{Sec} [c+dx] + C \text{Sec} [c+dx]^2) \right) / \\
& \quad \left( 4 (i + \sqrt{2}) d (A + 2C + 2B \cos [c+dx] + A \cos [2c+2dx]) \text{Sec} [c+dx]^{7/2} \right) - \\
& \quad \left( \left( \frac{1}{16} - \frac{i}{16} \right) \left( (-1+i) + \sqrt{2} \right) \left( (6+2i) B + 2\sqrt{2} B + (9+3i) C + 3\sqrt{2} C \right) \right. \\
& \quad \left. \text{Log} [2 - \sqrt{2} \cos \left[ \frac{1}{2} (c+dx) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c+dx) \right]] \text{Sec} \left[ \frac{1}{2} (c+dx) \right]^3 \right. \\
& \quad \left. (a (1 + \text{Sec} [c+dx]))^{3/2} (A + B \text{Sec} [c+dx] + C \text{Sec} [c+dx]^2) \right) / \\
& \quad \left( \sqrt{2} (i + \sqrt{2}) d (A + 2C + 2B \cos [c+dx] + A \cos [2c+2dx]) \text{Sec} [c+dx]^{7/2} \right) + \\
& \quad \left( \left( \frac{1}{16} + \frac{i}{16} \right) \left( (1+i) + \sqrt{2} \right) \left( (-6+2i) B + 2\sqrt{2} B - (9-3i) C + 3\sqrt{2} C \right) \right. \\
& \quad \left. \text{Log} [2 + \sqrt{2} \cos \left[ \frac{1}{2} (c+dx) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c+dx) \right]] \text{Sec} \left[ \frac{1}{2} (c+dx) \right]^3 \right. \\
& \quad \left. (a (1 + \text{Sec} [c+dx]))^{3/2} (A + B \text{Sec} [c+dx] + C \text{Sec} [c+dx]^2) \right) / \\
& \quad \left( \sqrt{2} (i + \sqrt{2}) d (A + 2C + 2B \cos [c+dx] + A \cos [2c+2dx]) \text{Sec} [c+dx]^{7/2} \right) + \\
& \quad \left( C \text{Sec} \left[ \frac{1}{2} (c+dx) \right]^3 (a (1 + \text{Sec} [c+dx]))^{3/2} (A + B \text{Sec} [c+dx] + C \text{Sec} [c+dx]^2) \right) / \\
& \quad \left( 2d (A + 2C + 2B \cos [c+dx] + A \cos [2c+2dx]) \right. \\
& \quad \left. \text{Sec} [c+dx]^{7/2} \left( \cos \left[ \frac{1}{2} (c+dx) \right] - \sin \left[ \frac{1}{2} (c+dx) \right] \right) \right) - \\
& \quad \left( C \text{Sec} \left[ \frac{1}{2} (c+dx) \right]^3 (a (1 + \text{Sec} [c+dx]))^{3/2} (A + B \text{Sec} [c+dx] + C \text{Sec} [c+dx]^2) \right) / \\
& \quad \left( 2d (A + 2C + 2B \cos [c+dx] + A \cos [2c+2dx]) \right. \\
& \quad \left. \text{Sec} [c+dx]^{7/2} \left( \cos \left[ \frac{1}{2} (c+dx) \right] + \sin \left[ \frac{1}{2} (c+dx) \right] \right) \right) + \\
& \quad \left( A \text{Sec} \left[ \frac{1}{2} (c+dx) \right]^3 (a (1 + \text{Sec} [c+dx]))^{3/2} (A + B \text{Sec} [c+dx] + C \text{Sec} [c+dx]^2) \right. \\
& \quad \left. \sin \left[ \frac{3}{2} (c+dx) \right] \right) / (3d (A + 2C + 2B \cos [c+dx] + A \cos [2c+2dx]) \text{Sec} [c+dx]^{7/2}) +
\end{aligned}$$



$$\left( (3A + 2B) \operatorname{Sec} \left[ \frac{1}{2} (c + dx) \right]^2 (a (1 + \operatorname{Sec} [c + dx]))^{3/2} (A + B \operatorname{Sec} [c + dx] + C \operatorname{Sec} [c + dx]^2) \right. \\ \left. \operatorname{Tan} \left[ \frac{1}{2} (c + dx) \right] \right) / (d (A + 2C + 2B \operatorname{Cos} [c + dx] + A \operatorname{Cos} [2c + 2dx]) \operatorname{Sec} [c + dx]^{7/2})$$

**Problem 591: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \operatorname{Sec} [c + dx])^{3/2} (A + B \operatorname{Sec} [c + dx] + C \operatorname{Sec} [c + dx]^2)}{\operatorname{Sec} [c + dx]^{5/2}} dx$$

Optimal (type 3, 172 leaves, 5 steps):

$$\frac{2 a^{3/2} C \operatorname{ArcSinh} \left[ \frac{\sqrt{a} \operatorname{Tan} [c + dx]}{\sqrt{a + a \operatorname{Sec} [c + dx]}} \right]}{d} + \frac{2 a^2 (12 A + 20 B + 15 C) \sqrt{\operatorname{Sec} [c + dx]} \operatorname{Sin} [c + dx]}{15 d \sqrt{a + a \operatorname{Sec} [c + dx]}} + \\ \frac{2 a (3 A + 5 B) \sqrt{a + a \operatorname{Sec} [c + dx]} \operatorname{Sin} [c + dx]}{15 d \sqrt{\operatorname{Sec} [c + dx]}} + \frac{2 A (a + a \operatorname{Sec} [c + dx])^{3/2} \operatorname{Sin} [c + dx]}{5 d \operatorname{Sec} [c + dx]^{3/2}}$$

Result (type 3, 387 leaves):

$$\frac{1}{60 d \sqrt{\operatorname{Sec} [c + dx]}} a \operatorname{Sec} \left[ \frac{1}{2} (c + dx) \right] \sqrt{a (1 + \operatorname{Sec} [c + dx])} \\ \left( -30 i \sqrt{2} C \operatorname{ArcTan} \left[ \frac{\operatorname{Cos} \left[ \frac{1}{4} (c + dx) \right] - (-1 + \sqrt{2}) \operatorname{Sin} \left[ \frac{1}{4} (c + dx) \right]}{(1 + \sqrt{2}) \operatorname{Cos} \left[ \frac{1}{4} (c + dx) \right] - \operatorname{Sin} \left[ \frac{1}{4} (c + dx) \right]} \right] - \right. \\ \left. 30 i \sqrt{2} C \operatorname{ArcTan} \left[ \frac{\operatorname{Cos} \left[ \frac{1}{4} (c + dx) \right] - (1 + \sqrt{2}) \operatorname{Sin} \left[ \frac{1}{4} (c + dx) \right]}{(-1 + \sqrt{2}) \operatorname{Cos} \left[ \frac{1}{4} (c + dx) \right] - \operatorname{Sin} \left[ \frac{1}{4} (c + dx) \right]} \right] + \right. \\ \left. 30 \sqrt{2} C \operatorname{Log} \left[ \sqrt{2} + 2 \operatorname{Sin} \left[ \frac{1}{2} (c + dx) \right] \right] - \right. \\ \left. 15 \sqrt{2} C \operatorname{Log} \left[ 2 - \sqrt{2} \operatorname{Cos} \left[ \frac{1}{2} (c + dx) \right] - \sqrt{2} \operatorname{Sin} \left[ \frac{1}{2} (c + dx) \right] \right] - \right. \\ \left. 15 \sqrt{2} C \operatorname{Log} \left[ 2 + \sqrt{2} \operatorname{Cos} \left[ \frac{1}{2} (c + dx) \right] - \sqrt{2} \operatorname{Sin} \left[ \frac{1}{2} (c + dx) \right] \right] + \right. \\ \left. 120 A \operatorname{Sin} \left[ \frac{1}{2} (c + dx) \right] + 180 B \operatorname{Sin} \left[ \frac{1}{2} (c + dx) \right] + 120 C \operatorname{Sin} \left[ \frac{1}{2} (c + dx) \right] + \right. \\ \left. 30 A \operatorname{Sin} \left[ \frac{3}{2} (c + dx) \right] + 20 B \operatorname{Sin} \left[ \frac{3}{2} (c + dx) \right] + 6 A \operatorname{Sin} \left[ \frac{5}{2} (c + dx) \right] \right)$$

**Problem 595: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec} [c + dx]^{5/2} (a + a \operatorname{Sec} [c + dx])^{5/2} (A + B \operatorname{Sec} [c + dx] + C \operatorname{Sec} [c + dx]^2) dx$$

Optimal (type 3, 333 leaves, 8 steps):

$$\frac{a^{5/2} (1304 A + 1132 B + 1015 C) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{512 d} +$$

$$\frac{a^3 (1304 A + 1132 B + 1015 C) \operatorname{Sec}[c+dx]^{3/2} \operatorname{Sin}[c+dx]}{512 d \sqrt{a+a \operatorname{Sec}[c+dx]}} +$$

$$\frac{a^3 (1304 A + 1132 B + 1015 C) \operatorname{Sec}[c+dx]^{5/2} \operatorname{Sin}[c+dx]}{768 d \sqrt{a+a \operatorname{Sec}[c+dx]}} +$$

$$\frac{a^3 (680 A + 628 B + 545 C) \operatorname{Sec}[c+dx]^{7/2} \operatorname{Sin}[c+dx]}{960 d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{1}{480 d}$$

$$a^2 (120 A + 156 B + 115 C) \operatorname{Sec}[c+dx]^{7/2} \sqrt{a+a \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx] +$$

$$\frac{a (12 B + 5 C) \operatorname{Sec}[c+dx]^{7/2} (a+a \operatorname{Sec}[c+dx])^{3/2} \operatorname{Sin}[c+dx]}{60 d} +$$

$$\frac{C \operatorname{Sec}[c+dx]^{7/2} (a+a \operatorname{Sec}[c+dx])^{5/2} \operatorname{Sin}[c+dx]}{6 d}$$

Result (type 3, 1361 leaves):

$$-\left(\left(\left(\frac{1}{8192} + \frac{i}{8192}\right) \left((-1+i) + \sqrt{2}\right) \left((3912 + 1304 i) A +\right.\right.\right.$$

$$\left.\left.\left.1304 \sqrt{2} A + (3396 + 1132 i) B + 1132 \sqrt{2} B + (3045 + 1015 i) C + 1015 \sqrt{2} C\right)\right.\right.$$

$$\left.\operatorname{ArcTan}\left[\frac{\operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right] - \sqrt{2} \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right]}{-\operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] + \sqrt{2} \operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right]}\right]\right.\right.$$

$$\left.\left.\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\operatorname{Sec}[c+dx]))^{5/2} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2)\right]\right) /$$

$$\left(\sqrt{2} (i + \sqrt{2}) d (A + 2 C + 2 B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) \operatorname{Sec}[c+dx]^{9/2}\right) -$$

$$\left(\left(\frac{1}{8192} - \frac{i}{8192}\right) \left((1+i) + \sqrt{2}\right) \left((-3912 + 1304 i) A + 1304 \sqrt{2} A -\right.\right.$$

$$\left.\left.(3396 - 1132 i) B + 1132 \sqrt{2} B - (3045 - 1015 i) C + 1015 \sqrt{2} C\right)\right.\right.$$

$$\left.\operatorname{ArcTan}\left[\frac{\operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right] - \sqrt{2} \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right]}{\operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] + \sqrt{2} \operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right]}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^5\right.\right.$$

$$\left.\left.(a(1+\operatorname{Sec}[c+dx]))^{5/2} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2)\right)\right) /$$

$$\left(\sqrt{2} (i + \sqrt{2}) d (A + 2 C + 2 B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) \operatorname{Sec}[c+dx]^{9/2}\right) +$$

$$\begin{aligned}
 & \left( (2608 A + 1304 i \sqrt{2} A + 2264 B + 1132 i \sqrt{2} B + 2030 C + 1015 i \sqrt{2} C) \operatorname{Log} \left[ \sqrt{2} + 2 \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^5 (a (1 + \operatorname{Sec} [c + d x]))^{5/2} (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) \right) / \\
 & \quad (4096 (i + \sqrt{2}) d (A + 2 C + 2 B \operatorname{Cos} [c + d x] + A \operatorname{Cos} [2 c + 2 d x]) \operatorname{Sec} [c + d x]^{9/2}) - \\
 & \quad \left( \left( \frac{1}{16384} - \frac{i}{16384} \right) ((-1 + i) + \sqrt{2}) \right. \\
 & \quad \left. \left( (3912 + 1304 i) A + 1304 \sqrt{2} A + (3396 + 1132 i) B + 1132 \sqrt{2} B + (3045 + 1015 i) C + 1015 \sqrt{2} C \right) \right. \\
 & \quad \left. \operatorname{Log} \left[ 2 - \sqrt{2} \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right] - \sqrt{2} \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] \right] \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^5 \right. \\
 & \quad \left. (a (1 + \operatorname{Sec} [c + d x]))^{5/2} (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) \right) / \\
 & \quad (\sqrt{2} (i + \sqrt{2}) d (A + 2 C + 2 B \operatorname{Cos} [c + d x] + A \operatorname{Cos} [2 c + 2 d x]) \operatorname{Sec} [c + d x]^{9/2}) + \\
 & \quad \left( \left( \frac{1}{16384} + \frac{i}{16384} \right) ((1 + i) + \sqrt{2}) \left( (-3912 + 1304 i) A + 1304 \sqrt{2} A - \right. \right. \\
 & \quad \left. \left. (3396 - 1132 i) B + 1132 \sqrt{2} B - (3045 - 1015 i) C + 1015 \sqrt{2} C \right) \right. \\
 & \quad \left. \operatorname{Log} \left[ 2 + \sqrt{2} \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right] - \sqrt{2} \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] \right] \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^5 \right. \\
 & \quad \left. (a (1 + \operatorname{Sec} [c + d x]))^{5/2} (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) \right) / \\
 & \quad (\sqrt{2} (i + \sqrt{2}) d (A + 2 C + 2 B \operatorname{Cos} [c + d x] + A \operatorname{Cos} [2 c + 2 d x]) \operatorname{Sec} [c + d x]^{9/2}) + \\
 & \quad \frac{1}{491520 d (A + 2 C + 2 B \operatorname{Cos} [c + d x] + A \operatorname{Cos} [2 c + 2 d x])} \\
 & \quad \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^5 \operatorname{Sec} [c + d x]^{3/2} (a (1 + \operatorname{Sec} [c + d x]))^{5/2} (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) \\
 & \quad \left( -96720 A \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] - 78120 B \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] - 47250 C \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] \right) + \\
 & \quad 164240 A \operatorname{Sin} \left[ \frac{3}{2} (c + d x) \right] + 167944 B \operatorname{Sin} \left[ \frac{3}{2} (c + d x) \right] + 184490 C \operatorname{Sin} \left[ \frac{3}{2} (c + d x) \right] - \\
 & \quad 7560 A \operatorname{Sin} \left[ \frac{5}{2} (c + d x) \right] + 13980 B \operatorname{Sin} \left[ \frac{5}{2} (c + d x) \right] + 28275 C \operatorname{Sin} \left[ \frac{5}{2} (c + d x) \right] + \\
 & \quad 101160 A \operatorname{Sin} \left[ \frac{7}{2} (c + d x) \right] + 98484 B \operatorname{Sin} \left[ \frac{7}{2} (c + d x) \right] + 88305 C \operatorname{Sin} \left[ \frac{7}{2} (c + d x) \right] + \\
 & \quad 6520 A \operatorname{Sin} \left[ \frac{9}{2} (c + d x) \right] + 5660 B \operatorname{Sin} \left[ \frac{9}{2} (c + d x) \right] + 5075 C \operatorname{Sin} \left[ \frac{9}{2} (c + d x) \right] + \\
 & \quad 19560 A \operatorname{Sin} \left[ \frac{11}{2} (c + d x) \right] + 16980 B \operatorname{Sin} \left[ \frac{11}{2} (c + d x) \right] + 15225 C \operatorname{Sin} \left[ \frac{11}{2} (c + d x) \right] \Big)
 \end{aligned}$$

**Problem 596: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec} [c + d x]^{3/2} (a + a \operatorname{Sec} [c + d x])^{5/2} (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) dx$$

Optimal (type 3, 281 leaves, 7 steps):

$$\frac{a^{5/2} (400 A + 326 B + 283 C) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{128 d} +$$

$$\frac{a^3 (400 A + 326 B + 283 C) \operatorname{Sec}[c+dx]^{3/2} \operatorname{Sin}[c+dx]}{128 d \sqrt{a+a \operatorname{Sec}[c+dx]}} +$$

$$\frac{a^3 (1040 A + 950 B + 787 C) \operatorname{Sec}[c+dx]^{5/2} \operatorname{Sin}[c+dx]}{960 d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{1}{240 d}$$

$$a^2 (80 A + 110 B + 79 C) \operatorname{Sec}[c+dx]^{5/2} \sqrt{a+a \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx] +$$

$$\frac{a (2 B + C) \operatorname{Sec}[c+dx]^{5/2} (a+a \operatorname{Sec}[c+dx])^{3/2} \operatorname{Sin}[c+dx]}{8 d} +$$

$$\frac{C \operatorname{Sec}[c+dx]^{5/2} (a+a \operatorname{Sec}[c+dx])^{5/2} \operatorname{Sin}[c+dx]}{5 d}$$

Result (type 3, 2352 leaves):

$$-\left(\left(\frac{1}{2048} + \frac{i}{2048}\right) \left((-1+i) + \sqrt{2}\right) \left(\left(1200 + 400 i\right) A + 400 \sqrt{2} A + \left(978 + 326 i\right) B + 326 \sqrt{2} B + \left(849 + 283 i\right) C + 283 \sqrt{2} C\right) \operatorname{ArcTan}\left[\frac{\operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right] - \sqrt{2} \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right]}{-\operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] + \sqrt{2} \operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right]}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^5 \left(a \left(1 + \operatorname{Sec}[c+dx]\right)\right)^{5/2} \left(A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2\right)\right] /$$

$$\left(\sqrt{2} (i + \sqrt{2}) d \left(A + 2 C + 2 B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]\right) \operatorname{Sec}[c+dx]^{9/2}\right) -$$

$$\left(\left(\frac{1}{2048} - \frac{i}{2048}\right) \left((1+i) + \sqrt{2}\right) \left(\left(-1200 + 400 i\right) A + 400 \sqrt{2} A - \left(978 - 326 i\right) B + 326 \sqrt{2} B - \left(849 - 283 i\right) C + 283 \sqrt{2} C\right) \operatorname{ArcTan}\left[\frac{\operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right] - \sqrt{2} \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right]}{\operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] + \sqrt{2} \operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right]}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^5 \left(a \left(1 + \operatorname{Sec}[c+dx]\right)\right)^{5/2} \left(A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2\right)\right] /$$

$$\left(\sqrt{2} (i + \sqrt{2}) d \left(A + 2 C + 2 B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]\right) \operatorname{Sec}[c+dx]^{9/2}\right) +$$

$$\left(\left(800 A + 400 i \sqrt{2} A + 652 B + 326 i \sqrt{2} B + 566 C + 283 i \sqrt{2} C\right) \operatorname{Log}\left[\sqrt{2} + 2 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^5 \left(a \left(1 + \operatorname{Sec}[c+dx]\right)\right)^{5/2} \left(A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2\right)\right) /$$

$$\left(1024 (i + \sqrt{2}) d \left(A + 2 C + 2 B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]\right) \operatorname{Sec}[c+dx]^{9/2}\right) -$$

$$\begin{aligned}
 & \left( \left( \frac{1}{4096} - \frac{i}{4096} \right) \left( (-1+i) + \sqrt{2} \right) \right. \\
 & \quad \left( (1200+400i)A + 400\sqrt{2}A + (978+326i)B + 326\sqrt{2}B + (849+283i)C + 283\sqrt{2}C \right) \\
 & \quad \text{Log} \left[ 2 - \sqrt{2} \cos \left[ \frac{1}{2}(c+dx) \right] - \sqrt{2} \sin \left[ \frac{1}{2}(c+dx) \right] \right] \sec \left[ \frac{1}{2}(c+dx) \right]^5 \\
 & \quad \left. \left( a(1+\sec[c+dx]) \right)^{5/2} (A+B \sec[c+dx] + C \sec^2[c+dx]) \right) / \\
 & \quad \left( \sqrt{2} (i + \sqrt{2}) d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \sec[c+dx]^{9/2} \right) + \\
 & \left( \left( \frac{1}{4096} + \frac{i}{4096} \right) \left( (1+i) + \sqrt{2} \right) \right. \\
 & \quad \left( (-1200+400i)A + 400\sqrt{2}A - (978-326i)B + 326\sqrt{2}B - (849-283i)C + 283\sqrt{2}C \right) \\
 & \quad \text{Log} \left[ 2 + \sqrt{2} \cos \left[ \frac{1}{2}(c+dx) \right] - \sqrt{2} \sin \left[ \frac{1}{2}(c+dx) \right] \right] \sec \left[ \frac{1}{2}(c+dx) \right]^5 \\
 & \quad \left. \left( a(1+\sec[c+dx]) \right)^{5/2} (A+B \sec[c+dx] + C \sec^2[c+dx]) \right) / \\
 & \quad \left( \sqrt{2} (i + \sqrt{2}) d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \sec[c+dx]^{9/2} \right) + \\
 & \left( C \sec \left[ \frac{1}{2}(c+dx) \right]^5 \left( a(1+\sec[c+dx]) \right)^{5/2} (A+B \sec[c+dx] + C \sec^2[c+dx]) \right) / \\
 & \quad \left( 80d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right. \\
 & \quad \left. \sec[c+dx]^{9/2} \left( \cos \left[ \frac{1}{2}(c+dx) \right] - \sin \left[ \frac{1}{2}(c+dx) \right] \right)^5 \right) + \\
 & \left( (16A+46B+59C) \sec \left[ \frac{1}{2}(c+dx) \right]^5 \left( a(1+\sec[c+dx]) \right)^{5/2} \right. \\
 & \quad \left. (A+B \sec[c+dx] + C \sec^2[c+dx]) \right) / \left( 384d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right. \\
 & \quad \left. \sec[c+dx]^{9/2} \left( \cos \left[ \frac{1}{2}(c+dx) \right] - \sin \left[ \frac{1}{2}(c+dx) \right] \right)^3 \right) + \\
 & \left( (400A+326B+283C) \sec \left[ \frac{1}{2}(c+dx) \right]^5 \left( a(1+\sec[c+dx]) \right)^{5/2} \right. \\
 & \quad \left. (A+B \sec[c+dx] + C \sec^2[c+dx]) \right) / \left( 512d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right. \\
 & \quad \left. \sec[c+dx]^{9/2} \left( \cos \left[ \frac{1}{2}(c+dx) \right] - \sin \left[ \frac{1}{2}(c+dx) \right] \right) \right) - \\
 & \left( C \sec \left[ \frac{1}{2}(c+dx) \right]^5 \left( a(1+\sec[c+dx]) \right)^{5/2} (A+B \sec[c+dx] + C \sec^2[c+dx]) \right) / \\
 & \quad \left( 80d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right. \\
 & \quad \left. \sec[c+dx]^{9/2} \left( \cos \left[ \frac{1}{2}(c+dx) \right] + \sin \left[ \frac{1}{2}(c+dx) \right] \right)^5 \right) + \\
 & \left( (-16A-46B-59C) \sec \left[ \frac{1}{2}(c+dx) \right]^5 \left( a(1+\sec[c+dx]) \right)^{5/2} \right. \\
 & \quad \left. (A+B \sec[c+dx] + C \sec^2[c+dx]) \right) / \left( 384d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \operatorname{Sec}[c+dx]^{9/2} \left( \cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3 + \\
 & \left( (-400A - 326B - 283C) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\operatorname{Sec}[c+dx]))^{5/2} \right. \\
 & \quad \left. (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \left( 512d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right) \\
 & \operatorname{Sec}[c+dx]^{9/2} \left( \cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right) + \\
 & \left( \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\operatorname{Sec}[c+dx]))^{5/2} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right. \\
 & \quad \left. \left( 2B \sin\left[\frac{1}{2}(c+dx)\right] + 5C \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) / \\
 & \left( 64d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \operatorname{Sec}[c+dx]^{9/2} \right. \\
 & \quad \left. \left( \cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right] \right)^4 \right) + \\
 & \left( \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\operatorname{Sec}[c+dx]))^{5/2} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right. \\
 & \quad \left. \left( 2B \sin\left[\frac{1}{2}(c+dx)\right] + 5C \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) / \\
 & \left( 64d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \operatorname{Sec}[c+dx]^{9/2} \right. \\
 & \quad \left. \left( \cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^4 \right) + \\
 & \left( \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\operatorname{Sec}[c+dx]))^{5/2} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right. \\
 & \quad \left. \left( 80A \sin\left[\frac{1}{2}(c+dx)\right] + 86B \sin\left[\frac{1}{2}(c+dx)\right] + 75C \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) / \\
 & \left( 256d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \operatorname{Sec}[c+dx]^{9/2} \right. \\
 & \quad \left. \left( \cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right] \right)^2 \right) + \\
 & \left( \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\operatorname{Sec}[c+dx]))^{5/2} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right. \\
 & \quad \left. \left( 80A \sin\left[\frac{1}{2}(c+dx)\right] + 86B \sin\left[\frac{1}{2}(c+dx)\right] + 75C \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) / \\
 & \left( 256d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \operatorname{Sec}[c+dx]^{9/2} \right. \\
 & \quad \left. \left( \cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^2 \right)
 \end{aligned}$$

**Problem 597: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \sqrt{\sec[c + dx]} (a + a \sec[c + dx])^{5/2} (A + B \sec[c + dx] + C \sec[c + dx]^2) dx$$

Optimal (type 3, 233 leaves, 6 steps):

$$\frac{a^{5/2} (304 A + 200 B + 163 C) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan[c + dx]}{\sqrt{a + a \sec[c + dx]}}\right]}{64 d} +$$

$$\frac{a^3 (432 A + 392 B + 299 C) \sec[c + dx]^{3/2} \sin[c + dx]}{192 d \sqrt{a + a \sec[c + dx]}} +$$

$$\frac{a^2 (16 A + 24 B + 17 C) \sec[c + dx]^{3/2} \sqrt{a + a \sec[c + dx]} \sin[c + dx]}{32 d} +$$

$$\frac{a (8 B + 5 C) \sec[c + dx]^{3/2} (a + a \sec[c + dx])^{3/2} \sin[c + dx]}{24 d} +$$

$$\frac{C \sec[c + dx]^{3/2} (a + a \sec[c + dx])^{5/2} \sin[c + dx]}{4 d}$$

Result (type 3, 2084 leaves):

$$- \left( \left( \frac{1}{1024} + \frac{i}{1024} \right) \left( (-1 + i) + \sqrt{2} \right) \right.$$

$$\left. \left( (912 + 304 i) A + 304 \sqrt{2} A + (600 + 200 i) B + 200 \sqrt{2} B + (489 + 163 i) C + 163 \sqrt{2} C \right) \right.$$

$$\left. \operatorname{ArcTan}\left[ \frac{\cos\left[\frac{1}{4}(c + dx)\right] - \sin\left[\frac{1}{4}(c + dx)\right] - \sqrt{2} \sin\left[\frac{1}{4}(c + dx)\right]}{-\cos\left[\frac{1}{4}(c + dx)\right] + \sqrt{2} \cos\left[\frac{1}{4}(c + dx)\right] - \sin\left[\frac{1}{4}(c + dx)\right]} \right] \right.$$

$$\left. \sec\left[\frac{1}{2}(c + dx)\right]^5 (a (1 + \sec[c + dx]))^{5/2} (A + B \sec[c + dx] + C \sec[c + dx]^2) \right) /$$

$$\left( \sqrt{2} (i + \sqrt{2}) d (A + 2 C + 2 B \cos[c + dx] + A \cos[2c + 2dx]) \sec[c + dx]^{9/2} \right) -$$

$$\left( \left( \frac{1}{1024} - \frac{i}{1024} \right) \left( (1 + i) + \sqrt{2} \right) \left( (-912 + 304 i) A + 304 \sqrt{2} A - \right. \right.$$

$$\left. (600 - 200 i) B + 200 \sqrt{2} B - (489 - 163 i) C + 163 \sqrt{2} C \right) \right.$$

$$\left. \operatorname{ArcTan}\left[ \frac{\cos\left[\frac{1}{4}(c + dx)\right] + \sin\left[\frac{1}{4}(c + dx)\right] - \sqrt{2} \sin\left[\frac{1}{4}(c + dx)\right]}{\cos\left[\frac{1}{4}(c + dx)\right] + \sqrt{2} \cos\left[\frac{1}{4}(c + dx)\right] - \sin\left[\frac{1}{4}(c + dx)\right]} \right] \sec\left[\frac{1}{2}(c + dx)\right]^5 \right.$$

$$\left. (a (1 + \sec[c + dx]))^{5/2} (A + B \sec[c + dx] + C \sec[c + dx]^2) \right) /$$

$$\left( \sqrt{2} (i + \sqrt{2}) d (A + 2 C + 2 B \cos[c + dx] + A \cos[2c + 2dx]) \sec[c + dx]^{9/2} \right) +$$

$$\left( (608 A + 304 i \sqrt{2} A + 400 B + 200 i \sqrt{2} B + 326 C + 163 i \sqrt{2} C) \operatorname{Log}\left[\sqrt{2} + 2 \sin\left[\frac{1}{2}(c + dx)\right]\right] \right)$$

$$\begin{aligned}
& \left. \left( \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^5 (a (1 + \text{Sec} [c + d x]))^{5/2} (A + B \text{Sec} [c + d x] + C \text{Sec} [c + d x]^2) \right) \right) / \\
& \left( 512 (\mathbf{i} + \sqrt{2}) d (A + 2 C + 2 B \text{Cos} [c + d x] + A \text{Cos} [2 c + 2 d x]) \text{Sec} [c + d x]^{9/2} \right) - \\
& \left( \left( \frac{1}{2048} - \frac{\mathbf{i}}{2048} \right) \left( (-1 + \mathbf{i}) + \sqrt{2} \right) \right. \\
& \quad \left( (912 + 304 \mathbf{i}) A + 304 \sqrt{2} A + (600 + 200 \mathbf{i}) B + 200 \sqrt{2} B + (489 + 163 \mathbf{i}) C + 163 \sqrt{2} C \right) \\
& \quad \left. \text{Log} \left[ 2 - \sqrt{2} \text{Cos} \left[ \frac{1}{2} (c + d x) \right] - \sqrt{2} \text{Sin} \left[ \frac{1}{2} (c + d x) \right] \right] \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^5 \right. \\
& \quad \left. (a (1 + \text{Sec} [c + d x]))^{5/2} (A + B \text{Sec} [c + d x] + C \text{Sec} [c + d x]^2) \right) \Big/ \\
& \left( \sqrt{2} (\mathbf{i} + \sqrt{2}) d (A + 2 C + 2 B \text{Cos} [c + d x] + A \text{Cos} [2 c + 2 d x]) \text{Sec} [c + d x]^{9/2} \right) + \\
& \left( \left( \frac{1}{2048} + \frac{\mathbf{i}}{2048} \right) \left( (1 + \mathbf{i}) + \sqrt{2} \right) \right. \\
& \quad \left( (-912 + 304 \mathbf{i}) A + 304 \sqrt{2} A - (600 - 200 \mathbf{i}) B + 200 \sqrt{2} B - (489 - 163 \mathbf{i}) C + 163 \sqrt{2} C \right) \\
& \quad \left. \text{Log} \left[ 2 + \sqrt{2} \text{Cos} \left[ \frac{1}{2} (c + d x) \right] - \sqrt{2} \text{Sin} \left[ \frac{1}{2} (c + d x) \right] \right] \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^5 \right. \\
& \quad \left. (a (1 + \text{Sec} [c + d x]))^{5/2} (A + B \text{Sec} [c + d x] + C \text{Sec} [c + d x]^2) \right) \Big/ \\
& \left( \sqrt{2} (\mathbf{i} + \sqrt{2}) d (A + 2 C + 2 B \text{Cos} [c + d x] + A \text{Cos} [2 c + 2 d x]) \text{Sec} [c + d x]^{9/2} \right) + \\
& \left( (8 B + 23 C) \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^5 (a (1 + \text{Sec} [c + d x]))^{5/2} (A + B \text{Sec} [c + d x] + C \text{Sec} [c + d x]^2) \right) \Big/ \\
& \left( 192 d (A + 2 C + 2 B \text{Cos} [c + d x] + A \text{Cos} [2 c + 2 d x]) \right. \\
& \quad \left. \text{Sec} [c + d x]^{9/2} \left( \text{Cos} \left[ \frac{1}{2} (c + d x) \right] - \text{Sin} \left[ \frac{1}{2} (c + d x) \right] \right)^3 \right) + \\
& \left( (176 A + 200 B + 163 C) \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^5 (a (1 + \text{Sec} [c + d x]))^{5/2} \right. \\
& \quad \left. (A + B \text{Sec} [c + d x] + C \text{Sec} [c + d x]^2) \right) \Big/ \left( 256 d (A + 2 C + 2 B \text{Cos} [c + d x] + A \text{Cos} [2 c + 2 d x]) \right. \\
& \quad \left. \text{Sec} [c + d x]^{9/2} \left( \text{Cos} \left[ \frac{1}{2} (c + d x) \right] - \text{Sin} \left[ \frac{1}{2} (c + d x) \right] \right) \right) + \\
& \left( (-8 B - 23 C) \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^5 (a (1 + \text{Sec} [c + d x]))^{5/2} (A + B \text{Sec} [c + d x] + C \text{Sec} [c + d x]^2) \right) \Big/ \\
& \left( 192 d (A + 2 C + 2 B \text{Cos} [c + d x] + A \text{Cos} [2 c + 2 d x]) \right. \\
& \quad \left. \text{Sec} [c + d x]^{9/2} \left( \text{Cos} \left[ \frac{1}{2} (c + d x) \right] + \text{Sin} \left[ \frac{1}{2} (c + d x) \right] \right)^3 \right) + \\
& \left( (-176 A - 200 B - 163 C) \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^5 (a (1 + \text{Sec} [c + d x]))^{5/2} \right. \\
& \quad \left. (A + B \text{Sec} [c + d x] + C \text{Sec} [c + d x]^2) \right) \Big/ \left( 256 d (A + 2 C + 2 B \text{Cos} [c + d x] + A \text{Cos} [2 c + 2 d x]) \right. \\
& \quad \left. \text{Sec} [c + d x]^{9/2} \left( \text{Cos} \left[ \frac{1}{2} (c + d x) \right] + \text{Sin} \left[ \frac{1}{2} (c + d x) \right] \right) \right) + \\
& \left( \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^5 (a (1 + \text{Sec} [c + d x]))^{5/2} (A + B \text{Sec} [c + d x] + C \text{Sec} [c + d x]^2) \right)
\end{aligned}$$



$$\begin{aligned}
 & \left( 16 A \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + 40 B \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + 43 C \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \Big/ \\
 & \left( 128 d (A+2 C+2 B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2 c+2 d x]) \operatorname{Sec}[c+dx]^{9/2} \right. \\
 & \left. \left( \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^2 \right) + \\
 & \left( \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\operatorname{Sec}[c+dx]))^{5/2} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right. \\
 & \left. \left( 16 A \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + 40 B \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + 43 C \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \Big/ \right. \\
 & \left. \left( 128 d (A+2 C+2 B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2 c+2 d x]) \operatorname{Sec}[c+dx]^{9/2} \right. \right. \\
 & \left. \left. \left( \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^2 \right) \right) + \\
 & \left( C \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4 (a(1+\operatorname{Sec}[c+dx]))^{5/2} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \Big/ \left( 32 d (A+2 C+2 B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2 c+2 d x]) \right. \\
 & \left. \operatorname{Sec}[c+dx]^{9/2} \left( \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^4 \right) + \\
 & \left( C \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4 (a(1+\operatorname{Sec}[c+dx]))^{5/2} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \Big/ \left( 32 d (A+2 C+2 B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2 c+2 d x]) \right. \\
 & \left. \operatorname{Sec}[c+dx]^{9/2} \left( \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^4 \right)
 \end{aligned}$$

**Problem 598: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(a+a \operatorname{Sec}[c+dx])^{5/2} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2)}{\sqrt{\operatorname{Sec}[c+dx]}} dx$$

Optimal (type 3, 233 leaves, 6 steps):

$$\begin{aligned}
 & \frac{a^{5/2} (40 A + 38 B + 25 C) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{8 d} + \frac{a^3 (24 A - 54 B - 49 C) \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{24 d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \\
 & \frac{a^2 (24 A + 42 B + 31 C) \sqrt{\operatorname{Sec}[c+dx]} \sqrt{a+a \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{24 d} + \\
 & \frac{a (6 B + 5 C) \sqrt{\operatorname{Sec}[c+dx]} (a+a \operatorname{Sec}[c+dx])^{3/2} \operatorname{Sin}[c+dx]}{12 d} + \\
 & \frac{C \sqrt{\operatorname{Sec}[c+dx]} (a+a \operatorname{Sec}[c+dx])^{5/2} \operatorname{Sin}[c+dx]}{3 d}
 \end{aligned}$$

Result (type 3, 1894 leaves):

$$\begin{aligned}
 & - \left( \left( \frac{1}{128} + \frac{i}{128} \right) \left( (-1+i) + \sqrt{2} \right) \right. \\
 & \quad \left( (120+40i)A + 40\sqrt{2}A + (114+38i)B + 38\sqrt{2}B + (75+25i)C + 25\sqrt{2}C \right) \\
 & \quad \text{ArcTan} \left[ \frac{\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right] - \sqrt{2}\sin\left[\frac{1}{4}(c+dx)\right]}{-\cos\left[\frac{1}{4}(c+dx)\right] + \sqrt{2}\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]} \right] \\
 & \quad \left. \text{Sec} \left[ \frac{1}{2}(c+dx) \right]^5 \left( a(1+\text{Sec}[c+dx]) \right)^{5/2} \left( A+B\text{Sec}[c+dx] + C\text{Sec}[c+dx]^2 \right) \right] / \\
 & \quad \left( \sqrt{2}(i+\sqrt{2})d(A+2C+2B\cos[c+dx] + A\cos[2c+2dx])\text{Sec}[c+dx]^{9/2} \right) - \\
 & \left( \left( \frac{1}{128} - \frac{i}{128} \right) \left( (1+i) + \sqrt{2} \right) \left( (-120+40i)A + 40\sqrt{2}A - (114-38i)B + 38\sqrt{2}B - \right. \right. \\
 & \quad \left. \left. (75-25i)C + 25\sqrt{2}C \right) \text{ArcTan} \left[ \frac{\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right] - \sqrt{2}\sin\left[\frac{1}{4}(c+dx)\right]}{\cos\left[\frac{1}{4}(c+dx)\right] + \sqrt{2}\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]} \right] \right) \\
 & \quad \left. \text{Sec} \left[ \frac{1}{2}(c+dx) \right]^5 \left( a(1+\text{Sec}[c+dx]) \right)^{5/2} \left( A+B\text{Sec}[c+dx] + C\text{Sec}[c+dx]^2 \right) \right] / \\
 & \quad \left( \sqrt{2}(i+\sqrt{2})d(A+2C+2B\cos[c+dx] + A\cos[2c+2dx])\text{Sec}[c+dx]^{9/2} \right) + \\
 & \left( (80A+40i\sqrt{2}A+76B+38i\sqrt{2}B+50C+25i\sqrt{2}C) \text{Log} \left[ \sqrt{2} + 2\sin\left[\frac{1}{2}(c+dx)\right] \right] \right) \\
 & \quad \left. \text{Sec} \left[ \frac{1}{2}(c+dx) \right]^5 \left( a(1+\text{Sec}[c+dx]) \right)^{5/2} \left( A+B\text{Sec}[c+dx] + C\text{Sec}[c+dx]^2 \right) \right] / \\
 & \quad \left( 64(i+\sqrt{2})d(A+2C+2B\cos[c+dx] + A\cos[2c+2dx])\text{Sec}[c+dx]^{9/2} \right) - \\
 & \left( \left( \frac{1}{256} - \frac{i}{256} \right) \left( (-1+i) + \sqrt{2} \right) \right. \\
 & \quad \left( (120+40i)A + 40\sqrt{2}A + (114+38i)B + 38\sqrt{2}B + (75+25i)C + 25\sqrt{2}C \right) \\
 & \quad \text{Log} \left[ 2 - \sqrt{2}\cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2}\sin\left[\frac{1}{2}(c+dx)\right] \right] \text{Sec} \left[ \frac{1}{2}(c+dx) \right]^5 \\
 & \quad \left. \left( a(1+\text{Sec}[c+dx]) \right)^{5/2} \left( A+B\text{Sec}[c+dx] + C\text{Sec}[c+dx]^2 \right) \right] / \\
 & \quad \left( \sqrt{2}(i+\sqrt{2})d(A+2C+2B\cos[c+dx] + A\cos[2c+2dx])\text{Sec}[c+dx]^{9/2} \right) + \\
 & \left( \left( \frac{1}{256} + \frac{i}{256} \right) \left( (1+i) + \sqrt{2} \right) \right. \\
 & \quad \left( (-120+40i)A + 40\sqrt{2}A - (114-38i)B + 38\sqrt{2}B - (75-25i)C + 25\sqrt{2}C \right) \\
 & \quad \text{Log} \left[ 2 + \sqrt{2}\cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2}\sin\left[\frac{1}{2}(c+dx)\right] \right] \text{Sec} \left[ \frac{1}{2}(c+dx) \right]^5 \\
 & \quad \left. \left( a(1+\text{Sec}[c+dx]) \right)^{5/2} \left( A+B\text{Sec}[c+dx] + C\text{Sec}[c+dx]^2 \right) \right] /
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{2} \left( \frac{1}{2} + \frac{1}{2} \right) d \left( A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx] \right) \sec [c + dx]^{9/2} \right) + \\
 & \left( C \sec \left[ \frac{1}{2} (c + dx) \right]^5 \left( a \left( 1 + \sec [c + dx] \right) \right)^{5/2} \left( A + B \sec [c + dx] + C \sec [c + dx]^2 \right) \right) / \\
 & \left( 24 d \left( A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx] \right) \right. \\
 & \quad \left. \sec [c + dx]^{9/2} \left( \cos \left[ \frac{1}{2} (c + dx) \right] - \sin \left[ \frac{1}{2} (c + dx) \right] \right)^3 \right) + \\
 & \left( (8A + 22B + 25C) \sec \left[ \frac{1}{2} (c + dx) \right]^5 \left( a \left( 1 + \sec [c + dx] \right) \right)^{5/2} \right. \\
 & \quad \left. \left( A + B \sec [c + dx] + C \sec [c + dx]^2 \right) \right) / \left( 32 d \left( A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx] \right) \right. \\
 & \quad \left. \sec [c + dx]^{9/2} \left( \cos \left[ \frac{1}{2} (c + dx) \right] - \sin \left[ \frac{1}{2} (c + dx) \right] \right) \right) - \\
 & \left( C \sec \left[ \frac{1}{2} (c + dx) \right]^5 \left( a \left( 1 + \sec [c + dx] \right) \right)^{5/2} \left( A + B \sec [c + dx] + C \sec [c + dx]^2 \right) \right) / \\
 & \left( 24 d \left( A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx] \right) \right. \\
 & \quad \left. \sec [c + dx]^{9/2} \left( \cos \left[ \frac{1}{2} (c + dx) \right] + \sin \left[ \frac{1}{2} (c + dx) \right] \right)^3 \right) + \\
 & \left( (-8A - 22B - 25C) \sec \left[ \frac{1}{2} (c + dx) \right]^5 \left( a \left( 1 + \sec [c + dx] \right) \right)^{5/2} \right. \\
 & \quad \left. \left( A + B \sec [c + dx] + C \sec [c + dx]^2 \right) \right) / \left( 32 d \left( A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx] \right) \right. \\
 & \quad \left. \sec [c + dx]^{9/2} \left( \cos \left[ \frac{1}{2} (c + dx) \right] + \sin \left[ \frac{1}{2} (c + dx) \right] \right) \right) + \\
 & \left( \sec \left[ \frac{1}{2} (c + dx) \right]^5 \left( a \left( 1 + \sec [c + dx] \right) \right)^{5/2} \left( A + B \sec [c + dx] + C \sec [c + dx]^2 \right) \right. \\
 & \quad \left. \left( 2B \sin \left[ \frac{1}{2} (c + dx) \right] + 5C \sin \left[ \frac{1}{2} (c + dx) \right] \right) \right) / \\
 & \left( 16 d \left( A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx] \right) \sec [c + dx]^{9/2} \right. \\
 & \quad \left. \left( \cos \left[ \frac{1}{2} (c + dx) \right] - \sin \left[ \frac{1}{2} (c + dx) \right] \right)^2 \right) + \\
 & \left( \sec \left[ \frac{1}{2} (c + dx) \right]^5 \left( a \left( 1 + \sec [c + dx] \right) \right)^{5/2} \left( A + B \sec [c + dx] + C \sec [c + dx]^2 \right) \right. \\
 & \quad \left. \left( 2B \sin \left[ \frac{1}{2} (c + dx) \right] + 5C \sin \left[ \frac{1}{2} (c + dx) \right] \right) \right) / \\
 & \left( 16 d \left( A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx] \right) \sec [c + dx]^{9/2} \right. \\
 & \quad \left. \left( \cos \left[ \frac{1}{2} (c + dx) \right] + \sin \left[ \frac{1}{2} (c + dx) \right] \right)^2 \right) + \\
 & \left( A \sec \left[ \frac{1}{2} (c + dx) \right]^4 \left( a \left( 1 + \sec [c + dx] \right) \right)^{5/2} \left( A + B \sec [c + dx] + C \sec [c + dx]^2 \right) \right. \\
 & \quad \left. \tan \left[ \frac{1}{2} (c + dx) \right] \right) / \left( d \left( A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx] \right) \sec [c + dx]^{9/2} \right)
 \end{aligned}$$

**Problem 599: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \operatorname{Sec}[c + d x])^{5/2} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[c + d x]^{3/2}} dx$$

Optimal (type 3, 233 leaves, 6 steps):

$$\frac{a^{5/2} (8 A + 20 B + 19 C) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c + d x]}{\sqrt{a + a \operatorname{Sec}[c + d x]}}\right]}{4 d} + \frac{a^3 (56 A + 12 B - 27 C) \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{12 d \sqrt{a + a \operatorname{Sec}[c + d x]}} -$$

$$\frac{a^2 (8 A - 12 B - 21 C) \sqrt{\operatorname{Sec}[c + d x]} \sqrt{a + a \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{12 d} -$$

$$\frac{a (4 A - 3 C) \sqrt{\operatorname{Sec}[c + d x]} (a + a \operatorname{Sec}[c + d x])^{3/2} \operatorname{Sin}[c + d x]}{6 d} +$$

$$\frac{2 A (a + a \operatorname{Sec}[c + d x])^{5/2} \operatorname{Sin}[c + d x]}{3 d \sqrt{\operatorname{Sec}[c + d x]}}$$

Result (type 3, 1736 leaves):

$$- \left( \left( \frac{1}{64} + \frac{i}{64} \right) \left( (-1 + i) + \sqrt{2} \right) \right.$$

$$\left. \left( (24 + 8 i) A + 8 \sqrt{2} A + (60 + 20 i) B + 20 \sqrt{2} B + (57 + 19 i) C + 19 \sqrt{2} C \right) \right.$$

$$\left. \operatorname{ArcTan}\left[ \frac{\operatorname{Cos}\left[\frac{1}{4}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{4}(c + d x)\right] - \sqrt{2} \operatorname{Sin}\left[\frac{1}{4}(c + d x)\right]}{-\operatorname{Cos}\left[\frac{1}{4}(c + d x)\right] + \sqrt{2} \operatorname{Cos}\left[\frac{1}{4}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{4}(c + d x)\right]} \right] \right.$$

$$\left. \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^5 (a (1 + \operatorname{Sec}[c + d x]))^{5/2} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) /$$

$$\left( \sqrt{2} (i + \sqrt{2}) d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \operatorname{Sec}[c + d x]^{9/2} \right) -$$

$$\left( \left( \frac{1}{64} - \frac{i}{64} \right) \left( (1 + i) + \sqrt{2} \right) \left( (-24 + 8 i) A + 8 \sqrt{2} A - (60 - 20 i) B + 20 \sqrt{2} B - (57 - 19 i) C + \right. \right.$$

$$\left. 19 \sqrt{2} C \right) \operatorname{ArcTan}\left[ \frac{\operatorname{Cos}\left[\frac{1}{4}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{4}(c + d x)\right] - \sqrt{2} \operatorname{Sin}\left[\frac{1}{4}(c + d x)\right]}{\operatorname{Cos}\left[\frac{1}{4}(c + d x)\right] + \sqrt{2} \operatorname{Cos}\left[\frac{1}{4}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{4}(c + d x)\right]} \right] \right.$$

$$\left. \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^5 (a (1 + \operatorname{Sec}[c + d x]))^{5/2} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) /$$

$$\left( \sqrt{2} (i + \sqrt{2}) d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \operatorname{Sec}[c + d x]^{9/2} \right) +$$

$$\left( (16 A + 8 i \sqrt{2} A + 40 B + 20 i \sqrt{2} B + 38 C + 19 i \sqrt{2} C) \operatorname{Log}\left[\sqrt{2} + 2 \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right)$$

$$\begin{aligned}
 & \left. \left( \sec \left[ \frac{1}{2} (c+dx) \right]^5 (a(1+\sec[c+dx]))^{5/2} (A+B \sec[c+dx]+C \sec[c+dx]^2) \right) \right/ \\
 & \left( 32 (\sqrt{2} + i) d (A+2C+2B \cos[c+dx]+A \cos[2c+2dx]) \sec[c+dx]^{9/2} \right) - \\
 & \left( \left( \frac{1}{128} - \frac{i}{128} \right) ((-1+i) + \sqrt{2}) \right. \\
 & \quad \left( (24+8i)A + 8\sqrt{2}A + (60+20i)B + 20\sqrt{2}B + (57+19i)C + 19\sqrt{2}C \right) \\
 & \quad \left. \log \left[ 2 - \sqrt{2} \cos \left[ \frac{1}{2} (c+dx) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c+dx) \right] \right] \sec \left[ \frac{1}{2} (c+dx) \right]^5 \right. \\
 & \quad \left. (a(1+\sec[c+dx]))^{5/2} (A+B \sec[c+dx]+C \sec[c+dx]^2) \right) \right/ \\
 & \left( \sqrt{2} (\sqrt{2} + i) d (A+2C+2B \cos[c+dx]+A \cos[2c+2dx]) \sec[c+dx]^{9/2} \right) + \\
 & \left( \left( \frac{1}{128} + \frac{i}{128} \right) ((1+i) + \sqrt{2}) \right. \\
 & \quad \left( (-24+8i)A + 8\sqrt{2}A - (60-20i)B + 20\sqrt{2}B - (57-19i)C + 19\sqrt{2}C \right) \\
 & \quad \left. \log \left[ 2 + \sqrt{2} \cos \left[ \frac{1}{2} (c+dx) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c+dx) \right] \right] \sec \left[ \frac{1}{2} (c+dx) \right]^5 \right. \\
 & \quad \left. (a(1+\sec[c+dx]))^{5/2} (A+B \sec[c+dx]+C \sec[c+dx]^2) \right) \right/ \\
 & \left( \sqrt{2} (\sqrt{2} + i) d (A+2C+2B \cos[c+dx]+A \cos[2c+2dx]) \sec[c+dx]^{9/2} \right) + \\
 & \left( (4B+11C) \sec \left[ \frac{1}{2} (c+dx) \right]^5 (a(1+\sec[c+dx]))^{5/2} (A+B \sec[c+dx]+C \sec[c+dx]^2) \right) \right/ \\
 & \left( 16d (A+2C+2B \cos[c+dx]+A \cos[2c+2dx]) \right. \\
 & \quad \left. \sec[c+dx]^{9/2} \left( \cos \left[ \frac{1}{2} (c+dx) \right] - \sin \left[ \frac{1}{2} (c+dx) \right] \right) \right) + \\
 & \left( (-4B-11C) \sec \left[ \frac{1}{2} (c+dx) \right]^5 (a(1+\sec[c+dx]))^{5/2} (A+B \sec[c+dx]+C \sec[c+dx]^2) \right) \right/ \\
 & \left( 16d (A+2C+2B \cos[c+dx]+A \cos[2c+2dx]) \right. \\
 & \quad \left. \sec[c+dx]^{9/2} \left( \cos \left[ \frac{1}{2} (c+dx) \right] + \sin \left[ \frac{1}{2} (c+dx) \right] \right) \right) + \\
 & \left( A \sec \left[ \frac{1}{2} (c+dx) \right]^5 (a(1+\sec[c+dx]))^{5/2} (A+B \sec[c+dx]+C \sec[c+dx]^2) \right. \\
 & \quad \left. \sin \left[ \frac{3}{2} (c+dx) \right] \right) \right/ (6d (A+2C+2B \cos[c+dx]+A \cos[2c+2dx]) \sec[c+dx]^{9/2}) + \\
 & \left( (5A+2B) \sec \left[ \frac{1}{2} (c+dx) \right]^4 (a(1+\sec[c+dx]))^{5/2} (A+B \sec[c+dx]+C \sec[c+dx]^2) \right. \\
 & \quad \left. \tan \left[ \frac{1}{2} (c+dx) \right] \right) \right/ (2d (A+2C+2B \cos[c+dx]+A \cos[2c+2dx]) \sec[c+dx]^{9/2}) + \\
 & \left( C \sec \left[ \frac{1}{2} (c+dx) \right]^4 (a(1+\sec[c+dx]))^{5/2} (A+B \sec[c+dx]+C \sec[c+dx]^2) \right. \\
 & \quad \left. \tan \left[ \frac{1}{2} (c+dx) \right] \right) \right/ (8d (A+2C+2B \cos[c+dx]+A \cos[2c+2dx]) \\
 & \quad \left. \sec[c+dx]^{9/2} \left( \cos \left[ \frac{1}{2} (c+dx) \right] - \sin \left[ \frac{1}{2} (c+dx) \right] \right)^2 \right) +
 \end{aligned}$$

$$\left( C \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^4 \left( a \left( 1 + \operatorname{Sec} [c + d x] \right) \right)^{5/2} \left( A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2 \right) \right. \\ \left. \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right) / \left( 8 d \left( A + 2 C + 2 B \operatorname{Cos} [c + d x] + A \operatorname{Cos} [2 c + 2 d x] \right) \right. \\ \left. \operatorname{Sec} [c + d x]^{9/2} \left( \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right)$$

**Problem 600: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\left( a + a \operatorname{Sec} [c + d x] \right)^{5/2} \left( A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2 \right)}{\operatorname{Sec} [c + d x]^{5/2}} dx$$

Optimal (type 3, 223 leaves, 6 steps):

$$\frac{a^{5/2} (2 B + 5 C) \operatorname{ArcSinh} \left[ \frac{\sqrt{a} \operatorname{Tan} [c + d x]}{\sqrt{a + a \operatorname{Sec} [c + d x]}} \right]}{d} + \frac{a^3 (64 A + 70 B + 15 C) \sqrt{\operatorname{Sec} [c + d x]} \operatorname{Sin} [c + d x]}{15 d \sqrt{a + a \operatorname{Sec} [c + d x]}} - \\ \frac{a^2 (16 A + 10 B - 15 C) \sqrt{\operatorname{Sec} [c + d x]} \sqrt{a + a \operatorname{Sec} [c + d x]} \operatorname{Sin} [c + d x]}{15 d} + \\ \frac{2 a (A + B) \left( a + a \operatorname{Sec} [c + d x] \right)^{3/2} \operatorname{Sin} [c + d x]}{3 d \sqrt{\operatorname{Sec} [c + d x]}} + \frac{2 A \left( a + a \operatorname{Sec} [c + d x] \right)^{5/2} \operatorname{Sin} [c + d x]}{5 d \operatorname{Sec} [c + d x]^{3/2}}$$

Result (type 3, 1519 leaves):

$$- \left( \left( \left( \frac{1}{16} + \frac{i}{16} \right) \left( (-1 + i) + \sqrt{2} \right) \left( (6 + 2 i) B + 2 \sqrt{2} B + (15 + 5 i) C + 5 \sqrt{2} C \right) \right. \right. \\ \left. \operatorname{ArcTan} \left[ \frac{\operatorname{Cos} \left[ \frac{1}{4} (c + d x) \right] - \operatorname{Sin} \left[ \frac{1}{4} (c + d x) \right] - \sqrt{2} \operatorname{Sin} \left[ \frac{1}{4} (c + d x) \right]}{-\operatorname{Cos} \left[ \frac{1}{4} (c + d x) \right] + \sqrt{2} \operatorname{Cos} \left[ \frac{1}{4} (c + d x) \right] - \operatorname{Sin} \left[ \frac{1}{4} (c + d x) \right]} \right] \right. \\ \left. \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^5 \left( a \left( 1 + \operatorname{Sec} [c + d x] \right) \right)^{5/2} \left( A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2 \right) \right) / \\ \left( \sqrt{2} \left( i + \sqrt{2} \right) d \left( A + 2 C + 2 B \operatorname{Cos} [c + d x] + A \operatorname{Cos} [2 c + 2 d x] \right) \operatorname{Sec} [c + d x]^{9/2} \right) - \\ \left( \left( \frac{1}{16} - \frac{i}{16} \right) \left( (1 + i) + \sqrt{2} \right) \left( (-6 + 2 i) B + 2 \sqrt{2} B - (15 - 5 i) C + 5 \sqrt{2} C \right) \right. \\ \left. \operatorname{ArcTan} \left[ \frac{\operatorname{Cos} \left[ \frac{1}{4} (c + d x) \right] + \operatorname{Sin} \left[ \frac{1}{4} (c + d x) \right] - \sqrt{2} \operatorname{Sin} \left[ \frac{1}{4} (c + d x) \right]}{\operatorname{Cos} \left[ \frac{1}{4} (c + d x) \right] + \sqrt{2} \operatorname{Cos} \left[ \frac{1}{4} (c + d x) \right] - \operatorname{Sin} \left[ \frac{1}{4} (c + d x) \right]} \right] \right. \\ \left. \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^5 \left( a \left( 1 + \operatorname{Sec} [c + d x] \right) \right)^{5/2} \left( A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2 \right) \right) /$$

$$\begin{aligned}
 & \left( \sqrt{2} \left( i + \sqrt{2} \right) d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \sec [c + d x]^{9/2} \right) + \\
 & \left( \left( 4 B + 2 i \sqrt{2} B + 10 C + 5 i \sqrt{2} C \right) \log \left[ \sqrt{2} + 2 \sin \left[ \frac{1}{2} (c + d x) \right] \right] \sec \left[ \frac{1}{2} (c + d x) \right]^5 \right. \\
 & \quad \left. \left( a \left( 1 + \sec [c + d x] \right) \right)^{5/2} \left( A + B \sec [c + d x] + C \sec [c + d x]^2 \right) \right) / \\
 & \left( 8 \left( i + \sqrt{2} \right) d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \sec [c + d x]^{9/2} \right) - \\
 & \left( \left( \frac{1}{32} - \frac{i}{32} \right) \left( (-1 + i) + \sqrt{2} \right) \left( (6 + 2 i) B + 2 \sqrt{2} B + (15 + 5 i) C + 5 \sqrt{2} C \right) \right. \\
 & \quad \left. \log \left[ 2 - \sqrt{2} \cos \left[ \frac{1}{2} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c + d x) \right] \right] \sec \left[ \frac{1}{2} (c + d x) \right]^5 \right. \\
 & \quad \left. \left( a \left( 1 + \sec [c + d x] \right) \right)^{5/2} \left( A + B \sec [c + d x] + C \sec [c + d x]^2 \right) \right) / \\
 & \left( \sqrt{2} \left( i + \sqrt{2} \right) d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \sec [c + d x]^{9/2} \right) + \\
 & \left( \left( \frac{1}{32} + \frac{i}{32} \right) \left( (1 + i) + \sqrt{2} \right) \left( (-6 + 2 i) B + 2 \sqrt{2} B - (15 - 5 i) C + 5 \sqrt{2} C \right) \right. \\
 & \quad \left. \log \left[ 2 + \sqrt{2} \cos \left[ \frac{1}{2} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c + d x) \right] \right] \sec \left[ \frac{1}{2} (c + d x) \right]^5 \right. \\
 & \quad \left. \left( a \left( 1 + \sec [c + d x] \right) \right)^{5/2} \left( A + B \sec [c + d x] + C \sec [c + d x]^2 \right) \right) / \\
 & \left( \sqrt{2} \left( i + \sqrt{2} \right) d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \sec [c + d x]^{9/2} \right) + \\
 & \left( C \sec \left[ \frac{1}{2} (c + d x) \right]^5 \left( a \left( 1 + \sec [c + d x] \right) \right)^{5/2} \left( A + B \sec [c + d x] + C \sec [c + d x]^2 \right) \right) / \\
 & \left( 4 d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \right. \\
 & \quad \left. \sec [c + d x]^{9/2} \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) - \\
 & \left( C \sec \left[ \frac{1}{2} (c + d x) \right]^5 \left( a \left( 1 + \sec [c + d x] \right) \right)^{5/2} \left( A + B \sec [c + d x] + C \sec [c + d x]^2 \right) \right) / \\
 & \left( 4 d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \right. \\
 & \quad \left. \sec [c + d x]^{9/2} \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) + \\
 & \left( (5 A + 2 B) \sec \left[ \frac{1}{2} (c + d x) \right]^5 \left( a \left( 1 + \sec [c + d x] \right) \right)^{5/2} \left( A + B \sec [c + d x] + C \sec [c + d x]^2 \right) \right. \\
 & \quad \left. \sin \left[ \frac{3}{2} (c + d x) \right] \right) / \left( 12 d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \sec [c + d x]^{9/2} \right) + \\
 & \left( A \sec \left[ \frac{1}{2} (c + d x) \right]^5 \left( a \left( 1 + \sec [c + d x] \right) \right)^{5/2} \left( A + B \sec [c + d x] + C \sec [c + d x]^2 \right) \right. \\
 & \quad \left. \sin \left[ \frac{5}{2} (c + d x) \right] \right) / \left( 20 d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \sec [c + d x]^{9/2} \right) + \\
 & \left( (5 A + 5 B + 2 C) \sec \left[ \frac{1}{2} (c + d x) \right]^4 \left( a \left( 1 + \sec [c + d x] \right) \right)^{5/2} \left( A + B \sec [c + d x] + C \sec [c + d x]^2 \right) \right. \\
 & \quad \left. \tan \left[ \frac{1}{2} (c + d x) \right] \right) / \left( 2 d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \sec [c + d x]^{9/2} \right)
 \end{aligned}$$

**Problem 601: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{(a + a \operatorname{Sec}[c + d x])^{5/2} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[c + d x]^{7/2}} dx$$

Optimal (type 3, 222 leaves, 6 steps):

$$\frac{2 a^{5/2} C \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right]}{d} + \frac{2 a^3 (160 A + 224 B + 245 C) \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{105 d \sqrt{a+a \operatorname{Sec}[c+d x]}} +$$

$$\frac{2 a^2 (40 A + 56 B + 35 C) \sqrt{a+a \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{105 d \sqrt{\operatorname{Sec}[c+d x]}} +$$

$$\frac{2 a (5 A + 7 B) (a+a \operatorname{Sec}[c+d x])^{3/2} \operatorname{Sin}[c+d x]}{35 d \operatorname{Sec}[c+d x]^{3/2}} + \frac{2 A (a+a \operatorname{Sec}[c+d x])^{5/2} \operatorname{Sin}[c+d x]}{7 d \operatorname{Sec}[c+d x]^{5/2}}$$

Result (type 3, 428 leaves):

$$\frac{1}{420 d \sqrt{\operatorname{Sec}[c+d x]}} a^2 \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right] \sqrt{a(1+\operatorname{Sec}[c+d x])}$$

$$\left( -210 i \sqrt{2} C \operatorname{ArcTan}\left[\frac{\cos\left[\frac{1}{4}(c+d x)\right] - (-1+\sqrt{2}) \operatorname{Sin}\left[\frac{1}{4}(c+d x)\right]}{(1+\sqrt{2}) \cos\left[\frac{1}{4}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{4}(c+d x)\right]}\right] - \right.$$

$$210 i \sqrt{2} C \operatorname{ArcTan}\left[\frac{\cos\left[\frac{1}{4}(c+d x)\right] - (1+\sqrt{2}) \operatorname{Sin}\left[\frac{1}{4}(c+d x)\right]}{(-1+\sqrt{2}) \cos\left[\frac{1}{4}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{4}(c+d x)\right]}\right] +$$

$$210 \sqrt{2} C \operatorname{Log}\left[\sqrt{2} + 2 \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] -$$

$$105 \sqrt{2} C \operatorname{Log}\left[2 - \sqrt{2} \cos\left[\frac{1}{2}(c+d x)\right] - \sqrt{2} \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] -$$

$$105 \sqrt{2} C \operatorname{Log}\left[2 + \sqrt{2} \cos\left[\frac{1}{2}(c+d x)\right] - \sqrt{2} \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] +$$

$$1575 A \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] + 2100 B \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] + 2100 C \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] +$$

$$385 A \operatorname{Sin}\left[\frac{3}{2}(c+d x)\right] + 350 B \operatorname{Sin}\left[\frac{3}{2}(c+d x)\right] + 140 C \operatorname{Sin}\left[\frac{3}{2}(c+d x)\right] +$$

$$105 A \operatorname{Sin}\left[\frac{5}{2}(c+d x)\right] + 42 B \operatorname{Sin}\left[\frac{5}{2}(c+d x)\right] + 15 A \operatorname{Sin}\left[\frac{7}{2}(c+d x)\right] \left. \right)$$

**Problem 605: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c+d x]^{5/2} (A + B \operatorname{Sec}[c+d x] + C \operatorname{Sec}[c+d x]^2)}{\sqrt{a+a \operatorname{Sec}[c+d x]}} dx$$



Optimal (type 3, 241 leaves, 8 steps):

$$\begin{aligned}
 & - \frac{(8A - 14B + 9C) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{8\sqrt{a}d} + \\
 & \frac{\sqrt{2}(A-B+C) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{\sqrt{2} \sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{\sqrt{a}d} + \frac{(8A-2B+7C) \operatorname{Sec}[c+dx]^{3/2} \operatorname{Sin}[c+dx]}{8d\sqrt{a+a \operatorname{Sec}[c+dx]}} + \\
 & \frac{(6B-C) \operatorname{Sec}[c+dx]^{5/2} \operatorname{Sin}[c+dx]}{12d\sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{C \operatorname{Sec}[c+dx]^{7/2} \operatorname{Sin}[c+dx]}{3d\sqrt{a+a \operatorname{Sec}[c+dx]}}
 \end{aligned}$$

Result (type 3, 2012 leaves):

$$\begin{aligned}
 & - \left( \left( \frac{1}{16} - \frac{i}{16} \right) \left( (1+i) - i\sqrt{2} \right) \right. \\
 & \quad \left( (24+8i)A + 8\sqrt{2}A - (42+14i)B - 14\sqrt{2}B + (27+9i)C + 9\sqrt{2}C \right) \\
 & \quad \operatorname{ArcTan}\left[ \frac{\operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right] - \sqrt{2} \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right]}{-\operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] + \sqrt{2} \operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right]} \right] \\
 & \quad \left. \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \left( \sqrt{2} (i+\sqrt{2})d \right. \\
 & \quad \left. (A+2C+2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) \operatorname{Sec}[c+dx]^{3/2} \sqrt{a(1+\operatorname{Sec}[c+dx])} \right) + \\
 & \left( \left( \frac{1}{16} - \frac{i}{16} \right) \left( (1+i) + \sqrt{2} \right) \left( (-24+8i)A + 8\sqrt{2}A + (42-14i)B - 14\sqrt{2}B - (27-9i)C + 9\sqrt{2}C \right) \right. \\
 & \quad \operatorname{ArcTan}\left[ \frac{\operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right] - \sqrt{2} \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right]}{\operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] + \sqrt{2} \operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right]} \right] \\
 & \quad \left. \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad \left( \sqrt{2} (i+\sqrt{2})d (A+2C+2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) \right. \\
 & \quad \left. \operatorname{Sec}[c+dx]^{3/2} \sqrt{a(1+\operatorname{Sec}[c+dx])} \right) - \\
 & \quad \left( 4(A-B+C) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right]\right] \right. \\
 & \quad \left. (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad \left( d (A+2C+2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) \operatorname{Sec}[c+dx]^{3/2} \sqrt{a(1+\operatorname{Sec}[c+dx])} \right) + \\
 & \quad \left( 4(A-B+C) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right]\right] \right)
 \end{aligned}$$

$$\begin{aligned}
& \left. \left( A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2 \right) \right) / \\
& \left( d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \operatorname{Sec}[c + d x]^{3/2} \sqrt{a (1 + \operatorname{Sec}[c + d x])} \right) + \\
& \left( (-16 A - 8 i \sqrt{2} A + 28 B + 14 i \sqrt{2} B - 18 C - 9 i \sqrt{2} C) \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] \right. \\
& \left. \operatorname{Log}\left[\sqrt{2} + 2 \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) / \\
& \left( 8 (i + \sqrt{2}) d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \operatorname{Sec}[c + d x]^{3/2} \right. \\
& \left. \sqrt{a (1 + \operatorname{Sec}[c + d x])} \right) + \left( \left( \frac{1}{32} + \frac{i}{32} \right) ((1 + i) - i \sqrt{2}) \right. \\
& \left. \left( (24 + 8 i) A + 8 \sqrt{2} A - (42 + 14 i) B - 14 \sqrt{2} B + (27 + 9 i) C + 9 \sqrt{2} C \right) \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] \right. \\
& \left. \operatorname{Log}\left[2 - \sqrt{2} \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \sqrt{2} \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) / \\
& \left( \sqrt{2} (i + \sqrt{2}) d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \right. \\
& \left. \operatorname{Sec}[c + d x]^{3/2} \sqrt{a (1 + \operatorname{Sec}[c + d x])} \right) - \\
& \left( \left( \frac{1}{32} + \frac{i}{32} \right) ((1 + i) + \sqrt{2}) \left( (-24 + 8 i) A + 8 \sqrt{2} A + (42 - 14 i) B - 14 \sqrt{2} B - (27 - 9 i) C + 9 \sqrt{2} C \right) \right. \\
& \left. \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] \operatorname{Log}\left[2 + \sqrt{2} \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \sqrt{2} \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right. \\
& \left. (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) / \left( \sqrt{2} (i + \sqrt{2}) d \right. \\
& \left. (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \operatorname{Sec}[c + d x]^{3/2} \sqrt{a (1 + \operatorname{Sec}[c + d x])} \right) + \\
& \left( C \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) / \\
& \left( 3 d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \operatorname{Sec}[c + d x]^{3/2} \right. \\
& \left. \sqrt{a (1 + \operatorname{Sec}[c + d x])} \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^3 \right) + \\
& \left( (8 A - 2 B + 7 C) \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) / \\
& \left( 4 d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \operatorname{Sec}[c + d x]^{3/2} \right. \\
& \left. \sqrt{a (1 + \operatorname{Sec}[c + d x])} \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \right) - \\
& \left( C \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) / \\
& \left( 3 d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \operatorname{Sec}[c + d x]^{3/2} \right. \\
& \left. \sqrt{a (1 + \operatorname{Sec}[c + d x])} \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^3 \right) + \\
& \left( (-8 A + 2 B - 7 C) \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) /
\end{aligned}$$

$$\begin{aligned}
 & \left( 4 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \operatorname{Sec}[c + d x]^{3/2} \right. \\
 & \quad \left. \sqrt{a (1 + \operatorname{Sec}[c + d x])} \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) + \\
 & \left( \cos \left[ \frac{1}{2} (c + d x) \right] (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \quad \left. \left( 2 B \sin \left[ \frac{1}{2} (c + d x) \right] - C \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) / \\
 & \left( 2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \operatorname{Sec}[c + d x]^{3/2} \right. \\
 & \quad \left. \sqrt{a (1 + \operatorname{Sec}[c + d x])} \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right)^2 + \\
 & \left( \cos \left[ \frac{1}{2} (c + d x) \right] (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \quad \left. \left( 2 B \sin \left[ \frac{1}{2} (c + d x) \right] - C \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) / \\
 & \left( 2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \operatorname{Sec}[c + d x]^{3/2} \right. \\
 & \quad \left. \sqrt{a (1 + \operatorname{Sec}[c + d x])} \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right)^2
 \end{aligned}$$

**Problem 606: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c + d x]^{3/2} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\sqrt{a + a \operatorname{Sec}[c + d x]}} dx$$

Optimal (type 3, 195 leaves, 7 steps):

$$\begin{aligned}
 & \frac{(8 A - 4 B + 7 C) \operatorname{ArcSinh} \left[ \frac{\sqrt{a} \operatorname{Tan}[c + d x]}{\sqrt{a + a \operatorname{Sec}[c + d x]}} \right]}{4 \sqrt{a} d} - \frac{\sqrt{2} (A - B + C) \operatorname{ArcTanh} \left[ \frac{\sqrt{a} \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{\sqrt{2} \sqrt{a + a \operatorname{Sec}[c + d x]}} \right]}{\sqrt{a} d} + \\
 & \frac{(4 B - C) \operatorname{Sec}[c + d x]^{3/2} \operatorname{Sin}[c + d x]}{4 d \sqrt{a + a \operatorname{Sec}[c + d x]}} + \frac{C \operatorname{Sec}[c + d x]^{5/2} \operatorname{Sin}[c + d x]}{2 d \sqrt{a + a \operatorname{Sec}[c + d x]}}
 \end{aligned}$$

Result (type 3, 1732 leaves):

$$\begin{aligned}
 & - \left( \left( \left( \frac{1}{8} + \frac{i}{8} \right) \left( (-1 + i) + \sqrt{2} \right) \left( (24 + 8 i) A + 8 \sqrt{2} A - (12 + 4 i) B - 4 \sqrt{2} B + (21 + 7 i) C + 7 \sqrt{2} C \right) \right. \right. \\
 & \quad \left. \operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{4} (c + d x) \right]}{-\cos \left[ \frac{1}{4} (c + d x) \right] + \sqrt{2} \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right]} \right] \right. \\
 & \quad \left. \left. \cos \left[ \frac{1}{2} (c + d x) \right] (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) \right) / \left( \sqrt{2} (i + \sqrt{2}) d \right)
 \end{aligned}$$

$$\begin{aligned}
& \left. \left( (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \operatorname{Sec}[c + dx]^{3/2} \sqrt{a(1 + \operatorname{Sec}[c + dx])} \right) \right) - \\
& \left( \left( \frac{1}{8} - \frac{i}{8} \right) \left( (1 + i) + \sqrt{2} \right) \left( (-24 + 8i)A + 8\sqrt{2}A + (12 - 4i)B - 4\sqrt{2}B - (21 - 7i)C + 7\sqrt{2}C \right) \right. \\
& \operatorname{ArcTan} \left[ \frac{\cos\left[\frac{1}{4}(c + dx)\right] + \sin\left[\frac{1}{4}(c + dx)\right] - \sqrt{2} \sin\left[\frac{1}{4}(c + dx)\right]}{\cos\left[\frac{1}{4}(c + dx)\right] + \sqrt{2} \cos\left[\frac{1}{4}(c + dx)\right] - \sin\left[\frac{1}{4}(c + dx)\right]} \right] \\
& \left. \cos\left[\frac{1}{2}(c + dx)\right] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right) / \\
& \left( \sqrt{2} (i + \sqrt{2}) d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \right. \\
& \left. \operatorname{Sec}[c + dx]^{3/2} \sqrt{a(1 + \operatorname{Sec}[c + dx])} \right) + \\
& \left( 4(A - B + C) \cos\left[\frac{1}{2}(c + dx)\right] \log\left[\cos\left[\frac{1}{4}(c + dx)\right] - \sin\left[\frac{1}{4}(c + dx)\right]\right] \right. \\
& \left. (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right) / \\
& \left( d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \operatorname{Sec}[c + dx]^{3/2} \sqrt{a(1 + \operatorname{Sec}[c + dx])} \right) - \\
& \left( 4(A - B + C) \cos\left[\frac{1}{2}(c + dx)\right] \log\left[\cos\left[\frac{1}{4}(c + dx)\right] + \sin\left[\frac{1}{4}(c + dx)\right]\right] \right. \\
& \left. (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right) / \\
& \left( d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \operatorname{Sec}[c + dx]^{3/2} \sqrt{a(1 + \operatorname{Sec}[c + dx])} \right) + \\
& \left( (16A + 8i\sqrt{2}A - 8B - 4i\sqrt{2}B + 14C + 7i\sqrt{2}C) \cos\left[\frac{1}{2}(c + dx)\right] \right. \\
& \left. \log\left[\sqrt{2} + 2 \sin\left[\frac{1}{2}(c + dx)\right]\right] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right) / \\
& \left( 4(i + \sqrt{2}) d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \right. \\
& \left. \operatorname{Sec}[c + dx]^{3/2} \sqrt{a(1 + \operatorname{Sec}[c + dx])} \right) - \\
& \left( \left( \frac{1}{16} - \frac{i}{16} \right) \left( (-1 + i) + \sqrt{2} \right) \left( (24 + 8i)A + 8\sqrt{2}A - (12 + 4i)B - 4\sqrt{2}B + (21 + 7i)C + 7\sqrt{2}C \right) \right. \\
& \left. \cos\left[\frac{1}{2}(c + dx)\right] \log\left[2 - \sqrt{2} \cos\left[\frac{1}{2}(c + dx)\right] - \sqrt{2} \sin\left[\frac{1}{2}(c + dx)\right]\right] \right. \\
& \left. (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right) / \left( \sqrt{2} (i + \sqrt{2}) d \right. \\
& \left. (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \operatorname{Sec}[c + dx]^{3/2} \sqrt{a(1 + \operatorname{Sec}[c + dx])} \right) + \\
& \left( \left( \frac{1}{16} + \frac{i}{16} \right) \left( (1 + i) + \sqrt{2} \right) \left( (-24 + 8i)A + 8\sqrt{2}A + (12 - 4i)B - 4\sqrt{2}B - (21 - 7i)C + 7\sqrt{2}C \right) \right. \\
& \left. \cos\left[\frac{1}{2}(c + dx)\right] \log\left[2 + \sqrt{2} \cos\left[\frac{1}{2}(c + dx)\right] - \sqrt{2} \sin\left[\frac{1}{2}(c + dx)\right]\right] \right)
\end{aligned}$$

$$\begin{aligned}
 & \left( (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) / \left( \sqrt{2} (\sqrt{2} + \sqrt{2}) d \right. \\
 & \left. (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \operatorname{Sec}[c + d x]^{3/2} \sqrt{a (1 + \operatorname{Sec}[c + d x])} \right) + \\
 & \left( (4 B - C) \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) / \\
 & \left( 2 d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \operatorname{Sec}[c + d x]^{3/2} \right. \\
 & \left. \sqrt{a (1 + \operatorname{Sec}[c + d x])} \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \right) + \\
 & \left( C \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) / \\
 & \left( d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \operatorname{Sec}[c + d x]^{3/2} \right. \\
 & \left. \sqrt{a (1 + \operatorname{Sec}[c + d x])} \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^2 \right) + \\
 & \left( C \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) / \\
 & \left( d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \operatorname{Sec}[c + d x]^{3/2} \right. \\
 & \left. \sqrt{a (1 + \operatorname{Sec}[c + d x])} \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^2 \right) + \\
 & \left( (-4 B + C) \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) / \\
 & \left( 2 d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \operatorname{Sec}[c + d x]^{3/2} \right. \\
 & \left. \sqrt{a (1 + \operatorname{Sec}[c + d x])} \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \right)
 \end{aligned}$$

**Problem 607: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\operatorname{Sec}[c + d x]} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\sqrt{a + a \operatorname{Sec}[c + d x]}} dx$$

Optimal (type 3, 141 leaves, 6 steps):

$$\begin{aligned}
 & \frac{(2 B - C) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c + d x]}{\sqrt{a + a \operatorname{Sec}[c + d x]}}\right]}{\sqrt{a} d} + \\
 & \frac{\sqrt{2} (A - B + C) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{\sqrt{2} \sqrt{a + a \operatorname{Sec}[c + d x]}}\right]}{\sqrt{a} d} + \frac{C \operatorname{Sec}[c + d x]^{3/2} \operatorname{Sin}[c + d x]}{d \sqrt{a + a \operatorname{Sec}[c + d x]}}
 \end{aligned}$$

Result (type 3, 644 leaves):

$$\left( \left( \frac{1}{8} + \frac{i}{8} \right) \cos \left[ \frac{1}{2} (c + d x) \right] (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\ \left. \left( \frac{1}{i + \sqrt{2}} 2 i \sqrt{2} \left( (-3 + i) + \sqrt{2} \right) \left( (1 + i) + \sqrt{2} \right) (2 B - C) \right. \right. \\ \left. \left. \operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c + d x) \right] - (-1 + \sqrt{2}) \sin \left[ \frac{1}{4} (c + d x) \right]}{(1 + \sqrt{2}) \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right]} \right] - \frac{1}{i + \sqrt{2}} 2 \sqrt{2} \left( (-1 + i) + \sqrt{2} \right) \right. \right. \\ \left. \left. \left( (3 + i) + \sqrt{2} \right) (2 B - C) \operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c + d x) \right] - (1 + \sqrt{2}) \sin \left[ \frac{1}{4} (c + d x) \right]}{(-1 + \sqrt{2}) \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right]} \right] - \right. \right. \\ (16 - 16 i) (A - B + C) \operatorname{Log} \left[ \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right] \right] + \\ (16 - 16 i) (A - B + C) \operatorname{Log} \left[ \cos \left[ \frac{1}{4} (c + d x) \right] + \sin \left[ \frac{1}{4} (c + d x) \right] \right] + \\ \left. \frac{(4 + 4 i) (-2 i + \sqrt{2}) (2 B - C) \operatorname{Log} \left[ \sqrt{2} + 2 \sin \left[ \frac{1}{2} (c + d x) \right] \right]}{i + \sqrt{2}} + \right. \\ \left. \frac{1}{i + \sqrt{2}} i \sqrt{2} \left( (-1 + i) + \sqrt{2} \right) \left( (3 + i) + \sqrt{2} \right) (2 B - C) \right. \\ \left. \operatorname{Log} \left[ 2 - \sqrt{2} \cos \left[ \frac{1}{2} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c + d x) \right] \right] + \frac{1}{i + \sqrt{2}} \sqrt{2} \left( (-3 + i) + \sqrt{2} \right) \right. \\ \left. \left( (1 + i) + \sqrt{2} \right) (2 B - C) \operatorname{Log} \left[ 2 + \sqrt{2} \cos \left[ \frac{1}{2} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c + d x) \right] \right] + \right. \\ \left. \frac{(8 - 8 i) C}{\cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right]} - \frac{(8 - 8 i) C}{\cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right]} \right) \Bigg/ \\ \left( d (A + 2 C + 2 B \cos[c + d x] + A \cos[2(c + d x)]) \operatorname{Sec}[c + d x]^{3/2} \sqrt{a (1 + \operatorname{Sec}[c + d x])} \right)$$

**Problem 608: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2}{\sqrt{\operatorname{Sec}[c + d x]} \sqrt{a + a \operatorname{Sec}[c + d x]}} dx$$

Optimal (type 3, 138 leaves, 6 steps):

$$\frac{2 C \operatorname{ArcSinh} \left[ \frac{\sqrt{a} \operatorname{Tan}[c + d x]}{\sqrt{a + a \operatorname{Sec}[c + d x]}} \right]}{\sqrt{a} d} - \\ \frac{\sqrt{2} (A - B + C) \operatorname{ArcTanh} \left[ \frac{\sqrt{a} \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{\sqrt{2} \sqrt{a + a \operatorname{Sec}[c + d x]}} \right]}{\sqrt{a} d} + \frac{2 A \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{d \sqrt{a + a \operatorname{Sec}[c + d x]}}$$

Result (type 3, 477 leaves):

$$\frac{1}{2 d \sqrt{a} (1 + \sec [c + d x])} \cos \left[ \frac{1}{2} (c + d x) \right] \sqrt{\sec [c + d x]} \left( -2 i \sqrt{2} C \operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c + d x) \right] - (-1 + \sqrt{2}) \sin \left[ \frac{1}{4} (c + d x) \right]}{(1 + \sqrt{2}) \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right]} \right] - 2 i \sqrt{2} C \operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c + d x) \right] - (1 + \sqrt{2}) \sin \left[ \frac{1}{4} (c + d x) \right]}{(-1 + \sqrt{2}) \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right]} \right] + 4 A \operatorname{Log} \left[ \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right] \right] - 4 B \operatorname{Log} \left[ \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right] \right] + 4 C \operatorname{Log} \left[ \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right] \right] - 4 A \operatorname{Log} \left[ \cos \left[ \frac{1}{4} (c + d x) \right] + \sin \left[ \frac{1}{4} (c + d x) \right] \right] + 4 B \operatorname{Log} \left[ \cos \left[ \frac{1}{4} (c + d x) \right] + \sin \left[ \frac{1}{4} (c + d x) \right] \right] - 4 C \operatorname{Log} \left[ \cos \left[ \frac{1}{4} (c + d x) \right] + \sin \left[ \frac{1}{4} (c + d x) \right] \right] + 2 \sqrt{2} C \operatorname{Log} \left[ \sqrt{2} + 2 \sin \left[ \frac{1}{2} (c + d x) \right] \right] - \sqrt{2} C \operatorname{Log} \left[ 2 - \sqrt{2} \cos \left[ \frac{1}{2} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c + d x) \right] \right] - \sqrt{2} C \operatorname{Log} \left[ 2 + \sqrt{2} \cos \left[ \frac{1}{2} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c + d x) \right] \right] + 8 A \sin \left[ \frac{1}{2} (c + d x) \right] \right)$$

**Problem 612: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\sec [c + d x]} (a A + (A b + a B) \sec [c + d x] + b B \sec [c + d x]^2)}{\sqrt{a + a \sec [c + d x]}} dx$$

Optimal (type 3, 152 leaves, 6 steps):

$$\frac{(2 A b + 2 a B - b B) \operatorname{ArcSinh} \left[ \frac{\sqrt{a} \tan [c + d x]}{\sqrt{a + a \sec [c + d x]}} \right]}{\sqrt{a} d} + \frac{\sqrt{2} (a - b) (A - B) \operatorname{ArcTanh} \left[ \frac{\sqrt{a} \sqrt{\sec [c + d x]} \sin [c + d x]}{\sqrt{2} \sqrt{a + a \sec [c + d x]}} \right]}{\sqrt{a} d} + \frac{b B \sec [c + d x]^{3/2} \sin [c + d x]}{d \sqrt{a + a \sec [c + d x]}}$$

Result (type 3, 638 leaves):

$$\frac{1}{d \sqrt{a (1 + \text{Sec}[c + d x])}} \left( \frac{1}{16} + \frac{i}{16} \right) \text{Cos} \left[ \frac{1}{2} (c + d x) \right] \sqrt{\text{Sec}[c + d x]}$$

$$\left( \frac{1}{i + \sqrt{2}} 2 i \sqrt{2} \left( (-3 + i) + \sqrt{2} \right) \left( (1 + i) + \sqrt{2} \right) (2 A b + 2 a B - b B) \right.$$

$$\text{ArcTan} \left[ \frac{\text{Cos} \left[ \frac{1}{4} (c + d x) \right] - (-1 + \sqrt{2}) \text{Sin} \left[ \frac{1}{4} (c + d x) \right]}{\left( 1 + \sqrt{2} \right) \text{Cos} \left[ \frac{1}{4} (c + d x) \right] - \text{Sin} \left[ \frac{1}{4} (c + d x) \right]} \right] - \frac{1}{i + \sqrt{2}} 2 \sqrt{2} \left( (-1 + i) + \sqrt{2} \right)$$

$$\left. \left( (3 + i) + \sqrt{2} \right) (2 A b + 2 a B - b B) \text{ArcTan} \left[ \frac{\text{Cos} \left[ \frac{1}{4} (c + d x) \right] - (1 + \sqrt{2}) \text{Sin} \left[ \frac{1}{4} (c + d x) \right]}{(-1 + \sqrt{2}) \text{Cos} \left[ \frac{1}{4} (c + d x) \right] - \text{Sin} \left[ \frac{1}{4} (c + d x) \right]} \right] - \right.$$

$$(16 - 16 i) (a - b) (A - B) \text{Log} \left[ \text{Cos} \left[ \frac{1}{4} (c + d x) \right] - \text{Sin} \left[ \frac{1}{4} (c + d x) \right] \right] +$$

$$(16 - 16 i) (a - b) (A - B) \text{Log} \left[ \text{Cos} \left[ \frac{1}{4} (c + d x) \right] + \text{Sin} \left[ \frac{1}{4} (c + d x) \right] \right] + \frac{1}{i + \sqrt{2}}$$

$$(4 + 4 i) (-2 i + \sqrt{2}) (2 A b + 2 a B - b B) \text{Log} \left[ \sqrt{2} + 2 \text{Sin} \left[ \frac{1}{2} (c + d x) \right] \right] +$$

$$\frac{1}{i + \sqrt{2}} i \sqrt{2} \left( (-1 + i) + \sqrt{2} \right) \left( (3 + i) + \sqrt{2} \right) (2 A b + 2 a B - b B)$$

$$\text{Log} \left[ 2 - \sqrt{2} \text{Cos} \left[ \frac{1}{2} (c + d x) \right] - \sqrt{2} \text{Sin} \left[ \frac{1}{2} (c + d x) \right] \right] + \frac{1}{i + \sqrt{2}} \sqrt{2} \left( (-3 + i) + \sqrt{2} \right)$$

$$\left. \left( (1 + i) + \sqrt{2} \right) (2 A b + 2 a B - b B) \text{Log} \left[ 2 + \sqrt{2} \text{Cos} \left[ \frac{1}{2} (c + d x) \right] - \sqrt{2} \text{Sin} \left[ \frac{1}{2} (c + d x) \right] \right] + \right.$$

$$\left. \frac{(8 - 8 i) b B}{\text{Cos} \left[ \frac{1}{2} (c + d x) \right] - \text{Sin} \left[ \frac{1}{2} (c + d x) \right]} - \frac{(8 - 8 i) b B}{\text{Cos} \left[ \frac{1}{2} (c + d x) \right] + \text{Sin} \left[ \frac{1}{2} (c + d x) \right]} \right)$$

**Problem 613: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\text{Sec}[c + d x]^{5/2} (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2)}{(a + a \text{Sec}[c + d x])^{3/2}} dx$$

Optimal (type 3, 260 leaves, 8 steps):

$$\frac{(8 A - 12 B + 19 C) \text{ArcSinh} \left[ \frac{-\sqrt{a} \text{Tan}[c + d x]}{\sqrt{a + a \text{Sec}[c + d x]}} \right]}{4 a^{3/2} d} -$$

$$\frac{(5 A - 9 B + 13 C) \text{ArcTanh} \left[ \frac{\sqrt{a} \sqrt{\text{Sec}[c + d x]} \text{Sin}[c + d x]}{\sqrt{2} \sqrt{a + a \text{Sec}[c + d x]}} \right]}{2 \sqrt{2} a^{3/2} d} - \frac{(A - B + C) \text{Sec}[c + d x]^{7/2} \text{Sin}[c + d x]}{2 d (a + a \text{Sec}[c + d x])^{3/2}} -$$

$$\frac{(2 A - 6 B + 7 C) \text{Sec}[c + d x]^{3/2} \text{Sin}[c + d x]}{4 a d \sqrt{a + a \text{Sec}[c + d x]}} + \frac{(A - B + 2 C) \text{Sec}[c + d x]^{5/2} \text{Sin}[c + d x]}{2 a d \sqrt{a + a \text{Sec}[c + d x]}}$$



Result (type 3, 1996 leaves):

$$\begin{aligned}
 & - \left( \left( \frac{1}{4} + \frac{i}{4} \right) \left( (-1 + i) + \sqrt{2} \right) \right. \\
 & \quad \left( (24 + 8i) A + 8\sqrt{2} A - (36 + 12i) B - 12\sqrt{2} B + (57 + 19i) C + 19\sqrt{2} C \right) \\
 & \quad \text{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c + dx) \right] - \sin \left[ \frac{1}{4} (c + dx) \right] - \sqrt{2} \sin \left[ \frac{1}{4} (c + dx) \right]}{-\cos \left[ \frac{1}{4} (c + dx) \right] + \sqrt{2} \cos \left[ \frac{1}{4} (c + dx) \right] - \sin \left[ \frac{1}{4} (c + dx) \right]} \right] \\
 & \quad \left. \cos \left[ \frac{1}{2} (c + dx) \right]^3 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) / \left( \sqrt{2} (i + \sqrt{2}) d \right. \\
 & \quad \left. (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sqrt{\sec [c + dx]} (a (1 + \sec [c + dx]))^{3/2} \right) - \\
 & \left( \left( \frac{1}{4} - \frac{i}{4} \right) \left( (1 + i) + \sqrt{2} \right) \left( (-24 + 8i) A + 8\sqrt{2} A + (36 - 12i) B - 12\sqrt{2} B - (57 - 19i) C + \right. \right. \\
 & \quad \left. \left. 19\sqrt{2} C \right) \text{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c + dx) \right] + \sin \left[ \frac{1}{4} (c + dx) \right] - \sqrt{2} \sin \left[ \frac{1}{4} (c + dx) \right]}{\cos \left[ \frac{1}{4} (c + dx) \right] + \sqrt{2} \cos \left[ \frac{1}{4} (c + dx) \right] - \sin \left[ \frac{1}{4} (c + dx) \right]} \right] \right. \\
 & \quad \left. \cos \left[ \frac{1}{2} (c + dx) \right]^3 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) / \\
 & \quad \left( \sqrt{2} (i + \sqrt{2}) d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \right. \\
 & \quad \left. \sqrt{\sec [c + dx]} (a (1 + \sec [c + dx]))^{3/2} \right) + \\
 & \left( 2 (5A - 9B + 13C) \cos \left[ \frac{1}{2} (c + dx) \right]^3 \log \left[ \cos \left[ \frac{1}{4} (c + dx) \right] - \sin \left[ \frac{1}{4} (c + dx) \right] \right] \right. \\
 & \quad \left. (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) / \\
 & \quad \left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sqrt{\sec [c + dx]} (a (1 + \sec [c + dx]))^{3/2} \right) - \\
 & \left( 2 (5A - 9B + 13C) \cos \left[ \frac{1}{2} (c + dx) \right]^3 \log \left[ \cos \left[ \frac{1}{4} (c + dx) \right] + \sin \left[ \frac{1}{4} (c + dx) \right] \right] \right. \\
 & \quad \left. (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) / \\
 & \quad \left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sqrt{\sec [c + dx]} (a (1 + \sec [c + dx]))^{3/2} \right) + \\
 & \left( (16A + 8i\sqrt{2}A - 24B - 12i\sqrt{2}B + 38C + 19i\sqrt{2}C) \cos \left[ \frac{1}{2} (c + dx) \right]^3 \right. \\
 & \quad \left. \log \left[ \sqrt{2} + 2 \sin \left[ \frac{1}{2} (c + dx) \right] \right] (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) / \\
 & \left( 2 (i + \sqrt{2}) d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sqrt{\sec [c + dx]} \right. \\
 & \quad \left. (a (1 + \sec [c + dx]))^{3/2} \right) - \left( \left( \frac{1}{8} - \frac{i}{8} \right) \left( (-1 + i) + \sqrt{2} \right) \right. \\
 & \quad \left. \left( (24 + 8i) A + 8\sqrt{2} A - (36 + 12i) B - 12\sqrt{2} B + (57 + 19i) C + 19\sqrt{2} C \right) \cos \left[ \frac{1}{2} (c + dx) \right]^3 \right)
 \end{aligned}$$

$$\begin{aligned}
& \left( \text{Log}\left[2 - \sqrt{2} \cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{2}(c+dx)\right]\right] (A+B \sec[c+dx] + C \sec[c+dx]^2) \right) / \\
& \left( \sqrt{2} (i + \sqrt{2}) d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \sqrt{\sec[c+dx]} \right. \\
& \left. (a(1+\sec[c+dx]))^{3/2} + \left(\left(\frac{1}{8} + \frac{i}{8}\right) ((1+i) + \sqrt{2})\right) \right. \\
& \left. \left( (-24+8i)A + 8\sqrt{2}A + (36-12i)B - 12\sqrt{2}B - (57-19i)C + 19\sqrt{2}C \right) \cos\left[\frac{1}{2}(c+dx)\right]^3 \right. \\
& \left. \text{Log}\left[2 + \sqrt{2} \cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{2}(c+dx)\right]\right] (A+B \sec[c+dx] + C \sec[c+dx]^2) \right) / \\
& \left( \sqrt{2} (i + \sqrt{2}) d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \sqrt{\sec[c+dx]} \right. \\
& \left. \sqrt{\sec[c+dx]} (a(1+\sec[c+dx]))^{3/2} + \right. \\
& \left. \left( (-A+B-C) \cos\left[\frac{1}{2}(c+dx)\right]^3 (A+B \sec[c+dx] + C \sec[c+dx]^2) \right) / \right. \\
& \left. \left( d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \sqrt{\sec[c+dx]} \right. \right. \\
& \left. \left. (a(1+\sec[c+dx]))^{3/2} \left( \cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right] \right)^2 \right) + \right. \\
& \left. \left( (A-B+C) \cos\left[\frac{1}{2}(c+dx)\right]^3 (A+B \sec[c+dx] + C \sec[c+dx]^2) \right) / \right. \\
& \left. \left( d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \sqrt{\sec[c+dx]} \right. \right. \\
& \left. \left. (a(1+\sec[c+dx]))^{3/2} \left( \cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right] \right)^2 \right) + \right. \\
& \left. \left( (4B-5C) \cos\left[\frac{1}{2}(c+dx)\right]^3 (A+B \sec[c+dx] + C \sec[c+dx]^2) \right) / \right. \\
& \left. \left( d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \sqrt{\sec[c+dx]} \right. \right. \\
& \left. \left. (a(1+\sec[c+dx]))^{3/2} \left( \cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) + \right. \\
& \left. \left( 2C \cos\left[\frac{1}{2}(c+dx)\right]^3 (A+B \sec[c+dx] + C \sec[c+dx]^2) \sin\left[\frac{1}{2}(c+dx)\right] \right) / \right. \\
& \left. \left( d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \sqrt{\sec[c+dx]} \right. \right. \\
& \left. \left. (a(1+\sec[c+dx]))^{3/2} \left( \cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right] \right)^2 \right) + \right. \\
& \left. \left( 2C \cos\left[\frac{1}{2}(c+dx)\right]^3 (A+B \sec[c+dx] + C \sec[c+dx]^2) \sin\left[\frac{1}{2}(c+dx)\right] \right) / \right. \\
& \left. \left( d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \sqrt{\sec[c+dx]} \right. \right. \\
& \left. \left. (a(1+\sec[c+dx]))^{3/2} \left( \cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^2 \right) + \right. \\
& \left. \left( (-4B+5C) \cos\left[\frac{1}{2}(c+dx)\right]^3 (A+B \sec[c+dx] + C \sec[c+dx]^2) \right) / \right. \\
& \left. \left( d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \sqrt{\sec[c+dx]} \right) \right)
\end{aligned}$$

$$\left( a \left( 1 + \sec [c + d x] \right) \right)^{3/2} \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)$$

**Problem 614: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c + d x]^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2)}{(a + a \sec [c + d x])^{3/2}} dx$$

Optimal (type 3, 202 leaves, 7 steps):

$$\frac{(2 B - 3 C) \operatorname{ArcSinh} \left[ \frac{\sqrt{a} \operatorname{Tan}[c + d x]}{\sqrt{a + a \sec [c + d x]}} \right]}{a^{3/2} d} + \frac{(A - 5 B + 9 C) \operatorname{ArcTanh} \left[ \frac{\sqrt{a} \sqrt{\sec [c + d x]} \operatorname{Sin}[c + d x]}{\sqrt{2} \sqrt{a + a \sec [c + d x]}} \right]}{2 \sqrt{2} a^{3/2} d} -$$

$$\frac{(A - B + C) \sec [c + d x]^{5/2} \operatorname{Sin}[c + d x]}{2 d (a + a \sec [c + d x])^{3/2}} + \frac{(A - B + 3 C) \sec [c + d x]^{3/2} \operatorname{Sin}[c + d x]}{2 a d \sqrt{a + a \sec [c + d x]}}$$

Result (type 3, 1669 leaves):

$$- \left( \left( (1 - i) \left( (1 + i) - i \sqrt{2} \right) \left( (-6 - 2 i) B - 2 \sqrt{2} B + (9 + 3 i) C + 3 \sqrt{2} C \right) \right. \right.$$

$$\operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{4} (c + d x) \right]}{-\cos \left[ \frac{1}{4} (c + d x) \right] + \sqrt{2} \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right]} \right]$$

$$\left. \cos \left[ \frac{1}{2} (c + d x) \right]^3 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \left( \sqrt{2} (i + \sqrt{2}) d \right.$$

$$\left. \left. (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{\sec [c + d x]} (a (1 + \sec [c + d x]))^{3/2} \right) \right) +$$

$$\left( (1 - i) \left( (1 + i) + \sqrt{2} \right) \left( (6 - 2 i) B - 2 \sqrt{2} B - (9 - 3 i) C + 3 \sqrt{2} C \right) \right.$$

$$\operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c + d x) \right] + \sin \left[ \frac{1}{4} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{4} (c + d x) \right]}{\cos \left[ \frac{1}{4} (c + d x) \right] + \sqrt{2} \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right]} \right]$$

$$\left. \cos \left[ \frac{1}{2} (c + d x) \right]^3 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) /$$

$$\left( \sqrt{2} (i + \sqrt{2}) d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right.$$

$$\left. \sqrt{\sec [c + d x]} (a (1 + \sec [c + d x]))^{3/2} \right) -$$

$$\left( 2 (A - 5 B + 9 C) \cos \left[ \frac{1}{2} (c + d x) \right]^3 \operatorname{Log} \left[ \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right] \right] \right.$$

$$\left. \left. (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) \right) /$$

$$\begin{aligned}
& \left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sqrt{\sec [c + dx]} (a (1 + \sec [c + dx]))^{3/2} + \right. \\
& \left. \left( 2 (A - 5B + 9C) \cos \left[ \frac{1}{2} (c + dx) \right]^3 \log \left[ \cos \left[ \frac{1}{4} (c + dx) \right] + \sin \left[ \frac{1}{4} (c + dx) \right] \right] \right. \right. \\
& \left. \left. (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) \right) / \\
& \left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sqrt{\sec [c + dx]} (a (1 + \sec [c + dx]))^{3/2} + \right. \\
& \left. \left( 2 (4B + 2i\sqrt{2}B - 6C - 3i\sqrt{2}C) \cos \left[ \frac{1}{2} (c + dx) \right]^3 \log \left[ \sqrt{2} + 2 \sin \left[ \frac{1}{2} (c + dx) \right] \right] \right. \right. \\
& \left. \left. (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) \right) / \left( (i + \sqrt{2}) d \right. \\
& \left. (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sqrt{\sec [c + dx]} (a (1 + \sec [c + dx]))^{3/2} + \right. \\
& \left. \left( \left( \frac{1}{2} + \frac{i}{2} \right) \left( (1 + i) - i\sqrt{2} \right) \left( (-6 - 2i)B - 2\sqrt{2}B + (9 + 3i)C + 3\sqrt{2}C \right) \cos \left[ \frac{1}{2} (c + dx) \right]^3 \right. \right. \\
& \left. \left. \log \left[ 2 - \sqrt{2} \cos \left[ \frac{1}{2} (c + dx) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c + dx) \right] \right] (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) \right) / \\
& \left( \sqrt{2} (i + \sqrt{2}) d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \right. \\
& \left. \sqrt{\sec [c + dx]} (a (1 + \sec [c + dx]))^{3/2} - \right. \\
& \left. \left( \left( \frac{1}{2} + \frac{i}{2} \right) \left( (1 + i) + \sqrt{2} \right) \left( (6 - 2i)B - 2\sqrt{2}B - (9 - 3i)C + 3\sqrt{2}C \right) \cos \left[ \frac{1}{2} (c + dx) \right]^3 \right. \right. \\
& \left. \left. \log \left[ 2 + \sqrt{2} \cos \left[ \frac{1}{2} (c + dx) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c + dx) \right] \right] (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) \right) / \\
& \left( \sqrt{2} (i + \sqrt{2}) d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \right. \\
& \left. \sqrt{\sec [c + dx]} (a (1 + \sec [c + dx]))^{3/2} + \right. \\
& \left. \left( (A - B + C) \cos \left[ \frac{1}{2} (c + dx) \right]^3 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) \right) / \\
& \left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sqrt{\sec [c + dx]} \right. \\
& \left. (a (1 + \sec [c + dx]))^{3/2} \left( \cos \left[ \frac{1}{4} (c + dx) \right] - \sin \left[ \frac{1}{4} (c + dx) \right] \right)^2 \right) + \\
& \left( (-A + B - C) \cos \left[ \frac{1}{2} (c + dx) \right]^3 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) / \\
& \left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sqrt{\sec [c + dx]} \right. \\
& \left. (a (1 + \sec [c + dx]))^{3/2} \left( \cos \left[ \frac{1}{4} (c + dx) \right] + \sin \left[ \frac{1}{4} (c + dx) \right] \right)^2 \right) + \\
& \left( 4C \cos \left[ \frac{1}{2} (c + dx) \right]^3 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) / \\
& \left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sqrt{\sec [c + dx]} \right. \\
& \left. (a (1 + \sec [c + dx]))^{3/2} \left( \cos \left[ \frac{1}{2} (c + dx) \right] - \sin \left[ \frac{1}{2} (c + dx) \right] \right) \right) - \\
& \left( 4C \cos \left[ \frac{1}{2} (c + dx) \right]^3 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) / \\
& \left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sqrt{\sec [c + dx]} \right.
\end{aligned}$$

$$\left( a \left( 1 + \sec [c + d x] \right) \right)^{3/2} \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)$$

**Problem 615: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2)}{(a + a \sec [c + d x])^{3/2}} dx$$

Optimal (type 3, 149 leaves, 6 steps):

$$\frac{2 C \operatorname{ArcSinh} \left[ \frac{\sqrt{a} \tan [c + d x]}{\sqrt{a + a \sec [c + d x]}} \right]}{a^{3/2} d} + \frac{(3 A + B - 5 C) \operatorname{ArcTanh} \left[ \frac{\sqrt{a} \sqrt{\sec [c + d x]} \sin [c + d x]}{\sqrt{2} \sqrt{a + a \sec [c + d x]}} \right]}{2 \sqrt{2} a^{3/2} d} - \frac{(A - B + C) \sec [c + d x]^{3/2} \sin [c + d x]}{2 d (a + a \sec [c + d x])^{3/2}}$$

Result (type 3, 1259 leaves):

$$\begin{aligned} & - \left( \left( 2 \left( (-1 + i) + \sqrt{2} \right) \left( (1 + i) + \sqrt{2} \right) C \right. \right. \\ & \quad \operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{4} (c + d x) \right]}{-\cos \left[ \frac{1}{4} (c + d x) \right] + \sqrt{2} \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right]} \right] \\ & \quad \left. \cos \left[ \frac{1}{2} (c + d x) \right]^3 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \\ & \quad \left( d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{\sec [c + d x]} (a (1 + \sec [c + d x]))^{3/2} \right) - \\ & \left( 2 \left( (-1 + i) + \sqrt{2} \right) \left( (1 + i) + \sqrt{2} \right) C \right. \\ & \quad \operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c + d x) \right] + \sin \left[ \frac{1}{4} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{4} (c + d x) \right]}{\cos \left[ \frac{1}{4} (c + d x) \right] + \sqrt{2} \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right]} \right] \\ & \quad \left. \cos \left[ \frac{1}{2} (c + d x) \right]^3 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \\ & \quad \left( d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{\sec [c + d x]} (a (1 + \sec [c + d x]))^{3/2} \right) - \\ & \quad \left( 2 (3 A + B - 5 C) \cos \left[ \frac{1}{2} (c + d x) \right]^3 \log \left[ \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right] \right] \right. \\ & \quad \left. (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \end{aligned}$$

$$\begin{aligned}
 & \left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sqrt{\sec [c + dx]} (a (1 + \sec [c + dx]))^{3/2} \right. \\
 & \left. \left( 2 (3A + B - 5C) \cos \left[ \frac{1}{2} (c + dx) \right]^3 \operatorname{Log} \left[ \cos \left[ \frac{1}{4} (c + dx) \right] + \sin \left[ \frac{1}{4} (c + dx) \right] \right] \right. \right. \\
 & \left. \left. (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) \right) / \\
 & \left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sqrt{\sec [c + dx]} (a (1 + \sec [c + dx]))^{3/2} \right. \\
 & \left. \left( 4 \sqrt{2} C \cos \left[ \frac{1}{2} (c + dx) \right]^3 \operatorname{Log} \left[ \sqrt{2} + 2 \sin \left[ \frac{1}{2} (c + dx) \right] \right] (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) \right) / \\
 & \left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sqrt{\sec [c + dx]} (a (1 + \sec [c + dx]))^{3/2} \right. \\
 & \left. \left( i \left( (-1 + i) + \sqrt{2} \right) \left( (1 + i) + \sqrt{2} \right) C \cos \left[ \frac{1}{2} (c + dx) \right]^3 \right. \right. \\
 & \left. \left. \operatorname{Log} \left[ 2 - \sqrt{2} \cos \left[ \frac{1}{2} (c + dx) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c + dx) \right] \right] (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) \right) / \\
 & \left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sqrt{\sec [c + dx]} (a (1 + \sec [c + dx]))^{3/2} \right. \\
 & \left. \left( i \left( (-1 + i) + \sqrt{2} \right) \left( (1 + i) + \sqrt{2} \right) C \cos \left[ \frac{1}{2} (c + dx) \right]^3 \right. \right. \\
 & \left. \left. \operatorname{Log} \left[ 2 + \sqrt{2} \cos \left[ \frac{1}{2} (c + dx) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c + dx) \right] \right] (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) \right) / \\
 & \left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sqrt{\sec [c + dx]} (a (1 + \sec [c + dx]))^{3/2} \right. \\
 & \left. \left( (-A + B - C) \cos \left[ \frac{1}{2} (c + dx) \right]^3 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) \right) / \\
 & \left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sqrt{\sec [c + dx]} \right. \\
 & \left. (a (1 + \sec [c + dx]))^{3/2} \left( \cos \left[ \frac{1}{4} (c + dx) \right] - \sin \left[ \frac{1}{4} (c + dx) \right] \right)^2 \right) + \\
 & \left( (A - B + C) \cos \left[ \frac{1}{2} (c + dx) \right]^3 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right) / \\
 & \left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sqrt{\sec [c + dx]} \right. \\
 & \left. (a (1 + \sec [c + dx]))^{3/2} \left( \cos \left[ \frac{1}{4} (c + dx) \right] + \sin \left[ \frac{1}{4} (c + dx) \right] \right)^2 \right)
 \end{aligned}$$

**Problem 616: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec [c + dx] + C \sec [c + dx]^2}{\sqrt{\sec [c + dx]} (a + a \sec [c + dx])^{3/2}} dx$$

Optimal (type 3, 161 leaves, 4 steps):

$$\begin{aligned}
 & \frac{(7A - 3B - C) \operatorname{ArcTanh} \left[ \frac{\sqrt{a} \sqrt{\sec [c + dx]} \sin [c + dx]}{\sqrt{2} \sqrt{a + a \sec [c + dx]}} \right]}{2 \sqrt{2} a^{3/2} d} \\
 & + \frac{(A - B + C) \sqrt{\sec [c + dx]} \sin [c + dx]}{2 d (a + a \sec [c + dx])^{3/2}} + \frac{(5A - B + C) \sqrt{\sec [c + dx]} \sin [c + dx]}{2 a d \sqrt{a + a \sec [c + dx]}}
 \end{aligned}$$

Result (type 3, 578 leaves):

$$\begin{aligned}
 & \left( 2 (7A - 3B - C) \cos\left[\frac{1}{2}(c + dx)\right]^3 \right. \\
 & \quad \left. \log\left[\cos\left[\frac{1}{4}(c + dx)\right] - \sin\left[\frac{1}{4}(c + dx)\right]\right] (A + B \sec[c + dx] + C \sec[c + dx]^2)\right) / \\
 & \left( d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{\sec[c + dx]} (a (1 + \sec[c + dx]))^{3/2} \right) - \\
 & \left( 2 (7A - 3B - C) \cos\left[\frac{1}{2}(c + dx)\right]^3 \log\left[\cos\left[\frac{1}{4}(c + dx)\right] + \sin\left[\frac{1}{4}(c + dx)\right]\right] \right. \\
 & \quad \left. (A + B \sec[c + dx] + C \sec[c + dx]^2)\right) / \\
 & \left( d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{\sec[c + dx]} (a (1 + \sec[c + dx]))^{3/2} \right) + \\
 & \left( (A - B + C) \cos\left[\frac{1}{2}(c + dx)\right]^3 (A + B \sec[c + dx] + C \sec[c + dx]^2)\right) / \\
 & \left( d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{\sec[c + dx]} \right. \\
 & \quad \left. (a (1 + \sec[c + dx]))^{3/2} \left( \cos\left[\frac{1}{4}(c + dx)\right] - \sin\left[\frac{1}{4}(c + dx)\right] \right)^2 \right) + \\
 & \left( (-A + B - C) \cos\left[\frac{1}{2}(c + dx)\right]^3 (A + B \sec[c + dx] + C \sec[c + dx]^2)\right) / \\
 & \left( d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{\sec[c + dx]} \right. \\
 & \quad \left. (a (1 + \sec[c + dx]))^{3/2} \left( \cos\left[\frac{1}{4}(c + dx)\right] + \sin\left[\frac{1}{4}(c + dx)\right] \right)^2 \right) + \\
 & \left( 16A \cos\left[\frac{1}{2}(c + dx)\right]^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) \sin\left[\frac{1}{2}(c + dx)\right] \right) / \\
 & \left( d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{\sec[c + dx]} (a (1 + \sec[c + dx]))^{3/2} \right)
 \end{aligned}$$

**Problem 619: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\sec[c + dx]^{5/2} (A + B \sec[c + dx] + C \sec[c + dx]^2)}{(a + a \sec[c + dx])^{5/2}} dx$$

Optimal (type 3, 254 leaves, 8 steps):

$$\begin{aligned}
 & \frac{(2B - 5C) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan[c + dx]}{\sqrt{a + a \sec[c + dx]}}\right]}{a^{5/2} d} + \\
 & \frac{(3A - 43B + 115C) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\sec[c + dx]} \sin[c + dx]}{\sqrt{2} \sqrt{a + a \sec[c + dx]}}\right]}{16 \sqrt{2} a^{5/2} d} - \frac{(A - B + C) \sec[c + dx]^{7/2} \sin[c + dx]}{4 d (a + a \sec[c + dx])^{5/2}} + \\
 & \frac{(A + 7B - 15C) \sec[c + dx]^{5/2} \sin[c + dx]}{16 a d (a + a \sec[c + dx])^{3/2}} + \frac{(3A - 11B + 35C) \sec[c + dx]^{3/2} \sin[c + dx]}{16 a^2 d \sqrt{a + a \sec[c + dx]}}
 \end{aligned}$$

Result (type 3, 1923 leaves):

$$\begin{aligned}
 & - \left( \left( (1-i) \sqrt{2} \left( (1+i) - i \sqrt{2} \right) \left( (-6-2i) B - 2\sqrt{2} B + (15+5i) C + 5\sqrt{2} C \right) \right. \right. \\
 & \quad \text{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c+dx) \right] - \sin \left[ \frac{1}{4} (c+dx) \right] - \sqrt{2} \sin \left[ \frac{1}{4} (c+dx) \right]}{-\cos \left[ \frac{1}{4} (c+dx) \right] + \sqrt{2} \cos \left[ \frac{1}{4} (c+dx) \right] - \sin \left[ \frac{1}{4} (c+dx) \right]} \right] \\
 & \quad \left. \cos \left[ \frac{1}{2} (c+dx) \right]^5 \sqrt{\sec [c+dx]} (A+B \sec [c+dx] + C \sec [c+dx]^2) \right) / \\
 & \quad \left. \left( (i+\sqrt{2}) d (A+2C+2B \cos [c+dx] + A \cos [2c+2dx]) (a(1+\sec [c+dx]))^{5/2} \right) \right) + \\
 & \left( (1-i) \sqrt{2} \left( (1+i) + \sqrt{2} \right) \left( (6-2i) B - 2\sqrt{2} B - (15-5i) C + 5\sqrt{2} C \right) \right. \\
 & \quad \text{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c+dx) \right] + \sin \left[ \frac{1}{4} (c+dx) \right] - \sqrt{2} \sin \left[ \frac{1}{4} (c+dx) \right]}{\cos \left[ \frac{1}{4} (c+dx) \right] + \sqrt{2} \cos \left[ \frac{1}{4} (c+dx) \right] - \sin \left[ \frac{1}{4} (c+dx) \right]} \right] \\
 & \quad \left. \cos \left[ \frac{1}{2} (c+dx) \right]^5 \sqrt{\sec [c+dx]} (A+B \sec [c+dx] + C \sec [c+dx]^2) \right) / \\
 & \quad \left( (i+\sqrt{2}) d (A+2C+2B \cos [c+dx] + A \cos [2c+2dx]) (a(1+\sec [c+dx]))^{5/2} \right) + \\
 & \quad \left( (-3A+43B-115C) \cos \left[ \frac{1}{2} (c+dx) \right]^5 \log \left[ \cos \left[ \frac{1}{4} (c+dx) \right] - \sin \left[ \frac{1}{4} (c+dx) \right] \right] \right. \\
 & \quad \left. \sqrt{\sec [c+dx]} (A+B \sec [c+dx] + C \sec [c+dx]^2) \right) / \\
 & \quad \left( 2d (A+2C+2B \cos [c+dx] + A \cos [2c+2dx]) (a(1+\sec [c+dx]))^{5/2} \right) + \\
 & \quad \left( (3A-43B+115C) \cos \left[ \frac{1}{2} (c+dx) \right]^5 \log \left[ \cos \left[ \frac{1}{4} (c+dx) \right] + \sin \left[ \frac{1}{4} (c+dx) \right] \right] \right. \\
 & \quad \left. \sqrt{\sec [c+dx]} (A+B \sec [c+dx] + C \sec [c+dx]^2) \right) / \\
 & \quad \left( 2d (A+2C+2B \cos [c+dx] + A \cos [2c+2dx]) (a(1+\sec [c+dx]))^{5/2} \right) + \\
 & \quad \left( 4(4B+2i\sqrt{2}B-10C-5i\sqrt{2}C) \cos \left[ \frac{1}{2} (c+dx) \right]^5 \log \left[ \sqrt{2} + 2 \sin \left[ \frac{1}{2} (c+dx) \right] \right] \right. \\
 & \quad \left. \sqrt{\sec [c+dx]} (A+B \sec [c+dx] + C \sec [c+dx]^2) \right) / \\
 & \quad \left( (i+\sqrt{2}) d (A+2C+2B \cos [c+dx] + A \cos [2c+2dx]) (a(1+\sec [c+dx]))^{5/2} \right) + \\
 & \quad \left( (1+i) \left( (1+i) - i \sqrt{2} \right) \left( (-6-2i) B - 2\sqrt{2} B + (15+5i) C + 5\sqrt{2} C \right) \right. \\
 & \quad \left. \cos \left[ \frac{1}{2} (c+dx) \right]^5 \log \left[ 2 - \sqrt{2} \cos \left[ \frac{1}{2} (c+dx) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c+dx) \right] \right] \right. \\
 & \quad \left. \sqrt{\sec [c+dx]} (A+B \sec [c+dx] + C \sec [c+dx]^2) \right) /
 \end{aligned}$$



$$\begin{aligned}
 & \left( \sqrt{2} \left( i + \sqrt{2} \right) d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \left( a \left( 1 + \sec [c + d x] \right) \right)^{5/2} \right) - \\
 & \left( (1 + i) \left( (1 + i) + \sqrt{2} \right) \left( (6 - 2 i) B - 2 \sqrt{2} B - (15 - 5 i) C + 5 \sqrt{2} C \right) \right. \\
 & \quad \left. \cos \left[ \frac{1}{2} (c + d x) \right]^5 \log \left[ 2 + \sqrt{2} \cos \left[ \frac{1}{2} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c + d x) \right] \right] \right. \\
 & \quad \left. \sqrt{\sec [c + d x]} \left( A + B \sec [c + d x] + C \sec [c + d x]^2 \right) \right) / \\
 & \left( \sqrt{2} \left( i + \sqrt{2} \right) d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \left( a \left( 1 + \sec [c + d x] \right) \right)^{5/2} \right) + \\
 & \left( (A - B + C) \cos \left[ \frac{1}{2} (c + d x) \right]^5 \sqrt{\sec [c + d x]} \left( A + B \sec [c + d x] + C \sec [c + d x]^2 \right) \right) / \\
 & \left( 4 d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \right. \\
 & \quad \left. \left( a \left( 1 + \sec [c + d x] \right) \right)^{5/2} \left( \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right] \right)^4 \right) + \\
 & \left( (3 A - 11 B + 19 C) \cos \left[ \frac{1}{2} (c + d x) \right]^5 \sqrt{\sec [c + d x]} \left( A + B \sec [c + d x] + C \sec [c + d x]^2 \right) \right) / \\
 & \left( 4 d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \right. \\
 & \quad \left. \left( a \left( 1 + \sec [c + d x] \right) \right)^{5/2} \left( \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right] \right)^2 \right) + \\
 & \left( (-A + B - C) \cos \left[ \frac{1}{2} (c + d x) \right]^5 \sqrt{\sec [c + d x]} \left( A + B \sec [c + d x] + C \sec [c + d x]^2 \right) \right) / \\
 & \left( 4 d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \right. \\
 & \quad \left. \left( a \left( 1 + \sec [c + d x] \right) \right)^{5/2} \left( \cos \left[ \frac{1}{4} (c + d x) \right] + \sin \left[ \frac{1}{4} (c + d x) \right] \right)^4 \right) + \\
 & \left( (-3 A + 11 B - 19 C) \cos \left[ \frac{1}{2} (c + d x) \right]^5 \sqrt{\sec [c + d x]} \left( A + B \sec [c + d x] + C \sec [c + d x]^2 \right) \right) / \\
 & \left( 4 d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \right. \\
 & \quad \left. \left( a \left( 1 + \sec [c + d x] \right) \right)^{5/2} \left( \cos \left[ \frac{1}{4} (c + d x) \right] + \sin \left[ \frac{1}{4} (c + d x) \right] \right)^2 \right) + \\
 & \left( 8 C \cos \left[ \frac{1}{2} (c + d x) \right]^5 \sqrt{\sec [c + d x]} \left( A + B \sec [c + d x] + C \sec [c + d x]^2 \right) \right) / \\
 & \left( d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \right. \\
 & \quad \left. \left( a \left( 1 + \sec [c + d x] \right) \right)^{5/2} \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) - \\
 & \left( 8 C \cos \left[ \frac{1}{2} (c + d x) \right]^5 \sqrt{\sec [c + d x]} \left( A + B \sec [c + d x] + C \sec [c + d x]^2 \right) \right) / \\
 & \left( d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \right. \\
 & \quad \left. \left( a \left( 1 + \sec [c + d x] \right) \right)^{5/2} \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right)
 \end{aligned}$$

**Problem 620: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\text{Sec}[c + dx]^{3/2} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2)}{(a + a \text{Sec}[c + dx])^{5/2}} dx$$

Optimal (type 3, 201 leaves, 7 steps):

$$\frac{2 C \text{ArcSinh}\left[\frac{\sqrt{a} \text{Tan}[c+dx]}{\sqrt{a+a \text{Sec}[c+dx]}}\right]}{a^{5/2} d} + \frac{(5 A + 3 B - 43 C) \text{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\text{Sec}[c+dx]} \text{Sin}[c+dx]}{\sqrt{2} \sqrt{a+a \text{Sec}[c+dx]}}\right]}{16 \sqrt{2} a^{5/2} d} - \frac{(A - B + C) \text{Sec}[c + dx]^{5/2} \text{Sin}[c + dx]}{4 d (a + a \text{Sec}[c + dx])^{5/2}} + \frac{(5 A + 3 B - 11 C) \text{Sec}[c + dx]^{3/2} \text{Sin}[c + dx]}{16 a d (a + a \text{Sec}[c + dx])^{3/2}}$$

Result (type 3, 1521 leaves):

$$\begin{aligned} & - \left( \left( 4 \left( (-1 + i) + \sqrt{2} \right) \left( (1 + i) + \sqrt{2} \right) C \right. \right. \\ & \quad \left. \left. \text{ArcTan}\left[ \frac{\text{Cos}\left[\frac{1}{4}(c + dx)\right] - \text{Sin}\left[\frac{1}{4}(c + dx)\right] - \sqrt{2} \text{Sin}\left[\frac{1}{4}(c + dx)\right]}{-\text{Cos}\left[\frac{1}{4}(c + dx)\right] + \sqrt{2} \text{Cos}\left[\frac{1}{4}(c + dx)\right] - \text{Sin}\left[\frac{1}{4}(c + dx)\right]} \right] \right. \right. \\ & \quad \left. \left. \text{Cos}\left[\frac{1}{2}(c + dx)\right]^5 \sqrt{\text{Sec}[c + dx]} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \right) \right) / \\ & \quad \left( d (A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2 c + 2 d x]) (a (1 + \text{Sec}[c + dx]))^{5/2} \right) - \\ & \left( 4 \left( (-1 + i) + \sqrt{2} \right) \left( (1 + i) + \sqrt{2} \right) C \right. \\ & \quad \left. \text{ArcTan}\left[ \frac{\text{Cos}\left[\frac{1}{4}(c + dx)\right] + \text{Sin}\left[\frac{1}{4}(c + dx)\right] - \sqrt{2} \text{Sin}\left[\frac{1}{4}(c + dx)\right]}{\text{Cos}\left[\frac{1}{4}(c + dx)\right] + \sqrt{2} \text{Cos}\left[\frac{1}{4}(c + dx)\right] - \text{Sin}\left[\frac{1}{4}(c + dx)\right]} \right] \right. \\ & \quad \left. \text{Cos}\left[\frac{1}{2}(c + dx)\right]^5 \sqrt{\text{Sec}[c + dx]} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \right) / \\ & \quad \left( d (A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2 c + 2 d x]) (a (1 + \text{Sec}[c + dx]))^{5/2} \right) + \\ & \quad \left( (-5 A - 3 B + 43 C) \text{Cos}\left[\frac{1}{2}(c + dx)\right]^5 \text{Log}\left[\text{Cos}\left[\frac{1}{4}(c + dx)\right] - \text{Sin}\left[\frac{1}{4}(c + dx)\right] \right] \right. \\ & \quad \left. \sqrt{\text{Sec}[c + dx]} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \right) / \\ & \quad \left( 2 d (A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2 c + 2 d x]) (a (1 + \text{Sec}[c + dx]))^{5/2} \right) + \\ & \quad \left( (5 A + 3 B - 43 C) \text{Cos}\left[\frac{1}{2}(c + dx)\right]^5 \text{Log}\left[\text{Cos}\left[\frac{1}{4}(c + dx)\right] + \text{Sin}\left[\frac{1}{4}(c + dx)\right] \right] \right) \end{aligned}$$

$$\begin{aligned}
 & \left. \sqrt{\sec [c+d x]} \left( A+B \sec [c+d x]+C \sec [c+d x]^2 \right) \right) / \\
 & \left( 2 d \left( A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x] \right) \left( a \left( 1+\sec [c+d x] \right) \right)^{5 / 2} \right) + \\
 & \left( 8 \sqrt{2} C \cos \left[ \frac{1}{2}(c+d x) \right]^5 \operatorname{Log} \left[ \sqrt{2}+2 \sin \left[ \frac{1}{2}(c+d x) \right] \right] \right. \\
 & \left. \sqrt{\sec [c+d x]} \left( A+B \sec [c+d x]+C \sec [c+d x]^2 \right) \right) / \\
 & \left( d \left( A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x] \right) \left( a \left( 1+\sec [c+d x] \right) \right)^{5 / 2} \right) + \\
 & \left( 2 i \left( (-1+i)+\sqrt{2} \right) \left( (1+i)+\sqrt{2} \right) C \cos \left[ \frac{1}{2}(c+d x) \right]^5 \right. \\
 & \left. \operatorname{Log} \left[ 2-\sqrt{2} \cos \left[ \frac{1}{2}(c+d x) \right]-\sqrt{2} \sin \left[ \frac{1}{2}(c+d x) \right] \right] \right. \\
 & \left. \sqrt{\sec [c+d x]} \left( A+B \sec [c+d x]+C \sec [c+d x]^2 \right) \right) / \\
 & \left( d \left( A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x] \right) \left( a \left( 1+\sec [c+d x] \right) \right)^{5 / 2} \right) + \\
 & \left( 2 i \left( (-1+i)+\sqrt{2} \right) \left( (1+i)+\sqrt{2} \right) C \cos \left[ \frac{1}{2}(c+d x) \right]^5 \right. \\
 & \left. \operatorname{Log} \left[ 2+\sqrt{2} \cos \left[ \frac{1}{2}(c+d x) \right]-\sqrt{2} \sin \left[ \frac{1}{2}(c+d x) \right] \right] \right. \\
 & \left. \sqrt{\sec [c+d x]} \left( A+B \sec [c+d x]+C \sec [c+d x]^2 \right) \right) / \\
 & \left( d \left( A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x] \right) \left( a \left( 1+\sec [c+d x] \right) \right)^{5 / 2} \right) + \\
 & \left( (-A+B-C) \cos \left[ \frac{1}{2}(c+d x) \right]^5 \sqrt{\sec [c+d x]} \left( A+B \sec [c+d x]+C \sec [c+d x]^2 \right) \right) / \\
 & \left( 4 d \left( A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x] \right) \right. \\
 & \left. \left( a \left( 1+\sec [c+d x] \right) \right)^{5 / 2} \left( \cos \left[ \frac{1}{4}(c+d x) \right]-\sin \left[ \frac{1}{4}(c+d x) \right] \right)^4 \right) + \\
 & \left( (5 A+3 B-11 C) \cos \left[ \frac{1}{2}(c+d x) \right]^5 \sqrt{\sec [c+d x]} \left( A+B \sec [c+d x]+C \sec [c+d x]^2 \right) \right) / \\
 & \left( 4 d \left( A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x] \right) \right. \\
 & \left. \left( a \left( 1+\sec [c+d x] \right) \right)^{5 / 2} \left( \cos \left[ \frac{1}{4}(c+d x) \right]-\sin \left[ \frac{1}{4}(c+d x) \right] \right)^2 \right) + \\
 & \left( (A-B+C) \cos \left[ \frac{1}{2}(c+d x) \right]^5 \sqrt{\sec [c+d x]} \left( A+B \sec [c+d x]+C \sec [c+d x]^2 \right) \right) / \\
 & \left( 4 d \left( A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x] \right) \right. \\
 & \left. \left( a \left( 1+\sec [c+d x] \right) \right)^{5 / 2} \left( \cos \left[ \frac{1}{4}(c+d x) \right]+\sin \left[ \frac{1}{4}(c+d x) \right] \right)^4 \right) + \\
 & \left( (-5 A-3 B+11 C) \cos \left[ \frac{1}{2}(c+d x) \right]^5 \sqrt{\sec [c+d x]} \left( A+B \sec [c+d x]+C \sec [c+d x]^2 \right) \right) / \\
 & \left( 4 d \left( A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x] \right) \right)
 \end{aligned}$$

$$\left( a \left( 1 + \operatorname{Sec}[c + d x] \right) \right)^{5/2} \left( \cos\left[ \frac{1}{4} (c + d x) \right] + \sin\left[ \frac{1}{4} (c + d x) \right] \right)^2$$

**Problem 622: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2}{\sqrt{\operatorname{Sec}[c + d x]} (a + a \operatorname{Sec}[c + d x])^{5/2}} dx$$

Optimal (type 3, 211 leaves, 5 steps):

$$\begin{aligned} & - \frac{(75 A - 19 B - 5 C) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{\sqrt{2} \sqrt{a+a \operatorname{Sec}[c+d x]}}\right]}{16 \sqrt{2} a^{5/2} d} - \frac{(A - B + C) \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{4 d (a + a \operatorname{Sec}[c + d x])^{5/2}} \\ & + \frac{(13 A - 5 B - 3 C) \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{16 a d (a + a \operatorname{Sec}[c + d x])^{3/2}} + \frac{(49 A - 9 B + C) \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{16 a^2 d \sqrt{a + a \operatorname{Sec}[c + d x]}} \end{aligned}$$

Result (type 3, 836 leaves):

$$\begin{aligned}
 & \left( (75A - 19B - 5C) \cos\left[\frac{1}{2}(c+dx)\right]^5 \log\left[\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]\right] \right. \\
 & \quad \left. \sqrt{\sec[c+dx]} (A+B \sec[c+dx] + C \sec[c+dx]^2) \right) / \\
 & \left( 2d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) (a(1+\sec[c+dx]))^{5/2} \right) + \\
 & \left( (-75A + 19B + 5C) \cos\left[\frac{1}{2}(c+dx)\right]^5 \log\left[\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right]\right] \right. \\
 & \quad \left. \sqrt{\sec[c+dx]} (A+B \sec[c+dx] + C \sec[c+dx]^2) \right) / \\
 & \left( 2d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) (a(1+\sec[c+dx]))^{5/2} \right) + \\
 & \left( (-A+B-C) \cos\left[\frac{1}{2}(c+dx)\right]^5 \sqrt{\sec[c+dx]} (A+B \sec[c+dx] + C \sec[c+dx]^2) \right) / \\
 & \left( 4d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right. \\
 & \quad \left. (a(1+\sec[c+dx]))^{5/2} \left( \cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right] \right)^4 \right) + \\
 & \left( (21A - 13B + 5C) \cos\left[\frac{1}{2}(c+dx)\right]^5 \sqrt{\sec[c+dx]} (A+B \sec[c+dx] + C \sec[c+dx]^2) \right) / \\
 & \left( 4d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right. \\
 & \quad \left. (a(1+\sec[c+dx]))^{5/2} \left( \cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right] \right)^2 \right) + \\
 & \left( (A-B+C) \cos\left[\frac{1}{2}(c+dx)\right]^5 \sqrt{\sec[c+dx]} (A+B \sec[c+dx] + C \sec[c+dx]^2) \right) / \\
 & \left( 4d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right. \\
 & \quad \left. (a(1+\sec[c+dx]))^{5/2} \left( \cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right] \right)^4 \right) + \\
 & \left( (-21A + 13B - 5C) \cos\left[\frac{1}{2}(c+dx)\right]^5 \sqrt{\sec[c+dx]} (A+B \sec[c+dx] + C \sec[c+dx]^2) \right) / \\
 & \left( 4d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right. \\
 & \quad \left. (a(1+\sec[c+dx]))^{5/2} \left( \cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right] \right)^2 \right) + \\
 & \left( 32A \cos\left[\frac{1}{2}(c+dx)\right]^5 \sqrt{\sec[c+dx]} (A+B \sec[c+dx] + C \sec[c+dx]^2) \sin\left[\frac{1}{2}(c+dx)\right] \right) / \\
 & \left( d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) (a(1+\sec[c+dx]))^{5/2} \right)
 \end{aligned}$$

**Problem 623: Result more than twice size of optimal antiderivative.**

$$\int \frac{A+B \sec[c+dx] + C \sec[c+dx]^2}{\sec[c+dx]^{3/2} (a+a \sec[c+dx])^{5/2}} dx$$

Optimal (type 3, 261 leaves, 6 steps):

$$\frac{(163 A - 75 B + 19 C) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{\sqrt{2} \sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{16 \sqrt{2} a^{5/2} d} - \frac{(A - B + C) \operatorname{Sin}[c+dx]}{4 d \sqrt{\operatorname{Sec}[c+dx]} (a + a \operatorname{Sec}[c+dx])^{5/2}} - \frac{(17 A - 9 B + C) \operatorname{Sin}[c+dx]}{16 a d \sqrt{\operatorname{Sec}[c+dx]} (a + a \operatorname{Sec}[c+dx])^{3/2}} + \frac{(95 A - 39 B + 15 C) \operatorname{Sin}[c+dx]}{48 a^2 d \sqrt{\operatorname{Sec}[c+dx]} \sqrt{a + a \operatorname{Sec}[c+dx]}} - \frac{(299 A - 147 B + 27 C) \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{48 a^2 d \sqrt{a + a \operatorname{Sec}[c+dx]}}$$

Result (type 3, 943 leaves):

$$\begin{aligned}
 & \left( (-163A + 75B - 19C) \cos\left[\frac{1}{2}(c+dx)\right]^5 \right. \\
 & \quad \left. \log\left[\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]\right] \sqrt{\sec[c+dx]} (A+B \sec[c+dx] + C \sec[c+dx]^2) \right) / \\
 & \quad \left( 2d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) (a(1+\sec[c+dx]))^{5/2} \right) + \\
 & \left( (163A - 75B + 19C) \cos\left[\frac{1}{2}(c+dx)\right]^5 \log\left[\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right]\right] \right. \\
 & \quad \left. \sqrt{\sec[c+dx]} (A+B \sec[c+dx] + C \sec[c+dx]^2) \right) / \\
 & \quad \left( 2d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) (a(1+\sec[c+dx]))^{5/2} \right) + \\
 & \left( (A-B+C) \cos\left[\frac{1}{2}(c+dx)\right]^5 \sqrt{\sec[c+dx]} (A+B \sec[c+dx] + C \sec[c+dx]^2) \right) / \\
 & \quad \left( 4d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right. \\
 & \quad \left. (a(1+\sec[c+dx]))^{5/2} \left( \cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right] \right)^4 \right) + \\
 & \left( (-29A + 21B - 13C) \cos\left[\frac{1}{2}(c+dx)\right]^5 \sqrt{\sec[c+dx]} (A+B \sec[c+dx] + C \sec[c+dx]^2) \right) / \\
 & \quad \left( 4d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right. \\
 & \quad \left. (a(1+\sec[c+dx]))^{5/2} \left( \cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right] \right)^2 \right) + \\
 & \left( (-A+B-C) \cos\left[\frac{1}{2}(c+dx)\right]^5 \sqrt{\sec[c+dx]} (A+B \sec[c+dx] + C \sec[c+dx]^2) \right) / \\
 & \quad \left( 4d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right. \\
 & \quad \left. (a(1+\sec[c+dx]))^{5/2} \left( \cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right] \right)^4 \right) + \\
 & \left( (29A - 21B + 13C) \cos\left[\frac{1}{2}(c+dx)\right]^5 \sqrt{\sec[c+dx]} (A+B \sec[c+dx] + C \sec[c+dx]^2) \right) / \\
 & \quad \left( 4d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right. \\
 & \quad \left. (a(1+\sec[c+dx]))^{5/2} \left( \cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right] \right)^2 \right) - \\
 & \left( 16(5A - 2B) \cos\left[\frac{1}{2}(c+dx)\right]^5 \sqrt{\sec[c+dx]} (A+B \sec[c+dx] + C \sec[c+dx]^2) \right. \\
 & \quad \left. \sin\left[\frac{1}{2}(c+dx)\right] \right) / \left( d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) (a(1+\sec[c+dx]))^{5/2} \right) + \\
 & \left( 16A \cos\left[\frac{1}{2}(c+dx)\right]^5 \sqrt{\sec[c+dx]} (A+B \sec[c+dx] + C \sec[c+dx]^2) \sin\left[\frac{3}{2}(c+dx)\right] \right) / \\
 & \quad \left( 3d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) (a(1+\sec[c+dx]))^{5/2} \right)
 \end{aligned}$$

**Problem 624: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2}{\operatorname{Sec}[c + d x]^{5/2} (a + a \operatorname{Sec}[c + d x])^{5/2}} dx$$

Optimal (type 3, 313 leaves, 7 steps):

$$\begin{aligned} & - \frac{(283 A - 163 B + 75 C) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{\sqrt{2} \sqrt{a+a \operatorname{Sec}[c+d x]}}\right]}{16 \sqrt{2} a^{5/2} d} - \frac{(A - B + C) \operatorname{Sin}[c + d x]}{4 d \operatorname{Sec}[c + d x]^{3/2} (a + a \operatorname{Sec}[c + d x])^{5/2}} \\ & + \frac{(21 A - 13 B + 5 C) \operatorname{Sin}[c + d x]}{16 a d \operatorname{Sec}[c + d x]^{3/2} (a + a \operatorname{Sec}[c + d x])^{3/2}} + \frac{(157 A - 85 B + 45 C) \operatorname{Sin}[c + d x]}{80 a^2 d \operatorname{Sec}[c + d x]^{3/2} \sqrt{a + a \operatorname{Sec}[c + d x]}} - \\ & + \frac{(787 A - 475 B + 195 C) \operatorname{Sin}[c + d x]}{240 a^2 d \sqrt{\operatorname{Sec}[c + d x]} \sqrt{a + a \operatorname{Sec}[c + d x]}} + \frac{(2671 A - 1495 B + 735 C) \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{240 a^2 d \sqrt{a + a \operatorname{Sec}[c + d x]}} \end{aligned}$$

Result (type 3, 1053 leaves):



$$\begin{aligned}
 & \left( (283 A - 163 B + 75 C) \cos\left[\frac{1}{2}(c+dx)\right]^5 \log\left[\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]\right] \right. \\
 & \quad \left. \sqrt{\sec[c+dx]} (A+B \sec[c+dx] + C \sec^2[c+dx]) \right) / \\
 & \left( 2d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) (a(1+\sec[c+dx]))^{5/2} \right) + \\
 & \left( (-283 A + 163 B - 75 C) \cos\left[\frac{1}{2}(c+dx)\right]^5 \log\left[\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right]\right] \right. \\
 & \quad \left. \sqrt{\sec[c+dx]} (A+B \sec[c+dx] + C \sec^2[c+dx]) \right) / \\
 & \left( 2d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) (a(1+\sec[c+dx]))^{5/2} \right) + \\
 & \left( (-A+B-C) \cos\left[\frac{1}{2}(c+dx)\right]^5 \sqrt{\sec[c+dx]} (A+B \sec[c+dx] + C \sec^2[c+dx]) \right) / \\
 & \left( 4d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right. \\
 & \quad \left. (a(1+\sec[c+dx]))^{5/2} \left( \cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right] \right)^4 \right) + \\
 & \left( (37 A - 29 B + 21 C) \cos\left[\frac{1}{2}(c+dx)\right]^5 \sqrt{\sec[c+dx]} (A+B \sec[c+dx] + C \sec^2[c+dx]) \right) / \\
 & \left( 4d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right. \\
 & \quad \left. (a(1+\sec[c+dx]))^{5/2} \left( \cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right] \right)^2 \right) + \\
 & \left( (A-B+C) \cos\left[\frac{1}{2}(c+dx)\right]^5 \sqrt{\sec[c+dx]} (A+B \sec[c+dx] + C \sec^2[c+dx]) \right) / \\
 & \left( 4d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right. \\
 & \quad \left. (a(1+\sec[c+dx]))^{5/2} \left( \cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right] \right)^4 \right) + \\
 & \left( (-37 A + 29 B - 21 C) \cos\left[\frac{1}{2}(c+dx)\right]^5 \sqrt{\sec[c+dx]} (A+B \sec[c+dx] + C \sec^2[c+dx]) \right) / \\
 & \left( 4d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right. \\
 & \quad \left. (a(1+\sec[c+dx]))^{5/2} \left( \cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right] \right)^2 \right) + \\
 & \left( 16 (10 A - 5 B + 2 C) \cos\left[\frac{1}{2}(c+dx)\right]^5 \sqrt{\sec[c+dx]} (A+B \sec[c+dx] + C \sec^2[c+dx]) \right. \\
 & \quad \left. \sin\left[\frac{1}{2}(c+dx)\right] \right) / \left( d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) (a(1+\sec[c+dx]))^{5/2} \right) - \\
 & \left( 8 (5 A - 2 B) \cos\left[\frac{1}{2}(c+dx)\right]^5 \sqrt{\sec[c+dx]} (A+B \sec[c+dx] + C \sec^2[c+dx]) \sin\left[\frac{3}{2}(c+dx)\right] \right) / \\
 & \left( 3d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) (a(1+\sec[c+dx]))^{5/2} \right) + \\
 & \left( 8 A \cos\left[\frac{1}{2}(c+dx)\right]^5 \sqrt{\sec[c+dx]} (A+B \sec[c+dx] + C \sec^2[c+dx]) \sin\left[\frac{5}{2}(c+dx)\right] \right) / \\
 & \left( 5d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) (a(1+\sec[c+dx]))^{5/2} \right)
 \end{aligned}$$

### Problem 625: Result more than twice size of optimal antiderivative.

$$\int (a + a \operatorname{Sec}[c + d x])^{2/3} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 6, 446 leaves, 10 steps):

$$\frac{3 C (a + a \operatorname{Sec}[c + d x])^{2/3} \operatorname{Tan}[c + d x]}{5 d} +$$

$$\left( 3 \sqrt{2} \operatorname{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \frac{1}{2} (1 + \operatorname{Sec}[c + d x]), 1 + \operatorname{Sec}[c + d x]\right] (a + a \operatorname{Sec}[c + d x])^{2/3} \right.$$

$$\left. \operatorname{Tan}[c + d x] \right) / \left( 7 d \sqrt{1 - \operatorname{Sec}[c + d x]} \right) + \frac{3 (5 B + 2 C) (a + a \operatorname{Sec}[c + d x])^{2/3} \operatorname{Tan}[c + d x]}{10 d (1 + \operatorname{Sec}[c + d x])} -$$

$$\left( 3^{3/4} (5 B + 2 C) \operatorname{EllipticF}\left[\operatorname{ArcCos}\left[\frac{2^{1/3} - (1 - \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}\right], \frac{1}{4} (2 + \sqrt{3})\right] \right.$$

$$\left. (a + a \operatorname{Sec}[c + d x])^{2/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3}) \right.$$

$$\left. \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \operatorname{Sec}[c + d x])^{1/3} + (1 + \operatorname{Sec}[c + d x])^{2/3}}{(2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3})^2}} \operatorname{Tan}[c + d x] \right) / \left( 10 \times 2^{1/3} d \right.$$

$$\left. (1 - \operatorname{Sec}[c + d x]) (1 + \operatorname{Sec}[c + d x]) \sqrt{-\frac{(1 + \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3})}{(2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3})^2}} \right)$$

Result (type 6, 7349 leaves):

$$\left( \operatorname{Cos}[c + d x]^2 (1 + \operatorname{Cos}[c + d x]) \operatorname{Sec}[c + d x] \right)^{2/3}$$

$$\left( (a (1 + \operatorname{Sec}[c + d x]))^{2/3} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right.$$

$$\left. \left( \frac{3}{5} \operatorname{Sec}\left[\frac{1}{2} (c + d x)\right] \left( 5 B \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right] + 2 C \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right] \right) + \frac{6}{5} C \operatorname{Tan}[c + d x] \right) \right) /$$

$$\left( d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) (1 + \operatorname{Sec}[c + d x])^{2/3} \right) +$$

$$\left( 2^{2/3} \operatorname{Cos}[c + d x]^3 \left( \operatorname{Cos}\left[\frac{1}{2} (c + d x)\right]^2 \operatorname{Sec}[c + d x] \right)^{5/3} \right.$$

$$\left. (a (1 + \operatorname{Sec}[c + d x]))^{2/3} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right.$$

$$\left. \left( A \operatorname{Cos}[c + d x] \operatorname{Sec}\left[\frac{1}{2} (c + d x)\right]^2 (1 + \operatorname{Sec}[c + d x])^{2/3} + \operatorname{Sec}\left[\frac{1}{2} (c + d x)\right]^2 \right.$$

$$\left. \left( A (1 + \operatorname{Sec}[c + d x])^{2/3} + \frac{1}{2} B (1 + \operatorname{Sec}[c + d x])^{2/3} + \frac{1}{5} C (1 + \operatorname{Sec}[c + d x])^{2/3} \right) \right)$$

$$\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right] \left( -10 (5 B + 2 C) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2, \right.$$

$$\left. -\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2 \right] \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2 \right] - \right.$$

$$\left. 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2 \right] \right) \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^4 +$$

$$\begin{aligned}
 & 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \\
 & \left(-2(20A+5B+2C)\left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \\
 & \quad \left. \left. 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + \right. \\
 & \quad \left. 5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left. \left(\left(60A+(5B+2C)\left(3+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)\right)\right)\right)\right) / \\
 & \left(5d(A+2C+2B \operatorname{Cos}[c+dx]+A \operatorname{Cos}[2c+2dx])\left(1+\operatorname{Sec}[c+dx]\right)^{2/3}\right. \\
 & \quad \left(-9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. 2\left(3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \\
 & \quad \left. \left. 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \\
 & \quad \left(-15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. 2\left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \\
 & \quad \left. \left. 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \\
 & \quad \left(\left(\operatorname{Cos}[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2\left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx]\right)^{5/3}\right.\right. \\
 & \quad \left(-10(5B+2C) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left.\left(3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\right.\right. \\
 & \quad \quad \left.\left.\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^4 + \right. \\
 & \quad \left. 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \left(-2(20A+ \right. \right. \\
 & \quad \quad \left. \left. 5B+2C)\left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \right. \\
 & \quad \quad \left. \left. 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \right. \right. \\
 & \quad \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + 5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\left(60A+(5B+2C)\left(3+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)\right)\right)\right) / \\
 & \quad \left(5 \times 2^{1/3}\left(-9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. 2\left(3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\right.\right. \right.
 \end{aligned}$$

$$\begin{aligned}
& \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \\
& \left( -15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \\
& \quad \quad \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) - \\
& \left( 2^{2/3} \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx] \right)^{5/3} \sin[c+dx] \tan\left[\frac{1}{2}(c+dx)\right] \right. \\
& \quad \left( -10(5B+2C) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \quad \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[ \right. \right. \\
& \quad \quad \quad \left. \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^4 + \\
& \quad 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left( -2(20A + \right. \right. \\
& \quad \quad \left. \left. 5B+2C) \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right)^2 - \right. \right. \\
& \quad \quad \left. \left. 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
& \quad \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 + 5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \quad \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left( 60A + (5B+2C) \left( 3 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \Bigg) \Bigg) / \\
& \left( 5 \left( -9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
& \quad 2 \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[ \right. \right. \\
& \quad \quad \left. \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \\
& \quad \left( -15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \\
& \quad \quad \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) - \\
& \left( 2^{2/3} \cos[c+dx] \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx] \right)^{5/3} \tan\left[\frac{1}{2}(c+dx)\right] \right. \\
& \quad \left( 2 \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \\
& \quad \quad \left. \left. \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[ \right. \right. \\
& \quad \quad \left. \left. \frac{1}{2}(c+dx)\right] - 9 \left( -\frac{1}{3} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right)^2 \right)
\end{aligned}$$

$$\begin{aligned}
 & \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{9} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \\
 & -\tan\left[\frac{1}{2}(c+dx)\right]^2 \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \left(3 \left(-\frac{6}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 3, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]\right)^2 \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 2, \frac{7}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]\right)^2 \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) - \\
 & 2 \left(-\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]\right)^2 \\
 & \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \operatorname{AppellF1}\left[\frac{5}{2}, \frac{8}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{2}(c+dx)\right]\right)^2 \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \Big) \\
 & \left(-10(5B+2C) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]\right)^2 \\
 & \quad \left(3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]\right)^2 - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]\right)^2 \tan\left[\frac{1}{2}(c+dx)\right]^4 + \\
 & 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]\right)^2 \left(-2(20A + \right. \\
 & \quad \left. 5B+2C) \left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]\right)^2 - \right. \\
 & \quad \left. 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]\right)^2 \right) \\
 & \quad \tan\left[\frac{1}{2}(c+dx)\right]^2 + 5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \\
 & \quad \left. -\tan\left[\frac{1}{2}(c+dx)\right]\right)^2 \left(60A + (5B+2C) \left(3 + \tan\left[\frac{1}{2}(c+dx)\right]\right)^2 \right) \Big) \Big) \Big) / \\
 & \left(5 \left(-9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]\right)^2 + \right. \\
 & \quad \left. 2 \left(3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]\right)^2 - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]\right)^2 \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Big)^2 \\
 & \left(-15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]\right)^2 + \\
 & \quad 2 \left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]\right)^2 - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]\right)^2 \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Big) - \\
 & \left(2^{2/3} \cos[c+dx] \left(\cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx]\right)^{5/3} \tan\left[\frac{1}{2}(c+dx)\right] \right)
 \end{aligned}$$

$$\begin{aligned}
& \left( 2 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \frac{5}{2}, \right. \right. \right. \\
& \quad \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} \right. \\
& \quad \left. (c+dx) \right] - 15 \left( -\frac{3}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] + \frac{2}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
& \quad \left. \left. -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] + 2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right. \\
& \quad \left. \left( 3 \left( -\frac{10}{7} \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{2}{3}, 3, \frac{9}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \right. \right. \\
& \quad \left. \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] + \frac{10}{21} \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{5}{3}, 2, \frac{9}{2}, \right. \right. \right. \\
& \quad \left. \left. \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right) \right) - \\
& \quad 2 \left( -\frac{5}{7} \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{5}{3}, 2, \frac{9}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] + \frac{25}{21} \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{8}{3}, 1, \frac{9}{2}, \operatorname{Tan} \left[ \right. \right. \right. \\
& \quad \left. \left. \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right) \Big) \Big) \\
& \left( -10 (5B + 2C) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \left( 3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \right. \right. \\
& \quad \left. \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^4 + \\
& \quad 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \left( -2 (20A + \right. \\
& \quad \left. 5B + 2C) \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] - \right. \right. \\
& \quad \left. \left. 2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \right. \\
& \quad \left. \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + 5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
& \quad \left. \left. -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \left( 60A + (5B + 2C) \left( 3 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \right) \Big) \Big) \Big) / \\
& \left( 5 \left( -9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \right. \\
& \quad \left. \left. 2 \left( 3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \right. \right. \right. \right. \\
& \quad \left. \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \\
& \quad \left( -15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right.
\end{aligned}$$

$$\begin{aligned}
 & 2 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \Bigg) + \\
 & \left( 2^{2/3} \cos [c+dx] \left( \cos \left[ \frac{1}{2} (c+dx) \right]^2 \sec [c+dx] \right)^{5/3} \tan \left[ \frac{1}{2} (c+dx) \right] \right. \\
 & \quad \left( -20 (5B+2C) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
 & \quad \left( 3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] - \right. \\
 & \quad \left. \left. 2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \right) \\
 & \quad \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right]^3 - 10 (5B+2C) \\
 & \quad \left( 3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \right. \right. \\
 & \quad \left. \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^4 \\
 & \quad \left( -\frac{3}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
 & \quad \left. \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{2}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) - 10 (5B+2C) \\
 & \quad \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \tan \left[ \frac{1}{2} (c+dx) \right]^4 \\
 & \quad \left( 3 \left( -\frac{6}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 3, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \right. \\
 & \quad \left. \left. \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{2}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, 2, \frac{7}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \Bigg) - \\
 & \quad 2 \left( -\frac{3}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
 & \quad \left. \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{8}{3}, 1, \frac{7}{2}, \tan \left[ \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \Bigg) + \\
 & \quad 9 \left( -\frac{1}{3} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
 & \quad \left. \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{2}{9} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \left( -2 (20A+5B+2C) \right. \\
 & \quad \left. \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] - \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
& \tan\left[\frac{1}{2}(c+dx)\right]^2 + 5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
& \quad \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(60A + (5B + 2C) \left(3 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) + \\
& 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
& \left(5(5B + 2C) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - 2(20A + 5B + 2C) \right. \\
& \quad \left. \left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \\
& \quad \left. \left. 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
& \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - 2(20A + 5B + 2C) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
& \quad \left. \left(3 \left(-\frac{10}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{2}{3}, 3, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \right. \\
& \quad \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{10}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, 2, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) \right) - \right. \\
& \quad \left. 2 \left(-\frac{5}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, 2, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
& \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{25}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{8}{3}, 1, \right. \right. \\
& \quad \left. \left. \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]\right)\right) + 5 \left(-\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{5} \operatorname{AppellF1}\left[\right. \right. \\
& \quad \left. \left. \frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]\right)\right) \left(60A + (5B + 2C) \left(3 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) \right) \Big/ \\
& \left(5 \left(-9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
& \quad \left. \left. 2 \left(3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\right. \right. \right. \right. \\
& \quad \left. \left. \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right. \\
& \quad \left. \left(-15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right.
\end{aligned}$$



$$\begin{aligned}
 & 2 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \Bigg) + \\
 & \left( 2^{2/3} \operatorname{Cos} [c+dx] \left( \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Sec} [c+dx] \right)^{2/3} \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right. \\
 & \quad \left( -10 (5B+2C) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
 & \quad \left( 3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \right. \right. \\
 & \quad \quad \left. \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^4 + \\
 & \quad 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \left( -2 (20A + \right. \\
 & \quad \quad 5B+2C) \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] - \right. \\
 & \quad \quad 2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \\
 & \quad \left. \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + 5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \left( 60A + (5B+2C) \left( 3 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \right) \Bigg) \\
 & \left( -\operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right] \operatorname{Sec} [c+dx] \operatorname{Sin} \left[ \frac{1}{2} (c+dx) \right] + \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right]^2 \right. \\
 & \quad \left. \operatorname{Sec} [c+dx] \operatorname{Tan} [c+dx] \right) \Bigg) / \\
 & \left( 3 \left( -9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \right. \\
 & \quad 2 \left( 3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \right. \right. \\
 & \quad \quad \left. \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \\
 & \quad \left( -15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad 2 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \frac{5}{2}, \right. \right. \\
 & \quad \quad \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \Bigg) \Bigg)
 \end{aligned}$$

**Problem 626: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \operatorname{Sec} [c+dx] + C \operatorname{Sec} [c+dx]^2}{(a + a \operatorname{Sec} [c+dx])^{1/3}} dx$$

Optimal (type 6, 390 leaves, 9 steps):

$$\frac{3 C \operatorname{Tan}[c+d x]}{2 d (a+a \operatorname{Sec}[c+d x])^{1/3}} +$$

$$\left( 3 \sqrt{2} \operatorname{AppellF1}\left[\frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \frac{1}{2} (1+\operatorname{Sec}[c+d x]), 1+\operatorname{Sec}[c+d x]\right] \operatorname{Tan}[c+d x] \right) /$$

$$\left( d \sqrt{1-\operatorname{Sec}[c+d x]} (a+a \operatorname{Sec}[c+d x])^{1/3} \right) -$$

$$\left( 3^{3/4} (2 B-C) \operatorname{EllipticF}\left[\operatorname{ArcCos}\left[\frac{2^{1/3}-\left(1-\sqrt{3}\right)(1+\operatorname{Sec}[c+d x])^{1/3}}{2^{1/3}-\left(1+\sqrt{3}\right)(1+\operatorname{Sec}[c+d x])^{1/3}}\right], \frac{1}{4} (2+\sqrt{3})\right] \right.$$

$$\left. \left( 2^{1/3}-\left(1+\operatorname{Sec}[c+d x]\right)^{1/3} \right) \sqrt{\frac{2^{2/3}+2^{1/3}(1+\operatorname{Sec}[c+d x])^{1/3}+(1+\operatorname{Sec}[c+d x])^{2/3}}{\left(2^{1/3}-\left(1+\sqrt{3}\right)(1+\operatorname{Sec}[c+d x])^{1/3}\right)^2}} \right.$$

$$\left. \operatorname{Tan}[c+d x] \right) / \left( 2 \times 2^{1/3} d (1-\operatorname{Sec}[c+d x]) (a+a \operatorname{Sec}[c+d x])^{1/3} \right.$$

$$\left. \sqrt{-\frac{(1+\operatorname{Sec}[c+d x])^{1/3} \left(2^{1/3}-\left(1+\operatorname{Sec}[c+d x]\right)^{1/3}\right)}{\left(2^{1/3}-\left(1+\sqrt{3}\right)(1+\operatorname{Sec}[c+d x])^{1/3}\right)^2}} \right)$$

Result (type 6, 7485 leaves):

$$\left( 3 C \operatorname{Cos}[c+d x]^2 \left( (1+\operatorname{Cos}[c+d x]) \operatorname{Sec}[c+d x] \right)^{2/3} \right.$$

$$\left. (1+\operatorname{Sec}[c+d x])^{1/3} (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] \right) /$$

$$\left( d (A+2 C+2 B \operatorname{Cos}[c+d x]+A \operatorname{Cos}[2 c+2 d x]) (a(1+\operatorname{Sec}[c+d x]))^{1/3} \right) +$$

$$\left( 2^{2/3} \operatorname{Cos}[c+d x]^3 \left( \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Sec}[c+d x] \right)^{5/3} (1+\operatorname{Sec}[c+d x])^{1/3} \right.$$

$$\left. (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \left( A \operatorname{Cos}[c+d x] \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 (1+\operatorname{Sec}[c+d x])^{2/3} + \right. \right.$$

$$\left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \left( B (1+\operatorname{Sec}[c+d x])^{2/3} - \frac{1}{2} C (1+\operatorname{Sec}[c+d x])^{2/3} \right) \right) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] \right.$$

$$\left( 10 (2 A-2 B+C) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right] \right.$$

$$\left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right] - \right.$$

$$\left. 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^4 -$$

$$9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right]$$

$$\left( -5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right] \right.$$

$$\left. (2 (A+2 B-C) + (4 A+2 B-C) \operatorname{Cos}[c+d x]) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 + 2 (2 A+2 B-C) \right)$$

$$\begin{aligned}
 & \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \Big/ \\
 & \left( d (A + 2C + 2B \cos[c+dx] + A \cos[2c+2dx]) (a (1 + \sec[c+dx]))^{1/3} \right. \\
 & \quad \left( -9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. 2 \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \\
 & \quad \left. \left. 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \quad \left( -15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. 2 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \\
 & \quad \left. \left. 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \quad \left( \left( \cos[c+dx] \sec\left[\frac{1}{2}(c+dx)\right]^2 \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^{5/3} \right. \right. \\
 & \quad \left( 10 (2A - 2B + C) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \quad \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[ \right. \right. \\
 & \quad \quad \left. \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^4 - \right. \\
 & \quad \left. 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left( -5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] (2(A + 2B - C) + \right. \\
 & \quad \left. (4A + 2B - C) \cos[c+dx]) \sec\left[\frac{1}{2}(c+dx)\right]^2 + 2(2A + 2B - C) \left( 3 \operatorname{AppellF1}\left[ \right. \right. \\
 & \quad \quad \left. \left. \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \right. \right. \\
 & \quad \quad \left. \left. 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \Big/ \\
 & \quad \left( 2^{1/3} \left( -9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \quad \left. 2 \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[ \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \quad \left( -15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. 2 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \Big/
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \\
 & \left( 2^{2/3} \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^{5/3} \sin[c+dx] \tan\left[\frac{1}{2}(c+dx)\right] \right. \\
 & \quad \left( 10(2A-2B+C) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
 & \quad \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^4 - \\
 & \quad 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left. \left( -5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] (2(A+2B-C) + \right. \right. \\
 & \quad \left. \left. (4A+2B-C) \cos[c+dx]) \sec\left[\frac{1}{2}(c+dx)\right]^2 + 2(2A+2B-C) \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) / \\
 & \left( \left( -9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \quad 2 \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \quad \left. \left( -15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. 2 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) - \\
 & \left( 2^{2/3} \cos[c+dx] \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^{5/3} \tan\left[\frac{1}{2}(c+dx)\right] \right. \\
 & \quad \left( 10(2A-2B+C) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
 & \quad \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^4 - \\
 & \quad 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left. \left( -5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
 & \quad \left. \left( 2(A+2B-C) + (4A+2B-C) \cos[c+dx] \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 + 2(2A+2B-C) \right)
 \end{aligned}$$



$$\begin{aligned}
& 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \\
& \left(-5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left.(2(A+2B-C) + (4A+2B-C) \operatorname{Cos}[c+dx]) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 + 2(2A+2B-C) \right. \\
& \quad \left.(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \\
& \left(2\left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \\
& \quad \left. \left. 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \right. \\
& \quad \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - 15\left(-\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \right. \right. \\
& \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
& \quad \left. \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) + 2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
& \quad \left. \left(3\left(-\frac{10}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{2}{3}, 3, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \right. \\
& \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{10}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, 2, \frac{9}{2}, \right. \right. \right. \\
& \quad \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)\right) - \right. \\
& \quad \left. 2\left(-\frac{5}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, 2, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
& \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{25}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{8}{3}, 1, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
& \quad \left. \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)\right)\right)\right) / \\
& \left(\left(-9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
& \quad \left. \left. 2\left(3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \right. \\
& \quad \left. \left(-15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
& \quad \left. \left. 2\left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \right) +
\end{aligned}$$

$$\begin{aligned}
 & \left( 2^{2/3} \cos [c + d x] \left( \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sec [c + d x] \right)^{5/3} \tan \left[ \frac{1}{2} (c + d x) \right] \right. \\
 & \quad \left( 20 (2 A - 2 B + C) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right. \\
 & \quad \left( 3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] - \right. \\
 & \quad \left. \left. 2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \right. \\
 & \quad \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right]^3 + 10 (2 A - 2 B + C) \\
 & \quad \left( 3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] - \right. \\
 & \quad \left. \left. 2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \right. \\
 & \quad \tan \left[ \frac{1}{2} (c + d x) \right]^4 \left( -\frac{3}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] + \frac{2}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, 1, \right. \right. \\
 & \quad \left. \left. \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] \right) - \\
 & \quad 9 \left( -\frac{1}{3} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right. \\
 & \quad \left. \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] + \frac{2}{9} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] \right) \\
 & \quad \left( -5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right. \\
 & \quad \left. \left( 2 (A + 2 B - C) + (4 A + 2 B - C) \cos [c + d x] \right) \sec \left[ \frac{1}{2} (c + d x) \right]^2 + 2 (2 A + 2 B - C) \right. \\
 & \quad \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) + \\
 & \quad 10 (2 A - 2 B + C) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \\
 & \quad \tan \left[ \frac{1}{2} (c + d x) \right]^4 \\
 & \quad \left( 3 \left( -\frac{6}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 3, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right. \right. \\
 & \quad \left. \left. \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] + \frac{2}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, 2, \frac{7}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] \right) \right) - \\
 & \quad 2 \left( -\frac{3}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right.
 \end{aligned}$$

$$\begin{aligned}
& \left( \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right] + \text{AppellF1}\left[\frac{5}{2}, \frac{8}{3}, 1, \frac{7}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right] \right) - \\
& 9 \text{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \\
& \left( 5(4A+2B-C) \text{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \left. \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Sin}[c+dx] + 2(2A+2B-C) \left( 3 \text{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \right. \right. \right. \\
& \left. \left. \left. \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \text{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \right. \right. \right. \\
& \left. \left. \left. \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right] - \right. \\
& \left. 5 \text{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \left. (2(A+2B-C) + (4A+2B-C) \text{Cos}[c+dx]) \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right] - \right. \\
& \left. 5(2(A+2B-C) + (4A+2B-C) \text{Cos}[c+dx]) \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
& \left. \left( -\frac{3}{5} \text{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
& \left. \left. \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{2}{5} \text{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \right. \right. \right. \\
& \left. \left. \left. \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) + \\
& 2(2A+2B-C) \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left( 3 \left( -\frac{10}{7} \text{AppellF1}\left[\frac{7}{2}, \frac{2}{3}, 3, \frac{9}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
& \left. \left. \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
& \left. \left. \frac{10}{21} \text{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, 2, \frac{9}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
& \left. \left. \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right] \right) - 2 \left( -\frac{5}{7} \text{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, 2, \right. \right. \right. \\
& \left. \left. \left. \frac{9}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
& \left. \left. \text{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{25}{21} \text{AppellF1}\left[\frac{7}{2}, \frac{8}{3}, 1, \frac{9}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \left. \left. \left. -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \Big/ \\
& \left( \left( -9 \text{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
& \left. \left. 2 \left( 3 \text{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \text{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \right. \right. \right. \right. \\
& \left. \left. \left. \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right)
\end{aligned}$$



$$\begin{aligned}
 & \left( -15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad 2 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \\
 & \quad \quad \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \left. \right) + \right. \\
 & \left. \left( 5 \times 2^{2/3} \cos[c+dx] \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^{2/3} \tan\left[\frac{1}{2}(c+dx)\right] \right. \right. \\
 & \quad \left( 10(2A-2B+C) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \quad \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[ \right. \right. \\
 & \quad \quad \left. \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^4 - \right. \\
 & \quad 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
 & \quad \left. \left( -5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \quad \quad \left. \left( 2(A+2B-C) + (4A+2B-C) \cos[c+dx] \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 + 2(2A+2B-C) \right. \\
 & \quad \quad \left. \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[ \right. \right. \right. \\
 & \quad \quad \quad \left. \left. \frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \left. \right) \right) \\
 & \quad \left. \left( -\cos\left[\frac{1}{2}(c+dx)\right] \sec[c+dx] \sin\left[\frac{1}{2}(c+dx)\right] + \cos\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
 & \quad \quad \left. \left. \sec[c+dx] \tan[c+dx] \right) \right) \left. \right) / \\
 & \left( 3 \left( -9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \quad 2 \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[ \right. \right. \\
 & \quad \quad \left. \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \quad \left( -15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad 2 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \\
 & \quad \quad \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \left. \right) \left. \right) \left. \right)
 \end{aligned}$$

**Problem 627: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec[c+dx] + C \sec[c+dx]^2}{(a + a \sec[c+dx])^{4/3}} dx$$

Optimal (type 6, 402 leaves, 9 steps):

$$\begin{aligned}
 & -\frac{3(A-B+C)\operatorname{Tan}[c+dx]}{5d(a+a\operatorname{Sec}[c+dx])^{4/3}} + \\
 & \left( 3\sqrt{2} \operatorname{AppellF1}\left[\frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \frac{1}{2}(1+\operatorname{Sec}[c+dx]), 1+\operatorname{Sec}[c+dx]\right] \operatorname{Tan}[c+dx] \right) / \\
 & \left( a d \sqrt{1-\operatorname{Sec}[c+dx]} (a+a\operatorname{Sec}[c+dx])^{1/3} \right) + \\
 & \left( 3^{3/4} (A-B-4C) \operatorname{EllipticF}\left[\operatorname{ArcCos}\left[\frac{2^{1/3}-(1-\sqrt{3})(1+\operatorname{Sec}[c+dx])^{1/3}}{2^{1/3}-(1+\sqrt{3})(1+\operatorname{Sec}[c+dx])^{1/3}}\right], \frac{1}{4}(2+\sqrt{3})\right] \right. \\
 & \left. (2^{1/3}-(1+\operatorname{Sec}[c+dx])^{1/3}) \sqrt{\frac{2^{2/3}+2^{1/3}(1+\operatorname{Sec}[c+dx])^{1/3}+(1+\operatorname{Sec}[c+dx])^{2/3}}{(2^{1/3}-(1+\sqrt{3})(1+\operatorname{Sec}[c+dx])^{1/3})^2}} \right. \\
 & \left. \operatorname{Tan}[c+dx] \right) / \left( 5 \times 2^{1/3} a d (1-\operatorname{Sec}[c+dx]) (a+a\operatorname{Sec}[c+dx])^{1/3} \right. \\
 & \left. \sqrt{-\frac{(1+\operatorname{Sec}[c+dx])^{1/3} (2^{1/3}-(1+\operatorname{Sec}[c+dx])^{1/3})}{(2^{1/3}-(1+\sqrt{3})(1+\operatorname{Sec}[c+dx])^{1/3})^2}} \right)
 \end{aligned}$$

Result (type 6, 7586 leaves):

$$\begin{aligned}
 & \left( \operatorname{Cos}[c+dx]^2 ((1+\operatorname{Cos}[c+dx]) \operatorname{Sec}[c+dx])^{2/3} \right. \\
 & \left( (1+\operatorname{Sec}[c+dx])^{4/3} (A+B\operatorname{Sec}[c+dx]+C\operatorname{Sec}[c+dx]^2) \right. \\
 & \left( -\frac{6}{5} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \left( A \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] - B \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + C \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \right. \\
 & \left. \left. \left. + \frac{3}{5} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^3 \left( A \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] - B \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + C \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) / \\
 & \left( d (A+2C+2B\operatorname{Cos}[c+dx]+A\operatorname{Cos}[2c+2dx]) (a(1+\operatorname{Sec}[c+dx]))^{4/3} \right) + \\
 & \left( 2 \times 2^{2/3} \operatorname{Cos}[c+dx]^3 \left( \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx] \right)^{5/3} \right. \\
 & \left( (1+\operatorname{Sec}[c+dx])^{4/3} (A+B\operatorname{Sec}[c+dx]+C\operatorname{Sec}[c+dx]^2) \right. \\
 & \left( A \operatorname{Cos}[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 (1+\operatorname{Sec}[c+dx])^{2/3} + \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \left. \left( -\frac{1}{5} A (1+\operatorname{Sec}[c+dx])^{2/3} + \frac{1}{5} B (1+\operatorname{Sec}[c+dx])^{2/3} + \frac{4}{5} C (1+\operatorname{Sec}[c+dx])^{2/3} \right) \right) \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \left( 10(6A-B-4C) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right] \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right] - \right. \right. \\
 & \left. \left. 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^4 - \right.
 \end{aligned}$$

$$\begin{aligned}
 & 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \\
 & \left(-5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right. \\
 & \quad \left.(3A+2B+8C+(9A+B+4C)\operatorname{Cos}[c+dx])\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2+2(4A+B+4C)\right. \\
 & \quad \left.\left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]-2 \operatorname{AppellF1}\left[\frac{5}{2},\right.\right.\right. \\
 & \quad \left.\left.\frac{5}{3}, 1, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)\right) / \\
 & \left(5d(A+2C+2B\operatorname{Cos}[c+dx]+A\operatorname{Cos}[2c+2dx])\left(a(1+\operatorname{Sec}[c+dx])\right)^{4/3}\right. \\
 & \quad \left(-9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]+2\right. \\
 & \quad \left.2\left(3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]-2 \operatorname{AppellF1}\left[\frac{3}{2},\right.\right.\right. \\
 & \quad \left.\left.\frac{5}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \\
 & \quad \left(-15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]+2\right. \\
 & \quad \left.2\left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]-2 \operatorname{AppellF1}\left[\frac{5}{2},\right.\right.\right. \\
 & \quad \left.\left.\frac{5}{3}, 1, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \\
 & \quad \left.\left(\left(2^{2/3}\operatorname{Cos}[c+dx]\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2\left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2\operatorname{Sec}[c+dx]\right)^{5/3}\right.\right.\right. \\
 & \quad \left.\left.10(6A-B-4C)\operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right.\right. \\
 & \quad \left.\left.3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]-2 \operatorname{AppellF1}\left[\frac{3}{2},\right.\right.\right. \\
 & \quad \left.\left.\frac{5}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^4-9 \operatorname{AppellF1}\left[\frac{1}{2},\right.\right. \\
 & \quad \left.\left.\frac{2}{3}, 1, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \\
 & \quad \left.\left(-5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right)(3A+2B+8C+ \right. \\
 & \quad \left.(9A+B+4C)\operatorname{Cos}[c+dx])\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2+2(4A+B+4C)\left(3 \operatorname{AppellF1}\left[\frac{5}{2},\right.\right.\right. \\
 & \quad \left.\left.\frac{2}{3}, 2, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]-2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3},\right.\right. \\
 & \quad \left.\left.1, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)\right) / \\
 & \left(5\left(-9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]+2\right.\right. \\
 & \quad \left.2\left(3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]-2 \operatorname{AppellF1}\left[\frac{3}{2},\right.\right.\right.
 \end{aligned}$$

$$\begin{aligned}
& \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \\
& \left( -15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \\
& \quad \quad \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) - \\
& \left( 2 \times 2^{2/3} \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^{5/3} \sin[c+dx] \tan\left[\frac{1}{2}(c+dx)\right] \right. \\
& \quad \left( 10(6A - B - 4C) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[ \right. \right. \\
& \quad \quad \left. \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^4 - \\
& \quad 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
& \quad \left( -5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] (3A + 2B + 8C + \right. \\
& \quad \quad \left. (9A + B + 4C) \cos[c+dx] \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 + 2(4A + B + 4C) \left( 3 \operatorname{AppellF1}\left[ \right. \right. \\
& \quad \quad \left. \left. \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \right. \right. \\
& \quad \quad \left. \left. 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \Bigg) / \\
& \left( 5 \left( -9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
& \quad 2 \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[ \right. \right. \\
& \quad \quad \left. \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \\
& \left( -15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \\
& \quad \quad \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) - \\
& \left( 2 \times 2^{2/3} \cos[c+dx] \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^{5/3} \tan\left[\frac{1}{2}(c+dx)\right] \right. \\
& \quad \left( 10(6A - B - 4C) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[ \right. \right. \\
& \quad \quad \left. \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^4 -
\end{aligned}$$

$$\begin{aligned}
 & 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
 & \left(-5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right. \\
 & \quad \left.(3A+2B+8C+(9A+B+4C)\cos[c+dx]\right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 + 2(4A+B+4C) \\
 & \quad \left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Big) \\
 & \left(2\left(3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - 9\left(-\frac{1}{3} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{9} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) + 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \quad \left(3\left(-\frac{6}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 3, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) - \\
 & \quad 2\left(-\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \operatorname{AppellF1}\left[\frac{5}{2}, \frac{8}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) \Big) \Big) / \\
 & \left(5\left(-9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \quad \left. 2\left(3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \\
 & \quad \left(-15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. 2\left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \Big) - \\
 & \left(2 \times 2^{2/3} \cos[c+dx] \left(\cos\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx]\right)^{5/3} \tan\left[\frac{1}{2}(c+dx)\right]\right)
 \end{aligned}$$

$$\begin{aligned}
& \left( 10 (6A - B - 4C) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right. \\
& \quad \left( 3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \right. \right. \\
& \quad \quad \left. \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + dx) \right]^4 - \\
& 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \\
& \quad \left( -5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right. \\
& \quad \quad \left( 3A + 2B + 8C + (9A + B + 4C) \cos [c + dx] \right) \operatorname{Sec} \left[ \frac{1}{2} (c + dx) \right]^2 + 2 (4A + B + 4C) \\
& \quad \quad \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \right. \right. \\
& \quad \quad \quad \left. \left. \frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + dx) \right]^2 \left. \right) \\
& \left( 2 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \right. \right. \right. \\
& \quad \quad \left. \left. \frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) \operatorname{Sec} \left[ \frac{1}{2} (c + dx) \right]^2 \tan \left[ \frac{1}{2} \right. \\
& \quad \quad \left. (c + dx) \right] - 15 \left( -\frac{3}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right. \\
& \quad \quad \operatorname{Sec} \left[ \frac{1}{2} (c + dx) \right]^2 \tan \left[ \frac{1}{2} (c + dx) \right] + \frac{2}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \right. \\
& \quad \quad \left. \left. -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c + dx) \right]^2 \tan \left[ \frac{1}{2} (c + dx) \right] \right) + 2 \tan \left[ \frac{1}{2} (c + dx) \right]^2 \\
& \quad \left( 3 \left( -\frac{10}{7} \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{2}{3}, 3, \frac{9}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right. \right. \\
& \quad \quad \operatorname{Sec} \left[ \frac{1}{2} (c + dx) \right]^2 \tan \left[ \frac{1}{2} (c + dx) \right] + \frac{10}{21} \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{5}{3}, 2, \frac{9}{2}, \right. \\
& \quad \quad \left. \left. \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c + dx) \right]^2 \tan \left[ \frac{1}{2} (c + dx) \right] \right) \left. \right) - \\
& 2 \left( -\frac{5}{7} \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{5}{3}, 2, \frac{9}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right. \\
& \quad \operatorname{Sec} \left[ \frac{1}{2} (c + dx) \right]^2 \tan \left[ \frac{1}{2} (c + dx) \right] + \frac{25}{21} \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{8}{3}, 1, \frac{9}{2}, \tan \left[ \frac{1}{2} (c + \right. \right. \\
& \quad \quad \left. \left. dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c + dx) \right]^2 \tan \left[ \frac{1}{2} (c + dx) \right] \left. \right) \left. \right) \left. \right) \left. \right) / \\
& \left( 5 \left( -9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + \right. \right. \\
& \quad 2 \left( 3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \right. \right. \\
& \quad \quad \left. \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + dx) \right]^2 \left. \right) \\
& \quad \left( -15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + \right.
\end{aligned}$$

$$\begin{aligned}
 & 2 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \Bigg) + \\
 & \left( 2 \times 2^{2/3} \operatorname{Cos} [c+dx] \left( \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Sec} [c+dx] \right)^{5/3} \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right. \\
 & \quad \left( 20 (6A - B - 4C) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
 & \quad \left( 3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] - \right. \\
 & \quad \left. 2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \\
 & \quad \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^3 + 10 (6A - B - 4C) \\
 & \quad \left( 3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] - \right. \\
 & \quad \left. 2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \\
 & \quad \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^4 \left( -\frac{3}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] + \frac{2}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, 1, \right. \right. \\
 & \quad \left. \left. \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right) \Bigg) - \\
 & 9 \left( -\frac{1}{3} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
 & \quad \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] + \frac{2}{9} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \right. \\
 & \quad \left. \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \Bigg) \\
 & \left( -5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
 & \quad \left. (3A + 2B + 8C + (9A + B + 4C) \operatorname{Cos} [c+dx]) \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 + 2 (4A + B + 4C) \right. \\
 & \quad \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \Bigg) + \\
 & 10 (6A - B - 4C) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \\
 & \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^4 \\
 & \left( 3 \left( -\frac{6}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 3, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \right. \\
 & \quad \left. \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] + \frac{2}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, 2, \frac{7}{2}, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& \left. \left( \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) - \\
& 2 \left( -\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right. \\
& \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \operatorname{AppellF1}\left[\frac{5}{2}, \frac{8}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) - \\
& 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \\
& \left( 5(9A+B+4C) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right. \\
& \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \sin[c+dx] + 2(4A+B+4C) \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - \right. \\
& \quad \left. 5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \\
& \quad (3A+2B+8C+(9A+B+4C) \cos[c+dx]) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - \\
& \quad 5(3A+2B+8C+(9A+B+4C) \cos[c+dx]) \sec\left[\frac{1}{2}(c+dx)\right]^2 \\
& \quad \left( -\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right. \\
& \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + \\
& 2(4A+B+4C) \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( 3 \left( -\frac{10}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{2}{3}, 3, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right. \right. \\
& \quad \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
& \quad \left. \frac{10}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, 2, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) - 2 \left( -\frac{5}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, 2, \right. \right. \\
& \quad \left. \left. \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
& \quad \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{25}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{8}{3}, 1, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \Big/ \\
& \left( 5 \left( -9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + \right. \right.
\end{aligned}$$



$$\begin{aligned}
 & 2 \left( 3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \right. \right. \\
 & \quad \left. \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \\
 & \left( -15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad 2 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \left. \right) + \\
 & \left( 2 \times 2^{2/3} \operatorname{Cos} [c+dx] \left( \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Sec} [c+dx] \right)^{2/3} \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right. \\
 & \quad \left( 10 (6A - B - 4C) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
 & \quad \left( 3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \right. \right. \\
 & \quad \left. \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^4 - \\
 & \quad 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \\
 & \quad \left( -5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
 & \quad \left. (3A + 2B + 8C + (9A + B + 4C) \operatorname{Cos} [c+dx]) \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 + 2 (4A + B + 4C) \right. \\
 & \quad \left. \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \left. \right) \right) \\
 & \quad \left( -\operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right] \operatorname{Sec} [c+dx] \operatorname{Sin} \left[ \frac{1}{2} (c+dx) \right] + \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right]^2 \right. \\
 & \quad \left. \left. \operatorname{Sec} [c+dx] \operatorname{Tan} [c+dx] \right) \right) / \\
 & \left( 3 \left( -9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \right. \\
 & \quad 2 \left( 3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \right. \right. \\
 & \quad \left. \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \\
 & \quad \left( -15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \left. 2 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \left. \right) \right)
 \end{aligned}$$

Problem 628: Result more than twice size of optimal antiderivative.

$$\int \frac{A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2}{(a + a \operatorname{Sec}[c + d x])^{7/3}} dx$$

Optimal (type 6, 466 leaves, 10 steps):

$$\begin{aligned} & - \frac{3(A - B + C) \operatorname{Tan}[c + d x]}{11 d (a + a \operatorname{Sec}[c + d x])^{7/3}} - \frac{3(4A - 4B - 7C) \operatorname{Tan}[c + d x]}{55 a^2 d (1 + \operatorname{Sec}[c + d x]) (a + a \operatorname{Sec}[c + d x])^{1/3}} - \\ & \left( 3 \sqrt{2} A \operatorname{AppellF1}\left[-\frac{5}{6}, \frac{1}{2}, 1, \frac{1}{6}, \frac{1}{2} (1 + \operatorname{Sec}[c + d x]), 1 + \operatorname{Sec}[c + d x]\right] \operatorname{Tan}[c + d x] \right) / \\ & \left( 5 a^2 d \sqrt{1 - \operatorname{Sec}[c + d x]} (1 + \operatorname{Sec}[c + d x]) (a + a \operatorname{Sec}[c + d x])^{1/3} \right) + \\ & \left( 3^{3/4} (4A - 4B - 7C) \operatorname{EllipticF}\left[\operatorname{ArcCos}\left[\frac{2^{1/3} - (1 - \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}\right], \frac{1}{4} (2 + \sqrt{3})\right] \right. \\ & \left. (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3}) \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \operatorname{Sec}[c + d x])^{1/3} + (1 + \operatorname{Sec}[c + d x])^{2/3}}{(2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3})^2}} \right. \\ & \left. \operatorname{Tan}[c + d x] \right) / \left( 55 \times 2^{1/3} a^2 d (1 - \operatorname{Sec}[c + d x]) (a + a \operatorname{Sec}[c + d x])^{1/3} \right. \\ & \left. \sqrt{-\frac{(1 + \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3})}{(2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3})^2}} \right) \end{aligned}$$

Result (type 6, 7682 leaves):

$$\begin{aligned} & \left( \operatorname{Cos}[c + d x]^2 ((1 + \operatorname{Cos}[c + d x]) \operatorname{Sec}[c + d x])^{2/3} \right. \\ & \left( (1 + \operatorname{Sec}[c + d x])^{7/3} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\ & \left( -\frac{6}{55} \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right] \left( 20A \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] - 9B \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] - 2C \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) - \right. \\ & \left. \frac{3}{22} \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^5 \left( A \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] - B \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] + C \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) + \frac{3}{55} \right. \\ & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^3 \left( 25A \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] - 14B \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] + 3C \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \right) \right) / \\ & \left( d (A + 2C + 2B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2c + 2d x]) (a (1 + \operatorname{Sec}[c + d x]))^{7/3} \right) + \\ & \left( 2 \times 2^{2/3} \operatorname{Cos}[c + d x]^3 \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]^2 \operatorname{Sec}[c + d x] \right)^{5/3} \right. \\ & \left( (1 + \operatorname{Sec}[c + d x])^{7/3} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\ & \left( A \operatorname{Cos}[c + d x] \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^2 (1 + \operatorname{Sec}[c + d x])^{2/3} + \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^2 \right. \\ & \left. \left( -\frac{3}{11} A (1 + \operatorname{Sec}[c + d x])^{2/3} + \frac{4}{55} B (1 + \operatorname{Sec}[c + d x])^{2/3} + \frac{7}{55} C (1 + \operatorname{Sec}[c + d x])^{2/3} \right) \right) \\ & \left. \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] \left( 10 (70A - 4B - 7C) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2, \right. \right. \right. \end{aligned}$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{2}(c+dx)\right]^2 \left(3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \\
 & 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left. \right) \tan\left[\frac{1}{2}(c+dx)\right]^4 - \\
 & 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
 & \left(-5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \left. (25A + 8B + 14C + (95A + 4B + 7C) \cos[c+dx]) \sec\left[\frac{1}{2}(c+dx)\right]^2 + 2(40A + 4B + 7C) \right. \\
 & \left. \left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \right. \\
 & \left. \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Big/ \\
 & \left(55d(A + 2C + 2B \cos[c+dx] + A \cos[2c + 2dx]) (a(1 + \sec[c+dx]))^{7/3} \right. \\
 & \left. \left(-9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & 2 \left(3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \\
 & \left. \left. 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \left(-15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & 2 \left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \\
 & \left. \left. 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \left. \left(2^{2/3} \cos[c+dx] \sec\left[\frac{1}{2}(c+dx)\right]^2 \left(\cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx]\right)^{5/3} \right. \right. \\
 & \left. \left(10(70A - 4B - 7C) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \left. \left(3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \right. \right. \right. \\
 & \left. \left. \left. \frac{5}{2}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^4 - \right. \\
 & \left. 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \left(-5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \right. \right. \\
 & \left. \left. 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] (25A + 8B + 14C + (95A + 4B + 7C) \right. \right. \\
 & \left. \left. \cos[c+dx]) \sec\left[\frac{1}{2}(c+dx)\right]^2 + 2(40A + 4B + 7C) \left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \right. \right. \right. \\
 & \left. \left. \left. 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \right. \right. \right. \\
 & \left. \left. \left. \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Big/
 \end{aligned}$$

$$\begin{aligned}
& \left( 55 \left( -9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \right. \\
& \quad 2 \left( 3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \right. \right. \\
& \quad \quad \left. \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \\
& \quad \left( -15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad 2 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \frac{5}{2}, \right. \right. \\
& \quad \quad \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) - \\
& \quad \left( 2 \times 2^{2/3} \left( \cos \left[ \frac{1}{2} (c+dx) \right]^2 \sec [c+dx] \right)^{5/3} \sin [c+dx] \tan \left[ \frac{1}{2} (c+dx) \right] \right. \\
& \quad \left( 10 (70A - 4B - 7C) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \left( 3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \right. \right. \\
& \quad \quad \left. \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^4 - \\
& \quad 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \left( -5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \right. \right. \\
& \quad \quad \left. \left. 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) (25A + 8B + 14C + (95A + 4B + 7C) \right. \\
& \quad \quad \left. \cos [c+dx]) \sec \left[ \frac{1}{2} (c+dx) \right]^2 + 2 (40A + 4B + 7C) \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \right. \right. \right. \\
& \quad \quad \quad \left. \left. 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, 1, \right. \right. \\
& \quad \quad \quad \left. \left. \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \left. \right) \Big/ \\
& \quad \left( 55 \left( -9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \right. \\
& \quad 2 \left( 3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \right. \right. \\
& \quad \quad \left. \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \\
& \quad \left( -15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad 2 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \frac{5}{2}, \right. \right. \\
& \quad \quad \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) - \\
& \quad \left( 2 \times 2^{2/3} \cos [c+dx] \left( \cos \left[ \frac{1}{2} (c+dx) \right]^2 \sec [c+dx] \right)^{5/3} \tan \left[ \frac{1}{2} (c+dx) \right] \right. \\
& \quad \left. \left( 10 (70A - 4B - 7C) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \right)
\end{aligned}$$

$$\begin{aligned}
 & \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^4 - \\
 & 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
 & \left( -5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] (25A + 8B + \right. \\
 & \quad \left. 14C + (95A + 4B + 7C) \cos[c+dx]) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 + 2(40A + 4B + 7C) \right. \\
 & \quad \left. \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \left( 2 \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - 9 \left( -\frac{1}{3} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right)^2 \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{9} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \left. \left( 3 \left( -\frac{6}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 3, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 2, \frac{7}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) - \\
 & \quad 2 \left( -\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \operatorname{AppellF1}\left[\frac{5}{2}, \frac{8}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \Big/ \\
 & \left( 55 \left( -9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \quad \left. 2 \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \\
 & \quad \left( -15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. 2 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& \left. \left. \left. \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) - \right. \\
& \left. \left( 2 \times 2^{2/3} \cos[c+dx] \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^{5/3} \tan\left[\frac{1}{2}(c+dx)\right] \right. \right. \\
& \left. \left( 10(70A-4B-7C) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \right. \\
& \left. \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^4 - \right. \\
& \left. 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
& \left. \left( -5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] (25A+8B+ \right. \right. \\
& \left. \left. 14C + (95A+4B+7C) \cos[c+dx] \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 + 2(40A+4B+7C) \right. \\
& \left. \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \\
& \left( 2 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right. \\
& \left. (c+dx) - 15 \left( -\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
& \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
& \left. \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right. \\
& \left. \left( 3 \left( -\frac{10}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{2}{3}, 3, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \right. \\
& \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{10}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, 2, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
& \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \right) \right) \right) / \\
& \left( 55 \left( -9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
& \left. \left. 2 \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right) \right) \right)
\end{aligned}$$

$$\begin{aligned}
 & \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \\
 & \left( -15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad 2 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg)^2 \Bigg) + \\
 & \left( 2 \times 2^{2/3} \cos[c+dx] \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^{5/3} \tan\left[\frac{1}{2}(c+dx)\right] \right. \\
 & \left( 20(70A - 4B - 7C) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \\
 & \quad \left. 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
 & \quad \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^3 + 10(70A - 4B - 7C) \\
 & \quad \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \\
 & \quad \left. 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
 & \quad \tan\left[\frac{1}{2}(c+dx)\right]^4 \left( -\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \right. \right. \\
 & \quad \left. \left. \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \Bigg) - \\
 & 9 \left( -\frac{1}{3} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{9} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \Bigg) \\
 & \left( -5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] (25A + \right. \\
 & \quad \left. 8B + 14C + (95A + 4B + 7C) \cos[c+dx] \sec\left[\frac{1}{2}(c+dx)\right]^2 + 2(40A + 4B + 7C) \right. \\
 & \quad \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) + \\
 & 10(70A - 4B - 7C) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^4
 \end{aligned}$$

$$\begin{aligned}
& \left( 3 \left( -\frac{6}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 3, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \right. \\
& \quad \left. \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{2}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, 2, \frac{7}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) - \\
& 2 \left( -\frac{3}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{8}{3}, 1, \frac{7}{2}, \tan \left[ \right. \right. \right. \\
& \quad \left. \left. \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) - \\
& 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \\
& \left( 5 (95A + 4B + 7C) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \sin [c+dx] + 2 (40A + 4B + 7C) \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \right. \right. \right. \\
& \quad \left. \left. \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] - \right. \\
& 5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] (25A + \\
& \quad 8B + 14C + (95A + 4B + 7C) \cos [c+dx]) \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] - \\
& 5 (25A + 8B + 14C + (95A + 4B + 7C) \cos [c+dx]) \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \\
& \left( -\frac{3}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{2}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) + \\
& 2 (40A + 4B + 7C) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \left( 3 \left( -\frac{10}{7} \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{2}{3}, 3, \frac{9}{2}, \tan \left[ \frac{1}{2} (c+ \right. \right. \right. \right. \\
& \quad \left. \left. \left. dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \right. \\
& \quad \left. \frac{10}{21} \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{5}{3}, 2, \frac{9}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) - 2 \left( -\frac{5}{7} \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{5}{3}, 2, \right. \right. \\
& \quad \left. \left. \frac{9}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \right. \\
& \quad \left. \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{25}{21} \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{8}{3}, 1, \frac{9}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right.
\end{aligned}$$



$$\begin{aligned}
 & -\tan\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right)\right)\right)\right)\right)\right)\right) / \\
 & \left( 55 \left( -9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \quad 2 \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \quad \left( -15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \quad 2 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
 & \quad \left( 2 \times 2^{2/3} \cos[c+dx] \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx] \right)^{2/3} \tan\left[\frac{1}{2}(c+dx)\right] \right. \\
 & \quad \left( 10 (70A - 4B - 7C) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \quad \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^4 - \\
 & \quad \quad 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
 & \quad \quad \left. \left( -5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] (25A + 8B + \right. \right. \\
 & \quad \quad \quad \left. \left. 14C + (95A + 4B + 7C) \cos[c+dx] \right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 + 2(40A + 4B + 7C) \right. \\
 & \quad \quad \quad \left. \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \\
 & \quad \left. \left( -\cos\left[\frac{1}{2}(c+dx)\right] \operatorname{Sec}[c+dx] \sin\left[\frac{1}{2}(c+dx)\right] + \cos\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
 & \quad \quad \left. \left. \operatorname{Sec}[c+dx] \tan[c+dx] \right) \right)\right)\right)\right)\right) / \\
 & \left( 33 \left( -9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \quad 2 \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \quad \left( -15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \quad 2 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right)
 \end{aligned}$$

$$\left. \left. \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right)$$

### Problem 629: Result more than twice size of optimal antiderivative.

$$\int (a + a \sec[c + dx])^{4/3} (A + B \sec[c + dx] + C \sec[c + dx]^2) dx$$

Optimal (type 6, 839 leaves, 12 steps):

$$\begin{aligned} & \frac{3 a (7 B + 4 C) (a + a \sec[c + dx])^{1/3} \tan[c + dx]}{28 d} + \\ & \left( 3 \sqrt{2} a \operatorname{AppellF1}\left[\frac{11}{6}, \frac{1}{2}, 1, \frac{17}{6}, \frac{1}{2} (1 + \sec[c + dx]), 1 + \sec[c + dx]\right] \right. \\ & \quad \left. (1 + \sec[c + dx]) (a + a \sec[c + dx])^{1/3} \tan[c + dx] \right) / \\ & \left( 11 d \sqrt{1 - \sec[c + dx]} \right) + \frac{3 C (a + a \sec[c + dx])^{4/3} \tan[c + dx]}{7 d} - \\ & \frac{15 (1 + \sqrt{3}) a (7 B + 4 C) (a + a \sec[c + dx])^{1/3} \tan[c + dx]}{28 d (1 + \sec[c + dx])^{2/3} (2^{1/3} - (1 + \sqrt{3})) (1 + \sec[c + dx])^{1/3}} + \\ & \left( 15 \times 3^{1/4} a (7 B + 4 C) \operatorname{EllipticE}\left[\operatorname{ArcCos}\left[\frac{2^{1/3} - (1 - \sqrt{3}) (1 + \sec[c + dx])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \sec[c + dx])^{1/3}}\right], \frac{1}{4} (2 + \sqrt{3})\right] \right. \\ & \quad \left. (a + a \sec[c + dx])^{1/3} (2^{1/3} - (1 + \sec[c + dx])^{1/3}) \right. \\ & \quad \left. \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \sec[c + dx])^{1/3} + (1 + \sec[c + dx])^{2/3}}{(2^{1/3} - (1 + \sqrt{3})) (1 + \sec[c + dx])^{1/3}} \tan[c + dx]} \right) / \left( 14 \times 2^{2/3} d \right. \\ & \quad \left. (1 - \sec[c + dx]) (1 + \sec[c + dx])^{2/3} \sqrt{-\frac{(1 + \sec[c + dx])^{1/3} (2^{1/3} - (1 + \sec[c + dx])^{1/3})}{(2^{1/3} - (1 + \sqrt{3})) (1 + \sec[c + dx])^{1/3}} \right) + \\ & \left( 5 \times 3^{3/4} (1 - \sqrt{3}) a (7 B + 4 C) \operatorname{EllipticF}\left[\operatorname{ArcCos}\left[\frac{2^{1/3} - (1 - \sqrt{3}) (1 + \sec[c + dx])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \sec[c + dx])^{1/3}}\right], \right. \right. \\ & \quad \left. \left. \frac{1}{4} (2 + \sqrt{3}) \right] (a + a \sec[c + dx])^{1/3} (2^{1/3} - (1 + \sec[c + dx])^{1/3}) \right. \\ & \quad \left. \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \sec[c + dx])^{1/3} + (1 + \sec[c + dx])^{2/3}}{(2^{1/3} - (1 + \sqrt{3})) (1 + \sec[c + dx])^{1/3}} \tan[c + dx]} \right) / \left( 28 \times 2^{2/3} d \right. \\ & \quad \left. (1 - \sec[c + dx]) (1 + \sec[c + dx])^{2/3} \sqrt{-\frac{(1 + \sec[c + dx])^{1/3} (2^{1/3} - (1 + \sec[c + dx])^{1/3})}{(2^{1/3} - (1 + \sqrt{3})) (1 + \sec[c + dx])^{1/3}} \right) \end{aligned}$$

Result (type 6, 5459 leaves):

$$\begin{aligned}
 & \left( \cos [c+d x]^2 \left( (1+\cos [c+d x]) \sec [c+d x] \right)^{1/3} \left( a \left( 1+\sec [c+d x] \right) \right)^{4/3} \right. \\
 & \quad \left. (A+B \sec [c+d x]+C \sec [c+d x]^2) \left( \frac{3}{14} (28 A+35 B+20 C) \sin [c+d x]+ \right. \right. \\
 & \quad \left. \left. \frac{3}{14} \sec [c+d x] (7 B \sin [c+d x]+8 C \sin [c+d x])+\frac{6}{7} C \sec [c+d x] \tan [c+d x] \right) \right) / \\
 & \quad \left( d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) (1+\sec [c+d x])^{4/3}- \right. \\
 & \quad \left. \left( \cos [c+d x]^2 \left( a \left( 1+\sec [c+d x] \right) \right)^{4/3} (A+B \sec [c+d x]+C \sec [c+d x]^2) \right. \right. \\
 & \quad \left. \left( 4 A (1+\sec [c+d x])^{1/3}+\frac{5}{2} B (1+\sec [c+d x])^{1/3}+ \right. \right. \\
 & \quad \left. \left. \frac{10}{7} C (1+\sec [c+d x])^{1/3}+\cos [c+d x] \left( -6 A (1+\sec [c+d x])^{1/3}- \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{15}{2} B (1+\sec [c+d x])^{1/3}-\frac{30}{7} C (1+\sec [c+d x])^{1/3} \right) \right) \tan \left[ \frac{1}{2} (c+d x) \right] \right) / \\
 & \quad \left( \left( 9 (28 A-5 (7 B+4 C)) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2 \right] \right) / \right. \\
 & \quad \left( 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2 \right] + \right. \\
 & \quad \left. 2 \left( -3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2 \right] + \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+d x) \right]^2 \right) + \\
 & \quad \left( (28 A+35 B+20 C) \left( 6 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2 \right] - \right. \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2 \right] \right) \right. \\
 & \quad \left. \cos [c+d x] \sec \left[ \frac{1}{2} (c+d x) \right]^2 \tan \left[ \frac{1}{2} (c+d x) \right]^2+5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2 \right] \left( -9+8 \tan \left[ \frac{1}{2} (c+d x) \right]^2 \right) \right) \right) / \\
 & \quad \left( 15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2 \right] + \right. \\
 & \quad \left. 2 \left( -3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2 \right] + \operatorname{AppellF1} \left[ \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \frac{4}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+d x) \right]^2 \right) \right) / \\
 & \quad \left( 7 \times 2^{2/3} d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \left( \cos \left[ \frac{1}{2} (c+d x) \right]^2 \sec [c+d x] \right)^{2/3} \right. \\
 & \quad \left. (1+\sec [c+d x])^{4/3} \right. \\
 & \quad \left. \left( -1+\tan \left[ \frac{1}{2} (c+d x) \right] \right)^4 \right)
 \end{aligned}$$

$$\begin{aligned}
& \left( \frac{1}{7 \left( \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sec [c + d x] \right)^{2/3} \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right]^4 \right)^2} \right. \\
& 2^{1/3} \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right]^4 \left( \left( 9 (28 A - 5 (7 B + 4 C)) \right. \right. \\
& \quad \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) / \\
& \left( 9 \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad 2 \left( -3 \text{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \text{AppellF1} \left[ \frac{3}{2}, \right. \right. \\
& \quad \quad \left. \frac{4}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 + \left( (28 A + \right. \\
& \quad \left. 35 B + 20 C) \left( 6 \left( 3 \text{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] - \right. \right. \right. \\
& \quad \quad \left. \left. \text{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \right) \\
& \quad \left. \cos [c + d x] \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right]^2 + 5 \text{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \right. \right. \\
& \quad \left. \left. \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \left( -9 + 8 \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) \right) / \\
& \left( 15 \text{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad 2 \left( -3 \text{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \text{AppellF1} \left[ \right. \right. \\
& \quad \quad \left. \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \left. \right) - \\
& \left. \left( 1 / \left( 14 \times 2^{2/3} \left( \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sec [c + d x] \right)^{2/3} \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right]^4 \right) \right) \right) \right) \\
& \sec \left[ \frac{1}{2} (c + d x) \right]^2 \left( \left( 9 (28 A - 5 (7 B + 4 C)) \right. \right. \\
& \quad \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) / \\
& \left( 9 \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad 2 \left( -3 \text{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \text{AppellF1} \left[ \frac{3}{2}, \right. \right. \\
& \quad \quad \left. \frac{4}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 + \left( (28 A + \right. \\
& \quad \left. 35 B + 20 C) \left( 6 \left( 3 \text{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] - \right. \right. \right. \\
& \quad \quad \left. \left. \text{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \right) \\
& \quad \left. \cos [c + d x] \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right]^2 + 5 \text{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \right. \right. \\
& \quad \left. \left. \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \left( -9 + 8 \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) \right)
\end{aligned}$$

$$\begin{aligned}
 & \left. \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \left(-9+8 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)\right) \Big/ \\
 & \left(15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad 2 \left(-3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \Big) - \\
 & \left. \left(1 / \left(7 \times 2^{2/3} \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx]\right)^{2/3} \left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^4\right)\right)\right)\right) \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \left(\left(9(28A-5(7B+4C))\right.\right. \\
 & \quad \left.\left(-\frac{1}{3} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right.\right. \\
 & \quad \left.\left.\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{1}{9} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right.\right.\right. \\
 & \quad \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)\right) \Big/ \\
 & \left(9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad 2 \left(-3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right.\right. \\
 & \quad \left.\left.\frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \Big) - \\
 & \left(9(28A-5(7B+4C)) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
 & \quad \left(2 \left(-3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right.\right. \\
 & \quad \left.\left.\operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \right) \\
 & \quad \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 9 \left(-\frac{1}{3} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \right.\right. \\
 & \quad \left.\left.\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left.\frac{1}{9} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
 & \quad \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \Big) + 2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left(-\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 2, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \left.\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{4}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{3}, 1, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right.\right. \\
 & \quad \left.\left.-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - 3 \left(-\frac{6}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 3, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right.\right.
 \end{aligned}$$

$$\begin{aligned}
& \left( \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right)\right) / \\
& \left( 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \right. \\
& \quad \left. \left( -3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 - \\
& \left( (28A + 35B + 20C) \left( 6 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
& \quad \left. \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \cos[c+dx] \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 + 5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left( -9 + 8 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \\
& \left( 2 \left( -3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right) \\
& \quad \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 15 \left( -\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
& \quad \left. \frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( -\frac{5}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, 2, \frac{9}{2}, \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
& \quad \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{20}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{7}{3}, 1, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - 3 \left( -\frac{10}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{1}{3}, 3, \frac{9}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right. \\
& \quad \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{5}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, 2, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right)\right) / \\
& \left( 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \right)
\end{aligned}$$

$$\begin{aligned}
 & \left( -3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 + \\
 & \left( (28A + 35B + 20C) \left( 40 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 6 \right. \\
 & \quad \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
 & \cos[c+dx] \sec\left[\frac{1}{2}(c+dx)\right]^4 \tan\left[\frac{1}{2}(c+dx)\right] - 6 \\
 & \quad \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
 & \sec\left[\frac{1}{2}(c+dx)\right]^2 \sin[c+dx] \tan\left[\frac{1}{2}(c+dx)\right]^2 + 6 \\
 & \quad \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \cos[c+dx] \\
 & \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^3 + 5 \left( -\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \left( -9 + 8 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + 6 \\
 & \cos[c+dx] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( \frac{5}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, 2, \frac{9}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - \right. \\
 & \quad \left. \frac{20}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{7}{3}, 1, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 3 \left( -\frac{10}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{1}{3}, 3, \right. \right. \right. \\
 & \quad \left. \left. \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{5}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, 2, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
& \left( 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2 \left( -3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) + \\
& \quad \frac{1}{2^{1/3}} \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^{5/3} \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^4 \right) \\
& \quad \tan\left[\frac{1}{2}(c+dx)\right] \\
& \quad \left( \left( 9(28A - 5(7B + 4C)) \right. \right. \\
& \quad \quad \left. \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) / \\
& \quad \left( 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \quad 2 \left( -3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) + \\
& \quad \left( (28A + 35B + 20C) \left( 6 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \right. \\
& \quad \left. \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \cos[c+dx] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
& \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 + 5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left. \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( -9 + 8 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) / \\
& \quad \left( 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \quad 2 \left( -3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \\
& \quad \left( -\cos\left[\frac{1}{2}(c+dx)\right] \sec[c+dx] \sin\left[\frac{1}{2}(c+dx)\right] + \cos\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
& \quad \quad \left. \sec[c+dx] \tan[c+dx] \right) \Bigg) \Bigg)
\end{aligned}$$

**Problem 630: Result more than twice size of optimal antiderivative.**



$$\int (a + a \operatorname{Sec}[c + d x])^{1/3} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 6, 786 leaves, 11 steps):

$$\begin{aligned} & \frac{3 C (a + a \operatorname{Sec}[c + d x])^{1/3} \operatorname{Tan}[c + d x]}{4 d} + \\ & \left( 3 \sqrt{2} \operatorname{AppellF1}\left[\frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \frac{1}{2} (1 + \operatorname{Sec}[c + d x]), 1 + \operatorname{Sec}[c + d x]\right] \right. \\ & \quad \left. (a + a \operatorname{Sec}[c + d x])^{1/3} \operatorname{Tan}[c + d x] \right) / \left( 5 d \sqrt{1 - \operatorname{Sec}[c + d x]} \right) - \\ & \frac{3 (1 + \sqrt{3}) (4 B + C) (a + a \operatorname{Sec}[c + d x])^{1/3} \operatorname{Tan}[c + d x]}{4 d (1 + \operatorname{Sec}[c + d x])^{2/3} (2^{1/3} - (1 + \sqrt{3})) (1 + \operatorname{Sec}[c + d x])^{1/3}} + \\ & \left( 3 \times 3^{1/4} (4 B + C) \operatorname{EllipticE}\left[\operatorname{ArcCos}\left[\frac{2^{1/3} - (1 - \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}\right], \frac{1}{4} (2 + \sqrt{3})\right] \right. \\ & \quad \left. (a + a \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3}) \right. \\ & \quad \left. \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \operatorname{Sec}[c + d x])^{1/3} + (1 + \operatorname{Sec}[c + d x])^{2/3}}{(2^{1/3} - (1 + \sqrt{3})) (1 + \operatorname{Sec}[c + d x])^{1/3}}^2} \operatorname{Tan}[c + d x]} \right) / \left( 2 \times 2^{2/3} d \right. \\ & \quad \left. (1 - \operatorname{Sec}[c + d x]) (1 + \operatorname{Sec}[c + d x])^{2/3} \sqrt{-\frac{(1 + \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3})}{(2^{1/3} - (1 + \sqrt{3})) (1 + \operatorname{Sec}[c + d x])^{1/3}}^2}} \right) + \\ & \left( 3^{3/4} (1 - \sqrt{3}) (4 B + C) \operatorname{EllipticF}\left[\operatorname{ArcCos}\left[\frac{2^{1/3} - (1 - \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}\right], \frac{1}{4} (2 + \sqrt{3})\right] \right. \\ & \quad \left. (a + a \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3}) \right. \\ & \quad \left. \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \operatorname{Sec}[c + d x])^{1/3} + (1 + \operatorname{Sec}[c + d x])^{2/3}}{(2^{1/3} - (1 + \sqrt{3})) (1 + \operatorname{Sec}[c + d x])^{1/3}}^2} \operatorname{Tan}[c + d x]} \right) / \left( 4 \times 2^{2/3} d \right. \\ & \quad \left. (1 - \operatorname{Sec}[c + d x]) (1 + \operatorname{Sec}[c + d x])^{2/3} \sqrt{-\frac{(1 + \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3})}{(2^{1/3} - (1 + \sqrt{3})) (1 + \operatorname{Sec}[c + d x])^{1/3}}^2}} \right) \end{aligned}$$

Result (type 6, 5345 leaves):

$$\begin{aligned} & \left( \operatorname{Cos}[c + d x]^2 ((1 + \operatorname{Cos}[c + d x]) \operatorname{Sec}[c + d x])^{1/3} (a (1 + \operatorname{Sec}[c + d x]))^{1/3} \right. \\ & \quad \left. (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \left( \frac{3}{2} (4 B + C) \operatorname{Sin}[c + d x] + \frac{3}{2} C \operatorname{Tan}[c + d x] \right) \right) / \\ & \left( d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) (1 + \operatorname{Sec}[c + d x])^{1/3} \right) - \end{aligned}$$

$$\begin{aligned}
& \left( \cos [c+d x]^2 (a (1+\sec [c+d x]))^{1/3} (A+B \sec [c+d x]+C \sec [c+d x]^2) \right. \\
& \left( 2 A (1+\sec [c+d x])^{1/3}+2 B (1+\sec [c+d x])^{1/3}+\frac{1}{2} C (1+\sec [c+d x])^{1/3}+ \right. \\
& \left. \cos [c+d x] \left( -6 B (1+\sec [c+d x])^{1/3}-\frac{3}{2} C (1+\sec [c+d x])^{1/3} \right) \tan \left[ \frac{1}{2} (c+d x) \right] \right. \\
& \left. \left( \left( 9 (8 A-4 B-C) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2\right] \right) \right) / \right. \\
& \left( 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2\right] + \right. \\
& \left. 2 \left( -3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2\right] + \right. \right. \\
& \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2\right] \right) \tan \left[ \frac{1}{2} (c+d x) \right]^2 \right) + \\
& \left( (4 B+C) \left( 6 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2\right] - \right. \right. \right. \\
& \left. \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2\right] \right) \right. \\
& \left. \cos [c+d x] \sec \left[ \frac{1}{2} (c+d x) \right]^2 \tan \left[ \frac{1}{2} (c+d x) \right]^2+5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \right. \right. \\
& \left. \left. \frac{5}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2\right] \left( -9+8 \tan \left[ \frac{1}{2} (c+d x) \right]^2 \right) \right) \right) / \\
& \left( 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2\right] + \right. \\
& \left. 2 \left( -3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2\right] + \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \right. \\
& \left. \left. \frac{4}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2\right] \right) \tan \left[ \frac{1}{2} (c+d x) \right]^2 \right) \right) / \\
& \left( 2^{2/3} d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \left( \cos \left[ \frac{1}{2} (c+d x) \right]^2 \sec [c+d x] \right)^{2/3} \right. \\
& (1+\sec [c+d x])^{1/3} \\
& \left. \left( -1+\tan \left[ \frac{1}{2} (c+d x) \right]^4 \right) \right. \\
& \left( \frac{1}{\left( \cos \left[ \frac{1}{2} (c+d x) \right]^2 \sec [c+d x] \right)^{2/3} \left( -1+\tan \left[ \frac{1}{2} (c+d x) \right]^4 \right)^2} \right. \\
& 2^{1/3} \sec \left[ \frac{1}{2} (c+d x) \right]^2 \tan \left[ \frac{1}{2} (c+d x) \right]^4 \\
& \left. \left( \left( 9 (8 A-4 B-C) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2\right] \right) \right) / \right. \\
& \left( 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2\right] + \right. \\
& \left. 2 \left( -3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2\right] + \operatorname{AppellF1}\left[ \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & \left. \left( \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + \right. \\
 & \left( (4B+C) \left( 6 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right) \right. \\
 & \quad \left. \cos[c+dx] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 + 5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left( -9 + 8 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \Big/ \\
 & \left( 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad 2 \left( -3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[ \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \Big) - \\
 & \left( 1 \Big/ \left( 2 \times 2^{2/3} \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^{2/3} \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^4 \right) \right) \right) \\
 & \sec\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \left( \left( 9(8A-4B-C) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \Big/ \right. \\
 & \quad \left( 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad 2 \left( -3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[ \right. \right. \\
 & \quad \left. \left. \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + \\
 & \quad \left( (4B+C) \left( 6 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right) \right. \\
 & \quad \left. \cos[c+dx] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 + 5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left( -9 + 8 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \Big/ \\
 & \left( 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad 2 \left( -3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[ \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \Big) - \\
 & \left( 1 \Big/ \left( 2^{2/3} \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^{2/3} \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^4 \right) \right) \right) \\
 & \tan\left[\frac{1}{2}(c+dx)\right]
 \end{aligned}$$

$$\begin{aligned}
& \left( \left( 9(8A-4B-C) \left( -\frac{1}{3} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \right. \right. \\
& \quad \left. \left. \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{1}{9} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \right. \right. \right. \right. \\
& \quad \left. \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \right) \right) / \\
& \left( 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad \left. 2 \left( -3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \operatorname{AppellF1} \left[ \right. \right. \right. \\
& \quad \left. \left. \left. \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) - \\
& \left( 9(8A-4B-C) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \left( 2 \left( -3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \right) \\
& \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + 9 \left( -\frac{1}{3} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \right. \right. \right. \\
& \quad \left. \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \right. \right. \\
& \quad \left. \left. \frac{1}{9} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \right. \\
& \quad \left. \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) + 2 \tan \left[ \frac{1}{2} (c+dx) \right]^2 \left( -\frac{3}{5} \operatorname{AppellF1} \left[ \right. \right. \right. \\
& \quad \left. \left. \left. \frac{5}{2}, \frac{4}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{4}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{7}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] - 3 \left( -\frac{6}{5} \operatorname{AppellF1} \left[ \right. \right. \right. \\
& \quad \left. \left. \left. \frac{5}{2}, \frac{1}{3}, 3, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{1}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \right) \right) \right) / \\
& \left( 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + 2 \right. \\
& \quad \left( -3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \operatorname{AppellF1} \left[ \right. \right. \\
& \quad \left. \left. \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^2 - \\
& \left( (4B+C) \left( 6 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] - \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \\
 & \cos[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + 5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \right. \\
 & \left. 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \left(-9 + 8 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \\
 & \left(2 \left(-3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 15 \left(-\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \right. \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \left. \left. \frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) + 2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left(-\frac{5}{7} \operatorname{AppellF1}\left[\right. \right. \right. \\
 & \left. \left. \frac{7}{2}, \frac{4}{3}, 2, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{20}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{7}{3}, 1, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - 3 \left(-\frac{10}{7} \operatorname{AppellF1}\left[\right. \right. \right. \\
 & \left. \left. \frac{7}{2}, \frac{1}{3}, 3, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{5}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, 2, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)\right)\right) / \\
 & \left(15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \right. \\
 & \left. \left(-3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\right. \right. \right. \\
 & \left. \left. \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^2 + \\
 & \left((4B+C) \left(40 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 6 \left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \right. \right. \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] - \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \right. \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \cos[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4 \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - 6 \left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 - \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right], \\
 & -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sin}[c+dx] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + 6 \\
 & \left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \\
 & \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \operatorname{Cos}[c+dx] \\
 & \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3 + 5 \left(-\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \left. \frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) \left(-9 + 8 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) + 6 \\
 & \operatorname{Cos}[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left(\frac{5}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, 2, \frac{9}{2}, \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - \right. \\
 & \left. \frac{20}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{7}{3}, 1, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 3 \left(-\frac{10}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{1}{3}, 3, \right. \right. \right. \\
 & \left. \left. \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{5}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, 2, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)\right) \Big/ \\
 & \left(15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \left. 2 \left(-3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\right. \right. \right. \\
 & \left. \left. \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)\right) + \\
 & \frac{1}{2^{1/3}} \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx]\right)^{5/3} \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^4\right) \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \\
 & \left(\left(9(8A-4B-C) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right)\right) \Big/ \\
 & \left(9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 \left( -3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + \operatorname{AppellF1} \left[ \right. \right. \\
 & \quad \left. \left. \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + dx) \right]^2 + \\
 & \left( (4B + C) \left( 6 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] - \right. \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) \right. \\
 & \quad \left. \cos [c + dx] \operatorname{Sec} \left[ \frac{1}{2} (c + dx) \right]^2 \tan \left[ \frac{1}{2} (c + dx) \right]^2 + 5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \left( -9 + 8 \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \right) \right) / \\
 & \left( 15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + \right. \\
 & \quad \left. 2 \left( -3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + \operatorname{AppellF1} \left[ \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \\
 & \left( -\cos \left[ \frac{1}{2} (c + dx) \right] \operatorname{Sec} [c + dx] \sin \left[ \frac{1}{2} (c + dx) \right] + \cos \left[ \frac{1}{2} (c + dx) \right]^2 \right. \\
 & \quad \left. \operatorname{Sec} [c + dx] \tan [c + dx] \right) \left. \right) \left. \right) \left. \right)
 \end{aligned}$$

**Problem 631: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \operatorname{Sec} [c + dx] + C \operatorname{Sec} [c + dx]^2}{(a + a \operatorname{Sec} [c + dx])^{2/3}} dx$$

Optimal (type 6, 803 leaves, 11 steps):

$$\begin{aligned}
& - \frac{3 (A - B + C) \operatorname{Tan}[c + d x]}{d (a + a \operatorname{Sec}[c + d x])^{2/3}} + \\
& \left( 3 \sqrt{2} \operatorname{AppellF1}\left[\frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \frac{1}{2} (1 + \operatorname{Sec}[c + d x]), 1 + \operatorname{Sec}[c + d x]\right] (a + a \operatorname{Sec}[c + d x])^{1/3} \right. \\
& \quad \left. \operatorname{Tan}[c + d x] \right) / \left( 5 a d \sqrt{1 - \operatorname{Sec}[c + d x]} \right) - \\
& \frac{3 (1 + \sqrt{3}) (A - B + 2 C) (a + a \operatorname{Sec}[c + d x])^{1/3} \operatorname{Tan}[c + d x]}{a d (1 + \operatorname{Sec}[c + d x])^{2/3} (2^{1/3} - (1 + \sqrt{3})) (1 + \operatorname{Sec}[c + d x])^{1/3}} + \\
& \left( 3 \times 2^{1/3} \times 3^{1/4} (A - B + 2 C) \operatorname{EllipticE}\left[\operatorname{ArcCos}\left[\frac{2^{1/3} - (1 - \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}\right], \frac{1}{4} (2 + \sqrt{3})\right] \right. \\
& \quad \left. (a + a \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3}) \right. \\
& \quad \left. \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \operatorname{Sec}[c + d x])^{1/3} + (1 + \operatorname{Sec}[c + d x])^{2/3}}{(2^{1/3} - (1 + \sqrt{3})) (1 + \operatorname{Sec}[c + d x])^{1/3}} \operatorname{Tan}[c + d x]} \right) / \left( a d (1 - \operatorname{Sec}[c + d x]) \right) \\
& (1 + \operatorname{Sec}[c + d x])^{2/3} \sqrt{-\frac{(1 + \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3})}{(2^{1/3} - (1 + \sqrt{3})) (1 + \operatorname{Sec}[c + d x])^{1/3}} \operatorname{Tan}[c + d x]} + \\
& \left( 3^{3/4} (1 - \sqrt{3}) (A - B + 2 C) \operatorname{EllipticF}\left[\operatorname{ArcCos}\left[\frac{2^{1/3} - (1 - \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}\right], \frac{1}{4} (2 + \sqrt{3})\right] \right. \\
& \quad \left. (a + a \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3}) \right. \\
& \quad \left. \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \operatorname{Sec}[c + d x])^{1/3} + (1 + \operatorname{Sec}[c + d x])^{2/3}}{(2^{1/3} - (1 + \sqrt{3})) (1 + \operatorname{Sec}[c + d x])^{1/3}} \operatorname{Tan}[c + d x]} \right) / \left( 2^{2/3} a d \right. \\
& \quad \left. (1 - \operatorname{Sec}[c + d x]) (1 + \operatorname{Sec}[c + d x])^{2/3} \sqrt{-\frac{(1 + \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3})}{(2^{1/3} - (1 + \sqrt{3})) (1 + \operatorname{Sec}[c + d x])^{1/3}} \operatorname{Tan}[c + d x]} \right)
\end{aligned}$$

Result (type 6, 5389 leaves):

$$\begin{aligned}
& \left( \operatorname{Cos}[c + d x]^2 ((1 + \operatorname{Cos}[c + d x]) \operatorname{Sec}[c + d x])^{1/3} \right. \\
& \quad (1 + \operatorname{Sec}[c + d x])^{2/3} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\
& \quad \left( -6 \operatorname{Sec}\left[\frac{1}{2} (c + d x)\right] \left( A \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right] - B \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right] + C \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right] \right) \right. \\
& \quad \left. \left. + 6 (A - B + 2 C) \operatorname{Sin}[c + d x] \right) \right) / \\
& \left( d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) (a (1 + \operatorname{Sec}[c + d x]))^{2/3} - \right. \\
& \left. \left( 2 \times 2^{1/3} \operatorname{Cos}[c + d x]^2 (1 + \operatorname{Sec}[c + d x])^{2/3} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) \right)
\end{aligned}$$



$$\begin{aligned}
 & \left( 4 A (1 + \sec [c + d x])^{1/3} - 2 B (1 + \sec [c + d x])^{1/3} + 4 C (1 + \sec [c + d x])^{1/3} + \cos [c + d x] \right. \\
 & \quad \left. (-6 A (1 + \sec [c + d x])^{1/3} + 6 B (1 + \sec [c + d x])^{1/3} - 12 C (1 + \sec [c + d x])^{1/3}) \right) \tan \left[ \frac{1}{2} \right. \\
 & \quad \left. (c + d x) \right] \left( \left( 9 (A + B - 2 C) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) / \right. \\
 & \quad \left( 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
 & \quad \left. 2 \left( -3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) + \\
 & \quad \left( (A - B + 2 C) \left( 6 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] - \right. \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \right. \\
 & \quad \left. \cos [c + d x] \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right]^2 + 5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \left( -9 + 8 \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) \right) / \\
 & \quad \left( 15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
 & \quad \left. 2 \left( -3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \operatorname{AppellF1} \left[ \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \frac{4}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) / \\
 & \quad \left( d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \left( \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sec [c + d x] \right)^{2/3} \right. \\
 & \quad \left. (a (1 + \sec [c + d x]))^{2/3} \right. \\
 & \quad \left. (-1 + \tan \left[ \frac{1}{2} (c + d x) \right]^4) \right) \\
 & \quad \left( \frac{1}{\left( \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sec [c + d x] \right)^{2/3} (-1 + \tan \left[ \frac{1}{2} (c + d x) \right]^4)^2} \right. \\
 & \quad \left. 4 \times 2^{1/3} \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right]^4 \right. \\
 & \quad \left( \left( 9 (A + B - 2 C) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) / \right. \\
 & \quad \left( 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
 & \quad \left. 2 \left( -3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \operatorname{AppellF1} \left[ \right. \right. \right. \\
 & \quad \left. \left. \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) + \\
 & \quad \left. \left( (A - B + 2 C) \left( 6 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] - \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \text{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
 & \cos[c+dx] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 + 5 \text{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(-9 + 8 \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \Bigg) / \\
 & \left(15 \text{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \left. 2 \left(-3 \text{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \text{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2\right) - \\
 & \frac{1}{\left(\cos\left[\frac{1}{2}(c+dx)\right]^2 \text{Sec}[c+dx]\right)^{2/3} \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^4\right)} 2^{1/3} \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \left(\left(9(A+B-2C) \text{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) / \right. \\
 & \left(9 \text{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \left. 2 \left(-3 \text{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \text{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2\right) + \\
 & \left.(A-B+2C\right) \left(6 \left(3 \text{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \\
 & \left. \left. \text{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right) \\
 & \cos[c+dx] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 + 5 \text{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(-9 + 8 \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \Bigg) / \\
 & \left(15 \text{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \left. 2 \left(-3 \text{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \text{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2\right) - \\
 & \frac{1}{\left(\cos\left[\frac{1}{2}(c+dx)\right]^2 \text{Sec}[c+dx]\right)^{2/3} \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^4\right)} 2 \times 2^{1/3} \tan\left[\frac{1}{2}(c+dx)\right] \\
 & \left(\left(9(A+B-2C) \left(-\frac{1}{3} \text{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \right. \\
 & \left. \left. \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{9} \text{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) \Bigg) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad 2 \left( -3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \operatorname{AppellF1} \left[ \right. \right. \\
 & \quad \quad \left. \left. \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) - \\
 & \left( 9 (A+B-2C) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
 & \quad \left( 2 \left( -3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \right. \\
 & \quad \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \right) \\
 & \quad \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + 9 \left( -\frac{1}{3} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \right. \right. \\
 & \quad \quad \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \right. \\
 & \quad \left. \frac{1}{9} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \\
 & \quad \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) + 2 \tan \left[ \frac{1}{2} (c+dx) \right]^2 \left( -\frac{3}{5} \operatorname{AppellF1} \left[ \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \frac{4}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \right. \\
 & \quad \left. \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{4}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{7}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] - 3 \left( -\frac{6}{5} \operatorname{AppellF1} \left[ \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{5}{2}, \frac{1}{3}, 3, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \right. \right. \\
 & \quad \quad \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{1}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \right) \right) \Big/ \\
 & \left( 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + 2 \right. \\
 & \quad \left( -3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \operatorname{AppellF1} \left[ \right. \right. \\
 & \quad \quad \left. \left. \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^2 - \\
 & \left( (A-B+2C) \left( 6 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] - \right. \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \right) \\
 & \quad \cos [c+dx] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right]^2 + 5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \right. \\
 & \quad \left. 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \left( -9 + 8 \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right)
 \end{aligned}$$

$$\begin{aligned}
& \left( 2 \left( -3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \right. \\
& \quad \left. \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \\
& \quad \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] + 15 \left( -\frac{3}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \right. \right. \\
& \quad \left. \left. \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] + \right. \\
& \quad \left. \frac{1}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right) + 2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \left( -\frac{5}{7} \operatorname{AppellF1} \left[ \right. \right. \\
& \quad \left. \left. \frac{7}{2}, \frac{4}{3}, 2, \frac{9}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \right. \\
& \quad \left. \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] + \frac{20}{21} \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{7}{3}, 1, \frac{9}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
& \quad \left. \left. -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] - 3 \left( -\frac{10}{7} \operatorname{AppellF1} \left[ \right. \right. \right. \\
& \quad \left. \left. \left. \frac{7}{2}, \frac{1}{3}, 3, \frac{9}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \right. \right. \\
& \quad \left. \left. \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] + \frac{5}{21} \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{4}{3}, 2, \frac{9}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right) \right) \right) / \\
& \left( 15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] + 2 \right. \\
& \quad \left( -3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \operatorname{AppellF1} \left[ \right. \right. \\
& \quad \left. \left. \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right)^2 + \\
& \left( (A-B+2C) \left( 40 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \right. \\
& \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] + 6 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \right. \right. \right. \\
& \quad \left. \left. \left. \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] - \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \right. \right. \right. \\
& \quad \left. \left. \left. \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \operatorname{Cos} [c+dx] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^4 \right. \\
& \quad \left. \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] - 6 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] - \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Sin} [c+dx] \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + 6 \right. \\
& \quad \left. \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] - \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & \text{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \cos[c+dx] \\
 & \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^3 + 5 \left(-\frac{3}{5} \text{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \right. \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \frac{1}{5} \text{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) \left(-9 + 8 \tan\left[\frac{1}{2}(c+dx)\right]^2\right) + 6 \\
 & \cos[c+dx] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left(\frac{5}{7} \text{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, 2, \frac{9}{2}, \right. \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - \right. \\
 & \quad \left. \frac{20}{21} \text{AppellF1}\left[\frac{7}{2}, \frac{7}{3}, 1, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 3 \left(-\frac{10}{7} \text{AppellF1}\left[\frac{7}{2}, \frac{1}{3}, 3, \right. \right. \right. \\
 & \quad \left. \left. \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{5}{21} \text{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, 2, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right)\right) \Big/ \\
 & \left(15 \text{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. 2 \left(-3 \text{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \text{AppellF1}\left[\right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \Big/ \\
 & \quad \quad \quad 1 \\
 & \frac{3 \left(\cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx]\right)^{5/3} \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^4\right)}{2^{1/3}} \\
 & \quad \quad \quad \tan\left[\frac{1}{2}(c+dx)\right] \\
 & \left(\left(9(A+B-2C) \text{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \Big/ \right. \\
 & \quad \left(9 \text{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. 2 \left(-3 \text{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \text{AppellF1}\left[\right. \right. \right. \\
 & \quad \left. \left. \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2\right) + \\
 & \quad \left((A-B+2C) \left(6 \left(3 \text{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned} & \text{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\ & \cos[c+dx] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 + 5 \text{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(-9 + 8 \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) / \\ & \left( 15 \text{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\ & \quad 2 \left( -3 \text{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \text{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\ & \left. \left( -\cos\left[\frac{1}{2}(c+dx)\right] \text{Sec}[c+dx] \sin\left[\frac{1}{2}(c+dx)\right] + \cos\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\ & \quad \left. \left. \text{Sec}[c+dx] \tan[c+dx] \right) \right) \right) \end{aligned}$$

**Problem 632: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2}{(a + a \text{Sec}[c + dx])^{5/3}} dx$$

Optimal (type 6, 856 leaves, 12 steps):

$$\begin{aligned}
 & - \frac{3 (A - B + C) \operatorname{Tan}[c + d x]}{7 d (a + a \operatorname{Sec}[c + d x])^{5/3}} - \frac{3 (2 A - 2 B - 5 C) \operatorname{Tan}[c + d x]}{7 a d (a + a \operatorname{Sec}[c + d x])^{2/3}} \\
 & \left( 3 \sqrt{2} \operatorname{AppellF1}\left[-\frac{1}{6}, \frac{1}{2}, 1, \frac{5}{6}, \frac{1}{2} (1 + \operatorname{Sec}[c + d x]), 1 + \operatorname{Sec}[c + d x]\right] \operatorname{Tan}[c + d x] \right) / \\
 & \left( a d \sqrt{1 - \operatorname{Sec}[c + d x]} (a + a \operatorname{Sec}[c + d x])^{2/3} \right) - \\
 & \frac{3 (1 + \sqrt{3}) (2 A - 2 B - 5 C) (1 + \operatorname{Sec}[c + d x])^{1/3} \operatorname{Tan}[c + d x]}{7 a d (a + a \operatorname{Sec}[c + d x])^{2/3} (2^{1/3} - (1 + \sqrt{3})) (1 + \operatorname{Sec}[c + d x])^{1/3}} + \\
 & \left( 3 \times 2^{1/3} \times 3^{1/4} (2 A - 2 B - 5 C) \operatorname{EllipticE}\left[\operatorname{ArcCos}\left[\frac{2^{1/3} - (1 - \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}\right], \right. \right. \\
 & \left. \left. \frac{1}{4} (2 + \sqrt{3}) \right] (1 + \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3}) \right. \\
 & \left. \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \operatorname{Sec}[c + d x])^{1/3} + (1 + \operatorname{Sec}[c + d x])^{2/3}}{(2^{1/3} - (1 + \sqrt{3})) (1 + \operatorname{Sec}[c + d x])^{1/3}} \operatorname{Tan}[c + d x]} \right) / \left( 7 a d (1 - \operatorname{Sec}[c + d x]) \right) \\
 & (a + a \operatorname{Sec}[c + d x])^{2/3} \sqrt{-\frac{(1 + \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3})}{(2^{1/3} - (1 + \sqrt{3})) (1 + \operatorname{Sec}[c + d x])^{1/3}} \operatorname{Tan}[c + d x]} + \\
 & \left( 3^{3/4} (1 - \sqrt{3}) (2 A - 2 B - 5 C) \operatorname{EllipticF}\left[\operatorname{ArcCos}\left[\frac{2^{1/3} - (1 - \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}\right], \right. \right. \\
 & \left. \left. \frac{1}{4} (2 + \sqrt{3}) \right] (1 + \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3}) \right. \\
 & \left. \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \operatorname{Sec}[c + d x])^{1/3} + (1 + \operatorname{Sec}[c + d x])^{2/3}}{(2^{1/3} - (1 + \sqrt{3})) (1 + \operatorname{Sec}[c + d x])^{1/3}} \operatorname{Tan}[c + d x]} \right) / \left( 7 \times 2^{2/3} a d \right. \\
 & \left. (1 - \operatorname{Sec}[c + d x]) (a + a \operatorname{Sec}[c + d x])^{2/3} \sqrt{-\frac{(1 + \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3})}{(2^{1/3} - (1 + \sqrt{3})) (1 + \operatorname{Sec}[c + d x])^{1/3}} \operatorname{Tan}[c + d x]} \right)
 \end{aligned}$$

Result (type 6, 5507 leaves):

$$\begin{aligned}
 & \left( \operatorname{Cos}[c + d x]^2 ((1 + \operatorname{Cos}[c + d x]) \operatorname{Sec}[c + d x])^{1/3} \right. \\
 & (1 + \operatorname{Sec}[c + d x])^{5/3} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\
 & \left( -\frac{6}{7} \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right] \left( 10 A \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] - 3 B \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] - 4 C \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \right) + \\
 & \frac{3}{7} \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^3 \left( A \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] - B \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] + C \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) + \\
 & \left. \frac{6}{7} (9 A - 2 B - 5 C) \operatorname{Sin}[c + d x] \right) /
 \end{aligned}$$

$$\begin{aligned}
& \left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) (a (1 + \sec [c + dx]))^{5/3} - \right. \\
& \left. 2 \times 2^{1/3} \cos [c + dx]^2 (1 + \sec [c + dx])^{5/3} (A + B \sec [c + dx] + C \sec [c + dx]^2) \right. \\
& \left. \left( \frac{32}{7} A (1 + \sec [c + dx])^{1/3} - \frac{4}{7} B (1 + \sec [c + dx])^{1/3} - \right. \right. \\
& \left. \left. \frac{10}{7} C (1 + \sec [c + dx])^{1/3} + \cos [c + dx] \left( -\frac{54}{7} A (1 + \sec [c + dx])^{1/3} + \right. \right. \right. \\
& \left. \left. \left. \frac{12}{7} B (1 + \sec [c + dx])^{1/3} + \frac{30}{7} C (1 + \sec [c + dx])^{1/3} \right) \right) \tan \left[ \frac{1}{2} (c + dx) \right] \right. \\
& \left. \left( \left( 9 (5A + 2B + 5C) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) / \right. \right. \\
& \left. \left( 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + \right. \right. \\
& \left. \left. 2 \left( -3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + \right. \right. \right. \\
& \left. \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) + \right. \\
& \left. \left( (9A - 2B - 5C) \left( 6 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] - \right. \right. \right. \right. \\
& \left. \left. \left. \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) \right. \right. \\
& \left. \left. \cos [c + dx] \sec \left[ \frac{1}{2} (c + dx) \right]^2 \tan \left[ \frac{1}{2} (c + dx) \right]^2 + 5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \right. \right. \right. \\
& \left. \left. \left. \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \left( -9 + 8 \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \right) \right) / \right. \\
& \left. \left( 15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + \right. \right. \\
& \left. \left. 2 \left( -3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + \operatorname{AppellF1} \left[ \frac{5}{2}, \right. \right. \right. \right. \\
& \left. \left. \left. \frac{4}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \right) / \right. \\
& \left. \left( 7d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \left( \cos \left[ \frac{1}{2} (c + dx) \right]^2 \sec [c + dx] \right)^{2/3} \right. \right. \\
& \left. \left. (a (1 + \sec [c + dx]))^{5/3} \right. \right. \\
& \left. \left. \left( -1 + \tan \left[ \frac{1}{2} (c + dx) \right]^4 \right) \right. \right. \\
& \left. \left. \left( \frac{1}{7 \left( \cos \left[ \frac{1}{2} (c + dx) \right]^2 \sec [c + dx] \right)^{2/3} \left( -1 + \tan \left[ \frac{1}{2} (c + dx) \right]^4 \right)^2} \right. \right. \right. \\
& \left. \left. \left. 4 \times 2^{1/3} \sec \left[ \frac{1}{2} (c + dx) \right]^2 \tan \left[ \frac{1}{2} (c + dx) \right]^4 \right. \right. \right. \\
& \left. \left. \left. \left( \left( 9 (5A + 2B + 5C) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) / \right. \right. \right. \right. \\
& \left. \left. \left. \left( 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + \right. \right. \right. \right.
\end{aligned}$$





$$\begin{aligned}
& \left( \left( 9 (5A + 2B + 5C) \left( -\frac{1}{3} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right. \right. \right. \\
& \quad \left. \left. \left. \operatorname{Sec} \left[ \frac{1}{2} (c + dx) \right]^2 \tan \left[ \frac{1}{2} (c + dx) \right] + \frac{1}{9} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \right. \right. \right. \right. \\
& \quad \left. \left. \left. \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c + dx) \right]^2 \tan \left[ \frac{1}{2} (c + dx) \right] \right) \right) \right) / \\
& \left( 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + \right. \\
& \quad \left. 2 \left( -3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + \operatorname{AppellF1} \left[ \right. \right. \right. \\
& \quad \left. \left. \left. \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) - \\
& \left( 9 (5A + 2B + 5C) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right. \\
& \quad \left( 2 \left( -3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) \right) \\
& \quad \operatorname{Sec} \left[ \frac{1}{2} (c + dx) \right]^2 \tan \left[ \frac{1}{2} (c + dx) \right] + 9 \left( -\frac{1}{3} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c + dx) \right]^2 \tan \left[ \frac{1}{2} (c + dx) \right] + \right. \\
& \quad \left. \frac{1}{9} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right. \\
& \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c + dx) \right]^2 \tan \left[ \frac{1}{2} (c + dx) \right] \right) + 2 \tan \left[ \frac{1}{2} (c + dx) \right]^2 \left( -\frac{3}{5} \operatorname{AppellF1} \left[ \right. \right. \\
& \quad \left. \left. \frac{5}{2}, \frac{4}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c + dx) \right]^2 \right. \\
& \quad \left. \tan \left[ \frac{1}{2} (c + dx) \right] + \frac{4}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{7}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c + dx) \right]^2 \tan \left[ \frac{1}{2} (c + dx) \right] - 3 \left( -\frac{6}{5} \operatorname{AppellF1} \left[ \right. \right. \right. \\
& \quad \left. \left. \left. \frac{5}{2}, \frac{1}{3}, 3, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c + dx) \right]^2 \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c + dx) \right] + \frac{1}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c + dx) \right]^2 \tan \left[ \frac{1}{2} (c + dx) \right] \right) \right) \right) \right) / \\
& \left( 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + 2 \right. \\
& \quad \left( -3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + \operatorname{AppellF1} \left[ \right. \right. \\
& \quad \left. \left. \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right)^2 - \\
& \left( (9A - 2B - 5C) \left( 6 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right. \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \\
 & \cos [c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + 5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \right. \\
 & \left. 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \left(-9+8 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \\
 & \left(2\left(-3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 15\left(-\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \right. \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \left. \left. \frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) + 2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left(-\frac{5}{7} \operatorname{AppellF1}\left[\right. \right. \right. \\
 & \left. \left. \frac{7}{2}, \frac{4}{3}, 2, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{20}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{7}{3}, 1, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - 3\left(-\frac{10}{7} \operatorname{AppellF1}\left[\right. \right. \right. \\
 & \left. \left. \frac{7}{2}, \frac{1}{3}, 3, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{5}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, 2, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)\right)\right) / \\
 & \left(15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \right. \\
 & \left. \left(-3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\right. \right. \right. \\
 & \left. \left. \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^2 + \\
 & \left((9A-2B-5C)\left(40 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 6\left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \right. \right. \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] - \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \right. \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \cos [c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4 \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - 6\left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 - \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right], \\
 & -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sin}[c+dx] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + 6 \\
 & \left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \\
 & \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \operatorname{Cos}[c+dx] \\
 & \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3 + 5 \left(-\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \left. \frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) \left(-9 + 8 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) + 6 \\
 & \operatorname{Cos}[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left(\frac{5}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, 2, \frac{9}{2}, \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - \right. \\
 & \left. \frac{20}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{7}{3}, 1, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 3 \left(-\frac{10}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{1}{3}, 3, \right. \right. \right. \\
 & \left. \left. \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{5}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, 2, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)\right) \Big/ \\
 & \left(15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \left. 2 \left(-3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\right. \right. \right. \\
 & \left. \left. \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)\right) + \\
 & \frac{1}{21} \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx]\right)^{5/3} \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^4\right) \\
 & \frac{4 \times}{2^{1/3}} \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \\
 & \left(\left(9(5A+2B+5C) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right)\right) \Big/ \\
 & \left(9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 \left( -3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + \operatorname{AppellF1} \left[ \right. \right. \\
 & \quad \left. \left. \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + dx) \right]^2 + \\
 & \left( (9A - 2B - 5C) \left( 6 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] - \right. \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) \right. \\
 & \quad \left. \cos [c + dx] \operatorname{Sec} \left[ \frac{1}{2} (c + dx) \right]^2 \tan \left[ \frac{1}{2} (c + dx) \right]^2 + 5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \left( -9 + 8 \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \right) \right) / \\
 & \left( 15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + \right. \\
 & \quad \left. 2 \left( -3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + \operatorname{AppellF1} \left[ \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \\
 & \left( -\cos \left[ \frac{1}{2} (c + dx) \right] \operatorname{Sec} [c + dx] \sin \left[ \frac{1}{2} (c + dx) \right] + \cos \left[ \frac{1}{2} (c + dx) \right]^2 \right. \\
 & \quad \left. \operatorname{Sec} [c + dx] \tan [c + dx] \right) \Big) \Big) \Big)
 \end{aligned}$$

### Problem 633: Unable to integrate problem.

$$\int \operatorname{Sec} [c + dx]^m (a + a \operatorname{Sec} [c + dx])^n (A + B \operatorname{Sec} [c + dx] + C \operatorname{Sec} [c + dx]^2) dx$$

Optimal (type 6, 259 leaves, 8 steps):

$$\begin{aligned}
 & \frac{C \operatorname{Sec} [c + dx]^{1+m} (a + a \operatorname{Sec} [c + dx])^n \sin [c + dx]}{d (1 + m + n)} + \frac{1}{d (1 + m + n)} \\
 & 2^{\frac{3}{2}+n} (C n + B (1 + m + n)) \operatorname{AppellF1} \left[ \frac{1}{2}, 1 - m, -\frac{1}{2} - n, \frac{3}{2}, 1 - \operatorname{Sec} [c + dx], \frac{1}{2} (1 - \operatorname{Sec} [c + dx]) \right] \\
 & (1 + \operatorname{Sec} [c + dx])^{-\frac{1}{2}-n} (a + a \operatorname{Sec} [c + dx])^n \tan [c + dx] + \frac{1}{d (1 + m + n)} \\
 & 2^{\frac{1}{2}+n} (C (m - n) + A (1 + m + n) - B (1 + m + n)) \operatorname{AppellF1} \left[ \frac{1}{2}, 1 - m, \frac{1}{2} - n, \frac{3}{2}, 1 - \operatorname{Sec} [c + dx], \right. \\
 & \quad \left. \frac{1}{2} (1 - \operatorname{Sec} [c + dx]) \right] (1 + \operatorname{Sec} [c + dx])^{-\frac{1}{2}-n} (a + a \operatorname{Sec} [c + dx])^n \tan [c + dx]
 \end{aligned}$$

Result (type 8, 43 leaves):

$$\int \operatorname{Sec} [c + dx]^m (a + a \operatorname{Sec} [c + dx])^n (A + B \operatorname{Sec} [c + dx] + C \operatorname{Sec} [c + dx]^2) dx$$

### Problem 634: Unable to integrate problem.

$$\int \sec [c + d x]^{-1-n} (a + a \sec [c + d x])^n (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 6, 258 leaves, 8 steps):

$$\frac{A \sec [c + d x]^{-n} (a + a \sec [c + d x])^n \sin [c + d x]}{d (1 + n)} +$$

$$\left( (A n + B (1 + n) - C (1 + n)) \operatorname{Hypergeometric2F1} \left[ \frac{1}{2} - n, -n, 1 - n, -\frac{2 \sec [c + d x]}{1 - \sec [c + d x]} \right] \sec [c + d x]^{1-n} \right.$$

$$\left. \left( \frac{1 + \sec [c + d x]}{1 - \sec [c + d x]} \right)^{\frac{1}{2}-n} (a + a \sec [c + d x])^n \sin [c + d x] \right) / (d n (1 + n) (1 + \sec [c + d x])) +$$

$$\frac{1}{d} 2^{\frac{3}{2}+n} C \operatorname{AppellF1} \left[ \frac{1}{2}, 1 + n, -\frac{1}{2} - n, \frac{3}{2}, 1 - \sec [c + d x], \frac{1}{2} (1 - \sec [c + d x]) \right]$$

$$(1 + \sec [c + d x])^{-\frac{1}{2}-n} (a + a \sec [c + d x])^n \tan [c + d x]$$

Result (type 8, 47 leaves):

$$\int \sec [c + d x]^{-1-n} (a + a \sec [c + d x])^n (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

### Problem 636: Result more than twice size of optimal antiderivative.

$$\int (a + a \sec [c + d x])^m (B - C + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 6, 171 leaves, 8 steps):

$$\left( \sqrt{2} (B - C) \operatorname{AppellF1} \left[ \frac{3}{2} + m, \frac{1}{2}, 1, \frac{5}{2} + m, \frac{1}{2} (1 + \sec [c + d x]), 1 + \sec [c + d x] \right] \right.$$

$$\left. (1 + \sec [c + d x]) (a + a \sec [c + d x])^m \tan [c + d x] \right) / (d (3 + 2m) \sqrt{1 - \sec [c + d x]}) +$$

$$\frac{1}{d} 2^{\frac{3}{2}+m} C \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, -\frac{1}{2} - m, \frac{3}{2}, \frac{1}{2} (1 - \sec [c + d x]) \right]$$

$$(1 + \sec [c + d x])^{-\frac{1}{2}-m} (a + a \sec [c + d x])^m \tan [c + d x]$$

Result (type 6, 2582 leaves):

$$\left( 2^{1+m} \cos \left[ \frac{1}{2} (c + d x) \right] \cos [c + d x] \left( \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sec [c + d x] \right)^m (1 + \sec [c + d x])^{-1-m} \right.$$

$$\left. (a (1 + \sec [c + d x]))^{1+m} (B - C + C \sec [c + d x]) (2 C \sec [c + d x]^2 (1 + \sec [c + d x])^m + \right.$$

$$\left. \sec [c + d x] (2 B (1 + \sec [c + d x])^m - 2 C (1 + \sec [c + d x])^m) \right)$$

$$\sin \left[ \frac{1}{2} (c + d x) \right] \left( (B - C) \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, 1 + m, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + 2 C \right.$$

$$\left. \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, 2 + m, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \left( \cos [c + d x] \sec \left[ \frac{1}{2} (c + d x) \right]^2 \right)^m +$$

$$\left( 3 (B - C) \operatorname{AppellF1} \left[ \frac{1}{2}, m, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \cos \left[ \frac{1}{2} (c + d x) \right]^2 \right) /$$

$$\begin{aligned}
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, m, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \\
 & \quad \left. 2 \left( \operatorname{AppellF1}\left[\frac{3}{2}, m, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - m \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. \left. 1+m, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \\
 & \left( a d (C+B \cos[c+dx] - C \cos[c+dx]) \left( 2^m \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx] \right)^m \right. \right. \\
 & \quad \left. \left( \left( (B-C) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1+m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 C \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. 2+m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \left( \cos[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right)^m + \left( 3(B-C) \right. \right. \\
 & \quad \quad \left. \operatorname{AppellF1}\left[\frac{1}{2}, m, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \cos\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \\
 & \quad \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, m, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \\
 & \quad \left. 2 \left( \operatorname{AppellF1}\left[\frac{3}{2}, m, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - m \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. \left. 1+m, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
 & 2^{1+m} \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx] \right)^m \tan\left[\frac{1}{2}(c+dx)\right] \\
 & \left( m \left( (B-C) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1+m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 C \operatorname{Hypergeometric2F1}\left[ \right. \right. \right. \\
 & \quad \quad \left. \left. \left. \frac{1}{2}, 2+m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \left( \cos[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right)^{-1+m} \right. \\
 & \quad \left. \left( -\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \sin[c+dx] + \cos[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) - \\
 & \quad \left( 3(B-C) \operatorname{AppellF1}\left[\frac{1}{2}, m, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \cos\left[\frac{1}{2}(c+dx)\right] \right. \\
 & \quad \left. \sin\left[\frac{1}{2}(c+dx)\right] \right) / \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, m, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \\
 & \quad \left. 2 \left( \operatorname{AppellF1}\left[\frac{3}{2}, m, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - m \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. \left. 1+m, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + \\
 & \quad \left( 3(B-C) \cos\left[\frac{1}{2}(c+dx)\right]^2 \left( -\frac{1}{3} \operatorname{AppellF1}\left[\frac{3}{2}, m, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[ \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. \frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{3} m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, 1, \right. \right. \right. \\
 & \quad \quad \left. \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) / \\
 & \quad \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, m, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \\
 & \quad \left. 2 \left( \operatorname{AppellF1}\left[\frac{3}{2}, m, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - m \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 1+m, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \Big) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Big) - \\
 & \left( 3(B-C) \operatorname{AppellF1}\left[\frac{1}{2}, m, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \cos\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \left. -2 \left( \operatorname{AppellF1}\left[\frac{3}{2}, m, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - m \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. 1+m, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2} \right. \right. \\
 & \quad \quad \left. \left. (c+dx)\right] + 3 \left( -\frac{1}{3} \operatorname{AppellF1}\left[\frac{3}{2}, m, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \quad \quad \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{3} m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, 1, \frac{5}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) - \\
 & 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( -\frac{6}{5} \operatorname{AppellF1}\left[\frac{5}{2}, m, 3, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \frac{3}{5} m \operatorname{AppellF1}\left[\frac{5}{2}, 1+m, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - m \left( -\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, 1+m, 2, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
 & \quad \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{3}{5} (1+m) \operatorname{AppellF1}\left[\frac{5}{2}, 2+m, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \Big) \Big) / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, m, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \\
 & \quad \left. 2 \left( \operatorname{AppellF1}\left[\frac{3}{2}, m, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - m \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. 1+m, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 + \\
 & \left( \cos[c+dx] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right)^m \left( C \csc\left[\frac{1}{2}(c+dx)\right] \sec\left[\frac{1}{2}(c+dx)\right] \right. \\
 & \quad \left( -\operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 2+m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. \left( 1 - \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^{-2-m} \right) + \\
 & \quad \frac{1}{2} (B-C) \csc\left[\frac{1}{2}(c+dx)\right] \sec\left[\frac{1}{2}(c+dx)\right] \left( -\operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \right. \right. \\
 & \quad \quad \left. \left. 1+m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \left( 1 - \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^{-1-m} \right) \right) \Big) + \\
 & 2^{1+m} m \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^{-1+m} \tan\left[\frac{1}{2}(c+dx)\right]
 \end{aligned}$$



$$\left( \left( (B-C) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1+m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2C \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 2+m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \left( \cos[c+dx] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right)^m + \left( 3(B-C) \operatorname{AppellF1}\left[\frac{1}{2}, m, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \cos\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, m, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \left( \operatorname{AppellF1}\left[\frac{3}{2}, m, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( -\cos\left[\frac{1}{2}(c+dx)\right] \sec[c+dx] \sin\left[\frac{1}{2}(c+dx)\right] + \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \tan[c+dx] \right) \right)$$

**Problem 637: Result more than twice size of optimal antiderivative.**

$$\int \sec[c+dx]^3 (a+b \sec[c+dx]) (A+C \sec[c+dx]^2) dx$$

Optimal (type 3, 140 leaves, 7 steps):

$$\frac{a(4A+3C) \operatorname{ArcTanh}[\sin[c+dx]]}{8d} + \frac{b(5A+4C) \tan[c+dx]}{5d} + \frac{a(4A+3C) \sec[c+dx] \tan[c+dx]}{8d} + \frac{aC \sec[c+dx]^3 \tan[c+dx]}{4d} + \frac{bC \sec[c+dx]^4 \tan[c+dx]}{5d} + \frac{b(5A+4C) \tan[c+dx]^3}{15d}$$

Result (type 3, 426 leaves):

$$\begin{aligned}
 & - \frac{a A \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right]}{2d} - \frac{3 a C \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right]}{8d} + \\
 & \frac{a A \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right]}{2d} + \frac{3 a C \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right]}{8d} + \\
 & \frac{16 d \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^4}{3 a C} + \frac{4 d \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^2}{a A} + \\
 & \frac{16 d \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^2}{a A} - \frac{16 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^4}{3 a C} - \\
 & \frac{4 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^2}{3 a C} - \frac{16 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^2}{3 a C} + \\
 & \frac{2 A b \operatorname{Tan}[c+dx]}{3 d} + \frac{8 b C \operatorname{Tan}[c+dx]}{15 d} + \frac{A b \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx]}{3 d} + \\
 & \frac{4 b C \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx]}{15 d} + \frac{b C \operatorname{Sec}[c+dx]^4 \operatorname{Tan}[c+dx]}{5 d}
 \end{aligned}$$

**Problem 638: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c+dx]^2 (a+b \operatorname{Sec}[c+dx]) (A+C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 3, 117 leaves, 7 steps):

$$\begin{aligned}
 & \frac{b (4 A + 3 C) \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{8 d} + \frac{a (3 A + 2 C) \operatorname{Tan}[c+dx]}{3 d} + \\
 & \frac{b (4 A + 3 C) \operatorname{Sec}[c+dx] \operatorname{Tan}[c+dx]}{8 d} + \frac{a C \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx]}{3 d} + \frac{b C \operatorname{Sec}[c+dx]^3 \operatorname{Tan}[c+dx]}{4 d}
 \end{aligned}$$

Result (type 3, 377 leaves):

$$\begin{aligned}
 & - \frac{A b \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right]}{2d} - \frac{3 b C \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right]}{8d} + \\
 & \frac{A b \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right]}{2d} + \frac{3 b C \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right]}{8d} + \\
 & \frac{16 d \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^4}{3 b C} + \frac{4 d \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^2}{b C} + \\
 & \frac{16 d \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^2}{A b} - \frac{16 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^4}{3 b C} - \\
 & \frac{4 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^2}{3 b C} - \frac{16 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^2}{3 b C} + \\
 & \frac{a A \operatorname{Tan}[c+dx]}{d} + \frac{2 a C \operatorname{Tan}[c+dx]}{3 d} + \frac{a C \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx]}{3 d}
 \end{aligned}$$

**Problem 640: Result more than twice size of optimal antiderivative.**

$$\int (a + b \sec [c + d x]) (A + C \sec [c + d x]^2) dx$$

Optimal (type 3, 58 leaves, 5 steps):

$$a A x + \frac{b (2 A + C) \operatorname{ArcTanh}[\sin [c + d x]]}{2 d} + \frac{a C \tan [c + d x]}{d} + \frac{b C \sec [c + d x] \tan [c + d x]}{2 d}$$

Result (type 3, 218 leaves):

$$\begin{aligned} a A x - \frac{A b \operatorname{Log}\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d} + \\ \frac{A b \operatorname{Log}\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] - b C \operatorname{Log}\left[\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right]}{2 d} + \\ \frac{b C \operatorname{Log}\left[\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right]}{2 d} + \frac{b C}{4 d \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right)^2} - \\ \frac{b C}{4 d \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right)^2} + \frac{a C \tan [c + d x]}{d} \end{aligned}$$

**Problem 641: Result more than twice size of optimal antiderivative.**

$$\int \cos [c + d x] (a + b \sec [c + d x]) (A + C \sec [c + d x]^2) dx$$

Optimal (type 3, 42 leaves, 5 steps):

$$A b x + \frac{a C \operatorname{ArcTanh}[\sin [c + d x]]}{d} + \frac{a A \sin [c + d x]}{d} + \frac{b C \tan [c + d x]}{d}$$

Result (type 3, 112 leaves):

$$\begin{aligned} A b x - \frac{a C \operatorname{Log}\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d} + \frac{a C \operatorname{Log}\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d} + \\ \frac{a A \cos [d x] \sin [c]}{d} + \frac{a A \cos [c] \sin [d x]}{d} + \frac{b C \tan [c + d x]}{d} \end{aligned}$$

**Problem 642: Result more than twice size of optimal antiderivative.**

$$\int \cos [c + d x]^2 (a + b \sec [c + d x]) (A + C \sec [c + d x]^2) dx$$

Optimal (type 3, 58 leaves, 5 steps):

$$\frac{1}{2} a (A + 2 C) x + \frac{b C \operatorname{ArcTanh}[\sin [c + d x]]}{d} + \frac{A b \sin [c + d x]}{d} + \frac{a A \cos [c + d x] \sin [c + d x]}{2 d}$$

Result (type 3, 131 leaves):

$$\begin{aligned}
 & a C x + \frac{a A (c + d x)}{2 d} - \frac{b C \operatorname{Log}\left[\cos\left[\frac{c}{2} + \frac{d x}{2}\right] - \sin\left[\frac{c}{2} + \frac{d x}{2}\right]\right]}{d} + \frac{b C \operatorname{Log}\left[\cos\left[\frac{c}{2} + \frac{d x}{2}\right] + \sin\left[\frac{c}{2} + \frac{d x}{2}\right]\right]}{d} + \\
 & \frac{A b \cos[d x] \sin[c]}{d} + \frac{A b \cos[c] \sin[d x]}{d} + \frac{a A \sin[2(c + d x)]}{4 d}
 \end{aligned}$$

**Problem 647: Result more than twice size of optimal antiderivative.**

$$\int \sec[c + d x] (a + b \sec[c + d x])^2 (A + C \sec[c + d x])^2 dx$$

Optimal (type 3, 170 leaves, 7 steps):

$$\begin{aligned}
 & \frac{(4 a^2 (2 A + C) + b^2 (4 A + 3 C)) \operatorname{ArcTanh}[\sin[c + d x]]}{8 d} + \\
 & \frac{a (12 A b^2 - a^2 C + 8 b^2 C) \tan[c + d x]}{6 b d} - \frac{(2 a^2 C - 3 b^2 (4 A + 3 C)) \sec[c + d x] \tan[c + d x]}{24 d} - \\
 & \frac{a C (a + b \sec[c + d x])^2 \tan[c + d x]}{12 b d} + \frac{C (a + b \sec[c + d x])^3 \tan[c + d x]}{4 b d}
 \end{aligned}$$

Result (type 3, 1123 leaves):

$$\begin{aligned}
 & \left( (-8 a^2 A - 4 A b^2 - 4 a^2 C - 3 b^2 C) \operatorname{Cos}[c + d x]^4 \right. \\
 & \quad \left. \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] (a + b \operatorname{Sec}[c + d x])^2 (A + C \operatorname{Sec}[c + d x]^2)\right) / \\
 & \quad \left( 4 d (b + a \operatorname{Cos}[c + d x])^2 (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) \right) + \\
 & \left( (8 a^2 A + 4 A b^2 + 4 a^2 C + 3 b^2 C) \operatorname{Cos}[c + d x]^4 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right) \\
 & \quad \left( a + b \operatorname{Sec}[c + d x] \right)^2 (A + C \operatorname{Sec}[c + d x]^2) \Big/ \\
 & \quad \left( 4 d (b + a \operatorname{Cos}[c + d x])^2 (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) \right) + \\
 & \left( b^2 C \operatorname{Cos}[c + d x]^4 (a + b \operatorname{Sec}[c + d x])^2 (A + C \operatorname{Sec}[c + d x]^2) \right) / \\
 & \quad \left( 8 d (b + a \operatorname{Cos}[c + d x])^2 (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^4 \right) + \\
 & \left( (12 A b^2 + 12 a^2 C + 8 a b C + 9 b^2 C) \operatorname{Cos}[c + d x]^4 (a + b \operatorname{Sec}[c + d x])^2 (A + C \operatorname{Sec}[c + d x]^2) \right) / \\
 & \quad \left( 24 d (b + a \operatorname{Cos}[c + d x])^2 (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^2 \right) + \\
 & \left( 2 a b C \operatorname{Cos}[c + d x]^4 (a + b \operatorname{Sec}[c + d x])^2 (A + C \operatorname{Sec}[c + d x]^2) \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) / \\
 & \quad \left( 3 d (b + a \operatorname{Cos}[c + d x])^2 (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^3 \right) - \\
 & \left( b^2 C \operatorname{Cos}[c + d x]^4 (a + b \operatorname{Sec}[c + d x])^2 (A + C \operatorname{Sec}[c + d x]^2) \right) / \\
 & \quad \left( 8 d (b + a \operatorname{Cos}[c + d x])^2 (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^4 \right) + \\
 & \left( 2 a b C \operatorname{Cos}[c + d x]^4 (a + b \operatorname{Sec}[c + d x])^2 (A + C \operatorname{Sec}[c + d x]^2) \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) / \\
 & \quad \left( 3 d (b + a \operatorname{Cos}[c + d x])^2 (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^3 \right) + \\
 & \left( (-12 A b^2 - 12 a^2 C - 8 a b C - 9 b^2 C) \operatorname{Cos}[c + d x]^4 (a + b \operatorname{Sec}[c + d x])^2 (A + C \operatorname{Sec}[c + d x]^2) \right) / \\
 & \quad \left( 24 d (b + a \operatorname{Cos}[c + d x])^2 (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^2 \right) + \\
 & \left( 4 \operatorname{Cos}[c + d x]^4 (a + b \operatorname{Sec}[c + d x])^2 (A + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \quad \left. \left( 3 a A b \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] + 2 a b C \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \right) / \\
 & \quad \left( 3 d (b + a \operatorname{Cos}[c + d x])^2 (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \right) + \\
 & \left( 4 \operatorname{Cos}[c + d x]^4 (a + b \operatorname{Sec}[c + d x])^2 (A + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \quad \left. \left( 3 a A b \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] + 2 a b C \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \right) / \\
 & \quad \left( 3 d (b + a \operatorname{Cos}[c + d x])^2 (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \right)
 \end{aligned}$$

### Problem 648: Result more than twice size of optimal antiderivative.

$$\int (a + b \operatorname{Sec}[c + d x])^2 (A + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 3, 103 leaves, 6 steps):

$$a^2 A x + \frac{a b (2 A + C) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{d} + \frac{(3 A b^2 + 2 (a^2 + b^2) C) \operatorname{Tan}[c + d x]}{3 d} +$$

$$\frac{a b C \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x]}{3 d} + \frac{C (a + b \operatorname{Sec}[c + d x])^2 \operatorname{Tan}[c + d x]}{3 d}$$

Result (type 3, 242 leaves):

$$\frac{1}{12 d} \operatorname{Sec}[c + d x]^3 \left( 9 a \operatorname{Cos}[c + d x] \left( a A (c + d x) - b (2 A + C) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right]\right) + \right.$$

$$\left. b (2 A + C) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right]\right) +$$

$$3 a \operatorname{Cos}[3(c + d x)] \left( a A (c + d x) - b (2 A + C) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right]\right) +$$

$$\left. b (2 A + C) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right]\right) +$$

$$2 (3 A b^2 + 3 a^2 C + 4 b^2 C + 6 a b C \operatorname{Cos}[c + d x] + (3 A b^2 + 3 a^2 C + 2 b^2 C) \operatorname{Cos}[2(c + d x)])$$

$$\operatorname{Sin}[c + d x]$$

### Problem 649: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cos}[c + d x] (a + b \operatorname{Sec}[c + d x])^2 (A + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 3, 109 leaves, 6 steps):

$$2 a A b x + \frac{(2 A b^2 + (2 a^2 + b^2) C) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{2 d} + \frac{A (a + b \operatorname{Sec}[c + d x])^2 \operatorname{Sin}[c + d x]}{d} -$$

$$\frac{2 a b (A - C) \operatorname{Tan}[c + d x]}{d} - \frac{b^2 (2 A - C) \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x]}{2 d}$$

Result (type 3, 352 leaves):

$$\begin{aligned}
 & \frac{1}{4d} \operatorname{Sec}[c+dx]^2 \left( 4aAbc + 4aAbdx - 2Ab^2 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - \right. \\
 & \quad \left. 2a^2C \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - \right. \\
 & \quad \left. b^2C \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + 2Ab^2 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \right) + \\
 & \quad \left. 2a^2C \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + \right. \\
 & \quad \left. b^2C \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + \operatorname{Cos}[2(c+dx)] \right. \\
 & \quad \left( 4aAb(c+dx) - (2Ab^2 + (2a^2 + b^2)C) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \right) + \\
 & \quad \left. (2Ab^2 + 2a^2C + b^2C) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \right) + \\
 & \quad \left. (a^2A + 2b^2C) \operatorname{Sin}[c+dx] + 4abc \operatorname{Sin}[2(c+dx)] + a^2A \operatorname{Sin}[3(c+dx)] \right)
 \end{aligned}$$

### Problem 656: Result more than twice size of optimal antiderivative.

$$\int (a+b \operatorname{Sec}[c+dx])^3 (A+C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 3, 167 leaves, 7 steps):

$$\begin{aligned}
 & a^3 Ax + \frac{b(12a^2(2A+C) + b^2(4A+3C)) \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{8d} + \\
 & \frac{a(6Ab^2 + (a^2 + 4b^2)C) \operatorname{Tan}[c+dx]}{2d} + \frac{b(2a^2C + b^2(4A+3C)) \operatorname{Sec}[c+dx] \operatorname{Tan}[c+dx]}{8d} + \\
 & \frac{aC(a+b \operatorname{Sec}[c+dx])^2 \operatorname{Tan}[c+dx]}{4d} + \frac{C(a+b \operatorname{Sec}[c+dx])^3 \operatorname{Tan}[c+dx]}{4d}
 \end{aligned}$$

Result (type 3, 1241 leaves):

$$\begin{aligned}
 & \frac{2a^3A(c+dx) \operatorname{Cos}[c+dx]^5 (a+b \operatorname{Sec}[c+dx])^3 (A+C \operatorname{Sec}[c+dx]^2)}{d(b+a \operatorname{Cos}[c+dx])^3 (A+2C+A \operatorname{Cos}[2c+2dx])} + \\
 & \left( (-24a^2Ab - 4Ab^3 - 12a^2bC - 3b^3C) \operatorname{Cos}[c+dx]^5 \right. \\
 & \quad \left. \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] (a+b \operatorname{Sec}[c+dx])^3 (A+C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \left( 4d(b+a \operatorname{Cos}[c+dx])^3 (A+2C+A \operatorname{Cos}[2c+2dx]) \right) + \\
 & \left( (24a^2Ab + 4Ab^3 + 12a^2bC + 3b^3C) \operatorname{Cos}[c+dx]^5 \right. \\
 & \quad \left. \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] (a+b \operatorname{Sec}[c+dx])^3 (A+C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \left( 4d(b+a \operatorname{Cos}[c+dx])^3 (A+2C+A \operatorname{Cos}[2c+2dx]) \right) + \\
 & \left( b^3C \operatorname{Cos}[c+dx]^5 (a+b \operatorname{Sec}[c+dx])^3 (A+C \operatorname{Sec}[c+dx]^2) \right) /
 \end{aligned}$$

$$\begin{aligned}
& \left( 8 d (b + a \cos [c + d x])^3 (A + 2 C + A \cos [2 c + 2 d x]) \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^4 \right) + \\
& \left( 4 A b^3 + 12 a^2 b C + 4 a b^2 C + 3 b^3 C \right) \cos [c + d x]^5 (a + b \sec [c + d x])^3 (A + C \sec [c + d x]^2) \Big/ \\
& \left( 8 d (b + a \cos [c + d x])^3 (A + 2 C + A \cos [2 c + 2 d x]) \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right) + \\
& \left( a b^2 C \cos [c + d x]^5 (a + b \sec [c + d x])^3 (A + C \sec [c + d x]^2) \sin \left[ \frac{1}{2} (c + d x) \right] \right) \Big/ \\
& \left( d (b + a \cos [c + d x])^3 (A + 2 C + A \cos [2 c + 2 d x]) \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^3 \right) - \\
& \left( b^3 C \cos [c + d x]^5 (a + b \sec [c + d x])^3 (A + C \sec [c + d x]^2) \right) \Big/ \\
& \left( 8 d (b + a \cos [c + d x])^3 (A + 2 C + A \cos [2 c + 2 d x]) \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^4 \right) + \\
& \left( a b^2 C \cos [c + d x]^5 (a + b \sec [c + d x])^3 (A + C \sec [c + d x]^2) \sin \left[ \frac{1}{2} (c + d x) \right] \right) \Big/ \\
& \left( d (b + a \cos [c + d x])^3 (A + 2 C + A \cos [2 c + 2 d x]) \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^3 \right) + \\
& \left( -4 A b^3 - 12 a^2 b C - 4 a b^2 C - 3 b^3 C \right) \cos [c + d x]^5 (a + b \sec [c + d x])^3 (A + C \sec [c + d x]^2) \Big/ \\
& \left( 8 d (b + a \cos [c + d x])^3 (A + 2 C + A \cos [2 c + 2 d x]) \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right) + \\
& \left( 2 \cos [c + d x]^5 (a + b \sec [c + d x])^3 (A + C \sec [c + d x]^2) \right. \\
& \quad \left. \left( 3 a A b^2 \sin \left[ \frac{1}{2} (c + d x) \right] + a^3 C \sin \left[ \frac{1}{2} (c + d x) \right] + 2 a b^2 C \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) \Big/ \\
& \left( d (b + a \cos [c + d x])^3 (A + 2 C + A \cos [2 c + 2 d x]) \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) + \\
& \left( 2 \cos [c + d x]^5 (a + b \sec [c + d x])^3 (A + C \sec [c + d x]^2) \right. \\
& \quad \left. \left( 3 a A b^2 \sin \left[ \frac{1}{2} (c + d x) \right] + a^3 C \sin \left[ \frac{1}{2} (c + d x) \right] + 2 a b^2 C \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) \Big/ \\
& \left( d (b + a \cos [c + d x])^3 (A + 2 C + A \cos [2 c + 2 d x]) \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right)
\end{aligned}$$

**Problem 665: Result more than twice size of optimal antiderivative.**

$$\int (a + b \sec [c + d x])^4 (A + C \sec [c + d x]^2) dx$$

Optimal (type 3, 227 leaves, 8 steps):



$$\begin{aligned}
 & a^4 A x + \frac{a b (4 a^2 (2 A + C) + b^2 (4 A + 3 C)) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{2 d} + \\
 & \frac{(6 a^4 C + 2 b^4 (5 A + 4 C) + a^2 b^2 (85 A + 56 C)) \operatorname{Tan}[c + d x]}{15 d} + \\
 & \frac{a b (40 A b^2 + 6 a^2 C + 29 b^2 C) \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x]}{30 d} + \\
 & \frac{(3 a^2 C + b^2 (5 A + 4 C)) (a + b \operatorname{Sec}[c + d x])^2 \operatorname{Tan}[c + d x]}{15 d} + \\
 & \frac{a C (a + b \operatorname{Sec}[c + d x])^3 \operatorname{Tan}[c + d x]}{5 d} + \frac{C (a + b \operatorname{Sec}[c + d x])^4 \operatorname{Tan}[c + d x]}{5 d}
 \end{aligned}$$

Result (type 3, 503 leaves):

$$\begin{aligned}
 & \frac{1}{120 d (A + 2 C + A \operatorname{Cos}[2 (c + d x)])} (C + A \operatorname{Cos}[c + d x])^2 \operatorname{Sec}[c + d x]^5 \\
 & \left( 150 a^4 A (c + d x) \operatorname{Cos}[c + d x] + 75 a^4 A (c + d x) \operatorname{Cos}[3 (c + d x)] + 15 a^4 A c \operatorname{Cos}[5 (c + d x)] + \right. \\
 & 15 a^4 A d x \operatorname{Cos}[5 (c + d x)] - 120 a b (4 a^2 (2 A + C) + b^2 (4 A + 3 C)) \operatorname{Cos}[c + d x]^5 \\
 & \left. \left( \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2} (c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]\right] - \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2} (c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]\right] \right) + \right. \\
 & 180 a^2 A b^2 \operatorname{Sin}[c + d x] + 40 A b^4 \operatorname{Sin}[c + d x] + 30 a^4 C \operatorname{Sin}[c + d x] + \\
 & 240 a^2 b^2 C \operatorname{Sin}[c + d x] + 80 b^4 C \operatorname{Sin}[c + d x] + 120 a A b^3 \operatorname{Sin}[2 (c + d x)] + \\
 & 120 a^3 b C \operatorname{Sin}[2 (c + d x)] + 210 a b^3 C \operatorname{Sin}[2 (c + d x)] + 270 a^2 A b^2 \operatorname{Sin}[3 (c + d x)] + \\
 & 50 A b^4 \operatorname{Sin}[3 (c + d x)] + 45 a^4 C \operatorname{Sin}[3 (c + d x)] + 300 a^2 b^2 C \operatorname{Sin}[3 (c + d x)] + \\
 & 40 b^4 C \operatorname{Sin}[3 (c + d x)] + 60 a A b^3 \operatorname{Sin}[4 (c + d x)] + 60 a^3 b C \operatorname{Sin}[4 (c + d x)] + \\
 & 45 a b^3 C \operatorname{Sin}[4 (c + d x)] + 90 a^2 A b^2 \operatorname{Sin}[5 (c + d x)] + 10 A b^4 \operatorname{Sin}[5 (c + d x)] + \\
 & \left. 15 a^4 C \operatorname{Sin}[5 (c + d x)] + 60 a^2 b^2 C \operatorname{Sin}[5 (c + d x)] + 8 b^4 C \operatorname{Sin}[5 (c + d x)] \right)
 \end{aligned}$$

**Problem 666: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Cos}[c + d x] (a + b \operatorname{Sec}[c + d x])^4 (A + C \operatorname{Sec}[c + d x])^2 dx$$

Optimal (type 3, 229 leaves, 8 steps):

$$\begin{aligned}
 & 4 a^3 A b x + \frac{(8 a^4 C + 24 a^2 b^2 (2 A + C) + b^4 (4 A + 3 C)) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{8 d} + \\
 & \frac{A (a + b \operatorname{Sec}[c + d x])^4 \operatorname{Sin}[c + d x]}{d} - \frac{a b (a^2 (12 A - 19 C) - 8 b^2 (3 A + 2 C)) \operatorname{Tan}[c + d x]}{6 d} - \\
 & \frac{b^2 (a^2 (24 A - 26 C) - 3 b^2 (4 A + 3 C)) \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x]}{24 d} - \\
 & \frac{a b (12 A - 7 C) (a + b \operatorname{Sec}[c + d x])^2 \operatorname{Tan}[c + d x]}{12 d} - \frac{b (4 A - C) (a + b \operatorname{Sec}[c + d x])^3 \operatorname{Tan}[c + d x]}{4 d}
 \end{aligned}$$

Result (type 3, 1357 leaves):

$$\begin{aligned}
 & \left( 8 a^3 A b (c + d x) \operatorname{Cos}[c + d x]^6 (a + b \operatorname{Sec}[c + d x])^4 (A + C \operatorname{Sec}[c + d x])^2 \right) / \\
 & \left( d (b + a \operatorname{Cos}[c + d x])^4 (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) \right) +
 \end{aligned}$$

$$\begin{aligned}
& \left( (-48 a^2 A b^2 - 4 A b^4 - 8 a^4 C - 24 a^2 b^2 C - 3 b^4 C) \cos [c + d x]^6 \right. \\
& \quad \left. \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] (a + b \sec [c + d x])^4 (A + C \sec [c + d x]^2) \right) / \\
& \quad \left( 4 d (b + a \cos [c + d x])^4 (A + 2 C + A \cos [2 c + 2 d x]) \right) + \\
& \left( (48 a^2 A b^2 + 4 A b^4 + 8 a^4 C + 24 a^2 b^2 C + 3 b^4 C) \cos [c + d x]^6 \right. \\
& \quad \left. \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] (a + b \sec [c + d x])^4 (A + C \sec [c + d x]^2) \right) / \\
& \quad \left( 4 d (b + a \cos [c + d x])^4 (A + 2 C + A \cos [2 c + 2 d x]) \right) + \\
& \left( b^4 C \cos [c + d x]^6 (a + b \sec [c + d x])^4 (A + C \sec [c + d x]^2) \right) / \\
& \quad \left( 8 d (b + a \cos [c + d x])^4 (A + 2 C + A \cos [2 c + 2 d x]) \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^4 \right) + \\
& \left( (12 A b^4 + 72 a^2 b^2 C + 16 a b^3 C + 9 b^4 C) \cos [c + d x]^6 (a + b \sec [c + d x])^4 (A + C \sec [c + d x]^2) \right) / \\
& \quad \left( 24 d (b + a \cos [c + d x])^4 (A + 2 C + A \cos [2 c + 2 d x]) \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right) + \\
& \left( 4 a b^3 C \cos [c + d x]^6 (a + b \sec [c + d x])^4 (A + C \sec [c + d x]^2) \sin \left[ \frac{1}{2} (c + d x) \right] \right) / \\
& \quad \left( 3 d (b + a \cos [c + d x])^4 (A + 2 C + A \cos [2 c + 2 d x]) \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^3 \right) - \\
& \left( b^4 C \cos [c + d x]^6 (a + b \sec [c + d x])^4 (A + C \sec [c + d x]^2) \right) / \\
& \quad \left( 8 d (b + a \cos [c + d x])^4 (A + 2 C + A \cos [2 c + 2 d x]) \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^4 \right) + \\
& \left( 4 a b^3 C \cos [c + d x]^6 (a + b \sec [c + d x])^4 (A + C \sec [c + d x]^2) \sin \left[ \frac{1}{2} (c + d x) \right] \right) / \\
& \quad \left( 3 d (b + a \cos [c + d x])^4 (A + 2 C + A \cos [2 c + 2 d x]) \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^3 \right) + \\
& \left( (-12 A b^4 - 72 a^2 b^2 C - 16 a b^3 C - 9 b^4 C) \cos [c + d x]^6 (a + b \sec [c + d x])^4 (A + C \sec [c + d x]^2) \right) / \\
& \quad \left( 24 d (b + a \cos [c + d x])^4 (A + 2 C + A \cos [2 c + 2 d x]) \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right) + \\
& \left( 8 \cos [c + d x]^6 (a + b \sec [c + d x])^4 (A + C \sec [c + d x]^2) \right. \\
& \quad \left. \left( 3 a A b^3 \sin \left[ \frac{1}{2} (c + d x) \right] + 3 a^3 b C \sin \left[ \frac{1}{2} (c + d x) \right] + 2 a b^3 C \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) / \\
& \quad \left( 3 d (b + a \cos [c + d x])^4 (A + 2 C + A \cos [2 c + 2 d x]) \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) + \\
& \left( 8 \cos [c + d x]^6 (a + b \sec [c + d x])^4 (A + C \sec [c + d x]^2) \right. \\
& \quad \left. \left( 3 a A b^3 \sin \left[ \frac{1}{2} (c + d x) \right] + 3 a^3 b C \sin \left[ \frac{1}{2} (c + d x) \right] + 2 a b^3 C \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) / \\
& \quad \left( 3 d (b + a \cos [c + d x])^4 (A + 2 C + A \cos [2 c + 2 d x]) \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) +
\end{aligned}$$

$$\left( 2 a^4 A \cos [c+d x]^6 (a+b \sec [c+d x])^4 (A+C \sec [c+d x]^2) \sin [c+d x] \right) / \left( d (b+a \cos [c+d x])^4 (A+2 C+A \cos [2 c+2 d x]) \right)$$

**Problem 667: Result more than twice size of optimal antiderivative.**

$$\int \cos [c+d x]^2 (a+b \sec [c+d x])^4 (A+C \sec [c+d x]^2) dx$$

Optimal (type 3, 219 leaves, 8 steps):

$$\begin{aligned} & \frac{1}{2} a^2 (12 A b^2 + a^2 (A+2 C)) x + \frac{2 a b (2 A b^2 + (2 a^2 + b^2) C) \operatorname{ArcTanh}[\sin [c+d x]]}{d} + \\ & \frac{2 A b (a+b \sec [c+d x])^3 \sin [c+d x]}{d} + \frac{A \cos [c+d x] (a+b \sec [c+d x])^4 \sin [c+d x]}{2 d} - \\ & \frac{b^2 (a^2 (39 A - 34 C) - 2 b^2 (3 A + 2 C)) \tan [c+d x]}{6 d} - \\ & \frac{a b^3 (9 A - 4 C) \sec [c+d x] \tan [c+d x]}{3 d} - \frac{b^2 (15 A - 2 C) (a+b \sec [c+d x])^2 \tan [c+d x]}{6 d} \end{aligned}$$

Result (type 3, 864 leaves):

$$\begin{aligned}
& \frac{a^2 (a^2 A + 12 A b^2 + 2 a^2 C) (c + d x) \cos [c + d x]^4 (a + b \sec [c + d x])^4}{2 d (b + a \cos [c + d x])^4} - \\
& \left( 2 (2 a A b^3 + 2 a^3 b C + a b^3 C) \cos [c + d x]^4 \right. \\
& \quad \left. \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] (a + b \sec [c + d x])^4 \right) / (d (b + a \cos [c + d x])^4) + \\
& \left( 2 (2 a A b^3 + 2 a^3 b C + a b^3 C) \cos [c + d x]^4 \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] \right. \\
& \quad \left. (a + b \sec [c + d x])^4 \right) / (d (b + a \cos [c + d x])^4) + \\
& \frac{(12 a b^3 C + b^4 C) \cos [c + d x]^4 (a + b \sec [c + d x])^4}{12 d (b + a \cos [c + d x])^4 \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2} + \\
& \frac{b^4 C \cos [c + d x]^4 (a + b \sec [c + d x])^4 \sin \left[ \frac{1}{2} (c + d x) \right]}{6 d (b + a \cos [c + d x])^4 \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^3} + \\
& \frac{b^4 C \cos [c + d x]^4 (a + b \sec [c + d x])^4 \sin \left[ \frac{1}{2} (c + d x) \right]}{6 d (b + a \cos [c + d x])^4 \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^3} + \\
& \frac{(-12 a b^3 C - b^4 C) \cos [c + d x]^4 (a + b \sec [c + d x])^4}{12 d (b + a \cos [c + d x])^4 \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2} + \\
& \left( \cos [c + d x]^4 (a + b \sec [c + d x])^4 \right. \\
& \quad \left. \left( 3 A b^4 \sin \left[ \frac{1}{2} (c + d x) \right] + 18 a^2 b^2 C \sin \left[ \frac{1}{2} (c + d x) \right] + 2 b^4 C \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) / \\
& \left( 3 d (b + a \cos [c + d x])^4 \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) + \\
& \left( \cos [c + d x]^4 (a + b \sec [c + d x])^4 \right. \\
& \quad \left. \left( 3 A b^4 \sin \left[ \frac{1}{2} (c + d x) \right] + 18 a^2 b^2 C \sin \left[ \frac{1}{2} (c + d x) \right] + 2 b^4 C \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) / \\
& \left( 3 d (b + a \cos [c + d x])^4 \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) + \\
& \frac{4 a^3 A b \cos [c + d x]^4 (a + b \sec [c + d x])^4 \sin [c + d x]}{d (b + a \cos [c + d x])^4} + \\
& \frac{a^4 A \cos [c + d x]^4 (a + b \sec [c + d x])^4 \sin [2 (c + d x)]}{4 d (b + a \cos [c + d x])^4}
\end{aligned}$$

**Problem 673: Result more than twice size of optimal antiderivative.**

$$\int (a + b \sec [c + d x])^3 (a^2 - b^2 \sec [c + d x]^2) dx$$

Optimal (type 3, 158 leaves, 8 steps):

$$\begin{aligned}
 & a^5 x + \frac{b (24 a^4 - 8 a^2 b^2 - 3 b^4) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{8 d} + \\
 & \frac{a b^2 (5 a^2 - 4 b^2) \operatorname{Tan}[c + d x]}{2 d} + \frac{b^3 (2 a^2 - 3 b^2) \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x]}{8 d} - \\
 & \frac{a b^2 (a + b \operatorname{Sec}[c + d x])^2 \operatorname{Tan}[c + d x]}{4 d} - \frac{b^2 (a + b \operatorname{Sec}[c + d x])^3 \operatorname{Tan}[c + d x]}{4 d}
 \end{aligned}$$

Result (type 3, 1299 leaves):

$$\begin{aligned}
 & \frac{2 a^5 (c + d x) \operatorname{Cos}[c + d x]^5 (a + b \operatorname{Sec}[c + d x])^3 (a^2 - b^2 \operatorname{Sec}[c + d x]^2)}{d (b + a \operatorname{Cos}[c + d x])^3 (a^2 - 2 b^2 + a^2 \operatorname{Cos}[2 c + 2 d x])} + \\
 & \left( (-24 a^4 b + 8 a^2 b^3 + 3 b^5) \operatorname{Cos}[c + d x]^5 \right. \\
 & \quad \left. \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] (a + b \operatorname{Sec}[c + d x])^3 (a^2 - b^2 \operatorname{Sec}[c + d x]^2)\right) / \\
 & \left( 4 d (b + a \operatorname{Cos}[c + d x])^3 (a^2 - 2 b^2 + a^2 \operatorname{Cos}[2 c + 2 d x]) \right) + \\
 & \left( (24 a^4 b - 8 a^2 b^3 - 3 b^5) \operatorname{Cos}[c + d x]^5 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] (a + b \operatorname{Sec}[c + d x])^3 \right. \\
 & \quad \left. (a^2 - b^2 \operatorname{Sec}[c + d x]^2)\right) / \left( 4 d (b + a \operatorname{Cos}[c + d x])^3 (a^2 - 2 b^2 + a^2 \operatorname{Cos}[2 c + 2 d x]) \right) - \\
 & \left( b^5 \operatorname{Cos}[c + d x]^5 (a + b \operatorname{Sec}[c + d x])^3 (a^2 - b^2 \operatorname{Sec}[c + d x]^2) \right) / \\
 & \left( 8 d (b + a \operatorname{Cos}[c + d x])^3 (a^2 - 2 b^2 + a^2 \operatorname{Cos}[2 c + 2 d x]) \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^4 \right) + \\
 & \left( (-8 a^2 b^3 - 4 a b^4 - 3 b^5) \operatorname{Cos}[c + d x]^5 (a + b \operatorname{Sec}[c + d x])^3 (a^2 - b^2 \operatorname{Sec}[c + d x]^2) \right) / \\
 & \left( 8 d (b + a \operatorname{Cos}[c + d x])^3 (a^2 - 2 b^2 + a^2 \operatorname{Cos}[2 c + 2 d x]) \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^2 \right) - \\
 & \left( a b^4 \operatorname{Cos}[c + d x]^5 (a + b \operatorname{Sec}[c + d x])^3 (a^2 - b^2 \operatorname{Sec}[c + d x]^2) \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) / \\
 & \left( d (b + a \operatorname{Cos}[c + d x])^3 (a^2 - 2 b^2 + a^2 \operatorname{Cos}[2 c + 2 d x]) \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^3 \right) + \\
 & \left( b^5 \operatorname{Cos}[c + d x]^5 (a + b \operatorname{Sec}[c + d x])^3 (a^2 - b^2 \operatorname{Sec}[c + d x]^2) \right) / \\
 & \left( 8 d (b + a \operatorname{Cos}[c + d x])^3 (a^2 - 2 b^2 + a^2 \operatorname{Cos}[2 c + 2 d x]) \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^4 \right) - \\
 & \left( a b^4 \operatorname{Cos}[c + d x]^5 (a + b \operatorname{Sec}[c + d x])^3 (a^2 - b^2 \operatorname{Sec}[c + d x]^2) \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) / \\
 & \left( d (b + a \operatorname{Cos}[c + d x])^3 (a^2 - 2 b^2 + a^2 \operatorname{Cos}[2 c + 2 d x]) \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^3 \right) + \\
 & \left( (8 a^2 b^3 + 4 a b^4 + 3 b^5) \operatorname{Cos}[c + d x]^5 (a + b \operatorname{Sec}[c + d x])^3 (a^2 - b^2 \operatorname{Sec}[c + d x]^2) \right) / \\
 & \left( 8 d (b + a \operatorname{Cos}[c + d x])^3 (a^2 - 2 b^2 + a^2 \operatorname{Cos}[2 c + 2 d x]) \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^2 \right) - \\
 & \left( 4 \operatorname{Cos}[c + d x]^5 (a + b \operatorname{Sec}[c + d x])^3 (a^2 - b^2 \operatorname{Sec}[c + d x]^2) \right)
 \end{aligned}$$

$$\begin{aligned} & \left( -a^3 b^2 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + a b^4 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) / \\ & \left( d (b+a \operatorname{Cos}[c+dx])^3 (a^2-2b^2+a^2 \operatorname{Cos}[2c+2dx]) \left( \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \right) - \\ & \left( 4 \operatorname{Cos}[c+dx]^5 (a+b \operatorname{Sec}[c+dx])^3 (a^2-b^2 \operatorname{Sec}[c+dx]^2) \right. \\ & \left. \left( -a^3 b^2 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + a b^4 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \right) / \\ & \left( d (b+a \operatorname{Cos}[c+dx])^3 (a^2-2b^2+a^2 \operatorname{Cos}[2c+2dx]) \left( \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \right) \end{aligned}$$

**Problem 675: Result more than twice size of optimal antiderivative.**

$$\int (a+b \operatorname{Sec}[c+dx]) (a^2-b^2 \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 3, 75 leaves, 6 steps):

$$a^3 x + \frac{b(2a^2-b^2) \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{2d} - \frac{a b^2 \operatorname{Tan}[c+dx]}{2d} - \frac{b^2(a+b \operatorname{Sec}[c+dx]) \operatorname{Tan}[c+dx]}{2d}$$

Result (type 3, 230 leaves):

$$\begin{aligned} & a^3 x - \frac{a^2 b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] - \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d} + \\ & \frac{a^2 b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d} + \frac{b^3 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{2d} - \\ & \frac{b^3 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{2d} - \frac{b^3}{4d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^2} + \\ & \frac{b^3}{4d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^2} - \frac{a b^2 \operatorname{Tan}[c+dx]}{d} \end{aligned}$$

**Problem 676: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c+dx]^3 (A+C \operatorname{Sec}[c+dx]^2)}{a+b \operatorname{Sec}[c+dx]} dx$$

Optimal (type 3, 186 leaves, 8 steps):

$$\begin{aligned} & - \frac{a(2Ab^2+(2a^2+b^2)C) \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{2b^4 d} + \frac{2a^2(Ab^2+a^2C) \operatorname{ArcTanh}\left[\frac{\sqrt{a-b} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a+b}}\right]}{\sqrt{a-b} b^4 \sqrt{a+b} d} + \\ & \frac{(3a^2 C+b^2(3A+2C)) \operatorname{Tan}[c+dx]}{3b^3 d} - \frac{aC \operatorname{Sec}[c+dx] \operatorname{Tan}[c+dx]}{2b^2 d} + \frac{C \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx]}{3b d} \end{aligned}$$

Result (type 3, 657 leaves):

$$\begin{aligned}
 & \frac{1}{6 b^4 d (A + 2 C + A \cos [2 (c + d x)]) (a + b \sec [c + d x])} \cos [c + d x] (b + a \cos [c + d x]) \\
 & (A + C \sec [c + d x]^2) \left( 6 a (2 A b^2 + (2 a^2 + b^2) C) \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] - \right. \\
 & 6 a (2 A b^2 + (2 a^2 + b^2) C) \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] - \\
 & \left. \left( 24 i a^2 (A b^2 + a^2 C) \operatorname{ArcTan} \left[ \frac{(i \cos [c] + \sin [c]) (a \sin [c] + (-b + a \cos [c]) \tan \left[ \frac{d x}{2} \right])}{\sqrt{a^2 - b^2} \sqrt{(\cos [c] - i \sin [c])^2}} \right] \right) \right. \\
 & \left. (\cos [c] - i \sin [c]) \right) \left/ \left( \sqrt{a^2 - b^2} \sqrt{(\cos [c] - i \sin [c])^2} \right) + \right. \\
 & \frac{2 b^3 C \sin \left[ \frac{d x}{2} \right]}{\left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^3} + \\
 & \frac{b^2 C \left( (-3 a + b) \cos \left[ \frac{c}{2} \right] + (3 a + b) \sin \left[ \frac{c}{2} \right] \right)}{\left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2} + \\
 & \frac{4 b (3 A b^2 + 3 a^2 C + 2 b^2 C) \sin \left[ \frac{d x}{2} \right]}{\left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)} + \\
 & \frac{2 b^3 C \sin \left[ \frac{d x}{2} \right]}{\left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^3} + \\
 & \frac{b^2 C \left( (3 a - b) \cos \left[ \frac{c}{2} \right] + (3 a + b) \sin \left[ \frac{c}{2} \right] \right)}{\left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2} + \\
 & \left. \frac{4 b (3 A b^2 + 3 a^2 C + 2 b^2 C) \sin \left[ \frac{d x}{2} \right]}{\left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)} \right)
 \end{aligned}$$

**Problem 677: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c + d x]^2 (A + C \sec [c + d x]^2)}{a + b \sec [c + d x]} dx$$

Optimal (type 3, 137 leaves, 7 steps):

$$\frac{(2 a^2 C + b^2 (2 A + C)) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{2 b^3 d} - \frac{2 a (A b^2 + a^2 C) \operatorname{ArcTanh}\left[\frac{\sqrt{a-b} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a+b}}\right]}{\sqrt{a-b} b^3 \sqrt{a+b} d} - \frac{a C \operatorname{Tan}[c + d x]}{b^2 d} + \frac{C \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x]}{2 b d}$$

Result (type 3, 428 leaves):

$$\frac{1}{2 b^3 d (A + 2 C + A \operatorname{Cos}[2(c + d x)]) (a + b \operatorname{Sec}[c + d x])} \operatorname{Cos}[c + d x] (b + a \operatorname{Cos}[c + d x])$$

$$(A + C \operatorname{Sec}[c + d x]^2) \left( -2 (2 A b^2 + (2 a^2 + b^2) C) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + \right.$$

$$\left. 2 (2 A b^2 + (2 a^2 + b^2) C) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + \left( 8 a (A b^2 + a^2 C) \right. \right.$$

$$\left. \operatorname{ArcTan}\left[\frac{(i \operatorname{Cos}[c] + \operatorname{Sin}[c]) (a \operatorname{Sin}[c] + (-b + a \operatorname{Cos}[c]) \operatorname{Tan}\left[\frac{d x}{2}\right])}{\sqrt{a^2 - b^2} \sqrt{(\operatorname{Cos}[c] - i \operatorname{Sin}[c])^2}}\right] (i \operatorname{Cos}[c] + \operatorname{Sin}[c]) \right) /$$

$$\left( \sqrt{a^2 - b^2} \sqrt{(\operatorname{Cos}[c] - i \operatorname{Sin}[c])^2} \right) + \frac{b^2 C}{(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right])^2} -$$

$$\frac{4 a b C \operatorname{Sin}\left[\frac{d x}{2}\right]}{(\operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right]) (\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right])} -$$

$$\frac{b^2 C}{(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right])^2} -$$

$$\left. \frac{4 a b C \operatorname{Sin}\left[\frac{d x}{2}\right]}{(\operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right]) (\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right])} \right)$$

**Problem 678: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c + d x] (A + C \operatorname{Sec}[c + d x]^2)}{a + b \operatorname{Sec}[c + d x]} dx$$

Optimal (type 3, 95 leaves, 6 steps):

$$- \frac{a C \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{b^2 d} + \frac{2 (A b^2 + a^2 C) \operatorname{ArcTanh}\left[\frac{\sqrt{a-b} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a+b}}\right]}{\sqrt{a-b} b^2 \sqrt{a+b} d} + \frac{C \operatorname{Tan}[c + d x]}{b d}$$

Result (type 3, 331 leaves):



$$\begin{aligned}
 & \frac{1}{b^2 d (A + 2 C + A \cos [2 (c + d x)]) (a + b \sec [c + d x])} \\
 & \frac{2 \cos [c + d x] (b + a \cos [c + d x]) (A + C \sec [c + d x])^2}{\left( a C \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] - a C \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right) - \right.} \\
 & \left. \left( 2 i (A b^2 + a^2 C) \operatorname{ArcTan} \left[ \frac{(i \cos [c] + \sin [c]) (a \sin [c] + (-b + a \cos [c]) \tan \left[ \frac{dx}{2} \right])}{\sqrt{a^2 - b^2} \sqrt{(\cos [c] - i \sin [c])^2}} \right] \right) \right. \\
 & \left. (\cos [c] - i \sin [c]) \right) / \left( \sqrt{a^2 - b^2} \sqrt{(\cos [c] - i \sin [c])^2} \right) + \\
 & \frac{b C \sin \left[ \frac{dx}{2} \right]}{\left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)} + \\
 & \left. \frac{b C \sin \left[ \frac{dx}{2} \right]}{\left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)} \right)
 \end{aligned}$$

**Problem 679: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{A + C \sec [c + d x]^2}{a + b \sec [c + d x]} dx$$

Optimal (type 3, 88 leaves, 6 steps):

$$\frac{A x}{a} + \frac{C \operatorname{ArcTanh}[\sin [c + d x]]}{b d} - \frac{2 (A b^2 + a^2 C) \operatorname{ArcTanh} \left[ \frac{\sqrt{a-b} \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a+b}} \right]}{a \sqrt{a-b} b \sqrt{a+b} d}$$

Result (type 3, 239 leaves):

$$\begin{aligned}
 & \left( 2 (C + A \cos [c + d x])^2 \left( \sqrt{a^2 - b^2} \left( A b d x - a C \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] + \right. \right. \right. \\
 & \left. \left. a C \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] \right) \sqrt{(\cos [c] - i \sin [c])^2} + 2 (A b^2 + a^2 C) \right. \\
 & \left. \operatorname{ArcTan} \left[ \frac{(i \cos [c] + \sin [c]) (a \sin [c] + (-b + a \cos [c]) \tan \left[ \frac{dx}{2} \right])}{\sqrt{a^2 - b^2} \sqrt{(\cos [c] - i \sin [c])^2}} \right] (i \cos [c] + \sin [c]) \right) \right) / \\
 & \left( a b \sqrt{a^2 - b^2} d (A + 2 C + A \cos [2 (c + d x)]) \sqrt{(\cos [c] - i \sin [c])^2} \right)
 \end{aligned}$$

### Problem 685: Result more than twice size of optimal antiderivative.

$$\int \frac{\sec [c+d x]^2 (A+C \sec [c+d x]^2)}{(a+b \sec [c+d x])^2} dx$$

Optimal (type 3, 153 leaves, 7 steps):

$$\frac{2 a C \operatorname{ArcTanh}[\sin [c+d x]]}{b^3 d} - \frac{2 (A b^4 - 2 a^4 C + 3 a^2 b^2 C) \operatorname{ArcTanh}\left[\frac{\sqrt{a-b} \tan\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a+b}}\right]}{(a-b)^{3/2} b^3 (a+b)^{3/2} d} +$$

$$\frac{C \tan [c+d x]}{b^2 d} + \frac{a (A b^2 + a^2 C) \tan [c+d x]}{b^2 (a^2 - b^2) d (a+b \sec [c+d x])}$$

Result (type 3, 336 leaves):

$$\frac{1}{b^3 d (A+2 C+A \cos [2(c+d x)]) (a+b \sec [c+d x])^2} 2 (b+a \cos [c+d x]) (A+C \sec [c+d x])^2$$

$$\left( \frac{1}{(a^2 - b^2)^{3/2}} 2 (A b^4 - 2 a^4 C + 3 a^2 b^2 C) \operatorname{ArcTanh}\left[\frac{(-a+b) \tan\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2 - b^2}}\right] (b+a \cos [c+d x]) + \right.$$

$$2 a C (b+a \cos [c+d x]) \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+d x)\right] - \sin\left[\frac{1}{2}(c+d x)\right]\right] - 2 a C (b+a \cos [c+d x])$$

$$\operatorname{Log}\left[\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right] + \frac{b C (b+a \cos [c+d x]) \sin\left[\frac{1}{2}(c+d x)\right]}{\cos\left[\frac{1}{2}(c+d x)\right] - \sin\left[\frac{1}{2}(c+d x)\right]} +$$

$$\left. \frac{b C (b+a \cos [c+d x]) \sin\left[\frac{1}{2}(c+d x)\right]}{\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]} + \frac{a b (A b^2 + a^2 C) \sin [c+d x]}{(a-b)(a+b)} \right)$$

### Problem 686: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\sec [c+d x] (A+C \sec [c+d x]^2)}{(a+b \sec [c+d x])^2} dx$$

Optimal (type 3, 135 leaves, 6 steps):

$$\frac{C \operatorname{ArcTanh}[\sin [c+d x]]}{b^2 d} +$$

$$\frac{2 a (A b^2 - a^2 C + 2 b^2 C) \operatorname{ArcTanh}\left[\frac{\sqrt{a-b} \tan\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a+b}}\right]}{(a-b)^{3/2} b^2 (a+b)^{3/2} d} - \frac{(A b^2 + a^2 C) \tan [c+d x]}{b (a^2 - b^2) d (a+b \sec [c+d x])}$$

Result (type 3, 331 leaves):

$$\frac{1}{b^2 d (A + 2C + A \cos[2(c + dx)]) (a + b \sec[c + dx])^2} \left( (b + a \cos[c + dx])^2 \right. \\
 (A + C \sec[c + dx])^2 \left( -C (b + a \cos[c + dx]) \log\left[\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right] + \right. \\
 \left. C (b + a \cos[c + dx]) \log\left[\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right] + \right. \\
 \left. \left( 2a (-Ab^2 + (a^2 - 2b^2)C) \operatorname{ArcTan}\left[\frac{(i \cos[c] + \sin[c]) (a \sin[c] + (-b + a \cos[c]) \tan[\frac{dx}{2}])}{\sqrt{a^2 - b^2} \sqrt{(\cos[c] - i \sin[c])^2}}\right] \right) \right. \\
 \left. (b + a \cos[c + dx]) (i \cos[c] + \sin[c]) \right) / \left( (a^2 - b^2)^{3/2} \sqrt{(\cos[c] - i \sin[c])^2} + \right. \\
 \left. \frac{b (Ab^2 + a^2C) (b \sin[c] - a \sin[dx])}{a (a - b) (a + b) \left(\cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right]\right) \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right]\right)} \right)$$

**Problem 687: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{A + C \sec[c + dx]^2}{(a + b \sec[c + dx])^2} dx$$

Optimal (type 3, 125 leaves, 5 steps):

$$\frac{Ax}{a^2} - \frac{2b(2a^2A - Ab^2 + a^2C) \operatorname{ArcTanh}\left[\frac{\sqrt{a-b} \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a+b}}\right]}{a^2(a-b)^{3/2}(a+b)^{3/2}d} + \frac{(Ab^2 + a^2C) \tan[c + dx]}{a(a^2 - b^2)d(a + b \sec[c + dx])}$$

Result (type 3, 270 leaves):

$$\left( 2(b + a \cos[c + dx]) (A + C \sec[c + dx])^2 \left( Ax (b + a \cos[c + dx]) + \right. \right. \\
 \left. \left( 2b (-Ab^2 + a^2(2A + C)) \operatorname{ArcTan}\left[\frac{(i \cos[c] + \sin[c]) (a \sin[c] + (-b + a \cos[c]) \tan[\frac{dx}{2}])}{\sqrt{a^2 - b^2} \sqrt{(\cos[c] - i \sin[c])^2}}\right] \right) \right. \\
 \left. (b + a \cos[c + dx]) (i \cos[c] + \sin[c]) \right) / \left( (a^2 - b^2)^{3/2} d \sqrt{(\cos[c] - i \sin[c])^2} + \right. \\
 \left. \frac{(Ab^2 + a^2C) (-b \sin[c] + a \sin[dx])}{(a - b) (a + b) d \left(\cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right]\right) \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right]\right)} \right) / \\
 (a^2 (A + 2C + A \cos[2(c + dx)]) (a + b \sec[c + dx])^2)$$

**Problem 691: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Sec}[c + d x]^4 (A + C \text{Sec}[c + d x]^2)}{(a + b \text{Sec}[c + d x])^3} dx$$

Optimal (type 3, 381 leaves, 9 steps):

$$\frac{(2 A b^2 + (12 a^2 + b^2) C) \text{ArcTanh}[\text{Sin}[c + d x]]}{2 b^5 d} - \left( a (6 A b^6 + a^4 b^2 (2 A - 29 C) - 5 a^2 b^4 (A - 4 C) + 12 a^6 C) \text{ArcTanh}\left[\frac{\sqrt{a - b} \text{Tan}\left[\frac{1}{2} (c + d x)\right]}{\sqrt{a + b}}\right] \right) / \left( (a - b)^{5/2} b^5 (a + b)^{5/2} d - \frac{a (a^2 b^2 (2 A - 21 C) - b^4 (5 A - 6 C) + 12 a^4 C) \text{Tan}[c + d x]}{2 b^4 (a^2 - b^2)^2 d} + \frac{(a^2 b^2 (A - 10 C) - b^4 (4 A - C) + 6 a^4 C) \text{Sec}[c + d x] \text{Tan}[c + d x]}{2 b^3 (a^2 - b^2)^2 d} - \frac{(A b^2 + a^2 C) \text{Sec}[c + d x]^3 \text{Tan}[c + d x]}{2 b (a^2 - b^2) d (a + b \text{Sec}[c + d x])^2} + \frac{(3 A b^4 - 4 a^4 C + 7 a^2 b^2 C) \text{Sec}[c + d x]^2 \text{Tan}[c + d x]}{2 b^2 (a^2 - b^2)^2 d (a + b \text{Sec}[c + d x])} \right)$$

Result (type 3, 1028 leaves):

$$\begin{aligned}
 & \left( 2 a (2 a^4 A b^2 - 5 a^2 A b^4 + 6 A b^6 + 12 a^6 C - 29 a^4 b^2 C + 20 a^2 b^4 C) \right. \\
 & \quad \left. \operatorname{ArcTanh} \left[ \frac{(-a+b) \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{\sqrt{a^2-b^2}} \right] (b+a \operatorname{Cos}[c+d x])^3 \operatorname{Sec}[c+d x] (A+C \operatorname{Sec}[c+d x]^2) \right) / \\
 & \quad \left( b^5 \sqrt{a^2-b^2} (-a^2+b^2)^2 d (A+2 C+A \operatorname{Cos}[2 c+2 d x]) (a+b \operatorname{Sec}[c+d x])^3 \right) + \\
 & \quad \left( (-2 A b^2 - 12 a^2 C - b^2 C) (b+a \operatorname{Cos}[c+d x])^3 \operatorname{Log} \left[ \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right] - \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right] \right] \right. \\
 & \quad \left. \operatorname{Sec}[c+d x] (A+C \operatorname{Sec}[c+d x]^2) \right) / \left( b^5 d (A+2 C+A \operatorname{Cos}[2 c+2 d x]) (a+b \operatorname{Sec}[c+d x])^3 \right) + \\
 & \quad \left( (2 A b^2 + 12 a^2 C + b^2 C) (b+a \operatorname{Cos}[c+d x])^3 \operatorname{Log} \left[ \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right] + \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right] \right] \right. \\
 & \quad \left. \operatorname{Sec}[c+d x] (A+C \operatorname{Sec}[c+d x]^2) \right) / \left( b^5 d (A+2 C+A \operatorname{Cos}[2 c+2 d x]) (a+b \operatorname{Sec}[c+d x])^3 \right) + \\
 & \quad \left( C (b+a \operatorname{Cos}[c+d x])^3 \operatorname{Sec}[c+d x] (A+C \operatorname{Sec}[c+d x]^2) \right) / \\
 & \quad \left( 2 b^3 d (A+2 C+A \operatorname{Cos}[2 c+2 d x]) (a+b \operatorname{Sec}[c+d x])^3 \left( \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right] - \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right] \right)^2 \right) - \\
 & \quad \left( 6 a C (b+a \operatorname{Cos}[c+d x])^3 \operatorname{Sec}[c+d x] (A+C \operatorname{Sec}[c+d x]^2) \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right] \right) / \\
 & \quad \left( b^4 d (A+2 C+A \operatorname{Cos}[2 c+2 d x]) (a+b \operatorname{Sec}[c+d x])^3 \left( \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right] - \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right] \right) \right) - \\
 & \quad \left( C (b+a \operatorname{Cos}[c+d x])^3 \operatorname{Sec}[c+d x] (A+C \operatorname{Sec}[c+d x]^2) \right) / \\
 & \quad \left( 2 b^3 d (A+2 C+A \operatorname{Cos}[2 c+2 d x]) (a+b \operatorname{Sec}[c+d x])^3 \left( \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right] + \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right] \right)^2 \right) - \\
 & \quad \left( 6 a C (b+a \operatorname{Cos}[c+d x])^3 \operatorname{Sec}[c+d x] (A+C \operatorname{Sec}[c+d x]^2) \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right] \right) / \\
 & \quad \left( b^4 d (A+2 C+A \operatorname{Cos}[2 c+2 d x]) (a+b \operatorname{Sec}[c+d x])^3 \left( \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right] + \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right] \right) \right) + \\
 & \quad \left( (b+a \operatorname{Cos}[c+d x]) \operatorname{Sec}[c+d x] (A+C \operatorname{Sec}[c+d x]^2) (a^2 A b^2 \operatorname{Sin}[c+d x] + a^4 C \operatorname{Sin}[c+d x]) \right) / \\
 & \quad \left( b^3 (-a+b) (a+b) d (A+2 C+A \operatorname{Cos}[2 c+2 d x]) (a+b \operatorname{Sec}[c+d x])^3 \right) + \\
 & \quad \left( (b+a \operatorname{Cos}[c+d x])^2 \operatorname{Sec}[c+d x] (A+C \operatorname{Sec}[c+d x]^2) \right. \\
 & \quad \left. (-2 a^4 A b^2 \operatorname{Sin}[c+d x] + 5 a^2 A b^4 \operatorname{Sin}[c+d x] - 6 a^6 C \operatorname{Sin}[c+d x] + 9 a^4 b^2 C \operatorname{Sin}[c+d x]) \right) / \\
 & \quad \left( b^4 (-a+b)^2 (a+b)^2 d (A+2 C+A \operatorname{Cos}[2 c+2 d x]) (a+b \operatorname{Sec}[c+d x])^3 \right)
 \end{aligned}$$

**Problem 693: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c+d x]^2 (A+C \operatorname{Sec}[c+d x]^2)}{(a+b \operatorname{Sec}[c+d x])^3} dx$$

Optimal (type 3, 212 leaves, 7 steps):

$$\frac{C \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{b^3 d} - \frac{a (3 A b^4 + (2 a^4 - 5 a^2 b^2 + 6 b^4) C) \operatorname{ArcTanh}\left[\frac{\sqrt{a-b} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a+b}}\right]}{(a-b)^{5/2} b^3 (a+b)^{5/2} d} +$$

$$\frac{a (A b^2 + a^2 C) \operatorname{Tan}[c + d x]}{2 b^2 (a^2 - b^2) d (a + b \operatorname{Sec}[c + d x])^2} + \frac{(2 A b^4 - 3 a^4 C + a^2 b^2 (A + 6 C)) \operatorname{Tan}[c + d x]}{2 b^2 (a^2 - b^2)^2 d (a + b \operatorname{Sec}[c + d x])}$$

Result (type 3, 895 leaves):

$$- \left( \left( 2 C (b + a \operatorname{Cos}[c + d x])^3 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right] - \operatorname{Sin}\left[\frac{c}{2} + \frac{d x}{2}\right]\right] \operatorname{Sec}[c + d x] (A + C \operatorname{Sec}[c + d x]^2) \right) / \right.$$

$$\left. \left( b^3 d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) (a + b \operatorname{Sec}[c + d x])^3 \right) \right) +$$

$$\left( 2 C (b + a \operatorname{Cos}[c + d x])^3 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{d x}{2}\right]\right] \operatorname{Sec}[c + d x] (A + C \operatorname{Sec}[c + d x]^2) \right) /$$

$$\left( b^3 d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) (a + b \operatorname{Sec}[c + d x])^3 \right) +$$

$$\left( (3 A b^4 + 2 a^4 C - 5 a^2 b^2 C + 6 b^4 C) (b + a \operatorname{Cos}[c + d x])^3 \operatorname{Sec}[c + d x] \right.$$

$$\left. (A + C \operatorname{Sec}[c + d x]^2) \left( \left( 2 i a \operatorname{ArcTan}\left[\operatorname{Sec}\left[\frac{d x}{2}\right]\right] \left( \frac{\operatorname{Cos}[c]}{\sqrt{a^2 - b^2} \sqrt{\operatorname{Cos}[2 c] - i \operatorname{Sin}[2 c]}} - \right. \right. \right.$$

$$\left. \left. \frac{i \operatorname{Sin}[c]}{\sqrt{a^2 - b^2} \sqrt{\operatorname{Cos}[2 c] - i \operatorname{Sin}[2 c]}} \right) \left( -i b \operatorname{Sin}\left[\frac{d x}{2}\right] + i a \operatorname{Sin}\left[c + \frac{d x}{2}\right] \right) \operatorname{Cos}[c] \right) / \right.$$

$$\left. \left( b^3 \sqrt{a^2 - b^2} d \sqrt{\operatorname{Cos}[2 c] - i \operatorname{Sin}[2 c]} \right) + \left( 2 a \operatorname{ArcTan}\left[\operatorname{Sec}\left[\frac{d x}{2}\right]\right] \right.$$

$$\left. \left( \frac{\operatorname{Cos}[c]}{\sqrt{a^2 - b^2} \sqrt{\operatorname{Cos}[2 c] - i \operatorname{Sin}[2 c]}} - \frac{i \operatorname{Sin}[c]}{\sqrt{a^2 - b^2} \sqrt{\operatorname{Cos}[2 c] - i \operatorname{Sin}[2 c]}} \right) \left( -i b \operatorname{Sin}\left[\frac{d x}{2}\right] + i a \operatorname{Sin}\left[c + \frac{d x}{2}\right] \right) \operatorname{Sin}[c] \right) / \left( b^3 \sqrt{a^2 - b^2} d \sqrt{\operatorname{Cos}[2 c] - i \operatorname{Sin}[2 c]} \right) \right) /$$

$$\left( (-a^2 + b^2)^2 (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) (a + b \operatorname{Sec}[c + d x])^3 \right) +$$

$$\frac{1}{2 a b^2 (-a^2 + b^2)^2 d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) (a + b \operatorname{Sec}[c + d x])^3}$$

$$(b + a \operatorname{Cos}[c + d x])$$

$$\operatorname{Sec}[c] \operatorname{Sec}[c + d x]$$

$$(A + C \operatorname{Sec}[c + d x]^2)$$

$$(-2 a^4 A b^2 \operatorname{Sin}[c] - 5 a^2 A b^4 \operatorname{Sin}[c] - 2 A b^6 \operatorname{Sin}[c] + 2 a^6 C \operatorname{Sin}[c] - a^4 b^2 C \operatorname{Sin}[c] -$$

$$10 a^2 b^4 C \operatorname{Sin}[c] + 5 a^3 A b^3 \operatorname{Sin}[d x] + 4 a A b^5 \operatorname{Sin}[d x] - 7 a^5 b C \operatorname{Sin}[d x] +$$

$$16 a^3 b^3 C \operatorname{Sin}[d x] - 3 a^3 A b^3 \operatorname{Sin}[2 c + d x] + a^5 b C \operatorname{Sin}[2 c + d x] - 4 a^3 b^3 C \operatorname{Sin}[2 c + d x] +$$

$$2 a^4 A b^2 \operatorname{Sin}[c + 2 d x] + a^2 A b^4 \operatorname{Sin}[c + 2 d x] - 2 a^6 C \operatorname{Sin}[c + 2 d x] + 5 a^4 b^2 C \operatorname{Sin}[c + 2 d x])$$

**Problem 694: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\operatorname{Sec}[c + d x] (A + C \operatorname{Sec}[c + d x]^2)}{(a + b \operatorname{Sec}[c + d x])^3} dx$$

Optimal (type 3, 177 leaves, 6 steps):

$$\frac{(a^2 (2A + C) + b^2 (A + 2C)) \operatorname{ArcTanh}\left[\frac{\sqrt{a-b} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a+b}}\right]}{(a-b)^{5/2} (a+b)^{5/2} d} - \frac{(Ab^2 + a^2C) \operatorname{Tan}[c+dx]}{2b(a^2-b^2)d(a+b \operatorname{Sec}[c+dx])^2} - \frac{a(3Ab^2 - a^2C + 4b^2C) \operatorname{Tan}[c+dx]}{2b(a^2-b^2)^2 d(a+b \operatorname{Sec}[c+dx])}$$

Result (type 3, 342 leaves):

$$\left( (b + a \cos[c + dx]) \operatorname{Sec}[c + dx] (A + C \operatorname{Sec}[c + dx])^2 \right. \\ \left. - \left( \left( 4i(a^2(2A + C) + b^2(A + 2C)) \operatorname{ArcTanh}\left[\frac{\sqrt{a-b} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a+b}}\right]\right) \left( i \cos[c] + \sin[c] \right) \left( a \sin[c] + (-b + a \cos[c]) \operatorname{Tan}\left[\frac{dx}{2}\right] \right) \right) / \left( \sqrt{a^2 - b^2} \sqrt{(\cos[c] - i \sin[c])^2} \right) (b + a \cos[c + dx])^2 \right. \\ \left. (\cos[c] - i \sin[c]) \right) / \left( (a^2 - b^2)^{5/2} \sqrt{(\cos[c] - i \sin[c])^2} \right) + \frac{1}{(a^3 - ab^2)^2} \\ \left( a \operatorname{Sec}[c] \left( (2Ab^4 + a^4C - a^2b^2(11A + 10C)) \sin[dx] + (-2Ab^4 + a^4C + a^2b^2(5A + 2C)) \sin[2c + dx] \right) + a b (Ab^2 - a^2(4A + 3C)) \sin[c + 2dx] \right) + \\ \left. b(a^2 + 2b^2)(-Ab^2 + a^2(4A + 3C)) \operatorname{Tan}[c] \right) / \left( 2d(A + 2C + A \cos[2(c + dx)]) (a + b \operatorname{Sec}[c + dx])^3 \right)$$

**Problem 695: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{A + C \operatorname{Sec}[c + dx]^2}{(a + b \operatorname{Sec}[c + dx])^3} dx$$

Optimal (type 3, 202 leaves, 6 steps):

$$\frac{Ax}{a^3} + \frac{b(5a^2Ab^2 - 2Ab^4 - 3a^4(2A + C)) \operatorname{ArcTanh}\left[\frac{\sqrt{a-b} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a+b}}\right]}{a^3(a-b)^{5/2}(a+b)^{5/2}d} + \frac{(Ab^2 + a^2C) \operatorname{Tan}[c+dx]}{2a(a^2-b^2)d(a+b \operatorname{Sec}[c+dx])^2} - \frac{(2Ab^4 - a^4C - a^2b^2(5A + 2C)) \operatorname{Tan}[c+dx]}{2a^2(a^2-b^2)^2 d(a+b \operatorname{Sec}[c+dx])}$$

Result (type 3, 926 leaves):

$$\begin{aligned} & \left( (6 a^4 A - 5 a^2 A b^2 + 2 A b^4 + 3 a^4 C) (b + a \operatorname{Cos}[c + d x])^3 \operatorname{Sec}[c + d x] \right. \\ & \quad (A + C \operatorname{Sec}[c + d x])^2 \left( \left( 2 i b \operatorname{ArcTan}\left[\operatorname{Sec}\left[\frac{d x}{2}\right]\right] \left( \frac{\operatorname{Cos}[c]}{\sqrt{a^2 - b^2} \sqrt{\operatorname{Cos}[2 c] - i \operatorname{Sin}[2 c]}} - \right. \right. \right. \\ & \quad \left. \left. \left. \frac{i \operatorname{Sin}[c]}{\sqrt{a^2 - b^2} \sqrt{\operatorname{Cos}[2 c] - i \operatorname{Sin}[2 c]}} \right) \left( -i b \operatorname{Sin}\left[\frac{d x}{2}\right] + i a \operatorname{Sin}\left[c + \frac{d x}{2}\right] \right) \right) \right. \\ & \quad \left. \operatorname{Cos}[c] \right) / \left( a^3 \sqrt{a^2 - b^2} d \sqrt{\operatorname{Cos}[2 c] - i \operatorname{Sin}[2 c]} \right) + \\ & \quad \left( 2 b \operatorname{ArcTan}\left[\operatorname{Sec}\left[\frac{d x}{2}\right]\right] \left( \frac{\operatorname{Cos}[c]}{\sqrt{a^2 - b^2} \sqrt{\operatorname{Cos}[2 c] - i \operatorname{Sin}[2 c]}} - \right. \right. \\ & \quad \left. \left. \frac{i \operatorname{Sin}[c]}{\sqrt{a^2 - b^2} \sqrt{\operatorname{Cos}[2 c] - i \operatorname{Sin}[2 c]}} \right) \left( -i b \operatorname{Sin}\left[\frac{d x}{2}\right] + i a \operatorname{Sin}\left[c + \frac{d x}{2}\right] \right) \right) \\ & \quad \left. \operatorname{Sin}[c] \right) / \left( a^3 \sqrt{a^2 - b^2} d \sqrt{\operatorname{Cos}[2 c] - i \operatorname{Sin}[2 c]} \right) \Big) / \\ & \quad \left( (-a^2 + b^2)^2 (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) (a + b \operatorname{Sec}[c + d x])^3 \right) + \\ & \quad \frac{1}{2 a^3 (a^2 - b^2)^2 d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) (a + b \operatorname{Sec}[c + d x])^3} \\ & \quad (b + a \operatorname{Cos}[c + d x]) \\ & \quad \operatorname{Sec}[c] \\ & \quad \operatorname{Sec}[c + d x] \\ & \quad (A + C \operatorname{Sec}[c + d x])^2 \\ & \quad (2 a^6 A d x \operatorname{Cos}[c] - 6 a^2 A b^4 d x \operatorname{Cos}[c] + 4 A b^6 d x \operatorname{Cos}[c] + 4 a^5 A b d x \operatorname{Cos}[d x] - \\ & \quad 8 a^3 A b^3 d x \operatorname{Cos}[d x] + 4 a A b^5 d x \operatorname{Cos}[d x] + 4 a^5 A b d x \operatorname{Cos}[2 c + d x] - \\ & \quad 8 a^3 A b^3 d x \operatorname{Cos}[2 c + d x] + 4 a A b^5 d x \operatorname{Cos}[2 c + d x] + a^6 A d x \operatorname{Cos}[c + 2 d x] - \\ & \quad 2 a^4 A b^2 d x \operatorname{Cos}[c + 2 d x] + a^2 A b^4 d x \operatorname{Cos}[c + 2 d x] + a^6 A d x \operatorname{Cos}[3 c + 2 d x] - \\ & \quad 2 a^4 A b^2 d x \operatorname{Cos}[3 c + 2 d x] + a^2 A b^4 d x \operatorname{Cos}[3 c + 2 d x] - 6 a^4 A b^2 \operatorname{Sin}[c] - \\ & \quad 9 a^2 A b^4 \operatorname{Sin}[c] + 6 A b^6 \operatorname{Sin}[c] - 2 a^6 C \operatorname{Sin}[c] - 5 a^4 b^2 C \operatorname{Sin}[c] - 2 a^2 b^4 C \operatorname{Sin}[c] + \\ & \quad 17 a^3 A b^3 \operatorname{Sin}[d x] - 8 a A b^5 \operatorname{Sin}[d x] + 5 a^5 b C \operatorname{Sin}[d x] + 4 a^3 b^3 C \operatorname{Sin}[d x] - \\ & \quad 7 a^3 A b^3 \operatorname{Sin}[2 c + d x] + 4 a A b^5 \operatorname{Sin}[2 c + d x] - 3 a^5 b C \operatorname{Sin}[2 c + d x] + \\ & \quad 6 a^4 A b^2 \operatorname{Sin}[c + 2 d x] - 3 a^2 A b^4 \operatorname{Sin}[c + 2 d x] + 2 a^6 C \operatorname{Sin}[c + 2 d x] + a^4 b^2 C \operatorname{Sin}[c + 2 d x]) \end{aligned}$$

**Problem 696: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Cos}[c + d x] (A + C \operatorname{Sec}[c + d x])^2}{(a + b \operatorname{Sec}[c + d x])^3} dx$$

Optimal (type 3, 266 leaves, 7 steps):



$$\begin{aligned}
 & -\frac{3 A b x}{a^4} - \left( (15 a^2 A b^4 - 6 A b^6 - 2 a^6 C - a^4 b^2 (12 A + C)) \operatorname{ArcTanh}\left[\frac{\sqrt{a-b} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a+b}}\right] \right) / \\
 & \left( a^4 (a-b)^{5/2} (a+b)^{5/2} d \right) - \frac{(11 a^2 A b^2 - 6 A b^4 - a^4 (2 A - 3 C)) \operatorname{Sin}[c+d x]}{2 a^3 (a^2 - b^2)^2 d} + \\
 & \frac{(A b^2 + a^2 C) \operatorname{Sin}[c+d x]}{2 a (a^2 - b^2) d (a+b \operatorname{Sec}[c+d x])^2} - \frac{(3 A b^4 - 2 a^4 C - a^2 b^2 (6 A + C)) \operatorname{Sin}[c+d x]}{2 a^2 (a^2 - b^2)^2 d (a+b \operatorname{Sec}[c+d x])}
 \end{aligned}$$

Result(type 3, 1186 leaves):

$$\frac{1}{(-a^2 + b^2)^2 (A + 2C + A \cos[2c + 2dx]) (a + b \sec[c + dx])^3} \\ (12a^4Ab^2 - 15a^2A^2b^4 + 6A^2b^6 + 2a^6C + a^4b^2C) (b + a \cos[c + dx])^3 \sec[c + dx] \\ (A + C \sec[c + dx])^2 \left( - \left( \left( 2i \operatorname{ArcTan}\left[\sec\left[\frac{dx}{2}\right]\right] \left( \frac{\cos[c]}{\sqrt{a^2 - b^2} \sqrt{\cos[2c] - i \sin[2c]}} - \frac{i \sin[c]}{\sqrt{a^2 - b^2} \sqrt{\cos[2c] - i \sin[2c]}} \right) \left( -i b \sin\left[\frac{dx}{2}\right] + i a \sin\left[c + \frac{dx}{2}\right] \right) \right) \right) \\ \left. \cos[c] \right) / \left( a^4 \sqrt{a^2 - b^2} d \sqrt{\cos[2c] - i \sin[2c]} \right) - \\ \left( 2 \operatorname{ArcTan}\left[\sec\left[\frac{dx}{2}\right]\right] \left( \frac{\cos[c]}{\sqrt{a^2 - b^2} \sqrt{\cos[2c] - i \sin[2c]}} - \frac{i \sin[c]}{\sqrt{a^2 - b^2} \sqrt{\cos[2c] - i \sin[2c]}} \right) \right. \\ \left. \left( -i b \sin\left[\frac{dx}{2}\right] + i a \sin\left[c + \frac{dx}{2}\right] \right) \sin[c] \right) / \\ \left. \left( a^4 \sqrt{a^2 - b^2} d \sqrt{\cos[2c] - i \sin[2c]} \right) \right) +$$

$$\frac{1}{4a^4 (a^2 - b^2)^2 d (A + 2C + A \cos[2c + 2dx]) (a + b \sec[c + dx])^3} \\ (b + a \cos[c + dx]) \\ \sec[c] \\ \sec[c + dx] \\ (A + C \sec[c + dx])^2 \\ (-12a^6Ab^2dx \cos[c] + 36a^2Ab^5dx \cos[c] - 24Ab^7dx \cos[c] - 24a^5Ab^2dx \cos[dx] + \\ 48a^3Ab^4dx \cos[dx] - 24aAb^6dx \cos[dx] - 24a^5Ab^2dx \cos[2c + dx] + \\ 48a^3Ab^4dx \cos[2c + dx] - 24aAb^6dx \cos[2c + dx] - 6a^6Ab^2dx \cos[3c + 2dx] + \\ 12a^4Ab^3dx \cos[3c + 2dx] - 6a^2Ab^5dx \cos[3c + 2dx] - 6a^6Ab^2dx \cos[3c + 2dx] + \\ 12a^4Ab^3dx \cos[3c + 2dx] - 6a^2Ab^5dx \cos[3c + 2dx] + 16a^4Ab^3 \sin[c] + \\ 22a^2Ab^5 \sin[c] - 20Ab^7 \sin[c] + 8a^6bC \sin[c] + 14a^4b^3C \sin[c] - 4a^2b^5C \sin[c] + \\ a^7A \sin[dx] + 2a^5Ab^2 \sin[dx] - 53a^3Ab^4 \sin[dx] + 32aAb^6 \sin[dx] - \\ 22a^5b^2C \sin[dx] + 4a^3b^4C \sin[dx] + a^7A \sin[2c + dx] + 2a^5Ab^2 \sin[2c + dx] + \\ 11a^3Ab^4 \sin[2c + dx] - 8aAb^6 \sin[2c + dx] + 10a^5b^2C \sin[2c + dx] - \\ 4a^3b^4C \sin[2c + dx] + 4a^6Ab \sin[c + 2dx] - 24a^4Ab^3 \sin[c + 2dx] + \\ 14a^2Ab^5 \sin[c + 2dx] - 8a^6bC \sin[c + 2dx] + 2a^4b^3C \sin[c + 2dx] + \\ 4a^6Ab \sin[3c + 2dx] - 8a^4Ab^3 \sin[3c + 2dx] + 4a^2Ab^5 \sin[3c + 2dx] + \\ a^7A \sin[2c + 3dx] - 2a^5Ab^2 \sin[2c + 3dx] + a^3Ab^4 \sin[2c + 3dx] + \\ a^7A \sin[4c + 3dx] - 2a^5Ab^2 \sin[4c + 3dx] + a^3Ab^4 \sin[4c + 3dx])$$

**Problem 698: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec[c + dx]^4 (A + C \sec[c + dx])^2}{(a + b \sec[c + dx])^4} dx$$

Optimal (type 3, 378 leaves, 9 steps):

$$\begin{aligned}
 & - \frac{4 a C \operatorname{ArcTanh}[\operatorname{Sin}[c+d x]]}{b^5 d} - \\
 & \left( \frac{(2 A b^8 - 8 a^8 C + 28 a^6 b^2 C - 35 a^4 b^4 C + a^2 b^6 (3 A + 20 C)) \operatorname{ArcTanh}\left[\frac{\sqrt{a-b} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a+b}}\right]}{\right) / \\
 & \left( (a-b)^{7/2} b^5 (a+b)^{7/2} d - \frac{(5 A b^4 - (12 a^4 - 23 a^2 b^2 + 6 b^4) C) \operatorname{Tan}[c+d x]}{6 b^4 (a^2 - b^2)^2 d} - \right. \\
 & \frac{(A b^2 + a^2 C) \operatorname{Sec}[c+d x]^3 \operatorname{Tan}[c+d x]}{3 b (a^2 - b^2) d (a+b \operatorname{Sec}[c+d x])^3} + \\
 & \frac{(3 A b^4 - 4 a^4 C + a^2 b^2 (2 A + 9 C)) \operatorname{Sec}[c+d x]^2 \operatorname{Tan}[c+d x]}{6 b^2 (a^2 - b^2)^2 d (a+b \operatorname{Sec}[c+d x])^2} + \\
 & \left. \frac{a (2 A b^6 + 4 a^6 C - 11 a^4 b^2 C + 3 a^2 b^4 (A + 4 C)) \operatorname{Tan}[c+d x]}{2 b^4 (a^2 - b^2)^3 d (a+b \operatorname{Sec}[c+d x])} \right)
 \end{aligned}$$

Result (type 3, 874 leaves):

$$\begin{aligned}
 & - \left( \left( 2 (3 a^2 A b^6 + 2 A b^8 - 8 a^8 C + 28 a^6 b^2 C - 35 a^4 b^4 C + 20 a^2 b^6 C) \right. \right. \\
 & \left. \left. \operatorname{ArcTanh}\left[\frac{(-a+b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2 - b^2}}\right] (b+a \operatorname{Cos}[c+d x])^4 \operatorname{Sec}[c+d x]^2 (A+C \operatorname{Sec}[c+d x]^2) \right) \right) / \\
 & \left( b^5 \sqrt{a^2 - b^2} (-a^2 + b^2)^3 d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) (a+b \operatorname{Sec}[c+d x])^4 \right) + \\
 & \left( 8 a C (b+a \operatorname{Cos}[c+d x])^4 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] \operatorname{Sec}[c+d x]^2 \right. \\
 & \left. (A+C \operatorname{Sec}[c+d x]^2) \right) / \left( b^5 d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) (a+b \operatorname{Sec}[c+d x])^4 \right) - \\
 & \left( 8 a C (b+a \operatorname{Cos}[c+d x])^4 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] \operatorname{Sec}[c+d x]^2 \right. \\
 & \left. (A+C \operatorname{Sec}[c+d x]^2) \right) / \left( b^5 d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) (a+b \operatorname{Sec}[c+d x])^4 \right) + \\
 & \frac{1}{24 b^4 (-a^2 + b^2)^3 d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) (a+b \operatorname{Sec}[c+d x])^4} \\
 & (b+a \operatorname{Cos}[c+d x]) \operatorname{Sec}[c+d x]^3 (A+C \operatorname{Sec}[c+d x]^2) \\
 & (-6 a^4 A b^5 \operatorname{Sin}[c+d x] - 54 a^2 A b^7 \operatorname{Sin}[c+d x] - 120 a^8 b C \operatorname{Sin}[c+d x] + \\
 & 294 a^6 b^3 C \operatorname{Sin}[c+d x] - 174 a^4 b^5 C \operatorname{Sin}[c+d x] - 108 a^2 b^7 C \operatorname{Sin}[c+d x] + \\
 & 48 b^9 C \operatorname{Sin}[c+d x] - 16 a^5 A b^4 \operatorname{Sin}[2(c+d x)] - 2 a^3 A b^6 \operatorname{Sin}[2(c+d x)] - \\
 & 72 a A b^8 \operatorname{Sin}[2(c+d x)] - 48 a^9 C \operatorname{Sin}[2(c+d x)] - 40 a^7 b^2 C \operatorname{Sin}[2(c+d x)] + \\
 & 370 a^5 b^4 C \operatorname{Sin}[2(c+d x)] - 444 a^3 b^6 C \operatorname{Sin}[2(c+d x)] + 72 a b^8 C \operatorname{Sin}[2(c+d x)] - \\
 & 6 a^4 A b^5 \operatorname{Sin}[3(c+d x)] - 54 a^2 A b^7 \operatorname{Sin}[3(c+d x)] - 120 a^8 b C \operatorname{Sin}[3(c+d x)] + \\
 & 342 a^6 b^3 C \operatorname{Sin}[3(c+d x)] - 318 a^4 b^5 C \operatorname{Sin}[3(c+d x)] + 36 a^2 b^7 C \operatorname{Sin}[3(c+d x)] - \\
 & 4 a^5 A b^4 \operatorname{Sin}[4(c+d x)] - 11 a^3 A b^6 \operatorname{Sin}[4(c+d x)] - 24 a^9 C \operatorname{Sin}[4(c+d x)] + \\
 & 68 a^7 b^2 C \operatorname{Sin}[4(c+d x)] - 65 a^5 b^4 C \operatorname{Sin}[4(c+d x)] + 6 a^3 b^6 C \operatorname{Sin}[4(c+d x)])
 \end{aligned}$$

**Problem 699: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\text{Sec}[c + d x]^3 (A + C \text{Sec}[c + d x]^2)}{(a + b \text{Sec}[c + d x])^4} dx$$

Optimal (type 3, 313 leaves, 8 steps):

$$\frac{C \text{ArcTanh}[\text{Sin}[c + d x]]}{b^4 d} + \left( a (a^2 b^4 (A - 8 C) - 2 a^6 C + 7 a^4 b^2 C + 4 b^6 (A + 2 C)) \text{ArcTanh}\left[\frac{\sqrt{a - b} \text{Tan}\left[\frac{1}{2} (c + d x)\right]}{\sqrt{a + b}}\right] \right) / \left( (a - b)^{7/2} b^4 (a + b)^{7/2} d \right) - \frac{(A b^2 + a^2 C) \text{Sec}[c + d x]^2 \text{Tan}[c + d x]}{3 b (a^2 - b^2) d (a + b \text{Sec}[c + d x])^3} - \frac{a (2 A b^4 - 3 a^4 C + a^2 b^2 (3 A + 8 C)) \text{Tan}[c + d x]}{6 b^3 (a^2 - b^2)^2 d (a + b \text{Sec}[c + d x])^2} - \frac{(4 A b^6 + 9 a^6 C + 2 a^2 b^4 (7 A + 17 C) - a^4 b^2 (3 A + 28 C)) \text{Tan}[c + d x]}{6 b^3 (a^2 - b^2)^3 d (a + b \text{Sec}[c + d x])}$$

Result (type 3, 1092 leaves):

$$\begin{aligned}
 & - \left( \left( 2 C (b + a \cos [c + d x])^4 \operatorname{Log} \left[ \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right] \sec [c + d x]^2 (A + C \sec [c + d x]^2) \right) / \right. \\
 & \quad \left. (b^4 d (A + 2 C + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^4) \right) + \\
 & \left( 2 C (b + a \cos [c + d x])^4 \operatorname{Log} \left[ \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right] \sec [c + d x]^2 (A + C \sec [c + d x]^2) \right) / \\
 & \quad (b^4 d (A + 2 C + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^4) + \\
 & \quad \frac{1}{(-a^2 + b^2)^3 (A + 2 C + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^4} \\
 & \quad (a^2 A b^4 + 4 A b^6 - 2 a^6 C + 7 a^4 b^2 C - 8 a^2 b^4 C + 8 b^6 C) \\
 & \quad (b + a \cos [c + d x])^4 \sec [c + d x]^2 (A + C \sec [c + d x]^2) \\
 & \quad \left( \left( 2 i a \operatorname{ArcTan} \left[ \sec \left[ \frac{d x}{2} \right] \right] \left( \frac{\cos [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} - \frac{i \sin [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} \right) \right. \right. \\
 & \quad \left. \left. (-i b \sin \left[ \frac{d x}{2} \right] + i a \sin \left[ c + \frac{d x}{2} \right]) \cos [c] \right) / (b^4 \sqrt{a^2 - b^2} d \sqrt{\cos [2 c] - i \sin [2 c]}) \right) + \\
 & \quad \left( 2 a \operatorname{ArcTan} \left[ \sec \left[ \frac{d x}{2} \right] \right] \left( \frac{\cos [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} - \frac{i \sin [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} \right) \right. \\
 & \quad \left. (-i b \sin \left[ \frac{d x}{2} \right] + i a \sin \left[ c + \frac{d x}{2} \right]) \sin [c] \right) / \\
 & \quad \left( b^4 \sqrt{a^2 - b^2} d \sqrt{\cos [2 c] - i \sin [2 c]} \right) - (2 (b + a \cos [c + d x]) \sec [c] \sec [c + d x]^2 \\
 & \quad (A + C \sec [c + d x]^2) (A b^3 \sin [c] + a^2 b C \sin [c] - a A b^2 \sin [d x] - a^3 C \sin [d x])) / \\
 & \quad (3 a b (-a^2 + b^2) d (A + 2 C + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^4) + \\
 & \quad \left( (b + a \cos [c + d x])^2 \sec [c] \sec [c + d x]^2 (A + C \sec [c + d x]^2) (-5 a A b^3 \sin [c] + a^3 b C \sin [c] - \right. \\
 & \quad \left. 6 a b^3 C \sin [c] + 3 a^2 A b^2 \sin [d x] + 2 A b^4 \sin [d x] - 3 a^4 C \sin [d x] + 8 a^2 b^2 C \sin [d x]) \right) / \\
 & \quad (3 b^2 (-a^2 + b^2)^2 d (A + 2 C + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^4) + \\
 & \quad \left( (b + a \cos [c + d x])^3 \sec [c] \sec [c + d x]^2 (A + C \sec [c + d x]^2) \right. \\
 & \quad \left. (-3 a^3 A b^3 \sin [c] - 12 a A b^5 \sin [c] - 3 a^5 b C \sin [c] + 6 a^3 b^3 C \sin [c] - 18 a b^5 C \sin [c] + 13 a^2 A \right. \\
 & \quad \left. b^4 \sin [d x] + 2 A b^6 \sin [d x] + 6 a^6 C \sin [d x] - 17 a^4 b^2 C \sin [d x] + 26 a^2 b^4 C \sin [d x]) \right) / \\
 & \quad (3 b^3 (-a^2 + b^2)^3 d (A + 2 C + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^4)
 \end{aligned}$$

**Problem 701: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c + d x] (A + C \sec [c + d x]^2)}{(a + b \sec [c + d x])^4} dx$$

Optimal (type 3, 252 leaves, 7 steps):

$$\frac{a \left( a^2 (2A + C) + b^2 (3A + 4C) \right) \text{ArcTanh} \left[ \frac{\sqrt{a-b} \tan \left[ \frac{1}{2} (c+dx) \right]}{\sqrt{a+b}} \right]}{(a-b)^{7/2} (a+b)^{7/2} d} - \frac{(Ab^2 + a^2C) \tan [c+dx]}{3b(a^2 - b^2)d(a+b \sec [c+dx])^3} -$$

$$\frac{a(5Ab^2 - a^2C + 6b^2C) \tan [c+dx]}{6b(a^2 - b^2)^2 d(a+b \sec [c+dx])^2} + \frac{(a^4C - 2b^4(2A+3C) - a^2b^2(11A+10C)) \tan [c+dx]}{6b(a^2 - b^2)^3 d(a+b \sec [c+dx])}$$

Result (type 3, 868 leaves):

$$\left( (2a^2A + 3Ab^2 + a^2C + 4b^2C) (b + a \cos [c+dx])^4 \sec [c+dx]^2 \right.$$

$$(A + C \sec [c+dx])^2 \left( \left( 2i a \text{ArcTan} \left[ \sec \left[ \frac{dx}{2} \right] \right] \left( \frac{\cos [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2c] - i \sin [2c]}} - \right. \right. \right.$$

$$\left. \left. \frac{i \sin [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2c] - i \sin [2c]}} \right) \left( -i b \sin \left[ \frac{dx}{2} \right] + i a \sin \left[ c + \frac{dx}{2} \right] \right) \cos [c] \right) /$$

$$\left( \sqrt{a^2 - b^2} d \sqrt{\cos [2c] - i \sin [2c]} \right) + \left( 2a \text{ArcTan} \left[ \sec \left[ \frac{dx}{2} \right] \right] \right.$$

$$\left( \frac{\cos [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2c] - i \sin [2c]}} - \frac{i \sin [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2c] - i \sin [2c]}} \right)$$

$$\left( -i b \sin \left[ \frac{dx}{2} \right] + i a \sin \left[ c + \frac{dx}{2} \right] \right) \left. \right) /$$

$$\left( \sqrt{a^2 - b^2} d \sqrt{\cos [2c] - i \sin [2c]} \right) \left. \right) /$$

$$\left( (-a^2 + b^2)^3 (A + 2C + A \cos [2c + 2dx]) (a + b \sec [c+dx])^4 \right) +$$

$$(2(b + a \cos [c+dx]) \sec [c] \sec [c+dx]^2 (A + C \sec [c+dx])^2 (Ab^4 \sin [c] + a^2 b^2 C \sin [c] - aAb^3 \sin [dx] - a^3 bC \sin [dx])) /$$

$$(3a^3(a^2 - b^2)d(A + 2C + A \cos [2c + 2dx]) (a + b \sec [c+dx])^4) +$$

$$\left( (b + a \cos [c+dx])^2 \sec [c] \sec [c+dx]^2 (A + C \sec [c+dx])^2 \right.$$

$$\left( -11a^2Ab^3 \sin [c] + 6Ab^5 \sin [c] - 5a^4bC \sin [c] + 9a^3Ab^2 \sin [dx] - \right.$$

$$\left. 4aAb^4 \sin [dx] + 3a^5C \sin [dx] + 2a^3b^2C \sin [dx] \right) /$$

$$(3a^3(a^2 - b^2)^2d(A + 2C + A \cos [2c + 2dx]) (a + b \sec [c+dx])^4) +$$

$$\left( (b + a \cos [c+dx])^3 \sec [c] \sec [c+dx]^2 (A + C \sec [c+dx])^2 \right.$$

$$(27a^4Ab^2 \sin [c] - 18a^2Ab^4 \sin [c] + 6Ab^6 \sin [c] + 3a^6C \sin [c] + 12a^4b^2C \sin [c] - 18a^5Ab$$

$$\sin [dx] + 5a^3Ab^3 \sin [dx] - 2aAb^5 \sin [dx] - 13a^5bC \sin [dx] - 2a^3b^3C \sin [dx]) \left. \right) /$$

$$(3a^3(a^2 - b^2)^3d(A + 2C + A \cos [2c + 2dx]) (a + b \sec [c+dx])^4)$$

Problem 702: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{A + C \operatorname{Sec}[c + d x]^2}{(a + b \operatorname{Sec}[c + d x])^4} dx$$

Optimal (type 3, 292 leaves, 7 steps):

$$\begin{aligned} & \frac{A x}{a^4} - \left( b \left( 7 a^2 A b^4 - 2 A b^6 - a^4 b^2 (8 A - C) + 4 a^6 (2 A + C) \right) \operatorname{ArcTanh} \left[ \frac{\sqrt{a-b} \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a+b}} \right] \right) / \\ & \left( a^4 (a-b)^{7/2} (a+b)^{7/2} d \right) + \frac{(A b^2 + a^2 C) \operatorname{Tan}[c + d x]}{3 a (a^2 - b^2) d (a + b \operatorname{Sec}[c + d x])^3} - \\ & \frac{(3 A b^4 - 2 a^4 C - a^2 b^2 (8 A + 3 C)) \operatorname{Tan}[c + d x]}{6 a^2 (a^2 - b^2)^2 d (a + b \operatorname{Sec}[c + d x])^2} - \\ & \frac{(17 a^2 A b^4 - 6 A b^6 - 2 a^6 C - 13 a^4 b^2 (2 A + C)) \operatorname{Tan}[c + d x]}{6 a^3 (a^2 - b^2)^3 d (a + b \operatorname{Sec}[c + d x])} \end{aligned}$$

Result (type 3, 995 leaves):

$$\begin{aligned}
& \frac{2 A x (b + a \cos [c + d x])^4 \sec [c + d x]^2 (A + C \sec [c + d x]^2)}{a^4 (A + 2 C + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^4} + \\
& \frac{1}{(-a^2 + b^2)^3 (A + 2 C + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^4} \\
& (-8 a^6 A + 8 a^4 A b^2 - 7 a^2 A b^4 + 2 A b^6 - 4 a^6 C - a^4 b^2 C) \\
& (b + a \cos [c + d x])^4 \sec [c + d x]^2 (A + C \sec [c + d x]^2) \\
& \left( \left( 2 i b \operatorname{ArcTan} \left[ \sec \left[ \frac{d x}{2} \right] \right] \left( \frac{\cos [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} - \frac{i \sin [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} \right) \right. \right. \\
& \left. \left. (-i b \sin \left[ \frac{d x}{2} \right] + i a \sin \left[ c + \frac{d x}{2} \right]) \cos [c] \right) / \left( a^4 \sqrt{a^2 - b^2} d \sqrt{\cos [2 c] - i \sin [2 c]} \right) + \right. \\
& \left. \left( 2 b \operatorname{ArcTan} \left[ \sec \left[ \frac{d x}{2} \right] \right] \left( \frac{\cos [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} - \frac{i \sin [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} \right) \right. \right. \\
& \left. \left. (-i b \sin \left[ \frac{d x}{2} \right] + i a \sin \left[ c + \frac{d x}{2} \right]) \sin [c] \right) / \right. \\
& \left. \left( a^4 \sqrt{a^2 - b^2} d \sqrt{\cos [2 c] - i \sin [2 c]} \right) \right) - (2 (b + a \cos [c + d x]) \sec [c] \sec [c + d x]^2 \\
& (A + C \sec [c + d x]^2) (A b^5 \sin [c] + a^2 b^3 C \sin [c] - a A b^4 \sin [d x] - a^3 b^2 C \sin [d x])) / \\
& (3 a^4 (a^2 - b^2) d (A + 2 C + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^4) + \\
& ((b + a \cos [c + d x])^2 \sec [c] \sec [c + d x]^2 (A + C \sec [c + d x]^2) \\
& (14 a^2 A b^4 \sin [c] - 9 A b^6 \sin [c] + 8 a^4 b^2 C \sin [c] - 3 a^2 b^4 C \sin [c] - \\
& 12 a^3 A b^3 \sin [d x] + 7 a A b^5 \sin [d x] - 6 a^5 b C \sin [d x] + a^3 b^3 C \sin [d x])) / \\
& (3 a^4 (a^2 - b^2)^2 d (A + 2 C + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^4) + \\
& ((b + a \cos [c + d x])^3 \sec [c] \sec [c + d x]^2 (A + C \sec [c + d x]^2) \\
& (-48 a^4 A b^3 \sin [c] + 51 a^2 A b^5 \sin [c] - 18 A b^7 \sin [c] - 12 a^6 b C \sin [c] - \\
& 3 a^4 b^3 C \sin [c] + 36 a^5 A b^2 \sin [d x] - 32 a^3 A b^4 \sin [d x] + \\
& 11 a A b^6 \sin [d x] + 6 a^7 C \sin [d x] + 10 a^5 b^2 C \sin [d x] - a^3 b^4 C \sin [d x])) / \\
& (3 a^4 (a^2 - b^2)^3 d (A + 2 C + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^4)
\end{aligned}$$

**Problem 703: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\cos [c + d x] (A + C \sec [c + d x]^2)}{(a + b \sec [c + d x])^4} dx$$

Optimal (type 3, 367 leaves, 8 steps):



$$\begin{aligned}
 & -\frac{4 A b x}{a^5} - \\
 & \left( (35 a^4 A b^4 - 28 a^2 A b^6 + 8 A b^8 - 2 a^8 C - a^6 b^2 (20 A + 3 C)) \operatorname{ArcTanh}\left[\frac{\sqrt{a-b} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a+b}}\right] \right) / \\
 & \left( a^5 (a-b)^{7/2} (a+b)^{7/2} d \right) + \frac{(68 a^2 A b^4 - 24 A b^6 + a^6 (6 A - 11 C) - a^4 b^2 (65 A + 4 C)) \operatorname{Sin}[c+d x]}{6 a^4 (a^2 - b^2)^3 d} + \\
 & \frac{(A b^2 + a^2 C) \operatorname{Sin}[c+d x]}{3 a (a^2 - b^2) d (a+b \operatorname{Sec}[c+d x])^3} - \frac{(4 A b^4 - 3 a^4 C - a^2 b^2 (9 A + 2 C)) \operatorname{Sin}[c+d x]}{6 a^2 (a^2 - b^2)^2 d (a+b \operatorname{Sec}[c+d x])^2} - \\
 & \frac{(11 a^2 A b^4 - 4 A b^6 - 2 a^6 C - 3 a^4 b^2 (4 A + C)) \operatorname{Sin}[c+d x]}{2 a^3 (a^2 - b^2)^3 d (a+b \operatorname{Sec}[c+d x])}
 \end{aligned}$$

Result (type 3, 1089 leaves):

$$\begin{aligned}
& - \frac{8 A b x (b + a \cos [c + d x])^4 \sec [c + d x]^2 (A + C \sec [c + d x]^2)}{a^5 (A + 2 C + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^4} + \\
& \frac{1}{(-a^2 + b^2)^3 (A + 2 C + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^4} \\
& (-20 a^6 A b^2 + 35 a^4 A b^4 - 28 a^2 A b^6 + 8 A b^8 - 2 a^8 C - 3 a^6 b^2 C) (b + a \cos [c + d x])^4 \sec [c + d x]^2 \\
& (A + C \sec [c + d x]^2) \left( - \left( \left( 2 i \operatorname{ArcTan} \left[ \sec \left[ \frac{d x}{2} \right] \left( \frac{\cos [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]} - \frac{i \sin [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} \right) \right. \right. \right. \\
& \left. \left. \left. \frac{i \sin [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} \right) \left( -i b \sin \left[ \frac{d x}{2} \right] + i a \sin \left[ c + \frac{d x}{2} \right] \right) \right) \right) \\
& \left. \cos [c] \right) / \left( a^5 \sqrt{a^2 - b^2} d \sqrt{\cos [2 c] - i \sin [2 c]} \right) - \\
& \left( 2 \operatorname{ArcTan} \left[ \sec \left[ \frac{d x}{2} \right] \left( \frac{\cos [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]} - \frac{i \sin [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} \right) \right. \right. \\
& \left. \left. \left( -i b \sin \left[ \frac{d x}{2} \right] + i a \sin \left[ c + \frac{d x}{2} \right] \right) \right) \sin [c] \right) / \\
& \left. \left( a^5 \sqrt{a^2 - b^2} d \sqrt{\cos [2 c] - i \sin [2 c]} \right) \right) + \\
& (2 (b + a \cos [c + d x]) \sec [c] \sec [c + d x]^2 (A + C \sec [c + d x]^2) \\
& (A b^6 \sin [c] + a^2 b^4 C \sin [c] - a A b^5 \sin [d x] - a^3 b^3 C \sin [d x])) / \\
& (3 a^5 (a^2 - b^2) d (A + 2 C + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^4) + \\
& ((b + a \cos [c + d x])^2 \sec [c] \sec [c + d x]^2 (A + C \sec [c + d x]^2) \\
& (-17 a^2 A b^5 \sin [c] + 12 A b^7 \sin [c] - 11 a^4 b^3 C \sin [c] + 6 a^2 b^5 C \sin [c] + \\
& 15 a^3 A b^4 \sin [d x] - 10 a A b^6 \sin [d x] + 9 a^5 b^2 C \sin [d x] - 4 a^3 b^4 C \sin [d x])) / \\
& (3 a^5 (a^2 - b^2)^2 d (A + 2 C + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^4) + \\
& \frac{1}{3 a^5 (a^2 - b^2)^3 d (A + 2 C + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^4} \\
& (b + a \cos [c + d x])^3 \sec [c] \\
& \sec [c + d x]^2 (A + C \sec [c + d x]^2) \\
& (75 a^4 A b^4 \sin [c] - 96 a^2 A b^6 \sin [c] + 36 A b^8 \sin [c] + 27 a^6 b^2 C \sin [c] - \\
& 18 a^4 b^4 C \sin [c] + 6 a^2 b^6 C \sin [c] - 60 a^5 A b^3 \sin [d x] + 71 a^3 A b^5 \sin [d x] - \\
& 26 a A b^7 \sin [d x] - 18 a^7 b C \sin [d x] + 5 a^5 b^3 C \sin [d x] - 2 a^3 b^5 C \sin [d x]) + \\
& (2 A (b + a \cos [c + d x])^4 \sec [c + d x] (A + C \sec [c + d x]^2) \tan [c + d x]) / \\
& (a^4 d (A + 2 C + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^4)
\end{aligned}$$

**Problem 704: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos [c + d x]^2 (A + C \sec [c + d x]^2)}{(a + b \sec [c + d x])^4} dx$$

Optimal (type 3, 513 leaves, 9 steps):

$$\begin{aligned}
 & \frac{(20 A b^2 + a^2 (A + 2 C)) x}{2 a^6} + \left( (20 A b^9 - a^2 b^7 (69 A - 2 C) - 8 a^6 b^3 (5 A - C) + 7 a^4 b^5 (12 A - C) - 8 a^8 b C) \right. \\
 & \quad \left. \text{ArcTanh} \left[ \frac{\sqrt{a-b} \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a+b}} \right] \right) / \left( a^6 \sqrt{a-b} \sqrt{a+b} (a^2 - b^2)^3 d \right) + \frac{1}{6 a^5 (a^2 - b^2)^3 d} \\
 & b (60 A b^6 - a^6 (24 A - 26 C) + a^4 b^2 (146 A - 17 C) - a^2 b^4 (167 A - 6 C)) \text{Sin}[c + d x] - \\
 & \frac{1}{2 a^4 (a^2 - b^2)^3 d} (10 A b^6 - a^6 (A - 6 C) + a^4 b^2 (23 A - 2 C) - a^2 b^4 (27 A - C)) \text{Cos}[c + d x] \text{Sin}[c + d x] + \\
 & \frac{(A b^2 + a^2 C) \text{Cos}[c + d x] \text{Sin}[c + d x]}{3 a (a^2 - b^2) d (a + b \text{Sec}[c + d x])^3} - \frac{(5 A b^4 - 4 a^4 C - a^2 b^2 (10 A + C)) \text{Cos}[c + d x] \text{Sin}[c + d x]}{6 a^2 (a^2 - b^2)^2 d (a + b \text{Sec}[c + d x])^2} + \\
 & \left( (20 A b^6 - a^2 b^4 (53 A - 2 C) + 12 a^6 C + a^4 b^2 (48 A + C)) \text{Cos}[c + d x] \text{Sin}[c + d x] \right) / \\
 & \left( 6 a^3 (a^2 - b^2)^3 d (a + b \text{Sec}[c + d x]) \right)
 \end{aligned}$$

Result(type 3, 1452 leaves):

$$\left( b \left( -40 a^6 A b^2 + 84 a^4 A b^4 - 69 a^2 A b^6 + 20 A b^8 - 8 a^8 C + 8 a^6 b^2 C - 7 a^4 b^4 C + 2 a^2 b^6 C \right) \right. \\ \left. \operatorname{ArcTanh} \left[ \frac{(-a+b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}{\sqrt{a^2-b^2}} \right] \right) / \left( a^6 \sqrt{a^2-b^2} (-a^2+b^2)^3 d \right) - \\ \frac{1}{96 a^6 (a^2-b^2)^3 d (b+a \operatorname{Cos}[c+dx])^3} \left( -72 a^{10} A b (c+dx) - 1272 a^8 A b^3 (c+dx) + \right. \\ 3288 a^6 A b^5 (c+dx) - 1512 a^4 A b^7 (c+dx) - 1392 a^2 A b^9 (c+dx) + 960 A b^{11} (c+dx) - \\ 144 a^{10} b C (c+dx) + 336 a^8 b^3 C (c+dx) - 144 a^6 b^5 C (c+dx) - 144 a^4 b^7 C (c+dx) + \\ 96 a^2 b^9 C (c+dx) - 36 a^{11} A (c+dx) \operatorname{Cos}[c+dx] - 756 a^9 A b^2 (c+dx) \operatorname{Cos}[c+dx] - \\ 396 a^7 A b^4 (c+dx) \operatorname{Cos}[c+dx] + 6084 a^5 A b^6 (c+dx) \operatorname{Cos}[c+dx] - \\ 7776 a^3 A b^8 (c+dx) \operatorname{Cos}[c+dx] + 2880 a A b^{10} (c+dx) \operatorname{Cos}[c+dx] - \\ 72 a^{11} C (c+dx) \operatorname{Cos}[c+dx] - 72 a^9 b^2 C (c+dx) \operatorname{Cos}[c+dx] + 648 a^7 b^4 C (c+dx) \operatorname{Cos}[c+dx] - \\ 792 a^5 b^6 C (c+dx) \operatorname{Cos}[c+dx] + 288 a^3 b^8 C (c+dx) \operatorname{Cos}[c+dx] - \\ 72 a^{10} A b (c+dx) \operatorname{Cos}[2(c+dx)] - 1224 a^8 A b^3 (c+dx) \operatorname{Cos}[2(c+dx)] + \\ 4104 a^6 A b^5 (c+dx) \operatorname{Cos}[2(c+dx)] - 4248 a^4 A b^7 (c+dx) \operatorname{Cos}[2(c+dx)] + \\ 1440 a^2 A b^9 (c+dx) \operatorname{Cos}[2(c+dx)] - 144 a^{10} b C (c+dx) \operatorname{Cos}[2(c+dx)] + \\ 432 a^8 b^3 C (c+dx) \operatorname{Cos}[2(c+dx)] - 432 a^6 b^5 C (c+dx) \operatorname{Cos}[2(c+dx)] + \\ 144 a^4 b^7 C (c+dx) \operatorname{Cos}[2(c+dx)] - 12 a^{11} A (c+dx) \operatorname{Cos}[3(c+dx)] - \\ 204 a^9 A b^2 (c+dx) \operatorname{Cos}[3(c+dx)] + 684 a^7 A b^4 (c+dx) \operatorname{Cos}[3(c+dx)] - \\ 708 a^5 A b^6 (c+dx) \operatorname{Cos}[3(c+dx)] + 240 a^3 A b^8 (c+dx) \operatorname{Cos}[3(c+dx)] - \\ 24 a^{11} C (c+dx) \operatorname{Cos}[3(c+dx)] + 72 a^9 b^2 C (c+dx) \operatorname{Cos}[3(c+dx)] - \\ 72 a^7 b^4 C (c+dx) \operatorname{Cos}[3(c+dx)] + 24 a^5 b^6 C (c+dx) \operatorname{Cos}[3(c+dx)] - 6 a^{11} A \operatorname{Sin}[c+dx] + \\ 270 a^9 A b^2 \operatorname{Sin}[c+dx] - 750 a^7 A b^4 \operatorname{Sin}[c+dx] - 1086 a^5 A b^6 \operatorname{Sin}[c+dx] + \\ 2232 a^3 A b^8 \operatorname{Sin}[c+dx] - 960 a A b^{10} \operatorname{Sin}[c+dx] - 144 a^9 b^2 C \operatorname{Sin}[c+dx] - \\ 288 a^7 b^4 C \operatorname{Sin}[c+dx] + 228 a^5 b^6 C \operatorname{Sin}[c+dx] - 96 a^3 b^8 C \operatorname{Sin}[c+dx] + \\ 60 a^{10} A b \operatorname{Sin}[2(c+dx)] + 372 a^8 A b^3 \operatorname{Sin}[2(c+dx)] - 2772 a^6 A b^5 \operatorname{Sin}[2(c+dx)] + \\ 3300 a^4 A b^7 \operatorname{Sin}[2(c+dx)] - 1200 a^2 A b^9 \operatorname{Sin}[2(c+dx)] - 480 a^8 b^3 C \operatorname{Sin}[2(c+dx)] + \\ 360 a^6 b^5 C \operatorname{Sin}[2(c+dx)] - 120 a^4 b^7 C \operatorname{Sin}[2(c+dx)] - 9 a^{11} A \operatorname{Sin}[3(c+dx)] + \\ 279 a^9 A b^2 \operatorname{Sin}[3(c+dx)] - 1143 a^7 A b^4 \operatorname{Sin}[3(c+dx)] + 1253 a^5 A b^6 \operatorname{Sin}[3(c+dx)] - \\ 440 a^3 A b^8 \operatorname{Sin}[3(c+dx)] - 144 a^9 b^2 C \operatorname{Sin}[3(c+dx)] + 128 a^7 b^4 C \operatorname{Sin}[3(c+dx)] - \\ 44 a^5 b^6 C \operatorname{Sin}[3(c+dx)] + 30 a^{10} A b \operatorname{Sin}[4(c+dx)] - 90 a^8 A b^3 \operatorname{Sin}[4(c+dx)] + \\ 90 a^6 A b^5 \operatorname{Sin}[4(c+dx)] - 30 a^4 A b^7 \operatorname{Sin}[4(c+dx)] - 3 a^{11} A \operatorname{Sin}[5(c+dx)] + \\ 9 a^9 A b^2 \operatorname{Sin}[5(c+dx)] - 9 a^7 A b^4 \operatorname{Sin}[5(c+dx)] + 3 a^5 A b^6 \operatorname{Sin}[5(c+dx)] \left. \right)$$

### Problem 705: Result more than twice size of optimal antiderivative.

$$\int \frac{a^2 - b^2 \operatorname{Sec}[c+dx]^2}{a + b \operatorname{Sec}[c+dx]} dx$$

Optimal (type 3, 17 leaves, 3 steps):

$$a x - \frac{b \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{d}$$

Result (type 3, 73 leaves):

$$a x + \frac{b \operatorname{Log}\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d} - \frac{b \operatorname{Log}\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d}$$

**Problem 709: Attempted integration timed out after 120 seconds.**

$$\int \operatorname{Sec}[c + dx]^3 \sqrt{a + b \operatorname{Sec}[c + dx]} (A + C \operatorname{Sec}[c + dx]^2) dx$$

Optimal (type 4, 467 leaves, 7 steps):

$$\begin{aligned} & \frac{1}{315 b^5 d} 2 (a - b) \sqrt{a + b} (16 a^4 C + 6 a^2 b^2 (7 A + 4 C) - 21 b^4 (9 A + 7 C)) \operatorname{Cot}[c + dx] \\ & \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + dx]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \sqrt{\frac{b (1 - \operatorname{Sec}[c + dx])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec}[c + dx])}{a - b}} + \\ & \frac{1}{315 b^4 d} 2 (a - b) \sqrt{a + b} (16 a^3 C + 12 a^2 b C + 6 a b^2 (7 A + 6 C) + 21 b^3 (9 A + 7 C)) \operatorname{Cot}[c + dx] \\ & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + dx]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \sqrt{\frac{b (1 - \operatorname{Sec}[c + dx])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec}[c + dx])}{a - b}} + \\ & \frac{2 a (21 A b^2 + 8 a^2 C + 13 b^2 C) \sqrt{a + b \operatorname{Sec}[c + dx]} \operatorname{Tan}[c + dx]}{315 b^3 d} - \frac{1}{315 b^2 d} \\ & 2 (6 a^2 C - 7 b^2 (9 A + 7 C)) \operatorname{Sec}[c + dx] \sqrt{a + b \operatorname{Sec}[c + dx]} \operatorname{Tan}[c + dx] + \\ & \frac{2 a C \operatorname{Sec}[c + dx]^2 \sqrt{a + b \operatorname{Sec}[c + dx]} \operatorname{Tan}[c + dx]}{63 b d} + \\ & \frac{2 C \operatorname{Sec}[c + dx]^3 \sqrt{a + b \operatorname{Sec}[c + dx]} \operatorname{Tan}[c + dx]}{9 d} \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 710: Unable to integrate problem.**

$$\int \operatorname{Sec}[c + dx]^2 \sqrt{a + b \operatorname{Sec}[c + dx]} (A + C \operatorname{Sec}[c + dx]^2) dx$$

Optimal (type 4, 375 leaves, 6 steps):

$$\begin{aligned}
 & -\frac{1}{105 b^4 d} 2 a (a-b) \sqrt{a+b} (35 A b^2 + 8 a^2 C + 19 b^2 C) \operatorname{Cot}[c+d x] \operatorname{EllipticE}\left[ \right. \\
 & \quad \left. \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \\
 & \frac{1}{105 b^3 d} 2 (a-b) \sqrt{a+b} (35 A b^2 + (8 a^2 + 6 a b + 25 b^2) C) \operatorname{Cot}[c+d x] \\
 & \quad \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \\
 & \frac{2(8 a^2 C + 5 b^2(7 A + 5 C)) \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x]}{105 b^2 d} - \\
 & \frac{8 a C (a+b \operatorname{Sec}[c+d x])^{3/2} \operatorname{Tan}[c+d x]}{35 b^2 d} + \frac{2 C \operatorname{Sec}[c+d x] (a+b \operatorname{Sec}[c+d x])^{3/2} \operatorname{Tan}[c+d x]}{7 b d}
 \end{aligned}$$

Result (type 8, 37 leaves):

$$\int \operatorname{Sec}[c+d x]^2 \sqrt{a+b \operatorname{Sec}[c+d x]} (A+C \operatorname{Sec}[c+d x]^2) dx$$

### Problem 711: Unable to integrate problem.

$$\int \operatorname{Sec}[c+d x] \sqrt{a+b \operatorname{Sec}[c+d x]} (A+C \operatorname{Sec}[c+d x]^2) dx$$

Optimal (type 4, 308 leaves, 5 steps):

$$\begin{aligned}
 & \frac{1}{15 b^3 d} 2 (a-b) \sqrt{a+b} (2 a^2 C - 3 b^2 (5 A + 3 C)) \operatorname{Cot}[c+d x] \\
 & \quad \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \\
 & \frac{1}{15 b^2 d} 2 (a-b) \sqrt{a+b} (15 A b + 2 a C + 9 b C) \operatorname{Cot}[c+d x] \\
 & \quad \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \\
 & \frac{4 a C \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x]}{15 b d} + \frac{2 C (a+b \operatorname{Sec}[c+d x])^{3/2} \operatorname{Tan}[c+d x]}{5 b d}
 \end{aligned}$$

Result (type 8, 35 leaves):

$$\int \operatorname{Sec}[c+d x] \sqrt{a+b \operatorname{Sec}[c+d x]} (A+C \operatorname{Sec}[c+d x]^2) dx$$

**Problem 712: Result unnecessarily involves imaginary or complex numbers.**

$$\int \sqrt{a + b \operatorname{Sec}[c + d x]} (A + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 4, 355 leaves, 6 steps):

$$-\frac{1}{3 b^2 d} 2 a (a - b) \sqrt{a + b} C \operatorname{Cot}[c + d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right]$$

$$\sqrt{\frac{b(1 - \operatorname{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \operatorname{Sec}[c + d x])}{a - b}} + \frac{1}{3 b d}$$

$$2 \sqrt{a + b} (3 A b - (a - b) C) \operatorname{Cot}[c + d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right]$$

$$\sqrt{\frac{b(1 - \operatorname{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \operatorname{Sec}[c + d x])}{a - b}} - \frac{1}{d}$$

$$2 A \sqrt{a + b} \operatorname{Cot}[c + d x] \operatorname{EllipticPi}\left[\frac{a + b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right]$$

$$\sqrt{\frac{b(1 - \operatorname{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \operatorname{Sec}[c + d x])}{a - b}} + \frac{2 C \sqrt{a + b \operatorname{Sec}[c + d x]} \operatorname{Tan}[c + d x]}{3 d}$$

Result (type 4, 570 leaves):

$$\begin{aligned}
& \frac{1}{3 b \sqrt{\frac{-a+b}{a+b}} d (b+a \cos [c+d x]) (A+2 C+A \cos [2 c+2 d x])} \\
& 4 \cos \left[ \frac{1}{2} (c+d x) \right]^2 \cos [c+d x]^2 \sqrt{a+b \sec [c+d x]} (A+C \sec [c+d x]^2) \\
& \left( 2 i a (a-b) c \sqrt{\frac{\cos [c+d x]}{1+\cos [c+d x]}} \sqrt{\frac{b+a \cos [c+d x]}{(a+b)(1+\cos [c+d x])}} \operatorname{EllipticE} \left[ \right. \right. \\
& \quad \left. \left. i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+d x) \right] \right], \frac{a+b}{a-b} \right] + 2 i (a-b) b (3 A+C) \sqrt{\frac{\cos [c+d x]}{1+\cos [c+d x]}} \right. \\
& \quad \left. \sqrt{\frac{b+a \cos [c+d x]}{(a+b)(1+\cos [c+d x])}} \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+d x) \right] \right], \frac{a+b}{a-b} \right] - \right. \\
& \quad \left. 12 i a A b \sqrt{\frac{\cos [c+d x]}{1+\cos [c+d x]}} \sqrt{\frac{b+a \cos [c+d x]}{(a+b)(1+\cos [c+d x])}} \right. \\
& \quad \left. \operatorname{EllipticPi} \left[ -\frac{a+b}{a-b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+d x) \right] \right], \frac{a+b}{a-b} \right] - \right. \\
& \quad \left. a \sqrt{\frac{-a+b}{a+b}} C \cos [c+d x] (b+a \cos [c+d x]) \sec \left[ \frac{1}{2} (c+d x) \right]^2 \tan \left[ \frac{1}{2} (c+d x) \right] \right) + \\
& \left( \cos [c+d x]^2 \sqrt{a+b \sec [c+d x]} (A+C \sec [c+d x]^2) \left( \frac{4 a C \sin [c+d x]}{3 b} + \frac{4}{3} C \tan [c+d x] \right) \right) / \\
& (d (A+2 C+A \cos [2 c+2 d x]))
\end{aligned}$$

**Problem 713: Result more than twice size of optimal antiderivative.**

$$\int \cos [c+d x] \sqrt{a+b \sec [c+d x]} (A+C \sec [c+d x]^2) dx$$

Optimal (type 4, 352 leaves, 6 steps):



$$\begin{aligned}
 & \frac{1}{bd} (a-b) \sqrt{a+b} (A-2C) \cot[c+dx] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1-\sec[c+dx])}{a+b}} \sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} + \frac{1}{bd} \sqrt{a+b} (Ab+2(a-b)C) \cot[c+dx] \\
 & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec[c+dx])}{a+b}} \sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} - \\
 & \frac{1}{ad} Ab \sqrt{a+b} \cot[c+dx] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1-\sec[c+dx])}{a+b}} \sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} + \frac{A \sqrt{a+b \sec[c+dx]} \sin[c+dx]}{d}
 \end{aligned}$$

Result(type 4, 727 leaves):



twice size of optimal antiderivative.

$$\int \cos [c+d x]^2 \sqrt{a+b \sec [c+d x]} (A+C \sec [c+d x]^2) d x$$

Optimal (type 4, 411 leaves, 7 steps):

$$\begin{aligned} & \frac{1}{4 a d} A (a-b) \sqrt{a+b} \cot [c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{1}{4 a d} \\ & \sqrt{a+b} (A b+2 a(A+4 C)) \cot [c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{1}{4 a^2 d} \\ & \sqrt{a+b} (A b^2-4 a^2(A+2 C)) \cot [c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \\ & \frac{A b \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{4 a d} + \frac{A \cos [c+d x] \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{2 d} \end{aligned}$$

Result (type 4, 1417 leaves):

$$\begin{aligned} & \frac{A \sqrt{a+b \sec [c+d x]} \sin [2(c+d x)]}{4 d} + \\ & \left( \sqrt{a+b \sec [c+d x]} \left( -a A b \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2}(c+d x) \right] - A b^2 \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2}(c+d x) \right] + \right. \right. \\ & \quad \left. \left. 2 a A b \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2}(c+d x) \right]^3 - \right. \right. \\ & \quad \left. \left. a A b \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2}(c+d x) \right]^5 + A b^2 \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2}(c+d x) \right]^5 + \right. \right. \\ & \quad \left. \left. 8 i a^2 A \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2}(c+d x) \right]\right], \frac{a+b}{a-b}\right] \right. \right. \\ & \quad \left. \left. \sqrt{1-\tan \left[ \frac{1}{2}(c+d x) \right]^2} \sqrt{\frac{a+b-a \tan \left[ \frac{1}{2}(c+d x) \right]^2+b \tan \left[ \frac{1}{2}(c+d x) \right]^2}{a+b}} \right. \right. \end{aligned}$$

$$\begin{aligned}
 & 2 \, i \, A b^2 \text{EllipticPi} \left[ -\frac{a+b}{a-b}, \, i \, \text{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+dx) \right] \right], \, \frac{a+b}{a-b} \right] \\
 & \sqrt{1 - \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2} \sqrt{\frac{a+b - a \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2 + b \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} + \\
 & 16 \, i \, a^2 C \text{EllipticPi} \left[ -\frac{a+b}{a-b}, \, i \, \text{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+dx) \right] \right], \, \frac{a+b}{a-b} \right] \\
 & \sqrt{1 - \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2} \sqrt{\frac{a+b - a \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2 + b \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} + \\
 & 8 \, i \, a^2 A \text{EllipticPi} \left[ -\frac{a+b}{a-b}, \, i \, \text{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+dx) \right] \right], \, \frac{a+b}{a-b} \right] \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2 \\
 & \sqrt{1 - \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2} \sqrt{\frac{a+b - a \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2 + b \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} - \\
 & 2 \, i \, A b^2 \text{EllipticPi} \left[ -\frac{a+b}{a-b}, \, i \, \text{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+dx) \right] \right], \, \frac{a+b}{a-b} \right] \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2 \\
 & \sqrt{1 - \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2} \sqrt{\frac{a+b - a \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2 + b \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} + 16 \, i \, a^2 C \\
 & \text{EllipticPi} \left[ -\frac{a+b}{a-b}, \, i \, \text{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+dx) \right] \right], \, \frac{a+b}{a-b} \right] \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2 \\
 & \sqrt{1 - \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2} \sqrt{\frac{a+b - a \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2 + b \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} + \\
 & i \, A (a-b) b \text{EllipticE} \left[ i \, \text{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+dx) \right] \right], \, \frac{a+b}{a-b} \right] \\
 & \sqrt{1 - \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2} \left( 1 + \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2 \right) \\
 & \sqrt{\frac{a+b - a \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2 + b \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} - 2 \, i \, (a-b) (A b + 2 a (A + 2 C))
 \end{aligned}$$

$$\begin{aligned}
 & \text{EllipticF}\left[\text{i ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b-a\tan\left[\frac{1}{2}(c+dx)\right]^2+b\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \Bigg) \Bigg) / \\
 & \left(4a \sqrt{\frac{-a+b}{a+b}} d \sqrt{b+a \cos[c+dx]} \sqrt{\sec[c+dx]} \sqrt{\frac{1}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}} \right. \\
 & \left. \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^{3/2} \right. \\
 & \left. \sqrt{\frac{a+b-a\tan\left[\frac{1}{2}(c+dx)\right]^2+b\tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}} \right) \right)
 \end{aligned}$$

**Problem 715: Result more than twice size of optimal antiderivative.**

$$\int \cos[c+dx]^3 \sqrt{a+b \sec[c+dx]} (A+C \sec[c+dx]^2) dx$$

Optimal (type 4, 502 leaves, 8 steps):

$$\begin{aligned}
 & -\frac{1}{24 a^2 b d} (a-b) \sqrt{a+b} (3 A b^2 - 8 a^2 (2 A + 3 C)) \operatorname{Cot}[c+d x] \operatorname{EllipticE}\left[ \right. \\
 & \quad \left. \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \\
 & \frac{1}{24 a^2 d} \sqrt{a+b} (2 a A b - 3 A b^2 + 8 a^2 (2 A + 3 C)) \operatorname{Cot}[c+d x] \\
 & \quad \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \quad \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \frac{1}{8 a^3 d} \\
 & b \sqrt{a+b} (A b^2 + 4 a^2 (A + 2 C)) \operatorname{Cot}[c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \quad \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \\
 & \frac{(3 A b^2 - 8 a^2 (2 A + 3 C)) \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{24 a^2 d} + \\
 & \frac{A b \operatorname{Cos}[c+d x] \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{12 a d} + \\
 & \frac{A \operatorname{Cos}[c+d x]^2 \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{3 d}
 \end{aligned}$$

Result (type 4, 1347 leaves):

$$\begin{aligned}
 & \frac{1}{d} \sqrt{a+b \operatorname{Sec}[c+d x]} \left( \frac{1}{12} A \operatorname{Sin}[c+d x] + \frac{A b \operatorname{Sin}[2(c+d x)]}{24 a} + \frac{1}{12} A \operatorname{Sin}[3(c+d x)] \right) + \\
 & \left( \sqrt{a+b \operatorname{Sec}[c+d x]} \sqrt{\frac{1}{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}} \right. \\
 & \left. -16 a^3 A \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] -16 a^2 A b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] +3 a A b^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + \right. \\
 & 3 A b^3 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] -24 a^3 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] -24 a^2 b C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + \\
 & 32 a^3 A \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 -6 a A b^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 +48 a^3 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 - \\
 & 16 a^3 A \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 +16 a^2 A b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 +3 a A b^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - \\
 & \left. 3 A b^3 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 -24 a^3 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 +24 a^2 b C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + \right)
 \end{aligned}$$

$$\begin{aligned}
 & 24 a^2 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \\
 & 6 A b^3 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \\
 & \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \\
 & 48 a^2 b C \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \\
 & 24 a^2 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \\
 & 6 A b^3 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \\
 & 48 a^2 b C \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
 & (a+b)\left(-3 A b^2+8 a^2(2 A+3 C)\right) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right) \\
 & \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}}+2 a b(14 a A-A b+24 a C) \\
 & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}
 \end{aligned}$$

$$\left( \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]\right)^2 \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \right) /$$

$$\left( 24 a^2 d \sqrt{b+a \cos[c+dx]} \sqrt{\sec[c+dx]} \sqrt{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} \right.$$

$$\left. \left( a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]\right)^2 \right) - b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right)$$

**Problem 716: Result more than twice size of optimal antiderivative.**

$$\int \cos[c+dx]^4 \sqrt{a+b \sec[c+dx]} (A+C \sec[c+dx]^2) dx$$

Optimal (type 4, 587 leaves, 9 steps):

$$\frac{1}{192 a^3 d} (a-b) \sqrt{a+b} (15 A b^2 + 4 a^2 (7 A + 12 C)) \cot[c+dx]$$

$$\text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec[c+dx])}{a+b}} \sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} -$$

$$\frac{1}{192 a^3 d} \sqrt{a+b} (10 a A b^2 - 15 A b^3 - 24 a^3 (3 A + 4 C) - 4 a^2 b (7 A + 12 C)) \cot[c+dx]$$

$$\text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec[c+dx])}{a+b}} \sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} +$$

$$\frac{1}{64 a^4 d} \sqrt{a+b} (5 A b^4 + 8 a^2 b^2 (A + 2 C) - 16 a^4 (3 A + 4 C)) \cot[c+dx]$$

$$\text{EllipticPi}\left[\frac{a+b}{a}, \text{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec[c+dx])}{a+b}}$$

$$\sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} + \frac{b(15 A b^2 + 4 a^2 (7 A + 12 C)) \sqrt{a+b \sec[c+dx]} \sin[c+dx]}{192 a^3 d} -$$

$$\frac{1}{96 a^2 d} (5 A b^2 - 12 a^2 (3 A + 4 C)) \cos[c+dx] \sqrt{a+b \sec[c+dx]} \sin[c+dx] +$$

$$\frac{A b \cos[c+dx]^2 \sqrt{a+b \sec[c+dx]} \sin[c+dx]}{24 a d} + \frac{A \cos[c+dx]^3 \sqrt{a+b \sec[c+dx]} \sin[c+dx]}{4 d}$$

Result (type 4, 4121 leaves):

$$\frac{1}{d} \sqrt{a+b \sec[c+dx]} \left( \frac{A b \sin[c+dx]}{96 a} + \right.$$



$$\begin{aligned}
 & \left( \frac{(48 a^2 A - 5 A b^2 + 48 a^2 C) \operatorname{Sin}[2 (c + d x)]}{192 a^2} + \frac{A b \operatorname{Sin}[3 (c + d x)]}{96 a} + \frac{1}{32} A \operatorname{Sin}[4 (c + d x)] \right) + \\
 & \left( \left( \frac{3 a A}{8 \sqrt{b + a \operatorname{Cos}[c + d x]} \sqrt{\operatorname{Sec}[c + d x]}} + \frac{A b^2}{96 a \sqrt{b + a \operatorname{Cos}[c + d x]} \sqrt{\operatorname{Sec}[c + d x]}} + \right. \right. \\
 & \quad \frac{a C}{2 \sqrt{b + a \operatorname{Cos}[c + d x]} \sqrt{\operatorname{Sec}[c + d x]}} + \frac{25 A b \sqrt{\operatorname{Sec}[c + d x]}}{96 \sqrt{b + a \operatorname{Cos}[c + d x]}} + \\
 & \quad \frac{5 A b^3 \sqrt{\operatorname{Sec}[c + d x]}}{384 a^2 \sqrt{b + a \operatorname{Cos}[c + d x]}} + \frac{3 b C \sqrt{\operatorname{Sec}[c + d x]}}{8 \sqrt{b + a \operatorname{Cos}[c + d x]}} + \frac{7 A b \operatorname{Cos}[2 (c + d x)] \sqrt{\operatorname{Sec}[c + d x]}}{96 \sqrt{b + a \operatorname{Cos}[c + d x]}} + \\
 & \quad \left. \left. \frac{5 A b^3 \operatorname{Cos}[2 (c + d x)] \sqrt{\operatorname{Sec}[c + d x]}}{128 a^2 \sqrt{b + a \operatorname{Cos}[c + d x]}} + \frac{b C \operatorname{Cos}[2 (c + d x)] \sqrt{\operatorname{Sec}[c + d x]}}{8 \sqrt{b + a \operatorname{Cos}[c + d x]}} \right) \right) \\
 & \sqrt{a + b \operatorname{Sec}[c + d x]} \left( \left( b (15 A b^2 + 4 a^2 (7 A + 12 C)) \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right] \right. \right. \\
 & \quad \left. \left. \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2}} \right) / \left( 192 a^3 \sqrt{\frac{1 + \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2}{1 - \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2}} \right) + \right. \\
 & \quad \left( b (a + b) (15 A b^2 + 4 a^2 (7 A + 12 C)) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]\right], \frac{a - b}{a + b}\right] - \right. \\
 & \quad 2 a (2 a A b^2 + 5 A b^3 + 24 a^3 (3 A + 4 C) - 12 a^2 b (3 A + 4 C)) \operatorname{EllipticF}\left[ \right. \\
 & \quad \quad \left. \operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]\right], \frac{a - b}{a + b}\right] - 6 (-5 A b^4 - 8 a^2 b^2 (A + 2 C) + 16 a^4 (3 A + 4 C)) \\
 & \quad \left. \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]\right], \frac{a - b}{a + b}\right] \right) \\
 & \quad \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2}{a + b}} \\
 & \quad \left. \left. \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2}} \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^4} \right) / \right. \\
 & \quad \left. \left( 192 a^3 \sqrt{\frac{1}{1 - \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2}} \left( b - b \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^4 + a \left( -1 + \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2 \right)^2 \right) \right) \right) /
 \end{aligned}$$

$$\left( d \sqrt{b + a \cos [c + d x]} \sqrt{\sec [c + d x]} \left( \left( b (15 A b^2 + 4 a^2 (7 A + 12 C)) \sec \left[ \frac{1}{2} (c + d x) \right]^2 \right. \right. \right.$$

$$\left. \left. \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \right) / \left( 384 a^3 \sqrt{\frac{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \right) - \right.$$

$$\left. \left( b (a + b) (15 A b^2 + 4 a^2 (7 A + 12 C)) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a - b}{a + b} \right] - \right. \right.$$

$$\left. \left. 2 a (2 a A b^2 + 5 A b^3 + 24 a^3 (3 A + 4 C) - 12 a^2 b (3 A + 4 C)) \operatorname{EllipticF} \left[ \right. \right. \right.$$

$$\left. \left. \operatorname{ArcSin} \left[ \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a - b}{a + b} \right] - 6 (-5 A b^4 - 8 a^2 b^2 (A + 2 C) + 16 a^4 (3 A + 4 C)) \right. \right.$$

$$\left. \left. \operatorname{EllipticPi} \left[ -1, -\operatorname{ArcSin} \left[ \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a - b}{a + b} \right] \right) \right.$$

$$\left. \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} \right.$$

$$\left. \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \right.$$

$$\left. \sqrt{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^4} \left( -2 b \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right]^3 + \right. \right.$$

$$\left. \left. 2 a \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) \right) /$$

$$\left( 192 a^3 \sqrt{\frac{1}{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \left( b - b \tan \left[ \frac{1}{2} (c + d x) \right]^4 + a \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right)^2 \right)^2 \right) -$$

$$\left( b (a + b) (15 A b^2 + 4 a^2 (7 A + 12 C)) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a - b}{a + b} \right] - \right.$$

$$\left. \left. 2 a (2 a A b^2 + 5 A b^3 + 24 a^3 (3 A + 4 C) - 12 a^2 b (3 A + 4 C)) \operatorname{EllipticF} \left[ \right. \right. \right.$$

$$\left. \left. \operatorname{ArcSin} \left[ \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a - b}{a + b} \right] - 6 (-5 A b^4 - 8 a^2 b^2 (A + 2 C) + 16 a^4 (3 A + 4 C)) \right. \right.$$

$$\left. \left. \operatorname{EllipticPi} \left[ -1, -\operatorname{ArcSin} \left[ \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a - b}{a + b} \right] \right) \sec \left[ \frac{1}{2} (c + d x) \right]^2$$

$$\begin{aligned}
 & \tan\left[\frac{1}{2}(c+dx)\right]^3 \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \\
 & \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}} \Big/ \left(192 a^3 \sqrt{\frac{1}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}}\right. \\
 & \left.\sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^4} \left(b-b \tan\left[\frac{1}{2}(c+dx)\right]^4+a \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2\right)\right) + \\
 & \left( \left(b(a+b)(15Ab^2+4a^2(7A+12C)) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] - \right. \right. \\
 & \quad 2a(2aAb^2+5Ab^3+24a^3(3A+4C)-12a^2b(3A+4C)) \operatorname{EllipticF}\left[ \right. \\
 & \quad \quad \left. \operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] - 6(-5Ab^4-8a^2b^2(A+2C)+16a^4(3A+4C)) \\
 & \quad \quad \left. \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \right) \\
 & \quad \left(-a \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + b \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) \\
 & \quad \left. \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^4} \right) \Big/ \\
 & \left(384 a^3(a+b) \sqrt{\frac{1}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right. \\
 & \quad \left. \left(b-b \tan\left[\frac{1}{2}(c+dx)\right]^4+a \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2\right)\right) - \\
 & \frac{1}{384 a^3 \left(b-b \tan\left[\frac{1}{2}(c+dx)\right]^4+a \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2\right)} \\
 & \left( \left(b(a+b)(15Ab^2+4a^2(7A+12C)) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] - \right. \right. \\
 & \quad 2a(2aAb^2+5Ab^3+24a^3(3A+4C)-12a^2b(3A+4C)) \operatorname{EllipticF}\left[ \right. \\
 & \quad \quad \left. \operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] - 6(-5Ab^4-8a^2b^2(A+2C)+16a^4(3A+4C)) \\
 & \quad \quad \left. \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right] \sqrt{\frac{1}{1-\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \\
 & \sqrt{\frac{a+b-a \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \\
 & \sqrt{\frac{a+b-a \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1+\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{1-\text{Tan}\left[\frac{1}{2}(c+dx)\right]^4} - \\
 & \left( b (15 A b^2 + 4 a^2 (7 A + 12 C)) \text{Tan}\left[\frac{1}{2}(c+dx)\right] \right. \\
 & \left. \sqrt{\frac{a+b-a \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1+\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \right. \\
 & \left. \left( \frac{\text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right]}{1-\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2} + \left( \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right. \right. \\
 & \left. \left. \left( 1 + \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \left( 1 - \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) \right) / \\
 & \left( 384 a^3 \left( \frac{1 + \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 - \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{3/2} \right) + \left( b (15 A b^2 + 4 a^2 (7 A + 12 C)) \text{Tan}\left[\frac{1}{2}(c+dx)\right] \right. \\
 & \left. \left( \left( -a \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right] + b \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right] \right) / \right. \right. \\
 & \left. \left( 1 + \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - \left( \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right. \right. \\
 & \left. \left. \left( a + b - a \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \left( 1 + \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) \right) / \\
 & \left( 384 a^3 \sqrt{\frac{1 + \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 - \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{\frac{a+b-a \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1+\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \right) + \\
 & \left( b (a+b) (15 A b^2 + 4 a^2 (7 A + 12 C)) \text{EllipticE}\left[\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] - \right. \\
 & \left. 2 a (2 a A b^2 + 5 A b^3 + 24 a^3 (3 A + 4 C) - 12 a^2 b (3 A + 4 C)) \text{EllipticF}\left[ \right. \right. \\
 & \left. \left. \text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] - 6 (-5 A b^4 - 8 a^2 b^2 (A + 2 C) + 16 a^4 (3 A + 4 C)) \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \text{EllipticPi}\left[-1, -\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{\frac{a+b-a \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \sqrt{1-\text{Tan}\left[\frac{1}{2}(c+dx)\right]^4} \\
 & \left(\left(-a \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right]+b \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right]\right) / \right. \\
 & \quad \left.\left(1+\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)-\left(\text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right]\right)\right. \\
 & \quad \left.\left(a+b-a \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)\right) / \left(1+\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \right) / \\
 & \left(384 a^3 \sqrt{\frac{1}{1-\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{\frac{a+b-a \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1+\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}}\right. \\
 & \quad \left.\left(b-b \text{Tan}\left[\frac{1}{2}(c+dx)\right]^4+a\left(-1+\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^2\right)\right) + \\
 & \left(\sqrt{\frac{a+b-a \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}}\right. \\
 & \quad \sqrt{\frac{a+b-a \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1+\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{1-\text{Tan}\left[\frac{1}{2}(c+dx)\right]^4} \\
 & \quad \left.-\left(\left(a\left(2 a A b^2+5 A b^3+24 a^3(3 A+4 C)-12 a^2 b(3 A+4 C)\right) \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2\right) / \right.\right. \\
 & \quad \left.\left(\sqrt{1-\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{1-\frac{(a-b) \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}}\right)\right) + \\
 & \quad \left.\left(3\left(-5 A b^4-8 a^2 b^2(A+2 C)+16 a^4(3 A+4 C)\right) \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2\right) / \right. \\
 & \quad \left.\left(\sqrt{1-\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}\left(1+\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{1-\frac{(a-b) \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}}\right)\right) +
 \end{aligned}$$

$$\left( b (a+b) (15 A b^2 + 4 a^2 (7 A + 12 C)) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{1 - \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) / \left( 2 \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right) \right) / \left( 192 a^3 \sqrt{\frac{1}{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \left( b - b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^4 + a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) \right) \right)$$

**Problem 717: Attempted integration timed out after 120 seconds.**

$$\int \operatorname{Sec}[c+dx]^3 (a+b \operatorname{Sec}[c+dx])^{3/2} (A+C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 4, 550 leaves, 8 steps):

$$\frac{1}{1155 b^5 d} 4 a (a-b) \sqrt{a+b} (8 a^4 C + 3 a^2 b^2 (11 A + 6 C) - b^4 (451 A + 348 C))$$

$$\operatorname{Cot}[c+dx] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}} + \frac{1}{1155 b^4 d}$$

$$2(a-b) \sqrt{a+b} (16 a^4 C + 12 a^3 b C + 6 a^2 b^2 (11 A + 8 C) - 25 b^4 (11 A + 9 C) + 3 a b^3 (209 A + 157 C))$$

$$\operatorname{Cot}[c+dx] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}} + \frac{1}{1155 b^3 d}$$

$$2(8 a^4 C + 25 b^4 (11 A + 9 C) + a^2 b^2 (33 A + 19 C)) \sqrt{a+b \operatorname{Sec}[c+dx]} \operatorname{Tan}[c+dx] +$$

$$\frac{1}{1155 b^2 d} 4 a (132 A b^2 - 3 a^2 C + 101 b^2 C) \operatorname{Sec}[c+dx] \sqrt{a+b \operatorname{Sec}[c+dx]} \operatorname{Tan}[c+dx] +$$

$$\frac{1}{231 b d} 2(a^2 C + 3 b^2 (11 A + 9 C)) \operatorname{Sec}[c+dx]^2 \sqrt{a+b \operatorname{Sec}[c+dx]} \operatorname{Tan}[c+dx] +$$

$$\frac{2 a C \operatorname{Sec}[c+dx]^3 \sqrt{a+b \operatorname{Sec}[c+dx]} \operatorname{Tan}[c+dx]}{33 d} +$$

$$\frac{2 C \operatorname{Sec}[c+dx]^3 (a+b \operatorname{Sec}[c+dx])^{3/2} \operatorname{Tan}[c+dx]}{11 d}$$

Result (type 1, 1 leaves):

???

### Problem 718: Attempted integration timed out after 120 seconds.

$$\int \text{Sec}[c + d x]^2 (a + b \text{Sec}[c + d x])^{3/2} (A + C \text{Sec}[c + d x]^2) dx$$

Optimal (type 4, 454 leaves, 7 steps):

$$\begin{aligned}
 & -\frac{1}{315 b^4 d} 2 (a - b) \sqrt{a + b} (8 a^4 C + 21 b^4 (9 A + 7 C) + 3 a^2 b^2 (21 A + 11 C)) \\
 & \quad \text{Cot}[c + d x] \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \\
 & \quad \sqrt{\frac{b(1 - \text{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \text{Sec}[c + d x])}{a - b}} - \frac{1}{315 b^3 d} \\
 & 2 (a - b) \sqrt{a + b} (8 a^3 C + 6 a^2 b C - 21 b^3 (9 A + 7 C) + 3 a b^2 (21 A + 13 C)) \text{Cot}[c + d x] \\
 & \quad \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \sqrt{\frac{b(1 - \text{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \text{Sec}[c + d x])}{a - b}} + \\
 & \quad \frac{2 a (63 A b^2 + 8 a^2 C + 39 b^2 C) \sqrt{a + b \text{Sec}[c + d x]} \text{Tan}[c + d x]}{315 b^2 d} + \\
 & \quad \frac{2 (8 a^2 C + 7 b^2 (9 A + 7 C)) (a + b \text{Sec}[c + d x])^{3/2} \text{Tan}[c + d x]}{315 b^2 d} - \\
 & \quad \frac{8 a C (a + b \text{Sec}[c + d x])^{5/2} \text{Tan}[c + d x]}{63 b^2 d} + \frac{2 C \text{Sec}[c + d x] (a + b \text{Sec}[c + d x])^{5/2} \text{Tan}[c + d x]}{9 b d}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

### Problem 719: Attempted integration timed out after 120 seconds.

$$\int \text{Sec}[c + d x] (a + b \text{Sec}[c + d x])^{3/2} (A + C \text{Sec}[c + d x]^2) dx$$

Optimal (type 4, 374 leaves, 6 steps):

$$\begin{aligned}
 & -\frac{1}{105 b^3 d} 4 a (a-b) \sqrt{a+b} (70 A b^2 - 3 a^2 C + 41 b^2 C) \operatorname{Cot}[c+d x] \operatorname{EllipticE}\left[ \right. \\
 & \quad \left. \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \\
 & \frac{1}{105 b^2 d} 2 (a-b) \sqrt{a+b} (105 a A b - 35 A b^2 + 6 a^2 C + 57 a b C - 25 b^2 C) \operatorname{Cot}[c+d x] \\
 & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \\
 & \frac{2(6 a^2 C - 5 b^2(7 A + 5 C)) \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x]}{105 b d} - \\
 & \frac{4 a C (a+b \operatorname{Sec}[c+d x])^{3/2} \operatorname{Tan}[c+d x]}{35 b d} + \frac{2 C (a+b \operatorname{Sec}[c+d x])^{5/2} \operatorname{Tan}[c+d x]}{7 b d}
 \end{aligned}$$

Result(type 1, 1 leaves):

???

### Problem 720: Result more than twice size of optimal antiderivative.

$$\int (a+b \operatorname{Sec}[c+d x])^{3/2} (A+C \operatorname{Sec}[c+d x])^2 dx$$

Optimal(type 4, 415 leaves, 7 steps):

$$\begin{aligned}
 & -\frac{1}{5 b^2 d} 2 (a-b) \sqrt{a+b} (a^2 C + b^2 (5 A + 3 C)) \operatorname{Cot}[c+d x] \operatorname{EllipticE}\left[ \right. \\
 & \quad \left. \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \\
 & \frac{1}{5 b d} 2 \sqrt{a+b} (a^2 C - 2 a b (5 A + 2 C) + b^2 (5 A + 3 C)) \operatorname{Cot}[c+d x] \\
 & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \\
 & \frac{1}{d} 2 a A \sqrt{a+b} \operatorname{Cot}[c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \\
 & \frac{2 a C \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x]}{5 d} + \frac{2 C (a+b \operatorname{Sec}[c+d x])^{3/2} \operatorname{Tan}[c+d x]}{5 d}
 \end{aligned}$$

Result(type 4, 1023 leaves):





$$\left( 5 b d (b + a \cos [c + d x])^{3/2} (A + 2 C + A \cos [2 c + 2 d x]) \sec [c + d x]^{7/2} \right. \\ \left. \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)^{3/2} \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \right) + \\ \left( \cos [c + d x]^3 (a + b \sec [c + d x])^{3/2} (A + C \sec [c + d x]^2) \right. \\ \left. \left( \frac{4 (5 A b^2 + a^2 C + 3 b^2 C) \sin [c + d x]}{5 b} + \right. \right. \\ \left. \left. \frac{8}{5} a C \tan [c + d x] + \frac{4}{5} b C \sec [c + d x] \tan [c + d x] \right) \right) / \\ (d (b + a \cos [c + d x]) (A + 2 C + A \cos [2 c + 2 d x]))$$

**Problem 722: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \cos [c + d x]^2 (a + b \sec [c + d x])^{3/2} (A + C \sec [c + d x]^2) dx$$

Optimal (type 4, 414 leaves, 7 steps):

$$\frac{1}{4 d} (a - b) \sqrt{a + b} (5 A - 8 C) \cot [c + d x] \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \sec [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \\ \sqrt{\frac{b (1 - \sec [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \sec [c + d x])}{a - b}} + \frac{1}{4 d} \\ \sqrt{a + b} (2 a A + 5 A b + 16 a C - 8 b C) \cot [c + d x] \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \sec [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \\ \sqrt{\frac{b (1 - \sec [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \sec [c + d x])}{a - b}} - \frac{1}{4 a d} \\ \sqrt{a + b} (3 A b^2 + 4 a^2 (A + 2 C)) \cot [c + d x] \operatorname{EllipticPi} \left[ \frac{a + b}{a}, \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \sec [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \\ \sqrt{\frac{b (1 - \sec [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \sec [c + d x])}{a - b}} + \\ \frac{3 A b \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{4 d} + \frac{A \cos [c + d x] (a + b \sec [c + d x])^{3/2} \sin [c + d x]}{2 d}$$

Result (type 4, 1618 leaves):

$$\begin{aligned}
 & \frac{1}{2} \left( \left( \cos [c+d x] (a+b \sec [c+d x])^{3/2} \left( 4 b C \sin [c+d x] + \frac{1}{2} a A \sin [2(c+d x)] \right) \right) \right) / \\
 & \quad (d (b+a \cos [c+d x])) - \\
 & \quad \left( (a+b \sec [c+d x])^{3/2} \left( 5 a A b \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+d x) \right] + 5 A b^2 \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+d x) \right] - \right. \right. \\
 & \quad 8 a b \sqrt{\frac{-a+b}{a+b}} C \tan \left[ \frac{1}{2} (c+d x) \right] - 8 b^2 \sqrt{\frac{-a+b}{a+b}} C \tan \left[ \frac{1}{2} (c+d x) \right] - \\
 & \quad 10 a A b \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+d x) \right]^3 + 16 a b \sqrt{\frac{-a+b}{a+b}} C \tan \left[ \frac{1}{2} (c+d x) \right]^3 + \\
 & \quad 5 a A b \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+d x) \right]^5 - 5 A b^2 \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+d x) \right]^5 - \\
 & \quad 8 a b \sqrt{\frac{-a+b}{a+b}} C \tan \left[ \frac{1}{2} (c+d x) \right]^5 + 8 b^2 \sqrt{\frac{-a+b}{a+b}} C \tan \left[ \frac{1}{2} (c+d x) \right]^5 - \\
 & \quad 8 i a^2 A \operatorname{EllipticPi} \left[ -\frac{a+b}{a-b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+d x) \right] \right], \frac{a+b}{a-b} \right] \\
 & \quad \sqrt{1 - \tan \left[ \frac{1}{2} (c+d x) \right]^2} \sqrt{\frac{a+b - a \tan \left[ \frac{1}{2} (c+d x) \right]^2 + b \tan \left[ \frac{1}{2} (c+d x) \right]^2}{a+b}} - \\
 & \quad 6 i A b^2 \operatorname{EllipticPi} \left[ -\frac{a+b}{a-b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+d x) \right] \right], \frac{a+b}{a-b} \right] \\
 & \quad \sqrt{1 - \tan \left[ \frac{1}{2} (c+d x) \right]^2} \sqrt{\frac{a+b - a \tan \left[ \frac{1}{2} (c+d x) \right]^2 + b \tan \left[ \frac{1}{2} (c+d x) \right]^2}{a+b}} - \\
 & \quad 16 i a^2 C \operatorname{EllipticPi} \left[ -\frac{a+b}{a-b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+d x) \right] \right], \frac{a+b}{a-b} \right] \\
 & \quad \sqrt{1 - \tan \left[ \frac{1}{2} (c+d x) \right]^2} \sqrt{\frac{a+b - a \tan \left[ \frac{1}{2} (c+d x) \right]^2 + b \tan \left[ \frac{1}{2} (c+d x) \right]^2}{a+b}} - 8 i a^2 A \\
 & \quad \operatorname{EllipticPi} \left[ -\frac{a+b}{a-b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+d x) \right] \right], \frac{a+b}{a-b} \right] \tan \left[ \frac{1}{2} (c+d x) \right]^2
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - 6 i A b^2 \\
 & \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - 16 i a^2 C \\
 & \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & i (a-b) b (5A - 8C) \text{EllipticE}\left[i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \\
 & \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + 2 i (a-b) (b(A - 4C) + 2a(A + 2C)) \\
 & \text{EllipticF}\left[i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) / \\
 & \left(2 \sqrt{\frac{-a+b}{a+b}} d (b+a \cos[c+dx])^{3/2} \text{Sec}[c+dx]^{3/2} \sqrt{\frac{1}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}} \right. \\
 & \left. \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^{3/2} \right. \\
 & \left. \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}} \right) \right)
 \end{aligned}$$

### Problem 723: Result more than twice size of optimal antiderivative.

$$\int \cos [c + d x]^3 (a + b \operatorname{Sec} [c + d x])^{3/2} (A + C \operatorname{Sec} [c + d x]^2) dx$$

Optimal (type 4, 504 leaves, 8 steps):

$$\begin{aligned} & \frac{1}{24 a b d} (a - b) \sqrt{a + b} (3 A b^2 + 8 a^2 (2 A + 3 C)) \operatorname{Cot} [c + d x] \\ & \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \operatorname{Sec} [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \sqrt{\frac{b (1 - \operatorname{Sec} [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec} [c + d x])}{a - b}} + \\ & \frac{1}{24 a d} \sqrt{a + b} (16 a^2 A + 14 a A b + 3 A b^2 + 24 a^2 C + 48 a b C) \operatorname{Cot} [c + d x] \\ & \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \operatorname{Sec} [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \sqrt{\frac{b (1 - \operatorname{Sec} [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec} [c + d x])}{a - b}} + \\ & \frac{1}{8 a^2 d} b \sqrt{a + b} (A b^2 - 12 a^2 (A + 2 C)) \operatorname{Cot} [c + d x] \\ & \operatorname{EllipticPi} \left[ \frac{a + b}{a}, \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \operatorname{Sec} [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \sqrt{\frac{b (1 - \operatorname{Sec} [c + d x])}{a + b}} \\ & \sqrt{-\frac{b (1 + \operatorname{Sec} [c + d x])}{a - b}} + \frac{(3 A b^2 + 8 a^2 (2 A + 3 C)) \sqrt{a + b \operatorname{Sec} [c + d x]} \operatorname{Sin} [c + d x]}{24 a d} + \\ & \frac{A b \operatorname{Cos} [c + d x] \sqrt{a + b \operatorname{Sec} [c + d x]} \operatorname{Sin} [c + d x]}{4 d} + \frac{A \operatorname{Cos} [c + d x]^2 (a + b \operatorname{Sec} [c + d x])^{3/2} \operatorname{Sin} [c + d x]}{3 d} \end{aligned}$$

Result (type 4, 1393 leaves):

$$\begin{aligned} & \left( \cos [c + d x]^3 (a + b \operatorname{Sec} [c + d x])^{3/2} (A + C \operatorname{Sec} [c + d x]^2) \right. \\ & \left. \left( \frac{1}{6} a A \operatorname{Sin} [c + d x] + \frac{7}{12} A b \operatorname{Sin} [2 (c + d x)] + \frac{1}{6} a A \operatorname{Sin} [3 (c + d x)] \right) \right) / \\ & (d (b + a \operatorname{Cos} [c + d x]) (A + 2 C + A \operatorname{Cos} [2 c + 2 d x])) + \\ & \left( (a + b \operatorname{Sec} [c + d x])^{3/2} (A + C \operatorname{Sec} [c + d x]^2) \sqrt{\frac{1}{1 - \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}} \right. \\ & \left( 16 a^3 A \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] + 16 a^2 A b \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] + 3 a A b^2 \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] + \right. \\ & 3 A b^3 \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] + 24 a^3 C \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] + 24 a^2 b C \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] - \\ & \left. \left. 32 a^3 A \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^3 - 6 a A b^2 \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^3 - 48 a^3 C \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^3 + \right. \right. \end{aligned}$$

$$\begin{aligned}
 & 16 a^3 A \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - 16 a^2 A b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + 3 a A b^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - \\
 & 3 A b^3 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + 24 a^3 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - 24 a^2 b C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - \\
 & 72 a^2 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \\
 & 6 A b^3 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \\
 & \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
 & 144 a^2 b C \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
 & 72 a^2 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \\
 & 6 A b^3 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
 & 144 a^2 b C \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \\
 & (a+b)\left(3 A b^2+8 a^2(2 A+3 C)\right) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right) \\
 & \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}}-2 a b(26 a A-7 A b+48 a C-24 b C)
 \end{aligned}$$

$$\begin{aligned}
 & \text{EllipticF}\left[\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1+\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b-a\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \Bigg) \Bigg) / \\
 & \left(12ad(b+a\text{Cos}[c+dx])^{3/2}(A+2C+A\text{Cos}[2c+2dx])\text{Sec}[c+dx]^{7/2}\right. \\
 & \left.\left(1+\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^{3/2} \sqrt{\frac{a+b-a\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1+\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}}\right)\right)
 \end{aligned}$$

**Problem 724: Result more than twice size of optimal antiderivative.**

$$\int \text{Cos}[c+dx]^4 (a+b\text{Sec}[c+dx])^{3/2} (A+C\text{Sec}[c+dx]^2) dx$$

Optimal (type 4, 583 leaves, 9 steps):

$$\begin{aligned}
 & -\frac{1}{64 a^2 d} (a-b) \sqrt{a+b} (3 A b^2-4 a^2(13 A+20 C)) \operatorname{Cot}[c+d x] \operatorname{EllipticE}\left[\right. \\
 & \quad \left. \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \\
 & \frac{1}{64 a^2 d} \sqrt{a+b} (2 a A b^2-3 A b^3+8 a^3(3 A+4 C)+a^2(52 A b+80 b C)) \operatorname{Cot}[c+d x] \\
 & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \\
 & \frac{1}{64 a^3 d} \sqrt{a+b} (3 A b^4+24 a^2 b^2(A+2 C)+16 a^4(3 A+4 C)) \operatorname{Cot}[c+d x] \\
 & \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \\
 & \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \frac{b(3 A b^2-4 a^2(13 A+20 C)) \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{64 a^2 d} + \\
 & \frac{(A b^2+4 a^2(3 A+4 C)) \operatorname{Cos}[c+d x] \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{32 a d} + \\
 & \frac{A b \operatorname{Cos}[c+d x]^2 \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{8 d} + \\
 & \frac{A \operatorname{Cos}[c+d x]^3 (a+b \operatorname{Sec}[c+d x])^{3 / 2} \operatorname{Sin}[c+d x]}{4 d}
 \end{aligned}$$

Result (type 4, 4278 leaves):

$$\begin{aligned}
 & \left( \operatorname{Cos}[c+d x]^3 (a+b \operatorname{Sec}[c+d x])^{3 / 2} (A+C \operatorname{Sec}[c+d x]^2) \right. \\
 & \quad \left( \frac{3}{16} A b \operatorname{Sin}[c+d x] + \frac{(16 a^2 A+A b^2+16 a^2 C) \operatorname{Sin}[2(c+d x)]}{32 a} + \frac{3}{16} A b \operatorname{Sin}[3(c+d x)] + \right. \\
 & \quad \left. \left. \frac{1}{16} a A \operatorname{Sin}[4(c+d x)] \right) \right) / (d(b+a \operatorname{Cos}[c+d x])(A+2 C+A \operatorname{Cos}[2 c+2 d x])) + \\
 & \left( \left( \frac{3 a^2 A}{4 \sqrt{b+a \operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]}} + \frac{19 A b^2}{16 \sqrt{b+a \operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]}} + \right. \right. \\
 & \quad \frac{a^2 C}{\sqrt{b+a \operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]}} + \frac{2 b^2 C}{\sqrt{b+a \operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]}} + \\
 & \quad \frac{19 a A b \sqrt{\operatorname{Sec}[c+d x]}}{16 \sqrt{b+a \operatorname{Cos}[c+d x]}} - \frac{A b^3 \sqrt{\operatorname{Sec}[c+d x]}}{64 a \sqrt{b+a \operatorname{Cos}[c+d x]}} + \frac{7 a b C \sqrt{\operatorname{Sec}[c+d x]}}{4 \sqrt{b+a \operatorname{Cos}[c+d x]}} + \\
 & \quad \left. \left. \frac{13 a A b \operatorname{Cos}[2(c+d x)] \sqrt{\operatorname{Sec}[c+d x]}}{16 \sqrt{b+a \operatorname{Cos}[c+d x]}} - \frac{3 A b^3 \operatorname{Cos}[2(c+d x)] \sqrt{\operatorname{Sec}[c+d x]}}{64 a \sqrt{b+a \operatorname{Cos}[c+d x]}} \right) \right) +
 \end{aligned}$$



$$\begin{aligned}
 & \frac{5 a b C \cos \left[ 2 (c+d x) \right] \sqrt{\sec [c+d x]}}{4 \sqrt{b+a \cos [c+d x]}} \left( a+b \sec [c+d x] \right)^{3 / 2} \\
 & (A+C \sec [c+d x])^2 \left( \left( b \left( -3 A b^2+a^2 (52 A+80 C) \right) \tan \left[ \frac{1}{2} (c+d x) \right] \right. \right. \\
 & \left. \left. \sqrt{\frac{a+b-a \tan \left[ \frac{1}{2} (c+d x) \right]^2+b \tan \left[ \frac{1}{2} (c+d x) \right]^2}{1+\tan \left[ \frac{1}{2} (c+d x) \right]^2}} \right) / \left( 32 a^2 \sqrt{\frac{1+\tan \left[ \frac{1}{2} (c+d x) \right]^2}{1-\tan \left[ \frac{1}{2} (c+d x) \right]^2}} \right) - \right. \\
 & \left. \left( b (a+b) \left( 3 A b^2-4 a^2 (13 A+20 C) \right) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \tan \left[ \frac{1}{2} (c+d x) \right] \right], \frac{a-b}{a+b} \right] + \right. \right. \\
 & \left. \left. 2 \left( a \left( -A b^3+8 a^3 (3 A+4 C) -4 a^2 b (3 A+4 C) +2 a b^2 (19 A+32 C) \right) \operatorname{EllipticF} \left[ \right. \right. \right. \right. \\
 & \left. \left. \left. \operatorname{ArcSin} \left[ \tan \left[ \frac{1}{2} (c+d x) \right] \right], \frac{a-b}{a+b} \right] + \left( 3 A b^4+24 a^2 b^2 (A+2 C) +16 a^4 (3 A+4 C) \right) \right. \right. \\
 & \left. \left. \left. \operatorname{EllipticPi} \left[ -1,-\operatorname{ArcSin} \left[ \tan \left[ \frac{1}{2} (c+d x) \right] \right], \frac{a-b}{a+b} \right] \right) \right) \right) \\
 & \left. \sqrt{\frac{a+b-a \tan \left[ \frac{1}{2} (c+d x) \right]^2+b \tan \left[ \frac{1}{2} (c+d x) \right]^2}{a+b}} \right. \\
 & \left. \sqrt{\frac{a+b-a \tan \left[ \frac{1}{2} (c+d x) \right]^2+b \tan \left[ \frac{1}{2} (c+d x) \right]^2}{1+\tan \left[ \frac{1}{2} (c+d x) \right]^2}} \sqrt{1-\tan \left[ \frac{1}{2} (c+d x) \right]^4} \right) / \\
 & \left. \left( 32 a^2 \sqrt{\frac{1}{1-\tan \left[ \frac{1}{2} (c+d x) \right]^2}} \left( b-b \tan \left[ \frac{1}{2} (c+d x) \right]^4+a \left( -1+\tan \left[ \frac{1}{2} (c+d x) \right]^2 \right)^2 \right) \right) \right) / \\
 & \left( d (b+a \cos [c+d x])^{3 / 2} (A+2 C+A \cos [2 c+2 d x]) \sec [c+d x]^{7 / 2} \right. \\
 & \left. \left( \left( b \left( -3 A b^2+a^2 (52 A+80 C) \right) \sec \left[ \frac{1}{2} (c+d x) \right]^2 \right. \right. \right. \\
 & \left. \left. \sqrt{\frac{a+b-a \tan \left[ \frac{1}{2} (c+d x) \right]^2+b \tan \left[ \frac{1}{2} (c+d x) \right]^2}{1+\tan \left[ \frac{1}{2} (c+d x) \right]^2}} \right) / \left( 64 a^2 \sqrt{\frac{1+\tan \left[ \frac{1}{2} (c+d x) \right]^2}{1-\tan \left[ \frac{1}{2} (c+d x) \right]^2}} \right) + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( b (a+b) (3 A b^2 - 4 a^2 (13 A + 20 C)) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] + \right. \\
 & 2 \left( a (-A b^3 + 8 a^3 (3 A + 4 C) - 4 a^2 b (3 A + 4 C) + 2 a b^2 (19 A + 32 C)) \operatorname{EllipticF}\left[ \right. \right. \\
 & \quad \operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] + (3 A b^4 + 24 a^2 b^2 (A + 2 C) + 16 a^4 (3 A + 4 C)) \\
 & \quad \left. \left. \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right]\right) \right) \\
 & \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} \\
 & \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}} \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^4}\left(-2 b \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 + \right. \\
 & \left. 2 a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)\right) \Big/ \\
 & \left( 32 a^2 \sqrt{\frac{1}{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}}\left(b-b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^4+a\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)^2\right)^2 \right) + \\
 & \left( b (a+b) (3 A b^2 - 4 a^2 (13 A + 20 C)) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] + \right. \\
 & 2 \left( a (-A b^3 + 8 a^3 (3 A + 4 C) - 4 a^2 b (3 A + 4 C) + 2 a b^2 (19 A + 32 C)) \operatorname{EllipticF}\left[ \right. \right. \\
 & \quad \operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] + (3 A b^4 + 24 a^2 b^2 (A + 2 C) + 16 a^4 (3 A + 4 C)) \\
 & \quad \left. \left. \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right]\right) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} \\
 & \left. \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}} \right) \Big/ \left( 32 a^2 \sqrt{\frac{1}{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^4} \left( b - b \tan\left[\frac{1}{2}(c+dx)\right]^4 + a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) \right) - \\
 & \left( b(a+b)(3Ab^2 - 4a^2(13A + 20C)) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] + \right. \\
 & \quad 2 \left( a(-Ab^3 + 8a^3(3A + 4C) - 4a^2b(3A + 4C) + 2ab^2(19A + 32C)) \operatorname{EllipticF}\left[ \right. \right. \\
 & \quad \quad \left. \operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] + (3Ab^4 + 24a^2b^2(A + 2C) + 16a^4(3A + 4C)) \right. \\
 & \quad \quad \left. \left. \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \right) \right) \\
 & \quad \left( -a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + b \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \\
 & \quad \left. \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^4} \right) / \\
 & \left( 64a^2(a+b) \sqrt{\frac{1}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right. \\
 & \quad \left. \left( b - b \tan\left[\frac{1}{2}(c+dx)\right]^4 + a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) \right) + \\
 & \frac{1}{64a^2 \left( b - b \tan\left[\frac{1}{2}(c+dx)\right]^4 + a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right)} \\
 & \left( b(a+b)(3Ab^2 - 4a^2(13A + 20C)) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] + \right. \\
 & \quad 2 \left( a(-Ab^3 + 8a^3(3A + 4C) - 4a^2b(3A + 4C) + 2ab^2(19A + 32C)) \right. \\
 & \quad \quad \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] + (3Ab^4 + 24a^2b^2(A + 2C) + \right. \right. \\
 & \quad \quad \left. \left. 16a^4(3A + 4C)) \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \right) \right) \\
 & \quad \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \sqrt{\frac{1}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}} \\
 & \quad \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}}
 \end{aligned}$$

$$\begin{aligned}
& \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^4} - \\
& \left( b(-3Ab^2+a^2(52A+80C)) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right. \\
& \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \\
& \left. \left( \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} + \left( \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right. \right. \\
& \left. \left. \left( 1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \left( 1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) \right) / \\
& \left( 64a^2 \left( \frac{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{3/2} \right) + \left( b(-3Ab^2+a^2(52A+80C)) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right. \\
& \left. \left( \left( -a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + b \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) / \right. \right. \\
& \left. \left( 1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - \left( \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right. \right. \\
& \left. \left. \left( a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \left( 1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) \right) / \\
& \left( 64a^2 \sqrt{\frac{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \right) - \\
& \left( b(a+b)(3Ab^2-4a^2(13A+20C)) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] + \right. \\
& 2 \left( a(-Ab^3+8a^3(3A+4C)-4a^2b(3A+4C)+2ab^2(19A+32C)) \operatorname{EllipticF}\left[ \right. \right. \\
& \left. \left. \operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] + (3Ab^4+24a^2b^2(A+2C)+16a^4(3A+4C)) \right. \\
& \left. \left. \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \right) \right) \\
& \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^4}
\end{aligned}$$

$$\begin{aligned}
 & \left( \left( -a \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] + b \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right) / \right. \\
 & \quad \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) - \left( \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right. \\
 & \quad \left. \left. \left( a + b - a \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right)^2 \right) / \\
 & \left( 64 a^2 \sqrt{\frac{1}{1 - \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}} \sqrt{\frac{a + b - a \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}} \right. \\
 & \quad \left. \left( b - b \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^4 + a \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right)^2 \right) \right) - \\
 & \left( \sqrt{\frac{a + b - a \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a + b}} \right. \\
 & \quad \left. \sqrt{\frac{a + b - a \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}} \sqrt{1 - \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^4} \right. \\
 & \quad \left( \left( b (a + b) (3 A b^2 - 4 a^2 (13 A + 20 C)) \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \right. \right. \\
 & \quad \left. \left. \sqrt{1 - \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a + b}} \right) / \left( 2 \sqrt{1 - \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \right) + 2 \left( a (-A b^3 + \right. \right. \\
 & \quad \left. \left. 8 a^3 (3 A + 4 C) - 4 a^2 b (3 A + 4 C) + 2 a b^2 (19 A + 32 C)) \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \right) / \right. \\
 & \quad \left. \left( 2 \sqrt{1 - \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \sqrt{1 - \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a + b}} \right) - \left( (3 A b^4 + 24 a^2 b^2 \right. \right. \\
 & \quad \left. \left. (A + 2 C) + 16 a^4 (3 A + 4 C)) \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \right) / \left( 2 \sqrt{1 - \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \right)^2 \right)
 \end{aligned}$$

$$\left( \left( \left( \left( \left( \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]\right)^2 \right) \sqrt{1 - \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \right) \right) \right) \right) \right) \left( \left( \left( \left( \left( \left( 32 a^2 \sqrt{\frac{1}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}} \left( b - b \tan\left[\frac{1}{2}(c+dx)\right]^4 + a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) /$$

**Problem 725: Attempted integration timed out after 120 seconds.**

$$\int \text{Sec}[c+dx]^3 (a+b \text{Sec}[c+dx])^{5/2} (A+C \text{Sec}[c+dx]^2) dx$$

Optimal (type 4, 650 leaves, 9 steps):

$$\begin{aligned} &\frac{1}{45045 b^5 d} 2 (a-b) \sqrt{a+b} \\ &\quad (240 a^6 C - 1617 b^6 (13 A + 11 C) + 10 a^4 b^2 (143 A + 76 C) - 3 a^2 b^4 (13 299 A + 10 223 C)) \text{Cot}[c+dx] \\ &\text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \text{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\text{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\text{Sec}[c+dx])}{a-b}} + \\ &\frac{1}{45045 b^4 d} 2 (a-b) \sqrt{a+b} (240 a^5 C + 180 a^4 b C + 1617 b^5 (13 A + 11 C) + \\ &\quad 10 a^3 b^2 (143 A + 94 C) + 15 a^2 b^3 (1573 A + 1175 C) - 6 a b^4 (2717 A + 2174 C)) \\ &\text{Cot}[c+dx] \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \text{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ &\sqrt{\frac{b(1-\text{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\text{Sec}[c+dx])}{a-b}} + \frac{1}{45045 b^3 d} \\ &2 a (120 a^4 C + 5 a^2 b^2 (143 A + 79 C) + b^4 (23 309 A + 18 973 C)) \sqrt{a+b \text{Sec}[c+dx]} \text{Tan}[c+dx] - \\ &\frac{1}{45045 b^2 d} 2 (90 a^4 C - 539 b^4 (13 A + 11 C) - 15 a^2 b^2 (715 A + 543 C)) \\ &\quad \text{Sec}[c+dx] \sqrt{a+b \text{Sec}[c+dx]} \text{Tan}[c+dx] + \frac{1}{9009 b d} \\ &2 a (2717 A b^2 + 15 a^2 C + 2209 b^2 C) \text{Sec}[c+dx]^2 \sqrt{a+b \text{Sec}[c+dx]} \text{Tan}[c+dx] + \\ &\frac{1}{1287 d} 2 (15 a^2 C + 11 b^2 (13 A + 11 C)) \text{Sec}[c+dx]^3 \sqrt{a+b \text{Sec}[c+dx]} \text{Tan}[c+dx] + \\ &\frac{10 a C \text{Sec}[c+dx]^3 (a+b \text{Sec}[c+dx])^{3/2} \text{Tan}[c+dx]}{143 d} + \\ &\frac{2 C \text{Sec}[c+dx]^3 (a+b \text{Sec}[c+dx])^{5/2} \text{Tan}[c+dx]}{13 d} \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 726: Attempted integration timed out after 120 seconds.**

$$\int \sec [c + d x]^2 (a + b \sec [c + d x])^{5/2} (A + C \sec [c + d x]^2) dx$$

Optimal (type 4, 534 leaves, 8 steps):

$$\begin{aligned}
 & -\frac{1}{693 b^4 d} 2 a (a-b) \sqrt{a+b} (8 a^4 C + 3 a^2 b^2 (33 A + 17 C) + 3 b^4 (319 A + 247 C)) \\
 & \quad \cot [c + d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c + d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \quad \sqrt{\frac{b(1-\sec [c + d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c + d x])}{a-b}} - \frac{1}{693 b^3 d} \\
 & 2(a-b) \sqrt{a+b} (8 a^4 C + 6 a^3 b C + 15 b^4 (11 A + 9 C) + 3 a^2 b^2 (33 A + 19 C) - 6 a b^3 (132 A + 101 C)) \\
 & \quad \cot [c + d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c + d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \quad \sqrt{\frac{b(1-\sec [c + d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c + d x])}{a-b}} + \frac{1}{693 b^2 d} \\
 & \frac{2(8 a^4 C + 15 b^4 (11 A + 9 C) + 3 a^2 b^2 (33 A + 19 C)) \sqrt{a+b \sec [c + d x]} \tan [c + d x] +}{693 b^2 d} \\
 & \frac{2 a (99 A b^2 + 8 a^2 C + 67 b^2 C) (a+b \sec [c + d x])^{3/2} \tan [c + d x]}{693 b^2 d} + \\
 & \frac{2(8 a^2 C + 9 b^2 (11 A + 9 C)) (a+b \sec [c + d x])^{5/2} \tan [c + d x]}{693 b^2 d} - \\
 & \frac{8 a C (a+b \sec [c + d x])^{7/2} \tan [c + d x]}{99 b^2 d} + \frac{2 C \sec [c + d x] (a+b \sec [c + d x])^{7/2} \tan [c + d x]}{11 b d}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 727: Attempted integration timed out after 120 seconds.**

$$\int \sec [c + d x] (a + b \sec [c + d x])^{5/2} (A + C \sec [c + d x]^2) dx$$

Optimal (type 4, 454 leaves, 7 steps):

$$\frac{1}{315 b^3 d} 2 (a-b) \sqrt{a+b} (10 a^4 C - 21 b^4 (9 A + 7 C) - 3 a^2 b^2 (161 A + 93 C)) \operatorname{Cot}[c+d x]$$

$$\operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} +$$

$$\frac{1}{315 b^2 d} 2 (a-b) \sqrt{a+b} (10 a^3 C + 21 b^3 (9 A + 7 C) + 15 a^2 b (21 A + 11 C) - 6 a b^2 (28 A + 19 C))$$

$$\operatorname{Cot}[c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}}$$

$$\sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \frac{4 a (84 A b^2 - 5 a^2 C + 57 b^2 C) \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x]}{315 b d} -$$

$$\frac{2 (10 a^2 C - 7 b^2 (9 A + 7 C)) (a+b \operatorname{Sec}[c+d x])^{3/2} \operatorname{Tan}[c+d x]}{315 b d} -$$

$$\frac{4 a C (a+b \operatorname{Sec}[c+d x])^{5/2} \operatorname{Tan}[c+d x]}{63 b d} + \frac{2 C (a+b \operatorname{Sec}[c+d x])^{7/2} \operatorname{Tan}[c+d x]}{9 b d}$$

Result (type 1, 1 leaves):

???

### Problem 729: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cos}[c+d x] (a+b \operatorname{Sec}[c+d x])^{5/2} (A+C \operatorname{Sec}[c+d x]^2) dx$$

Optimal (type 4, 478 leaves, 8 steps):

$$\frac{1}{15 b d} (a-b) \sqrt{a+b} (a^2 (15 A - 46 C) - 6 b^2 (5 A + 3 C)) \operatorname{Cot}[c+d x]$$

$$\operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} +$$

$$\frac{1}{15 b d} \sqrt{a+b} (a^2 b (15 A - 46 C) + 30 a^3 C - 6 b^3 (5 A + 3 C) + 2 a b^2 (45 A + 17 C)) \operatorname{Cot}[c+d x]$$

$$\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} -$$

$$\frac{1}{d} 5 a A b \sqrt{a+b} \operatorname{Cot}[c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \frac{A (a+b \operatorname{Sec}[c+d x])^{5/2} \operatorname{Sin}[c+d x]}{d} -$$

$$\frac{a b (15 A - 16 C) \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x]}{15 d} - \frac{b (5 A - 2 C) (a+b \operatorname{Sec}[c+d x])^{3/2} \operatorname{Tan}[c+d x]}{5 d}$$



Result (type 4, 1129 leaves):

$$\left( 2 (a + b \operatorname{Sec}[c + d x])^{5/2} (A + C \operatorname{Sec}[c + d x]^2) \right.$$

$$\sqrt{\frac{1}{1 - \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}} \left( 15 a^3 A \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] + 15 a^2 A b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] - \right.$$

$$30 a A b^2 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] - 30 A b^3 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] - 46 a^3 C \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] -$$

$$46 a^2 b C \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] - 18 a b^2 C \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] - 18 b^3 C \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] -$$

$$30 a^3 A \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^3 + 60 a A b^2 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^3 + 92 a^3 C \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^3 +$$

$$36 a b^2 C \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^3 + 15 a^3 A \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^5 - 15 a^2 A b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^5 -$$

$$30 a A b^2 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^5 + 30 A b^3 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^5 - 46 a^3 C \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^5 +$$

$$46 a^2 b C \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^5 - 18 a b^2 C \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^5 + 18 b^3 C \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^5 -$$

$$150 a^2 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right], \frac{a - b}{a + b}\right]$$

$$\sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2} \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{a + b}} -$$

$$150 a^2 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right], \frac{a - b}{a + b}\right] \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2$$

$$\sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2} \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{a + b}} +$$

$$(a + b) (a^2 (15 A - 46 C) - 6 b^2 (5 A + 3 C)) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right], \frac{a - b}{a + b}\right]$$

$$\sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2} \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right)^2$$

$$\sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{a + b}} +$$

$$2 (15 a^3 C + 3 b^3 (5 A + 3 C) + a b^2 (45 A + 17 C) + a^2 (-45 A b + 23 b C))$$

$$\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right], \frac{a - b}{a + b}\right] \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}$$

$$\left( \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \right) /$$

$$\left( 15 d (b + a \cos[c+dx])^{5/2} (A + 2C + A \cos[2c + 2dx]) \sec[c+dx]^{9/2} \right.$$

$$\left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^{3/2}$$

$$\sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}} \right) +$$

$$\left( \cos[c+dx]^4 (a + b \sec[c+dx])^{5/2} (A + C \sec[c+dx]^2) \right.$$

$$\left( \frac{4}{15} (15Ab^2 + 23a^2C + 9b^2C) \sin[c+dx] + \right.$$

$$\left. \frac{44}{15} abC \tan[c+dx] + \frac{4}{5} b^2C \sec[c+dx] \tan[c+dx] \right) /$$

$$\left( d (b + a \cos[c+dx])^2 (A + 2C + A \cos[2c + 2dx]) \right)$$

**Problem 731: Result more than twice size of optimal antiderivative.**

$$\int \cos[c+dx]^3 (a + b \sec[c+dx])^{5/2} (A + C \sec[c+dx]^2) dx$$

Optimal (type 4, 507 leaves, 8 steps):

$$\begin{aligned}
 & \frac{1}{24 b d} (a-b) \sqrt{a+b} \left( 3 b^2 (11 A-16 C)+8 a^2 (2 A+3 C) \right) \operatorname{Cot}[c+d x] \\
 & \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \\
 & \frac{1}{24 d} \sqrt{a+b} \left( 16 a^2 A+26 a A b+33 A b^2+24 a^2 C+144 a b C-48 b^2 C \right) \operatorname{Cot}[c+d x] \\
 & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \\
 & \frac{1}{8 a d} 5 b \sqrt{a+b} \left( A b^2+4 a^2 (A+2 C) \right) \operatorname{Cot}[c+d x] \\
 & \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \\
 & \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \frac{(15 A b^2+8 a^2 (2 A+3 C)) \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{24 d} + \\
 & \frac{5 A b \operatorname{Cos}[c+d x] (a+b \operatorname{Sec}[c+d x])^{3/2} \operatorname{Sin}[c+d x]}{12 d} + \\
 & \frac{A \operatorname{Cos}[c+d x]^2 (a+b \operatorname{Sec}[c+d x])^{5/2} \operatorname{Sin}[c+d x]}{3 d}
 \end{aligned}$$

Result (type 4, 1513 leaves):

$$\begin{aligned}
 & \left( \operatorname{Cos}[c+d x]^4 (a+b \operatorname{Sec}[c+d x])^{5/2} (A+C \operatorname{Sec}[c+d x]^2) \right. \\
 & \left. \left( \frac{1}{6} (a^2 A+24 b^2 C) \operatorname{Sin}[c+d x] + \frac{13}{12} a A b \operatorname{Sin}[2(c+d x)] + \frac{1}{6} a^2 A \operatorname{Sin}[3(c+d x)] \right) \right) / \\
 & \left( d (b+a \operatorname{Cos}[c+d x])^2 (A+2 C+A \operatorname{Cos}[2 c+2 d x]) \right) + \\
 & \left( (a+b \operatorname{Sec}[c+d x])^{5/2} (A+C \operatorname{Sec}[c+d x]^2) \sqrt{\frac{1}{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}} \right. \\
 & \left. \left( 16 a^3 A \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + 16 a^2 A b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + \right. \right. \\
 & \left. \left. 33 a A b^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + 33 A b^3 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + 24 a^3 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + \right. \right. \\
 & \left. \left. 24 a^2 b C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] - 48 a b^2 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] - 48 b^3 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] - \right. \right. \\
 & \left. \left. 32 a^3 A \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 - 66 a A b^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 - 48 a^3 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 + \right. \right. \\
 & \left. \left. 96 a b^2 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 + 16 a^3 A \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - 16 a^2 A b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 33 a A b^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - 33 A b^3 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + 24 a^3 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - \\
 & 24 a^2 b C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - 48 a b^2 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + 48 b^3 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - \\
 & 120 a^2 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
 & 30 A b^3 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
 & 240 a^2 b C \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
 & 120 a^2 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
 & 30 A b^3 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
 & 240 a^2 b C \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \\
 & (a+b)\left(3 b^2(11 A-16 C)+8 a^2(2 A+3 C)\right) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right) \\
 & \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
 & 2 b\left(24 b^2(A-C)-a b(13 A+72 C)+a^2(38 A+72 C)\right)
 \end{aligned}$$

$$\text{EllipticF}\left[\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}$$

$$\left(1+\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b-a\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \Bigg) \Bigg/$$

$$\left(12d(b+a\text{Cos}[c+dx])^{5/2}(A+2C+A\text{Cos}[2c+2dx])\text{Sec}[c+dx]^{9/2}\right.$$

$$\left.\left(1+\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^{3/2} \sqrt{\frac{a+b-a\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1+\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}}\right)$$

**Problem 734: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \sqrt{a+b\text{Sec}[c+dx]} (a^2-b^2\text{Sec}[c+dx]^2) dx$$

Optimal (type 4, 353 leaves, 7 steps):

$$\frac{1}{3d} 2a(a-b)\sqrt{a+b}\text{Cot}[c+dx]\text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a+b\text{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\text{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\text{Sec}[c+dx])}{a-b}} + \frac{1}{3d} 2\sqrt{a+b}(3a^2+ab-b^2)\text{Cot}[c+dx]$$

$$\text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a+b\text{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\text{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\text{Sec}[c+dx])}{a-b}} -$$

$$\frac{1}{d} 2a^2\sqrt{a+b}\text{Cot}[c+dx]\text{EllipticPi}\left[\frac{a+b}{a}, \text{ArcSin}\left[\frac{\sqrt{a+b\text{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\text{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\text{Sec}[c+dx])}{a-b}} - \frac{2b^2\sqrt{a+b\text{Sec}[c+dx]}\text{Tan}[c+dx]}{3d}$$

Result (type 4, 799 leaves):

$$-\left(\left(4\sqrt{a+b\text{Sec}[c+dx]}(a^2-b^2\text{Sec}[c+dx]^2)\sqrt{\frac{a+b-a\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1+\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}}\right.\right.$$

$$\begin{aligned}
 & \left( i a (a-b) b \operatorname{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right], \frac{a+b}{a-b} \right] \right. \\
 & \quad \sqrt{1 - \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \\
 & \quad \sqrt{\frac{a+b - a \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} - i (3a^3 - 3a^2b - ab^2 + b^3) \\
 & \quad \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right], \frac{a+b}{a-b} \right] \sqrt{1 - \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \\
 & \quad \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \sqrt{\frac{a+b - a \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} + \\
 & \quad 6 i a^3 \operatorname{EllipticPi} \left[ -\frac{a+b}{a-b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right], \frac{a+b}{a-b} \right] \\
 & \quad \sqrt{1 - \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \\
 & \quad \sqrt{\frac{a+b - a \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} - \\
 & \quad \left. \left. \left. a b \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \left( b - b \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^4 + a \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right)^2 \right) \right) \right) \right) / \right. \\
 & \left( 3 \sqrt{\frac{-a+b}{a+b}} d \sqrt{b+a \operatorname{Cos} [c+dx]} (a^2 - 2b^2 + a^2 \operatorname{Cos} [2c+2dx]) \operatorname{Sec} [c+dx]^{5/2} \right. \\
 & \quad \left. \sqrt{\frac{1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{1 - \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}} \left( b - b \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^4 + a \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right)^2 \right) \right) + \\
 & \quad \left( \operatorname{Cos} [c+dx]^2 \sqrt{a+b \operatorname{Sec} [c+dx]} (a^2 - b^2 \operatorname{Sec} [c+dx]^2) \right. \\
 & \quad \left. \left( -\frac{4}{3} a b \operatorname{Sin} [c+dx] - \frac{4}{3} b^2 \operatorname{Tan} [c+dx] \right) \right) / \\
 & \quad \left( d (a^2 - 2b^2 + a^2 \operatorname{Cos} [2c+2dx]) \right)
 \end{aligned}$$

Problem 735: Unable to integrate problem.

$$\int \frac{\text{Sec}[c + dx]^3 (A + C \text{Sec}[c + dx]^2)}{\sqrt{a + b \text{Sec}[c + dx]}} dx$$

Optimal (type 4, 393 leaves, 6 steps):

$$\begin{aligned} & \frac{1}{105 b^5 d} 4 a (a - b) \sqrt{a + b} (35 A b^2 + 24 a^2 C + 22 b^2 C) \text{Cot}[c + dx] \\ & \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + dx]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \sqrt{\frac{b (1 - \text{Sec}[c + dx])}{a + b}} \sqrt{-\frac{b (1 + \text{Sec}[c + dx])}{a - b}} + \\ & \frac{1}{105 b^4 d} 2 \sqrt{a + b} (48 a^3 C - 12 a^2 b C + 5 b^3 (7 A + 5 C) + 2 a b^2 (35 A + 22 C)) \text{Cot}[c + dx] \\ & \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + dx]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \sqrt{\frac{b (1 - \text{Sec}[c + dx])}{a + b}} \sqrt{-\frac{b (1 + \text{Sec}[c + dx])}{a - b}} + \\ & \frac{2 (24 a^2 C + 5 b^2 (7 A + 5 C)) \sqrt{a + b \text{Sec}[c + dx]} \text{Tan}[c + dx]}{105 b^3 d} - \\ & \frac{12 a C \text{Sec}[c + dx] \sqrt{a + b \text{Sec}[c + dx]} \text{Tan}[c + dx]}{35 b^2 d} + \\ & \frac{2 C \text{Sec}[c + dx]^2 \sqrt{a + b \text{Sec}[c + dx]} \text{Tan}[c + dx]}{7 b d} \end{aligned}$$

Result (type 8, 37 leaves):

$$\int \frac{\text{Sec}[c + dx]^3 (A + C \text{Sec}[c + dx]^2)}{\sqrt{a + b \text{Sec}[c + dx]}} dx$$

**Problem 736: Unable to integrate problem.**

$$\int \frac{\text{Sec}[c + dx]^2 (A + C \text{Sec}[c + dx]^2)}{\sqrt{a + b \text{Sec}[c + dx]}} dx$$

Optimal (type 4, 320 leaves, 5 steps):

$$\begin{aligned} & -\frac{1}{15 b^4 d} 2 (a - b) \sqrt{a + b} (8 a^2 C + 3 b^2 (5 A + 3 C)) \text{Cot}[c + dx] \text{EllipticE}\left[ \right. \\ & \quad \left. \text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + dx]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \sqrt{\frac{b (1 - \text{Sec}[c + dx])}{a + b}} \sqrt{-\frac{b (1 + \text{Sec}[c + dx])}{a - b}} - \\ & \frac{1}{15 b^3 d} 2 \sqrt{a + b} (8 a^2 C - 2 a b C + 3 b^2 (5 A + 3 C)) \text{Cot}[c + dx] \\ & \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + dx]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \sqrt{\frac{b (1 - \text{Sec}[c + dx])}{a + b}} \sqrt{-\frac{b (1 + \text{Sec}[c + dx])}{a - b}} - \\ & \frac{8 a C \sqrt{a + b \text{Sec}[c + dx]} \text{Tan}[c + dx]}{15 b^2 d} + \frac{2 C \text{Sec}[c + dx] \sqrt{a + b \text{Sec}[c + dx]} \text{Tan}[c + dx]}{5 b d} \end{aligned}$$

Result (type 8, 37 leaves):

$$\int \frac{\text{Sec}[c + d x]^2 (A + C \text{Sec}[c + d x]^2)}{\sqrt{a + b \text{Sec}[c + d x]}} dx$$

Problem 737: Unable to integrate problem.

$$\int \frac{\text{Sec}[c + d x] (A + C \text{Sec}[c + d x]^2)}{\sqrt{a + b \text{Sec}[c + d x]}} dx$$

Optimal (type 4, 253 leaves, 4 steps):

$$\frac{1}{3 b^3 d} 4 a (a - b) \sqrt{a + b} C \cot[c + d x] \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right]$$

$$\sqrt{\frac{b(1 - \text{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \text{Sec}[c + d x])}{a - b}} + \frac{1}{3 b^2 d}$$

$$2 \sqrt{a + b} (3 A b + (2 a + b) C) \cot[c + d x] \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right]$$

$$\sqrt{\frac{b(1 - \text{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \text{Sec}[c + d x])}{a - b}} + \frac{2 C \sqrt{a + b \text{Sec}[c + d x]} \tan[c + d x]}{3 b d}$$

Result (type 8, 35 leaves):

$$\int \frac{\text{Sec}[c + d x] (A + C \text{Sec}[c + d x]^2)}{\sqrt{a + b \text{Sec}[c + d x]}} dx$$

Problem 738: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{A + C \text{Sec}[c + d x]^2}{\sqrt{a + b \text{Sec}[c + d x]}} dx$$

Optimal (type 4, 313 leaves, 5 steps):



$$\begin{aligned}
 & -\frac{1}{b^2 d} 2 (a-b) \sqrt{a+b} C \cot [c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} - \frac{1}{b d} \\
 & 2 \sqrt{a+b} C \cot [c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} - \frac{1}{a d} \\
 & 2 A \sqrt{a+b} \cot [c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}}
 \end{aligned}$$

Result (type 4, 914 leaves):

$$\begin{aligned}
 & \frac{4 C \cos [c+d x] (b+a \cos [c+d x]) (A+C \sec [c+d x]^2) \sin [c+d x]}{b d (A+2 C+A \cos [2 c+2 d x]) \sqrt{a+b \sec [c+d x]}} + \\
 & \left( 4 \sqrt{b+a \cos [c+d x]} (A+C \sec [c+d x]^2) \sqrt{\frac{1}{1-\tan \left[\frac{1}{2}(c+d x)\right]^2}} \right. \\
 & \left. \sqrt{1-\tan \left[\frac{1}{2}(c+d x)\right]^2} \left( -a \sqrt{\frac{-a+b}{a+b}} C \tan \left[\frac{1}{2}(c+d x)\right] \sqrt{1-\tan \left[\frac{1}{2}(c+d x)\right]^2} - \right. \right. \\
 & \left. \left. b \sqrt{\frac{-a+b}{a+b}} C \tan \left[\frac{1}{2}(c+d x)\right] \sqrt{1-\tan \left[\frac{1}{2}(c+d x)\right]^2} + a \sqrt{\frac{-a+b}{a+b}} C \tan \left[\frac{1}{2}(c+d x)\right]^3 \right. \right. \\
 & \left. \left. \sqrt{1-\tan \left[\frac{1}{2}(c+d x)\right]^2} - b \sqrt{\frac{-a+b}{a+b}} C \tan \left[\frac{1}{2}(c+d x)\right]^3 \sqrt{1-\tan \left[\frac{1}{2}(c+d x)\right]^2} - \right. \right. \\
 & \left. \left. 2 i A b \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan \left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right] \right. \right. \\
 & \left. \left. \sqrt{\frac{a+b-a \tan \left[\frac{1}{2}(c+d x)\right]^2+b \tan \left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \right. \right. \\
 & \left. \left. 2 i A b \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan \left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right] \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \tan\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{\frac{a+b-a\tan\left[\frac{1}{2}(c+dx)\right]^2+b\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & i(a-b) \operatorname{CEllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b-a\tan\left[\frac{1}{2}(c+dx)\right]^2+b\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & i b(A+C) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b-a\tan\left[\frac{1}{2}(c+dx)\right]^2+b\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \Bigg) \Bigg) / \\
 & \left( b \sqrt{\frac{-a+b}{a+b}} d(A+2C+A \cos[2c+2dx]) \operatorname{Sec}[c+dx]^{3/2} \sqrt{a+b} \operatorname{Sec}[c+dx] \right. \\
 & \left. \left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^{3/2} \sqrt{\frac{a+b-a\tan\left[\frac{1}{2}(c+dx)\right]^2+b\tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}} \right) \right)
 \end{aligned}$$

**Problem 740: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c+dx]^2 (A+C \operatorname{Sec}[c+dx]^2)}{\sqrt{a+b \operatorname{Sec}[c+dx]}} dx$$

Optimal (type 4, 411 leaves, 7 steps):

$$\begin{aligned}
 & -\frac{1}{4a^2d} 3A(a-b)\sqrt{a+b}\cot[c+dx]\operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b\sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1-\sec[c+dx])}{a+b}}\sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} + \frac{1}{4a^2d} \\
 & A(2a-3b)\sqrt{a+b}\cot[c+dx]\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b\sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1-\sec[c+dx])}{a+b}}\sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} - \frac{1}{4a^3d} \\
 & \sqrt{a+b}(3Ab^2+4a^2(A+2C))\cot[c+dx]\operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b\sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1-\sec[c+dx])}{a+b}}\sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} - \\
 & \frac{3Ab\sqrt{a+b\sec[c+dx]}\sin[c+dx]}{4a^2d} + \frac{A\cos[c+dx]\sqrt{a+b\sec[c+dx]}\sin[c+dx]}{2ad}
 \end{aligned}$$

Result (type 4, 1475 leaves):

$$\begin{aligned}
 & \frac{A(b+a\cos[c+dx])\sec[c+dx]\sin[2(c+dx)]}{4ad\sqrt{a+b\sec[c+dx]}} - \\
 & \left( \sqrt{b+a\cos[c+dx]}\sqrt{\sec[c+dx]}\sqrt{\frac{a+b-a\tan\left[\frac{1}{2}(c+dx)\right]^2+b\tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}} \right. \\
 & \left. \left( 3aAb\sqrt{\frac{-a+b}{a+b}}\tan\left[\frac{1}{2}(c+dx)\right] + 3Ab^2\sqrt{\frac{-a+b}{a+b}}\tan\left[\frac{1}{2}(c+dx)\right] - 6aAb\sqrt{\frac{-a+b}{a+b}} \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^3 + 3aAb\sqrt{\frac{-a+b}{a+b}}\tan\left[\frac{1}{2}(c+dx)\right]^5 - 3Ab^2\sqrt{\frac{-a+b}{a+b}}\tan\left[\frac{1}{2}(c+dx)\right]^5 + \right. \right. \\
 & \left. \left. 8i^2a^2A\operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i\operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}}\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \right. \right. \\
 & \left. \left. \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}\sqrt{\frac{a+b-a\tan\left[\frac{1}{2}(c+dx)\right]^2+b\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \right. \right. \\
 & \left. \left. 6iAb^2\operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i\operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}}\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \right)
 \end{aligned}$$

$$\begin{aligned}
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& 16 i a^2 C \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& 8 i a^2 A \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& 6 i A b^2 \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + 16 i a^2 C \\
& \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 3 i A (a-b) b \text{EllipticE}\left[i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \\
& \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - 2 i (-a A b + 3 A b^2 + 2 a^2 (A + 2 C)) \\
& \text{EllipticF}\left[i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}
\end{aligned}$$

$$\left( \left( 1 + \tan \left[ \frac{1}{2} (c + dx) \right] \right)^2 \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + dx) \right]^2 + b \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b}} \right) \Bigg/$$

$$\left( 4 a^2 \sqrt{\frac{-a + b}{a + b}} d \sqrt{a + b \sec [c + dx]} \left( -1 + \tan \left[ \frac{1}{2} (c + dx) \right] \right)^2 \sqrt{\frac{1 + \tan \left[ \frac{1}{2} (c + dx) \right]^2}{1 - \tan \left[ \frac{1}{2} (c + dx) \right]^2}} \right.$$

$$\left. \left( a \left( -1 + \tan \left[ \frac{1}{2} (c + dx) \right] \right)^2 - b \left( 1 + \tan \left[ \frac{1}{2} (c + dx) \right] \right)^2 \right) \right)$$

**Problem 741: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos [c + dx]^3 (A + C \sec [c + dx]^2)}{\sqrt{a + b \sec [c + dx]}} dx$$

Optimal (type 4, 506 leaves, 8 steps):

$$\frac{1}{24 a^3 b d} (a - b) \sqrt{a + b} (15 A b^2 + 8 a^2 (2 A + 3 C)) \cot [c + dx]$$

$$\text{EllipticE} \left[ \text{ArcSin} \left[ \frac{\sqrt{a + b \sec [c + dx]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \sqrt{\frac{b (1 - \sec [c + dx])}{a + b}} \sqrt{-\frac{b (1 + \sec [c + dx])}{a - b}} -$$

$$\frac{1}{24 a^3 d} \sqrt{a + b} (10 a A b - 15 A b^2 - 8 a^2 (2 A + 3 C)) \cot [c + dx]$$

$$\text{EllipticF} \left[ \text{ArcSin} \left[ \frac{\sqrt{a + b \sec [c + dx]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \sqrt{\frac{b (1 - \sec [c + dx])}{a + b}} \sqrt{-\frac{b (1 + \sec [c + dx])}{a - b}} +$$

$$\frac{1}{8 a^4 d} b \sqrt{a + b} (5 A b^2 + 4 a^2 (A + 2 C)) \cot [c + dx]$$

$$\text{EllipticPi} \left[ \frac{a + b}{a}, \text{ArcSin} \left[ \frac{\sqrt{a + b \sec [c + dx]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \sqrt{\frac{b (1 - \sec [c + dx])}{a + b}}$$

$$\sqrt{-\frac{b (1 + \sec [c + dx])}{a - b}} + \frac{(15 A b^2 + 8 a^2 (2 A + 3 C)) \sqrt{a + b \sec [c + dx]} \sin [c + dx]}{24 a^3 d} -$$

$$\frac{5 A b \cos [c + dx] \sqrt{a + b \sec [c + dx]} \sin [c + dx]}{12 a^2 d} + \frac{A \cos [c + dx]^2 \sqrt{a + b \sec [c + dx]} \sin [c + dx]}{3 a d}$$

Result (type 4, 1363 leaves):

$$\left( (b + a \cos [c + dx]) \sec [c + dx] \left( \frac{A \sin [c + dx]}{12 a} - \frac{5 A b \sin [2 (c + dx)]}{24 a^2} + \frac{A \sin [3 (c + dx)]}{12 a} \right) \right) \Bigg/$$

$$\begin{aligned}
 & \left( d \sqrt{a + b \operatorname{Sec}[c + d x]} \right) - \left( \sqrt{b + a \operatorname{Cos}[c + d x]} \sqrt{\operatorname{Sec}[c + d x]} \right. \\
 & \sqrt{\frac{1}{1 - \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}} \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}} \\
 & \left( 16 a^3 A \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] + 16 a^2 A b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] + 15 a A b^2 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] + \right. \\
 & 15 A b^3 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] + 24 a^3 C \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] + 24 a^2 b C \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] - \\
 & 32 a^3 A \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^3 - 30 a A b^2 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^3 - 48 a^3 C \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^3 + \\
 & 16 a^3 A \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^5 - 16 a^2 A b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^5 + 15 a A b^2 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^5 - \\
 & 15 A b^3 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^5 + 24 a^3 C \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^5 - 24 a^2 b C \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^5 + \\
 & \left. 24 a^2 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right], \frac{a - b}{a + b}\right] \right. \\
 & \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2} \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{a + b}} + \\
 & \left. 30 A b^3 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right], \frac{a - b}{a + b}\right] \right. \\
 & \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2} \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{a + b}} + \\
 & \left. 48 a^2 b C \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right], \frac{a - b}{a + b}\right] \right. \\
 & \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2} \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{a + b}} + \\
 & \left. 24 a^2 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right], \frac{a - b}{a + b}\right] \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 \right. \\
 & \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2} \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{a + b}} + \\
 & \left. 30 A b^3 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right], \frac{a - b}{a + b}\right] \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 \right)
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & 48 a^2 b C \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & (a+b) (15 A b^2 + 8 a^2 (2 A + 3 C)) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \\
 & \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 2 a A b (2 a + 5 b) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left. \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \right) / \\
 & \left( 24 a^3 d \sqrt{a+b \operatorname{Sec}[c+dx]} \sqrt{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} \right. \\
 & \left. \left( a \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) - b \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \right)
 \end{aligned}$$

**Problem 742: Attempted integration timed out after 120 seconds.**

$$\int \frac{\operatorname{Sec}[c+dx]^3 (A + C \operatorname{Sec}[c+dx]^2)}{(a+b \operatorname{Sec}[c+dx])^{3/2}} dx$$

Optimal (type 4, 460 leaves, 6 steps):

$$\begin{aligned}
 & - \frac{1}{5 b^5 \sqrt{a+b} d} 2 (2 a^2 b^2 (5 A-4 C)+16 a^4 C-b^4 (5 A+3 C)) \operatorname{Cot}[c+d x] \operatorname{EllipticE}\left[\right. \\
 & \quad \left. \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \\
 & \frac{1}{5 b^4 \sqrt{a+b} d} 2 (16 a^3 C+12 a^2 b C+2 a b^2 (5 A+2 C)+b^3 (5 A+3 C)) \operatorname{Cot}[c+d x] \\
 & \quad \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \\
 & \frac{2(A b^2+a^2 C) \operatorname{Sec}[c+d x]^2 \operatorname{Tan}[c+d x]}{b\left(a^2-b^2\right) d \sqrt{a+b \operatorname{Sec}[c+d x]}} - \\
 & \frac{2 a\left(5 A b^2+8 a^2 C-3 b^2 C\right) \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x]}{5 b^3\left(a^2-b^2\right) d} + \\
 & \frac{2\left(5 A b^2+6 a^2 C-b^2 C\right) \operatorname{Sec}[c+d x] \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x]}{5 b^2\left(a^2-b^2\right) d}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

### Problem 743: Attempted integration timed out after 120 seconds.

$$\int \frac{\operatorname{Sec}[c+d x]^2(A+C \operatorname{Sec}[c+d x]^2)}{(a+b \operatorname{Sec}[c+d x])^{3 / 2}} d x$$

Optimal (type 4, 327 leaves, 5 steps):

$$\begin{aligned}
 & \frac{1}{3 b^4 \sqrt{a+b} d} 2 a\left(3 A b^2+8 a^2 C-5 b^2 C\right) \operatorname{Cot}[c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \quad \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \frac{1}{3 b^3 \sqrt{a+b} d} \\
 & 2\left(3 A b^2+\left(8 a^2+6 a b+b^2\right) C\right) \operatorname{Cot}[c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \quad \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \\
 & \frac{2 a\left(A b^2+a^2 C\right) \operatorname{Tan}[c+d x]}{b^2\left(a^2-b^2\right) d \sqrt{a+b \operatorname{Sec}[c+d x]}} + \frac{2 C \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x]}{3 b^2 d}
 \end{aligned}$$

Result (type 1, 1 leaves):

???



**Problem 744: Attempted integration timed out after 120 seconds.**

$$\int \frac{\sec [c+d x] \left(A+C \sec [c+d x]^2\right)}{\left(a+b \sec [c+d x]\right)^{3 / 2}} d x$$

Optimal (type 4, 279 leaves, 4 steps):

$$-\frac{1}{b^3 \sqrt{a+b} d} 2 \left(A b^2+2 a^2 C-b^2 C\right) \cot [c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}}+\frac{1}{b^2 \sqrt{a+b} d}$$

$$2\left(A b-(2 a+b) C\right) \cot [c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}}-\frac{2\left(A b^2+a^2 C\right) \tan [c+d x]}{b\left(a^2-b^2\right) d \sqrt{a+b \sec [c+d x]}}$$

Result (type 1, 1 leaves):

???

**Problem 745: Result more than twice size of optimal antiderivative.**

$$\int \frac{A+C \sec [c+d x]^2}{\left(a+b \sec [c+d x]\right)^{3 / 2}} d x$$

Optimal (type 4, 381 leaves, 6 steps):

$$\frac{1}{a b^2 \sqrt{a+b} d} 2\left(A b^2+a^2 C\right) \cot [c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}}-\frac{1}{a b \sqrt{a+b} d} 2\left(A b-a C\right) \cot [c+d x]$$

$$\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}}$$

$$\frac{1}{a^2 d} 2 A \sqrt{a+b} \cot [c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}}+\frac{2\left(A b^2+a^2 C\right) \tan [c+d x]}{a\left(a^2-b^2\right) d \sqrt{a+b \sec [c+d x]}}$$

Result (type 4, 1127 leaves):

$$\begin{aligned}
& \left( (b + a \cos [c + d x])^2 (A + C \sec [c + d x])^2 \right. \\
& \quad \left. \left( \frac{4 (A b^2 + a^2 C) \sin [c + d x]}{a b (-a^2 + b^2)} + \frac{4 (A b^2 \sin [c + d x] + a^2 C \sin [c + d x])}{a (a^2 - b^2) (b + a \cos [c + d x])} \right) \right) / \\
& \quad (d (A + 2 C + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^{3/2}) - \\
& \quad \left( 4 (b + a \cos [c + d x])^{3/2} (A + C \sec [c + d x])^2 \sqrt{\frac{1}{1 - \tan^2 \left[ \frac{1}{2} (c + d x) \right]^2}} \right. \\
& \quad \left( a A b^2 \tan \left[ \frac{1}{2} (c + d x) \right] + A b^3 \tan \left[ \frac{1}{2} (c + d x) \right] + a^3 C \tan \left[ \frac{1}{2} (c + d x) \right] + \right. \\
& \quad a^2 b C \tan \left[ \frac{1}{2} (c + d x) \right] - 2 a A b^2 \tan \left[ \frac{1}{2} (c + d x) \right]^3 - 2 a^3 C \tan \left[ \frac{1}{2} (c + d x) \right]^3 + \\
& \quad a A b^2 \tan \left[ \frac{1}{2} (c + d x) \right]^5 - A b^3 \tan \left[ \frac{1}{2} (c + d x) \right]^5 + a^3 C \tan \left[ \frac{1}{2} (c + d x) \right]^5 - \\
& \quad a^2 b C \tan \left[ \frac{1}{2} (c + d x) \right]^5 - 2 a^2 A b \operatorname{EllipticPi} \left[ -1, -\operatorname{ArcSin} \left[ \tan \left[ \frac{1}{2} (c + d x) \right] \right] \right], \frac{a - b}{a + b} \\
& \quad \sqrt{1 - \tan^2 \left[ \frac{1}{2} (c + d x) \right]^2} \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} + \\
& \quad 2 A b^3 \operatorname{EllipticPi} \left[ -1, -\operatorname{ArcSin} \left[ \tan \left[ \frac{1}{2} (c + d x) \right] \right] \right], \frac{a - b}{a + b} \sqrt{1 - \tan^2 \left[ \frac{1}{2} (c + d x) \right]^2} \\
& \quad \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} - \\
& \quad 2 a^2 A b \operatorname{EllipticPi} \left[ -1, -\operatorname{ArcSin} \left[ \tan \left[ \frac{1}{2} (c + d x) \right] \right] \right], \frac{a - b}{a + b} \tan \left[ \frac{1}{2} (c + d x) \right]^2 \\
& \quad \sqrt{1 - \tan^2 \left[ \frac{1}{2} (c + d x) \right]^2} \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} + \\
& \quad 2 A b^3 \operatorname{EllipticPi} \left[ -1, -\operatorname{ArcSin} \left[ \tan \left[ \frac{1}{2} (c + d x) \right] \right] \right], \frac{a - b}{a + b} \tan \left[ \frac{1}{2} (c + d x) \right]^2 \\
& \quad \sqrt{1 - \tan^2 \left[ \frac{1}{2} (c + d x) \right]^2} \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} + \\
& \quad (a + b) (A b^2 + a^2 C) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \tan \left[ \frac{1}{2} (c + d x) \right] \right] \right], \frac{a - b}{a + b} \sqrt{1 - \tan^2 \left[ \frac{1}{2} (c + d x) \right]^2}
\end{aligned}$$

$$\left(1 + \tan\left[\frac{1}{2}(c+dx)\right]\right)^2 \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} -$$

$$ab(a+b)(A+C) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}$$

$$\left(1 + \tan\left[\frac{1}{2}(c+dx)\right]\right)^2 \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \Bigg) /$$

$$\left( a(-a^2b + b^3) d (A + 2C + A \cos[2c + 2dx]) \sqrt{\sec[c+dx]} (a + b \sec[c+dx])^{3/2} \right.$$

$$\left. \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]\right)^{3/2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}} \right)$$

**Problem 746: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c+dx] (A + C \sec[c+dx]^2)}{(a + b \sec[c+dx])^{3/2}} dx$$

Optimal (type 4, 431 leaves, 7 steps):

$$-\frac{1}{a^2 b \sqrt{a+b} d} (3Ab^2 - a^2(A-2C)) \cot[c+dx] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1 - \sec[c+dx])}{a+b}} \sqrt{-\frac{b(1 + \sec[c+dx])}{a-b}} + \frac{1}{a^2 b \sqrt{a+b} d}$$

$$(aAb + 3Ab^2 + 2a^2C) \cot[c+dx] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1 - \sec[c+dx])}{a+b}} \sqrt{-\frac{b(1 + \sec[c+dx])}{a-b}} + \frac{1}{a^3 d}$$

$$3Ab \sqrt{a+b} \cot[c+dx] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1 - \sec[c+dx])}{a+b}} \sqrt{-\frac{b(1 + \sec[c+dx])}{a-b}} +$$

$$\frac{A \sin[c+dx]}{a d \sqrt{a+b \sec[c+dx]}} - \frac{b(3Ab^2 - a^2(A-2C)) \tan[c+dx]}{a^2(a^2 - b^2) d \sqrt{a+b \sec[c+dx]}}$$

Result (type 4, 1259 leaves):

$$\begin{aligned}
 & \left( (b + a \cos [c + d x])^2 (A + C \sec [c + d x])^2 \right. \\
 & \quad \left. \left( \frac{4 (A b^2 + a^2 C) \sin [c + d x]}{a^2 (a^2 - b^2)} - \frac{4 (A b^3 \sin [c + d x] + a^2 b C \sin [c + d x])}{a^2 (a^2 - b^2) (b + a \cos [c + d x])} \right) \right) / \\
 & \quad (d (A + 2 C + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^{3/2}) - \\
 & \quad \left( 2 (b + a \cos [c + d x])^{3/2} (A + C \sec [c + d x])^2 \sqrt{\frac{1}{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \right. \\
 & \quad \left. \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \right. \\
 & \quad \left( a^3 A \tan \left[ \frac{1}{2} (c + d x) \right] + a^2 A b \tan \left[ \frac{1}{2} (c + d x) \right] - 3 a A b^2 \tan \left[ \frac{1}{2} (c + d x) \right] - \right. \\
 & \quad 3 A b^3 \tan \left[ \frac{1}{2} (c + d x) \right] - 2 a^3 C \tan \left[ \frac{1}{2} (c + d x) \right] - 2 a^2 b C \tan \left[ \frac{1}{2} (c + d x) \right] - \\
 & \quad 2 a^3 A \tan \left[ \frac{1}{2} (c + d x) \right]^3 + 6 a A b^2 \tan \left[ \frac{1}{2} (c + d x) \right]^3 + 4 a^3 C \tan \left[ \frac{1}{2} (c + d x) \right]^3 + \\
 & \quad a^3 A \tan \left[ \frac{1}{2} (c + d x) \right]^5 - a^2 A b \tan \left[ \frac{1}{2} (c + d x) \right]^5 - 3 a A b^2 \tan \left[ \frac{1}{2} (c + d x) \right]^5 + \\
 & \quad 3 A b^3 \tan \left[ \frac{1}{2} (c + d x) \right]^5 - 2 a^3 C \tan \left[ \frac{1}{2} (c + d x) \right]^5 + 2 a^2 b C \tan \left[ \frac{1}{2} (c + d x) \right]^5 + \\
 & \quad \left. 6 a^2 A b \operatorname{EllipticPi} \left[ -1, -\operatorname{ArcSin} \left[ \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a - b}{a + b} \right] \right. \\
 & \quad \left. \sqrt{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2} \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} - \right. \\
 & \quad \left. 6 A b^3 \operatorname{EllipticPi} \left[ -1, -\operatorname{ArcSin} \left[ \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a - b}{a + b} \right] \sqrt{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2} \right. \\
 & \quad \left. \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} + \right. \\
 & \quad \left. 6 a^2 A b \operatorname{EllipticPi} \left[ -1, -\operatorname{ArcSin} \left[ \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a - b}{a + b} \right] \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right. \\
 & \quad \left. \sqrt{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2} \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} - \right.
 \end{aligned}$$

$$\begin{aligned}
 & 6 A b^3 \text{EllipticPi}\left[-1, -\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1-\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & (a+b)(-3Ab^2+a^2(A-2C)) \text{EllipticE}\left[\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1-\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \left(1+\text{Tan}\left[\frac{1}{2}(c+dx)\right]\right)^2 \\
 & \sqrt{\frac{a+b-a \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & 2a(a+b)(Ab+aC) \text{EllipticF}\left[\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1+\text{Tan}\left[\frac{1}{2}(c+dx)\right]\right)^2 \sqrt{\frac{a+b-a \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \Bigg) \Bigg/ \\
 & \left(a^2(a^2-b^2)d(A+2C+A \text{Cos}[2c+2dx]) \sqrt{\text{Sec}[c+dx]} (a+b \text{Sec}[c+dx])^{3/2} \right. \\
 & \left. \sqrt{1+\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \left(a \left(-1+\text{Tan}\left[\frac{1}{2}(c+dx)\right]\right)^2 - b \left(1+\text{Tan}\left[\frac{1}{2}(c+dx)\right]\right)^2\right)\right)
 \end{aligned}$$

**Problem 747: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\text{Cos}[c+dx]^2 (A+C \text{Sec}[c+dx]^2)}{(a+b \text{Sec}[c+dx])^{3/2}} dx$$

Optimal (type 4, 501 leaves, 8 steps):

$$\frac{1}{4 a^3 \sqrt{a+b} d} (15 A b^2 - a^2 (7 A - 8 C)) \operatorname{Cot}[c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \frac{1}{4 a^3 \sqrt{a+b} d}$$

$$(5 a A b + 15 A b^2 - 2 a^2 (A - 4 C)) \operatorname{Cot}[c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \frac{1}{4 a^4 d} \sqrt{a+b} (15 A b^2 + 4 a^2 (A + 2 C))$$

$$\operatorname{Cot}[c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \frac{5 A b \operatorname{Sin}[c+d x]}{4 a^2 d \sqrt{a+b \operatorname{Sec}[c+d x]}} +$$

$$\frac{A \operatorname{Cos}[c+d x] \operatorname{Sin}[c+d x]}{2 a d \sqrt{a+b \operatorname{Sec}[c+d x]}} + \frac{b^2 (15 A b^2 - a^2 (7 A - 8 C)) \operatorname{Tan}[c+d x]}{4 a^3 (a^2 - b^2) d \sqrt{a+b \operatorname{Sec}[c+d x]}}$$

Result (type 4, 41966 leaves): Display of huge result suppressed!

**Problem 748: Attempted integration timed out after 120 seconds.**

$$\int \frac{\operatorname{Sec}[c+d x]^3 (A+C \operatorname{Sec}[c+d x]^2)}{(a+b \operatorname{Sec}[c+d x])^{5/2}} dx$$

Optimal (type 4, 488 leaves, 6 steps):

$$\left( 4 a (a^2 b^2 (A - 14 C) - b^4 (3 A - 4 C) + 8 a^4 C) \cot [c + d x] \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \operatorname{Sec} [c + d x]}}{\sqrt{a + b}} \right] \right], \right.$$

$$\left. \frac{a + b}{a - b} \sqrt{\frac{b (1 - \operatorname{Sec} [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec} [c + d x])}{a - b}} \right) / (3 b^5 \sqrt{a + b} (a^2 - b^2) d) +$$

$$\left( 2 (2 a^2 b^2 (A - 8 C) + 3 a b^3 (A - 3 C) + 16 a^4 C + 12 a^3 b C - b^4 (3 A + C)) \cot [c + d x] \operatorname{EllipticF} \left[ \right. \right.$$

$$\left. \left. \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \operatorname{Sec} [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \sqrt{\frac{b (1 - \operatorname{Sec} [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec} [c + d x])}{a - b}} \right] \right) /$$

$$(3 b^4 \sqrt{a + b} (a^2 - b^2) d) - \frac{2 (A b^2 + a^2 C) \operatorname{Sec} [c + d x]^2 \operatorname{Tan} [c + d x]}{3 b (a^2 - b^2) d (a + b \operatorname{Sec} [c + d x])^{3/2}} -$$

$$\frac{4 a (2 A b^4 - 3 a^4 C + 5 a^2 b^2 C) \operatorname{Tan} [c + d x]}{3 b^3 (a^2 - b^2)^2 d \sqrt{a + b \operatorname{Sec} [c + d x]}} +$$

$$\frac{2 (A b^2 + 2 a^2 C - b^2 C) \sqrt{a + b \operatorname{Sec} [c + d x]} \operatorname{Tan} [c + d x]}{3 b^3 (a^2 - b^2) d}$$

Result (type 1, 1 leaves):

???

**Problem 749: Attempted integration timed out after 120 seconds.**

$$\int \frac{\operatorname{Sec} [c + d x]^2 (A + C \operatorname{Sec} [c + d x]^2)}{(a + b \operatorname{Sec} [c + d x])^{5/2}} dx$$

Optimal (type 4, 408 leaves, 5 steps):

$$\left( 2 (3 b^4 (A - C) - 8 a^4 C + a^2 b^2 (A + 15 C)) \operatorname{Cot}[c + d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}}\right]\right], \right.$$

$$\left. \frac{a + b}{a - b} \sqrt{\frac{b (1 - \operatorname{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec}[c + d x])}{a - b}} \right) / (3 b^4 \sqrt{a + b} (a^2 - b^2) d) -$$

$$\left( 2 (3 b^3 (A - C) + 8 a^3 C + 6 a^2 b C - a b^2 (A + 9 C)) \operatorname{Cot}[c + d x] \operatorname{EllipticF}\left[\right.$$

$$\left. \operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b} \sqrt{\frac{b (1 - \operatorname{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec}[c + d x])}{a - b}} \right) /$$

$$(3 b^3 \sqrt{a + b} (a^2 - b^2) d) + \frac{2 a (A b^2 + a^2 C) \operatorname{Tan}[c + d x]}{3 b^2 (a^2 - b^2) d (a + b \operatorname{Sec}[c + d x])^{3/2}} +$$

$$\frac{2 (3 A b^4 - 5 a^4 C + a^2 b^2 (A + 9 C)) \operatorname{Tan}[c + d x]}{3 b^2 (a^2 - b^2)^2 d \sqrt{a + b \operatorname{Sec}[c + d x]}}$$

Result (type 1, 1 leaves):

???

### Problem 750: Unable to integrate problem.

$$\int \frac{\operatorname{Sec}[c + d x] (A + C \operatorname{Sec}[c + d x]^2)}{(a + b \operatorname{Sec}[c + d x])^{5/2}} dx$$

Optimal (type 4, 378 leaves, 5 steps):



$$\begin{aligned}
 & - \left( \left( 4 a (2 A b^2 - a^2 C + 3 b^2 C) \operatorname{Cot}[c + d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \right. \right. \\
 & \quad \left. \left. \sqrt{\frac{b (1 - \operatorname{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec}[c + d x])}{a - b}} \right) / \left( 3 (a - b) b^3 (a + b)^{3/2} d \right) \right) + \\
 & \left( 2 (2 a^2 C + 3 a b (A + C) - b^2 (A + 3 C)) \operatorname{Cot}[c + d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \right. \\
 & \quad \left. \sqrt{\frac{b (1 - \operatorname{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec}[c + d x])}{a - b}} \right) / \left( 3 b^2 \sqrt{a + b} (a^2 - b^2) d \right) - \\
 & \frac{2 (A b^2 + a^2 C) \operatorname{Tan}[c + d x]}{3 b (a^2 - b^2) d (a + b \operatorname{Sec}[c + d x])^{3/2}} - \frac{4 a (2 A b^2 - a^2 C + 3 b^2 C) \operatorname{Tan}[c + d x]}{3 b (a^2 - b^2)^2 d \sqrt{a + b \operatorname{Sec}[c + d x]}}
 \end{aligned}$$

Result (type 8, 35 leaves):

$$\int \frac{\operatorname{Sec}[c + d x] (A + C \operatorname{Sec}[c + d x]^2)}{(a + b \operatorname{Sec}[c + d x])^{5/2}} dx$$

**Problem 751: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + C \operatorname{Sec}[c + d x]^2}{(a + b \operatorname{Sec}[c + d x])^{5/2}} dx$$

Optimal (type 4, 517 leaves, 7 steps):

$$\begin{aligned}
 & - \left( \left( 2 (3 A b^4 - a^4 C - a^2 b^2 (7 A + 3 C)) \operatorname{Cot}[c + d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \right. \right. \\
 & \quad \left. \left. \sqrt{\frac{b (1 - \operatorname{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec}[c + d x])}{a - b}} \right) / (3 a^2 b^2 \sqrt{a + b} (a^2 - b^2) d) \right) - \\
 & \left( 2 (6 a^2 A b - a A b^2 - 3 A b^3 - a^3 C + 3 a^2 b C) \operatorname{Cot}[c + d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}}\right], \right. \right. \\
 & \quad \left. \left. \frac{a + b}{a - b} \right] \sqrt{\frac{b (1 - \operatorname{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec}[c + d x])}{a - b}} \right) / (3 a^2 (a - b) b (a + b)^{3/2} d) - \\
 & \frac{1}{a^3 d} 2 A \sqrt{a + b} \operatorname{Cot}[c + d x] \operatorname{EllipticPi}\left[\frac{a + b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \\
 & \quad \sqrt{\frac{b (1 - \operatorname{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec}[c + d x])}{a - b}} + \\
 & \quad \frac{2 (A b^2 + a^2 C) \operatorname{Tan}[c + d x]}{3 a (a^2 - b^2) d (a + b \operatorname{Sec}[c + d x])^{3/2}} - \\
 & \quad \frac{2 (3 A b^4 - a^4 C - a^2 b^2 (7 A + 3 C)) \operatorname{Tan}[c + d x]}{3 a^2 (a^2 - b^2)^2 d \sqrt{a + b \operatorname{Sec}[c + d x]}}
 \end{aligned}$$

Result (type 4, 1727 leaves):

$$\begin{aligned}
 & \left( (b + a \operatorname{Cos}[c + d x])^3 \operatorname{Sec}[c + d x] (A + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \quad \left( \frac{4 (-7 a^2 A b^2 + 3 A b^4 - a^4 C - 3 a^2 b^2 C) \operatorname{Sin}[c + d x]}{3 a^2 b (-a^2 + b^2)^2} - \frac{4 (A b^3 \operatorname{Sin}[c + d x] + a^2 b C \operatorname{Sin}[c + d x])}{3 a^2 (a^2 - b^2) (b + a \operatorname{Cos}[c + d x])^2} \right. \\
 & \quad \left. \left. (8 (4 a^2 A b^2 \operatorname{Sin}[c + d x] - 2 A b^4 \operatorname{Sin}[c + d x] + a^4 C \operatorname{Sin}[c + d x] + a^2 b^2 C \operatorname{Sin}[c + d x])) / \right. \right. \\
 & \quad \left. \left. (3 a^2 (a^2 - b^2)^2 (b + a \operatorname{Cos}[c + d x])) \right) \right) / \\
 & \left( d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) (a + b \operatorname{Sec}[c + d x])^{5/2} \right) - \\
 & \left( 4 (b + a \operatorname{Cos}[c + d x])^{5/2} \sqrt{\operatorname{Sec}[c + d x]} (A + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \quad \left. \sqrt{\frac{1}{1 - \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2}} \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2}} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( 7 a^3 A b^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + 7 a^2 A b^3 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] - 3 a A b^4 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] - 3 A b^5 \right. \\
 & \quad \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + a^5 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + a^4 b C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + 3 a^3 b^2 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + \\
 & \quad 3 a^2 b^3 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] - 14 a^3 A b^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 + 6 a A b^4 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 - \\
 & \quad 2 a^5 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 - 6 a^3 b^2 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 + 7 a^3 A b^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - \\
 & \quad 7 a^2 A b^3 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - 3 a A b^4 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + 3 A b^5 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + \\
 & \quad a^5 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - a^4 b C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + 3 a^3 b^2 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - \\
 & \quad \left. 3 a^2 b^3 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - 6 a^4 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \right. \\
 & \quad \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \\
 & \quad 12 a^2 A b^3 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \\
 & \quad \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
 & \quad 6 A b^5 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \\
 & \quad \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
 & \quad 6 a^4 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
 & \quad \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \\
 & \quad 12 a^2 A b^3 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
 & \quad \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
 & \quad \left. 6 A b^5 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \right)
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & (a+b) \left(-3Ab^4 + a^4C + a^2b^2(7A+3C)\right) \text{EllipticE}\left[\text{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \\
 & \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & ab(a+b) \left(-2Ab^2 + 3ab(A+C) + a^2(3A+C)\right) \text{EllipticF}\left[\text{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \\
 & \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \Bigg) \Bigg/ \\
 & \left(3a^2b(a^2-b^2)^2d(A+2C+A\cos[2c+2dx]) (a+b\sec[c+dx])^{5/2} \right. \\
 & \left. \sqrt{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} \right. \\
 & \left. \left(a\left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) - b\left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right)\right)
 \end{aligned}$$

**Problem 752: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c+dx] (A+C\sec[c+dx]^2)}{(a+b\sec[c+dx])^{5/2}} dx$$

Optimal (type 4, 559 leaves, 8 steps):

$$\begin{aligned}
 & - \left( \left( (26 a^2 A b^2 - 15 A b^4 - a^4 (3 A - 8 C)) \cot [c + d x] \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \sec [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \right. \right. \\
 & \quad \left. \left. \sqrt{\frac{b (1 - \sec [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \sec [c + d x])}{a - b}} \right) / (3 a^3 (a - b) b (a + b)^{3/2} d) \right) + \\
 & \left( (21 a^2 A b^2 - 5 a A b^3 - 15 A b^4 + a^3 b (3 A - 2 C) + 6 a^4 C) \cot [c + d x] \right. \\
 & \quad \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \sec [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \sqrt{\frac{b (1 - \sec [c + d x])}{a + b}} \\
 & \quad \left. \sqrt{-\frac{b (1 + \sec [c + d x])}{a - b}} \right) / (3 a^3 (a - b) b (a + b)^{3/2} d) + \frac{1}{a^4 d} \\
 & 5 A b \sqrt{a + b} \cot [c + d x] \operatorname{EllipticPi} \left[ \frac{a + b}{a}, \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \sec [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \\
 & \quad \sqrt{\frac{b (1 - \sec [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \sec [c + d x])}{a - b}} + \\
 & \quad \frac{A \sin [c + d x]}{a d (a + b \sec [c + d x])^{3/2}} - \frac{b (5 A b^2 - a^2 (3 A - 2 C)) \tan [c + d x]}{3 a^2 (a^2 - b^2) d (a + b \sec [c + d x])^{3/2}} - \\
 & \quad \frac{b (26 a^2 A b^2 - 15 A b^4 - a^4 (3 A - 8 C)) \tan [c + d x]}{3 a^3 (a^2 - b^2)^2 d \sqrt{a + b \sec [c + d x]}}
 \end{aligned}$$

Result (type 4, 1714 leaves):

$$\begin{aligned}
 & \left( (b + a \cos [c + d x])^3 \sec [c + d x] (A + C \sec [c + d x])^2 \right. \\
 & \quad \left( -\frac{8 (-5 a^2 A b^2 + 3 A b^4 - 2 a^4 C) \sin [c + d x]}{3 a^3 (-a^2 + b^2)^2} + \frac{4 (A b^4 \sin [c + d x] + a^2 b^2 C \sin [c + d x])}{3 a^3 (a^2 - b^2) (b + a \cos [c + d x])^2} + \right. \\
 & \quad \left. (4 (-11 a^2 A b^3 \sin [c + d x] + 7 A b^5 \sin [c + d x] - 5 a^4 b C \sin [c + d x] + a^2 b^3 C \sin [c + d x])) \right) / \\
 & \quad \left. (3 a^3 (a^2 - b^2)^2 (b + a \cos [c + d x])) \right) / \\
 & (d (A + 2 C + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^{5/2}) - \\
 & \left( 2 (b + a \cos [c + d x])^{5/2} \sqrt{\sec [c + d x]} (A + C \sec [c + d x])^2 \right)
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{1}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}} \\
 & \left( 3 a^5 A \tan\left[\frac{1}{2}(c+dx)\right] + 3 a^4 A b \tan\left[\frac{1}{2}(c+dx)\right] - 26 a^3 A b^2 \tan\left[\frac{1}{2}(c+dx)\right] - \right. \\
 & 26 a^2 A b^3 \tan\left[\frac{1}{2}(c+dx)\right] + 15 a A b^4 \tan\left[\frac{1}{2}(c+dx)\right] + 15 A b^5 \tan\left[\frac{1}{2}(c+dx)\right] - \\
 & 8 a^5 C \tan\left[\frac{1}{2}(c+dx)\right] - 8 a^4 b C \tan\left[\frac{1}{2}(c+dx)\right] - 6 a^5 A \tan\left[\frac{1}{2}(c+dx)\right]^3 + \\
 & 52 a^3 A b^2 \tan\left[\frac{1}{2}(c+dx)\right]^3 - 30 a A b^4 \tan\left[\frac{1}{2}(c+dx)\right]^3 + 16 a^5 C \tan\left[\frac{1}{2}(c+dx)\right]^3 + \\
 & 3 a^5 A \tan\left[\frac{1}{2}(c+dx)\right]^5 - 3 a^4 A b \tan\left[\frac{1}{2}(c+dx)\right]^5 - 26 a^3 A b^2 \tan\left[\frac{1}{2}(c+dx)\right]^5 + \\
 & 26 a^2 A b^3 \tan\left[\frac{1}{2}(c+dx)\right]^5 + 15 a A b^4 \tan\left[\frac{1}{2}(c+dx)\right]^5 - \\
 & 15 A b^5 \tan\left[\frac{1}{2}(c+dx)\right]^5 - 8 a^5 C \tan\left[\frac{1}{2}(c+dx)\right]^5 + 8 a^4 b C \tan\left[\frac{1}{2}(c+dx)\right]^5 + \\
 & \left. 30 a^4 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \right. \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 60 a^2 A b^3 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & 30 A b^5 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & 30 a^4 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 60 a^2 A b^3 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & 30 A b^5 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & (a+b) (-26 a^2 A b^2 + 15 A b^4 + a^4 (3 A - 8 C)) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \\
 & \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & 2 a (a+b) (3 a A b^2 - 5 A b^3 + 3 a^3 C + a^2 b (6 A + C)) \\
 & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left. \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \right) \Bigg/ \\
 & \left( 3 a (a^3 - a b^2)^2 d (A + 2 C + A \cos[2c + 2dx]) (a + b \sec[c + dx])^{5/2} \right. \\
 & \left. \sqrt{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} \right. \\
 & \left. \left( a \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) - b \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \right)
 \end{aligned}$$

**Problem 753: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c+dx]^2 (A+C \sec[c+dx]^2)}{(a+b \sec[c+dx])^{5/2}} dx$$

Optimal (type 4, 645 leaves, 9 steps):

$$\begin{aligned}
 & - \left( \left( 105 A b^4 + a^4 (33 A - 56 C) - 2 a^2 b^2 (85 A - 12 C) \right) \right. \\
 & \quad \text{Cot}[c + d x] \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \\
 & \quad \left. \sqrt{\frac{b(1 - \text{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \text{Sec}[c + d x])}{a - b}} \right) / \left( 12 a^4 \sqrt{a + b} (a^2 - b^2) d \right) + \\
 & \left( (35 a A b^3 + 105 A b^4 + 6 a^4 (A - 8 C) - 3 a^2 b^2 (45 A - 8 C) - a^3 (27 A b - 8 b C)) \right. \\
 & \quad \text{Cot}[c + d x] \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \\
 & \quad \left. \sqrt{\frac{b(1 - \text{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \text{Sec}[c + d x])}{a - b}} \right) / \left( 12 a^4 \sqrt{a + b} (a^2 - b^2) d \right) - \\
 & \frac{1}{4 a^5 d} \sqrt{a + b} (35 A b^2 + 4 a^2 (A + 2 C)) \text{Cot}[c + d x] \\
 & \quad \text{EllipticPi}\left[\frac{a + b}{a}, \text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \\
 & \quad \sqrt{\frac{b(1 - \text{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \text{Sec}[c + d x])}{a - b}} - \\
 & \quad \frac{7 A b \text{Sin}[c + d x]}{4 a^2 d (a + b \text{Sec}[c + d x])^{3/2}} + \frac{A \text{Cos}[c + d x] \text{Sin}[c + d x]}{2 a d (a + b \text{Sec}[c + d x])^{3/2}} + \\
 & \quad \frac{b^2 (35 A b^2 - a^2 (27 A - 8 C)) \text{Tan}[c + d x]}{12 a^3 (a^2 - b^2) d (a + b \text{Sec}[c + d x])^{3/2}} - \\
 & \quad \frac{b^2 (105 A b^4 + a^4 (33 A - 56 C) - 2 a^2 b^2 (85 A - 12 C)) \text{Tan}[c + d x]}{12 a^4 (a^2 - b^2)^2 d \sqrt{a + b \text{Sec}[c + d x]}}
 \end{aligned}$$

Result (type 4, 4981 leaves):

$$\begin{aligned}
 & \frac{1}{2} \left( \left( (b + a \text{Cos}[c + d x])^3 \text{Sec}[c + d x] \right)^3 \left( \frac{4 b (-13 a^2 A b^2 + 9 A b^4 - 7 a^4 C + 3 a^2 b^2 C) \text{Sin}[c + d x]}{3 a^4 (-a^2 + b^2)^2} - \right. \right. \\
 & \quad \frac{4 (A b^5 \text{Sin}[c + d x] + a^2 b^3 C \text{Sin}[c + d x])}{3 a^4 (a^2 - b^2) (b + a \text{Cos}[c + d x])^2} - (8 (-7 a^2 A b^4 \text{Sin}[c + d x] + \\
 & \quad \left. \left. 5 A b^6 \text{Sin}[c + d x] - 4 a^4 b^2 C \text{Sin}[c + d x] + 2 a^2 b^4 C \text{Sin}[c + d x]) \right) \right) /
 \end{aligned}$$



$$\begin{aligned}
 & \left( 3 a^4 (a^2 - b^2)^2 (b + a \cos [c + d x]) + \frac{A \sin [2 (c + d x)]}{2 a^3} \right) / \left( d (a + b \sec [c + d x])^{5/2} \right) + \\
 & \left( (b + a \cos [c + d x])^{5/2} \left( \frac{a^2 A}{(a^2 - b^2)^2 \sqrt{b + a \cos [c + d x]} \sqrt{\sec [c + d x]}} + \right. \right. \\
 & \quad \frac{4 A b^2}{(a^2 - b^2)^2 \sqrt{b + a \cos [c + d x]} \sqrt{\sec [c + d x]}} - \\
 & \quad \frac{7 A b^4}{3 a^2 (a^2 - b^2)^2 \sqrt{b + a \cos [c + d x]} \sqrt{\sec [c + d x]}} + \\
 & \quad \frac{2 a^2 C}{(a^2 - b^2)^2 \sqrt{b + a \cos [c + d x]} \sqrt{\sec [c + d x]}} + \\
 & \quad \frac{2 b^2 C}{3 (a^2 - b^2)^2 \sqrt{b + a \cos [c + d x]} \sqrt{\sec [c + d x]}} - \\
 & \quad \frac{9 a A b \sqrt{\sec [c + d x]}}{4 (a^2 - b^2)^2 \sqrt{b + a \cos [c + d x]}} + \frac{31 A b^3 \sqrt{\sec [c + d x]}}{6 a (a^2 - b^2)^2 \sqrt{b + a \cos [c + d x]}} - \\
 & \quad \frac{35 A b^5 \sqrt{\sec [c + d x]}}{12 a^3 (a^2 - b^2)^2 \sqrt{b + a \cos [c + d x]}} + \frac{2 a b C \sqrt{\sec [c + d x]}}{3 (a^2 - b^2)^2 \sqrt{b + a \cos [c + d x]}} - \\
 & \quad \frac{2 b^3 C \sqrt{\sec [c + d x]}}{3 a (a^2 - b^2)^2 \sqrt{b + a \cos [c + d x]}} - \frac{11 a A b \cos [2 (c + d x)] \sqrt{\sec [c + d x]}}{4 (a^2 - b^2)^2 \sqrt{b + a \cos [c + d x]}} + \\
 & \quad \frac{85 A b^3 \cos [2 (c + d x)] \sqrt{\sec [c + d x]}}{6 a (a^2 - b^2)^2 \sqrt{b + a \cos [c + d x]}} - \frac{35 A b^5 \cos [2 (c + d x)] \sqrt{\sec [c + d x]}}{4 a^3 (a^2 - b^2)^2 \sqrt{b + a \cos [c + d x]}} + \\
 & \quad \left. \frac{14 a b C \cos [2 (c + d x)] \sqrt{\sec [c + d x]}}{3 (a^2 - b^2)^2 \sqrt{b + a \cos [c + d x]}} - \frac{2 b^3 C \cos [2 (c + d x)] \sqrt{\sec [c + d x]}}{a (a^2 - b^2)^2 \sqrt{b + a \cos [c + d x]}} \right) \\
 & \sec [c + d x]^{5/2} \left( - \left( \left( b (105 A b^4 + a^4 (33 A - 56 C) + 2 a^2 b^2 (-85 A + 12 C)) \right. \right. \right. \\
 & \quad \left. \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right] \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \right) / \right. \right. \\
 & \quad \left. \left. \left( 6 a^4 (a^2 - b^2)^2 \sqrt{\frac{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \right) \right) \right) -
 \end{aligned}$$

$$\left( (a+b) \left( b (105 A b^4 + a^4 (33 A - 56 C) + 2 a^2 b^2 (-85 A + 12 C)) \text{EllipticE} \left[ \text{ArcSin} \left[ \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a-b}{a+b} \right] + 2 a (21 a A b^3 - 35 A b^4 + a^2 b^2 (33 A - 8 C) + 6 a^4 (A + 2 C) + a^3 (-9 A b + 12 b C)) \text{EllipticF} \left[ \text{ArcSin} \left[ \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a-b}{a+b} \right] + 6 (a-b)^2 (a+b) (35 A b^2 + 4 a^2 (A + 2 C)) \text{EllipticPi} \left[ -1, -\text{ArcSin} \left[ \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a-b}{a+b} \right] \sqrt{\frac{a+b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a+b}} \right. \right.$$

$$\left. \sqrt{\frac{a+b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \sqrt{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^4} \right) /$$

$$\left( 6 a^4 (a^2 - b^2)^2 \sqrt{\frac{1}{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \left( b - b \tan \left[ \frac{1}{2} (c + d x) \right] \right)^4 + a \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right)^2 \right) /$$

$$\left( d (a+b \sec [c + d x])^{5/2} \left( - \left( \left( b (105 A b^4 + a^4 (33 A - 56 C) + 2 a^2 b^2 (-85 A + 12 C)) \text{Sec} \left[ \frac{1}{2} (c + d x) \right] \right)^2 \sqrt{\frac{a+b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \right) / \right. \right.$$

$$\left. \left( 12 a^4 (a^2 - b^2)^2 \sqrt{\frac{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \right) \right) +$$

$$\left( (a+b) \left( b (105 A b^4 + a^4 (33 A - 56 C) + 2 a^2 b^2 (-85 A + 12 C)) \text{EllipticE} \left[ \text{ArcSin} \left[ \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a-b}{a+b} \right] + 2 a (21 a A b^3 - 35 A b^4 + a^2 b^2 (33 A - 8 C) + 6 a^4 (A + 2 C) + a^3 (-9 A b + 12 b C)) \text{EllipticF} \left[ \text{ArcSin} \left[ \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a-b}{a+b} \right] + 6 (a-b)^2 (a+b) (35 A b^2 + 4 a^2 (A + 2 C)) \text{EllipticPi} \left[ -1, -\text{ArcSin} \left[ \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a-b}{a+b} \right] \sqrt{\frac{a+b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a+b}} \right. \right.$$

$$\begin{aligned}
 & \left. \tan\left[\frac{1}{2}(c+dx)\right], \frac{a-b}{a+b}\right) \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \\
 & \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^4} \\
 & \left(-2 b \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^3+\right. \\
 & \left. 2 a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) / \left(6 a^4\left(a^2-b^2\right)^2\right. \\
 & \left.\sqrt{\frac{1}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}\left(b-b \tan\left[\frac{1}{2}(c+dx)\right]^4+a\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2\right)}\right) + \\
 & \left((a+b)\left(b\left(105 A b^4+a^4(33 A-56 C)+2 a^2 b^2(-85 A+12 C)\right) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right], \frac{a-b}{a+b}\right]+2 a\left(21 a A b^3-35 A b^4+a^2 b^2(33 A-8 C)+6 a^4(A+2 C)+\right.\right.\right.\right. \\
 & \left.\left.\left.\left.a^3(-9 A b+12 b C)\right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right], \frac{a-b}{a+b}\right]+6(a-b)^2(a+b)(35 A b^2+4 a^2(A+2 C)) \operatorname{EllipticPi}\left[-1,-\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right], \frac{a-b}{a+b}\right]\right]\right)\right) \\
 & \left.\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^3 \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}}\right. \right. \\
 & \left.\left.\sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}}\right) / \left(6 a^4\left(a^2-b^2\right)^2 \sqrt{\frac{1}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^4}\right.\right. \\
 & \left.\left.\left(b-b \tan\left[\frac{1}{2}(c+dx)\right]^4+a\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2\right)\right) - \right. \\
 & \left.\left(\left(b\left(105 A b^4+a^4(33 A-56 C)+2 a^2 b^2(-85 A+12 C)\right) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right], \frac{a-b}{a+b}\right]\right]\right)\right)
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{2} (c + d x) \Big] \Big], \frac{a-b}{a+b} \Big] + 2 a (21 a A b^3 - 35 A b^4 + a^2 b^2 (33 A - 8 C) + 6 a^4 (A + 2 C) + \\
 & a^3 (-9 A b + 12 b C)) \text{EllipticF}\left[\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2} (c + d x)\right]\right], \frac{a-b}{a+b}\right] + 6 (a-b)^2 (a + \\
 & b) (35 A b^2 + 4 a^2 (A + 2 C)) \text{EllipticPi}\left[-1, -\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2} (c + d x)\right]\right], \frac{a-b}{a+b}\right] \\
 & \left(-a \text{Sec}\left[\frac{1}{2} (c + d x)\right]^2 \text{Tan}\left[\frac{1}{2} (c + d x)\right] + b \text{Sec}\left[\frac{1}{2} (c + d x)\right]^2 \text{Tan}\left[\frac{1}{2} (c + d x)\right]\right) \\
 & \sqrt{\frac{a+b-a \text{Tan}\left[\frac{1}{2} (c + d x)\right]^2 + b \text{Tan}\left[\frac{1}{2} (c + d x)\right]^2}{1 + \text{Tan}\left[\frac{1}{2} (c + d x)\right]^2}} \sqrt{1 - \text{Tan}\left[\frac{1}{2} (c + d x)\right]^4} \Big/ \left(12 a^4 \right. \\
 & (a^2 - b^2)^2 \sqrt{\frac{1}{1 - \text{Tan}\left[\frac{1}{2} (c + d x)\right]^2}} \sqrt{\frac{a+b-a \text{Tan}\left[\frac{1}{2} (c + d x)\right]^2 + b \text{Tan}\left[\frac{1}{2} (c + d x)\right]^2}{a+b}} \\
 & \left. \left(b - b \text{Tan}\left[\frac{1}{2} (c + d x)\right]^4 + a \left(-1 + \text{Tan}\left[\frac{1}{2} (c + d x)\right]^2\right)^2\right)\right) \Big] + \\
 & \left( (a+b) \left( b (105 A b^4 + a^4 (33 A - 56 C) + 2 a^2 b^2 (-85 A + 12 C)) \text{EllipticE}\left[\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2} (c + d x)\right]\right], \frac{a-b}{a+b}\right] + 2 a (21 a A b^3 - 35 A b^4 + a^2 b^2 (33 A - 8 C) + 6 a^4 (A + 2 C) + \right. \right. \\
 & a^3 (-9 A b + 12 b C)) \text{EllipticF}\left[\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2} (c + d x)\right]\right], \frac{a-b}{a+b}\right] + 6 (a-b)^2 (a + \\
 & b) (35 A b^2 + 4 a^2 (A + 2 C)) \text{EllipticPi}\left[-1, -\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2} (c + d x)\right]\right], \frac{a-b}{a+b}\right] \Big) \\
 & \text{Sec}\left[\frac{1}{2} (c + d x)\right]^2 \text{Tan}\left[\frac{1}{2} (c + d x)\right] \sqrt{\frac{1}{1 - \text{Tan}\left[\frac{1}{2} (c + d x)\right]^2}} \\
 & \sqrt{\frac{a+b-a \text{Tan}\left[\frac{1}{2} (c + d x)\right]^2 + b \text{Tan}\left[\frac{1}{2} (c + d x)\right]^2}{a+b}} \\
 & \sqrt{\frac{a+b-a \text{Tan}\left[\frac{1}{2} (c + d x)\right]^2 + b \text{Tan}\left[\frac{1}{2} (c + d x)\right]^2}{1 + \text{Tan}\left[\frac{1}{2} (c + d x)\right]^2}} \sqrt{1 - \text{Tan}\left[\frac{1}{2} (c + d x)\right]^4} \Big/ \\
 & \left. \left(12 a^4 (a^2 - b^2)^2 \left(b - b \text{Tan}\left[\frac{1}{2} (c + d x)\right]^4 + a \left(-1 + \text{Tan}\left[\frac{1}{2} (c + d x)\right]^2\right)^2\right)\right) \right) \Big] +
 \end{aligned}$$

$$\left( b (105 A b^4 + a^4 (33 A - 56 C) + 2 a^2 b^2 (-85 A + 12 C)) \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right] \right. \\ \left. \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2}} \left( \frac{\operatorname{Sec}\left[\frac{1}{2} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]}{1 - \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2} + \right. \right. \\ \left. \left. \left( \operatorname{Sec}\left[\frac{1}{2} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right] \left(1 + \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2\right) \right) \right) \right) / \\ \left. \left(1 - \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2\right)^2 \right) \left( 12 a^4 (a^2 - b^2)^2 \left( \frac{1 + \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2}{1 - \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2} \right)^{3/2} \right) -$$

$$\left( b (105 A b^4 + a^4 (33 A - 56 C) + 2 a^2 b^2 (-85 A + 12 C)) \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right] \right. \\ \left. \left( \left( -a \operatorname{Sec}\left[\frac{1}{2} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right] + b \operatorname{Sec}\left[\frac{1}{2} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right] \right) \right) / \right. \\ \left. \left(1 + \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2\right) - \left( \operatorname{Sec}\left[\frac{1}{2} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right] \right. \right. \\ \left. \left. \left( a + b - a \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2 \right) \right) \right) / \\ \left. \left(1 + \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2\right)^2 \right) \left( 12 a^4 (a^2 - b^2)^2 \sqrt{\frac{1 + \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2}{1 - \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2}} \right. \\ \left. \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2}} \right) -$$

$$\left( (a + b) \left( b (105 A b^4 + a^4 (33 A - 56 C) + 2 a^2 b^2 (-85 A + 12 C)) \right. \right. \\ \left. \left. \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]\right], \frac{a - b}{a + b}\right] + \right. \right. \\ \left. \left. 2 a (21 a A b^3 - 35 A b^4 + a^2 b^2 (33 A - 8 C) + 6 a^4 (A + 2 C) + a^3 (-9 A b + 12 b C)) \right. \right. \\ \left. \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]\right], \frac{a - b}{a + b}\right] + 6 (a - b)^2 (a + b) \right. \right. \\ \left. \left. (35 A b^2 + 4 a^2 (A + 2 C)) \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]\right], \frac{a - b}{a + b}\right] \right) \right. \\ \left. \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2}{a + b}} \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2} \right. \\ \left. \left( \left( -a \operatorname{Sec}\left[\frac{1}{2} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right] + b \operatorname{Sec}\left[\frac{1}{2} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right] \right) \right) / \right.$$

$$\begin{aligned}
 & \left( \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right] \right)^2 - \left( \sec\left[\frac{1}{2}(c+dx)\right] \tan\left[\frac{1}{2}(c+dx)\right] \left( a + b - \right. \right. \right. \\
 & \left. \left. \left. a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) / \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \left( 12 \right. \\
 & \left. a^4 (a^2 - b^2)^2 \sqrt{\frac{1}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{\frac{a + b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}} \right. \\
 & \left. \left( b - b \tan\left[\frac{1}{2}(c+dx)\right]^4 + a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) \right) - \\
 & \left( (a + b) \sqrt{\frac{a + b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a + b}} \right. \\
 & \left. \sqrt{\frac{a + b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^4} \right. \\
 & \left. \left( a (21 a A b^3 - 35 A b^4 + a^2 b^2 (33 A - 8 C) + 6 a^4 (A + 2 C) + a^3 (-9 A b + 12 b C)) \right) \right. \\
 & \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \right) / \left( \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{1 - \frac{(a - b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a + b}} \right) - \\
 & \left( 3 (a - b)^2 (a + b) (35 A b^2 + 4 a^2 (A + 2 C)) \sec\left[\frac{1}{2}(c+dx)\right]^2 \right) / \\
 & \left( \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \sqrt{1 - \frac{(a - b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a + b}} \right) + \\
 & \left( b (105 A b^4 + a^4 (33 A - 56 C) + 2 a^2 b^2 (-85 A + 12 C)) \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \left. \left. \sqrt{1 - \frac{(a - b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a + b}} \right) \right) / \left( 2 \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \right) \right) / \left( \right)
 \end{aligned}$$

$$\left( 6 a^4 (a^2 - b^2)^2 \sqrt{\frac{1}{1 - \tan\left[\frac{1}{2}(c + dx)\right]^2}} \left( b - b \tan\left[\frac{1}{2}(c + dx)\right] \right)^4 + \right. \\ \left. a \left( -1 + \tan\left[\frac{1}{2}(c + dx)\right] \right)^2 \right)^2 \right)$$

**Problem 754: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + C \operatorname{Sec}[c + dx]^2}{(a + b \operatorname{Sec}[c + dx])^{7/2}} dx$$

Optimal (type 4, 626 leaves, 8 steps):

$$\begin{aligned}
& - \left( \left( 2 (41 a^2 A b^4 - 15 A b^6 - 3 a^6 C - 29 a^4 b^2 (2 A + C)) \cot [c + d x] \right. \right. \\
& \quad \left. \left. \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \operatorname{Sec} [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \sqrt{\frac{b (1 - \operatorname{Sec} [c + d x])}{a + b}} \right. \right. \\
& \quad \left. \left. \sqrt{-\frac{b (1 + \operatorname{Sec} [c + d x])}{a - b}} \right) / \left( 15 a^3 b^2 \sqrt{a + b} (a^2 - b^2)^2 d \right) \right) + \\
& \left( 2 (36 a^2 A b^3 - 5 a A b^4 - 15 A b^5 + 3 a^5 C + a^3 b^2 (13 A + 5 C) - 3 a^4 b (15 A + 8 C)) \cot [c + d x] \right. \\
& \quad \left. \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \operatorname{Sec} [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \sqrt{\frac{b (1 - \operatorname{Sec} [c + d x])}{a + b}} \right. \right. \\
& \quad \left. \left. \sqrt{-\frac{b (1 + \operatorname{Sec} [c + d x])}{a - b}} \right) / \left( 15 a^3 b \sqrt{a + b} (a^2 - b^2)^2 d \right) - \frac{1}{a^4 d} \right. \\
& \quad \left. 2 A \sqrt{a + b} \cot [c + d x] \operatorname{EllipticPi} \left[ \frac{a + b}{a}, \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \operatorname{Sec} [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \right. \\
& \quad \left. \sqrt{\frac{b (1 - \operatorname{Sec} [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec} [c + d x])}{a - b}} + \right. \\
& \quad \frac{2 (A b^2 + a^2 C) \tan [c + d x]}{5 a (a^2 - b^2) d (a + b \operatorname{Sec} [c + d x])^{5/2}} - \\
& \quad \frac{2 (5 A b^4 - 3 a^4 C - a^2 b^2 (13 A + 5 C)) \tan [c + d x]}{15 a^2 (a^2 - b^2)^2 d (a + b \operatorname{Sec} [c + d x])^{3/2}} - \\
& \quad \left. \frac{2 (41 a^2 A b^4 - 15 A b^6 - 3 a^6 C - 29 a^4 b^2 (2 A + C)) \tan [c + d x]}{15 a^3 (a^2 - b^2)^3 d \sqrt{a + b \operatorname{Sec} [c + d x]}} \right)
\end{aligned}$$

Result (type 4, 2204 leaves):

$$\begin{aligned}
& \left( (b + a \cos [c + d x])^4 \sec [c + d x]^2 (A + C \sec [c + d x])^2 \right. \\
& \quad \left( \frac{4 (58 a^4 A b^2 - 41 a^2 A b^4 + 15 A b^6 + 3 a^6 C + 29 a^4 b^2 C) \sin [c + d x]}{15 a^3 b (-a^2 + b^2)^3} + \right. \\
& \quad \frac{4 (A b^4 \sin [c + d x] + a^2 b^2 C \sin [c + d x])}{5 a^3 (a^2 - b^2) (b + a \cos [c + d x])^3} + \\
& \quad \left. \left. \left( 4 (-19 a^2 A b^3 \sin [c + d x] + 11 A b^5 \sin [c + d x] - 9 a^4 b C \sin [c + d x] + a^2 b^3 C \sin [c + d x]) \right) / \right. \right. \\
& \quad \left. \left. (15 a^3 (a^2 - b^2)^2 (b + a \cos [c + d x])^2) + \right. \right.
\end{aligned}$$



$$\begin{aligned}
 & \left( 4 \left( 74 a^4 A b^2 \sin [c+d x] - 65 a^2 A b^4 \sin [c+d x] + 23 A b^6 \sin [c+d x] + \right. \right. \\
 & \quad \left. \left. 9 a^6 C \sin [c+d x] + 25 a^4 b^2 C \sin [c+d x] - 2 a^2 b^4 C \sin [c+d x] \right) \right) / \\
 & \quad \left( 15 a^3 \left( a^2 - b^2 \right)^3 \left( b + a \cos [c+d x] \right) \right) \Bigg) / \\
 & \left( d \left( A + 2 C + A \cos [2 c + 2 d x] \right) \left( a + b \sec [c+d x] \right)^{7/2} \right) - \\
 & \left( 4 \left( b + a \cos [c+d x] \right)^{7/2} \sec [c+d x]^{3/2} \right. \\
 & \quad \left. \left( A + C \sec [c+d x]^2 \right) \sqrt{\frac{1}{1 - \tan \left[ \frac{1}{2} (c+d x) \right]^2}} \right. \\
 & \quad \left. \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c+d x) \right]^2 + b \tan \left[ \frac{1}{2} (c+d x) \right]^2}{1 + \tan \left[ \frac{1}{2} (c+d x) \right]^2}} \right. \\
 & \quad \left( 58 a^5 A b^2 \tan \left[ \frac{1}{2} (c+d x) \right] + 58 a^4 A b^3 \tan \left[ \frac{1}{2} (c+d x) \right] - 41 a^3 A b^4 \tan \left[ \frac{1}{2} (c+d x) \right] - \right. \\
 & \quad 41 a^2 A b^5 \tan \left[ \frac{1}{2} (c+d x) \right] + 15 a A b^6 \tan \left[ \frac{1}{2} (c+d x) \right] + 15 A b^7 \tan \left[ \frac{1}{2} (c+d x) \right] + \\
 & \quad 3 a^7 C \tan \left[ \frac{1}{2} (c+d x) \right] + 3 a^6 b C \tan \left[ \frac{1}{2} (c+d x) \right] + 29 a^5 b^2 C \tan \left[ \frac{1}{2} (c+d x) \right] + \\
 & \quad 29 a^4 b^3 C \tan \left[ \frac{1}{2} (c+d x) \right] - 116 a^5 A b^2 \tan \left[ \frac{1}{2} (c+d x) \right]^3 + 82 a^3 A b^4 \tan \left[ \frac{1}{2} (c+d x) \right]^3 - \\
 & \quad 30 a A b^6 \tan \left[ \frac{1}{2} (c+d x) \right]^3 - 6 a^7 C \tan \left[ \frac{1}{2} (c+d x) \right]^3 - 58 a^5 b^2 C \tan \left[ \frac{1}{2} (c+d x) \right]^3 + \\
 & \quad 58 a^5 A b^2 \tan \left[ \frac{1}{2} (c+d x) \right]^5 - 58 a^4 A b^3 \tan \left[ \frac{1}{2} (c+d x) \right]^5 - 41 a^3 A b^4 \tan \left[ \frac{1}{2} (c+d x) \right]^5 + \\
 & \quad 41 a^2 A b^5 \tan \left[ \frac{1}{2} (c+d x) \right]^5 + 15 a A b^6 \tan \left[ \frac{1}{2} (c+d x) \right]^5 - 15 A b^7 \tan \left[ \frac{1}{2} (c+d x) \right]^5 + \\
 & \quad 3 a^7 C \tan \left[ \frac{1}{2} (c+d x) \right]^5 - 3 a^6 b C \tan \left[ \frac{1}{2} (c+d x) \right]^5 + 29 a^5 b^2 C \tan \left[ \frac{1}{2} (c+d x) \right]^5 - \\
 & \quad \left. 29 a^4 b^3 C \tan \left[ \frac{1}{2} (c+d x) \right]^5 - 30 a^6 A b \operatorname{EllipticPi} \left[ -1, -\operatorname{ArcSin} \left[ \tan \left[ \frac{1}{2} (c+d x) \right] \right] \right], \frac{a-b}{a+b} \right) \\
 & \quad \sqrt{1 - \tan \left[ \frac{1}{2} (c+d x) \right]^2} \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c+d x) \right]^2 + b \tan \left[ \frac{1}{2} (c+d x) \right]^2}{a + b}} + \\
 & \quad 90 a^4 A b^3 \operatorname{EllipticPi} \left[ -1, -\operatorname{ArcSin} \left[ \tan \left[ \frac{1}{2} (c+d x) \right] \right] \right], \frac{a-b}{a+b} \\
 & \quad \sqrt{1 - \tan \left[ \frac{1}{2} (c+d x) \right]^2} \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c+d x) \right]^2 + b \tan \left[ \frac{1}{2} (c+d x) \right]^2}{a + b}} -
 \end{aligned}$$

$$\begin{aligned}
& 90 a^2 A b^5 \text{EllipticPi}\left[-1, -\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1 - \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& 30 A b^7 \text{EllipticPi}\left[-1, -\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1 - \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 30 a^6 A b \text{EllipticPi}\left[-1, -\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& 90 a^4 A b^3 \text{EllipticPi}\left[-1, -\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 90 a^2 A b^5 \text{EllipticPi}\left[-1, -\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& 30 A b^7 \text{EllipticPi}\left[-1, -\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& (a+b) (-41 a^2 A b^4 + 15 A b^6 + 3 a^6 C + 29 a^4 b^2 (2A+C)) \\
& \text{EllipticE}\left[\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1 - \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \\
& \left(1 + \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& a b (a+b) (-6 a A b^3 + 10 A b^4 + 3 a^4 (5A+C) + 6 a^3 b (5A+4C) + a^2 b^2 (-17A+5C)) \\
& \text{EllipticF}\left[\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1 - \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}
\end{aligned}$$

$$\left( \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)^2 \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} \right) \Bigg/$$

$$\left( 15 a^3 b (a^2 - b^2)^3 d (A + 2 C + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^{7/2} \right.$$

$$\sqrt{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}$$

$$\left. \left( a \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)^2 - b \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right) \right)$$

**Problem 755: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{a^2 - b^2 \sec [c + d x]^2}{\sqrt{a + b \sec [c + d x]}} dx$$

Optimal (type 4, 303 leaves, 7 steps):

$$\frac{1}{d} 2 (a - b) \sqrt{a + b} \cot [c + d x] \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \sec [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right]$$

$$\sqrt{\frac{b (1 - \sec [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \sec [c + d x])}{a - b}} + \frac{1}{d} 2 b \sqrt{a + b} \cot [c + d x]$$

$$\operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \sec [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \sqrt{\frac{b (1 - \sec [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \sec [c + d x])}{a - b}} -$$

$$\frac{1}{d} 2 a \sqrt{a + b} \cot [c + d x] \operatorname{EllipticPi} \left[ \frac{a + b}{a}, \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \sec [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right]$$

$$\sqrt{\frac{b (1 - \sec [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \sec [c + d x])}{a - b}}$$

Result (type 4, 939 leaves):

$$- \left( (4 b \cos [c + d x] (b + a \cos [c + d x]) (a^2 - b^2 \sec [c + d x]^2) \sin [c + d x]) / \right.$$

$$\left. (d (a^2 - 2 b^2 + a^2 \cos [2 c + 2 d x]) \sqrt{a + b \sec [c + d x]}) \right) -$$

$$\left( 4 \sqrt{b + a \cos [c + d x]} (a^2 - b^2 \sec [c + d x]^2) \sqrt{\frac{1}{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \right.$$

$$\begin{aligned}
 & \sqrt{1 - \tan\left[\frac{1}{2}(c + dx)\right]^2} \left( -ab \sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c + dx)\right] \sqrt{1 - \tan\left[\frac{1}{2}(c + dx)\right]^2} - \right. \\
 & b^2 \sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c + dx)\right] \sqrt{1 - \tan\left[\frac{1}{2}(c + dx)\right]^2} + ab \sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c + dx)\right]^3 \\
 & \left. \sqrt{1 - \tan\left[\frac{1}{2}(c + dx)\right]^2} - b^2 \sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c + dx)\right]^3 \sqrt{1 - \tan\left[\frac{1}{2}(c + dx)\right]^2} + \right. \\
 & 2i a^2 \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c + dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c + dx)\right]^2 + b \tan\left[\frac{1}{2}(c + dx)\right]^2}{a+b}} + \\
 & 2i a^2 \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c + dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \tan\left[\frac{1}{2}(c + dx)\right]^2 \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c + dx)\right]^2 + b \tan\left[\frac{1}{2}(c + dx)\right]^2}{a+b}} + \\
 & i(a-b)b \text{EllipticE}\left[i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c + dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \left(1 + \tan\left[\frac{1}{2}(c + dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c + dx)\right]^2 + b \tan\left[\frac{1}{2}(c + dx)\right]^2}{a+b}} - \\
 & i(a^2 - b^2) \text{EllipticF}\left[i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c + dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \left. \left(1 + \tan\left[\frac{1}{2}(c + dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c + dx)\right]^2 + b \tan\left[\frac{1}{2}(c + dx)\right]^2}{a+b}} \right) \right) / \\
 & \left( \sqrt{\frac{-a+b}{a+b}} d (a^2 - 2b^2 + a^2 \cos[2c + 2dx]) \sec[c + dx]^{3/2} \sqrt{a+b \sec[c + dx]} \right. \\
 & \left. \left(1 + \tan\left[\frac{1}{2}(c + dx)\right]^2\right)^{3/2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c + dx)\right]^2 + b \tan\left[\frac{1}{2}(c + dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c + dx)\right]^2}} \right) \right)
 \end{aligned}$$

Problem 757: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{a^2 - b^2 \operatorname{Sec}[c + dx]^2}{(a + b \operatorname{Sec}[c + dx])^{5/2}} dx$$

Optimal (type 4, 338 leaves, 7 steps):

$$\begin{aligned} & \frac{1}{\sqrt{a+b} d} 4 \operatorname{Cot}[c + dx] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c + dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1 - \operatorname{Sec}[c + dx])}{a+b}} \sqrt{-\frac{b(1 + \operatorname{Sec}[c + dx])}{a-b}} - \frac{1}{\sqrt{a+b} d} 4 \operatorname{Cot}[c + dx] \\ & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c + dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1 - \operatorname{Sec}[c + dx])}{a+b}} \sqrt{-\frac{b(1 + \operatorname{Sec}[c + dx])}{a-b}} - \\ & \frac{1}{ad} 2 \sqrt{a+b} \operatorname{Cot}[c + dx] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c + dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1 - \operatorname{Sec}[c + dx])}{a+b}} \sqrt{-\frac{b(1 + \operatorname{Sec}[c + dx])}{a-b}} + \frac{4 b^2 \operatorname{Tan}[c + dx]}{(a^2 - b^2) d \sqrt{a+b \operatorname{Sec}[c + dx]}} \end{aligned}$$

Result (type 4, 790 leaves):

$$\begin{aligned}
& \left( (b + a \cos [c + d x])^2 \sec [c + d x] \right. \\
& \quad \left. (a - b \sec [c + d x]) \left( \frac{4 b \sin [c + d x]}{-a^2 + b^2} - \frac{4 b^2 \sin [c + d x]}{(-a^2 + b^2) (b + a \cos [c + d x])} \right) \right) / \\
& \quad \left( d (-b + a \cos [c + d x]) (a + b \sec [c + d x])^{3/2} \right) + \\
& \quad \left( 2 (b + a \cos [c + d x])^{3/2} \sqrt{\sec [c + d x]} (a - b \sec [c + d x]) \right. \\
& \quad \left( 2 i (a - b) b \operatorname{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a + b}{a - b} \right] \right. \\
& \quad \sqrt{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2} \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \\
& \quad \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} - i (a^2 + 2 a b - 3 b^2) \\
& \quad \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a + b}{a - b} \right] \sqrt{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2} \\
& \quad \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} + 2 i (a^2 - b^2) \\
& \quad \operatorname{EllipticPi} \left[ -\frac{a + b}{a - b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a + b}{a - b} \right] \sqrt{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2} \\
& \quad \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} - \\
& \quad \left. 2 b \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right] \left( b - b \tan \left[ \frac{1}{2} (c + d x) \right]^4 + a \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right)^2 \right) \right) / \\
& \quad \left( \sqrt{\frac{-a + b}{a + b}} (a^2 - b^2) d (-b + a \cos [c + d x]) (a + b \sec [c + d x])^{3/2} \sqrt{\frac{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \right. \\
& \quad \left. \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right]^4 \right) \right)
\end{aligned}$$

**Problem 758: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{a^2 - b^2 \operatorname{Sec}[c + dx]^2}{(a + b \operatorname{Sec}[c + dx])^{7/2}} dx$$

Optimal (type 4, 445 leaves, 8 steps):

$$\left( 2 (11 a^2 - 3 b^2) \operatorname{Cot}[c + dx] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + dx]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \right. \\ \left. \sqrt{\frac{b (1 - \operatorname{Sec}[c + dx])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec}[c + dx])}{a - b}} \right) / (3 a (a - b) (a + b)^{3/2} d) - \\ \left( 2 (9 a^2 - 2 a b - 3 b^2) \operatorname{Cot}[c + dx] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + dx]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \right. \\ \left. \sqrt{\frac{b (1 - \operatorname{Sec}[c + dx])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec}[c + dx])}{a - b}} \right) / (3 a (a - b) (a + b)^{3/2} d) - \\ \frac{1}{a^2 d} 2 \sqrt{a + b} \operatorname{Cot}[c + dx] \operatorname{EllipticPi}\left[\frac{a + b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + dx]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \\ \sqrt{\frac{b (1 - \operatorname{Sec}[c + dx])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec}[c + dx])}{a - b}} + \\ \frac{4 b^2 \operatorname{Tan}[c + dx]}{3 (a^2 - b^2) d (a + b \operatorname{Sec}[c + dx])^{3/2}} + \frac{2 b^2 (11 a^2 - 3 b^2) \operatorname{Tan}[c + dx]}{3 a (a^2 - b^2)^2 d \sqrt{a + b \operatorname{Sec}[c + dx]}}$$

Result (type 4, 1849 leaves):

$$\left( (b + a \operatorname{Cos}[c + dx])^3 \operatorname{Sec}[c + dx]^2 (a - b \operatorname{Sec}[c + dx]) \left( \frac{2 b (-11 a^2 + 3 b^2) \operatorname{Sin}[c + dx]}{3 a (-a^2 + b^2)^2} - \right. \right. \\ \left. \left. \frac{4 b^3 \operatorname{Sin}[c + dx]}{3 a (a^2 - b^2) (b + a \operatorname{Cos}[c + dx])^2} - \frac{2 (-13 a^2 b^2 \operatorname{Sin}[c + dx] + 5 b^4 \operatorname{Sin}[c + dx])}{3 a (a^2 - b^2)^2 (b + a \operatorname{Cos}[c + dx])} \right) \right) / \\ (d (-b + a \operatorname{Cos}[c + dx]) (a + b \operatorname{Sec}[c + dx])^{5/2}) + \left( 2 (b + a \operatorname{Cos}[c + dx])^{5/2} \operatorname{Sec}[c + dx]^{3/2} \right. \\ \left. (a - b \operatorname{Sec}[c + dx]) \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2}} \right)$$

$$\begin{aligned}
& \left( 11 a^3 b \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 11 a^2 b^2 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - \right. \\
& 3 a b^3 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - 3 b^4 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - \\
& 22 a^3 b \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3 + 6 a b^3 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3 + \\
& 11 a^3 b \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 - 11 a^2 b^2 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 - \\
& \left. 3 a b^3 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 + 3 b^4 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 - \right. \\
& 6 i a^4 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
& \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& 12 i a^2 b^2 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
& \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 6 i b^4 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
& \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 6 i a^4 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
& \left. \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + 12 i a^2 b^2 \right)
\end{aligned}$$



$$\begin{aligned}
 & \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 6 i b^4 \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & i b (11 a^3 - 11 a^2 b - 3 a b^2 + 3 b^3) \text{EllipticE}\left[i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \\
 & \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + i (3 a^4 + 9 a^3 b - 17 a^2 b^2 - a b^3 + 6 b^4) \\
 & \text{EllipticF}\left[i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left. \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}}\right) \right) / \\
 & \left(3 a \sqrt{\frac{-a+b}{a+b}} (a^2 - b^2)^2 d (-b + a \cos[c+dx]) (a+b \sec[c+dx])^{5/2} \right. \\
 & \left. \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}} \right. \right. \\
 & \left. \left. \left(a \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) - b \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) \right) \right)
 \end{aligned}$$

Problem 759: Unable to integrate problem.

$$\int \frac{A + C \operatorname{Sec}[c + d x]^2}{\sqrt{\operatorname{Sec}[c + d x]} (a + b \operatorname{Sec}[c + d x])} dx$$

Optimal (type 4, 145 leaves, 8 steps):

$$\frac{2 A \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{a d} - \frac{2 A b \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{a^2 d} + \frac{1}{a^2 (a + b) d} - 2 (A b^2 + a^2 C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticPi}\left[\frac{2 a}{a + b}, \frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}$$

Result (type 8, 37 leaves):

$$\int \frac{A + C \operatorname{Sec}[c + d x]^2}{\sqrt{\operatorname{Sec}[c + d x]} (a + b \operatorname{Sec}[c + d x])} dx$$

**Problem 760: Unable to integrate problem.**

$$\int \frac{A + C \operatorname{Sec}[c + d x]^2}{\sqrt{\operatorname{Sec}[c + d x]} \sqrt{a + b \operatorname{Sec}[c + d x]}} dx$$

Optimal (type 4, 213 leaves, 11 steps):

$$\frac{2 A b \sqrt{\frac{b+a \operatorname{Cos}[c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), \frac{2 a}{a+b}\right] \sqrt{\operatorname{Sec}[c + d x]}}{a d \sqrt{a + b \operatorname{Sec}[c + d x]}} + \frac{2 C \sqrt{\frac{b+a \operatorname{Cos}[c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c + d x), \frac{2 a}{a+b}\right] \sqrt{\operatorname{Sec}[c + d x]}}{d \sqrt{a + b \operatorname{Sec}[c + d x]}} + \frac{2 A \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), \frac{2 a}{a+b}\right] \sqrt{a + b \operatorname{Sec}[c + d x]}}{a d \sqrt{\frac{b+a \operatorname{Cos}[c+d x]}{a+b}} \sqrt{\operatorname{Sec}[c + d x]}}$$

Result (type 8, 39 leaves):

$$\int \frac{A + C \operatorname{Sec}[c + d x]^2}{\sqrt{\operatorname{Sec}[c + d x]} \sqrt{a + b \operatorname{Sec}[c + d x]}} dx$$

**Problem 761: Attempted integration timed out after 120 seconds.**

$$\int (a + b \operatorname{Sec}[c + d x])^{2/3} (A + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 8, 243 leaves, 8 steps):

$$\left( \sqrt{2} (a+b) C \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, -\frac{5}{3}, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sec}[c+dx]), \frac{b(1 - \operatorname{Sec}[c+dx])}{a+b} \right] \right. \\ \left. (a+b \operatorname{Sec}[c+dx])^{2/3} \operatorname{Tan}[c+dx] \right) / \left( b d \sqrt{1 + \operatorname{Sec}[c+dx]} \left( \frac{a+b \operatorname{Sec}[c+dx]}{a+b} \right)^{2/3} \right) - \\ \left( \sqrt{2} a C \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, -\frac{2}{3}, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sec}[c+dx]), \frac{b(1 - \operatorname{Sec}[c+dx])}{a+b} \right] \right. \\ \left. (a+b \operatorname{Sec}[c+dx])^{2/3} \operatorname{Tan}[c+dx] \right) / \\ \left( b d \sqrt{1 + \operatorname{Sec}[c+dx]} \left( \frac{a+b \operatorname{Sec}[c+dx]}{a+b} \right)^{2/3} \right) + A \operatorname{Int} \left[ (a+b \operatorname{Sec}[c+dx])^{2/3}, x \right]$$

Result (type 1, 1 leaves):

???

**Problem 763: Attempted integration timed out after 120 seconds.**

$$\int \frac{A + C \operatorname{Sec}[c+dx]^2}{(a+b \operatorname{Sec}[c+dx])^{1/3}} dx$$

Optimal (type 8, 240 leaves, 8 steps):

$$\left( \sqrt{2} C \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, -\frac{2}{3}, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sec}[c+dx]), \frac{b(1 - \operatorname{Sec}[c+dx])}{a+b} \right] \right. \\ \left. (a+b \operatorname{Sec}[c+dx])^{2/3} \operatorname{Tan}[c+dx] \right) / \left( b d \sqrt{1 + \operatorname{Sec}[c+dx]} \left( \frac{a+b \operatorname{Sec}[c+dx]}{a+b} \right)^{2/3} \right) - \\ \left( \sqrt{2} a C \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{3}, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sec}[c+dx]), \frac{b(1 - \operatorname{Sec}[c+dx])}{a+b} \right] \left( \frac{a+b \operatorname{Sec}[c+dx]}{a+b} \right)^{1/3} \right. \\ \left. \operatorname{Tan}[c+dx] \right) / \left( b d \sqrt{1 + \operatorname{Sec}[c+dx]} (a+b \operatorname{Sec}[c+dx])^{1/3} \right) + A \operatorname{Int} \left[ \frac{1}{(a+b \operatorname{Sec}[c+dx])^{1/3}}, x \right]$$

Result (type 1, 1 leaves):

???

**Problem 766: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c+dx]^2 (a+b \operatorname{Sec}[c+dx]) (B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 3, 114 leaves, 7 steps):

$$\frac{(4aB + 3bC) \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{8d} + \frac{(bB + aC) \operatorname{Tan}[c+dx]}{d} + \\ \frac{(4aB + 3bC) \operatorname{Sec}[c+dx] \operatorname{Tan}[c+dx]}{8d} + \frac{bC \operatorname{Sec}[c+dx]^3 \operatorname{Tan}[c+dx]}{4d} + \frac{(bB + aC) \operatorname{Tan}[c+dx]^3}{3d}$$

Result (type 3, 403 leaves):

$$\begin{aligned}
& - \frac{a B \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right]}{2d} - \frac{3 b C \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right]}{8d} + \\
& \frac{a B \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right]}{2d} + \frac{3 b C \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right]}{8d} + \\
& \frac{16 d \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^4}{3 b C} + \frac{4 d \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^2}{a B} + \\
& \frac{16 d \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^2}{a B} - \frac{16 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^4}{3 b C} - \\
& \frac{4 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^2}{3 b C} - \frac{16 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^2}{a B} + \\
& \frac{2 b B \operatorname{Tan}[c+dx]}{3 d} + \frac{2 a C \operatorname{Tan}[c+dx]}{3 d} + \frac{b B \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx]}{3 d} + \frac{a C \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx]}{3 d}
\end{aligned}$$

**Problem 768: Result more than twice size of optimal antiderivative.**

$$\int (a + b \operatorname{Sec}[c + dx]) (B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) dx$$

Optimal (type 3, 61 leaves, 5 steps):

$$\frac{(2 a B + b C) \operatorname{ArcTanh}[\operatorname{Sin}[c + dx]]}{2 d} + \frac{(b B + a C) \operatorname{Tan}[c + dx]}{d} + \frac{b C \operatorname{Sec}[c + dx] \operatorname{Tan}[c + dx]}{2 d}$$

Result (type 3, 164 leaves):

$$\begin{aligned}
& \frac{1}{4 d} \left( -2 (2 a B + b C) \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right] + \right. \\
& 4 a B \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right] + \\
& 2 b C \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right] + \frac{b C}{\left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^2} - \\
& \left. \frac{b C}{\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^2} + 4 (b B + a C) \operatorname{Tan}[c + dx] \right)
\end{aligned}$$

**Problem 769: Result more than twice size of optimal antiderivative.**

$$\int \cos[c + dx] (a + b \operatorname{Sec}[c + dx]) (B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) dx$$

Optimal (type 3, 35 leaves, 5 steps):

$$a B x + \frac{(b B + a C) \operatorname{ArcTanh}[\operatorname{Sin}[c + dx]]}{d} + \frac{b C \operatorname{Tan}[c + dx]}{d}$$

Result (type 3, 159 leaves):

$$a B x - \frac{b B \operatorname{Log}\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d} - \frac{a C \operatorname{Log}\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d} +$$

$$\frac{b B \operatorname{Log}\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d} + \frac{a C \operatorname{Log}\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d} + \frac{b C \operatorname{Tan}[c + dx]}{d}$$

**Problem 770: Result more than twice size of optimal antiderivative.**

$$\int \cos[c + dx]^2 (a + b \sec[c + dx]) (B \sec[c + dx] + C \sec[c + dx]^2) dx$$

Optimal (type 3, 35 leaves, 4 steps):

$$(b B + a C) x + \frac{b C \operatorname{ArcTanh}[\sin[c + dx]]}{d} + \frac{a B \sin[c + dx]}{d}$$

Result (type 3, 104 leaves):

$$b B x + a C x - \frac{b C \operatorname{Log}\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d} +$$

$$\frac{b C \operatorname{Log}\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d} + \frac{a B \cos[dx] \sin[c]}{d} + \frac{a B \cos[c] \sin[dx]}{d}$$

**Problem 776: Result more than twice size of optimal antiderivative.**

$$\int \sec[c + dx] (a + b \sec[c + dx])^2 (B \sec[c + dx] + C \sec[c + dx]^2) dx$$

Optimal (type 3, 179 leaves, 8 steps):

$$\frac{(8 a b B + 4 a^2 C + 3 b^2 C) \operatorname{ArcTanh}[\sin[c + dx]]}{8 d} +$$

$$\frac{(4 a^2 b B + 4 b^3 B - a^3 C + 8 a b^2 C) \operatorname{Tan}[c + dx]}{6 b d} + \frac{(8 a b B - 2 a^2 C + 9 b^2 C) \sec[c + dx] \operatorname{Tan}[c + dx]}{24 d} +$$

$$\frac{(4 b B - a C) (a + b \sec[c + dx])^2 \operatorname{Tan}[c + dx]}{12 b d} + \frac{C (a + b \sec[c + dx])^3 \operatorname{Tan}[c + dx]}{4 b d}$$

Result (type 3, 457 leaves):

$$\frac{1}{48 d} \left( -6 (8 a b B + 4 a^2 C + 3 b^2 C) \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] + \right. \\
6 (8 a b B + 4 a^2 C + 3 b^2 C) \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] + \\
\frac{3 b^2 C}{\left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^4} + \frac{12 a^2 C + 8 a b (3 B + C) + b^2 (4 B + 9 C)}{\left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2} + \\
\frac{8 b (b B + 2 a C) \sin \left[ \frac{1}{2} (c + d x) \right]}{\left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^3} + \frac{16 (3 a^2 B + 2 b^2 B + 4 a b C) \sin \left[ \frac{1}{2} (c + d x) \right]}{\cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right]} - \\
\frac{3 b^2 C}{\left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^4} + \frac{8 b (b B + 2 a C) \sin \left[ \frac{1}{2} (c + d x) \right]}{\left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^3} - \\
\left. \frac{12 a^2 C + 8 a b (3 B + C) + b^2 (4 B + 9 C)}{\left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2} + \frac{16 (3 a^2 B + 2 b^2 B + 4 a b C) \sin \left[ \frac{1}{2} (c + d x) \right]}{\cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right]} \right)$$

**Problem 778: Result more than twice size of optimal antiderivative.**

$$\int \cos [c + d x] (a + b \operatorname{Sec} [c + d x])^2 (B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) dx$$

Optimal (type 3, 86 leaves, 6 steps):

$$a^2 B x + \frac{(4 a b B + 2 a^2 C + b^2 C) \operatorname{ArcTanh} [\sin [c + d x]]}{2 d} + \\
\frac{b (2 b B + 3 a C) \tan [c + d x]}{2 d} + \frac{b C (a + b \operatorname{Sec} [c + d x]) \tan [c + d x]}{2 d}$$

Result (type 3, 225 leaves):

$$\frac{1}{4 d} \left( 4 a^2 B c + 4 a^2 B d x - 2 (4 a b B + 2 a^2 C + b^2 C) \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] + 8 a b B \right. \\
\operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] + 4 a^2 C \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] + \\
2 b^2 C \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] + \frac{b^2 C}{\left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2} - \\
\left. \frac{b^2 C}{\left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2} + 4 b (b B + 2 a C) \tan [c + d x] \right)$$

**Problem 786: Result more than twice size of optimal antiderivative.**

$$\int (a + b \operatorname{Sec}[c + d x])^3 (B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 3, 180 leaves, 7 steps):

$$\begin{aligned} & \frac{(8 a^3 B + 12 a b^2 B + 12 a^2 b C + 3 b^3 C) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{8 d} + \\ & \frac{(16 a^2 b B + 4 b^3 B + 3 a^3 C + 12 a b^2 C) \operatorname{Tan}[c + d x]}{6 d} + \\ & \frac{b (20 a b B + 6 a^2 C + 9 b^2 C) \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x]}{24 d} + \\ & \frac{(4 b B + 3 a C) (a + b \operatorname{Sec}[c + d x])^2 \operatorname{Tan}[c + d x]}{12 d} + \frac{C (a + b \operatorname{Sec}[c + d x])^3 \operatorname{Tan}[c + d x]}{4 d} \end{aligned}$$

Result (type 3, 639 leaves):

$$\begin{aligned} & \frac{1}{8 d} (-8 a^3 B - 12 a b^2 B - 12 a^2 b C - 3 b^3 C) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + \\ & \frac{1}{8 d} (8 a^3 B + 12 a b^2 B + 12 a^2 b C + 3 b^3 C) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + \\ & \frac{b^3 C}{16 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^4} + \frac{36 a b^2 B + 4 b^3 B + 36 a^2 b C + 12 a b^2 C + 9 b^3 C}{48 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} - \\ & \frac{b^3 C}{16 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^4} + \frac{-36 a b^2 B - 4 b^3 B - 36 a^2 b C - 12 a b^2 C - 9 b^3 C}{48 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} + \\ & \frac{b^3 B \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] + 3 a b^2 C \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]}{6 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^3} + \frac{b^3 B \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] + 3 a b^2 C \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]}{6 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^3} + \\ & \left(9 a^2 b B \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] + 2 b^3 B \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] + 3 a^3 C \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] + \right. \\ & \quad \left. 6 a b^2 C \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right) / \left(3 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)\right) + \\ & \left(9 a^2 b B \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] + 2 b^3 B \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] + 3 a^3 C \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] + \right. \\ & \quad \left. 6 a b^2 C \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right) / \left(3 d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)\right) \end{aligned}$$

**Problem 787: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Cos}[c + d x] (a + b \operatorname{Sec}[c + d x])^3 (B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 3, 137 leaves, 7 steps):

$$a^3 B x + \frac{(6 a^2 b B + b^3 B + 2 a^3 C + 3 a b^2 C) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{2 d} +$$

$$\frac{b (9 a b B + 8 a^2 C + 2 b^2 C) \operatorname{Tan}[c + d x]}{3 d} +$$

$$\frac{b^2 (3 b B + 5 a C) \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x]}{6 d} + \frac{b C (a + b \operatorname{Sec}[c + d x])^2 \operatorname{Tan}[c + d x]}{3 d}$$

Result (type 3, 392 leaves):

$$\frac{1}{12 d} \left( 12 a^3 B (c + d x) - 6 (6 a^2 b B + b^3 B + 2 a^3 C + 3 a b^2 C) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + \right.$$

$$6 (6 a^2 b B + b^3 B + 2 a^3 C + 3 a b^2 C) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] +$$

$$\frac{b^2 (9 a C + b (3 B + C))}{\left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} + \frac{2 b^3 C \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]}{\left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^3} +$$

$$\frac{4 b (9 a b B + 9 a^2 C + 2 b^2 C) \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]}{\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]} + \frac{2 b^3 C \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]}{\left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^3} -$$

$$\left. \frac{b^2 (9 a C + b (3 B + C))}{\left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} + \frac{4 b (9 a b B + 9 a^2 C + 2 b^2 C) \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]}{\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]} \right)$$

**Problem 788: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Cos}[c + d x]^2 (a + b \operatorname{Sec}[c + d x])^3 (B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 3, 131 leaves, 7 steps):

$$a^2 (3 b B + a C) x + \frac{b (6 a b B + 6 a^2 C + b^2 C) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{2 d} +$$

$$\frac{a B (a + b \operatorname{Sec}[c + d x])^2 \operatorname{Sin}[c + d x]}{d} - \frac{b (2 a^2 B - b^2 B - 3 a b C) \operatorname{Tan}[c + d x]}{d} -$$

$$\frac{b^2 (2 a B - b C) \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x]}{2 d}$$

Result (type 3, 277 leaves):



$$\frac{1}{4d} \left( 4a^2(3bB+aC)(c+dx) - 2b(6abB+6a^2C+b^2C) \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right] + \right. \\ \left. 2b(6abB+6a^2C+b^2C) \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right] + \right. \\ \left. \frac{b^3C}{\left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^2} + \frac{4b^2(bB+3aC)\sin\left[\frac{1}{2}(c+dx)\right]}{\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]} - \right. \\ \left. \frac{b^3C}{\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^2} + \frac{4b^2(bB+3aC)\sin\left[\frac{1}{2}(c+dx)\right]}{\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]} + 4a^3B\sin[c+dx] \right)$$

**Problem 793: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec[c+dx]^3 (B \sec[c+dx] + C \sec[c+dx]^2)}{a + b \sec[c+dx]} dx$$

Optimal (type 3, 187 leaves, 9 steps):

$$\frac{(2a^2 + b^2)(bB - aC) \operatorname{ArcTanh}[\sin[c+dx]]}{2b^4d} - \\ \frac{2a^3(bB - aC) \operatorname{ArcTanh}\left[\frac{\sqrt{a-b} \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a+b}}\right]}{\sqrt{a-b} b^4 \sqrt{a+b} d} - \frac{(3abB - 3a^2C - 2b^2C) \tan[c+dx]}{3b^3d} + \\ \frac{(bB - aC) \sec[c+dx] \tan[c+dx]}{2b^2d} + \frac{C \sec[c+dx]^2 \tan[c+dx]}{3bd}$$

Result (type 3, 422 leaves):

$$\frac{1}{12 b^4 d} \left( \frac{24 a^3 (b B - a C) \operatorname{ArcTanh} \left[ \frac{(-a+b) \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{\sqrt{a^2-b^2}} \right]}{\sqrt{a^2-b^2}} + \right.$$

$$6 (2 a^2 + b^2) (-b B + a C) \operatorname{Log} \left[ \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right] - \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right] \right] -$$

$$6 (2 a^2 + b^2) (-b B + a C) \operatorname{Log} \left[ \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right] + \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right] \right] +$$

$$\frac{b^2 (-3 a C + b (3 B + C))}{\left( \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right] - \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right] \right)^2} + \frac{2 b^3 C \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right]}{\left( \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right] - \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right] \right)^3} +$$

$$\frac{4 b (-3 a b B + 3 a^2 C + 2 b^2 C) \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right]}{\operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right] - \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right]} + \frac{2 b^3 C \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right]}{\left( \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right] + \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right] \right)^3} -$$

$$\left. \frac{b^2 (-3 a C + b (3 B + C))}{\left( \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right] + \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right] \right)^2} + \frac{4 b (-3 a b B + 3 a^2 C + 2 b^2 C) \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right]}{\operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right] + \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right]} \right)$$

**Problem 794: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c+d x]^2 (B \operatorname{Sec}[c+d x] + C \operatorname{Sec}[c+d x]^2)}{a+b \operatorname{Sec}[c+d x]} dx$$

Optimal (type 3, 143 leaves, 8 steps):

$$- \frac{(2 a b B - 2 a^2 C - b^2 C) \operatorname{ArcTanh}[\operatorname{Sin}[c+d x]]}{2 b^3 d} +$$

$$\frac{2 a^2 (b B - a C) \operatorname{ArcTanh} \left[ \frac{\sqrt{a-b} \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{\sqrt{a+b}} \right]}{\sqrt{a-b} b^3 \sqrt{a+b} d} + \frac{(b B - a C) \operatorname{Tan}[c+d x]}{b^2 d} + \frac{C \operatorname{Sec}[c+d x] \operatorname{Tan}[c+d x]}{2 b d}$$

Result (type 3, 300 leaves):

$$\frac{1}{4 b^3 d} \left( \frac{8 a^2 (-b B + a C) \operatorname{ArcTanh} \left[ \frac{(-a+b) \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{\sqrt{a^2-b^2}} \right]}{\sqrt{a^2-b^2}} - \right.$$

$$2 (-2 a b B + 2 a^2 C + b^2 C) \operatorname{Log} \left[ \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right] - \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right] \right] +$$

$$2 (-2 a b B + 2 a^2 C + b^2 C) \operatorname{Log} \left[ \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right] + \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right] \right] +$$

$$\frac{b^2 C}{\left( \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right] - \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right] \right)^2} + \frac{4 b (b B - a C) \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right]}{\operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right] - \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right]} -$$

$$\left. \frac{b^2 C}{\left( \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right] + \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right] \right)^2} + \frac{4 b (b B - a C) \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right]}{\operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right] + \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right]} \right)$$

**Problem 814: Attempted integration timed out after 120 seconds.**

$$\int \operatorname{Sec}[c+d x]^3 \sqrt{a+b \operatorname{Sec}[c+d x]} (B \operatorname{Sec}[c+d x] + C \operatorname{Sec}[c+d x]^2) dx$$

Optimal (type 4, 485 leaves, 8 steps):

$$-\frac{1}{315 b^5 d} 2 (a-b) \sqrt{a+b} (24 a^3 b B + 57 a b^3 B - 16 a^4 C - 24 a^2 b^2 C + 147 b^4 C)$$

$$\operatorname{Cot}[c+d x] \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}} \right], \frac{a+b}{a-b} \right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \frac{1}{315 b^4 d}$$

$$2 (a-b) \sqrt{a+b} (3 b^3 (25 B - 49 C) + 18 a b^2 (B - 2 C) + 12 a^2 b (2 B - C) - 16 a^3 C) \operatorname{Cot}[c+d x]$$

$$\operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}} \right], \frac{a+b}{a-b} \right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} -$$

$$\frac{1}{315 b^3 d} 2 (12 a^2 b B - 75 b^3 B - 8 a^3 C - 13 a b^2 C) \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x] +$$

$$\frac{1}{315 b^2 d} 2 (9 a b B - 6 a^2 C + 49 b^2 C) \operatorname{Sec}[c+d x] \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x] +$$

$$\frac{2 (9 b B + a C) \operatorname{Sec}[c+d x]^2 \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x]}{63 b d} +$$

$$\frac{2 C \operatorname{Sec}[c+d x]^3 \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x]}{9 d}$$

Result (type 1, 1 leaves):

???

**Problem 815: Attempted integration timed out after 120 seconds.**

$$\int \sec [c+d x]^2 \sqrt{a+b \sec [c+d x]} (B \sec [c+d x]+C \sec [c+d x]^2) d x$$

Optimal (type 4, 397 leaves, 7 steps):

$$\frac{1}{105 b^4 d} 2 (a-b) \sqrt{a+b} (14 a^2 b B-63 b^3 B-8 a^3 C-19 a b^2 C) \cot [c+d x]$$

$$\text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} +$$

$$\frac{1}{105 b^3 d} 2 (a-b) \sqrt{a+b} (b^2 (63 B-25 C)+2 a b (7 B-3 C)-8 a^2 C) \cot [c+d x]$$

$$\text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} +$$

$$\frac{2(7 a b B-4 a^2 C+25 b^2 C) \sqrt{a+b \sec [c+d x]} \tan [c+d x]}{105 b^2 d} +$$

$$\frac{2(7 b B+a C) \sec [c+d x] \sqrt{a+b \sec [c+d x]} \tan [c+d x]}{35 b d} +$$

$$\frac{2 C \sec [c+d x]^2 \sqrt{a+b \sec [c+d x]} \tan [c+d x]}{7 d}$$

Result (type 1, 1 leaves):

???

**Problem 816: Unable to integrate problem.**

$$\int \sec [c+d x] \sqrt{a+b \sec [c+d x]} (B \sec [c+d x]+C \sec [c+d x]^2) d x$$

Optimal (type 4, 314 leaves, 6 steps):

$$\begin{aligned}
 & -\frac{1}{15 b^3 d} 2 (a-b) \sqrt{a+b} (5 a b B - 2 a^2 C + 9 b^2 C) \\
 & \quad \text{Cot}[c+d x] \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \text{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \quad \sqrt{\frac{b(1-\text{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\text{Sec}[c+d x])}{a-b}} - \frac{1}{15 b^2 d} \\
 & 2 (a-b) \sqrt{a+b} (5 b B - 2 a C - 9 b C) \text{Cot}[c+d x] \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \text{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \quad \sqrt{\frac{b(1-\text{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\text{Sec}[c+d x])}{a-b}} + \\
 & \quad \frac{2(5 b B - 2 a C) \sqrt{a+b \text{Sec}[c+d x]} \text{Tan}[c+d x]}{15 b d} + \frac{2 C (a+b \text{Sec}[c+d x])^{3/2} \text{Tan}[c+d x]}{5 b d}
 \end{aligned}$$

Result (type 8, 42 leaves):

$$\int \text{Sec}[c+d x] \sqrt{a+b \text{Sec}[c+d x]} (B \text{Sec}[c+d x] + C \text{Sec}[c+d x]^2) dx$$

**Problem 817: Attempted integration timed out after 120 seconds.**

$$\int \sqrt{a+b \text{Sec}[c+d x]} (B \text{Sec}[c+d x] + C \text{Sec}[c+d x]^2) dx$$

Optimal (type 4, 256 leaves, 5 steps):

$$\begin{aligned}
 & -\frac{1}{3 b^2 d} 2 (a-b) \sqrt{a+b} (3 b B + a C) \text{Cot}[c+d x] \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \text{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \quad \sqrt{\frac{b(1-\text{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\text{Sec}[c+d x])}{a-b}} + \frac{1}{3 b d} \\
 & 2 (a-b) \sqrt{a+b} (3 B - C) \text{Cot}[c+d x] \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \text{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \quad \sqrt{\frac{b(1-\text{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\text{Sec}[c+d x])}{a-b}} + \frac{2 C \sqrt{a+b \text{Sec}[c+d x]} \text{Tan}[c+d x]}{3 d}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 818: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \cos [c+d x] \sqrt{a+b \sec [c+d x]} (B \sec [c+d x]+C \sec [c+d x]^2) d x$$

Optimal (type 4, 320 leaves, 6 steps):

$$-\frac{1}{b d} 2(a-b) \sqrt{a+b} C \cot [c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{1}{b d}$$

$$2 \sqrt{a+b}(b(B-C)+a C) \cot [c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} - \frac{1}{d}$$

$$2 \sqrt{a+b} B \cot [c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}}$$

Result (type 4, 863 leaves):

$$\frac{2 C \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{d} +$$

$$\left(2 \sqrt{a+b \sec [c+d x]} \left(a \sqrt{\frac{-a+b}{a+b}} C \tan \left[\frac{1}{2}(c+d x)\right] + b \sqrt{\frac{-a+b}{a+b}} C \tan \left[\frac{1}{2}(c+d x)\right] -\right.\right.$$

$$\left.2 a \sqrt{\frac{-a+b}{a+b}} C \tan \left[\frac{1}{2}(c+d x)\right]^3 + a \sqrt{\frac{-a+b}{a+b}} C \tan \left[\frac{1}{2}(c+d x)\right]^5 - b \sqrt{\frac{-a+b}{a+b}} C\right.$$

$$\left.\tan \left[\frac{1}{2}(c+d x)\right]^5 + 2 i a B \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan \left[\frac{1}{2}(c+d x)\right]\right],\right.\right.$$

$$\left.\frac{a+b}{a-b}\right] \sqrt{1-\tan \left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \tan \left[\frac{1}{2}(c+d x)\right]^2+b \tan \left[\frac{1}{2}(c+d x)\right]^2}{a+b}} +$$

$$2 i a B \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan \left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right] \tan \left[\frac{1}{2}(c+d x)\right]^2$$

$$\begin{aligned}
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & i(a-b) \operatorname{CEllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - i(a-b) \\
 & (B-C) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) / \\
 & \left( \sqrt{\frac{-a+b}{a+b}} d \sqrt{b+a \cos[c+dx]} \sqrt{\sec[c+dx]} \sqrt{\frac{1}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}} \right. \\
 & \left. \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^{3/2} \right. \\
 & \left. \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}} \right)
 \end{aligned}$$

**Problem 819: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \cos[c+dx]^2 \sqrt{a+b \sec[c+dx]} (B \sec[c+dx] + C \sec[c+dx]^2) dx$$

Optimal (type 4, 344 leaves, 7 steps):

$$\frac{1}{b d} (a-b) \sqrt{a+b} B \operatorname{Cot}[c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \frac{1}{d} \sqrt{a+b} (B+2 C) \operatorname{Cot}[c+d x]$$

$$\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}}$$

$$\frac{1}{a d} \sqrt{a+b} (b B+2 a C) \operatorname{Cot}[c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \frac{B \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{d}$$

Result(type 4, 1107 leaves):

$$\left( \sqrt{a+b \operatorname{Sec}[c+d x]} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}} \right.$$

$$\left. \left( a \sqrt{\frac{-a+b}{a+b}} B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + b \sqrt{\frac{-a+b}{a+b}} B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] - 2 a \sqrt{\frac{-a+b}{a+b}} B \right.$$

$$\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 + a \sqrt{\frac{-a+b}{a+b}} B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - b \sqrt{\frac{-a+b}{a+b}} B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 -$$

$$2 i b B \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}}$$

$$4 i a C \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}}$$

$$2 i b B \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right]$$



$$\begin{aligned}
 & \tan\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \\
 & 4 \operatorname{Im} a C \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, \operatorname{Im} \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \\
 & \operatorname{Im}(a-b) B \operatorname{EllipticE}\left[\operatorname{Im} \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + 2 \operatorname{Im}(a-b) \\
 & C \operatorname{EllipticF}\left[\operatorname{Im} \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \Bigg/ \\
 & \left( \sqrt{\frac{-a+b}{a+b}} d \sqrt{b+a \cos[c+dx]} \sqrt{\sec[c+dx]} \sqrt{\frac{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}} \right. \\
 & \left. \left( b - b \tan\left[\frac{1}{2}(c+dx)\right]^4 + a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) \right)
 \end{aligned}$$

**Problem 820: Result more than twice size of optimal antiderivative.**

$$\int \cos[c+dx]^3 \sqrt{a+b \sec[c+dx]} (B \sec[c+dx] + C \sec[c+dx]^2) dx$$

Optimal (type 4, 429 leaves, 8 steps):

$$\frac{1}{4 a b d} (a-b) \sqrt{a+b} (b B+4 a C) \operatorname{Cot}[c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \frac{1}{4 a d}$$

$$\sqrt{a+b} (b B+2 a(B+2 C)) \operatorname{Cot}[c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \frac{1}{4 a^2 d}$$

$$\sqrt{a+b} (4 a^2 B-b^2 B+4 a b C) \operatorname{Cot}[c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} +$$

$$\frac{(b B+4 a C) \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{4 a d} + \frac{B \operatorname{Cos}[c+d x] \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{2 d}$$

Result (type 4, 1161 leaves):

$$\frac{B \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[2(c+d x)]}{4 d} +$$

$$\left(\sqrt{a+b \operatorname{Sec}[c+d x]} \sqrt{\frac{1}{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}} \left(a b B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + b^2 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] +\right.\right.$$

$$4 a^2 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + 4 a b C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] - 2 a b B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 - 8 a^2 C$$

$$\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 + a b B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - b^2 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + 4 a^2 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 -$$

$$4 a b C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - 8 a^2 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right]$$

$$\sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} +$$

$$2 b^2 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}$$

$$\sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} -$$

$$8 a b C \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right]$$

$$\begin{aligned}
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 8 a^2 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & 2 b^2 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 8 a b C \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & (a+b)(bB+4aC) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 2 a (2 a B - b B + 4 b C) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left. \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \right) / \\
 & \left(4 a d \sqrt{b+a \operatorname{Cos}[c+dx]} \sqrt{\operatorname{Sec}[c+dx]} \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^{3/2} \right. \\
 & \left. \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}} \right)
 \end{aligned}$$

Problem 821: Attempted integration timed out after 120 seconds.

$$\int \text{Sec}[c + d x]^3 (a + b \text{Sec}[c + d x])^{3/2} (B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) dx$$

Optimal (type 4, 573 leaves, 9 steps):

$$\begin{aligned}
 & -\frac{1}{3465 b^5 d} 2 (a - b) \sqrt{a + b} (88 a^4 b B + 363 a^2 b^3 B + 1617 b^5 B - 48 a^5 C - 108 a^3 b^2 C + 2088 a b^4 C) \\
 & \quad \text{Cot}[c + d x] \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \\
 & \quad \sqrt{\frac{b(1 - \text{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \text{Sec}[c + d x])}{a - b}} - \frac{1}{3465 b^4 d} 2 (a - b) \sqrt{a + b} \\
 & \quad (3 a b^3 (143 B - 471 C) - 3 b^4 (539 B - 225 C) + 6 a^2 b^2 (11 B - 24 C) + 4 a^3 b (22 B - 9 C) - 48 a^4 C) \\
 & \quad \text{Cot}[c + d x] \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \\
 & \quad \sqrt{\frac{b(1 - \text{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \text{Sec}[c + d x])}{a - b}} + \frac{1}{3465 b^3 d} \\
 & \quad 2 (88 a^3 b B + 429 a b^3 B - 48 a^4 C - 144 a^2 b^2 C + 675 b^4 C) \sqrt{a + b \text{Sec}[c + d x]} \text{Tan}[c + d x] + \\
 & \quad \frac{1}{3465 b^3 d} 2 (88 a^2 b B + 539 b^3 B - 48 a^3 C - 204 a b^2 C) (a + b \text{Sec}[c + d x])^{3/2} \text{Tan}[c + d x] - \\
 & \quad \frac{2 (44 a b B - 24 a^2 C - 81 b^2 C) (a + b \text{Sec}[c + d x])^{5/2} \text{Tan}[c + d x]}{693 b^3 d} + \\
 & \quad \frac{2 (11 b B - 6 a C) \text{Sec}[c + d x] (a + b \text{Sec}[c + d x])^{5/2} \text{Tan}[c + d x]}{99 b^2 d} + \\
 & \quad \frac{2 C \text{Sec}[c + d x]^2 (a + b \text{Sec}[c + d x])^{5/2} \text{Tan}[c + d x]}{11 b d}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 822: Attempted integration timed out after 120 seconds.**

$$\int \text{Sec}[c + d x]^2 (a + b \text{Sec}[c + d x])^{3/2} (B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) dx$$

Optimal (type 4, 475 leaves, 8 steps):

$$\begin{aligned}
 & \frac{1}{315 b^4 d} 2 (a-b) \sqrt{a+b} (18 a^3 b B - 246 a b^3 B - 8 a^4 C - 33 a^2 b^2 C - 147 b^4 C) \\
 & \text{Cot}[c+d x] \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \text{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1-\text{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\text{Sec}[c+d x])}{a-b}} - \frac{1}{315 b^3 d} \\
 & 2(a-b) \sqrt{a+b} (3 b^3 (25 B - 49 C) - 3 a b^2 (57 B - 13 C) - 6 a^2 b (3 B - C) + 8 a^3 C) \text{Cot}[c+d x] \\
 & \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \text{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\text{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\text{Sec}[c+d x])}{a-b}} - \\
 & \frac{1}{315 b^2 d} 2 (18 a^2 b B - 75 b^3 B - 8 a^3 C - 39 a b^2 C) \sqrt{a+b \text{Sec}[c+d x]} \text{Tan}[c+d x] - \\
 & \frac{2 (18 a b B - 8 a^2 C - 49 b^2 C) (a+b \text{Sec}[c+d x])^{3/2} \text{Tan}[c+d x]}{315 b^2 d} + \\
 & \frac{2 (9 b B - 4 a C) (a+b \text{Sec}[c+d x])^{5/2} \text{Tan}[c+d x]}{63 b^2 d} + \\
 & \frac{2 C \text{Sec}[c+d x] (a+b \text{Sec}[c+d x])^{5/2} \text{Tan}[c+d x]}{9 b d}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 823: Attempted integration timed out after 120 seconds.**

$$\int \text{Sec}[c+d x] (a+b \text{Sec}[c+d x])^{3/2} (B \text{Sec}[c+d x] + C \text{Sec}[c+d x]^2) dx$$

Optimal (type 4, 387 leaves, 7 steps):

$$\begin{aligned}
& -\frac{1}{105 b^3 d} 2 (a-b) \sqrt{a+b} (21 a^2 b B + 63 b^3 B - 6 a^3 C + 82 a b^2 C) \\
& \quad \text{Cot}[c+d x] \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \text{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
& \quad \sqrt{\frac{b(1-\text{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\text{Sec}[c+d x])}{a-b}} - \frac{1}{105 b^2 d} \\
& 2 (a-b) \sqrt{a+b} (a b (21 B - 57 C) - b^2 (63 B - 25 C) - 6 a^2 C) \text{Cot}[c+d x] \\
& \quad \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \text{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\text{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\text{Sec}[c+d x])}{a-b}} + \\
& \quad \frac{2 (21 a b B - 6 a^2 C + 25 b^2 C) \sqrt{a+b \text{Sec}[c+d x]} \text{Tan}[c+d x]}{105 b d} + \\
& \quad \frac{2 (7 b B - 2 a C) (a+b \text{Sec}[c+d x])^{3/2} \text{Tan}[c+d x]}{35 b d} + \frac{2 C (a+b \text{Sec}[c+d x])^{5/2} \text{Tan}[c+d x]}{7 b d}
\end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 824: Attempted integration timed out after 120 seconds.**

$$\int (a+b \text{Sec}[c+d x])^{3/2} (B \text{Sec}[c+d x] + C \text{Sec}[c+d x]^2) dx$$

Optimal (type 4, 312 leaves, 6 steps):

$$\begin{aligned}
& -\frac{1}{15 b^2 d} 2 (a-b) \sqrt{a+b} (20 a b B + 3 a^2 C + 9 b^2 C) \text{Cot}[c+d x] \text{EllipticE}\left[ \right. \\
& \quad \text{ArcSin}\left[\frac{\sqrt{a+b \text{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\text{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\text{Sec}[c+d x])}{a-b}} + \\
& \quad \frac{1}{15 b d} 2 (a-b) \sqrt{a+b} (15 a B - 5 b B - 3 a C + 9 b C) \text{Cot}[c+d x] \\
& \quad \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \text{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\text{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\text{Sec}[c+d x])}{a-b}} + \\
& \quad \frac{2 (5 b B + 3 a C) \sqrt{a+b \text{Sec}[c+d x]} \text{Tan}[c+d x]}{15 d} + \frac{2 C (a+b \text{Sec}[c+d x])^{3/2} \text{Tan}[c+d x]}{5 d}
\end{aligned}$$

Result (type 1, 1 leaves):

???

### Problem 826: Result more than twice size of optimal antiderivative.

$$\int \cos [c+d x]^2 (a+b \sec [c+d x])^{3/2} (B \sec [c+d x]+C \sec [c+d x]^2) d x$$

Optimal (type 4, 361 leaves, 7 steps):

$$\begin{aligned} & \frac{1}{b d} (a-b) \sqrt{a+b} (a B-2 b C) \cot [c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{1}{d} \sqrt{a+b} (2 b(B-C)+a(B+4 C)) \cot [c+d x] \\ & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} - \\ & \frac{1}{d} \sqrt{a+b} (3 b B+2 a C) \cot [c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{a B \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{d} \end{aligned}$$

Result (type 4, 979 leaves):

$$\begin{aligned} & \frac{2 b C \cos [c+d x] (a+b \sec [c+d x])^{3/2} \sin [c+d x]}{d (b+a \cos [c+d x])} + \\ & \left( (a+b \sec [c+d x])^{3/2} \sqrt{\frac{1}{1-\tan \left[\frac{1}{2}(c+d x)\right]^2}} \right. \\ & \left. \left( a^2 B \tan \left[\frac{1}{2}(c+d x)\right] + a b B \tan \left[\frac{1}{2}(c+d x)\right] - 2 a b C \tan \left[\frac{1}{2}(c+d x)\right] - \right. \right. \\ & \left. \left. 2 b^2 C \tan \left[\frac{1}{2}(c+d x)\right] - 2 a^2 B \tan \left[\frac{1}{2}(c+d x)\right]^3 + 4 a b C \tan \left[\frac{1}{2}(c+d x)\right]^3 + \right. \right. \\ & \left. \left. a^2 B \tan \left[\frac{1}{2}(c+d x)\right]^5 - a b B \tan \left[\frac{1}{2}(c+d x)\right]^5 - 2 a b C \tan \left[\frac{1}{2}(c+d x)\right]^5 + \right. \right. \\ & \left. \left. 2 b^2 C \tan \left[\frac{1}{2}(c+d x)\right]^5 - 6 a b B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan \left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \right. \right. \\ & \left. \left. \sqrt{1-\tan \left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \tan \left[\frac{1}{2}(c+d x)\right]^2+b \tan \left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \right. \right. \\ & \left. \left. 4 a^2 C \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan \left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\tan \left[\frac{1}{2}(c+d x)\right]^2} \right) \end{aligned}$$

$$\begin{aligned}
& \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 6 a b B \operatorname{EllipticPi}\left[-1,-\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 4 a^2 C \operatorname{EllipticPi}\left[-1,-\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& (a+b)(a B-2 b C) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} \\
& \left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 2(2 a b(B-C)+a^2 C-b^2(B+C)) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} \left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \\
& \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \Bigg) \Bigg) / \\
& \left(d(b+a \cos[c+dx])^{3/2} \sec[c+dx]^{3/2} \left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^{3/2}\right. \\
& \left.\sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}}\right)
\end{aligned}$$

**Problem 827: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \cos[c+dx]^3 (a+b \sec[c+dx])^{3/2} (B \sec[c+dx]+C \sec[c+dx]^2) dx$$

Optimal (type 4, 428 leaves, 8 steps):



$$\frac{1}{4 b d} (a-b) \sqrt{a+b} (5 b B+4 a C) \operatorname{Cot}[c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{1}{4 d}$$

$$\sqrt{a+b} (2 a B+5 b B+4 a C+8 b C) \operatorname{Cot}[c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} - \frac{1}{4 a d} \sqrt{a+b} (4 a^2 B+3 b^2 B+12 a b C)$$

$$\operatorname{Cot}[c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} +$$

$$\frac{(5 b B+4 a C) \sqrt{a+b \sec [c+d x]} \operatorname{Sin}[c+d x]}{4 d} + \frac{a B \operatorname{Cos}[c+d x] \sqrt{a+b \sec [c+d x]} \operatorname{Sin}[c+d x]}{2 d}$$

Result (type 4, 1580 leaves):

$$\frac{a B \sqrt{a+b \sec [c+d x]} \operatorname{Sin}[2(c+d x)]}{4 d} -$$

$$\left(\sqrt{a+b \sec [c+d x]}\right) \left(5 a b \sqrt{\frac{-a+b}{a+b}} B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + 5 b^2 \sqrt{\frac{-a+b}{a+b}} B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] +\right.$$

$$4 a^2 \sqrt{\frac{-a+b}{a+b}} C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + 4 a b \sqrt{\frac{-a+b}{a+b}} C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] -$$

$$10 a b \sqrt{\frac{-a+b}{a+b}} B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 - 8 a^2 \sqrt{\frac{-a+b}{a+b}} C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 +$$

$$5 a b \sqrt{\frac{-a+b}{a+b}} B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - 5 b^2 \sqrt{\frac{-a+b}{a+b}} B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 +$$

$$4 a^2 \sqrt{\frac{-a+b}{a+b}} C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - 4 a b \sqrt{\frac{-a+b}{a+b}} C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 -$$

$$8 a^2 B \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right]$$

$$\begin{aligned}
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 6 \, i \, b^2 \, B \, \text{EllipticPi}\left[-\frac{a+b}{a-b}, \, i \, \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \, \frac{a+b}{a-b}\right] \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 24 \, i \, a \, b \, C \, \text{EllipticPi}\left[-\frac{a+b}{a-b}, \, i \, \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \, \frac{a+b}{a-b}\right] \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 8 \, i \, a^2 \, B \, \text{EllipticPi}\left[-\frac{a+b}{a-b}, \, i \, \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \, \frac{a+b}{a-b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 6 \, i \, b^2 \, B \, \text{EllipticPi}\left[-\frac{a+b}{a-b}, \, i \, \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \, \frac{a+b}{a-b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - 24 \, i \, a \, b \, C \\
& \text{EllipticPi}\left[-\frac{a+b}{a-b}, \, i \, \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \, \frac{a+b}{a-b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& i \, (a-b) \, (5 \, b \, B + 4 \, a \, C) \, \text{EllipticE}\left[i \, \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \, \frac{a+b}{a-b}\right] \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)
\end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + 2i(a-b)(2aB+b(B+4C)) \\
 & \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \Bigg) / \\
 & \left(4 \sqrt{\frac{-a+b}{a+b}} d \sqrt{b+a \operatorname{Cos}[c+dx]} \sqrt{\operatorname{Sec}[c+dx]} \sqrt{\frac{1}{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \right. \\
 & \left. \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^{3/2} \right. \\
 & \left. \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \right)
 \end{aligned}$$

**Problem 828: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Cos}[c+dx]^4 (a+b \operatorname{Sec}[c+dx])^{3/2} (B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 4, 520 leaves, 9 steps):

$$\frac{1}{24 a b d} (a-b) \sqrt{a+b} (16 a^2 B + 3 b^2 B + 30 a b C) \operatorname{Cot}[c+d x]$$

$$\operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} +$$

$$\frac{1}{24 a d} \sqrt{a+b} (16 a^2 B + 14 a b B + 3 b^2 B + 12 a^2 C + 30 a b C) \operatorname{Cot}[c+d x]$$

$$\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} -$$

$$\frac{1}{8 a^2 d} \sqrt{a+b} (12 a^2 b B - b^3 B + 8 a^3 C + 6 a b^2 C) \operatorname{Cot}[c+d x]$$

$$\operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}}$$

$$\sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \frac{(16 a^2 B + 3 b^2 B + 30 a b C) \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{24 a d} +$$

$$\frac{(7 b B + 6 a C) \operatorname{Cos}[c+d x] \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{12 d} +$$

$$\frac{a B \operatorname{Cos}[c+d x]^2 \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{3 d}$$

Result (type 4, 1532 leaves):

$$\frac{1}{d} \sqrt{a+b \operatorname{Sec}[c+d x]}$$

$$\left( \frac{1}{12} a B \operatorname{Sin}[c+d x] + \frac{1}{24} (7 b B + 6 a C) \operatorname{Sin}[2(c+d x)] + \frac{1}{12} a B \operatorname{Sin}[3(c+d x)] \right) +$$

$$\left( \sqrt{a+b \operatorname{Sec}[c+d x]} \sqrt{\frac{1}{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}} \left( 16 a^3 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + 16 a^2 b B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + \right. \right.$$

$$3 a b^2 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + 3 b^3 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + 30 a^2 b C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] +$$

$$30 a b^2 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 - 32 a^3 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 - 6 a b^2 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 -$$

$$60 a^2 b C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 + 16 a^3 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - 16 a^2 b B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 +$$

$$3 a b^2 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - 3 b^3 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + 30 a^2 b C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 -$$

$$30 a b^2 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - 72 a^2 b B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right]$$

$$\left. \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \right.$$

$$\begin{aligned}
 & 6 b^3 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 48 a^3 C \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 36 a b^2 C \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 72 a^2 b B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & 6 b^3 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 48 a^3 C \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 36 a b^2 C \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & (a+b) (16 a^2 B+3 b^2 B+30 a b C) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)
 \end{aligned}$$

$$\sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}}$$

$$2 a\left(a b(26 B-6 C)+12 a^2 C+b^2(-7 B+24 C)\right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right]$$

$$\sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)$$

$$\sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}}\right) /$$

$$\left(24 a d \sqrt{b+a \operatorname{Cos}[c+dx]} \sqrt{\operatorname{Sec}[c+dx]}\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^{3/2}\right.$$

$$\left.\sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}}\right)$$

**Problem 829: Attempted integration timed out after 120 seconds.**

$$\int \operatorname{Sec}[c+dx]^2 (a+b \operatorname{Sec}[c+dx])^{5/2} (B \operatorname{Sec}[c+dx]+C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 4, 565 leaves, 9 steps):

$$\begin{aligned}
 & \frac{1}{3465 b^4 d} 2 (a-b) \sqrt{a+b} (110 a^4 b B - 3069 a^2 b^3 B - 1617 b^5 B - 40 a^5 C - 255 a^3 b^2 C - 3705 a b^4 C) \\
 & \cot [c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} - \frac{1}{3465 b^3 d} 2 (a-b) \sqrt{a+b} \\
 & (6 a b^3 (209 B - 505 C) - 3 b^4 (539 B - 225 C) - a^3 b (110 B - 30 C) - 15 a^2 b^2 (121 B - 19 C) + 40 a^4 C) \\
 & \cot [c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} - \frac{1}{3465 b^2 d} \\
 & 2 (110 a^3 b B - 1254 a b^3 B - 40 a^4 C - 285 a^2 b^2 C - 675 b^4 C) \sqrt{a+b \sec [c+d x]} \tan [c+d x] - \\
 & \frac{1}{3465 b^2 d} 2 (110 a^2 b B - 539 b^3 B - 40 a^3 C - 335 a b^2 C) (a+b \sec [c+d x])^{3/2} \tan [c+d x] - \\
 & \frac{2 (22 a b B - 8 a^2 C - 81 b^2 C) (a+b \sec [c+d x])^{5/2} \tan [c+d x]}{693 b^2 d} + \\
 & \frac{2 (11 b B - 4 a C) (a+b \sec [c+d x])^{7/2} \tan [c+d x]}{99 b^2 d} + \\
 & \frac{2 C \sec [c+d x] (a+b \sec [c+d x])^{7/2} \tan [c+d x]}{11 b d}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 830: Attempted integration timed out after 120 seconds.**

$$\int \sec [c+d x] (a+b \sec [c+d x])^{5/2} (B \sec [c+d x] + C \sec [c+d x]^2) dx$$

Optimal (type 4, 469 leaves, 8 steps):

$$\begin{aligned}
& -\frac{1}{315 b^3 d} 2 (a-b) \sqrt{a+b} (45 a^3 b B + 435 a b^3 B - 10 a^4 C + 279 a^2 b^2 C + 147 b^4 C) \\
& \quad \text{Cot}[c+d x] \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \text{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
& \quad \sqrt{\frac{b(1-\text{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\text{Sec}[c+d x])}{a-b}} - \frac{1}{315 b^2 d} \\
& 2 (a-b) \sqrt{a+b} (3 b^3 (25 B - 49 C) - 6 a b^2 (60 B - 19 C) + 15 a^2 b (3 B - 11 C) - 10 a^3 C) \text{Cot}[c+d x] \\
& \quad \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \text{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\text{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\text{Sec}[c+d x])}{a-b}} + \\
& \quad \frac{1}{315 b d} 2 (45 a^2 b B + 75 b^3 B - 10 a^3 C + 114 a b^2 C) \sqrt{a+b \text{Sec}[c+d x]} \text{Tan}[c+d x] + \\
& \quad \frac{2 (45 a b B - 10 a^2 C + 49 b^2 C) (a+b \text{Sec}[c+d x])^{3/2} \text{Tan}[c+d x]}{315 b d} + \\
& \quad \frac{2 (9 b B - 2 a C) (a+b \text{Sec}[c+d x])^{5/2} \text{Tan}[c+d x]}{63 b d} + \frac{2 C (a+b \text{Sec}[c+d x])^{7/2} \text{Tan}[c+d x]}{9 b d}
\end{aligned}$$

Result (type 1, 1 leaves):

???

### Problem 831: Attempted integration timed out after 120 seconds.

$$\int (a+b \text{Sec}[c+d x])^{5/2} (B \text{Sec}[c+d x] + C \text{Sec}[c+d x]^2) dx$$

Optimal (type 4, 384 leaves, 7 steps):

$$\begin{aligned}
& -\frac{1}{105 b^2 d} 2 (a-b) \sqrt{a+b} (161 a^2 b B + 63 b^3 B + 15 a^3 C + 145 a b^2 C) \\
& \quad \text{Cot}[c+d x] \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \text{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
& \quad \sqrt{\frac{b(1-\text{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\text{Sec}[c+d x])}{a-b}} + \frac{1}{105 b d} \\
& 2 (a-b) \sqrt{a+b} (b^2 (63 B - 25 C) - 8 a b (7 B - 15 C) + 15 a^2 (7 B - C)) \text{Cot}[c+d x] \\
& \quad \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \text{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\text{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\text{Sec}[c+d x])}{a-b}} + \\
& \quad \frac{2 (56 a b B + 15 a^2 C + 25 b^2 C) \sqrt{a+b \text{Sec}[c+d x]} \text{Tan}[c+d x]}{105 d} + \\
& \quad \frac{2 (7 b B + 5 a C) (a+b \text{Sec}[c+d x])^{3/2} \text{Tan}[c+d x]}{35 d} + \frac{2 C (a+b \text{Sec}[c+d x])^{5/2} \text{Tan}[c+d x]}{7 d}
\end{aligned}$$

Result (type 1, 1 leaves):



???

### Problem 833: Result more than twice size of optimal antiderivative.

$$\int \cos [c + d x]^2 (a + b \sec [c + d x])^{5/2} (B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 4, 433 leaves, 8 steps):

$$\begin{aligned} & \frac{1}{3 b d} (a - b) \sqrt{a + b} (3 a^2 B - 6 b^2 B - 14 a b C) \cot [c + d x] \\ & \text{EllipticE} \left[ \text{ArcSin} \left[ \frac{\sqrt{a + b \sec [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \sqrt{\frac{b (1 - \sec [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \sec [c + d x])}{a - b}} + \\ & \frac{1}{3 d} \sqrt{a + b} (2 a b (9 B - 7 C) - 2 b^2 (3 B - C) + 3 a^2 (B + 6 C)) \cot [c + d x] \\ & \text{EllipticF} \left[ \text{ArcSin} \left[ \frac{\sqrt{a + b \sec [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \sqrt{\frac{b (1 - \sec [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \sec [c + d x])}{a - b}} - \\ & \frac{1}{d} a \sqrt{a + b} (5 b B + 2 a C) \cot [c + d x] \text{EllipticPi} \left[ \frac{a + b}{a}, \text{ArcSin} \left[ \frac{\sqrt{a + b \sec [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \\ & \sqrt{\frac{b (1 - \sec [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \sec [c + d x])}{a - b}} + \\ & \frac{a B (a + b \sec [c + d x])^{3/2} \sin [c + d x]}{d} - \frac{b (3 a B - 2 b C) \sqrt{a + b \sec [c + d x]} \tan [c + d x]}{3 d} \end{aligned}$$

Result (type 4, 1146 leaves):

$$\begin{aligned} & \left( (a + b \sec [c + d x])^{5/2} \sqrt{\frac{1}{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \right. \\ & \left( 3 a^3 B \tan \left[ \frac{1}{2} (c + d x) \right] + 3 a^2 b B \tan \left[ \frac{1}{2} (c + d x) \right] - 6 a b^2 B \tan \left[ \frac{1}{2} (c + d x) \right] - \right. \\ & 6 b^3 B \tan \left[ \frac{1}{2} (c + d x) \right] - 14 a^2 b C \tan \left[ \frac{1}{2} (c + d x) \right] - 14 a b^2 C \tan \left[ \frac{1}{2} (c + d x) \right] - \\ & 6 a^3 B \tan \left[ \frac{1}{2} (c + d x) \right]^3 + 12 a b^2 B \tan \left[ \frac{1}{2} (c + d x) \right]^3 + 28 a^2 b C \tan \left[ \frac{1}{2} (c + d x) \right]^3 + \\ & 3 a^3 B \tan \left[ \frac{1}{2} (c + d x) \right]^5 - 3 a^2 b B \tan \left[ \frac{1}{2} (c + d x) \right]^5 - 6 a b^2 B \tan \left[ \frac{1}{2} (c + d x) \right]^5 + \\ & 6 b^3 B \tan \left[ \frac{1}{2} (c + d x) \right]^5 - 14 a^2 b C \tan \left[ \frac{1}{2} (c + d x) \right]^5 + 14 a b^2 C \tan \left[ \frac{1}{2} (c + d x) \right]^5 - \\ & \left. \left. 30 a^2 b B \text{EllipticPi} \left[ -1, -\text{ArcSin} \left[ \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a - b}{a + b} \right] \right) \right) \end{aligned}$$

$$\begin{aligned}
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 12 a^3 C \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 30 a^2 b B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 12 a^3 C \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& (a+b) (3 a^2 B - 6 b^2 B - 14 a b C) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \\
& \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 2 (9 a^2 b (B - C) + 3 a^3 C - b^3 (3 B + C) - a b^2 (9 B + 7 C)) \\
& \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
& \left. \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \right) / \\
& \left( 3 d (b + a \cos[c+dx])^{5/2} \sec[c+dx]^{5/2} \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^{3/2} \right. \\
& \left. \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}} \right) +
\end{aligned}$$

$$\frac{\left( \cos [c+d x]^2 (a+b \sec [c+d x])^{5/2} \left( \frac{2}{3} b (3 b B+7 a C) \sin [c+d x] + \frac{2}{3} b^2 C \tan [c+d x] \right) \right)}{\left( d (b+a \cos [c+d x])^2 \right)}$$

### Problem 834: Result more than twice size of optimal antiderivative.

$$\int \cos [c+d x]^3 (a+b \sec [c+d x])^{5/2} (B \sec [c+d x]+C \sec [c+d x]^2) dx$$

Optimal (type 4, 450 leaves, 8 steps):

$$\frac{1}{4 b d} (a-b) \sqrt{a+b} (9 a b B+4 a^2 C-8 b^2 C) \cot [c+d x]$$

$$\text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} +$$

$$\frac{1}{4 d} \sqrt{a+b} (8 b^2 (B-C)+2 a^2 (B+2 C)+3 a b (3 B+8 C)) \cot [c+d x]$$

$$\text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} -$$

$$\frac{1}{4 d} \sqrt{a+b} (4 a^2 B+15 b^2 B+20 a b C) \cot [c+d x]$$

$$\text{EllipticPi}\left[\frac{a+b}{a}, \text{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec [c+d x])}{a+b}}$$

$$\sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{a(7 b B+4 a C) \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{4 d} +$$

$$\frac{a B \cos [c+d x] (a+b \sec [c+d x])^{3/2} \sin [c+d x]}{2 d}$$

Result (type 4, 1338 leaves):

$$\left( \cos [c+d x]^2 (a+b \sec [c+d x])^{5/2} \left( 2 b^2 C \sin [c+d x] + \frac{1}{4} a^2 B \sin [2(c+d x)] \right) \right) /$$

$$\left( d (b+a \cos [c+d x])^2 \right) + \left( (a+b \sec [c+d x])^{5/2} \sqrt{\frac{1}{1-\tan \left[ \frac{1}{2}(c+d x) \right]^2}} \right)$$

$$\left( 9 a^2 b B \tan \left[ \frac{1}{2}(c+d x) \right] + 9 a b^2 B \tan \left[ \frac{1}{2}(c+d x) \right] + 4 a^3 C \tan \left[ \frac{1}{2}(c+d x) \right] + \right.$$

$$\left. 4 a^2 b C \tan \left[ \frac{1}{2}(c+d x) \right] - 8 a b^2 C \tan \left[ \frac{1}{2}(c+d x) \right] - 8 b^3 C \tan \left[ \frac{1}{2}(c+d x) \right] - \right)$$

$$\begin{aligned}
& 18 a^2 b B \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3 - 8 a^3 C \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3 + 16 a b^2 C \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3 + \\
& 9 a^2 b B \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 - 9 a b^2 B \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 + 4 a^3 C \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 - \\
& 4 a^2 b C \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 - 8 a b^2 C \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 + 8 b^3 C \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 - \\
& 8 a^3 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 30 a b^2 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 40 a^2 b C \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 8 a^3 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 30 a b^2 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 40 a^2 b C \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& (a+b) (9 a b B + 4 a^2 C - 8 b^2 C) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)
\end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \\
 & 2\left(2a^3B-a^2b(B-12C)+12ab^2(B-C)-4b^3(B+C)\right) \\
 & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \\
 & \left(4d(b+a \operatorname{Cos}[c+dx])^{5/2} \operatorname{Sec}[c+dx]^{5/2} \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^{3/2} \right. \\
 & \left. \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}}\right)
 \end{aligned}$$

**Problem 835: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Cos}[c+dx]^4 (a+b \operatorname{Sec}[c+dx])^{5/2} (B \operatorname{Sec}[c+dx]+C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 4, 518 leaves, 9 steps):

$$\frac{1}{24 b d} (a-b) \sqrt{a+b} (16 a^2 B + 33 b^2 B + 54 a b C) \operatorname{Cot}[c+d x]$$

$$\operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} +$$

$$\frac{1}{24 d} \sqrt{a+b} (4 a^2 (4 B+3 C) + 3 b^2 (11 B+16 C) + a b (26 B+54 C)) \operatorname{Cot}[c+d x]$$

$$\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} -$$

$$\frac{1}{8 a d} \sqrt{a+b} (20 a^2 b B + 5 b^3 B + 8 a^3 C + 30 a b^2 C) \operatorname{Cot}[c+d x]$$

$$\operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}}$$

$$\sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \frac{(16 a^2 B + 33 b^2 B + 54 a b C) \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{24 d} +$$

$$\frac{a(3 b B + 2 a C) \operatorname{Cos}[c+d x] \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{4 d} +$$

$$\frac{a B \operatorname{Cos}[c+d x]^2 (a+b \operatorname{Sec}[c+d x])^{3/2} \operatorname{Sin}[c+d x]}{3 d}$$

Result (type 4, 1546 leaves):

$$\frac{1}{d} \sqrt{a+b \operatorname{Sec}[c+d x]}$$

$$\left( \frac{1}{12} a^2 B \operatorname{Sin}[c+d x] + \frac{1}{24} a (13 b B + 6 a C) \operatorname{Sin}[2(c+d x)] + \frac{1}{12} a^2 B \operatorname{Sin}[3(c+d x)] \right) +$$

$$\left( \sqrt{a+b \operatorname{Sec}[c+d x]} \sqrt{\frac{1}{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}} \left( 16 a^3 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + 16 a^2 b B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + \right. \right.$$

$$33 a b^2 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + 33 b^3 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + 54 a^2 b C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] +$$

$$54 a b^2 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] - 32 a^3 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 - 66 a b^2 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 -$$

$$108 a^2 b C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 + 16 a^3 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - 16 a^2 b B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 +$$

$$33 a b^2 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - 33 b^3 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + 54 a^2 b C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 -$$

$$54 a b^2 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - 120 a^2 b B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right]$$

$$\left. \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \right)$$

$$\begin{aligned}
 & 30 b^3 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 48 a^3 C \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 180 a b^2 C \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 120 a^2 b B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 30 b^3 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 48 a^3 C \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 180 a b^2 C \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & (a+b) (16 a^2 B + 33 b^2 B + 54 a b C) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)
 \end{aligned}$$

$$\sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}}$$

$$2\left(a^2 b(38 B-6 C)+24 b^3(B-C)+12 a^3 C+a b^2(-13 B+72 C)\right)$$

$$\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}$$

$$\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \Bigg/$$

$$\left(24 d \sqrt{b+a \operatorname{Cos}[c+dx]} \sqrt{\operatorname{Sec}[c+dx]} \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^{3/2}\right.$$

$$\left.\sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}}\right)$$

**Problem 837: Attempted integration timed out after 120 seconds.**

$$\int \frac{\operatorname{Sec}[c+dx]^3 (B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2)}{\sqrt{a+b \operatorname{Sec}[c+dx]}} dx$$

Optimal (type 4, 411 leaves, 7 steps):

$$-\frac{1}{105 b^5 d} 2(a-b) \sqrt{a+b} (56 a^2 b B + 63 b^3 B - 48 a^3 C - 44 a b^2 C)$$

$$\operatorname{Cot}[c+dx] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}} - \frac{1}{105 b^4 d}$$

$$2 \sqrt{a+b} (b^3(63 B-25 C) - 48 a^3 C + 4 a^2 b(14 B+3 C) - 2 a b^2(7 B+22 C)) \operatorname{Cot}[c+dx]$$

$$\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}}$$

$$-\frac{2(28 a b B - 24 a^2 C - 25 b^2 C) \sqrt{a+b \operatorname{Sec}[c+dx]} \operatorname{Tan}[c+dx]}{105 b^3 d} +$$

$$\frac{2(7 b B - 6 a C) \operatorname{Sec}[c+dx] \sqrt{a+b \operatorname{Sec}[c+dx]} \operatorname{Tan}[c+dx]}{35 b^2 d} +$$

$$\frac{2 C \operatorname{Sec}[c+dx]^2 \sqrt{a+b \operatorname{Sec}[c+dx]} \operatorname{Tan}[c+dx]}{7 b d}$$



Result (type 1, 1 leaves):

???

### Problem 838: Unable to integrate problem.

$$\int \frac{\sec [c+d x]^2 (B \sec [c+d x]+C \sec [c+d x]^2)}{\sqrt{a+b \sec [c+d x]}} d x$$

Optimal (type 4, 329 leaves, 6 steps):

$$\begin{aligned} & \frac{1}{15 b^4 d} 2 (a-b) \sqrt{a+b} (10 a b B-8 a^2 C-9 b^2 C) \cot [c+d x] \\ & \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \\ & \frac{1}{15 b^3 d} 2 \sqrt{a+b} (b^2(5 B-9 C)-8 a^2 C+2 a b(5 B+C)) \cot [c+d x] \\ & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \\ & \frac{2(5 b B-4 a C) \sqrt{a+b \sec [c+d x]} \tan [c+d x]}{15 b^2 d} + \frac{2 C \sec [c+d x] \sqrt{a+b \sec [c+d x]} \tan [c+d x]}{5 b d} \end{aligned}$$

Result (type 8, 44 leaves):

$$\int \frac{\sec [c+d x]^2 (B \sec [c+d x]+C \sec [c+d x]^2)}{\sqrt{a+b \sec [c+d x]}} d x$$

### Problem 839: Attempted integration timed out after 120 seconds.

$$\int \frac{\sec [c+d x] (B \sec [c+d x]+C \sec [c+d x]^2)}{\sqrt{a+b \sec [c+d x]}} d x$$

Optimal (type 4, 261 leaves, 5 steps):

$$\begin{aligned} & -\frac{1}{3 b^3 d} 2 (a-b) \sqrt{a+b} (3 b B-2 a C) \cot [c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} - \frac{1}{3 b^2 d} \\ & 2 \sqrt{a+b} (3 b B-2 a C-b C) \cot [c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{2 C \sqrt{a+b \sec [c+d x]} \tan [c+d x]}{3 b d} \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 840: Unable to integrate problem.**

$$\int \frac{B \sec [c + d x] + C \sec [c + d x]^2}{\sqrt{a + b \sec [c + d x]}} dx$$

Optimal (type 4, 210 leaves, 4 steps):

$$-\frac{1}{b^2 d} 2 (a - b) \sqrt{a + b} C \cot [c + d x] \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \sec [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right]$$

$$\sqrt{\frac{b (1 - \sec [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \sec [c + d x])}{a - b}} + \frac{1}{b d}$$

$$2 \sqrt{a + b} (B - C) \cot [c + d x] \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \sec [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right]$$

$$\sqrt{\frac{b (1 - \sec [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \sec [c + d x])}{a - b}}$$

Result (type 8, 36 leaves):

$$\int \frac{B \sec [c + d x] + C \sec [c + d x]^2}{\sqrt{a + b \sec [c + d x]}} dx$$

**Problem 842: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\cos [c + d x]^2 (B \sec [c + d x] + C \sec [c + d x]^2)}{\sqrt{a + b \sec [c + d x]}} dx$$

Optimal (type 4, 348 leaves, 7 steps):

$$\frac{1}{abd} (a-b) \sqrt{a+b} B \cot[c+dx] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\sec[c+dx])}{a+b}} \sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} + \frac{1}{ad} \sqrt{a+b} B \cot[c+dx]$$

$$\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec[c+dx])}{a+b}} \sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} +$$

$$\frac{1}{a^2 d} \sqrt{a+b} (bB-2aC) \cot[c+dx] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\sec[c+dx])}{a+b}} \sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} + \frac{B \sqrt{a+b \sec[c+dx]} \sin[c+dx]}{ad}$$

Result(type 4, 1027 leaves):

$$\left( \sqrt{b+a \cos[c+dx]} \sqrt{\sec[c+dx]} \sqrt{\frac{1}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}} \right.$$

$$\left. \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} \left( a \sqrt{\frac{-a+b}{a+b}} B \tan\left[\frac{1}{2}(c+dx)\right] \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} + \right. \right.$$

$$\left. b \sqrt{\frac{-a+b}{a+b}} B \tan\left[\frac{1}{2}(c+dx)\right] \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} - a \sqrt{\frac{-a+b}{a+b}} B \tan\left[\frac{1}{2}(c+dx)\right]^3 \right.$$

$$\left. \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} + b \sqrt{\frac{-a+b}{a+b}} B \tan\left[\frac{1}{2}(c+dx)\right]^3 \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} + \right.$$

$$\left. 2 i b B \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \right.$$

$$\left. \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \right.$$

$$\left. 4 i a C \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \right.$$

$$\left. \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \right.$$

$$\begin{aligned}
& 2 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
& \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 4 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
& \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& \operatorname{EllipticE}\left[\operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
& \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 2 \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
& \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \Bigg) \Bigg/ \\
& \left( a \sqrt{\frac{-a+b}{a+b}} d \sqrt{a+b \operatorname{Sec}[c+dx]} \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^{3/2} \right. \\
& \left. \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \right)
\end{aligned}$$

**Problem 843: Attempted integration timed out after 120 seconds.**

$$\int \frac{\operatorname{Sec}[c+dx]^3 (B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2)}{(a+b \operatorname{Sec}[c+dx])^{3/2}} dx$$

Optimal (type 4, 471 leaves, 7 steps):

$$\frac{1}{15 b^5 \sqrt{a+b} d} 2 (40 a^3 b B - 25 a b^3 B - 48 a^4 C + 24 a^2 b^2 C + 9 b^4 C) \operatorname{Cot}[c+d x]$$

$$\operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} +$$

$$\frac{1}{15 b^4 \sqrt{a+b} d} 2 (b^3 (5 B - 9 C) + 4 a^2 b (10 B - 9 C) + 6 a b^2 (5 B - 2 C) - 48 a^3 C) \operatorname{Cot}[c+d x]$$

$$\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} +$$

$$\frac{2 a (b B - a C) \operatorname{Sec}[c+d x]^2 \operatorname{Tan}[c+d x]}{b (a^2 - b^2) d \sqrt{a+b \operatorname{Sec}[c+d x]}} + \frac{1}{15 b^3 (a^2 - b^2) d}$$

$$2 (20 a^2 b B - 5 b^3 B - 24 a^3 C + 9 a b^2 C) \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x] -$$

$$\frac{2 (5 a b B - 6 a^2 C + b^2 C) \operatorname{Sec}[c+d x] \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x]}{5 b^2 (a^2 - b^2) d}$$

Result(type 1, 1 leaves):

???

**Problem 844: Attempted integration timed out after 120 seconds.**

$$\int \frac{\operatorname{Sec}[c+d x]^2 (B \operatorname{Sec}[c+d x] + C \operatorname{Sec}[c+d x]^2)}{(a+b \operatorname{Sec}[c+d x])^{3/2}} dx$$

Optimal (type 4, 329 leaves, 6 steps):

$$-\frac{1}{3 b^4 \sqrt{a+b} d}$$

$$2 (6 a^2 b B - 3 b^3 B - 8 a^3 C + 5 a b^2 C) \operatorname{Cot}[c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \frac{1}{3 b^3 \sqrt{a+b} d}$$

$$2 (2 a+b) (3 b B - 4 a C - b C) \operatorname{Cot}[c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} -$$

$$\frac{2 a^2 (b B - a C) \operatorname{Tan}[c+d x]}{b^2 (a^2 - b^2) d \sqrt{a+b \operatorname{Sec}[c+d x]}} + \frac{2 C \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x]}{3 b^2 d}$$

Result(type 1, 1 leaves):

???

**Problem 845: Attempted integration timed out after 120 seconds.**

$$\int \frac{\sec [c+d x] (B \sec [c+d x]+C \sec [c+d x]^2)}{(a+b \sec [c+d x])^{3 / 2}} d x$$

Optimal (type 4, 275 leaves, 5 steps):

$$\frac{1}{b^3 \sqrt{a+b} d} 2 (a b B-2 a^2 C+b^2 C) \cot [c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{1}{b^2 \sqrt{a+b} d}$$

$$2(b(B-C)-2 a C) \cot [c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{2 a(b B-a C) \tan [c+d x]}{b\left(a^2-b^2\right) d \sqrt{a+b \sec [c+d x]}}$$

Result (type 1, 1 leaves):

???

**Problem 846: Attempted integration timed out after 120 seconds.**

$$\int \frac{B \sec [c+d x]+C \sec [c+d x]^2}{(a+b \sec [c+d x])^{3 / 2}} d x$$

Optimal (type 4, 254 leaves, 5 steps):

$$-\frac{1}{b^2 \sqrt{a+b} d} 2(b B-a C) \cot [c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{1}{b \sqrt{a+b} d}$$

$$2(B+C) \cot [c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} - \frac{2(b B-a C) \tan [c+d x]}{\left(a^2-b^2\right) d \sqrt{a+b \sec [c+d x]}}$$

Result (type 1, 1 leaves):

???

**Problem 847: Result unnecessarily involves complex numbers and more than**

twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x] \left( B \sec [c+d x]+C \sec [c+d x]^2 \right)}{\left( a+b \sec [c+d x] \right)^{3 / 2}} d x$$

Optimal (type 4, 376 leaves, 7 steps):

$$\begin{aligned} & \frac{1}{a b \sqrt{a+b} d} 2 (b B-a C) \cot [c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} - \frac{1}{a b \sqrt{a+b} d} 2 (b B-a C) \cot [c+d x] \\ & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} - \\ & \frac{1}{a^2 d} 2 \sqrt{a+b} B \cot [c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{2 b(b B-a C) \tan [c+d x]}{a\left(a^2-b^2\right) d \sqrt{a+b \sec [c+d x]}} \end{aligned}$$

Result (type 4, 1445 leaves):

$$\begin{aligned} & \left( (b+a \cos [c+d x]) \sec [c+d x] \right. \\ & \left. \left( \frac{2(-b B+a C) \sin [c+d x]}{a\left(a^2-b^2\right)} - \frac{2\left(-b^2 B \sin [c+d x]+a b C \sin [c+d x]\right)}{a\left(a^2-b^2\right)(b+a \cos [c+d x])} \right) \right) / \left( d \sqrt{a+b \sec [c+d x]} \right) + \\ & \left( 2 \sqrt{b+a \cos [c+d x]} \sqrt{\sec [c+d x]} \sqrt{\frac{a+b-a \tan \left[\frac{1}{2}(c+d x)\right]^2+b \tan \left[\frac{1}{2}(c+d x)\right]^2}{1+\tan \left[\frac{1}{2}(c+d x)\right]^2}} \right. \\ & \left( a b \sqrt{\frac{-a+b}{a+b}} B \tan \left[\frac{1}{2}(c+d x)\right] + b^2 \sqrt{\frac{-a+b}{a+b}} B \tan \left[\frac{1}{2}(c+d x)\right] - \right. \\ & a^2 \sqrt{\frac{-a+b}{a+b}} C \tan \left[\frac{1}{2}(c+d x)\right] - a b \sqrt{\frac{-a+b}{a+b}} C \tan \left[\frac{1}{2}(c+d x)\right] - \\ & 2 a b \sqrt{\frac{-a+b}{a+b}} B \tan \left[\frac{1}{2}(c+d x)\right]^3 + 2 a^2 \sqrt{\frac{-a+b}{a+b}} C \tan \left[\frac{1}{2}(c+d x)\right]^3 + \\ & \left. a b \sqrt{\frac{-a+b}{a+b}} B \tan \left[\frac{1}{2}(c+d x)\right]^5 - b^2 \sqrt{\frac{-a+b}{a+b}} B \tan \left[\frac{1}{2}(c+d x)\right]^5 - \right. \end{aligned}$$

$$\begin{aligned}
& a^2 \sqrt{\frac{-a+b}{a+b}} C \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 + a b \sqrt{\frac{-a+b}{a+b}} C \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 - \\
& 2 i a^2 B \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
& \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& 2 i b^2 B \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
& \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 2 i a^2 B \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& 2 i b^2 B \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& i (a-b) (-b B + a C) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
& \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \\
& \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + i (a-b) (2 b B + a (B-C)) \\
& \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}
\end{aligned}$$



$$\left( \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right] \right)^2 \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \right) /$$

$$\left( a \sqrt{\frac{-a+b}{a+b}} (a^2 - b^2) d \sqrt{a+b \sec[c+dx]} \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right] \right)^2 \right.$$

$$\left. \sqrt{\frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}} \left( a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right] \right)^2 - b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right] \right)^2 \right) \right)$$

**Problem 848: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c+dx]^2 (B \sec[c+dx] + C \sec[c+dx]^2)}{(a+b \sec[c+dx])^{3/2}} dx$$

Optimal (type 4, 427 leaves, 8 steps):

$$\frac{1}{a^2 b \sqrt{a+b} d} (a^2 B - 3 b^2 B + 2 a b C) \cot[c+dx] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\sec[c+dx])}{a+b}} \sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} + \frac{1}{a^2 \sqrt{a+b} d}$$

$$(3 b B + a (B - 2 C)) \cot[c+dx] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\sec[c+dx])}{a+b}} \sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} + \frac{1}{a^3 d}$$

$$\sqrt{a+b} (3 b B - 2 a C) \cot[c+dx] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\sec[c+dx])}{a+b}} \sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} +$$

$$\frac{B \sin[c+dx]}{a d \sqrt{a+b \sec[c+dx]}} + \frac{b (a^2 B - 3 b^2 B + 2 a b C) \tan[c+dx]}{a^2 (a^2 - b^2) d \sqrt{a+b \sec[c+dx]}}$$

Result (type 4, 1613 leaves):

$$\left( (b+a \cos[c+dx])^2 \sec[c+dx]^2 \right.$$

$$\left. \left( -\frac{2 b (b B - a C) \sin[c+dx]}{a^2 (-a^2 + b^2)} + \frac{2 (-b^3 B \sin[c+dx] + a b^2 C \sin[c+dx])}{a^2 (a^2 - b^2) (b+a \cos[c+dx])} \right) \right) /$$

$$\begin{aligned}
& \left( d (a + b \operatorname{Sec}[c + d x])^{3/2} \right) - \left( (b + a \operatorname{Cos}[c + d x])^{3/2} \operatorname{Sec}[c + d x]^{3/2} \right. \\
& \sqrt{\frac{1}{1 - \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}} \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}} \\
& \left( a^3 B \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] + a^2 b B \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] - 3 a b^2 B \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] - \right. \\
& 3 b^3 B \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] + 2 a^2 b C \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] + 2 a b^2 C \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] - \\
& 2 a^3 B \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^3 + 6 a b^2 B \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^3 - 4 a^2 b C \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^3 + \\
& a^3 B \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^5 - a^2 b B \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^5 - 3 a b^2 B \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^5 + \\
& 3 b^3 B \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^5 + 2 a^2 b C \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^5 - 2 a b^2 C \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^5 + \\
& \left. 6 a^2 b B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right], \frac{a - b}{a + b}\right] \right. \\
& \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2} \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{a + b}} - \\
& 6 b^3 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right], \frac{a - b}{a + b}\right] \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2} \\
& \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{a + b}} - \\
& 4 a^3 C \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right], \frac{a - b}{a + b}\right] \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2} \\
& \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{a + b}} + \\
& 4 a b^2 C \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right], \frac{a - b}{a + b}\right] \\
& \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2} \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{a + b}} + \\
& \left. 6 a^2 b B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right], \frac{a - b}{a + b}\right] \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 \right)
\end{aligned}$$

$$\begin{aligned}
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 6 b^3 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 4 a^3 C \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & 4 a b^2 C \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + (a+b) \\
 & (a^2 B - 3 b^2 B + 2 a b C) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 2 a (a+b) (-b B + a C) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) / \\
 & \left( a^2 (a^2 - b^2) d (a+b \operatorname{Sec}[c+dx])^{3/2} \sqrt{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} \right. \\
 & \left. \left( a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right)
 \end{aligned}$$

**Problem 849: Attempted integration timed out after 120 seconds.**

$$\int \frac{\operatorname{Sec}[c+dx]^3 (B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2)}{(a+b \operatorname{Sec}[c+dx])^{5/2}} dx$$

Optimal (type 4, 509 leaves, 7 steps):

$$\begin{aligned}
 & - \left( 2 \left( 8 a^4 b B - 15 a^2 b^3 B + 3 b^5 B - 16 a^5 C + 28 a^3 b^2 C - 8 a b^4 C \right) \right. \\
 & \quad \left. \operatorname{Cot}[c + d x] \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \right. \\
 & \quad \left. \sqrt{\frac{b(1 - \operatorname{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \operatorname{Sec}[c + d x])}{a - b}} \right) / \left( 3(a - b) b^5 (a + b)^{3/2} d \right) - \\
 & \left( 2 \left( a^3 b (8 B - 12 C) - 9 a b^3 (B - C) - b^4 (3 B - C) - 16 a^4 C + 2 a^2 b^2 (3 B + 8 C) \right) \right. \\
 & \quad \left. \operatorname{Cot}[c + d x] \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \right. \\
 & \quad \left. \sqrt{\frac{b(1 - \operatorname{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \operatorname{Sec}[c + d x])}{a - b}} \right) / \\
 & \quad \left( 3 b^4 \sqrt{a + b} (a^2 - b^2) d \right) + \frac{2 a (b B - a C) \operatorname{Sec}[c + d x]^2 \operatorname{Tan}[c + d x]}{3 b (a^2 - b^2) d (a + b \operatorname{Sec}[c + d x])^{3/2}} - \\
 & \quad \frac{2 a^2 (3 a^2 b B - 7 b^3 B - 6 a^3 C + 10 a b^2 C) \operatorname{Tan}[c + d x]}{3 b^3 (a^2 - b^2)^2 d \sqrt{a + b \operatorname{Sec}[c + d x]}} - \\
 & \quad \frac{2 (a b B - 2 a^2 C + b^2 C) \sqrt{a + b \operatorname{Sec}[c + d x]} \operatorname{Tan}[c + d x]}{3 b^3 (a^2 - b^2) d}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 850: Attempted integration timed out after 120 seconds.**

$$\int \frac{\operatorname{Sec}[c + d x]^2 (B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{(a + b \operatorname{Sec}[c + d x])^{5/2}} dx$$

Optimal (type 4, 417 leaves, 6 steps):

$$\left( 2 (2 a^3 b B - 6 a b^3 B - 8 a^4 C + 15 a^2 b^2 C - 3 b^4 C) \right.$$

$$\left. \text{Cot}[c + d x] \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \right.$$

$$\left. \sqrt{\frac{b (1 - \text{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b (1 + \text{Sec}[c + d x])}{a - b}} \right) / (3 (a - b) b^4 (a + b)^{3/2} d) +$$

$$\left( 2 (2 a^2 b (B - 3 C) - 3 b^3 (B - C) - 8 a^3 C + 3 a b^2 (B + 3 C)) \text{Cot}[c + d x] \text{EllipticF}\left[ \right. \right.$$

$$\left. \left. \text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \sqrt{\frac{b (1 - \text{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b (1 + \text{Sec}[c + d x])}{a - b}} \right) /$$

$$\left( 3 b^3 \sqrt{a + b} (a^2 - b^2) d \right) - \frac{2 a^2 (b B - a C) \text{Tan}[c + d x]}{3 b^2 (a^2 - b^2) d (a + b \text{Sec}[c + d x])^{3/2}} +$$

$$\frac{2 a (2 a^2 b B - 6 b^3 B - 5 a^3 C + 9 a b^2 C) \text{Tan}[c + d x]}{3 b^2 (a^2 - b^2)^2 d \sqrt{a + b \text{Sec}[c + d x]}}$$

Result (type 1, 1 leaves):

???

**Problem 851: Attempted integration timed out after 120 seconds.**

$$\int \frac{\text{Sec}[c + d x] (B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2)}{(a + b \text{Sec}[c + d x])^{5/2}} dx$$

Optimal (type 4, 387 leaves, 6 steps):

$$\left( 2 (a^2 b B + 3 b^3 B + 2 a^3 C - 6 a b^2 C) \cot [c + d x] \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \operatorname{Sec} [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \right. \\ \left. \sqrt{\frac{b (1 - \operatorname{Sec} [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec} [c + d x])}{a - b}} \right) / (3 (a - b) b^3 (a + b)^{3/2} d) + \\ \left( 2 (2 a^2 C - 3 b^2 (B + C) + a b (B + 3 C)) \cot [c + d x] \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \operatorname{Sec} [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \right. \\ \left. \sqrt{\frac{b (1 - \operatorname{Sec} [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec} [c + d x])}{a - b}} \right) / (3 b^2 \sqrt{a + b} (a^2 - b^2) d) + \\ \frac{2 a (b B - a C) \tan [c + d x]}{3 b (a^2 - b^2) d (a + b \operatorname{Sec} [c + d x])^{3/2}} + \frac{2 (a^2 b B + 3 b^3 B + 2 a^3 C - 6 a b^2 C) \tan [c + d x]}{3 b (a^2 - b^2)^2 d \sqrt{a + b \operatorname{Sec} [c + d x]}}$$

Result (type 1, 1 leaves):

???

### Problem 852: Unable to integrate problem.

$$\int \frac{B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2}{(a + b \operatorname{Sec} [c + d x])^{5/2}} dx$$

Optimal (type 4, 353 leaves, 6 steps):

$$- \left( \left( 2 (4 a b B - a^2 C - 3 b^2 C) \cot [c + d x] \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \operatorname{Sec} [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \right. \right. \\ \left. \sqrt{\frac{b (1 - \operatorname{Sec} [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec} [c + d x])}{a - b}} \right) / (3 (a - b) b^2 (a + b)^{3/2} d) \right) + \\ \left( 2 (3 a B - b B + a C - 3 b C) \cot [c + d x] \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \operatorname{Sec} [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \right. \\ \left. \sqrt{\frac{b (1 - \operatorname{Sec} [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec} [c + d x])}{a - b}} \right) / (3 (a - b) b (a + b)^{3/2} d) - \\ \frac{2 (b B - a C) \tan [c + d x]}{3 (a^2 - b^2) d (a + b \operatorname{Sec} [c + d x])^{3/2}} - \frac{2 (4 a b B - a^2 C - 3 b^2 C) \tan [c + d x]}{3 (a^2 - b^2)^2 d \sqrt{a + b \operatorname{Sec} [c + d x]}}$$

Result (type 8, 36 leaves):

$$\int \frac{B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2}{(a+b \operatorname{Sec}[c+dx])^{5/2}} dx$$

**Problem 853: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Cos}[c+dx] (B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2)}{(a+b \operatorname{Sec}[c+dx])^{5/2}} dx$$

Optimal (type 4, 495 leaves, 8 steps):

$$\left( 2 (7 a^2 b B - 3 b^3 B - 4 a^3 C) \operatorname{Cot}[c+dx] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \right. \\ \left. \sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}} \right) / (3 a^2 (a-b) b (a+b)^{3/2} d) - \\ \left( 2 (6 a^2 b B - a b^2 B - 3 b^3 B - 3 a^3 C + a^2 b C) \operatorname{Cot}[c+dx] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \right. \right. \\ \left. \left. \frac{a+b}{a-b} \right] \sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}} \right) / (3 a^2 (a-b) b (a+b)^{3/2} d) - \\ \frac{1}{a^3 d} 2 \sqrt{a+b} B \operatorname{Cot}[c+dx] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ \sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}} + \\ \frac{2 b (b B - a C) \operatorname{Tan}[c+dx]}{3 a (a^2 - b^2) d (a+b \operatorname{Sec}[c+dx])^{3/2}} + \frac{2 b (7 a^2 b B - 3 b^3 B - 4 a^3 C) \operatorname{Tan}[c+dx]}{3 a^2 (a^2 - b^2)^2 d \sqrt{a+b \operatorname{Sec}[c+dx]}}$$

Result (type 4, 2039 leaves):

$$\left( (b+a \operatorname{Cos}[c+dx])^3 \operatorname{Sec}[c+dx]^3 \right. \\ \left( \frac{2 (-7 a^2 b B + 3 b^3 B + 4 a^3 C) \operatorname{Sin}[c+dx]}{3 a^2 (a^2 - b^2)^2} - \frac{2 (b^3 B \operatorname{Sin}[c+dx] - a b^2 C \operatorname{Sin}[c+dx])}{3 a^2 (a^2 - b^2) (b+a \operatorname{Cos}[c+dx])^2} - \right. \\ \left. (2 (-8 a^2 b^2 B \operatorname{Sin}[c+dx] + 4 b^4 B \operatorname{Sin}[c+dx] + 5 a^3 b C \operatorname{Sin}[c+dx] - a b^3 C \operatorname{Sin}[c+dx])) \right) / \\ \left. (3 a^2 (a^2 - b^2)^2 (b+a \operatorname{Cos}[c+dx])) \right) / (d (a+b \operatorname{Sec}[c+dx])^{5/2}) +$$

$$\begin{aligned}
& \left( 2 (b + a \cos [c + d x])^{5/2} \sec [c + d x]^{5/2} \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \right. \\
& \left( 7 a^3 b \sqrt{\frac{-a + b}{a + b}} B \tan \left[ \frac{1}{2} (c + d x) \right] + 7 a^2 b^2 \sqrt{\frac{-a + b}{a + b}} B \tan \left[ \frac{1}{2} (c + d x) \right] - 3 a b^3 \sqrt{\frac{-a + b}{a + b}} B \right. \\
& \quad \tan \left[ \frac{1}{2} (c + d x) \right] - 3 b^4 \sqrt{\frac{-a + b}{a + b}} B \tan \left[ \frac{1}{2} (c + d x) \right] - 4 a^4 \sqrt{\frac{-a + b}{a + b}} C \tan \left[ \frac{1}{2} (c + d x) \right] - \\
& \quad 4 a^3 b \sqrt{\frac{-a + b}{a + b}} C \tan \left[ \frac{1}{2} (c + d x) \right] - 14 a^3 b \sqrt{\frac{-a + b}{a + b}} B \tan \left[ \frac{1}{2} (c + d x) \right]^3 + \\
& \quad 6 a b^3 \sqrt{\frac{-a + b}{a + b}} B \tan \left[ \frac{1}{2} (c + d x) \right]^3 + 8 a^4 \sqrt{\frac{-a + b}{a + b}} C \tan \left[ \frac{1}{2} (c + d x) \right]^3 + \\
& \quad 7 a^3 b \sqrt{\frac{-a + b}{a + b}} B \tan \left[ \frac{1}{2} (c + d x) \right]^5 - 7 a^2 b^2 \sqrt{\frac{-a + b}{a + b}} B \tan \left[ \frac{1}{2} (c + d x) \right]^5 - \\
& \quad 3 a b^3 \sqrt{\frac{-a + b}{a + b}} B \tan \left[ \frac{1}{2} (c + d x) \right]^5 + 3 b^4 \sqrt{\frac{-a + b}{a + b}} B \tan \left[ \frac{1}{2} (c + d x) \right]^5 - \\
& \quad 4 a^4 \sqrt{\frac{-a + b}{a + b}} C \tan \left[ \frac{1}{2} (c + d x) \right]^5 + 4 a^3 b \sqrt{\frac{-a + b}{a + b}} C \tan \left[ \frac{1}{2} (c + d x) \right]^5 - \\
& \quad 6 i a^4 B \operatorname{EllipticPi} \left[ -\frac{a + b}{a - b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a + b}{a - b} \right] \\
& \quad \sqrt{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2} \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} + \\
& \quad 12 i a^2 b^2 B \operatorname{EllipticPi} \left[ -\frac{a + b}{a - b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a + b}{a - b} \right] \\
& \quad \sqrt{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2} \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} - \\
& \quad 6 i b^4 B \operatorname{EllipticPi} \left[ -\frac{a + b}{a - b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a + b}{a - b} \right]
\end{aligned}$$



$$\begin{aligned}
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 6 i a^4 B \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + 12 i a^2 b^2 B \\
 & \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 6 i b^4 B \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & i (a-b) (-7 a^2 b B + 3 b^3 B + 4 a^3 C) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \\
 & \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & i (a-b) (-4 a b^2 B - 6 b^3 B + 3 a^3 (B-C) + a^2 b (9 B+C)) \\
 & \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) / \\
 & \left(3 a^2 \sqrt{\frac{-a+b}{a+b}} (a^2 - b^2)^2 d (a+b \operatorname{Sec}[c+dx])^{5/2} \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right)
 \end{aligned}$$

$$\sqrt{\frac{1 + \tan\left[\frac{1}{2}(c + dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c + dx)\right]^2}}$$

$$\left( a \left( -1 + \tan\left[\frac{1}{2}(c + dx)\right]^2 \right) - b \left( 1 + \tan\left[\frac{1}{2}(c + dx)\right]^2 \right) \right)$$

**Problem 854: Attempted integration timed out after 120 seconds.**

$$\int \frac{B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2}{(a + b \operatorname{Sec}[c + dx])^{7/2}} dx$$

Optimal (type 4, 446 leaves, 7 steps):

$$- \left( \left( 2 (23 a^2 b B + 9 b^3 B - 3 a^3 C - 29 a b^2 C) \operatorname{Cot}[c + dx] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + dx]}}{\sqrt{a + b}}\right]\right], \right. \right.$$

$$\left. \frac{a + b}{a - b} \sqrt{\frac{b (1 - \operatorname{Sec}[c + dx])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec}[c + dx])}{a - b}} \right) / (15 (a - b)^2 b^2 (a + b)^{5/2} d) +$$

$$\left( 2 (3 a^2 (5 B + C) - 8 a b (B + 3 C) + b^2 (9 B + 5 C)) \operatorname{Cot}[c + dx] \operatorname{EllipticF}\left[\right. \right.$$

$$\left. \operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + dx]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b} \sqrt{\frac{b (1 - \operatorname{Sec}[c + dx])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec}[c + dx])}{a - b}} \right) /$$

$$(15 b \sqrt{a + b} (a^2 - b^2)^2 d) - \frac{2 (b B - a C) \operatorname{Tan}[c + dx]}{5 (a^2 - b^2) d (a + b \operatorname{Sec}[c + dx])^{5/2}} -$$

$$\frac{2 (8 a b B - 3 a^2 C - 5 b^2 C) \operatorname{Tan}[c + dx]}{15 (a^2 - b^2)^2 d (a + b \operatorname{Sec}[c + dx])^{3/2}} -$$

$$\frac{2 (23 a^2 b B + 9 b^3 B - 3 a^3 C - 29 a b^2 C) \operatorname{Tan}[c + dx]}{15 (a^2 - b^2)^3 d \sqrt{a + b \operatorname{Sec}[c + dx]}}$$

Result (type 1, 1 leaves):

???

**Problem 857: Result more than twice size of optimal antiderivative.**

$$\int (a + b \operatorname{Sec}[c + dx])^{2/3} (B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) dx$$

Optimal (type 6, 229 leaves, 8 steps):

$$\left( \sqrt{2} (a+b) C \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, -\frac{5}{3}, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sec}[c+dx]), \frac{b(1 - \operatorname{Sec}[c+dx])}{a+b} \right] \right. \\ \left. (a+b \operatorname{Sec}[c+dx])^{2/3} \operatorname{Tan}[c+dx] \right) / \left( b d \sqrt{1 + \operatorname{Sec}[c+dx]} \left( \frac{a+b \operatorname{Sec}[c+dx]}{a+b} \right)^{2/3} \right) + \\ \left( \sqrt{2} (bB - aC) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, -\frac{2}{3}, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sec}[c+dx]), \frac{b(1 - \operatorname{Sec}[c+dx])}{a+b} \right] \right. \\ \left. (a+b \operatorname{Sec}[c+dx])^{2/3} \operatorname{Tan}[c+dx] \right) / \left( b d \sqrt{1 + \operatorname{Sec}[c+dx]} \left( \frac{a+b \operatorname{Sec}[c+dx]}{a+b} \right)^{2/3} \right)$$

Result (type 6, 33208 leaves): Display of huge result suppressed!

### Problem 858: Result more than twice size of optimal antiderivative.

$$\int (a+b \operatorname{Sec}[c+dx])^{1/3} (B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 6, 229 leaves, 8 steps):

$$\left( \sqrt{2} (a+b) C \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, -\frac{4}{3}, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sec}[c+dx]), \frac{b(1 - \operatorname{Sec}[c+dx])}{a+b} \right] \right. \\ \left. (a+b \operatorname{Sec}[c+dx])^{1/3} \operatorname{Tan}[c+dx] \right) / \left( b d \sqrt{1 + \operatorname{Sec}[c+dx]} \left( \frac{a+b \operatorname{Sec}[c+dx]}{a+b} \right)^{1/3} \right) + \\ \left( \sqrt{2} (bB - aC) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, -\frac{1}{3}, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sec}[c+dx]), \frac{b(1 - \operatorname{Sec}[c+dx])}{a+b} \right] \right. \\ \left. (a+b \operatorname{Sec}[c+dx])^{1/3} \operatorname{Tan}[c+dx] \right) / \left( b d \sqrt{1 + \operatorname{Sec}[c+dx]} \left( \frac{a+b \operatorname{Sec}[c+dx]}{a+b} \right)^{1/3} \right)$$

Result (type 6, 33199 leaves): Display of huge result suppressed!

### Problem 859: Result more than twice size of optimal antiderivative.

$$\int \frac{B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2}{(a+b \operatorname{Sec}[c+dx])^{1/3}} dx$$

Optimal (type 6, 226 leaves, 8 steps):

$$\left( \sqrt{2} C \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, -\frac{2}{3}, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sec}[c+dx]), \frac{b(1 - \operatorname{Sec}[c+dx])}{a+b} \right] \right. \\ \left. (a+b \operatorname{Sec}[c+dx])^{2/3} \operatorname{Tan}[c+dx] \right) / \left( b d \sqrt{1 + \operatorname{Sec}[c+dx]} \left( \frac{a+b \operatorname{Sec}[c+dx]}{a+b} \right)^{2/3} \right) + \\ \left( \sqrt{2} (bB - aC) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{3}, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sec}[c+dx]), \frac{b(1 - \operatorname{Sec}[c+dx])}{a+b} \right] \right. \\ \left. \left( \frac{a+b \operatorname{Sec}[c+dx]}{a+b} \right)^{1/3} \operatorname{Tan}[c+dx] \right) / \left( b d \sqrt{1 + \operatorname{Sec}[c+dx]} (a+b \operatorname{Sec}[c+dx])^{1/3} \right)$$

Result (type 6, 18676 leaves):

$$\begin{aligned}
& \left( 3 (b + a \cos [c + d x])^{1/3} \left( -\frac{C}{2 (b + a \cos [c + d x])^{1/3} \sec [c + d x]^{1/3}} + \frac{B \sec [c + d x]^{2/3}}{(b + a \cos [c + d x])^{1/3}} \right. \right. \\
& \quad \left. \left. - \frac{3 a C \sec [c + d x]^{2/3}}{4 b (b + a \cos [c + d x])^{1/3}} - \frac{3 a C \cos [2 (c + d x)] \sec [c + d x]^{2/3}}{4 b (b + a \cos [c + d x])^{1/3}} \right) \right. \\
& \quad \sec [c + d x]^{1/3} \tan \left[ \frac{1}{2} (c + d x) \right] \left( \frac{1}{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2} \right)^{2/3} \\
& \quad \left( \frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2} \right)^{2/3} \left( C \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) - \right. \\
& \quad \left. \left( 12 b (a + b) B \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \right) \right. \\
& \quad \left. \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) / \left( \left( a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right. \\
& \quad \left. \left( -9 (a + b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] - \right. \right. \\
& \quad \left. \left. 2 \left( (a - b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \right) + \right. \right. \\
& \quad \left. \left. 2 (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) - \\
& \quad \left( 3 b (a + b) C \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \right. \\
& \quad \left. \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) / \left( \left( a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right. \\
& \quad \left. \left( -9 (a + b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] - \right. \right. \\
& \quad \left. \left. 2 \left( (a - b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \right) + \right. \right. \\
& \quad \left. \left. 2 (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
 & \left( 5b(a+b) \operatorname{CAppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \right) / \\
 & \left( \left( a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right. \\
 & \quad \left( -15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] - \right. \\
 & \quad \left. 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \right. \\
 & \quad \left. \left. 2(a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) + \\
 & \left( 9a(a+b) \operatorname{CAppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
 & \quad \left. \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \right) / \\
 & \left( \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \right. \\
 & \quad \left. \left. 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \right. \right. \\
 & \quad \left. \left. \left. 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \right) \right) \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) - \\
 & \left( 5a(a+b) \operatorname{CAppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right.
 \end{aligned}$$





$$\begin{aligned}
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \right. \right. \\
 & \left. \left. \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \\
 & \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) - \\
 & \left( 5a(a+b) \operatorname{CAppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) / \\
 & \left( \left( 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) + \right. \\
 & \left. 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + 2(a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) \Bigg) + \\
 & \frac{1}{4b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right)^{1/3}} 3 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left( \frac{1}{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \\
 & \left( \frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \\
 & \left( c \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - \right.
 \end{aligned}$$



$$\begin{aligned}
 & \left( 12 b (a+b) \text{B AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
 & \quad \left. \left( 1 + \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \left( \left( a+b - a \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right. \\
 & \quad \left. \left( -9 (a+b) \text{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] - \right. \right. \\
 & \quad \left. \left. 2 \left( (a-b) \text{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) + \right. \right. \\
 & \quad \left. \left. 2 (a+b) \text{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(a-b) \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \right) - \\
 & \left( 3 b (a+b) \text{C AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
 & \quad \left. \left( 1 + \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \left( \left( a+b - a \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right. \\
 & \quad \left. \left( -9 (a+b) \text{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] - \right. \right. \\
 & \quad \left. \left. 2 \left( (a-b) \text{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) + \right. \right. \\
 & \quad \left. \left. 2 (a+b) \text{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(a-b) \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \right) + \\
 & \left( 5 b (a+b) \text{C AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
 & \quad \left. \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \left( 1 + \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \\
 & \left( \left( a+b - a \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right)
 \end{aligned}$$

$$\begin{aligned}
& \left( -15 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] - \right. \\
& 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
& 2 (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \\
& \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) + \\
& \left( 9 a (a+b) C \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
& \left. \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \left( \left( 9 (a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
& \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \right. \right. \right. \\
& \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + 2 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \right. \right. \right. \\
& \left. \left. \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \\
& \left. \left( a \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) - b \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \right) - \\
& \left( 5 a (a+b) C \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
& \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2 \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \\
& \left( \left( 15 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \\
& 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
& 2 (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right.
\end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \\
 & \left. \left. \left. \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right) \right) + \\
 & \frac{1}{b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right)^{1/3}} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \left( \frac{1}{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{5/3} \\
 & \left( \frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \\
 & \left( c \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - \right. \\
 & \left. \left( 12 b (a+b) \operatorname{BAppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \right. \\
 & \left. \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \left( \left( a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \\
 & \left( -9 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] - \right. \\
 & 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \\
 & 2 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) - \\
 & \left( 3 b (a+b) \operatorname{CAppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
 & \left. \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \left( \left( a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \\
 & \left( -9 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] - \right.
 \end{aligned}$$

$$\begin{aligned}
& 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
& \quad 2 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \\
& \quad \quad \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) + \\
& \left( 5 b (a+b) \operatorname{CAppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
& \quad \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2 \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \\
& \left( \left( a+b - a \tan \left[ \frac{1}{2} (c+dx) \right]^2 + b \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right. \\
& \left( -15 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] - \right. \\
& \quad 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
& \quad 2 (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \\
& \quad \quad \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \right) + \\
& \left( 9 a (a+b) \operatorname{CAppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
& \quad \left. \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \\
& \left( \left( 9 (a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \\
& \quad 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
& \quad \quad \left. 2 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \\
 & \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) - \\
 & \left( 5 a (a+b) \operatorname{CAppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) / \\
 & \left( \left( 15 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) + \right. \\
 & \left. 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) + \right. \\
 & \left. 2 (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \\
 & \left. \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \Bigg) \Bigg) + \\
 & \frac{1}{b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right)^{1/3} \left( \frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1/3}} \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \\
 & \left( \frac{1}{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \\
 & \left( \left( -a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + b \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \Bigg) / \right. \\
 & \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - \\
 & \left( \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \left( a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) / \\
 & \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \Bigg) \left( c \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - \right.
 \end{aligned}$$

$$\begin{aligned}
& \left( 12 b (a+b) B \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2}{a+b} \right] \right. \\
& \quad \left. \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2 \right) \right) / \left( \left( a+b - a \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2 \right) \right. \\
& \quad \left. \left( -9 (a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2}{a+b} \right] - \right. \right. \\
& \quad \left. \left. 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2}{a+b} \right] \right) + \right. \right. \\
& \quad \left. \left. 2 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2}{a+b} \right] \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2 \right) \right) \right) - \\
& \left( 3 b (a+b) C \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2}{a+b} \right] \right. \\
& \quad \left. \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2 \right) \right) / \left( \left( a+b - a \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2 \right) \right. \\
& \quad \left. \left( -9 (a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2}{a+b} \right] - \right. \right. \\
& \quad \left. \left. 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2}{a+b} \right] \right) + \right. \right. \\
& \quad \left. \left. 2 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2}{a+b} \right] \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2 \right) \right) \right) + \\
& \left( 5 b (a+b) C \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2}{a+b} \right] \right. \\
& \quad \left. \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2 \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2 \right) \right) / \\
& \left( \left( a+b - a \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2 \right) \right)
\end{aligned}$$

$$\begin{aligned}
 & \left( -15 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] - \right. \\
 & 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
 & 2 (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \\
 & \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) + \\
 & \left( 9 a (a+b) C \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
 & \left. \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \\
 & \left( \left( 9 (a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \\
 & 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
 & 2 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \\
 & \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right. \\
 & \left. \left( a \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) - b \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \right) - \\
 & \left( 5 a (a+b) C \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
 & \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2 \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \\
 & \left( \left( 15 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \\
 & 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right.
 \end{aligned}$$

$$\begin{aligned}
& 2 (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
& \quad \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \\
& \left( a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) + \\
& \frac{1}{2b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^{1/3}} 3 \tan\left[\frac{1}{2}(c+dx)\right] \left( \frac{1}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \\
& \left( \frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \\
& \left( C \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
& \left. \left( 12b(a+b) \operatorname{BAppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right. \\
& \quad \left( -a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + b \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \\
& \quad \left. \left. \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) / \left( \left( a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right. \\
& \left. \left( -9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) - \right. \\
& \quad \left. 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \\
& \quad \left. 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) + \\
& \left( 3b(a+b) \operatorname{CAppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \\
& \quad \left( -a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + b \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \\
& \quad \left. \left. \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) / \left( \left( a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right)^2
\end{aligned}$$



$$\begin{aligned}
 & \left( -9 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] - \right. \\
 & 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \Bigg) - \\
 & \left( 12 b (a+b) \operatorname{BAppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right] \right) / \\
 & \left( \left( a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right. \\
 & \left( -9 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] - \right. \\
 & 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \Bigg) - \\
 & \left( 3 b (a+b) \operatorname{CAppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right] \right) / \\
 & \left( \left( a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right. \\
 & \left( -9 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] - \right.
 \end{aligned}$$

$$\begin{aligned}
& 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
& \quad 2 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \\
& \quad \quad \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) - \\
& \left( 12 b (a+b) B \left( \frac{1}{9 (a+b)} (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
& \quad \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{2}{9} \right. \\
& \quad \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
& \quad \left. \left. \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \Big/ \\
& \left( \left( a+b - a \tan \left[ \frac{1}{2} (c+dx) \right]^2 + b \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \left( -9 (a+b) \right. \right. \\
& \quad \left. \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] - 2 \right. \\
& \quad \left. \left. \left( (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \right. \\
& \quad \left. \left. 2 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
& \quad \quad \left. \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \right) - \\
& \left( 3 b (a+b) C \left( \frac{1}{9 (a+b)} (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
& \quad \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{2}{9} \right. \\
& \quad \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
& \quad \left. \left. \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \Big/
\end{aligned}$$

$$\begin{aligned}
 & \left( \left( a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( -9(a+b) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] - 2 \right. \right. \\
 & \quad \left. \left. \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \right. \\
 & \quad \left. \left. 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) - \\
 & \left( 5b(a+b) C \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( -a \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + b \right. \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Big/ \\
 & \left( \left( a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \left( -15(a+b) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] - 2 \right. \right. \\
 & \quad \left. \left. \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \right. \\
 & \quad \left. \left. 2(a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
 & \left( 5b(a+b) C \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^3 \right) \Big/ \\
 & \left( \left( a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( -15 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] - \right. \\
 & 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2 (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \left. \right) + \right. \\
 & \left. \left( 5 b (a+b) C \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \right) / \\
 & \left( \left( a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right. \\
 & \left( -15 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] - \right. \\
 & 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2 (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \left. \right) + \right. \\
 & \left. \left( 5 b (a+b) C \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( \frac{1}{5(a+b)} (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) / \\
 & \left( \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \left( \left( a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( -15 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] - \right. \\
 & 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
 & 2 (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \\
 & \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) - \\
 & \left( 9 a (a+b) C \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
 & \left( a \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] - b \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \\
 & \left. \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \\
 & \left( \left( 9 (a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \\
 & 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
 & 2 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \\
 & \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right. \\
 & \left. \left( a \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) - b \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \right) + \\
 & \left( 5 a (a+b) C \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
 & \tan \left[ \frac{1}{2} (c+dx) \right]^2 \left( a \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] - b \right. \\
 & \left. \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \\
 & \left( \left( 15 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
 & \quad \left. 2 (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \\
 & \left( a \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) - b \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right)^2 + \\
 & \left( 9 a (a+b) \operatorname{C AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right) / \\
 & \left( \left( 9 (a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \\
 & \quad \left. \left. 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \right. \\
 & \quad \left. \left. 2 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \\
 & \left( a \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) - b \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right)^2 + \\
 & \left( 9 a (a+b) \operatorname{C} \left( \frac{1}{9 (a+b)} (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] + \frac{2}{9} \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \right. \\
 & \quad \left. \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( \left( 9 (a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \\
 & \quad 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
 & \quad \quad 2 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \\
 & \quad \quad \quad \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \\
 & \quad \left( a \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) - b \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \right) - \\
 & \left( 5 a (a+b) \operatorname{CAppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right]^3 \right) / \\
 & \left( \left( 15 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \\
 & \quad 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
 & \quad \quad 2 (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \\
 & \quad \quad \quad \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \\
 & \quad \left( a \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) - b \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \right) \right) - \\
 & \left( 5 a (a+b) \operatorname{CAppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \\
 & \left( \left( 15 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
 & \quad \left. 2 (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \\
 & \left( a \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) - b \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) - \left( 5 a (a+b) \right. \\
 & \left. c \tan \left[ \frac{1}{2} (c+dx) \right]^2 \left( \frac{1}{5 (a+b)} (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{2}{5} \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \right. \\
 & \quad \left. \left. \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \\
 & \left( \left( 15 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \\
 & \quad \left. \left. 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \right. \\
 & \quad \left. \left. 2 (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \\
 & \left( a \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) - b \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) + \\
 & \left( 12 b (a+b) \operatorname{BAppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
 & \left. \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \left( -2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + 2 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \right. \right. \right.
 \end{aligned}$$





$$\begin{aligned}
 & \left. \left( \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right)^2 + 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) + \\
 & \left( 3b(a+b) C \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( -2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right)^2 + 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - 9(a+b) \left( \frac{1}{9(a+b)} (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{2}{9} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) - 2 \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left( (a-b) \left( \frac{1}{5(a+b)} 4(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{7}{3}, \frac{7}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) + \\
 & 2(a+b) \left( \frac{1}{5(a+b)} (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \left. \left. \text{AppellF1}\left[\frac{5}{2}, \frac{8}{3}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\right.\right.\right.\right. \\
 & \left. \left. \left. \left. \left. \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right]\right]\right]\right]\right] / \\
 & \left( \left( a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( -9(a+b) \text{AppellF1}\left[\right.\right.\right. \\
 & \left. \left. \left. \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\right) - \right. \\
 & \left. 2 \left( (a-b) \text{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right.\right.\right. \\
 & \left. \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + 2(a+b) \text{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \right.\right.\right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) - \\
 & \left( 9a(a+b) \text{C AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\right) \\
 & \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( 2 \left( (a-b) \text{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right.\right.\right. \\
 & \left. \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + 2(a+b) \text{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \right.\right.\right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\right) \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \tan\left[\frac{1}{2}(c+dx)\right] + 9(a+b) \left( \frac{1}{9(a+b)} (a-b) \text{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \right.\right. \\
 & \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{9} \text{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right.\right. \\
 & \left. \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) + 2
 \end{aligned}$$

$$\begin{aligned}
 & \left( \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( (a-b) \left( \frac{1}{5(a+b)} 4(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{7}{3}, \frac{7}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \right. \\
 & \quad \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) + \\
 & 2(a+b) \left( \frac{1}{5(a+b)} (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \quad \left. \left. \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{8}{3}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \right. \right. \\
 & \quad \left. \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \right) \Big/ \\
 & \left( \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \right. \\
 & 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \left. \left( a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) - \\
 & \left( 5b(a+b) \operatorname{CAppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \\
 & \left. \left( -2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2(a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \quad \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - 15 \\
 & (a+b) \left( \frac{1}{5(a+b)} (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) - 2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \left( (a-b) \left( \frac{1}{21(a+b)} 20(a-b) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{2}{3}, \frac{7}{3}, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \frac{10}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, \frac{4}{3}, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) + 2(a+b) \\
 & \left( \frac{1}{21(a+b)} 5(a-b) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, \frac{4}{3}, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \frac{25}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{8}{3}, \frac{1}{3}, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \Bigg) \Bigg) \Bigg) \Bigg) / \\
 & \left( \left( a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( -15(a+b) \operatorname{AppellF1}\left[ \right. \right. \right. \\
 & \quad \left. \left. \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] - \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right], \right. \\
 & \quad \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + 2 (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \right. \\
 & \quad \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \Bigg)^2 + \\
 & \left( 5 a (a+b) C \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
 & \quad \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2 \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right. \\
 & \quad \left. \left( 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) + \right. \right. \\
 & \quad \left. \left. 2 (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + 15 \right. \right. \\
 & \quad \left. (a+b) \left( \frac{1}{5(a+b)} (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \right. \right. \\
 & \quad \left. \left. \frac{2}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \right. \\
 & \quad \left. \left. \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \right) + 2 \tan \left[ \frac{1}{2} (c+dx) \right]^2 \\
 & \left( (a-b) \left( \frac{1}{21(a+b)} 20 (a-b) \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{2}{3}, \frac{7}{3}, \frac{9}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \right. \right. \\
 & \quad \left. \left. \frac{10}{21} \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{5}{3}, \frac{4}{3}, \frac{9}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \right. \\
 & \quad \left. \left. \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \right) + 2 (a+b)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{1}{21(a+b)} 5(a-b) \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{5}{3}, \frac{4}{3}, \frac{9}{2}, \operatorname{Tan} \left[ \frac{1}{2}(c+dx) \right]^2 \right], \right. \\
 & \quad \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2}(c+dx) \right]^2}{a+b} \right] \operatorname{Sec} \left[ \frac{1}{2}(c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2}(c+dx) \right] + \\
 & \quad \frac{25}{21} \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{8}{3}, \frac{1}{3}, \frac{9}{2}, \operatorname{Tan} \left[ \frac{1}{2}(c+dx) \right]^2 \right], \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2}(c+dx) \right]^2}{a+b} \right] \\
 & \quad \left. \operatorname{Sec} \left[ \frac{1}{2}(c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2}(c+dx) \right] \right) \Bigg) \Bigg) \Bigg) \Bigg) \Bigg) / \\
 & \left( \left( \left( \left( \left( 15(a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2}(c+dx) \right]^2 \right], \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2}(c+dx) \right]^2}{a+b} \right] \right) \right) \right) \right) \right) + \\
 & \quad 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2}(c+dx) \right]^2 \right], \right. \\
 & \quad \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2}(c+dx) \right]^2}{a+b} \right] + 2(a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \right. \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[ \frac{1}{2}(c+dx) \right]^2 \right], \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2}(c+dx) \right]^2}{a+b} \right] \right) \operatorname{Tan} \left[ \frac{1}{2}(c+dx) \right]^2 \Bigg)^2 \\
 & \left. \left( \left( \left( \left( \left( a \left( -1 + \operatorname{Tan} \left[ \frac{1}{2}(c+dx) \right]^2 \right) - b \left( 1 + \operatorname{Tan} \left[ \frac{1}{2}(c+dx) \right]^2 \right) \right) \right) \right) \right) \right) \right) \right) + \\
 & \frac{3C(b+a \operatorname{Cos}[c+dx]) \operatorname{Tan}[c+dx]}{2bd(a+b \operatorname{Sec}[c+dx])^{1/3}}
 \end{aligned}$$

**Problem 860: Result more than twice size of optimal antiderivative.**

$$\int \frac{B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2}{(a+b \operatorname{Sec}[c+dx])^{2/3}} dx$$

Optimal (type 6, 226 leaves, 8 steps):

$$\left( \sqrt{2} C \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, -\frac{1}{3}, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sec}[c + d x]), \frac{b (1 - \operatorname{Sec}[c + d x])}{a + b} \right] \right. \\ \left. (a + b \operatorname{Sec}[c + d x])^{1/3} \operatorname{Tan}[c + d x] \right) / \left( b d \sqrt{1 + \operatorname{Sec}[c + d x]} \left( \frac{a + b \operatorname{Sec}[c + d x]}{a + b} \right)^{1/3} \right) + \\ \left( \sqrt{2} (b B - a C) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{2}{3}, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sec}[c + d x]), \frac{b (1 - \operatorname{Sec}[c + d x])}{a + b} \right] \right. \\ \left. \left( \frac{a + b \operatorname{Sec}[c + d x]}{a + b} \right)^{2/3} \operatorname{Tan}[c + d x] \right) / \left( b d \sqrt{1 + \operatorname{Sec}[c + d x]} (a + b \operatorname{Sec}[c + d x])^{2/3} \right)$$

Result (type 6, 18666 leaves):

$$\left( 3 (b + a \operatorname{Cos}[c + d x])^{2/3} \left( -\frac{2 C}{(b + a \operatorname{Cos}[c + d x])^{2/3} \operatorname{Sec}[c + d x]^{2/3}} + \frac{B \operatorname{Sec}[c + d x]^{1/3}}{(b + a \operatorname{Cos}[c + d x])^{2/3}} - \right. \right. \\ \left. \frac{3 a C \operatorname{Sec}[c + d x]^{1/3}}{2 b (b + a \operatorname{Cos}[c + d x])^{2/3}} - \frac{3 a C \operatorname{Cos}[2 (c + d x)] \operatorname{Sec}[c + d x]^{1/3}}{2 b (b + a \operatorname{Cos}[c + d x])^{2/3}} \right) \\ \operatorname{Sec}[c + d x]^{2/3} \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \left( \frac{1}{1 - \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2} \right)^{1/3} \\ \left( \frac{a + b - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2} \right)^{1/3} \left( C \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right) - \right. \\ \left. \left( 6 b (a + b) B \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \right. \right. \\ \left. \left. \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) \right) / \left( \left( a + b - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right. \\ \left. \left( -9 (a + b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] - \right. \right. \\ \left. \left. 2 \left( 2 (a - b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] + \right. \right. \right. \\ \left. \left. (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \right. \\ \left. \left. \left. \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) \right) + \\ \left( 3 b (a + b) C \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \right)$$



$$\begin{aligned}
 & \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \Bigg/ \left( \left( a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right. \\
 & \left( -9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] - \right. \\
 & 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) + \\
 & \left( 5b(a+b) \operatorname{CAppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg/ \\
 & \left( \left( a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right. \\
 & \left( -15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] - \right. \\
 & 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) + \\
 & \left( 9a(a+b) \operatorname{CAppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg/ \\
 & \left( \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 \left( 2 (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
 & \quad \left. (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \\
 & \quad \tan \left[ \frac{1}{2} (c+dx) \right]^2 \left( a \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) - b \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) - \\
 & \left( 5 a (a+b) \operatorname{CAppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
 & \quad \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2 \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \\
 & \left( \left( 15 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \\
 & \quad \left. 2 \left( 2 (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \\
 & \quad \left. \left. (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \right) \\
 & \quad \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2 \left( a \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) - b \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \right) \right) / \\
 & \left( b d (a+b \operatorname{Sec}[c+dx])^{2/3} \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^{2/3} \right. \\
 & \quad \left. - \frac{1}{b \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^{5/3}} 2 \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right]^2 \left( \frac{1}{1 - \tan \left[ \frac{1}{2} (c+dx) \right]^2} \right)^{1/3} \right. \\
 & \quad \left. \left( \frac{a+b - a \tan \left[ \frac{1}{2} (c+dx) \right]^2 + b \tan \left[ \frac{1}{2} (c+dx) \right]^2}{1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2} \right)^{1/3} \left( c \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) - \right. \right. \\
 & \quad \left. \left. 6 b (a+b) \operatorname{BAppellF1} \left[ \frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \Bigg/ \left( (a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2) \right. \\
 & \left. \left( -9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] - \right. \right. \\
 & \left. \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) + \\
 & \left( 3b(a+b) \operatorname{CAppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \Bigg/ \left( (a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2) \right. \right. \\
 & \left. \left. \left( -9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] - \right. \right. \right. \\
 & \left. \left. \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) + \\
 & \left( 5b(a+b) \operatorname{CAppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \Bigg) \Bigg/ \left( (a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + \right. \right. \\
 & \left. \left. b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( -15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] - 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \frac{1}{2} (c+dx)^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \right. \right. \right. \\
 & \left. \left. \left. \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
 & \left( 9 a (a+b) \operatorname{C AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
 & \left. \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \left( \left( 9 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + 2 \left( 2 (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \right. \right. \right. \\
 & \left. \left. \left. \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \\
 & \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) - \\
 & \left( 5 a (a+b) \operatorname{C AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \\
 & \left( \left( 15 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \right. \\
 & \left. \left. 2 \left( 2 (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \\
 & \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{2 b \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^{2/3}} 3 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left(\frac{1}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}\right)^{1/3} \\
 & \left(\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}\right)^{1/3} \\
 & \left(C \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) - \left(6 b (a+b) \operatorname{BAppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \right.\right.\right. \\
 & \left.\left.\left.\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right)\right) / \\
 & \left(\left(a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \left(-9 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \right.\right.\right. \\
 & \left.\left.\left.\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] - 2 \left(2 (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \right.\right.\right. \right. \\
 & \left.\left.\left.\frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \right.\right.\right. \right. \\
 & \left.\left.\left.\frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) + \\
 & \left(3 b (a+b) \operatorname{CAppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \\
 & \left.\left.\left.\left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) / \left(\left(a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) \right. \\
 & \left.\left(-9 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] - \right. \right. \\
 & \left.\left.2 \left(2 (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right.\right.\right. \right. \\
 & \left.\left.\left.\frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \right.\right.\right. \right. \\
 & \left.\left.\left.\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left( 5 b (a+b) C \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2}{a+b} \right] \right. \\
 & \quad \left. \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2 \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2 \right) \right) / \\
 & \left( \left( a+b - a \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2 \right) \left( -15 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2}{a+b} \right] - 2 \left( 2 (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \right. \right. \right. \\
 & \quad \left. \left. \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, \right. \right. \\
 & \quad \left. \left. \frac{2}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2}{a+b} \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2 \right) \right) + \\
 & \left( 9 a (a+b) C \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2}{a+b} \right] \right. \\
 & \quad \left. \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2 \right) \right) / \left( \left( 9 (a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2}{a+b} \right] + 2 \left( 2 (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, \right. \right. \\
 & \quad \left. \left. \frac{2}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2}{a+b} \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2 \right) \right) \\
 & \left( a \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2 \right) - b \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2 \right) \right) - \\
 & \left( 5 a (a+b) C \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2}{a+b} \right] \right. \\
 & \quad \left. \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2 \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2 \right) \right) / \\
 & \left( \left( 15 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^2}{a+b} \right] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 \left( 2 (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \right. \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \Bigg) \\
 & \left( a \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) - b \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \Bigg) + \\
 & \frac{1}{b \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right)^{2/3}} \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \\
 & \left( \frac{1}{1 - \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \right)^{4/3} \\
 & \left( \frac{a+b - a \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \right)^{1/3} \\
 & \left( c \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) - \right. \\
 & \left. \left( 6b(a+b) \operatorname{B AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \right. \\
 & \left. \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \left( \left( a+b - a \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right. \\
 & \left. \left( -9(a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \right) - \\
 & 2 \left( 2 (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \Bigg) + \\
 & \left( 3b(a+b) \operatorname{C AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \Bigg/ \left( \left(a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right. \\
 & \left. \left(-9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] - \right. \right. \\
 & \left. \left. 2 \left(2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
 & \left(5b(a+b) \operatorname{CAppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \Bigg/ \\
 & \left( \left(a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \left(-15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] - 2 \left(2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{2}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) + \\
 & \left(9a(a+b) \operatorname{CAppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \Bigg/ \left( \left(9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + 2 \left(2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \right. \right. \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & \left. \left. \left. \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \left. \left. \left. \left( a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right) - \right. \\
 & \left. \left. \left. \left( 5 a (a+b) C \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \right) \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right) / \\
 & \left( \left( \left( 15 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \right) + \right. \\
 & \left. \left. \left. 2 \left( 2 (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \right) \right) \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \left. \left. \left. \left( a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right) \right) \right) + \\
 & \frac{1}{b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^{2/3} \left( \frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3}} \\
 & \tan\left[\frac{1}{2}(c+dx)\right] \\
 & \left( \frac{1}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1/3} \\
 & \left( \left( -a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + b \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) / \\
 & \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \\
 & \left( \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \left( a + b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \\
 & \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2
 \end{aligned}$$

$$\begin{aligned}
 & \left( c \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \left( 6b(a+b) \operatorname{BAppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) / \\
 & \left( \left( a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( -9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] - 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \right. \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \right. \right. \right. \\
 & \quad \left. \left. \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
 & \left( 3b(a+b) \operatorname{CAppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \\
 & \left. \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \left( \left( a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right. \\
 & \left. \left( -9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] - \right. \right. \\
 & \quad \left. \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
 & \left( 5b(a+b) \operatorname{CAppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \\
 & \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) / \\
 & \left( \left( a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( -15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left( \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] - 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \right. \right. \right. \\
 & \left. \left. \left. \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \right. \right. \right. \\
 & \left. \left. \left. \frac{2}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
 & \left( 9a(a+b) C \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
 & \left. \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \\
 & \left( \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \right. \\
 & 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \left. \left( a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) - \\
 & \left( 5a(a+b) C \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
 & \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \\
 & \left( \left( 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \right. \\
 & 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)
 \end{aligned}$$



$$\begin{aligned}
 & \left( -9 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] - \right. \\
 & \quad 2 \left( 2 (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \right. \right. \\
 & \quad \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \Bigg) - \\
 & \left( 6 b (a+b) \operatorname{B AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \Bigg) / \\
 & \left( \left( a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( -9 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] - 2 \left( 2 (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \Bigg) + \\
 & \left( 3 b (a+b) \operatorname{C AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \Bigg) / \\
 & \left( \left( a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( -9 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] - 2 \left( 2 (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \Bigg) +
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) - \\
 & \left( 6b(a+b)B \left( \frac{1}{9(a+b)} {}_2F_1\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{9} \right. \right. \right. \\
 & \quad \left. \left. \left. \text{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \right. \right. \\
 & \quad \left. \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \right) / \\
 & \left( \left( a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( -9(a+b) \text{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] - 2 \left( 2(a-b) \text{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \text{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) + \\
 & \left( 3b(a+b)C \left( \frac{1}{9(a+b)} {}_2F_1\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{9} \right. \right. \right. \\
 & \quad \left. \left. \left. \text{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \right. \right. \\
 & \quad \left. \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \right) / \\
 & \left( \left( a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( -9(a+b) \text{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] - 2 \left( 2(a-b) \text{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \right. \right. \right. \\
 & \left. \left. \left. \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)\right) - \\
 & \left( 5b(a+b) \operatorname{CAppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left(-a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + b \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)\right) / \\
 & \left( \left(a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \left(-15(a+b) \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] - 2 \right. \right. \\
 & \left. \left. \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)\right) \right) + \\
 & \left( 5b(a+b) \operatorname{CAppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3\right) / \\
 & \left( \left(a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \left(-15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \right. \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] - 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \right. \right. \right. \\
 & \left. \left. \left. \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \frac{2}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
 & \left( 5b(a+b) \text{C AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \right. \\
 & \left. \left. \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right] \right) / \\
 & \left( \left( a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( -15(a+b) \text{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] - 2 \left( 2(a-b) \text{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \text{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{2}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
 & \left( 5b(a+b) \text{C Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left( \frac{1}{5(a+b)} 2(a-b) \text{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{5} \text{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \\
 & \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) / \left( \left( a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \\
 & \left( -15(a+b) \text{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] - \right. \\
 & \left. 2 \left( 2(a-b) \text{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \text{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \right. \right. \right. \right.
 \end{aligned}$$







$$\begin{aligned}
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \left. \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) - \\
 & \left( 5 a (a+b) C \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3 \right) / \\
 & \left( \left( 15 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
 & \left. \left. 2 \left( 2 (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) - \\
 & \left. \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) - \\
 & \left( 5 a (a+b) C \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \\
 & \left( \left( 15 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
 & \left. \left. 2 \left( 2 (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \right. \right. \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & \tan\left[\frac{1}{2}(c+dx)\right] - 9(a+b) \left( \frac{1}{9(a+b)} 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{9} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) - 2 \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( 2(a-b) \left( \frac{1}{a+b} (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{8}{3}, \frac{7}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) + \\
 & (a+b) \left( \frac{1}{5(a+b)} 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \frac{4}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{3}, \frac{2}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \Big/ \\
 & \left( \left( a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( -9(a+b) \operatorname{AppellF1}\left[ \right. \right. \right. \\
 & \quad \left. \left. \frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] - \right. \right. \\
 & \quad \left. \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \right. \right. \right. \right.
 \end{aligned}$$





$$\begin{aligned}
 & \left( \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \right. \\
 & \quad \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + \\
 & (a+b) \left( \frac{1}{5(a+b)} 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \right. \\
 & \quad \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \frac{4}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{3}, \frac{2}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \Bigg) \Bigg) \Bigg) \Bigg) / \\
 & \left( \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \right. \\
 & \quad \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \\
 & \left. \left( a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) - \\
 & \left( 5b(a+b) \operatorname{CAppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
 & \quad \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \left( -2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \right. \right. \\
 & \quad \left. \left. \frac{2}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2
 \end{aligned}$$



$$\begin{aligned}
 & \tan\left[\frac{1}{2}(c+dx)\right] - 15(a+b) \left( \frac{1}{5(a+b)} 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \right. \right. \\
 & \quad \left. \left. \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) - 2 \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( 2(a-b) \left( \frac{1}{21(a+b)} 25(a-b) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{1}{3}, \frac{8}{3}, \right. \right. \right. \\
 & \quad \left. \left. \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{5}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, \frac{5}{3}, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) + \\
 & (a+b) \left( \frac{1}{21(a+b)} 10(a-b) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, \frac{5}{3}, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \frac{20}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{7}{3}, \frac{2}{3}, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \Big/ \\
 & \left( \left( a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( -15(a+b) \operatorname{AppellF1}\left[ \right. \right. \right. \\
 & \quad \left. \left. \frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] - \right. \right. \\
 & \quad \left. \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \right. \right. \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & \frac{20}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{7}{3}, \frac{2}{3}, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \Bigg) \Bigg) \Bigg) \Bigg) \Bigg) / \\
 & \left( \left( \left( \left( \left( 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \right. \right. \right. \right. \\
 & 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \\
 & \left. \left. \left. \left. \left. \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right) \right) \right) \right) + \\
 & \frac{3C(b+a \operatorname{Cos}[c+dx]) \operatorname{Tan}[c+dx]}{bd(a+b \operatorname{Sec}[c+dx])^{2/3}}
 \end{aligned}$$

### Problem 861: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[c+dx]^3 (a+b \operatorname{Sec}[c+dx]) (A+B \operatorname{Sec}[c+dx]+C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 3, 165 leaves, 7 steps):

$$\begin{aligned}
 & \frac{(4aA+3bB+3aC) \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{8d} + \frac{(5Ab+5aB+4bC) \operatorname{Tan}[c+dx]}{5d} + \\
 & \frac{(4aA+3bB+3aC) \operatorname{Sec}[c+dx] \operatorname{Tan}[c+dx]}{8d} + \frac{(bB+aC) \operatorname{Sec}[c+dx]^3 \operatorname{Tan}[c+dx]}{4d} + \\
 & \frac{bC \operatorname{Sec}[c+dx]^4 \operatorname{Tan}[c+dx]}{5d} + \frac{(5Ab+5aB+4bC) \operatorname{Tan}[c+dx]^3}{15d}
 \end{aligned}$$

Result (type 3, 660 leaves):

$$\begin{aligned}
& - \frac{a A \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right]}{2d} - \frac{3 b B \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right]}{8d} - \\
& \frac{3 a C \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right]}{8d} + \frac{a A \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right]}{2d} + \\
& \frac{3 b B \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right]}{8d} + \frac{3 a C \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right]}{8d} + \\
& \frac{16 d \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^4}{a A} + \frac{16 d \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^4}{3 b B} + \\
& \frac{4 d \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^2}{3 a C} + \frac{16 d \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^2}{b B} - \\
& \frac{16 d \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^2}{a C} - \frac{16 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^4}{a A} - \\
& \frac{16 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^4}{3 b B} - \frac{4 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^2}{3 a C} + \\
& \frac{16 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^2}{2 A b \operatorname{Tan}[c+dx]} + \frac{2 a B \operatorname{Tan}[c+dx]}{3 d} + \frac{8 b C \operatorname{Tan}[c+dx]}{15 d} + \frac{A b \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx]}{3 d} + \\
& \frac{a B \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx]}{3 d} + \frac{4 b C \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx]}{15 d} + \frac{b C \operatorname{Sec}[c+dx]^4 \operatorname{Tan}[c+dx]}{5 d}
\end{aligned}$$

### Problem 862: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[c+dx]^2 (a+b \operatorname{Sec}[c+dx]) (A+B \operatorname{Sec}[c+dx]+C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 3, 137 leaves, 7 steps):

$$\begin{aligned}
& \frac{(4 A b + 4 a B + 3 b C) \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{8 d} + \\
& \frac{(3 a A + 2 b B + 2 a C) \operatorname{Tan}[c+dx]}{3 d} + \frac{(4 A b + 4 a B + 3 b C) \operatorname{Sec}[c+dx] \operatorname{Tan}[c+dx]}{8 d} + \\
& \frac{(b B + a C) \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx]}{3 d} + \frac{b C \operatorname{Sec}[c+dx]^3 \operatorname{Tan}[c+dx]}{4 d}
\end{aligned}$$

Result (type 3, 545 leaves):

$$\begin{aligned}
 & \frac{A b \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+d x)\right]-\sin\left[\frac{1}{2}(c+d x)\right]\right]}{2 d} - \\
 & \frac{a B \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+d x)\right]-\sin\left[\frac{1}{2}(c+d x)\right]\right]}{2 d} - \frac{3 b C \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+d x)\right]-\sin\left[\frac{1}{2}(c+d x)\right]\right]}{8 d} + \\
 & \frac{A b \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right]}{2 d} + \frac{a B \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right]}{2 d} + \\
 & \frac{3 b C \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right]}{8 d} + \frac{b C}{16 d\left(\cos\left[\frac{1}{2}(c+d x)\right]-\sin\left[\frac{1}{2}(c+d x)\right]\right)^4} + \\
 & \frac{A b}{4 d\left(\cos\left[\frac{1}{2}(c+d x)\right]-\sin\left[\frac{1}{2}(c+d x)\right]\right)^2} + \frac{a B}{4 d\left(\cos\left[\frac{1}{2}(c+d x)\right]-\sin\left[\frac{1}{2}(c+d x)\right]\right)^2} + \\
 & \frac{3 b C}{16 d\left(\cos\left[\frac{1}{2}(c+d x)\right]-\sin\left[\frac{1}{2}(c+d x)\right]\right)^2} - \frac{b C}{16 d\left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^4} - \\
 & \frac{A b}{4 d\left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^2} - \frac{a B}{4 d\left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^2} - \\
 & \frac{3 b C}{16 d\left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^2} + \frac{a A \operatorname{Tan}[c+d x]}{d} + \frac{2 b B \operatorname{Tan}[c+d x]}{3 d} + \\
 & \frac{2 a C \operatorname{Tan}[c+d x]}{3 d} + \frac{b B \operatorname{Sec}[c+d x]^2 \operatorname{Tan}[c+d x]}{3 d} + \frac{a C \operatorname{Sec}[c+d x]^2 \operatorname{Tan}[c+d x]}{3 d}
 \end{aligned}$$

**Problem 865: Result more than twice size of optimal antiderivative.**

$$\int \cos [c+d x](a+b \operatorname{Sec}[c+d x])(A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) d x$$

Optimal (type 3, 52 leaves, 5 steps):

$$(A b+a B) x+\frac{(b B+a C) \operatorname{ArcTanh}\left[\sin [c+d x]\right]}{d}+\frac{a A \sin [c+d x]}{d}+\frac{b C \operatorname{Tan}[c+d x]}{d}$$

Result (type 3, 187 leaves):

$$\begin{aligned}
 A b x+a B x-\frac{b B \operatorname{Log}\left[\cos \left[\frac{c}{2}+\frac{d x}{2}\right]-\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right]}{d}-\frac{a C \operatorname{Log}\left[\cos \left[\frac{c}{2}+\frac{d x}{2}\right]-\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right]}{d}+ \\
 \frac{b B \operatorname{Log}\left[\cos \left[\frac{c}{2}+\frac{d x}{2}\right]+\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right]}{d}+\frac{a C \operatorname{Log}\left[\cos \left[\frac{c}{2}+\frac{d x}{2}\right]+\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right]}{d}+ \\
 \frac{a A \cos [d x] \sin [c]}{d}+\frac{a A \cos [c] \sin [d x]}{d}+\frac{b C \operatorname{Tan}[c+d x]}{d}
 \end{aligned}$$

**Problem 872: Result more than twice size of optimal antiderivative.**

$$\int (a+b \operatorname{Sec}[c+d x])^2(A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) d x$$

Optimal (type 3, 134 leaves, 6 steps):

$$a^2 A x + \frac{(2 a^2 B + b^2 B + 2 a b (2 A + C)) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{2 d} +$$

$$\frac{(3 A b^2 + 6 a b B + 2 a^2 C + 2 b^2 C) \operatorname{Tan}[c + d x]}{3 d} +$$

$$\frac{b (3 b B + 2 a C) \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x]}{6 d} + \frac{C (a + b \operatorname{Sec}[c + d x])^2 \operatorname{Tan}[c + d x]}{3 d}$$

Result (type 3, 322 leaves):

$$\frac{1}{24 d} \operatorname{Sec}[c + d x]^3 \left( 9 \operatorname{Cos}[c + d x] \right.$$

$$\left. \left( 2 a^2 A (c + d x) - (2 a^2 B + b^2 B + 2 a b (2 A + C)) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right) + \right.$$

$$\left. \left( 2 a^2 B + b^2 B + 2 a b (2 A + C) \right) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right) + 3 \operatorname{Cos}[3(c + d x)]$$

$$\left( 2 a^2 A (c + d x) - (2 a^2 B + b^2 B + 2 a b (2 A + C)) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right) +$$

$$\left( 2 a^2 B + b^2 B + 2 a b (2 A + C) \right) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right) +$$

$$4 (3 A b^2 + 6 a b B + 3 a^2 C + 4 b^2 C + 3 b (b B + 2 a C) \operatorname{Cos}[c + d x] +$$

$$(3 A b^2 + 6 a b B + 3 a^2 C + 2 b^2 C) \operatorname{Cos}[2(c + d x)]) \operatorname{Sin}[c + d x]$$

### Problem 873: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cos}[c + d x] (a + b \operatorname{Sec}[c + d x])^2 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 3, 126 leaves, 6 steps):

$$a (2 A b + a B) x + \frac{(2 A b^2 + 4 a b B + 2 a^2 C + b^2 C) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{2 d} +$$

$$\frac{A (a + b \operatorname{Sec}[c + d x])^2 \operatorname{Sin}[c + d x]}{d} -$$

$$\frac{b (2 a A - b B - 2 a C) \operatorname{Tan}[c + d x]}{d} - \frac{b^2 (2 A - C) \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x]}{2 d}$$

Result (type 3, 453 leaves):

$$\frac{1}{4d} \operatorname{Sec}[c+dx]^2 \left( 4aAbc + 2a^2Bc + 4aAbdx + 2a^2Bdx - 2Ab^2 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - \right. \\ 4abB \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - \\ 2a^2C \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - b^2C \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + \\ 2Ab^2 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + 4abB \\ \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + 2a^2C \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + \\ b^2C \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + \operatorname{Cos}[2(c+dx)] \left( 2a(2Ab+aB)(c+dx) - \right. \\ (2Ab^2+4abB+2a^2C+b^2C) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + \\ \left. (2Ab^2+4abB+2a^2C+b^2C) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \right) + \\ (a^2A+2b^2C) \operatorname{Sin}[c+dx] + 2b^2B \operatorname{Sin}[2(c+dx)] + 4abC \operatorname{Sin}[2(c+dx)] + \\ \left. a^2A \operatorname{Sin}[3(c+dx)] \right)$$

**Problem 880: Result more than twice size of optimal antiderivative.**

$$\int (a+b \operatorname{Sec}[c+dx])^3 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 3, 207 leaves, 7 steps):

$$a^3 Ax + \frac{1}{8d} (8a^3B + 12ab^2B + 12a^2b(2A+C) + b^3(4A+3C)) \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]] + \\ \frac{(16a^2bB + 4b^3B + 3a^3C + 6ab^2(3A+2C)) \operatorname{Tan}[c+dx]}{6d} + \\ \frac{b(12Ab^2 + 20abB + 6a^2C + 9b^2C) \operatorname{Sec}[c+dx] \operatorname{Tan}[c+dx]}{24d} + \\ \frac{(4bB + 3aC)(a+b \operatorname{Sec}[c+dx])^2 \operatorname{Tan}[c+dx]}{12d} + \frac{C(a+b \operatorname{Sec}[c+dx])^3 \operatorname{Tan}[c+dx]}{4d}$$

Result (type 3, 687 leaves):

$$\begin{aligned}
& \left( (-24 a^2 A b - 4 A b^3 - 8 a^3 B - 12 a b^2 B - 12 a^2 b C - 3 b^3 C) \right. \\
& \quad \left. \cos [c+d x]^5 \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+d x)\right] - \sin\left[\frac{1}{2}(c+d x)\right]\right] \right. \\
& \quad \left. (a+b \operatorname{Sec}[c+d x])^3 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \right) / \\
& \left( 4 d (b+a \cos [c+d x])^3 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right) + \\
& \left( (24 a^2 A b+4 A b^3+8 a^3 B+12 a b^2 B+12 a^2 b C+3 b^3 C) \right. \\
& \quad \left. \cos [c+d x]^5 \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right] \right. \\
& \quad \left. (a+b \operatorname{Sec}[c+d x])^3 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \right) / \\
& \left( 4 d (b+a \cos [c+d x])^3 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right) + \\
& \left( 1 / \left( 48 d (b+a \cos [c+d x])^3 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right) \right) \\
& \cos [c+d x] (a+b \operatorname{Sec}[c+d x])^3 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \\
& (36 a^3 A (c+d x)+48 a^3 A (c+d x) \cos [2(c+d x)]+12 a^3 A (c+d x) \cos [4(c+d x)]+ \\
& 12 a b^3 \sin [c+d x]+36 a b^2 B \sin [c+d x]+36 a^2 b C \sin [c+d x]+ \\
& 33 b^3 C \sin [c+d x]+72 a A b^2 \sin [2(c+d x)]+72 a^2 b B \sin [2(c+d x)]+ \\
& 32 b^3 B \sin [2(c+d x)]+24 a^3 C \sin [2(c+d x)]+96 a b^2 C \sin [2(c+d x)]+ \\
& 12 A b^3 \sin [3(c+d x)]+36 a b^2 B \sin [3(c+d x)]+36 a^2 b C \sin [3(c+d x)]+ \\
& 9 b^3 C \sin [3(c+d x)]+36 a A b^2 \sin [4(c+d x)]+36 a^2 b B \sin [4(c+d x)]+ \\
& 8 b^3 B \sin [4(c+d x)]+12 a^3 C \sin [4(c+d x)]+24 a b^2 C \sin [4(c+d x)])
\end{aligned}$$

### Problem 881: Result more than twice size of optimal antiderivative.

$$\int \cos [c+d x] (a+b \operatorname{Sec}[c+d x])^3 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) dx$$

Optimal (type 3, 192 leaves, 7 steps):

$$\begin{aligned}
& a^2 (3 A b+a B) x + \frac{(6 a^2 b B+b^3 B+2 a^3 C+3 a b^2 (2 A+C)) \operatorname{ArcTanh}[\sin [c+d x]]}{2 d} + \\
& \frac{A (a+b \operatorname{Sec}[c+d x])^3 \sin [c+d x]}{d} + \frac{b (9 a b B-a^2 (6 A-8 C)+b^2 (3 A+2 C)) \tan [c+d x]}{3 d} - \\
& \frac{b^2 (6 a A-3 b B-5 a C) \operatorname{Sec}[c+d x] \tan [c+d x]}{6 d} - \frac{b (3 A-C) (a+b \operatorname{Sec}[c+d x])^2 \tan [c+d x]}{3 d}
\end{aligned}$$

Result (type 3, 1335 leaves):

$$\begin{aligned}
& \left( 2 a^2 (3 A b+a B) (c+d x) \cos [c+d x]^5 (a+b \operatorname{Sec}[c+d x])^3 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \right) / \\
& \left( d (b+a \cos [c+d x])^3 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right) + \\
& \left( (-6 a A b^2-6 a^2 b B-b^3 B-2 a^3 C-3 a b^2 C) \cos [c+d x]^5 \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+d x)\right] - \sin\left[\frac{1}{2}(c+d x)\right]\right] \right. \\
& \quad \left. (a+b \operatorname{Sec}[c+d x])^3 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \right) / \\
& \left( d (b+a \cos [c+d x])^3 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right) +
\end{aligned}$$



$$\begin{aligned}
 & \left( (6 a A b^2 + 6 a^2 b B + b^3 B + 2 a^3 C + 3 a b^2 C) \operatorname{Cos}[c + d x]^5 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right. \\
 & \quad \left. (a + b \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) / \\
 & \left( d (b + a \operatorname{Cos}[c + d x])^3 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \right) + \\
 & \left( (3 b^3 B + 9 a b^2 C + b^3 C) \operatorname{Cos}[c + d x]^5 (a + b \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) / \\
 & \left( 6 d (b + a \operatorname{Cos}[c + d x])^3 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \right. \\
 & \quad \left. \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^2 \right) + \\
 & \left( b^3 C \operatorname{Cos}[c + d x]^5 (a + b \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) / \\
 & \left( 3 d (b + a \operatorname{Cos}[c + d x])^3 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \right. \\
 & \quad \left. \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^3 \right) + \\
 & \left( b^3 C \operatorname{Cos}[c + d x]^5 (a + b \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) / \\
 & \left( 3 d (b + a \operatorname{Cos}[c + d x])^3 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \right. \\
 & \quad \left. \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^3 \right) + \\
 & \left( (-3 b^3 B - 9 a b^2 C - b^3 C) \operatorname{Cos}[c + d x]^5 (a + b \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) / \\
 & \left( 6 d (b + a \operatorname{Cos}[c + d x])^3 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \right. \\
 & \quad \left. \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^2 \right) + \\
 & \left( 2 \operatorname{Cos}[c + d x]^5 (a + b \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \left( 3 A b^3 \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] + \right. \right. \\
 & \quad \left. \left. 9 a b^2 B \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] + 9 a^2 b C \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] + 2 b^3 C \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \right) / \\
 & \left( 3 d (b + a \operatorname{Cos}[c + d x])^3 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \right. \\
 & \quad \left. \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \right) + \\
 & \left( 2 \operatorname{Cos}[c + d x]^5 (a + b \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \left( 3 A b^3 \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] + \right. \right. \\
 & \quad \left. \left. 9 a b^2 B \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] + 9 a^2 b C \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] + 2 b^3 C \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \right) / \\
 & \left( 3 d (b + a \operatorname{Cos}[c + d x])^3 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \right. \\
 & \quad \left. \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \right) + \\
 & \left( 2 a^3 A \operatorname{Cos}[c + d x]^5 (a + b \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \operatorname{Sin}[c + d x] \right) /
 \end{aligned}$$

$$\left( d \left( b + a \cos [c + d x] \right)^3 \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \right)$$

### Problem 887: Result more than twice size of optimal antiderivative.

$$\int \sec [c + d x]^2 (a + b \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 3, 491 leaves, 10 steps):

$$\begin{aligned} & \frac{1}{16 d} \left( 8 a^4 B + 36 a^2 b^2 B + 5 b^4 B + 8 a^3 b (4 A + 3 C) + 4 a b^3 (6 A + 5 C) \right) \operatorname{ArcTanh}[\sin [c + d x]] - \\ & \frac{1}{420 b^2 d} \left( 28 a^5 b B - 847 a^3 b^3 B - 896 a b^5 B - 8 a^6 C - 32 b^6 (7 A + 6 C) - \right. \\ & \quad \left. 4 a^4 b^2 (42 A + 23 C) - 32 a^2 b^4 (49 A + 39 C) \right) \tan [c + d x] - \frac{1}{1680 b d} \\ & \left( 56 a^4 b B - 1246 a^2 b^3 B - 525 b^5 B - 16 a^5 C - 48 a^3 b^2 (7 A + 4 C) - 4 a b^4 (406 A + 333 C) \right) \sec [c + d x] \\ & \tan [c + d x] - \frac{1}{840 b^2 d} \left( 28 a^3 b B - 371 a b^3 B - 8 a^4 C - 32 b^4 (7 A + 6 C) - 12 a^2 b^2 (14 A + 9 C) \right) \\ & (a + b \sec [c + d x])^2 \tan [c + d x] - \frac{1}{840 b^2 d} \\ & \left( 28 a^2 b B - 175 b^3 B - 8 a^3 C - 4 a b^2 (42 A + 31 C) \right) (a + b \sec [c + d x])^3 \tan [c + d x] + \\ & \frac{\left( 42 A b^2 - 7 a b B + 2 a^2 C + 36 b^2 C \right) (a + b \sec [c + d x])^4 \tan [c + d x]}{210 b^2 d} + \\ & \frac{(7 b B - 2 a C) (a + b \sec [c + d x])^5 \tan [c + d x]}{42 b^2 d} + \frac{C \sec [c + d x] (a + b \sec [c + d x])^5 \tan [c + d x]}{7 b d} \end{aligned}$$

Result (type 3, 1348 leaves):

$$\begin{aligned}
 & \left( (-32 a^3 A b - 24 a A b^3 - 8 a^4 B - 36 a^2 b^2 B - 5 b^4 B - 24 a^3 b C - 20 a b^3 C) \right. \\
 & \quad \left. \cos [c+d x]^6 \log \left[ \cos \left[ \frac{1}{2} (c+d x) \right] - \sin \left[ \frac{1}{2} (c+d x) \right] \right] \right. \\
 & \quad \left. (a+b \sec [c+d x])^4 (A+B \sec [c+d x]+C \sec [c+d x]^2) \right) / \\
 & \left( 8 d (b+a \cos [c+d x])^4 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right) + \\
 & \left( 32 a^3 A b + 24 a A b^3 + 8 a^4 B + 36 a^2 b^2 B + 5 b^4 B + 24 a^3 b C + 20 a b^3 C \right) \\
 & \quad \cos [c+d x]^6 \log \left[ \cos \left[ \frac{1}{2} (c+d x) \right] + \sin \left[ \frac{1}{2} (c+d x) \right] \right] \\
 & \quad (a+b \sec [c+d x])^4 (A+B \sec [c+d x]+C \sec [c+d x]^2) \right) / \\
 & \left( 8 d (b+a \cos [c+d x])^4 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right) + \\
 & \left( (a+b \sec [c+d x])^4 (A+B \sec [c+d x]+C \sec [c+d x]^2) \right. \\
 & \quad \left. (b^4 B \sin [c+d x]+4 a b^3 C \sin [c+d x]) \right) / \\
 & \left( 3 d (b+a \cos [c+d x])^4 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right) + \\
 & \left( \cos [c+d x]^2 (a+b \sec [c+d x])^4 (A+B \sec [c+d x]+C \sec [c+d x]^2) (24 a A b^3 \sin [c+d x] + \right. \\
 & \quad \left. 36 a^2 b^2 B \sin [c+d x]+5 b^4 B \sin [c+d x]+24 a^3 b C \sin [c+d x]+20 a b^3 C \sin [c+d x]) \right) / \\
 & \left( 12 d (b+a \cos [c+d x])^4 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right) + \\
 & \left( \cos [c+d x]^4 (a+b \sec [c+d x])^4 (A+B \sec [c+d x]+C \sec [c+d x]^2) \right. \\
 & \quad \left. (32 a^3 A b \sin [c+d x]+24 a A b^3 \sin [c+d x]+8 a^4 B \sin [c+d x]+36 a^2 b^2 B \sin [c+d x] + \right. \\
 & \quad \left. 5 b^4 B \sin [c+d x]+24 a^3 b C \sin [c+d x]+20 a b^3 C \sin [c+d x]) \right) / \\
 & \left( 8 d (b+a \cos [c+d x])^4 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right) + \\
 & \left( 2 \cos [c+d x] (a+b \sec [c+d x])^4 (A+B \sec [c+d x]+C \sec [c+d x]^2) \right. \\
 & \quad \left. (7 A b^4 \sin [c+d x]+28 a b^3 B \sin [c+d x]+42 a^2 b^2 C \sin [c+d x]+6 b^4 C \sin [c+d x]) \right) / \\
 & \left( 35 d (b+a \cos [c+d x])^4 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right) + \\
 & \left( 2 \cos [c+d x]^3 (a+b \sec [c+d x])^4 (A+B \sec [c+d x]+C \sec [c+d x]^2) \right. \\
 & \quad \left. (210 a^2 A b^2 \sin [c+d x]+28 A b^4 \sin [c+d x]+140 a^3 b B \sin [c+d x]+112 a b^3 B \sin [c+d x] + \right. \\
 & \quad \left. 35 a^4 C \sin [c+d x]+168 a^2 b^2 C \sin [c+d x]+24 b^4 C \sin [c+d x]) \right) / \\
 & \left( 105 d (b+a \cos [c+d x])^4 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right) + \\
 & \left( 2 \cos [c+d x]^5 (a+b \sec [c+d x])^4 (A+B \sec [c+d x]+C \sec [c+d x]^2) \right. \\
 & \quad \left. (105 a^4 A \sin [c+d x]+420 a^2 A b^2 \sin [c+d x]+56 A b^4 \sin [c+d x]+280 a^3 b B \sin [c+d x] + \right. \\
 & \quad \left. 224 a b^3 B \sin [c+d x]+70 a^4 C \sin [c+d x]+336 a^2 b^2 C \sin [c+d x]+48 b^4 C \sin [c+d x]) \right) / \\
 & \left( 105 d (b+a \cos [c+d x])^4 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right) + \\
 & \left( 2 b^4 C (a+b \sec [c+d x])^4 (A+B \sec [c+d x]+C \sec [c+d x]^2) \tan [c+d x] \right) / \\
 & \left( 7 d (b+a \cos [c+d x])^4 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right)
 \end{aligned}$$

### Problem 889: Result more than twice size of optimal antiderivative.

$$\int (a + b \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 3, 290 leaves, 8 steps):

$$\begin{aligned} & a^4 A x + \frac{1}{8 d} (8 a^4 B + 24 a^2 b^2 B + 3 b^4 B + 16 a^3 b (2 A + C) + 4 a b^3 (4 A + 3 C)) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]] + \\ & \frac{1}{30 d} (95 a^3 b B + 80 a b^3 B + 12 a^4 C + 4 b^4 (5 A + 4 C) + 2 a^2 b^2 (85 A + 56 C)) \operatorname{Tan}[c + d x] + \\ & \frac{1}{120 d} b (130 a^2 b B + 45 b^3 B + 24 a^3 C + 4 a b^2 (40 A + 29 C)) \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x] + \\ & \frac{(20 A b^2 + 35 a b B + 12 a^2 C + 16 b^2 C) (a + b \operatorname{Sec}[c + d x])^2 \operatorname{Tan}[c + d x]}{60 d} + \\ & \frac{(5 b B + 4 a C) (a + b \operatorname{Sec}[c + d x])^3 \operatorname{Tan}[c + d x]}{20 d} + \frac{C (a + b \operatorname{Sec}[c + d x])^4 \operatorname{Tan}[c + d x]}{5 d} \end{aligned}$$

Result (type 3, 915 leaves):

$$\begin{aligned} & \left( (-32 a^3 A b - 16 a A b^3 - 8 a^4 B - 24 a^2 b^2 B - 3 b^4 B - 16 a^3 b C - 12 a b^3 C) \right. \\ & \quad \left. \operatorname{Cos}[c + d x]^6 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right. \\ & \quad \left. (a + b \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) / \\ & \quad \left( 4 d (b + a \operatorname{Cos}[c + d x])^4 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \right) + \\ & \quad \left( (32 a^3 A b + 16 a A b^3 + 8 a^4 B + 24 a^2 b^2 B + 3 b^4 B + 16 a^3 b C + 12 a b^3 C) \right. \\ & \quad \left. \operatorname{Cos}[c + d x]^6 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right. \\ & \quad \left. (a + b \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right) / \\ & \quad \left( 4 d (b + a \operatorname{Cos}[c + d x])^4 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \right) + \\ & \quad \left( \operatorname{Cos}[c + d x] (a + b \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\ & \quad \left( 600 a^4 A (c + d x) \operatorname{Cos}[c + d x] + 300 a^4 A (c + d x) \operatorname{Cos}[3 (c + d x)] + 60 a^4 A (c + d x) \right. \\ & \quad \left. \operatorname{Cos}[5 (c + d x)] + 720 a^2 A b^2 \operatorname{Sin}[c + d x] + 160 A b^4 \operatorname{Sin}[c + d x] + 480 a^3 b B \operatorname{Sin}[c + d x] + \right. \\ & \quad \left. 640 a b^3 B \operatorname{Sin}[c + d x] + 120 a^4 C \operatorname{Sin}[c + d x] + 960 a^2 b^2 C \operatorname{Sin}[c + d x] + 320 b^4 C \operatorname{Sin}[c + d x] + \right. \\ & \quad \left. 480 a A b^3 \operatorname{Sin}[2 (c + d x)] + 720 a^2 b^2 B \operatorname{Sin}[2 (c + d x)] + 210 b^4 B \operatorname{Sin}[2 (c + d x)] + \right. \\ & \quad \left. 480 a^3 b C \operatorname{Sin}[2 (c + d x)] + 840 a b^3 C \operatorname{Sin}[2 (c + d x)] + 1080 a^2 A b^2 \operatorname{Sin}[3 (c + d x)] + \right. \\ & \quad \left. 200 A b^4 \operatorname{Sin}[3 (c + d x)] + 720 a^3 b B \operatorname{Sin}[3 (c + d x)] + 800 a b^3 B \operatorname{Sin}[3 (c + d x)] + \right. \\ & \quad \left. 180 a^4 C \operatorname{Sin}[3 (c + d x)] + 1200 a^2 b^2 C \operatorname{Sin}[3 (c + d x)] + 160 b^4 C \operatorname{Sin}[3 (c + d x)] + \right. \\ & \quad \left. 240 a A b^3 \operatorname{Sin}[4 (c + d x)] + 360 a^2 b^2 B \operatorname{Sin}[4 (c + d x)] + 45 b^4 B \operatorname{Sin}[4 (c + d x)] + \right. \\ & \quad \left. 240 a^3 b C \operatorname{Sin}[4 (c + d x)] + 180 a b^3 C \operatorname{Sin}[4 (c + d x)] + 360 a^2 A b^2 \operatorname{Sin}[5 (c + d x)] + \right. \\ & \quad \left. 40 A b^4 \operatorname{Sin}[5 (c + d x)] + 240 a^3 b B \operatorname{Sin}[5 (c + d x)] + 160 a b^3 B \operatorname{Sin}[5 (c + d x)] + \right. \\ & \quad \left. 60 a^4 C \operatorname{Sin}[5 (c + d x)] + 240 a^2 b^2 C \operatorname{Sin}[5 (c + d x)] + 32 b^4 C \operatorname{Sin}[5 (c + d x)] \right) / \\ & \quad \left. (480 d (b + a \operatorname{Cos}[c + d x])^4 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \right) \end{aligned}$$

### Problem 890: Result more than twice size of optimal antiderivative.

$$\int \cos [c + d x] (a + b \operatorname{Sec} [c + d x])^4 (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) dx$$

Optimal (type 3, 273 leaves, 8 steps):

$$\begin{aligned} & a^3 (4 A b + a B) x + \frac{1}{8 d} \\ & (32 a^3 b B + 16 a b^3 B + 8 a^4 C + 24 a^2 b^2 (2 A + C) + b^4 (4 A + 3 C)) \operatorname{ArcTanh} [\operatorname{Sin} [c + d x]] + \\ & \frac{A (a + b \operatorname{Sec} [c + d x])^4 \operatorname{Sin} [c + d x]}{d} + \\ & \frac{b (34 a^2 b B + 4 b^3 B - a^3 (12 A - 19 C) + 8 a b^2 (3 A + 2 C)) \operatorname{Tan} [c + d x]}{6 d} + \frac{1}{24 d} \\ & b^2 (32 a b B - a^2 (24 A - 26 C) + 3 b^2 (4 A + 3 C)) \operatorname{Sec} [c + d x] \operatorname{Tan} [c + d x] - \\ & \frac{b (12 a A - 4 b B - 7 a C) (a + b \operatorname{Sec} [c + d x])^2 \operatorname{Tan} [c + d x]}{12 d} - \\ & \frac{b (4 A - C) (a + b \operatorname{Sec} [c + d x])^3 \operatorname{Tan} [c + d x]}{4 d} \end{aligned}$$

Result (type 3, 813 leaves):

$$\begin{aligned} & \left( (-48 a^2 A b^2 - 4 A b^4 - 32 a^3 b B - 16 a b^3 B - 8 a^4 C - 24 a^2 b^2 C - 3 b^4 C) \right. \\ & \quad \left. \cos [c + d x]^6 \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] \right. \\ & \quad \left. (a + b \operatorname{Sec} [c + d x])^4 (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) \right) / \\ & \quad \left( 4 d (b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right) + \\ & \quad \left( (48 a^2 A b^2 + 4 A b^4 + 32 a^3 b B + 16 a b^3 B + 8 a^4 C + 24 a^2 b^2 C + 3 b^4 C) \right. \\ & \quad \left. \cos [c + d x]^6 \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] \right. \\ & \quad \left. (a + b \operatorname{Sec} [c + d x])^4 (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) \right) / \\ & \quad \left( 4 d (b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right) + \\ & \quad \left( 1 / \left( 48 d (b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right) \right) \\ & \quad \cos [c + d x]^2 (a + b \operatorname{Sec} [c + d x])^4 (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) \\ & \quad (144 a^3 A b (c + d x) + 36 a^4 B (c + d x) + 192 a^3 A b (c + d x) \cos [2 (c + d x)] + \\ & \quad 48 a^4 B (c + d x) \cos [2 (c + d x)] + 48 a^3 A b (c + d x) \cos [4 (c + d x)] + \\ & \quad 12 a^4 B (c + d x) \cos [4 (c + d x)] + 12 a^4 A \sin [c + d x] + 12 A b^4 \sin [c + d x] + \\ & \quad 48 a b^3 B \sin [c + d x] + 72 a^2 b^2 C \sin [c + d x] + 33 b^4 C \sin [c + d x] + 96 a A b^3 \sin [2 (c + d x)] + \\ & \quad 144 a^2 b^2 B \sin [2 (c + d x)] + 32 b^4 B \sin [2 (c + d x)] + 96 a^3 b C \sin [2 (c + d x)] + \\ & \quad 128 a b^3 C \sin [2 (c + d x)] + 18 a^4 A \sin [3 (c + d x)] + 12 A b^4 \sin [3 (c + d x)] + \\ & \quad 48 a b^3 B \sin [3 (c + d x)] + 72 a^2 b^2 C \sin [3 (c + d x)] + 9 b^4 C \sin [3 (c + d x)] + \\ & \quad 48 a A b^3 \sin [4 (c + d x)] + 72 a^2 b^2 B \sin [4 (c + d x)] + 8 b^4 B \sin [4 (c + d x)] + \\ & \quad 48 a^3 b C \sin [4 (c + d x)] + 32 a b^3 C \sin [4 (c + d x)] + 6 a^4 A \sin [5 (c + d x)]) \end{aligned}$$

### Problem 898: Result more than twice size of optimal antiderivative.

$$\int (a + b \operatorname{Sec}[c + dx])^2 (a b B - a^2 C + b^2 B \operatorname{Sec}[c + dx] + b^2 C \operatorname{Sec}[c + dx]^2) dx$$

Optimal (type 3, 149 leaves, 7 steps):

$$a^3 (b B - a C) x + \frac{b (6 a^2 b B + b^3 B - 4 a^3 C + 2 a b^2 C) \operatorname{ArcTanh}[\operatorname{Sin}[c + dx]]}{2 d} +$$

$$\frac{b^2 (9 a b B - a^2 C + 2 b^2 C) \operatorname{Tan}[c + dx]}{3 d} +$$

$$\frac{b^3 (3 b B + 2 a C) \operatorname{Sec}[c + dx] \operatorname{Tan}[c + dx]}{6 d} + \frac{b^2 C (a + b \operatorname{Sec}[c + dx])^2 \operatorname{Tan}[c + dx]}{3 d}$$

Result (type 3, 462 leaves):

$$-\frac{a^3 (-b B + a C) (c + dx)}{d} + \frac{1}{2 d}$$

$$(-6 a^2 b^2 B - b^4 B + 4 a^3 b C - 2 a b^3 C) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2} (c + dx)\right] - \operatorname{Sin}\left[\frac{1}{2} (c + dx)\right]\right] +$$

$$\frac{1}{2 d} (6 a^2 b^2 B + b^4 B - 4 a^3 b C + 2 a b^3 C) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2} (c + dx)\right] + \operatorname{Sin}\left[\frac{1}{2} (c + dx)\right]\right] +$$

$$\frac{3 b^4 B + 6 a b^3 C + b^4 C}{12 d \left(\operatorname{Cos}\left[\frac{1}{2} (c + dx)\right] - \operatorname{Sin}\left[\frac{1}{2} (c + dx)\right]\right)^2} + \frac{b^4 C \operatorname{Sin}\left[\frac{1}{2} (c + dx)\right]}{6 d \left(\operatorname{Cos}\left[\frac{1}{2} (c + dx)\right] - \operatorname{Sin}\left[\frac{1}{2} (c + dx)\right]\right)^3} +$$

$$\frac{b^4 C \operatorname{Sin}\left[\frac{1}{2} (c + dx)\right]}{6 d \left(\operatorname{Cos}\left[\frac{1}{2} (c + dx)\right] + \operatorname{Sin}\left[\frac{1}{2} (c + dx)\right]\right)^3} + \frac{-3 b^4 B - 6 a b^3 C - b^4 C}{12 d \left(\operatorname{Cos}\left[\frac{1}{2} (c + dx)\right] + \operatorname{Sin}\left[\frac{1}{2} (c + dx)\right]\right)^2} +$$

$$\frac{9 a b^3 B \operatorname{Sin}\left[\frac{1}{2} (c + dx)\right] + 2 b^4 C \operatorname{Sin}\left[\frac{1}{2} (c + dx)\right]}{3 d \left(\operatorname{Cos}\left[\frac{1}{2} (c + dx)\right] - \operatorname{Sin}\left[\frac{1}{2} (c + dx)\right]\right)} + \frac{9 a b^3 B \operatorname{Sin}\left[\frac{1}{2} (c + dx)\right] + 2 b^4 C \operatorname{Sin}\left[\frac{1}{2} (c + dx)\right]}{3 d \left(\operatorname{Cos}\left[\frac{1}{2} (c + dx)\right] + \operatorname{Sin}\left[\frac{1}{2} (c + dx)\right]\right)}$$

### Problem 899: Result more than twice size of optimal antiderivative.

$$\int (a + b \operatorname{Sec}[c + dx]) (a b B - a^2 C + b^2 B \operatorname{Sec}[c + dx] + b^2 C \operatorname{Sec}[c + dx]^2) dx$$

Optimal (type 3, 97 leaves, 6 steps):

$$a^2 (b B - a C) x + \frac{b (4 a b B - 2 a^2 C + b^2 C) \operatorname{ArcTanh}[\operatorname{Sin}[c + dx]]}{2 d} +$$

$$\frac{b^2 (2 b B + a C) \operatorname{Tan}[c + dx]}{2 d} + \frac{b^2 C (a + b \operatorname{Sec}[c + dx]) \operatorname{Tan}[c + dx]}{2 d}$$

Result (type 3, 379 leaves):

$$\begin{aligned}
 & -\frac{1}{4d} \operatorname{Sec}[c+dx]^2 \\
 & \left( -2a^2bBc + 2a^3cC - 2a^2bBdx + 2a^3Cdx + 4ab^2B \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - \right. \\
 & \quad \left. 2a^2bC \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + \right. \\
 & \quad \left. b^3C \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - 4ab^2B \right. \\
 & \quad \left. \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + 2a^2bC \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - \right. \\
 & \quad \left. b^3C \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + \operatorname{Cos}[2(c+dx)] \left( 2a^2(-bB+aC)(c+dx) + \right. \right. \\
 & \quad \left. \left. b(4abB - 2a^2C + b^2C) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - \right. \right. \\
 & \quad \left. \left. b(4abB - 2a^2C + b^2C) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \right) - \right. \\
 & \quad \left. \left. 2b^3C \operatorname{Sin}[c+dx] - 2b^3B \operatorname{Sin}[2(c+dx)] - 2ab^2C \operatorname{Sin}[2(c+dx)] \right) \right)
 \end{aligned}$$

**Problem 900: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c+dx]^3 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2)}{a+b \operatorname{Sec}[c+dx]} dx$$

Optimal (type 3, 215 leaves, 8 steps):

$$\begin{aligned}
 & \frac{(2a^2bB + b^3B - 2a^3C - a^2(2A+C)) \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{2b^4d} + \\
 & \frac{2a^2(Ab^2 - a(bB - aC)) \operatorname{ArcTanh}\left[\frac{\sqrt{a-b} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a+b}}\right]}{\sqrt{a-b} b^4 \sqrt{a+b} d} + \frac{(3Ab^2 - 3abB + 3a^2C + 2b^2C) \operatorname{Tan}[c+dx]}{3b^3d} + \\
 & \frac{(bB - aC) \operatorname{Sec}[c+dx] \operatorname{Tan}[c+dx]}{2b^2d} + \frac{C \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx]}{3bd}
 \end{aligned}$$

Result (type 3, 965 leaves):

$$\begin{aligned}
& \left( (2 a A b^2 - 2 a^2 b B - b^3 B + 2 a^3 C + a b^2 C) \cos [c + d x] (b + a \cos [c + d x]) \right. \\
& \quad \left. \log \left[ \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right] (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \\
& \quad \left( b^4 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \sec [c + d x]) \right) + \\
& \left( (-2 a A b^2 + 2 a^2 b B + b^3 B - 2 a^3 C - a b^2 C) \cos [c + d x] (b + a \cos [c + d x]) \right. \\
& \quad \left. \log \left[ \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right] (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \\
& \quad \left( b^4 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \sec [c + d x]) \right) + \\
& \left( (A b^2 - a b B + a^2 C) \cos [c + d x] (b + a \cos [c + d x]) (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
& \quad \left. - \left( \left( 4 i a^2 \operatorname{ArcTan} \left[ \sec \left[ \frac{d x}{2} \right] \right] \left( \frac{\cos [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} - \frac{i \sin [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} \right) \right. \right. \right. \\
& \quad \left. \left. \left( -i b \sin \left[ \frac{d x}{2} \right] + i a \sin \left[ c + \frac{d x}{2} \right] \right) \cos [c] \right) \right) / \\
& \quad \left( b^4 \sqrt{a^2 - b^2} d \sqrt{\cos [2 c] - i \sin [2 c]} \right) - \left( 4 a^2 \operatorname{ArcTan} \left[ \sec \left[ \frac{d x}{2} \right] \right] \right. \\
& \quad \left. \left( \frac{\cos [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} - \frac{i \sin [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} \right) \left( -i b \sin \left[ \frac{d x}{2} \right] + i a \sin \left[ c + \frac{d x}{2} \right] \right) \right) / \\
& \quad \left( b^4 \sqrt{a^2 - b^2} d \sqrt{\cos [2 c] - i \sin [2 c]} \right) \left. \right) / \\
& \quad \left( (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \sec [c + d x]) \right) + \\
& \quad \left( (b + a \cos [c + d x]) \sec [c] \sec [c + d x]^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
& \quad \left( 12 A b^2 \sin [d x] - 12 a b B \sin [d x] + 12 a^2 C \sin [d x] + 12 b^2 C \sin [d x] - 6 A b^2 \sin [2 c + d x] + \right. \\
& \quad \left. 6 a b B \sin [2 c + d x] - 6 a^2 C \sin [2 c + d x] + 3 b^2 B \sin [c + 2 d x] - 3 a b C \sin [c + 2 d x] + \right. \\
& \quad \left. 3 b^2 B \sin [3 c + 2 d x] - 3 a b C \sin [3 c + 2 d x] + 6 A b^2 \sin [2 c + 3 d x] - \right. \\
& \quad \left. 6 a b B \sin [2 c + 3 d x] + 6 a^2 C \sin [2 c + 3 d x] + 4 b^2 C \sin [2 c + 3 d x] \right) / \\
& \quad \left. (12 b^3 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])) \right)
\end{aligned}$$

**Problem 901: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c + d x]^2 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{a + b \sec [c + d x]} dx$$

Optimal (type 3, 153 leaves, 7 steps):



$$\frac{(b^2 (2A + C) - 2a (bB - aC)) \operatorname{ArcTanh}[\operatorname{Sin}[c + dx]]}{2b^3 d} -$$

$$\frac{2a (Ab^2 - a (bB - aC)) \operatorname{ArcTanh}\left[\frac{\sqrt{a-b} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a+b}}\right]}{\sqrt{a-b} b^3 \sqrt{a+b} d} +$$

$$\frac{(bB - aC) \operatorname{Tan}[c + dx]}{b^2 d} + \frac{C \operatorname{Sec}[c + dx] \operatorname{Tan}[c + dx]}{2bd}$$

Result (type 3, 472 leaves):

$$\left( \operatorname{Cos}[c + dx] (b + a \operatorname{Cos}[c + dx]) (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right.$$

$$\left( -2 (2Ab^2 - 2abB + 2a^2C + b^2C) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right] + \right.$$

$$\left. 2 (2Ab^2 - 2abB + 2a^2C + b^2C) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right] + \right.$$

$$\left. \left( 8a (Ab^2 + a (-bB + aC)) \operatorname{ArcTan}\left[ \frac{(i \operatorname{Cos}[c] + \operatorname{Sin}[c]) (a \operatorname{Sin}[c] + (-b + a \operatorname{Cos}[c]) \operatorname{Tan}\left[\frac{dx}{2}\right])}{\sqrt{a^2 - b^2} \sqrt{(\operatorname{Cos}[c] - i \operatorname{Sin}[c])^2}} \right] (i \operatorname{Cos}[c] + \operatorname{Sin}[c]) \right) \right) /$$

$$\left( \sqrt{a^2 - b^2} \sqrt{(\operatorname{Cos}[c] - i \operatorname{Sin}[c])^2} \right) + \frac{b^2 C}{(\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right])^2} +$$

$$\frac{4b (bB - aC) \operatorname{Sin}\left[\frac{dx}{2}\right]}{(\operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right]) (\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right])} -$$

$$\frac{b^2 C}{(\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right])^2} +$$

$$\left. \frac{4b (bB - aC) \operatorname{Sin}\left[\frac{dx}{2}\right]}{(\operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right]) (\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right])} \right) /$$

$$(2b^3 d (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2(c + dx)]) (a + b \operatorname{Sec}[c + dx]))$$

**Problem 902: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c + dx] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2)}{a + b \operatorname{Sec}[c + dx]} dx$$

Optimal (type 3, 106 leaves, 6 steps):

$$\frac{(bB - aC) \operatorname{ArcTanh}[\operatorname{Sin}[c + dx]]}{b^2 d} + \frac{2(Ab^2 - a(bB - aC)) \operatorname{ArcTanh}\left[\frac{\sqrt{a-b} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a+b}}\right]}{\sqrt{a-b} b^2 \sqrt{a+b} d} + \frac{C \operatorname{Tan}[c + dx]}{bd}$$

Result (type 3, 365 leaves):

$$\frac{1}{b^2 d (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2(c + dx)]) (a + b \operatorname{Sec}[c + dx])} \\ \frac{2 \operatorname{Cos}[c + dx] (b + a \operatorname{Cos}[c + dx]) (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2)}{\left( - (bB - aC) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right] + \right.} \\ \left. (bB - aC) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right] - \right.} \\ \left. \left( 2i(Ab^2 + a(-bB + aC)) \operatorname{ArcTan}\left[\frac{(i \operatorname{Cos}[c] + \operatorname{Sin}[c]) (a \operatorname{Sin}[c] + (-b + a \operatorname{Cos}[c]) \operatorname{Tan}\left[\frac{dx}{2}\right])}{\sqrt{a^2 - b^2} \sqrt{(\operatorname{Cos}[c] - i \operatorname{Sin}[c])^2}}\right]} \right. \right. \\ \left. \left. (\operatorname{Cos}[c] - i \operatorname{Sin}[c]) \right) \right] / \left( \sqrt{a^2 - b^2} \sqrt{(\operatorname{Cos}[c] - i \operatorname{Sin}[c])^2} \right) + \right.} \\ \left. \frac{bC \operatorname{Sin}\left[\frac{dx}{2}\right]}{\left( \operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right] \right)} + \right.} \\ \left. \frac{bC \operatorname{Sin}\left[\frac{dx}{2}\right]}{\left( \operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right] \right)} \right)$$

**Problem 903: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2}{a + b \operatorname{Sec}[c + dx]} dx$$

Optimal (type 3, 94 leaves, 6 steps):

$$\frac{Ax}{a} + \frac{C \operatorname{ArcTanh}[\operatorname{Sin}[c + dx]]}{bd} - \frac{2(Ab^2 - a(bB - aC)) \operatorname{ArcTanh}\left[\frac{\sqrt{a-b} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a+b}}\right]}{a \sqrt{a-b} b \sqrt{a+b} d}$$

Result (type 3, 261 leaves):

$$\left( 2 (C + B \cos [c + d x] + A \cos [c + d x]^2) \right. \\
 \left. \left( \sqrt{a^2 - b^2} \left( A b d x - a C \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] + \right. \right. \right. \\
 \left. \left. \left. a C \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] \right) \sqrt{(\cos [c] - i \sin [c])^2} + \right. \right. \\
 \left. \left. 2 (A b^2 + a (-b B + a C)) \operatorname{ArcTan} \left[ \frac{(i \cos [c] + \sin [c]) (a \sin [c] + (-b + a \cos [c]) \tan \left[ \frac{d x}{2} \right])}{\sqrt{a^2 - b^2} \sqrt{(\cos [c] - i \sin [c])^2}} \right] \right) \right) \\
 \left. \left. \left. (i \cos [c] + \sin [c]) \right) \right) \right) / \\
 \left( a b \sqrt{a^2 - b^2} d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 (c + d x)]) \sqrt{(\cos [c] - i \sin [c])^2} \right)$$

### Problem 908: Result more than twice size of optimal antiderivative.

$$\int \frac{\sec [c + d x]^4 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{(a + b \sec [c + d x])^2} dx$$

Optimal (type 3, 407 leaves, 9 steps):

$$\frac{(6 a^2 b B + b^3 B - 8 a^3 C - 2 a b^2 (2 A + C)) \operatorname{ArcTanh}[\sin [c + d x]]}{2 b^5 d} + \\
 \left( 2 a^2 (2 a^2 A b^2 - 3 A b^4 - 3 a^3 b B + 4 a b^3 B + 4 a^4 C - 5 a^2 b^2 C) \operatorname{ArcTanh} \left[ \frac{\sqrt{a - b} \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a + b}} \right] \right) / \\
 \left( (a - b)^{3/2} b^5 (a + b)^{3/2} d \right) - \frac{1}{3 b^4 (a^2 - b^2) d} \\
 \frac{(9 a^3 b B - 6 a b^3 B - a^2 b^2 (6 A - 7 C) - 12 a^4 C + b^4 (3 A + 2 C)) \tan [c + d x] + (3 a^2 b B - b^3 B - 2 a b^2 (A - C) - 4 a^3 C) \sec [c + d x] \tan [c + d x]}{2 b^3 (a^2 - b^2) d} + \\
 \frac{(3 A b^2 - 3 a b B + 4 a^2 C - b^2 C) \sec [c + d x]^2 \tan [c + d x]}{3 b^2 (a^2 - b^2) d} - \\
 \frac{(A b^2 - a (b B - a C)) \sec [c + d x]^3 \tan [c + d x]}{b (a^2 - b^2) d (a + b \sec [c + d x])}$$

Result (type 3, 973 leaves):

$$\begin{aligned}
& - \left( \left( 4 a^2 (-2 a^2 A b^2 + 3 A b^4 + 3 a^3 b B - 4 a b^3 B - 4 a^4 C + 5 a^2 b^2 C) \operatorname{ArcTanh} \left[ \frac{(-a+b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}{\sqrt{a^2-b^2}} \right] \right. \right. \\
& \quad \left. \left. (b+a \operatorname{Cos}[c+dx])^2 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) \right) / \\
& \quad \left( b^5 \sqrt{a^2-b^2} (-a^2+b^2) d (A+2C+2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) (a+b \operatorname{Sec}[c+dx])^2 \right) + \\
& \quad \left( 4 a A b^2 - 6 a^2 b B - b^3 B + 8 a^3 C + 2 a b^2 C \right) (b+a \operatorname{Cos}[c+dx])^2 \\
& \quad \operatorname{Log} \left[ \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right] - \operatorname{Sin} \left[ \frac{1}{2} (c+dx) \right] \right] (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
& \quad \left( b^5 d (A+2C+2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) (a+b \operatorname{Sec}[c+dx])^2 \right) + \\
& \quad \left( -4 a A b^2 + 6 a^2 b B + b^3 B - 8 a^3 C - 2 a b^2 C \right) (b+a \operatorname{Cos}[c+dx])^2 \\
& \quad \operatorname{Log} \left[ \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right] + \operatorname{Sin} \left[ \frac{1}{2} (c+dx) \right] \right] (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
& \quad \left( b^5 d (A+2C+2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) (a+b \operatorname{Sec}[c+dx])^2 \right) + \\
& \quad \left( (b+a \operatorname{Cos}[c+dx]) \operatorname{Sec}[c+dx]^3 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right. \\
& \quad \left. (-6 a^2 A b^3 \operatorname{Sin}[c+dx] + 6 A b^5 \operatorname{Sin}[c+dx] + 9 a^3 b^2 B \operatorname{Sin}[c+dx] - 9 a b^4 B \operatorname{Sin}[c+dx] - \right. \\
& \quad \left. 12 a^4 b C \operatorname{Sin}[c+dx] + 12 b^5 C \operatorname{Sin}[c+dx] - 12 a^3 A b^2 \operatorname{Sin}[2(c+dx)] + \right. \\
& \quad \left. 6 a A b^4 \operatorname{Sin}[2(c+dx)] + 18 a^4 b B \operatorname{Sin}[2(c+dx)] - 18 a^2 b^3 B \operatorname{Sin}[2(c+dx)] + \right. \\
& \quad \left. 6 b^5 B \operatorname{Sin}[2(c+dx)] - 24 a^5 C \operatorname{Sin}[2(c+dx)] + 22 a^3 b^2 C \operatorname{Sin}[2(c+dx)] - \right. \\
& \quad \left. 4 a b^4 C \operatorname{Sin}[2(c+dx)] - 6 a^2 A b^3 \operatorname{Sin}[3(c+dx)] + 6 A b^5 \operatorname{Sin}[3(c+dx)] + \right. \\
& \quad \left. 9 a^3 b^2 B \operatorname{Sin}[3(c+dx)] - 9 a b^4 B \operatorname{Sin}[3(c+dx)] - 12 a^4 b C \operatorname{Sin}[3(c+dx)] + \right. \\
& \quad \left. 8 a^2 b^3 C \operatorname{Sin}[3(c+dx)] + 4 b^5 C \operatorname{Sin}[3(c+dx)] - 6 a^3 A b^2 \operatorname{Sin}[4(c+dx)] + \right. \\
& \quad \left. 3 a A b^4 \operatorname{Sin}[4(c+dx)] + 9 a^4 b B \operatorname{Sin}[4(c+dx)] - 6 a^2 b^3 B \operatorname{Sin}[4(c+dx)] - \right. \\
& \quad \left. 12 a^5 C \operatorname{Sin}[4(c+dx)] + 7 a^3 b^2 C \operatorname{Sin}[4(c+dx)] + 2 a b^4 C \operatorname{Sin}[4(c+dx)] \right) \right) / \\
& \quad \left( 12 b^4 (-a^2+b^2) d (A+2C+2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) (a+b \operatorname{Sec}[c+dx])^2 \right)
\end{aligned}$$

**Problem 910: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c+dx]^2 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2)}{(a+b \operatorname{Sec}[c+dx])^2} dx$$

Optimal (type 3, 177 leaves, 7 steps):

$$\begin{aligned}
& \frac{(bB-2aC) \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{b^3 d} - \\
& \frac{2 (A b^4 + a^3 b B - 2 a b^3 B - 2 a^4 C + 3 a^2 b^2 C) \operatorname{ArcTanh} \left[ \frac{\sqrt{a-b} \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}{\sqrt{a+b}} \right]}{(a-b)^{3/2} b^3 (a+b)^{3/2} d} + \\
& \frac{C \operatorname{Tan}[c+dx]}{b^2 d} + \frac{a (A b^2 - a (bB - aC)) \operatorname{Tan}[c+dx]}{b^2 (a^2 - b^2) d (a+b \operatorname{Sec}[c+dx])}
\end{aligned}$$

Result (type 3, 382 leaves):

$$\left( \frac{1}{2} \left( \frac{b^3 d (A + 2C + 2B \cos[c + dx] + A \cos[2(c + dx)]) (a + b \sec[c + dx])^2}{(b + a \cos[c + dx]) (A + B \sec[c + dx] + C \sec[c + dx]^2)} \right) \right. \\ \left. \left( \frac{1}{(a^2 - b^2)^{3/2}} 2 (A b^4 + a (a^2 b B - 2 b^3 B - 2 a^3 C + 3 a b^2 C)) \operatorname{ArcTanh} \left[ \frac{(-a + b) \tan\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 - b^2}} \right] \right. \right. \\ \left. \left. (b + a \cos[c + dx]) - (b B - 2 a C) (b + a \cos[c + dx]) \right. \right. \\ \left. \left. \operatorname{Log} \left[ \cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right] + (b B - 2 a C) (b + a \cos[c + dx]) \right. \right. \\ \left. \left. \operatorname{Log} \left[ \cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right] + \frac{b C (b + a \cos[c + dx]) \sin\left[\frac{1}{2}(c + dx)\right]}{\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]} + \right. \right. \\ \left. \left. \frac{b C (b + a \cos[c + dx]) \sin\left[\frac{1}{2}(c + dx)\right]}{\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]} + \frac{a b (A b^2 + a (-b B + a C)) \sin[c + dx]}{(a - b) (a + b)} \right) \right)$$

**Problem 911: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\sec[c + dx] (A + B \sec[c + dx] + C \sec[c + dx]^2)}{(a + b \sec[c + dx])^2} dx$$

Optimal (type 3, 148 leaves, 6 steps):

$$\frac{C \operatorname{ArcTanh}[\sin[c + dx]]}{b^2 d} + \\ \frac{2 (a A b^2 - b^3 B - a^3 C + 2 a b^2 C) \operatorname{ArcTanh} \left[ \frac{\sqrt{a-b} \tan\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a+b}} \right]}{(a - b)^{3/2} b^2 (a + b)^{3/2} d} - \frac{(A b^2 - a (b B - a C)) \tan[c + dx]}{b (a^2 - b^2) d (a + b \sec[c + dx])}$$

Result (type 3, 356 leaves):

$$\begin{aligned}
& \left( \frac{1}{2} \left( b^2 d (A + 2C + 2B \cos[c + dx] + A \cos[2(c + dx)]) (a + b \sec[c + dx])^2 \right) \right. \\
& \left. - C (b + a \cos[c + dx]) \log \left[ \cos \left[ \frac{1}{2} (c + dx) \right] - \sin \left[ \frac{1}{2} (c + dx) \right] \right] + \right. \\
& \left. C (b + a \cos[c + dx]) \log \left[ \cos \left[ \frac{1}{2} (c + dx) \right] + \sin \left[ \frac{1}{2} (c + dx) \right] \right] + \left( 2 (b^3 B + a^3 C - a b^2 (A + 2C)) \right. \right. \\
& \left. \left. \operatorname{ArcTan} \left[ \frac{(i \cos[c] + \sin[c]) (a \sin[c] + (-b + a \cos[c]) \tan \left[ \frac{dx}{2} \right])}{\sqrt{a^2 - b^2} \sqrt{(\cos[c] - i \sin[c])^2}} \right] \right. \right. \\
& \left. \left. (b + a \cos[c + dx]) (i \cos[c] + \sin[c]) \right) \right] / \left( (a^2 - b^2)^{3/2} \sqrt{(\cos[c] - i \sin[c])^2} \right) + \\
& \left. \frac{b (A b^2 + a (-b B + a C)) (b \sin[c] - a \sin[dx])}{a (a - b) (a + b) \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right)} \right)
\end{aligned}$$

**Problem 912: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec[c + dx] + C \sec[c + dx]^2}{(a + b \sec[c + dx])^2} dx$$

Optimal (type 3, 138 leaves, 5 steps):

$$\frac{A x}{a^2} - \frac{2 (2 a^2 A b - A b^3 - a^3 B + a^2 b C) \operatorname{ArcTanh} \left[ \frac{\sqrt{a-b} \tan \left[ \frac{1}{2} (c + dx) \right]}{\sqrt{a+b}} \right]}{a^2 (a - b)^{3/2} (a + b)^{3/2} d} + \frac{(A b^2 - a (b B - a C)) \tan[c + dx]}{a (a^2 - b^2) d (a + b \sec[c + dx])}$$

Result (type 3, 299 leaves):

$$\begin{aligned}
 & \left( 2 (b + a \cos [c + d x]) (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \left. \left( A x (b + a \cos [c + d x]) - \left( 2 i (A b^3 + a^3 B - a^2 b (2 A + C)) \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{ArcTan} \left[ \frac{(i \cos [c] + \sin [c]) (a \sin [c] + (-b + a \cos [c]) \tan \left[ \frac{d x}{2} \right])}{\sqrt{a^2 - b^2} \sqrt{(\cos [c] - i \sin [c])^2}} \right] \right) \right) \right) \\
 & \quad \left. (b + a \cos [c + d x]) (\cos [c] - i \sin [c]) \right) \Bigg/ \left( (a^2 - b^2)^{3/2} d \sqrt{(\cos [c] - i \sin [c])^2} \right) + \\
 & \quad \left. \frac{(A b^2 + a (-b B + a C)) (-b \sin [c] + a \sin [d x])}{(a - b) (a + b) d (\cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right]) (\cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right])} \right) \Bigg/ \\
 & \left( a^2 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 (c + d x)]) (a + b \sec [c + d x])^2 \right)
 \end{aligned}$$

**Problem 916: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c + d x]^4 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{(a + b \sec [c + d x])^3} dx$$

Optimal (type 3, 465 leaves, 9 steps):

$$\begin{aligned}
 & \frac{(2 A b^2 - 6 a b B + 12 a^2 C + b^2 C) \operatorname{ArcTanh} [\sin [c + d x]]}{2 b^5 d} - \\
 & \left( a (6 A b^6 - 6 a^5 b B + 15 a^3 b^3 B - 12 a b^5 B + a^4 b^2 (2 A - 29 C) - 5 a^2 b^4 (A - 4 C) + 12 a^6 C) \right. \\
 & \quad \left. \operatorname{ArcTanh} \left[ \frac{\sqrt{a - b} \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a + b}} \right] \right) \Bigg/ \left( (a - b)^{5/2} b^5 (a + b)^{5/2} d \right) + \frac{1}{2 b^4 (a^2 - b^2)^2 d} \\
 & \quad (6 a^4 b B - 11 a^2 b^3 B + 2 b^5 B - a^3 b^2 (2 A - 21 C) + a b^4 (5 A - 6 C) - 12 a^5 C) \tan [c + d x] - \\
 & \quad \frac{1}{2 b^3 (a^2 - b^2)^2 d} (3 a^3 b B - 6 a b^3 B - a^2 b^2 (A - 10 C) + b^4 (4 A - C) - 6 a^4 C) \sec [c + d x] \tan [c + d x] - \\
 & \quad \frac{(A b^2 - a (b B - a C)) \sec [c + d x]^3 \tan [c + d x]}{2 b (a^2 - b^2) d (a + b \sec [c + d x])^2} + \\
 & \quad \left( (3 A b^4 + a (2 a^2 b B - 5 b^3 B - 4 a^3 C + 7 a b^2 C)) \sec [c + d x]^2 \tan [c + d x] \right) \Bigg/ \\
 & \quad \left( 2 b^2 (a^2 - b^2)^2 d (a + b \sec [c + d x]) \right)
 \end{aligned}$$

Result (type 3, 1124 leaves):

$$\begin{aligned}
& \left( 2 a \left( 2 a^4 A b^2 - 5 a^2 A b^4 + 6 A b^6 - 6 a^5 b B + 15 a^3 b^3 B - 12 a b^5 B + 12 a^6 C - 29 a^4 b^2 C + 20 a^2 b^4 C \right) \right. \\
& \quad \left. \operatorname{ArcTanh} \left[ \frac{(-a+b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}{\sqrt{a^2-b^2}} \right] (b+a \operatorname{Cos} [c+dx])^3 \right. \\
& \quad \left. \operatorname{Sec} [c+dx] (A+B \operatorname{Sec} [c+dx] + C \operatorname{Sec} [c+dx]^2) \right) / \\
& \quad \left( b^5 \sqrt{a^2-b^2} (-a^2+b^2)^2 d (A+2C+2B \operatorname{Cos} [c+dx] + A \operatorname{Cos} [2c+2dx]) (a+b \operatorname{Sec} [c+dx])^3 \right) + \\
& \quad \left( (-2Ab^2+6abB-12a^2C-b^2C) (b+a \operatorname{Cos} [c+dx])^3 \operatorname{Log} \left[ \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right] - \operatorname{Sin} \left[ \frac{1}{2} (c+dx) \right] \right] \right. \\
& \quad \left. \operatorname{Sec} [c+dx] (A+B \operatorname{Sec} [c+dx] + C \operatorname{Sec} [c+dx]^2) \right) / \\
& \quad \left( b^5 d (A+2C+2B \operatorname{Cos} [c+dx] + A \operatorname{Cos} [2c+2dx]) (a+b \operatorname{Sec} [c+dx])^3 \right) + \\
& \quad \left( (2Ab^2-6abB+12a^2C+b^2C) (b+a \operatorname{Cos} [c+dx])^3 \operatorname{Log} \left[ \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right] + \operatorname{Sin} \left[ \frac{1}{2} (c+dx) \right] \right] \right. \\
& \quad \left. \operatorname{Sec} [c+dx] (A+B \operatorname{Sec} [c+dx] + C \operatorname{Sec} [c+dx]^2) \right) / \\
& \quad \left( b^5 d (A+2C+2B \operatorname{Cos} [c+dx] + A \operatorname{Cos} [2c+2dx]) (a+b \operatorname{Sec} [c+dx])^3 \right) + \\
& \quad \left( (b+a \operatorname{Cos} [c+dx]) \operatorname{Sec} [c+dx]^3 (A+B \operatorname{Sec} [c+dx] + C \operatorname{Sec} [c+dx]^2) \right. \\
& \quad \left( -6a^4Ab^3 \operatorname{Sin} [c+dx] + 12a^2Ab^5 \operatorname{Sin} [c+dx] + 18a^5b^2B \operatorname{Sin} [c+dx] - 32a^3b^4B \operatorname{Sin} [c+dx] + \right. \\
& \quad \left. 8ab^6B \operatorname{Sin} [c+dx] - 36a^6bC \operatorname{Sin} [c+dx] + 72a^4b^3C \operatorname{Sin} [c+dx] - 38a^2b^5C \operatorname{Sin} [c+dx] + \right. \\
& \quad \left. 8b^7C \operatorname{Sin} [c+dx] - 4a^5Ab^2 \operatorname{Sin} [2(c+dx)] + 10a^3Ab^4 \operatorname{Sin} [2(c+dx)] + \right. \\
& \quad \left. 12a^6bB \operatorname{Sin} [2(c+dx)] - 14a^4b^3B \operatorname{Sin} [2(c+dx)] - 12a^2b^5B \operatorname{Sin} [2(c+dx)] + \right. \\
& \quad \left. 8b^7B \operatorname{Sin} [2(c+dx)] - 24a^7C \operatorname{Sin} [2(c+dx)] + 26a^5b^2C \operatorname{Sin} [2(c+dx)] + \right. \\
& \quad \left. 20a^3b^4C \operatorname{Sin} [2(c+dx)] - 16ab^6C \operatorname{Sin} [2(c+dx)] - 6a^4Ab^3 \operatorname{Sin} [3(c+dx)] + \right. \\
& \quad \left. 12a^2Ab^5 \operatorname{Sin} [3(c+dx)] + 18a^5b^2B \operatorname{Sin} [3(c+dx)] - 32a^3b^4B \operatorname{Sin} [3(c+dx)] + \right. \\
& \quad \left. 8ab^6B \operatorname{Sin} [3(c+dx)] - 36a^6bC \operatorname{Sin} [3(c+dx)] + 64a^4b^3C \operatorname{Sin} [3(c+dx)] - \right. \\
& \quad \left. 22a^2b^5C \operatorname{Sin} [3(c+dx)] - 2a^5Ab^2 \operatorname{Sin} [4(c+dx)] + 5a^3Ab^4 \operatorname{Sin} [4(c+dx)] + \right. \\
& \quad \left. 6a^6bB \operatorname{Sin} [4(c+dx)] - 11a^4b^3B \operatorname{Sin} [4(c+dx)] + 2a^2b^5B \operatorname{Sin} [4(c+dx)] - \right. \\
& \quad \left. 12a^7C \operatorname{Sin} [4(c+dx)] + 21a^5b^2C \operatorname{Sin} [4(c+dx)] - 6a^3b^4C \operatorname{Sin} [4(c+dx)] \right) / \\
& \quad \left. (8b^4(-a^2+b^2)^2 d (A+2C+2B \operatorname{Cos} [c+dx] + A \operatorname{Cos} [2c+2dx]) (a+b \operatorname{Sec} [c+dx])^3 \right)
\end{aligned}$$

**Problem 918: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec} [c+dx]^2 (A+B \operatorname{Sec} [c+dx] + C \operatorname{Sec} [c+dx]^2)}{(a+b \operatorname{Sec} [c+dx])^3} dx$$

Optimal (type 3, 242 leaves, 7 steps):



$$\frac{C \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{b^3 d} + \left( (a^2 b^3 B + 2 b^5 B - 2 a^5 C + 5 a^3 b^2 C - 3 a b^4 (A + 2 C)) \operatorname{ArcTanh}\left[\frac{\sqrt{a-b} \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}{\sqrt{a+b}}\right] \right) /$$

$$\left( (a-b)^{5/2} b^3 (a+b)^{5/2} d \right) + \frac{a (A b^2 - a (b B - a C)) \operatorname{Tan}[c + d x]}{2 b^2 (a^2 - b^2) d (a + b \operatorname{Sec}[c + d x])^2} +$$

$$\frac{(2 A b^4 + a^3 b B - 4 a b^3 B - 3 a^4 C + a^2 b^2 (A + 6 C)) \operatorname{Tan}[c + d x]}{2 b^2 (a^2 - b^2)^2 d (a + b \operatorname{Sec}[c + d x])}$$

Result(type 3, 1071 leaves):

$$\begin{aligned}
& - \left( \left( 2 C (b + a \cos [c + d x])^3 \right. \right. \\
& \quad \left. \left. \log \left[ \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right] \sec [c + d x] (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) \right) / \\
& \quad \left( b^3 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^3 \right) + \\
& \left( 2 C (b + a \cos [c + d x])^3 \log \left[ \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right] \sec [c + d x] \right. \\
& \quad \left. (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \\
& \quad \left( b^3 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^3 \right) + \\
& \left( -3 a A b^4 + a^2 b^3 B + 2 b^5 B - 2 a^5 C + 5 a^3 b^2 C - 6 a b^4 C \right) \\
& \quad (b + a \cos [c + d x])^3 \sec [c + d x] (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
& \quad \left( - \left( \left( 2 i \operatorname{ArcTan} \left[ \sec \left[ \frac{d x}{2} \right] \left( \frac{\cos [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} - \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. \frac{i \sin [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} \right) \right] (-i b \sin \left[ \frac{d x}{2} \right] + i a \sin \left[ c + \frac{d x}{2} \right]) \right) \right) \\
& \quad \left. \cos [c] \right) / \left( b^3 \sqrt{a^2 - b^2} d \sqrt{\cos [2 c] - i \sin [2 c]} \right) \right) - \\
& \quad \left( 2 \operatorname{ArcTan} \left[ \sec \left[ \frac{d x}{2} \right] \left( \frac{\cos [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} - \frac{i \sin [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} \right) \right] \right. \\
& \quad \left. (-i b \sin \left[ \frac{d x}{2} \right] + i a \sin \left[ c + \frac{d x}{2} \right]) \sin [c] \right) / \\
& \quad \left( b^3 \sqrt{a^2 - b^2} d \sqrt{\cos [2 c] - i \sin [2 c]} \right) \right) \right) / \\
& \quad \left( (-a^2 + b^2)^2 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^3 \right) + \\
& \quad \left( (b + a \cos [c + d x]) \sec [c] \sec [c + d x] (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
& \quad (-2 a^4 A b^2 \sin [c] - 5 a^2 A b^4 \sin [c] - 2 A b^6 \sin [c] + 3 a^3 b^3 B \sin [c] + 6 a b^5 B \sin [c] + \\
& \quad 2 a^6 C \sin [c] - a^4 b^2 C \sin [c] - 10 a^2 b^4 C \sin [c] + 5 a^3 A b^3 \sin [d x] + 4 a A b^5 \sin [d x] + \\
& \quad a^4 b^2 B \sin [d x] - 10 a^2 b^4 B \sin [d x] - 7 a^5 b C \sin [d x] + 16 a^3 b^3 C \sin [d x] - \\
& \quad 3 a^3 A b^3 \sin [2 c + d x] + a^4 b^2 B \sin [2 c + d x] + 2 a^2 b^4 B \sin [2 c + d x] + a^5 b C \sin [2 c + d x] - \\
& \quad 4 a^3 b^3 C \sin [2 c + d x] + 2 a^4 A b^2 \sin [c + 2 d x] + a^2 A b^4 \sin [c + 2 d x] - \\
& \quad \left. \left. 3 a^3 b^3 B \sin [c + 2 d x] - 2 a^6 C \sin [c + 2 d x] + 5 a^4 b^2 C \sin [c + 2 d x] \right) \right) / \\
& \quad \left( 2 a b^2 (-a^2 + b^2)^2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^3 \right)
\end{aligned}$$

**Problem 919: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c + d x] (A + B \sec [c + d x] + C \sec [c + d x]^2)}{(a + b \sec [c + d x])^3} dx$$

Optimal (type 3, 202 leaves, 6 steps):

$$\frac{(3 a b B - a^2 (2 A + C) - b^2 (A + 2 C)) \operatorname{ArcTanh}\left[\frac{\sqrt{a-b} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a+b}}\right]}{(a-b)^{5/2} (a+b)^{5/2} d} - \frac{(A b^2 - a (b B - a C)) \operatorname{Tan}[c+d x]}{2 b (a^2 - b^2) d (a+b \operatorname{Sec}[c+d x])^2} + \frac{(a^2 b B + 2 b^3 B + a^3 C - a b^2 (3 A + 4 C)) \operatorname{Tan}[c+d x]}{2 b (a^2 - b^2)^2 d (a+b \operatorname{Sec}[c+d x])}$$

Result (type 3, 800 leaves):

$$\left( (2 a^2 A + A b^2 - 3 a b B + a^2 C + 2 b^2 C) \right. \\
 (b + a \operatorname{Cos}[c+d x])^3 \operatorname{Sec}[c+d x] (A + B \operatorname{Sec}[c+d x] + C \operatorname{Sec}[c+d x])^2 \\
 \left. \left( - \left( \left( 2 i \operatorname{ArcTan}\left[\operatorname{Sec}\left[\frac{d x}{2}\right]\right] \left( \frac{\operatorname{Cos}[c]}{\sqrt{a^2 - b^2} \sqrt{\operatorname{Cos}[2 c] - i \operatorname{Sin}[2 c]}} - \frac{i \operatorname{Sin}[c]}{\sqrt{a^2 - b^2} \sqrt{\operatorname{Cos}[2 c] - i \operatorname{Sin}[2 c]}} \right) \left( -i b \operatorname{Sin}\left[\frac{d x}{2}\right] + i a \operatorname{Sin}\left[c + \frac{d x}{2}\right] \right) \right) \right) \right) \\
 \left. \operatorname{Cos}[c] \right) / \left( \sqrt{a^2 - b^2} d \sqrt{\operatorname{Cos}[2 c] - i \operatorname{Sin}[2 c]} \right) - \left( 2 \operatorname{ArcTan}\left[\operatorname{Sec}\left[\frac{d x}{2}\right]\right] \left( \frac{\operatorname{Cos}[c]}{\sqrt{a^2 - b^2} \sqrt{\operatorname{Cos}[2 c] - i \operatorname{Sin}[2 c]}} - \frac{i \operatorname{Sin}[c]}{\sqrt{a^2 - b^2} \sqrt{\operatorname{Cos}[2 c] - i \operatorname{Sin}[2 c]}} \right) \right. \\
 \left. \left( -i b \operatorname{Sin}\left[\frac{d x}{2}\right] + i a \operatorname{Sin}\left[c + \frac{d x}{2}\right] \right) \right) \\
 \left. \operatorname{Sin}[c] \right) / \left( \sqrt{a^2 - b^2} d \sqrt{\operatorname{Cos}[2 c] - i \operatorname{Sin}[2 c]} \right) \right) / \\
 \left( (-a^2 + b^2)^2 (A + 2 C + 2 B \operatorname{Cos}[c+d x] + A \operatorname{Cos}[2 c + 2 d x]) \right. \\
 (a + b \operatorname{Sec}[c+d x])^3 + \\
 (b + a \operatorname{Cos}[c+d x]) \operatorname{Sec}[c] \operatorname{Sec}[c+d x] \\
 (A + B \operatorname{Sec}[c+d x] + C \operatorname{Sec}[c+d x])^2 \\
 (4 a^4 A b \operatorname{Sin}[c] + 7 a^2 A b^3 \operatorname{Sin}[c] - 2 A b^5 \operatorname{Sin}[c] - 2 a^5 B \operatorname{Sin}[c] - 5 a^3 b^2 B \operatorname{Sin}[c] - \\
 2 a b^4 B \operatorname{Sin}[c] + 3 a^4 b C \operatorname{Sin}[c] + 6 a^2 b^3 C \operatorname{Sin}[c] - 11 a^3 A b^2 \operatorname{Sin}[d x] + 2 a A b^4 \operatorname{Sin}[d x] + \\
 5 a^4 b B \operatorname{Sin}[d x] + 4 a^2 b^3 B \operatorname{Sin}[d x] + a^5 C \operatorname{Sin}[d x] - 10 a^3 b^2 C \operatorname{Sin}[d x] + \\
 5 a^3 A b^2 \operatorname{Sin}[2 c + d x] - 2 a A b^4 \operatorname{Sin}[2 c + d x] - 3 a^4 b B \operatorname{Sin}[2 c + d x] + \\
 a^5 C \operatorname{Sin}[2 c + d x] + 2 a^3 b^2 C \operatorname{Sin}[2 c + d x] - 4 a^4 A b \operatorname{Sin}[c + 2 d x] + a^2 A b^3 \operatorname{Sin}[c + 2 d x] + \\
 2 a^5 B \operatorname{Sin}[c + 2 d x] + a^3 b^2 B \operatorname{Sin}[c + 2 d x] - 3 a^4 b C \operatorname{Sin}[c + 2 d x]) \right) / \\
 \left( 2 a^2 (a^2 - b^2)^2 d (A + 2 C + 2 B \operatorname{Cos}[c+d x] + A \operatorname{Cos}[2 c + 2 d x]) \right. \\
 \left. (a + b \operatorname{Sec}[c+d x])^3 \right)$$

**Problem 920: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \operatorname{Sec}[c+d x] + C \operatorname{Sec}[c+d x]^2}{(a + b \operatorname{Sec}[c+d x])^3} dx$$

Optimal (type 3, 229 leaves, 6 steps):

$$\frac{Ax}{a^3} + \left( (5a^2Ab^3 - 2Ab^5 + 2a^5B + a^3b^2B - 3a^4b(2A+C)) \operatorname{ArcTanh} \left[ \frac{\sqrt{a-b} \operatorname{Tan} \left[ \frac{1}{2}(c+dx) \right]}{\sqrt{a+b}} \right] \right) /$$

$$\left( a^3 (a-b)^{5/2} (a+b)^{5/2} d \right) + \frac{(Ab^2 - a(bB - aC)) \operatorname{Tan}[c+dx]}{2a(a^2 - b^2)d(a+b \operatorname{Sec}[c+dx])^2} -$$

$$\frac{(2Ab^4 + 3a^3bB - a^4C - a^2b^2(5A+2C)) \operatorname{Tan}[c+dx]}{2a^2(a^2 - b^2)^2d(a+b \operatorname{Sec}[c+dx])}$$

Result (type 3, 1093 leaves):

$$\left( (6a^4Ab - 5a^2Ab^3 + 2Ab^5 - 2a^5B - a^3b^2B + 3a^4bC) \right.$$

$$\left. (b + a \operatorname{Cos}[c+dx])^3 \operatorname{Sec}[c+dx] (A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right.$$

$$\left. \left( \left( 2i \operatorname{ArcTan} \left[ \operatorname{Sec} \left[ \frac{dx}{2} \right] \right] \left( \frac{\operatorname{Cos}[c]}{\sqrt{a^2 - b^2} \sqrt{\operatorname{Cos}[2c] - i \operatorname{Sin}[2c]}} - \frac{i \operatorname{Sin}[c]}{\sqrt{a^2 - b^2} \sqrt{\operatorname{Cos}[2c] - i \operatorname{Sin}[2c]}} \right) \right. \right. \right.$$

$$\left. \left. \left( -i b \operatorname{Sin} \left[ \frac{dx}{2} \right] + i a \operatorname{Sin} \left[ c + \frac{dx}{2} \right] \right) \right) \right.$$

$$\left. \operatorname{Cos}[c] \right) / \left( a^3 \sqrt{a^2 - b^2} d \sqrt{\operatorname{Cos}[2c] - i \operatorname{Sin}[2c]} \right) +$$

$$\left( 2 \operatorname{ArcTan} \left[ \operatorname{Sec} \left[ \frac{dx}{2} \right] \right] \left( \frac{\operatorname{Cos}[c]}{\sqrt{a^2 - b^2} \sqrt{\operatorname{Cos}[2c] - i \operatorname{Sin}[2c]}} - \frac{i \operatorname{Sin}[c]}{\sqrt{a^2 - b^2} \sqrt{\operatorname{Cos}[2c] - i \operatorname{Sin}[2c]}} \right) \right.$$

$$\left. \left( -i b \operatorname{Sin} \left[ \frac{dx}{2} \right] + i a \operatorname{Sin} \left[ c + \frac{dx}{2} \right] \right) \operatorname{Sin}[c] \right) /$$

$$\left( a^3 \sqrt{a^2 - b^2} d \sqrt{\operatorname{Cos}[2c] - i \operatorname{Sin}[2c]} \right) \left. \right) /$$

$$\left( (-a^2 + b^2)^2 (A + 2C + 2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c + 2dx]) \right.$$

$$\left. (a + b \operatorname{Sec}[c+dx])^3 \right) +$$

$$\left( (b + a \operatorname{Cos}[c+dx]) \operatorname{Sec}[c] \operatorname{Sec}[c+dx] (A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right.$$

$$\left( 2a^6Adx \operatorname{Cos}[c] - 6a^2Ab^4dx \operatorname{Cos}[c] + 4Ab^6dx \operatorname{Cos}[c] + 4a^5Abdx \operatorname{Cos}[dx] - \right.$$

$$8a^3Ab^3dx \operatorname{Cos}[dx] + 4aAb^5dx \operatorname{Cos}[dx] + 4a^5Abdx \operatorname{Cos}[2c+dx] -$$

$$8a^3Ab^3dx \operatorname{Cos}[2c+dx] + 4aAb^5dx \operatorname{Cos}[2c+dx] + a^6Adx \operatorname{Cos}[c+2dx] -$$

$$2a^4Ab^2dx \operatorname{Cos}[c+2dx] + a^2Ab^4dx \operatorname{Cos}[c+2dx] + a^6Adx \operatorname{Cos}[3c+2dx] -$$

$$2a^4Ab^2dx \operatorname{Cos}[3c+2dx] + a^2Ab^4dx \operatorname{Cos}[3c+2dx] - 6a^4Ab^2 \operatorname{Sin}[c] -$$

$$9a^2Ab^4 \operatorname{Sin}[c] + 6Ab^6 \operatorname{Sin}[c] + 4a^5bB \operatorname{Sin}[c] + 7a^3b^3B \operatorname{Sin}[c] - 2ab^5B \operatorname{Sin}[c] -$$

$$2a^6C \operatorname{Sin}[c] - 5a^4b^2C \operatorname{Sin}[c] - 2a^2b^4C \operatorname{Sin}[c] + 17a^3Ab^3 \operatorname{Sin}[dx] - 8aAb^5 \operatorname{Sin}[dx] -$$

$$11a^4b^2B \operatorname{Sin}[dx] + 2a^2b^4B \operatorname{Sin}[dx] + 5a^5bC \operatorname{Sin}[dx] + 4a^3b^3C \operatorname{Sin}[dx] -$$

$$7a^3Ab^3 \operatorname{Sin}[2c+dx] + 4aAb^5 \operatorname{Sin}[2c+dx] + 5a^4b^2B \operatorname{Sin}[2c+dx] - 2a^2b^4B \operatorname{Sin}[2c+dx] -$$

$$3a^5bC \operatorname{Sin}[2c+dx] + 6a^4Ab^2 \operatorname{Sin}[c+2dx] - 3a^2Ab^4 \operatorname{Sin}[c+2dx] -$$

$$4a^5bB \operatorname{Sin}[c+2dx] + a^3b^3B \operatorname{Sin}[c+2dx] + 2a^6C \operatorname{Sin}[c+2dx] + a^4b^2C \operatorname{Sin}[c+2dx] \left. \right) /$$

$$\left( 2a^3(a^2 - b^2)^2d(A + 2C + 2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c + 2dx]) (a + b \operatorname{Sec}[c+dx])^3 \right)$$

Problem 921: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x] \left(A+B \sec [c+d x]+C \sec [c+d x]^2\right)}{\left(a+b \sec [c+d x]\right)^3} d x$$

Optimal (type 3, 330 leaves, 7 steps):

$$\begin{aligned} & -\frac{(3 A b-a B) x}{a^4}-\left(\left(15 a^2 A b^4-6 A b^6+6 a^5 b B-5 a^3 b^3 B+2 a b^5 B-2 a^6 C-a^4 b^2(12 A+C)\right)\right. \\ & \left.\operatorname{ArcTanh}\left[\frac{\sqrt{a-b} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a+b}}\right]\right) / \left(a^4(a-b)^{5 / 2}(a+b)^{5 / 2} d\right)- \\ & \frac{\left(11 a^2 A b^2-6 A b^4-5 a^3 b B+2 a b^3 B-a^4(2 A-3 C)\right) \operatorname{Sin}[c+d x]}{2 a^3\left(a^2-b^2\right)^2 d}+ \\ & \frac{(A b^2-a(b B-a C)) \operatorname{Sin}[c+d x]}{2 a\left(a^2-b^2\right) d(a+b \sec [c+d x])^2}- \\ & \frac{\left(3 A b^4+4 a^3 b B-a b^3 B-2 a^4 C-a^2 b^2(6 A+C)\right) \operatorname{Sin}[c+d x]}{2 a^2\left(a^2-b^2\right)^2 d(a+b \sec [c+d x])} \end{aligned}$$

Result (type 3, 1015 leaves):

$$\begin{aligned}
& - \left( \left( 2 (3 A b - a B) x (b + a \cos [c + d x])^3 \sec [c + d x] (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \right. \\
& \quad \left. \left( a^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^3 \right) + \right. \\
& \quad \left( (12 a^4 A b^2 - 15 a^2 A b^4 + 6 A b^6 - 6 a^5 b B + 5 a^3 b^3 B - 2 a b^5 B + 2 a^6 C + a^4 b^2 C) \right. \\
& \quad \left. (b + a \cos [c + d x])^3 \sec [c + d x] (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
& \quad \left. \left( - \left( \left( 2 i \operatorname{ArcTan} \left[ \sec \left[ \frac{d x}{2} \right] \left( \frac{\cos [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} - \right. \right. \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. \frac{i \sin [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} \right) \left( -i b \sin \left[ \frac{d x}{2} \right] + i a \sin \left[ c + \frac{d x}{2} \right] \right) \right) \right) \right. \\
& \quad \left. \left. \cos [c] \right) / \left( a^4 \sqrt{a^2 - b^2} d \sqrt{\cos [2 c] - i \sin [2 c]} \right) \right) - \\
& \quad \left( 2 \operatorname{ArcTan} \left[ \sec \left[ \frac{d x}{2} \right] \left( \frac{\cos [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} - \frac{i \sin [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} \right) \right. \right. \\
& \quad \left. \left. \left( -i b \sin \left[ \frac{d x}{2} \right] + i a \sin \left[ c + \frac{d x}{2} \right] \right) \sin [c] \right) \right) / \\
& \quad \left. \left( a^4 \sqrt{a^2 - b^2} d \sqrt{\cos [2 c] - i \sin [2 c]} \right) \right) \right) / \\
& \quad \left( (-a^2 + b^2)^2 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
& \quad \left. (a + b \sec [c + d x])^3 \right) + \\
& \quad \left( (b + a \cos [c + d x]) \sec [c] \sec [c + d x] (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
& \quad \left. (-A b^5 \sin [c] + a b^4 B \sin [c] - a^2 b^3 C \sin [c] + \right. \\
& \quad \left. a A b^4 \sin [d x] - a^2 b^3 B \sin [d x] + a^3 b^2 C \sin [d x]) \right) / \\
& \quad \left( a^4 (a^2 - b^2) d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^3 \right) + \\
& \quad \left( (b + a \cos [c + d x])^2 \sec [c] \sec [c + d x] (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
& \quad \left. (9 a^2 A b^4 \sin [c] - 6 A b^6 \sin [c] - 7 a^3 b^3 B \sin [c] + 4 a b^5 B \sin [c] + \right. \\
& \quad \left. 5 a^4 b^2 C \sin [c] - 2 a^2 b^4 C \sin [c] - 8 a^3 A b^3 \sin [d x] + 5 a A b^5 \sin [d x] + \right. \\
& \quad \left. 6 a^4 b^2 B \sin [d x] - 3 a^2 b^4 B \sin [d x] - 4 a^5 b C \sin [d x] + a^3 b^3 C \sin [d x]) \right) / \\
& \quad \left( a^4 (a^2 - b^2)^2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^3 \right) + \\
& \quad \left( 2 A (b + a \cos [c + d x])^3 (A + B \sec [c + d x] + C \sec [c + d x]^2) \tan [c + d x] \right) / \\
& \quad \left. \left( a^3 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^3 \right) \right)
\end{aligned}$$

### Problem 922: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c + d x]^2 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{(a + b \sec [c + d x])^3} dx$$

Optimal (type 3, 453 leaves, 8 steps):

$$\begin{aligned}
 & \frac{(12 A b^2 - 6 a b B + a^2 (A + 2 C)) x}{2 a^5} - \\
 & \left( b (12 A b^6 - 12 a^5 b B + 15 a^3 b^3 B - 6 a b^5 B - a^2 b^4 (29 A - 2 C) + 5 a^4 b^2 (4 A - C) + 6 a^6 C) \right. \\
 & \quad \left. \text{ArcTanh} \left[ \frac{\sqrt{a-b} \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a+b}} \right] \right) / \left( a^5 (a-b)^{5/2} (a+b)^{5/2} d \right) - \frac{1}{2 a^4 (a^2 - b^2)^2 d} \\
 & \frac{(12 A b^5 - 2 a^5 B + 11 a^3 b^2 B - 6 a b^4 B + a^4 b (6 A - 5 C) - a^2 b^3 (21 A - 2 C)) \sin [c + d x] +}{2 a^3 (a^2 - b^2)^2 d} \\
 & \frac{1}{2 a^3 (a^2 - b^2)^2 d} (6 A b^4 + 6 a^3 b B - 3 a b^3 B + a^4 (A - 4 C) - a^2 b^2 (10 A - C)) \cos [c + d x] \sin [c + d x] + \\
 & \frac{(A b^2 - a (b B - a C)) \cos [c + d x] \sin [c + d x]}{2 a (a^2 - b^2) d (a + b \sec [c + d x])^2} + \\
 & \frac{(7 a^2 A b^2 - 4 A b^4 - 5 a^3 b B + 2 a b^3 B + 3 a^4 C) \cos [c + d x] \sin [c + d x]}{2 a^2 (a^2 - b^2)^2 d (a + b \sec [c + d x])}
 \end{aligned}$$

Result (type 3, 1150 leaves):

$$\left( b \left( 20 a^4 A b^2 - 29 a^2 A b^4 + 12 A b^6 - 12 a^5 b B + 15 a^3 b^3 B - 6 a b^5 B + 6 a^6 C - 5 a^4 b^2 C + 2 a^2 b^4 C \right) \right. \\ \left. \operatorname{ArcTanh} \left[ \frac{(-a+b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}{\sqrt{a^2-b^2}} \right] \right) / \\ \left( a^5 \sqrt{a^2-b^2} (-a^2+b^2)^2 d \right) + \frac{1}{16 a^5 (a^2-b^2)^2 d (b+a \operatorname{Cos} [c+dx])^2} \\ (4 a^8 A (c+dx) + 48 a^6 A b^2 (c+dx) - 12 a^4 A b^4 (c+dx) - 136 a^2 A b^6 (c+dx) + 96 A b^8 (c+dx) - \\ 24 a^7 b B (c+dx) + 72 a^3 b^5 B (c+dx) - 48 a b^7 B (c+dx) + 8 a^8 C (c+dx) - 24 a^4 b^4 C (c+dx) + \\ 16 a^2 b^6 C (c+dx) + 16 a^7 A b (c+dx) \operatorname{Cos} [c+dx] + 160 a^5 A b^3 (c+dx) \operatorname{Cos} [c+dx] - \\ 368 a^3 A b^5 (c+dx) \operatorname{Cos} [c+dx] + 192 a A b^7 (c+dx) \operatorname{Cos} [c+dx] - \\ 96 a^6 b^2 B (c+dx) \operatorname{Cos} [c+dx] + 192 a^4 b^4 B (c+dx) \operatorname{Cos} [c+dx] - \\ 96 a^2 b^6 B (c+dx) \operatorname{Cos} [c+dx] + 32 a^7 b C (c+dx) \operatorname{Cos} [c+dx] - 64 a^5 b^3 C (c+dx) \operatorname{Cos} [c+dx] + \\ 32 a^3 b^5 C (c+dx) \operatorname{Cos} [c+dx] + 4 a^8 A (c+dx) \operatorname{Cos} [2 (c+dx)] + \\ 40 a^6 A b^2 (c+dx) \operatorname{Cos} [2 (c+dx)] - 92 a^4 A b^4 (c+dx) \operatorname{Cos} [2 (c+dx)] + \\ 48 a^2 A b^6 (c+dx) \operatorname{Cos} [2 (c+dx)] - 24 a^7 b B (c+dx) \operatorname{Cos} [2 (c+dx)] + \\ 48 a^5 b^3 B (c+dx) \operatorname{Cos} [2 (c+dx)] - 24 a^3 b^5 B (c+dx) \operatorname{Cos} [2 (c+dx)] + \\ 8 a^8 C (c+dx) \operatorname{Cos} [2 (c+dx)] - 16 a^6 b^2 C (c+dx) \operatorname{Cos} [2 (c+dx)] + \\ 8 a^4 b^4 C (c+dx) \operatorname{Cos} [2 (c+dx)] - 8 a^7 A b \operatorname{Sin} [c+dx] - 32 a^5 A b^3 \operatorname{Sin} [c+dx] + \\ 160 a^3 A b^5 \operatorname{Sin} [c+dx] - 96 a A b^7 \operatorname{Sin} [c+dx] + 4 a^8 B \operatorname{Sin} [c+dx] + 8 a^6 b^2 B \operatorname{Sin} [c+dx] - \\ 84 a^4 b^4 B \operatorname{Sin} [c+dx] + 48 a^2 b^6 B \operatorname{Sin} [c+dx] + 40 a^5 b^3 C \operatorname{Sin} [c+dx] - 16 a^3 b^5 C \operatorname{Sin} [c+dx] + \\ 2 a^8 A \operatorname{Sin} [2 (c+dx)] - 48 a^6 A b^2 \operatorname{Sin} [2 (c+dx)] + 130 a^4 A b^4 \operatorname{Sin} [2 (c+dx)] - \\ 72 a^2 A b^6 \operatorname{Sin} [2 (c+dx)] + 16 a^7 b B \operatorname{Sin} [2 (c+dx)] - 64 a^5 b^3 B \operatorname{Sin} [2 (c+dx)] + \\ 36 a^3 b^5 B \operatorname{Sin} [2 (c+dx)] + 24 a^6 b^2 C \operatorname{Sin} [2 (c+dx)] - 12 a^4 b^4 C \operatorname{Sin} [2 (c+dx)] - \\ 8 a^7 A b \operatorname{Sin} [3 (c+dx)] + 16 a^5 A b^3 \operatorname{Sin} [3 (c+dx)] - 8 a^3 A b^5 \operatorname{Sin} [3 (c+dx)] + \\ 4 a^8 B \operatorname{Sin} [3 (c+dx)] - 8 a^6 b^2 B \operatorname{Sin} [3 (c+dx)] + 4 a^4 b^4 B \operatorname{Sin} [3 (c+dx)] + \\ a^8 A \operatorname{Sin} [4 (c+dx)] - 2 a^6 A b^2 \operatorname{Sin} [4 (c+dx)] + a^4 A b^4 \operatorname{Sin} [4 (c+dx)])$$

**Problem 923: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec} [c+dx]^4 (A+B \operatorname{Sec} [c+dx] + C \operatorname{Sec} [c+dx]^2)}{(a+b \operatorname{Sec} [c+dx])^4} dx$$

Optimal (type 3, 470 leaves, 9 steps):



$$\begin{aligned}
 & \frac{(b B - 4 a C) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{b^5 d} - \\
 & \left( (2 A b^8 + 2 a^7 b B - 7 a^5 b^3 B + 8 a^3 b^5 B - 8 a b^7 B - 8 a^8 C + 28 a^6 b^2 C - 35 a^4 b^4 C + a^2 b^6 (3 A + 20 C)) \right. \\
 & \quad \left. \operatorname{ArcTanh}\left[\frac{\sqrt{a-b} \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}{\sqrt{a+b}}\right] \right) / \left( (a-b)^{7/2} b^5 (a+b)^{7/2} d \right) - \\
 & \frac{(5 A b^4 + 3 a^3 b B - 8 a b^3 B - 12 a^4 C + 23 a^2 b^2 C - 6 b^4 C) \operatorname{Tan}[c + d x]}{6 b^4 (a^2 - b^2)^2 d} - \\
 & \frac{(A b^2 - a (b B - a C)) \operatorname{Sec}[c + d x]^3 \operatorname{Tan}[c + d x]}{3 b (a^2 - b^2) d (a + b \operatorname{Sec}[c + d x])^3} + \\
 & \left( (3 A b^4 + a^3 b B - 6 a b^3 B - 4 a^4 C + a^2 b^2 (2 A + 9 C)) \operatorname{Sec}[c + d x]^2 \operatorname{Tan}[c + d x] \right) / \\
 & \left( 6 b^2 (a^2 - b^2)^2 d (a + b \operatorname{Sec}[c + d x])^2 \right) + \\
 & \left( a (2 A b^6 - a^5 b B + 2 a^3 b^3 B - 6 a b^5 B + 4 a^6 C - 11 a^4 b^2 C + 3 a^2 b^4 (A + 4 C)) \operatorname{Tan}[c + d x] \right) / \\
 & \left( 2 b^4 (a^2 - b^2)^3 d (a + b \operatorname{Sec}[c + d x]) \right)
 \end{aligned}$$

Result (type 3, 1197 leaves):

$$\begin{aligned}
& - \left( \left( 2 \left( 3 a^2 A b^6 + 2 A b^8 + 2 a^7 b B - 7 a^5 b^3 B + 8 a^3 b^5 B - 8 a b^7 B - \right. \right. \right. \\
& \quad \left. \left. \left. 8 a^8 C + 28 a^6 b^2 C - 35 a^4 b^4 C + 20 a^2 b^6 C \right) \operatorname{ArcTanh} \left[ \frac{(-a+b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}{\sqrt{a^2-b^2}} \right] \right. \right. \\
& \quad \left. \left. \left. (b+a \operatorname{Cos}[c+dx])^4 \operatorname{Sec}[c+dx]^2 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) \right] / \right. \\
& \quad \left. \left( b^5 \sqrt{a^2-b^2} (-a^2+b^2)^3 d (A+2C+2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) (a+b \operatorname{Sec}[c+dx])^4 \right) \right) - \\
& \left( 2 (bB-4aC) (b+a \operatorname{Cos}[c+dx])^4 \operatorname{Log} \left[ \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right] - \operatorname{Sin} \left[ \frac{1}{2} (c+dx) \right] \right] \right. \\
& \quad \left. \operatorname{Sec}[c+dx]^2 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
& \left( b^5 d (A+2C+2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) (a+b \operatorname{Sec}[c+dx])^4 \right) + \\
& \left( 2 (bB-4aC) (b+a \operatorname{Cos}[c+dx])^4 \operatorname{Log} \left[ \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right] + \operatorname{Sin} \left[ \frac{1}{2} (c+dx) \right] \right] \right. \\
& \quad \left. \operatorname{Sec}[c+dx]^2 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
& \left( b^5 d (A+2C+2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) (a+b \operatorname{Sec}[c+dx])^4 \right) + \\
& \left( (b+a \operatorname{Cos}[c+dx]) \operatorname{Sec}[c+dx]^3 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right. \\
& \quad \left( -6 a^4 A b^5 \operatorname{Sin}[c+dx] - 54 a^2 A b^7 \operatorname{Sin}[c+dx] + 30 a^7 b^2 B \operatorname{Sin}[c+dx] - 90 a^5 b^4 B \operatorname{Sin}[c+dx] + \right. \\
& \quad 120 a^3 b^6 B \operatorname{Sin}[c+dx] - 120 a^8 b C \operatorname{Sin}[c+dx] + 294 a^6 b^3 C \operatorname{Sin}[c+dx] - \\
& \quad 174 a^4 b^5 C \operatorname{Sin}[c+dx] - 108 a^2 b^7 C \operatorname{Sin}[c+dx] + 48 b^9 C \operatorname{Sin}[c+dx] - \\
& \quad 16 a^5 A b^4 \operatorname{Sin}[2(c+dx)] - 2 a^3 A b^6 \operatorname{Sin}[2(c+dx)] - 72 a A b^8 \operatorname{Sin}[2(c+dx)] + \\
& \quad 12 a^8 b B \operatorname{Sin}[2(c+dx)] + 10 a^6 b^3 B \operatorname{Sin}[2(c+dx)] - 76 a^4 b^5 B \operatorname{Sin}[2(c+dx)] + \\
& \quad 144 a^2 b^7 B \operatorname{Sin}[2(c+dx)] - 48 a^9 C \operatorname{Sin}[2(c+dx)] - 40 a^7 b^2 C \operatorname{Sin}[2(c+dx)] + \\
& \quad 370 a^5 b^4 C \operatorname{Sin}[2(c+dx)] - 444 a^3 b^6 C \operatorname{Sin}[2(c+dx)] + 72 a b^8 C \operatorname{Sin}[2(c+dx)] - \\
& \quad 6 a^4 A b^5 \operatorname{Sin}[3(c+dx)] - 54 a^2 A b^7 \operatorname{Sin}[3(c+dx)] + 30 a^7 b^2 B \operatorname{Sin}[3(c+dx)] - \\
& \quad 90 a^5 b^4 B \operatorname{Sin}[3(c+dx)] + 120 a^3 b^6 B \operatorname{Sin}[3(c+dx)] - 120 a^8 b C \operatorname{Sin}[3(c+dx)] + \\
& \quad 342 a^6 b^3 C \operatorname{Sin}[3(c+dx)] - 318 a^4 b^5 C \operatorname{Sin}[3(c+dx)] + 36 a^2 b^7 C \operatorname{Sin}[3(c+dx)] - \\
& \quad 4 a^5 A b^4 \operatorname{Sin}[4(c+dx)] - 11 a^3 A b^6 \operatorname{Sin}[4(c+dx)] + 6 a^8 b B \operatorname{Sin}[4(c+dx)] - \\
& \quad 17 a^6 b^3 B \operatorname{Sin}[4(c+dx)] + 26 a^4 b^5 B \operatorname{Sin}[4(c+dx)] - 24 a^9 C \operatorname{Sin}[4(c+dx)] + \\
& \quad \left. \left. 68 a^7 b^2 C \operatorname{Sin}[4(c+dx)] - 65 a^5 b^4 C \operatorname{Sin}[4(c+dx)] + 6 a^3 b^6 C \operatorname{Sin}[4(c+dx)] \right) \right) / \\
& \left( 24 b^4 (-a^2+b^2)^3 d (A+2C+2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) (a+b \operatorname{Sec}[c+dx])^4 \right)
\end{aligned}$$

**Problem 924: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c+dx]^3 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2)}{(a+b \operatorname{Sec}[c+dx])^4} dx$$

Optimal (type 3, 358 leaves, 8 steps):

$$\begin{aligned}
 & \frac{C \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{b^4 d} - \left( (3 a^2 b^5 B + 2 b^7 B - a^3 b^4 (A - 8 C) + 2 a^7 C - 7 a^5 b^2 C - 4 a b^6 (A + 2 C)) \right. \\
 & \left. \operatorname{ArcTanh}\left[\frac{\sqrt{a-b} \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}{\sqrt{a+b}}\right] \right) / \left( (a-b)^{7/2} b^4 (a+b)^{7/2} d \right) - \\
 & \frac{(A b^2 - a (b B - a C)) \operatorname{Sec}[c + d x]^2 \operatorname{Tan}[c + d x]}{3 b (a^2 - b^2) d (a + b \operatorname{Sec}[c + d x])^3} - \\
 & \frac{a (2 A b^4 - 5 a b^3 B - 3 a^4 C + a^2 b^2 (3 A + 8 C)) \operatorname{Tan}[c + d x]}{6 b^3 (a^2 - b^2)^2 d (a + b \operatorname{Sec}[c + d x])^2} - \\
 & \frac{((4 A b^6 + a^3 b^3 B - 16 a b^5 B + 9 a^6 C + 2 a^2 b^4 (7 A + 17 C) - a^4 b^2 (3 A + 28 C)) \operatorname{Tan}[c + d x])}{(6 b^3 (a^2 - b^2)^3 d (a + b \operatorname{Sec}[c + d x]))} /
 \end{aligned}$$

Result (type 3, 1302 leaves):

$$\begin{aligned}
& - \left( \left( 2 C (b + a \cos [c + d x])^4 \operatorname{Log} \left[ \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right] \right. \right. \\
& \quad \left. \left. \operatorname{Sec} [c + d x]^2 (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) \right) \right) / \\
& \quad \left( b^4 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \operatorname{Sec} [c + d x])^4 \right) + \\
& \left( 2 C (b + a \cos [c + d x])^4 \operatorname{Log} \left[ \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right] \operatorname{Sec} [c + d x]^2 \right. \\
& \quad \left. (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) \right) / \\
& \quad \left( b^4 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \operatorname{Sec} [c + d x])^4 \right) + \\
& \left( -a^3 A b^4 - 4 a A b^6 + 3 a^2 b^5 B + 2 b^7 B + 2 a^7 C - 7 a^5 b^2 C + 8 a^3 b^4 C - 8 a b^6 C \right) \\
& \quad (b + a \cos [c + d x])^4 \operatorname{Sec} [c + d x]^2 (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) \\
& \quad \left( - \left( \left( 2 i \operatorname{ArcTan} \left[ \operatorname{Sec} \left[ \frac{d x}{2} \right] \left( \frac{\cos [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} - \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. \frac{i \sin [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} \right) \left( -i b \sin \left[ \frac{d x}{2} \right] + i a \sin \left[ c + \frac{d x}{2} \right] \right) \right] \right) \right. \\
& \quad \left. \left. \cos [c] \right) \right) / \left( b^4 \sqrt{a^2 - b^2} d \sqrt{\cos [2 c] - i \sin [2 c]} \right) \Bigg) - \\
& \quad \left( 2 \operatorname{ArcTan} \left[ \operatorname{Sec} \left[ \frac{d x}{2} \right] \left( \frac{\cos [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} - \frac{i \sin [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} \right) \right] \right. \\
& \quad \left. \left( -i b \sin \left[ \frac{d x}{2} \right] + i a \sin \left[ c + \frac{d x}{2} \right] \right) \sin [c] \right) \Bigg) / \\
& \quad \left( b^4 \sqrt{a^2 - b^2} d \sqrt{\cos [2 c] - i \sin [2 c]} \right) \Bigg) / \\
& \quad \left( (-a^2 + b^2)^3 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \operatorname{Sec} [c + d x])^4 \right) - \\
& \quad \left( 2 (b + a \cos [c + d x]) \operatorname{Sec} [c] \operatorname{Sec} [c + d x]^2 (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) \right. \\
& \quad \left. (A b^3 \sin [c] - a b^2 B \sin [c] + a^2 b C \sin [c] - a A b^2 \sin [d x] + a^2 b B \sin [d x] - a^3 C \sin [d x]) \right) / \\
& \quad \left( 3 a b (-a^2 + b^2) d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \operatorname{Sec} [c + d x])^4 \right) + \\
& \quad \left( (b + a \cos [c + d x])^2 \operatorname{Sec} [c] \operatorname{Sec} [c + d x]^2 (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) \right. \\
& \quad \left. (-5 a A b^3 \sin [c] + 2 a^2 b^2 B \sin [c] + 3 b^4 B \sin [c] + a^3 b C \sin [c] - 6 a b^3 C \sin [c] + \right. \\
& \quad \left. 3 a^2 A b^2 \sin [d x] + 2 A b^4 \sin [d x] - 5 a b^3 B \sin [d x] - 3 a^4 C \sin [d x] + 8 a^2 b^2 C \sin [d x]) \right) / \\
& \quad \left( 3 b^2 (-a^2 + b^2)^2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \operatorname{Sec} [c + d x])^4 \right) + \\
& \quad \left( (b + a \cos [c + d x])^3 \operatorname{Sec} [c] \operatorname{Sec} [c + d x]^2 (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) \right. \\
& \quad \left. (-3 a^3 A b^3 \sin [c] - 12 a A b^5 \sin [c] + 9 a^2 b^4 B \sin [c] + 6 b^6 B \sin [c] - 3 a^5 b C \sin [c] + \right. \\
& \quad \left. 6 a^3 b^3 C \sin [c] - 18 a b^5 C \sin [c] + 13 a^2 A b^4 \sin [d x] + 2 A b^6 \sin [d x] - 4 a^3 b^3 B \sin [d x] - \right. \\
& \quad \left. 11 a b^5 B \sin [d x] + 6 a^6 C \sin [d x] - 17 a^4 b^2 C \sin [d x] + 26 a^2 b^4 C \sin [d x]) \right) / \\
& \quad \left( 3 b^3 (-a^2 + b^2)^3 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \operatorname{Sec} [c + d x])^4 \right)
\end{aligned}$$

**Problem 926: Result unnecessarily involves complex numbers and more than**

twice size of optimal antiderivative.

$$\int \frac{\sec [c+d x] \left(A+B \sec [c+d x]+C \sec [c+d x]^2\right)}{\left(a+b \sec [c+d x]\right)^4} d x$$

Optimal (type 3, 299 leaves, 7 steps):

$$\begin{aligned} & - \left( \left( \left( 4 a^2 b B + b^3 B - a^3 (2 A + C) - a b^2 (3 A + 4 C) \right) \operatorname{ArcTanh} \left[ \frac{\sqrt{a-b} \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{\sqrt{a+b}} \right] \right) \right) / \\ & \left( (a-b)^{7/2} (a+b)^{7/2} d \right) - \frac{(A b^2 - a (b B - a C)) \operatorname{Tan}[c+d x]}{3 b (a^2 - b^2) d (a+b \sec [c+d x])^3} + \\ & \frac{(2 a^2 b B + 3 b^3 B + a^3 C - a b^2 (5 A + 6 C)) \operatorname{Tan}[c+d x]}{6 b (a^2 - b^2)^2 d (a+b \sec [c+d x])^2} + \\ & \left( (2 a^3 b B + 13 a b^3 B + a^4 C - 2 b^4 (2 A + 3 C) - a^2 b^2 (11 A + 10 C)) \operatorname{Tan}[c+d x] \right) / \\ & \left( 6 b (a^2 - b^2)^3 d (a+b \sec [c+d x]) \right) \end{aligned}$$

Result (type 3, 1069 leaves):

$$\begin{aligned}
& \left( (-2 a^3 A - 3 a A b^2 + 4 a^2 b B + b^3 B - a^3 C - 4 a b^2 C) \right. \\
& \quad (b + a \cos [c + d x])^4 \sec [c + d x]^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
& \quad \left( - \left( \left( 2 i \operatorname{ArcTan} \left[ \sec \left[ \frac{d x}{2} \right] \left( \frac{\cos [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} - \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. \frac{i \sin [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} \right) \left( -i b \sin \left[ \frac{d x}{2} \right] + i a \sin \left[ c + \frac{d x}{2} \right] \right) \right) \right) \\
& \quad \left. \cos [c] \right) / \left( \sqrt{a^2 - b^2} d \sqrt{\cos [2 c] - i \sin [2 c]} \right) - \\
& \quad \left( 2 \operatorname{ArcTan} \left[ \sec \left[ \frac{d x}{2} \right] \left( \frac{\cos [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} - \frac{i \sin [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} \right) \right. \right. \\
& \quad \left. \left. \left( -i b \sin \left[ \frac{d x}{2} \right] + i a \sin \left[ c + \frac{d x}{2} \right] \right) \right) \right) \\
& \quad \left. \sin [c] \right) / \left( \sqrt{a^2 - b^2} d \sqrt{\cos [2 c] - i \sin [2 c]} \right) \right) / \\
& \quad \left( (-a^2 + b^2)^3 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
& \quad \left. (a + b \sec [c + d x])^4 \right) + \\
& \quad \left( 2 (b + a \cos [c + d x]) \sec [c] \sec [c + d x]^2 \right. \\
& \quad \left. (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
& \quad \left. (A b^4 \sin [c] - a b^3 B \sin [c] + a^2 b^2 C \sin [c] - \right. \\
& \quad \left. a A b^3 \sin [d x] + a^2 b^2 B \sin [d x] - a^3 b C \sin [d x]) \right) / \\
& \quad \left( 3 a^3 (a^2 - b^2) d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
& \quad \left. (a + b \sec [c + d x])^4 \right) + \\
& \quad \left( (b + a \cos [c + d x])^2 \sec [c] \sec [c + d x]^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
& \quad \left. (-11 a^2 A b^3 \sin [c] + 6 A b^5 \sin [c] + 8 a^3 b^2 B \sin [c] - 3 a b^4 B \sin [c] - \right. \\
& \quad \left. 5 a^4 b C \sin [c] + 9 a^3 A b^2 \sin [d x] - 4 a A b^4 \sin [d x] - 6 a^4 b B \sin [d x] + \right. \\
& \quad \left. a^2 b^3 B \sin [d x] + 3 a^5 C \sin [d x] + 2 a^3 b^2 C \sin [d x]) \right) / \\
& \quad \left( 3 a^3 (a^2 - b^2)^2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^4 \right) + \\
& \quad \left( (b + a \cos [c + d x])^3 \sec [c] \sec [c + d x]^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
& \quad \left. (27 a^4 A b^2 \sin [c] - 18 a^2 A b^4 \sin [c] + 6 A b^6 \sin [c] - 12 a^5 b B \sin [c] - \right. \\
& \quad \left. 3 a^3 b^3 B \sin [c] + 3 a^6 C \sin [c] + 12 a^4 b^2 C \sin [c] - 18 a^5 A b \sin [d x] + \right. \\
& \quad \left. 5 a^3 A b^3 \sin [d x] - 2 a A b^5 \sin [d x] + 6 a^6 B \sin [d x] + 10 a^4 b^2 B \sin [d x] - \right. \\
& \quad \left. a^2 b^4 B \sin [d x] - 13 a^5 b C \sin [d x] - 2 a^3 b^3 C \sin [d x]) \right) / \\
& \quad \left. \left( 3 a^3 (a^2 - b^2)^3 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^4 \right) \right)
\end{aligned}$$

**Problem 927: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec [c + d x] + C \sec [c + d x]^2}{(a + b \sec [c + d x])^4} dx$$

Optimal (type 3, 336 leaves, 7 steps):

$$\frac{Ax}{a^4} - \left( (7a^2Ab^5 - 2Ab^7 - 2a^7B - 3a^5b^2B - a^4b^3(8A-C) + 4a^6b(2A+C)) \right. \\ \left. \text{ArcTanh}\left[\frac{\sqrt{a-b} \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a+b}}\right] \right) / (a^4(a-b)^{7/2}(a+b)^{7/2}d) + \\ \frac{(Ab^2 - a(bB - aC)) \tan[c+dx]}{3a(a^2 - b^2)d(a+b \sec[c+dx])^3} - \frac{(3Ab^4 + 5a^3bB - 2a^4C - a^2b^2(8A+3C)) \tan[c+dx]}{6a^2(a^2 - b^2)^2d(a+b \sec[c+dx])^2} - \\ \frac{((17a^2Ab^4 - 6Ab^6 + 11a^5bB + 4a^3b^3B - 2a^6C - 13a^4b^2(2A+C)) \tan[c+dx])}{(6a^3(a^2 - b^2)^3d(a+b \sec[c+dx]))}$$

Result (type 3, 1230 leaves):

$$\begin{aligned}
& \left( 2 A x (b + a \cos [c + d x])^4 \sec [c + d x]^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \\
& \left( a^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^4 \right) + \\
& \left( -8 a^6 A b + 8 a^4 A b^3 - 7 a^2 A b^5 + 2 A b^7 + 2 a^7 B + 3 a^5 b^2 B - 4 a^6 b C - a^4 b^3 C \right) \\
& \left( (b + a \cos [c + d x])^4 \sec [c + d x]^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
& \left. \left( \left( 2 i \operatorname{ArcTan} \left[ \sec \left[ \frac{d x}{2} \right] \left( \frac{\cos [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} - \frac{i \sin [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} \right) \right. \right. \right. \right. \\
& \left. \left. \left( -i b \sin \left[ \frac{d x}{2} \right] + i a \sin \left[ c + \frac{d x}{2} \right] \right) \cos [c] \right) \right) / \left( a^4 \sqrt{a^2 - b^2} d \right. \\
& \left. \sqrt{\cos [2 c] - i \sin [2 c]} \right) + \left( 2 \operatorname{ArcTan} \left[ \sec \left[ \frac{d x}{2} \right] \left( \frac{\cos [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} - \right. \right. \right. \\
& \left. \left. \frac{i \sin [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} \right) \right] \left( -i b \sin \left[ \frac{d x}{2} \right] + i a \sin \left[ c + \frac{d x}{2} \right] \right) \right] \\
& \left. \sin [c] \right) / \left( a^4 \sqrt{a^2 - b^2} d \sqrt{\cos [2 c] - i \sin [2 c]} \right) \left. \right) / \\
& \left( (-a^2 + b^2)^3 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^4 \right) - \\
& \left( 2 (b + a \cos [c + d x]) \sec [c] \sec [c + d x]^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
& \left. (A b^5 \sin [c] - a b^4 B \sin [c] + a^2 b^3 C \sin [c] - \right. \\
& \left. a A b^4 \sin [d x] + a^2 b^3 B \sin [d x] - a^3 b^2 C \sin [d x]) \right) / \\
& \left( 3 a^4 (a^2 - b^2) d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^4 \right) + \\
& \left( (b + a \cos [c + d x])^2 \sec [c] \sec [c + d x]^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
& \left. (14 a^2 A b^4 \sin [c] - 9 A b^6 \sin [c] - 11 a^3 b^3 B \sin [c] + 6 a b^5 B \sin [c] + \right. \\
& \left. 8 a^4 b^2 C \sin [c] - 3 a^2 b^4 C \sin [c] - 12 a^3 A b^3 \sin [d x] + 7 a A b^5 \sin [d x] + \right. \\
& \left. 9 a^4 b^2 B \sin [d x] - 4 a^2 b^4 B \sin [d x] - 6 a^5 b C \sin [d x] + a^3 b^3 C \sin [d x]) \right) / \\
& \left( 3 a^4 (a^2 - b^2)^2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^4 \right) + \\
& \left( (b + a \cos [c + d x])^3 \sec [c] \sec [c + d x]^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
& \left. (-48 a^4 A b^3 \sin [c] + 51 a^2 A b^5 \sin [c] - 18 A b^7 \sin [c] + 27 a^5 b^2 B \sin [c] - 18 a^3 b^4 B \sin [c] + \right. \\
& \left. 6 a b^6 B \sin [c] - 12 a^6 b C \sin [c] - 3 a^4 b^3 C \sin [c] + 36 a^5 A b^2 \sin [d x] - \right. \\
& \left. 32 a^3 A b^4 \sin [d x] + 11 a A b^6 \sin [d x] - 18 a^6 b B \sin [d x] + 5 a^4 b^3 B \sin [d x] - \right. \\
& \left. 2 a^2 b^5 B \sin [d x] + 6 a^7 C \sin [d x] + 10 a^5 b^2 C \sin [d x] - a^3 b^4 C \sin [d x]) \right) / \\
& \left( 3 a^4 (a^2 - b^2)^3 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^4 \right)
\end{aligned}$$

**Problem 928: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\cos [c + d x] (A + B \sec [c + d x] + C \sec [c + d x]^2)}{(a + b \sec [c + d x])^4} dx$$

Optimal (type 3, 471 leaves, 8 steps):



$$\begin{aligned}
 & - \frac{(4 A b - a B) x}{a^5} - \\
 & \left( (35 a^4 A b^4 - 28 a^2 A b^6 + 8 A b^8 + 8 a^7 b B - 8 a^5 b^3 B + 7 a^3 b^5 B - 2 a b^7 B - 2 a^8 C - a^6 b^2 (20 A + 3 C)) \right. \\
 & \left. \operatorname{ArcTanh}\left[\frac{\sqrt{a-b} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a+b}}\right] \right) / \left( a^5 (a-b)^{7/2} (a+b)^{7/2} d \right) + \frac{1}{6 a^4 (a^2-b^2)^3 d} \\
 & (68 a^2 A b^4 - 24 A b^6 + 26 a^5 b B - 17 a^3 b^3 B + 6 a b^5 B + a^6 (6 A - 11 C) - a^4 b^2 (65 A + 4 C)) \operatorname{Sin}[c+d x] + \\
 & \frac{(A b^2 - a (b B - a C)) \operatorname{Sin}[c+d x]}{3 a (a^2 - b^2) d (a + b \operatorname{Sec}[c+d x])^3} - \\
 & \frac{(4 A b^4 + 6 a^3 b B - a b^3 B - 3 a^4 C - a^2 b^2 (9 A + 2 C)) \operatorname{Sin}[c+d x]}{6 a^2 (a^2 - b^2)^2 d (a + b \operatorname{Sec}[c+d x])^2} - \\
 & \frac{((11 a^2 A b^4 - 4 A b^6 + 6 a^5 b B - 2 a^3 b^3 B + a b^5 B - 2 a^6 C - 3 a^4 b^2 (4 A + C)) \operatorname{Sin}[c+d x])}{(2 a^3 (a^2 - b^2)^3 d (a + b \operatorname{Sec}[c+d x]))} /
 \end{aligned}$$

Result(type 3, 1367 leaves):

$$\begin{aligned}
& - \left( \left( 2 (4 A b - a B) x (b + a \cos [c + d x])^4 \sec [c + d x]^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \right. \\
& \quad \left. \left( a^5 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^4 \right) + \right. \\
& \quad \left( -20 a^6 A b^2 + 35 a^4 A b^4 - 28 a^2 A b^6 + 8 A b^8 + 8 a^7 b B - 8 a^5 b^3 B + 7 a^3 b^5 B - 2 a b^7 B - 2 a^8 C - 3 a^6 b^2 C \right) \\
& \quad (b + a \cos [c + d x])^4 \sec [c + d x]^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
& \quad \left( - \left( \left( 2 i \operatorname{ArcTan} \left[ \sec \left[ \frac{d x}{2} \right] \left( \frac{\cos [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} - \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. \frac{i \sin [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} \right) \left( -i b \sin \left[ \frac{d x}{2} \right] + i a \sin \left[ c + \frac{d x}{2} \right] \right) \right) \right) \\
& \quad \left. \cos [c] \right) / \left( a^5 \sqrt{a^2 - b^2} d \sqrt{\cos [2 c] - i \sin [2 c]} \right) \left. \right) - \\
& \quad \left( 2 \operatorname{ArcTan} \left[ \sec \left[ \frac{d x}{2} \right] \left( \frac{\cos [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} - \frac{i \sin [c]}{\sqrt{a^2 - b^2} \sqrt{\cos [2 c] - i \sin [2 c]}} \right) \right. \right. \\
& \quad \left. \left. \left( -i b \sin \left[ \frac{d x}{2} \right] + i a \sin \left[ c + \frac{d x}{2} \right] \right) \sin [c] \right) \right) / \\
& \quad \left. \left( a^5 \sqrt{a^2 - b^2} d \sqrt{\cos [2 c] - i \sin [2 c]} \right) \right) \left. \right) / \\
& \quad \left( (-a^2 + b^2)^3 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
& \quad \left. (a + b \sec [c + d x])^4 \right) + \\
& \quad \left( 2 (b + a \cos [c + d x]) \sec [c] \sec [c + d x]^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
& \quad \left. (A b^6 \sin [c] - a b^5 B \sin [c] + a^2 b^4 C \sin [c] - \right. \\
& \quad \left. a A b^5 \sin [d x] + a^2 b^4 B \sin [d x] - a^3 b^3 C \sin [d x]) \right) / \\
& \quad \left( 3 a^5 (a^2 - b^2) d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^4 \right) + \\
& \quad \left( (b + a \cos [c + d x])^2 \sec [c] \sec [c + d x]^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
& \quad \left. (-17 a^2 A b^5 \sin [c] + 12 A b^7 \sin [c] + 14 a^3 b^4 B \sin [c] - 9 a b^6 B \sin [c] - \right. \\
& \quad \left. 11 a^4 b^3 C \sin [c] + 6 a^2 b^5 C \sin [c] + 15 a^3 A b^4 \sin [d x] - 10 a A b^6 \sin [d x] - \right. \\
& \quad \left. 12 a^4 b^3 B \sin [d x] + 7 a^2 b^5 B \sin [d x] + 9 a^5 b^2 C \sin [d x] - 4 a^3 b^4 C \sin [d x]) \right) / \\
& \quad \left( 3 a^5 (a^2 - b^2)^2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^4 \right) + \\
& \quad \left( (b + a \cos [c + d x])^3 \sec [c] \sec [c + d x]^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
& \quad \left. (75 a^4 A b^4 \sin [c] - 96 a^2 A b^6 \sin [c] + 36 A b^8 \sin [c] - 48 a^5 b^3 B \sin [c] + 51 a^3 b^5 B \sin [c] - \right. \\
& \quad \left. 18 a b^7 B \sin [c] + 27 a^6 b^2 C \sin [c] - 18 a^4 b^4 C \sin [c] + 6 a^2 b^6 C \sin [c] - 60 a^5 A b^3 \sin [d x] + \right. \\
& \quad \left. 71 a^3 A b^5 \sin [d x] - 26 a A b^7 \sin [d x] + 36 a^6 b^2 B \sin [d x] - 32 a^4 b^4 B \sin [d x] + \right. \\
& \quad \left. 11 a^2 b^6 B \sin [d x] - 18 a^7 b C \sin [d x] + 5 a^5 b^3 C \sin [d x] - 2 a^3 b^5 C \sin [d x]) \right) / \\
& \quad \left( 3 a^5 (a^2 - b^2)^3 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^4 \right) + \\
& \quad \left( 2 A (b + a \cos [c + d x])^4 \sec [c + d x] (A + B \sec [c + d x] + C \sec [c + d x]^2) \tan [c + d x] \right) / \\
& \quad \left( a^4 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^4 \right)
\end{aligned}$$

**Problem 929: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\cos [c+d x]^2 (A+B \sec [c+d x]+C \sec [c+d x]^2)}{(a+b \sec [c+d x])^4} dx$$

Optimal (type 3, 648 leaves, 9 steps):

$$\begin{aligned} & \frac{(20 A b^2 - 8 a b B + a^2 (A + 2 C)) x}{2 a^6} + \\ & \left( b (20 A b^8 + 20 a^7 b B - 35 a^5 b^3 B + 28 a^3 b^5 B - 8 a b^7 B - a^2 b^6 (69 A - 2 C) - \right. \\ & \quad \left. 8 a^6 b^2 (5 A - C) + 7 a^4 b^4 (12 A - C) - 8 a^8 C) \operatorname{ArcTanh}\left[\frac{\sqrt{a-b} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a+b}}\right] \right) / \\ & \left( a^6 \sqrt{a-b} \sqrt{a+b} (a^2 - b^2)^3 d \right) + \frac{1}{6 a^5 (a^2 - b^2)^3 d} (60 A b^7 + 6 a^7 B - 65 a^5 b^2 B + 68 a^3 b^4 B - 24 a b^6 B + \\ & \quad a^4 b^3 (146 A - 17 C) - a^2 b^5 (167 A - 6 C) - a^6 (24 A b - 26 b C)) \operatorname{Sin}[c+d x] - \frac{1}{2 a^4 (a^2 - b^2)^3 d} \\ & (10 A b^6 - 12 a^5 b B + 11 a^3 b^3 B - 4 a b^5 B - a^6 (A - 6 C) + a^4 b^2 (23 A - 2 C) - a^2 b^4 (27 A - C)) \\ & \operatorname{Cos}[c+d x] \operatorname{Sin}[c+d x] + \frac{(A b^2 - a (b B - a C)) \operatorname{Cos}[c+d x] \operatorname{Sin}[c+d x]}{3 a (a^2 - b^2) d (a + b \sec [c+d x])^3} - \\ & \left( (5 A b^4 + 7 a^3 b B - 2 a b^3 B - 4 a^4 C - a^2 b^2 (10 A + C)) \operatorname{Cos}[c+d x] \operatorname{Sin}[c+d x] \right) / \\ & \left( 6 a^2 (a^2 - b^2)^2 d (a + b \sec [c+d x])^2 \right) + \\ & \left( (20 A b^6 - 27 a^5 b B + 20 a^3 b^3 B - 8 a b^5 B - a^2 b^4 (53 A - 2 C) + 12 a^6 C + a^4 b^2 (48 A + C)) \right. \\ & \quad \left. \operatorname{Cos}[c+d x] \operatorname{Sin}[c+d x] \right) / \left( 6 a^3 (a^2 - b^2)^3 d (a + b \sec [c+d x]) \right) \end{aligned}$$

Result (type 3, 658 leaves):

$$\frac{(a^2 A + 20 A b^2 - 8 a b B + 2 a^2 C) (c + d x)}{2 a^6 d} +$$

$$\left( b (-40 a^6 A b^2 + 84 a^4 A b^4 - 69 a^2 A b^6 + 20 A b^8 + 20 a^7 b B - 35 a^5 b^3 B + 28 a^3 b^5 B - 8 a b^7 B -$$

$$8 a^8 C + 8 a^6 b^2 C - 7 a^4 b^4 C + 2 a^2 b^6 C) \operatorname{ArcTanh} \left[ \frac{(-a+b) \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{\sqrt{a^2-b^2}} \right] \right) /$$

$$\left( a^6 \sqrt{a^2-b^2} (-a^2+b^2)^3 d \right) + \frac{(4 A b - a B) \left( -\frac{i \operatorname{Cos}[c+d x]}{2 a^5} - \frac{\operatorname{Sin}[c+d x]}{2 a^5} \right)}{d} +$$

$$\frac{(4 A b - a B) \left( \frac{i \operatorname{Cos}[c+d x]}{2 a^5} - \frac{\operatorname{Sin}[c+d x]}{2 a^5} \right)}{d} +$$

$$\frac{A b^6 \operatorname{Sin}[c+d x] - a b^5 B \operatorname{Sin}[c+d x] + a^2 b^4 C \operatorname{Sin}[c+d x]}{3 a^5 (a^2-b^2) d (b+a \operatorname{Cos}[c+d x])^3} +$$

$$\left( -18 a^2 A b^5 \operatorname{Sin}[c+d x] + 13 A b^7 \operatorname{Sin}[c+d x] + 15 a^3 b^4 B \operatorname{Sin}[c+d x] - 10 a b^6 B \operatorname{Sin}[c+d x] -$$

$$12 a^4 b^3 C \operatorname{Sin}[c+d x] + 7 a^2 b^5 C \operatorname{Sin}[c+d x] \right) / \left( 6 a^5 (a^2-b^2)^2 d (b+a \operatorname{Cos}[c+d x])^2 \right) +$$

$$\left( 90 a^4 A b^4 \operatorname{Sin}[c+d x] - 122 a^2 A b^6 \operatorname{Sin}[c+d x] + 47 A b^8 \operatorname{Sin}[c+d x] - 60 a^5 b^3 B \operatorname{Sin}[c+d x] +$$

$$71 a^3 b^5 B \operatorname{Sin}[c+d x] - 26 a b^7 B \operatorname{Sin}[c+d x] + 36 a^6 b^2 C \operatorname{Sin}[c+d x] - 32 a^4 b^4 C \operatorname{Sin}[c+d x] +$$

$$11 a^2 b^6 C \operatorname{Sin}[c+d x] \right) / \left( 6 a^5 (a^2-b^2)^3 d (b+a \operatorname{Cos}[c+d x]) \right) + \frac{A \operatorname{Sin} \left[ 2 (c+d x) \right]}{4 a^4 d}$$

**Problem 930: Result more than twice size of optimal antiderivative.**

$$\int \frac{a b B - a^2 C + b^2 B \operatorname{Sec}[c+d x] + b^2 C \operatorname{Sec}[c+d x]^2}{a+b \operatorname{Sec}[c+d x]} dx$$

Optimal (type 3, 24 leaves, 3 steps):

$$(b B - a C) x + \frac{b C \operatorname{ArcTanh}[\operatorname{Sin}[c+d x]]}{d}$$

Result (type 3, 81 leaves):

$$b B x - a C x - \frac{b C \operatorname{Log} \left[ \operatorname{Cos} \left[ \frac{c}{2} + \frac{d x}{2} \right] - \operatorname{Sin} \left[ \frac{c}{2} + \frac{d x}{2} \right] \right]}{d} + \frac{b C \operatorname{Log} \left[ \operatorname{Cos} \left[ \frac{c}{2} + \frac{d x}{2} \right] + \operatorname{Sin} \left[ \frac{c}{2} + \frac{d x}{2} \right] \right]}{d}$$

**Problem 934: Result more than twice size of optimal antiderivative.**

$$\int \frac{a b B - a^2 C + b^2 B \operatorname{Sec}[c+d x] + b^2 C \operatorname{Sec}[c+d x]^2}{(a+b \operatorname{Sec}[c+d x])^5} dx$$

Optimal (type 3, 336 leaves, 8 steps):

$$\frac{(bB - aC)x}{a^4} - \left( b(8a^6bB - 8a^4b^3B + 7a^2b^5B - 2b^7B - 10a^7C + 5a^5b^2C - 7a^3b^4C + 2ab^6C) \right. \\ \left. \operatorname{ArcTanh}\left[\frac{\sqrt{a-b} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a+b}}\right] \right) / \left( a^4(a-b)^{7/2}(a+b)^{7/2}d \right) + \\ \frac{b^2(bB - 2aC) \operatorname{Tan}[c+dx]}{3a(a^2 - b^2)d(a+b \operatorname{Sec}[c+dx])^3} + \frac{b^2(8a^2bB - 3b^3B - 13a^3C + 3ab^2C) \operatorname{Tan}[c+dx]}{6a^2(a^2 - b^2)^2d(a+b \operatorname{Sec}[c+dx])^2} + \\ (b^2(26a^4bB - 17a^2b^3B + 6b^5B - 37a^5C + 13a^3b^2C - 6ab^4C) \operatorname{Tan}[c+dx]) / \\ (6a^3(a^2 - b^2)^3d(a+b \operatorname{Sec}[c+dx]))$$

Result (type 3, 1287 leaves):

$$\left( b(-8a^6bB + 8a^4b^3B - 7a^2b^5B + 2b^7B + 10a^7C - 5a^5b^2C + 7a^3b^4C - 2ab^6C) \operatorname{ArcTanh}\left[ \frac{(-a+b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2 - b^2}} \right] (b+a \operatorname{Cos}[c+dx])^4 \operatorname{Sec}[c+dx]^3 (bB - aC + bC \operatorname{Sec}[c+dx]) \right) / \\ \left( a^4 \sqrt{a^2 - b^2} (-a^2 + b^2)^3 d (bC + bB \operatorname{Cos}[c+dx] - aC \operatorname{Cos}[c+dx]) (a+b \operatorname{Sec}[c+dx])^4 \right) + \\ \left( (b+a \operatorname{Cos}[c+dx]) \operatorname{Sec}[c+dx]^3 (bB - aC + bC \operatorname{Sec}[c+dx]) \right. \\ (36a^8b^2B(c+dx) - 84a^6b^4B(c+dx) + 36a^4b^6B(c+dx) + 36a^2b^8B(c+dx) - \\ 24b^{10}B(c+dx) - 36a^9bC(c+dx) + 84a^7b^3C(c+dx) - 36a^5b^5C(c+dx) - \\ 36a^3b^7C(c+dx) + 24ab^9C(c+dx) + 18a^9bB(c+dx) \operatorname{Cos}[c+dx] + 18a^7b^3B(c+dx) \\ \operatorname{Cos}[c+dx] - 162a^5b^5B(c+dx) \operatorname{Cos}[c+dx] + 198a^3b^7B(c+dx) \operatorname{Cos}[c+dx] - \\ 72a^9bB(c+dx) \operatorname{Cos}[c+dx] - 18a^{10}C(c+dx) \operatorname{Cos}[c+dx] - 18a^8b^2C(c+dx) \operatorname{Cos}[c+dx] + \\ 162a^6b^4C(c+dx) \operatorname{Cos}[c+dx] - 198a^4b^6C(c+dx) \operatorname{Cos}[c+dx] + \\ 72a^2b^8C(c+dx) \operatorname{Cos}[c+dx] + 36a^8b^2B(c+dx) \operatorname{Cos}[2(c+dx)] - \\ 108a^6b^4B(c+dx) \operatorname{Cos}[2(c+dx)] + 108a^4b^6B(c+dx) \operatorname{Cos}[2(c+dx)] - \\ 36a^2b^8B(c+dx) \operatorname{Cos}[2(c+dx)] - 36a^9bC(c+dx) \operatorname{Cos}[2(c+dx)] + \\ 108a^7b^3C(c+dx) \operatorname{Cos}[2(c+dx)] - 108a^5b^5C(c+dx) \operatorname{Cos}[2(c+dx)] + \\ 36a^3b^7C(c+dx) \operatorname{Cos}[2(c+dx)] + 6a^9bB(c+dx) \operatorname{Cos}[3(c+dx)] - \\ 18a^7b^3B(c+dx) \operatorname{Cos}[3(c+dx)] + 18a^5b^5B(c+dx) \operatorname{Cos}[3(c+dx)] - \\ 6a^3b^7B(c+dx) \operatorname{Cos}[3(c+dx)] - 6a^{10}C(c+dx) \operatorname{Cos}[3(c+dx)] + \\ 18a^8b^2C(c+dx) \operatorname{Cos}[3(c+dx)] - 18a^6b^4C(c+dx) \operatorname{Cos}[3(c+dx)] + \\ 6a^4b^6C(c+dx) \operatorname{Cos}[3(c+dx)] + 36a^7b^3B \operatorname{Sin}[c+dx] + 72a^5b^5B \operatorname{Sin}[c+dx] - \\ 57a^3b^7B \operatorname{Sin}[c+dx] + 24a^9bB \operatorname{Sin}[c+dx] - 54a^8b^2C \operatorname{Sin}[c+dx] - \\ 111a^6b^4C \operatorname{Sin}[c+dx] + 39a^4b^6C \operatorname{Sin}[c+dx] - 24a^2b^8C \operatorname{Sin}[c+dx] + \\ 120a^6b^4B \operatorname{Sin}[2(c+dx)] - 90a^4b^6B \operatorname{Sin}[2(c+dx)] + 30a^2b^8B \operatorname{Sin}[2(c+dx)] - \\ 174a^7b^3C \operatorname{Sin}[2(c+dx)] + 84a^5b^5C \operatorname{Sin}[2(c+dx)] - 30a^3b^7C \operatorname{Sin}[2(c+dx)] + \\ 36a^7b^3B \operatorname{Sin}[3(c+dx)] - 32a^5b^5B \operatorname{Sin}[3(c+dx)] + 11a^3b^7B \operatorname{Sin}[3(c+dx)] - \\ 54a^8b^2C \operatorname{Sin}[3(c+dx)] + 37a^6b^4C \operatorname{Sin}[3(c+dx)] - 13a^4b^6C \operatorname{Sin}[3(c+dx)]) \left. \right) / \\ (24a^4(a^2 - b^2)^3d(bC + bB \operatorname{Cos}[c+dx] - aC \operatorname{Cos}[c+dx]) (a+b \operatorname{Sec}[c+dx])^4)$$

**Problem 935: Attempted integration timed out after 120 seconds.**

$$\int \text{Sec}[c + d x]^3 \sqrt{a + b \text{Sec}[c + d x]} (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) dx$$

Optimal (type 4, 517 leaves, 7 steps):

$$\begin{aligned}
 & -\frac{1}{315 b^5 d} 2 (a - b) \sqrt{a + b} (24 a^3 b B + 57 a b^3 B - 16 a^4 C - 6 a^2 b^2 (7 A + 4 C) + 21 b^4 (9 A + 7 C)) \\
 & \quad \text{Cot}[c + d x] \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \\
 & \quad \sqrt{\frac{b(1 - \text{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \text{Sec}[c + d x])}{a - b}} - \frac{1}{315 b^4 d} \\
 & 2 (a - b) \sqrt{a + b} (12 a^2 b (2 B - C) - 16 a^3 C - 6 a b^2 (7 A - 3 B + 6 C) - 3 b^3 (63 A - 25 B + 49 C)) \\
 & \quad \text{Cot}[c + d x] \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \\
 & \quad \sqrt{\frac{b(1 - \text{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \text{Sec}[c + d x])}{a - b}} - \frac{1}{315 b^3 d} \\
 & 2 (12 a^2 b B - 75 b^3 B - 8 a^3 C - a b^2 (21 A + 13 C)) \sqrt{a + b \text{Sec}[c + d x]} \text{Tan}[c + d x] + \frac{1}{315 b^2 d} \\
 & 2 (63 A b^2 + 9 a b B - 6 a^2 C + 49 b^2 C) \text{Sec}[c + d x] \sqrt{a + b \text{Sec}[c + d x]} \text{Tan}[c + d x] + \\
 & \frac{2 (9 b B + a C) \text{Sec}[c + d x]^2 \sqrt{a + b \text{Sec}[c + d x]} \text{Tan}[c + d x]}{63 b d} + \\
 & \frac{2 C \text{Sec}[c + d x]^3 \sqrt{a + b \text{Sec}[c + d x]} \text{Tan}[c + d x]}{9 d}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 936: Attempted integration timed out after 120 seconds.**

$$\int \text{Sec}[c + d x]^2 \sqrt{a + b \text{Sec}[c + d x]} (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) dx$$

Optimal (type 4, 413 leaves, 6 steps):

$$\frac{1}{105 b^4 d} 2 (a-b) \sqrt{a+b} (14 a^2 b B - 63 b^3 B - 8 a^3 C - a b^2 (35 A + 19 C)) \operatorname{Cot}[c+d x]$$

$$\operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} -$$

$$\frac{1}{105 b^3 d} 2 (a-b) \sqrt{a+b} (35 A b^2 - b^2 (63 B - 25 C) + 8 a^2 C - a (14 b B - 6 b C)) \operatorname{Cot}[c+d x]$$

$$\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} +$$

$$\frac{2(35 A b^2 - 14 a b B + 8 a^2 C + 25 b^2 C) \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x]}{105 b^2 d} +$$

$$\frac{2(7 b B - 4 a C) (a+b \operatorname{Sec}[c+d x])^{3/2} \operatorname{Tan}[c+d x]}{35 b^2 d} +$$

$$\frac{2 C \operatorname{Sec}[c+d x] (a+b \operatorname{Sec}[c+d x])^{3/2} \operatorname{Tan}[c+d x]}{7 b d}$$

Result(type 1, 1 leaves):

???

### Problem 937: Attempted integration timed out after 120 seconds.

$$\int \operatorname{Sec}[c+d x] \sqrt{a+b \operatorname{Sec}[c+d x]} (A+B \operatorname{Sec}[c+d x] + C \operatorname{Sec}[c+d x]^2) dx$$

Optimal (type 4, 324 leaves, 5 steps):

$$-\frac{1}{15 b^3 d} 2 (a-b) \sqrt{a+b} (3 b^2 (5 A + 3 C) + a (5 b B - 2 a C)) \operatorname{Cot}[c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} +$$

$$\frac{1}{15 b^2 d} 2 (a-b) \sqrt{a+b} (15 A b - 5 b B + 2 a C + 9 b C) \operatorname{Cot}[c+d x]$$

$$\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} +$$

$$\frac{2(5 b B - 2 a C) \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x]}{15 b d} + \frac{2 C (a+b \operatorname{Sec}[c+d x])^{3/2} \operatorname{Tan}[c+d x]}{5 b d}$$

Result(type 1, 1 leaves):

???

### Problem 938: Result more than twice size of optimal antiderivative.

$$\int \sqrt{a+b \operatorname{Sec}[c+dx]} (A+B \operatorname{Sec}[c+dx]+C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 4, 366 leaves, 6 steps):

$$-\frac{1}{3b^2d} 2(a-b) \sqrt{a+b} (3bB+aC) \operatorname{Cot}[c+dx] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}} + \frac{1}{3bd}$$

$$2\sqrt{a+b} (3Ab+(a-b)(3B-C)) \operatorname{Cot}[c+dx] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}} - \frac{1}{d}$$

$$2A\sqrt{a+b} \operatorname{Cot}[c+dx] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}} + \frac{2C\sqrt{a+b \operatorname{Sec}[c+dx]} \operatorname{Tan}[c+dx]}{3d}$$

Result (type 4, 892 leaves):

$$-\left( \left( 4\sqrt{a+b \operatorname{Sec}[c+dx]} (A+B \operatorname{Sec}[c+dx]+C \operatorname{Sec}[c+dx]^2) \sqrt{\frac{1}{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \right. \right. \\ \left. \left( 3abB \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 3b^2B \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + a^2C \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\ \left. \left. abC \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - 6abB \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3 - 2a^2C \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3 + \right. \right. \\ \left. \left. 3abB \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 - 3b^2B \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 + a^2C \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 - \right. \right. \\ \left. \left. abC \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 + 6aAb \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \right. \right. \\ \left. \left. \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \right. \right. \\ \left. \left. 6aAb \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\ \left. \left. \right) \right)$$



$$\begin{aligned}
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & (a+b) (3bB+aC) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & b (a(-3A+3B+C) + b(3A+3B+C)) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \\
 & \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \Bigg) \Bigg) / \\
 & \left(3bd \sqrt{b+a \cos[c+dx]} (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \right. \\
 & \left. \sec[c+dx]^{5/2} \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^{3/2} \right. \\
 & \left. \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}} \right) \Bigg) + \\
 & \left(\cos[c+dx]^2 \sqrt{a+b \sec[c+dx]} (A+B \sec[c+dx] + C \sec[c+dx]^2) \right. \\
 & \left. \left(\frac{4(3bB+aC) \sin[c+dx]}{3b} + \frac{4}{3} C \tan[c+dx]\right) \Bigg) / \\
 & (d(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]))
 \end{aligned}$$

**Problem 939: Result more than twice size of optimal antiderivative.**

$$\int \cos[c+dx] \sqrt{a+b \sec[c+dx]} (A+B \sec[c+dx] + C \sec[c+dx]^2) dx$$

Optimal (type 4, 362 leaves, 6 steps):

$$\frac{1}{bd} (a-b) \sqrt{a+b} (A-2C) \cot[c+dx] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}} + \frac{1}{bd} \sqrt{a+b} (Ab+2bB+2aC-2bC) \cot[c+dx]$$

$$\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}}$$

$$\frac{1}{ad} \sqrt{a+b} (Ab+2aB) \cot[c+dx] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}} + \frac{A \sqrt{a+b \operatorname{Sec}[c+dx]} \sin[c+dx]}{d}$$

Result(type 4, 930 leaves):

$$\frac{2C \sqrt{a+b \operatorname{Sec}[c+dx]} \sin[c+dx]}{d} +$$

$$\left( \sqrt{a+b \operatorname{Sec}[c+dx]} \sqrt{\frac{1}{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \left( aA \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + Ab \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) - \right.$$

$$2aC \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - 2bC \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - 2aA \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3 + 4aC$$

$$\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3 + aA \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 - Ab \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 - 2aC \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 +$$

$$2bC \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 - 2Ab \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right]$$

$$\sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} -$$

$$4aB \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}$$

$$\sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} -$$

$$2Ab \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2$$

$$\sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} -$$

$$4aB \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2$$

$$\begin{aligned}
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & (a+b)(A-2C) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 2(Ab + a(B-C) - b(B+C)) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \\
 & \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \Bigg) \Bigg) / \\
 & \left( d \sqrt{b+a \cos[c+dx]} \sqrt{\sec[c+dx]} \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^{3/2} \right. \\
 & \left. \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}} \right)
 \end{aligned}$$

**Problem 940: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \cos[c+dx]^2 \sqrt{a+b \sec[c+dx]} (A+B \sec[c+dx] + C \sec[c+dx]^2) dx$$

Optimal (type 4, 435 leaves, 7 steps):

$$\frac{1}{4 a b d} (a-b) \sqrt{a+b} (A b+4 a B) \operatorname{Cot}[c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \frac{1}{4 a d}$$

$$\sqrt{a+b} (A b+2 a(A+2 B+4 C)) \operatorname{Cot}[c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \frac{1}{4 a^2 d} \sqrt{a+b} (A b^2-4 a b B-4 a^2(A+2 C))$$

$$\operatorname{Cot}[c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} +$$

$$\frac{(A b+4 a B) \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{4 a d} + \frac{A \operatorname{Cos}[c+d x] \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{2 d}$$

Result (type 4, 1842 leaves):

$$\frac{A \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[2(c+d x)]}{4 d} +$$

$$\left(\sqrt{a+b \operatorname{Sec}[c+d x]}\right) \left(-a A b \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] - A b^2 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] -\right.$$

$$4 a^2 \sqrt{\frac{-a+b}{a+b}} B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] - 4 a b \sqrt{\frac{-a+b}{a+b}} B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] +$$

$$2 a A b \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 + 8 a^2 \sqrt{\frac{-a+b}{a+b}} B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 -$$

$$a A b \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + A b^2 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 -$$

$$4 a^2 \sqrt{\frac{-a+b}{a+b}} B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + 4 a b \sqrt{\frac{-a+b}{a+b}} B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 +$$

$$8 i a^2 A \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right]$$

$$\begin{aligned}
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 2 i A b^2 \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & 8 i a b B \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & 16 i a^2 C \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & 8 i a^2 A \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 2 i A b^2 \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + 8 i a b B \\
 & \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + 16 i a^2 C
 \end{aligned}$$

$$\begin{aligned}
& \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& i (a-b) (Ab + 4aB) \text{EllipticE}\left[i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \\
& \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - 2i (a-b) (Ab + 2a(A+2C)) \\
& \text{EllipticF}\left[i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
& \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \Bigg) \Bigg) / \\
& \left(4a \sqrt{\frac{-a+b}{a+b}} d \sqrt{b+a \cos[c+dx]} \sqrt{\sec[c+dx]} \sqrt{\frac{1}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}} \right. \\
& \left. \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^{3/2} \right. \\
& \left. \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}} \right)
\end{aligned}$$

**Problem 941: Result more than twice size of optimal antiderivative.**

$$\int \cos[c+dx]^3 \sqrt{a+b \sec[c+dx]} (A+B \sec[c+dx] + C \sec[c+dx]^2) dx$$

Optimal (type 4, 538 leaves, 8 steps):

$$\begin{aligned}
 & -\frac{1}{24 a^2 b d} (a-b) \sqrt{a+b} (3 A b^2-6 a b B-8 a^2(2 A+3 C)) \operatorname{Cot}[c+d x] \operatorname{EllipticE}\left[\right. \\
 & \quad \left. \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} \\
 & \frac{1}{24 a^2 d} \sqrt{a+b} (3 A b^2-2 a b(A+3 B)-4 a^2(4 A+3 B+6 C)) \operatorname{Cot}[c+d x] \\
 & \quad \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} \\
 & \frac{1}{8 a^3 d} \sqrt{a+b} (A b^3+8 a^3 B-2 a b^2 B+4 a^2 b(A+2 C)) \operatorname{Cot}[c+d x] \\
 & \quad \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \quad \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} \\
 & \quad \frac{(3 A b^2-6 a b B-8 a^2(2 A+3 C)) \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{24 a^2 d} + \\
 & \quad \frac{(A b+6 a B) \operatorname{Cos}[c+d x] \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{12 a d} + \\
 & \quad \frac{A \operatorname{Cos}[c+d x]^2 \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{3 d}
 \end{aligned}$$

Result (type 4, 4114 leaves):

$$\begin{aligned}
 & \frac{1}{d} \sqrt{a+b \operatorname{Sec}[c+d x]} \left( \frac{1}{12} A \operatorname{Sin}[c+d x] + \frac{(A b+6 a B) \operatorname{Sin}[2(c+d x)]}{24 a} + \frac{1}{12} A \operatorname{Sin}[3(c+d x)] \right) + \\
 & \left( \left( \frac{7 A b}{12 \sqrt{b+a \operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]}} + \frac{a B}{2 \sqrt{b+a \operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]}} + \right. \right. \\
 & \quad \frac{b C}{\sqrt{b+a \operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]}} + \frac{a A \sqrt{\operatorname{Sec}[c+d x]}}{3 \sqrt{b+a \operatorname{Cos}[c+d x]}} - \\
 & \quad \frac{A b^2 \sqrt{\operatorname{Sec}[c+d x]}}{48 a \sqrt{b+a \operatorname{Cos}[c+d x]}} + \frac{3 b B \sqrt{\operatorname{Sec}[c+d x]}}{8 \sqrt{b+a \operatorname{Cos}[c+d x]}} + \frac{a C \sqrt{\operatorname{Sec}[c+d x]}}{2 \sqrt{b+a \operatorname{Cos}[c+d x]}} + \\
 & \quad \frac{a A \operatorname{Cos}[2(c+d x)] \sqrt{\operatorname{Sec}[c+d x]}}{3 \sqrt{b+a \operatorname{Cos}[c+d x]}} - \frac{A b^2 \operatorname{Cos}[2(c+d x)] \sqrt{\operatorname{Sec}[c+d x]}}{16 a \sqrt{b+a \operatorname{Cos}[c+d x]}} + \\
 & \quad \left. \left. \frac{b B \operatorname{Cos}[2(c+d x)] \sqrt{\operatorname{Sec}[c+d x]}}{8 \sqrt{b+a \operatorname{Cos}[c+d x]}} + \frac{a C \operatorname{Cos}[2(c+d x)] \sqrt{\operatorname{Sec}[c+d x]}}{2 \sqrt{b+a \operatorname{Cos}[c+d x]}} \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{a + b \operatorname{Sec}[c + d x]} \left( \left( (-3 A b^2 + 6 a b B + 8 a^2 (2 A + 3 C)) \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] \right. \right. \\
 & \left. \left. \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}} \right) / \left( 24 a^2 \sqrt{\frac{1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{1 - \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}} \right) + \right. \\
 & \left. \left( (a + b) (-3 A b^2 + 6 a b B + 8 a^2 (2 A + 3 C)) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right], \frac{a - b}{a + b}\right] - \right. \right. \\
 & \left. \left. 2 \left( a (-A b^2 + 12 a^2 B + 2 a b (7 A - 3 B + 12 C)) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right], \frac{a - b}{a + b}\right] + 3 (A b^3 + 8 a^3 B - 2 a b^2 B + 4 a^2 b (A + 2 C)) \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right], \frac{a - b}{a + b}\right] \right) \right) \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{a + b}} \\
 & \left. \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}} \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^4} \right) / \\
 & \left( 24 a^2 \sqrt{\frac{1}{1 - \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}} \left( b - b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^4 + a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 \right)^2 \right) \right) / \\
 & \left( d \sqrt{b + a \operatorname{Cos}[c + d x]} \sqrt{\operatorname{Sec}[c + d x]} \left( \left( (-3 A b^2 + 6 a b B + 8 a^2 (2 A + 3 C)) \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^2 \right. \right. \right. \\
 & \left. \left. \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}} \right) / \left( 48 a^2 \sqrt{\frac{1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{1 - \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}} \right) - \right. \\
 & \left. \left( (a + b) (-3 A b^2 + 6 a b B + 8 a^2 (2 A + 3 C)) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right], \frac{a - b}{a + b}\right] - \right. \right. \\
 & \left. \left. 2 \left( a (-A b^2 + 12 a^2 B + 2 a b (7 A - 3 B + 12 C)) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right], \frac{a - b}{a + b}\right] + 3 (A b^3 + 8 a^3 B - 2 a b^2 B + 4 a^2 b (A + 2 C)) \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right], \frac{a - b}{a + b}\right] \right) \right) \right)
 \end{aligned}$$



$$\begin{aligned}
 & \left. \left. \left. \frac{1}{2} (c+dx) \right] \right], \frac{a-b}{a+b} \right] \right) \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \\
 & \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^4} \\
 & \left( -2b \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^3 + \right. \\
 & \left. 2a \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \left( -1+\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Big/ \\
 & \left( 24a^2 \sqrt{\frac{1}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}} \left( b-b \tan\left[\frac{1}{2}(c+dx)\right]^4+a \left( -1+\tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right)^2 \right) - \\
 & \left( \left( (a+b) (-3Ab^2+6abB+8a^2(2A+3C)) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] - \right. \right. \\
 & \left. 2 \left( a(-Ab^2+12a^2B+2ab(7A-3B+12C)) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \right. \right. \right. \\
 & \left. \left. \frac{a-b}{a+b}\right] + 3(Ab^3+8a^3B-2ab^2B+4a^2b(A+2C)) \operatorname{EllipticPi}\left[ \right. \right. \\
 & \left. \left. -1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \left. \tan\left[\frac{1}{2}(c+dx)\right]^3 \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right. \\
 & \left. \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}} \right) \Big/ \\
 & \left( 24a^2 \sqrt{\frac{1}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^4} \right. \\
 & \left. \left( b-b \tan\left[\frac{1}{2}(c+dx)\right]^4+a \left( -1+\tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) \right) + \\
 & \left( \left( (a+b) (-3Ab^2+6abB+8a^2(2A+3C)) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] - \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& 2 \left( a (-A b^2 + 12 a^2 B + 2 a b (7 A - 3 B + 12 C)) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right]\right], \right. \\
& \quad \left. \frac{a-b}{a+b} \right) + 3 (A b^3 + 8 a^3 B - 2 a b^2 B + 4 a^2 b (A + 2 C)) \operatorname{EllipticPi}\left[ \right. \\
& \quad \left. -1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b} \right] \left. \right) \\
& \left( -a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + b \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] \right) \\
& \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}} \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^4} \left. \right) / \\
& \left( 48 a^2 (a+b) \sqrt{\frac{1}{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} \right. \\
& \quad \left. \left( b - b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^4 + a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \right)^2 \right) \right) - \\
& \frac{1}{48 a^2 \left( b - b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^4 + a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \right)^2 \right)} \\
& \left( (a+b) (-3 A b^2 + 6 a b B + 8 a^2 (2 A + 3 C)) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right]\right], \frac{a-b}{a+b} \right) - \\
& 2 \left( a (-A b^2 + 12 a^2 B + 2 a b (7 A - 3 B + 12 C)) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right]\right], \right. \\
& \quad \left. \frac{a-b}{a+b} \right) + 3 (A b^3 + 8 a^3 B - 2 a b^2 B + 4 a^2 b (A + 2 C)) \operatorname{EllipticPi}\left[ -1, \right. \\
& \quad \left. -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b} \right] \left. \right) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] \\
& \sqrt{\frac{1}{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} \\
& \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}} \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^4} - \\
& \left( (-3 A b^2 + 6 a b B + 8 a^2 (2 A + 3 C)) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] \right)
\end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}} \\
 & \left( \frac{\sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} + \left( \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right. \right. \\
 & \quad \left. \left. \left( 1+\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \left( 1-\tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) / \\
 & \left( 48 a^2 \left( \frac{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{3/2} + \left( (-3 A b^2+6 a b B+8 a^2(2 A+3 C)) \tan\left[\frac{1}{2}(c+dx)\right] \right. \right. \\
 & \quad \left. \left( -a \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + b \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) / \right. \\
 & \quad \left. \left( 1+\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \left( \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right. \right. \\
 & \quad \left. \left. \left( a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \left( 1+\tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) / \\
 & \left( 48 a^2 \sqrt{\frac{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}} + \right. \\
 & \left. \left( (a+b)(-3 A b^2+6 a b B+8 a^2(2 A+3 C)) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] - \right. \right. \\
 & \quad 2 \left( a(-A b^2+12 a^2 B+2 a b(7 A-3 B+12 C)) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \right. \right. \\
 & \quad \left. \left. \frac{a-b}{a+b}\right] + 3(A b^3+8 a^3 B-2 a b^2 B+4 a^2 b(A+2 C)) \operatorname{EllipticPi}\left[ \right. \right. \\
 & \quad \left. \left. -1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \right) \right) \\
 & \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^4} \\
 & \left( \left( -a \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + b \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) / \right. \\
 & \quad \left. \left( 1+\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \left( \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right. \right. \\
 & \quad \left. \left. \left( a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \left( 1+\tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) /
 \end{aligned}$$



**Problem 942: Attempted integration timed out after 120 seconds.**

$$\int \text{Sec}[c + dx]^3 (a + b \text{Sec}[c + dx])^{3/2} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) dx$$

Optimal (type 4, 628 leaves, 8 steps):

$$\begin{aligned} & -\frac{1}{3465 b^5 d} 2 (a - b) \sqrt{a + b} \\ & \quad (88 a^4 b B + 363 a^2 b^3 B + 1617 b^5 B - 48 a^5 C - 18 a^3 b^2 (11 A + 6 C) + 6 a b^4 (451 A + 348 C)) \\ & \quad \text{Cot}[c + dx] \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + dx]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \\ & \quad \sqrt{\frac{b(1 - \text{Sec}[c + dx])}{a + b}} \sqrt{-\frac{b(1 + \text{Sec}[c + dx])}{a - b}} - \frac{1}{3465 b^4 d} \\ & \quad 2 (a - b) \sqrt{a + b} (4 a^3 b (22 B - 9 C) - 48 a^4 C - 6 a^2 b^2 (33 A - 11 B + 24 C) + \\ & \quad \quad 3 b^4 (275 A - 539 B + 225 C) - 3 a b^3 (627 A - 143 B + 471 C)) \text{Cot}[c + dx] \\ & \quad \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + dx]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \sqrt{\frac{b(1 - \text{Sec}[c + dx])}{a + b}} \sqrt{-\frac{b(1 + \text{Sec}[c + dx])}{a - b}} - \\ & \quad \frac{1}{3465 b^3 d} 2 (44 a^3 b B - 968 a b^3 B - 24 a^4 C - 75 b^4 (11 A + 9 C) - 3 a^2 b^2 (33 A + 19 C)) \\ & \quad \sqrt{a + b \text{Sec}[c + dx]} \text{Tan}[c + dx] + \frac{1}{3465 b^2 d} \\ & \quad 2 (33 a^2 b B + 539 b^3 B - 18 a^3 C + 6 a b^2 (132 A + 101 C)) \text{Sec}[c + dx] \sqrt{a + b \text{Sec}[c + dx]} \text{Tan}[c + dx] + \\ & \quad \frac{1}{693 b d} 2 (99 A b^2 + 110 a b B + 3 a^2 C + 81 b^2 C) \text{Sec}[c + dx]^2 \sqrt{a + b \text{Sec}[c + dx]} \text{Tan}[c + dx] + \\ & \quad \frac{2 (11 b B + 3 a C) \text{Sec}[c + dx]^3 \sqrt{a + b \text{Sec}[c + dx]} \text{Tan}[c + dx]}{99 d} + \\ & \quad \frac{2 C \text{Sec}[c + dx]^3 (a + b \text{Sec}[c + dx])^{3/2} \text{Tan}[c + dx]}{11 d} \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 943: Attempted integration timed out after 120 seconds.**

$$\int \text{Sec}[c + dx]^2 (a + b \text{Sec}[c + dx])^{3/2} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) dx$$

Optimal (type 4, 505 leaves, 7 steps):

$$\begin{aligned}
& \frac{1}{315 b^4 d} \\
& 2 (a-b) \sqrt{a+b} \left( 18 a^3 b B - 246 a b^3 B - 8 a^4 C - 21 b^4 (9 A + 7 C) - 3 a^2 b^2 (21 A + 11 C) \right) \operatorname{Cot}[c+d x] \\
& \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \\
& \frac{1}{315 b^3 d} 2 (a-b) \sqrt{a+b} \left( 6 a^2 b (3 B-C) - 8 a^3 C - 3 a b^2 (21 A-57 B+13 C) + 3 b^3 (63 A-25 B+49 C) \right) \\
& \operatorname{Cot}[c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
& \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \frac{1}{315 b^2 d} \\
& 2 \left( 18 a^2 b B - 75 b^3 B - 8 a^3 C - 3 a b^2 (21 A+13 C) \right) \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x] + \\
& \frac{1}{315 b^2 d} 2 \left( 63 A b^2 - 18 a b B + 8 a^2 C + 49 b^2 C \right) (a+b \operatorname{Sec}[c+d x])^{3/2} \operatorname{Tan}[c+d x] + \\
& \frac{2(9 b B - 4 a C) (a+b \operatorname{Sec}[c+d x])^{5/2} \operatorname{Tan}[c+d x]}{63 b^2 d} + \\
& \frac{2 C \operatorname{Sec}[c+d x] (a+b \operatorname{Sec}[c+d x])^{5/2} \operatorname{Tan}[c+d x]}{9 b d}
\end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 944: Attempted integration timed out after 120 seconds.**

$$\int \operatorname{Sec}[c+d x] (a+b \operatorname{Sec}[c+d x])^{3/2} (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) dx$$

Optimal (type 4, 406 leaves, 6 steps):

$$\begin{aligned}
 & -\frac{1}{105 b^3 d} 2 (a-b) \sqrt{a+b} (21 a^2 b B + 63 b^3 B - 6 a^3 C + 2 a b^2 (70 A + 41 C)) \\
 & \quad \text{Cot}[c+d x] \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \text{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \quad \sqrt{\frac{b(1-\text{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\text{Sec}[c+d x])}{a-b}} + \frac{1}{105 b^2 d} \\
 & 2 (a-b) \sqrt{a+b} (6 a^2 C + 3 a b (35 A - 7 B + 19 C) - b^2 (35 A - 63 B + 25 C)) \text{Cot}[c+d x] \\
 & \quad \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \text{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\text{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\text{Sec}[c+d x])}{a-b}} + \\
 & \quad \frac{2 (35 A b^2 + 21 a b B - 6 a^2 C + 25 b^2 C) \sqrt{a+b \text{Sec}[c+d x]} \text{Tan}[c+d x]}{105 b d} + \\
 & \quad \frac{2 (7 b B - 2 a C) (a+b \text{Sec}[c+d x])^{3/2} \text{Tan}[c+d x]}{35 b d} + \frac{2 C (a+b \text{Sec}[c+d x])^{5/2} \text{Tan}[c+d x]}{7 b d}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 945: Result more than twice size of optimal antiderivative.**

$$\int (a+b \text{Sec}[c+d x])^{3/2} (A+B \text{Sec}[c+d x] + C \text{Sec}[c+d x]^2) dx$$

Optimal (type 4, 443 leaves, 7 steps):

$$\begin{aligned}
 & -\frac{1}{15 b^2 d} 2 (a-b) \sqrt{a+b} (15 A b^2 + 20 a b B + 3 a^2 C + 9 b^2 C) \text{Cot}[c+d x] \text{EllipticE}\left[ \right. \\
 & \quad \left. \text{ArcSin}\left[\frac{\sqrt{a+b \text{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\text{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\text{Sec}[c+d x])}{a-b}} + \\
 & \quad \frac{1}{15 b d} 2 \sqrt{a+b} (3 a^2 (5 B - C) + 2 a b (15 A - 10 B + 6 C) - b^2 (15 A - 5 B + 9 C)) \text{Cot}[c+d x] \\
 & \quad \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \text{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\text{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\text{Sec}[c+d x])}{a-b}} - \\
 & \quad \frac{1}{d} 2 a A \sqrt{a+b} \text{Cot}[c+d x] \text{EllipticPi}\left[\frac{a+b}{a}, \text{ArcSin}\left[\frac{\sqrt{a+b \text{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \quad \sqrt{\frac{b(1-\text{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\text{Sec}[c+d x])}{a-b}} + \\
 & \quad \frac{2 (5 b B + 3 a C) \sqrt{a+b \text{Sec}[c+d x]} \text{Tan}[c+d x]}{15 d} + \frac{2 C (a+b \text{Sec}[c+d x])^{3/2} \text{Tan}[c+d x]}{5 d}
 \end{aligned}$$

Result (type 4, 1192 leaves):

$$\begin{aligned}
& - \left( 4 (a + b \operatorname{Sec}[c + d x])^{3/2} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
& \sqrt{\frac{1}{1 - \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}} \left( 15 a A b^2 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] + 15 A b^3 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] + \right. \\
& 20 a^2 b B \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] + 20 a b^2 B \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] + 3 a^3 C \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] + \\
& 3 a^2 b C \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] + 9 a b^2 C \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] + 9 b^3 C \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] - \\
& 30 a A b^2 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^3 - 40 a^2 b B \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^3 - 6 a^3 C \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^3 - \\
& 18 a b^2 C \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^3 + 15 a A b^2 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^5 - 15 A b^3 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^5 + \\
& 20 a^2 b B \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^5 - 20 a b^2 B \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^5 + 3 a^3 C \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^5 - \\
& 3 a^2 b C \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^5 + 9 a b^2 C \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^5 - 9 b^3 C \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^5 + \\
& \left. 30 a^2 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right], \frac{a - b}{a + b}\right] \right. \\
& \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2} \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{a + b}} + \\
& \left. 30 a^2 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right], \frac{a - b}{a + b}\right] \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 \right. \\
& \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2} \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{a + b}} + \\
& \left. (a + b) (15 A b^2 + 20 a b B + 3 a^2 C + 9 b^2 C) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right], \frac{a - b}{a + b}\right] \right. \\
& \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2} \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2\right) \\
& \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{a + b}} - \\
& \left. b (3 a^2 (-5 A + 5 B + C) + 2 a b (15 A + 10 B + 6 C) + b^2 (15 A + 5 B + 9 C)) \right. \\
& \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right], \frac{a - b}{a + b}\right] \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2} \right)
\end{aligned}$$



$$\left( \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)^2 \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} \right) \left( \right.$$

$$\left. 15 b d (b + a \cos [c + d x])^{3/2} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right.$$

$$\left. \sec [c + d x]^{7/2} \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right)^{3/2}$$

$$\left. \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \right) \left( \right.$$

$$\left. \cos [c + d x]^3 (a + b \sec [c + d x])^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right.$$

$$\left. \left( \frac{4 (15 A b^2 + 20 a b B + 3 a^2 C + 9 b^2 C) \sin [c + d x]}{15 b} + \right. \right.$$

$$\left. \left. \frac{4}{15} \sec [c + d x] (5 b B \sin [c + d x] + 6 a C \sin [c + d x]) + \frac{4}{5} b C \sec [c + d x] \tan [c + d x] \right) \right) \left. \right) /$$

$$(d (b + a \cos [c + d x]) (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]))$$

**Problem 946: Result more than twice size of optimal antiderivative.**

$$\int \cos [c + d x] (a + b \sec [c + d x])^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 4, 426 leaves, 7 steps):

$$\frac{1}{3 b d} (a-b) \sqrt{a+b} (3 a A-6 b B-8 a C) \operatorname{Cot}[c+d x]$$

$$\operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} +$$

$$\frac{1}{3 b d} \sqrt{a+b} (a b(3 A+12 B-8 C)+6 a^2 C+2 b^2(3 A-3 B+C)) \operatorname{Cot}[c+d x]$$

$$\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} -$$

$$\frac{1}{d} \sqrt{a+b} (3 A b+2 a B) \operatorname{Cot}[c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} +$$

$$\frac{A(a+b \operatorname{Sec}[c+d x])^{3 / 2} \operatorname{Sin}[c+d x]}{d} - \frac{b(3 A-2 C) \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x]}{3 d}$$

Result (type 4, 1208 leaves):

$$\left(2(a+b \operatorname{Sec}[c+d x])^{3 / 2}(A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2)\right.$$

$$\sqrt{\frac{1}{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}}\left(3 a^2 A \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]+3 a A b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]-\right.$$

$$6 a b B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]-6 b^2 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]-8 a^2 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]-$$

$$8 a b C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]-6 a^2 A \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3+12 a b B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3+$$

$$16 a^2 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3+3 a^2 A \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5-3 a A b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5-$$

$$6 a b B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5+6 b^2 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5-8 a^2 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5+$$

$$8 a b C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5-18 a A b \operatorname{EllipticPi}\left[-1,-\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right]$$

$$\sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} -$$

$$12 a^2 B \operatorname{EllipticPi}\left[-1,-\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right]$$

$$\begin{aligned}
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 18 a A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 12 a^2 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + (a+b) \\
 & (3 a A - 6 b B - 8 a C) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 2 (2 a b (3 A - 3 B - 2 C) + 3 a^2 (B - C) - b^2 (3 A + 3 B + C)) \\
 & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) / \\
 & \left(3 d (b + a \cos[c+dx])^{3/2} (A + 2 C + 2 B \cos[c+dx] + A \cos[2c+2dx]) \right. \\
 & \left. \sec[c+dx]^{7/2} \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^{3/2} \right. \\
 & \left. \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}} \right) + \\
 & \left(\cos[c+dx]^3 (a+b \sec[c+dx])^{3/2} (A+B \sec[c+dx] + C \sec[c+dx]^2) \right. \\
 & \left. \left(\frac{4}{3} (3 b B + 4 a C) \sin[c+dx] + \frac{4}{3} b C \tan[c+dx]\right) \right) / \\
 & (d (b + a \cos[c+dx]) (A + 2 C + 2 B \cos[c+dx] + A \cos[2c+2dx]))
 \end{aligned}$$

**Problem 949: Result more than twice size of optimal antiderivative.**

$$\int \cos [c+d x]^4 (a+b \operatorname{Sec}[c+d x])^{3 / 2}(A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) d x$$

Optimal (type 4, 650 leaves, 9 steps):

$$\begin{aligned}
 & -\frac{1}{192 a^2 b d}(a-b) \sqrt{a+b}\left(9 A b^3-128 a^3 B-24 a b^2 B-12 a^2 b(13 A+20 C)\right) \\
 & \quad \operatorname{Cot}[c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \quad \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}}-\frac{1}{192 a^2 d} \\
 & \quad \sqrt{a+b}\left(9 A b^3-6 a b^2(A+4 B)-8 a^3(9 A+16 B+12 C)-4 a^2 b(39 A+28 B+60 C)\right) \operatorname{Cot}[c+d x] \\
 & \quad \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}}- \\
 & \quad \frac{1}{64 a^3 d} \sqrt{a+b}\left(3 A b^4+96 a^3 b B-8 a b^3 B+24 a^2 b^2(A+2 C)+16 a^4(3 A+4 C)\right) \\
 & \quad \operatorname{Cot}[c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \quad \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}}-\frac{1}{192 a^2 d} \\
 & \quad (9 A b^3-128 a^3 B-24 a b^2 B-12 a^2 b(13 A+20 C)) \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]+ \\
 & \quad \frac{1}{96 a d}\left(3 A b^2+56 a b B+12 a^2(3 A+4 C)\right) \operatorname{Cos}[c+d x] \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]+ \\
 & \quad \frac{(3 A b+8 a B) \operatorname{Cos}[c+d x]^2 \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{24 d}+ \\
 & \quad \frac{A \operatorname{Cos}[c+d x]^3(a+b \operatorname{Sec}[c+d x])^{3 / 2} \operatorname{Sin}[c+d x]}{4 d}
 \end{aligned}$$

Result (type 4, 4781 leaves):

$$\begin{aligned}
 & \left(\cos [c+d x]^3(a+b \operatorname{Sec}[c+d x])^{3 / 2}(A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2)\right. \\
 & \quad \left(\frac{1}{48}(9 A b+8 a B) \operatorname{Sin}[c+d x]+\frac{(48 a^2 A+3 A b^2+56 a b B+48 a^2 C) \operatorname{Sin}[2(c+d x)]}{96 a}+\right. \\
 & \quad \left.\frac{1}{48}(9 A b+8 a B) \operatorname{Sin}[3(c+d x)]+\frac{1}{16} a A \operatorname{Sin}[4(c+d x)]\right) \left. \right) / \\
 & (d(b+a \operatorname{Cos}[c+d x])(A+2 C+2 B \operatorname{Cos}[c+d x]+A \operatorname{Cos}[2 c+2 d x]))+
 \end{aligned}$$

$$\left( \left( \frac{3 a^2 A}{4 \sqrt{b+a \cos [c+d x]} \sqrt{\sec [c+d x]}} + \frac{19 A b^2}{16 \sqrt{b+a \cos [c+d x]} \sqrt{\sec [c+d x]}} + \right. \right.$$

$$\frac{13 a b B}{6 \sqrt{b+a \cos [c+d x]} \sqrt{\sec [c+d x]}} + \frac{a^2 C}{\sqrt{b+a \cos [c+d x]} \sqrt{\sec [c+d x]}} +$$

$$\frac{2 b^2 C}{\sqrt{b+a \cos [c+d x]} \sqrt{\sec [c+d x]}} + \frac{19 a A b \sqrt{\sec [c+d x]}}{16 \sqrt{b+a \cos [c+d x]}} -$$

$$\frac{A b^3 \sqrt{\sec [c+d x]}}{64 a \sqrt{b+a \cos [c+d x]}} + \frac{2 a^2 B \sqrt{\sec [c+d x]}}{3 \sqrt{b+a \cos [c+d x]}} + \frac{17 b^2 B \sqrt{\sec [c+d x]}}{24 \sqrt{b+a \cos [c+d x]}} +$$

$$\frac{7 a b C \sqrt{\sec [c+d x]}}{4 \sqrt{b+a \cos [c+d x]}} + \frac{13 a A b \cos [2 (c+d x)] \sqrt{\sec [c+d x]}}{16 \sqrt{b+a \cos [c+d x]}} -$$

$$\frac{3 A b^3 \cos [2 (c+d x)] \sqrt{\sec [c+d x]}}{64 a \sqrt{b+a \cos [c+d x]}} + \frac{2 a^2 B \cos [2 (c+d x)] \sqrt{\sec [c+d x]}}{3 \sqrt{b+a \cos [c+d x]}} +$$

$$\left. \frac{b^2 B \cos [2 (c+d x)] \sqrt{\sec [c+d x]}}{8 \sqrt{b+a \cos [c+d x]}} + \frac{5 a b C \cos [2 (c+d x)] \sqrt{\sec [c+d x]}}{4 \sqrt{b+a \cos [c+d x]}} \right)$$

$$(a+b \sec [c+d x])^{3/2} (A+B \sec [c+d x]+C \sec [c+d x]^2)$$

$$\left( \left( -9 A b^3 + 128 a^3 B + 24 a b^2 B + 12 a^2 b (13 A + 20 C) \right) \tan \left[ \frac{1}{2} (c+d x) \right] \right.$$

$$\left. \sqrt{\frac{a+b-a \tan \left[ \frac{1}{2} (c+d x) \right]^2 + b \tan \left[ \frac{1}{2} (c+d x) \right]^2}{1+\tan \left[ \frac{1}{2} (c+d x) \right]^2}} \right) / \left( 96 a^2 \sqrt{\frac{1+\tan \left[ \frac{1}{2} (c+d x) \right]^2}{1-\tan \left[ \frac{1}{2} (c+d x) \right]^2}} \right) +$$

$$\left( (a+b) (-9 A b^3 + 128 a^3 B + 24 a b^2 B + 12 a^2 b (13 A + 20 C)) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \right. \right. \right.$$

$$\left. \left. \tan \left[ \frac{1}{2} (c+d x) \right] \right], \frac{a-b}{a+b} \right] - 2 a (-3 A b^3 + 24 a^3 (3 A + 4 C) - 4 a^2 b (9 A - 52 B + 12 C) + \right.$$

$$\left. 2 a b^2 (57 A - 28 B + 96 C) \right] \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \tan \left[ \frac{1}{2} (c+d x) \right] \right], \frac{a-b}{a+b} \right] - 6 (3 A b^4 + \right.$$

$$\left. 96 a^3 b B - 8 a b^3 B + 24 a^2 b^2 (A + 2 C) + 16 a^4 (3 A + 4 C) \right] \operatorname{EllipticPi} \left[ -1, -\operatorname{ArcSin} \left[ \right. \right. \right.$$

$$\left. \left. \tan \left[ \frac{1}{2} (c+d x) \right] \right], \frac{a-b}{a+b} \right] \sqrt{\frac{a+b-a \tan \left[ \frac{1}{2} (c+d x) \right]^2 + b \tan \left[ \frac{1}{2} (c+d x) \right]^2}{a+b}}$$

$$\left. \sqrt{\frac{a+b-a \tan \left[ \frac{1}{2} (c+d x) \right]^2 + b \tan \left[ \frac{1}{2} (c+d x) \right]^2}{1+\tan \left[ \frac{1}{2} (c+d x) \right]^2}} \sqrt{1-\tan \left[ \frac{1}{2} (c+d x) \right]^4} \right) /$$

$$\left( 96 a^2 \sqrt{\frac{1}{1 - \tan\left[\frac{1}{2}(c + dx)\right]^2}} \left( b - b \tan\left[\frac{1}{2}(c + dx)\right] \right)^4 + a \left( -1 + \tan\left[\frac{1}{2}(c + dx)\right] \right)^2 \right)^2 \Bigg) \Bigg) /$$

$$\left( d (b + a \cos[c + dx])^{3/2} (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \right.$$

$$\left. \sec[c + dx]^{7/2} \right.$$

$$\left. \left( (-9Ab^3 + 128a^3B + 24ab^2B + 12a^2b(13A + 20C)) \sec\left[\frac{1}{2}(c + dx)\right] \right)^2 \right.$$

$$\left. \sqrt{\frac{a + b - a \tan\left[\frac{1}{2}(c + dx)\right]^2 + b \tan\left[\frac{1}{2}(c + dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c + dx)\right]^2}} \right) / \left( 192 a^2 \sqrt{\frac{1 + \tan\left[\frac{1}{2}(c + dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c + dx)\right]^2}} \right) -$$

$$\left( (a + b) (-9Ab^3 + 128a^3B + 24ab^2B + 12a^2b(13A + 20C)) \right.$$

$$\left. \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c + dx)\right]\right], \frac{a - b}{a + b}\right] - \right.$$

$$\left. 2a(-3Ab^3 + 24a^3(3A + 4C) - 4a^2b(9A - 52B + 12C) + 2ab^2(57A - 28B + 96C)) \right.$$

$$\left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c + dx)\right]\right], \frac{a - b}{a + b}\right] - 6(3Ab^4 + 96a^3bB - 8ab^3B + 24a^2b^2 \right.$$

$$\left. (A + 2C) + 16a^4(3A + 4C)) \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c + dx)\right]\right], \frac{a - b}{a + b}\right] \right)$$

$$\sqrt{\frac{a + b - a \tan\left[\frac{1}{2}(c + dx)\right]^2 + b \tan\left[\frac{1}{2}(c + dx)\right]^2}{a + b}}$$

$$\sqrt{\frac{a + b - a \tan\left[\frac{1}{2}(c + dx)\right]^2 + b \tan\left[\frac{1}{2}(c + dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c + dx)\right]^2}}$$

$$\sqrt{1 - \tan\left[\frac{1}{2}(c + dx)\right]^4} \left( -2b \sec\left[\frac{1}{2}(c + dx)\right]^2 \tan\left[\frac{1}{2}(c + dx)\right]^3 + \right.$$

$$\left. 2a \sec\left[\frac{1}{2}(c + dx)\right]^2 \tan\left[\frac{1}{2}(c + dx)\right] \left( -1 + \tan\left[\frac{1}{2}(c + dx)\right]^2 \right) \right) \Bigg) /$$

$$\left( 96 a^2 \sqrt{\frac{1}{1 - \tan\left[\frac{1}{2}(c + dx)\right]^2}} \left( b - b \tan\left[\frac{1}{2}(c + dx)\right] \right)^4 + a \left( -1 + \tan\left[\frac{1}{2}(c + dx)\right] \right)^2 \right)^2 \Bigg) -$$

$$\left( (a+b) (-9 A b^3 + 128 a^3 B + 24 a b^2 B + 12 a^2 b (13 A + 20 C)) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] - 2 a (-3 A b^3 + 24 a^3 (3 A + 4 C) - 4 a^2 b (9 A - 52 B + 12 C) + 2 a b^2 (57 A - 28 B + 96 C)) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] - 6 (3 A b^4 + 96 a^3 b B - 8 a b^3 B + 24 a^2 b^2 (A + 2 C) + 16 a^4 (3 A + 4 C)) \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3 \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \right) / \left( 96 a^2 \sqrt{\frac{1}{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^4} \left(b-b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^4+a\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^2\right) \right) + \left( (a+b) (-9 A b^3 + 128 a^3 B + 24 a b^2 B + 12 a^2 b (13 A + 20 C)) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] - 2 a (-3 A b^3 + 24 a^3 (3 A + 4 C) - 4 a^2 b (9 A - 52 B + 12 C) + 2 a b^2 (57 A - 28 B + 96 C)) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] - 6 (3 A b^4 + 96 a^3 b B - 8 a b^3 B + 24 a^2 b^2 (A + 2 C) + 16 a^4 (3 A + 4 C)) \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \left(-a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + b \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^4} \right) / \left( 192 a^2 (a+b) \sqrt{\frac{1}{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right)$$

$$\begin{aligned}
& \left( b - b \tan\left[\frac{1}{2}(c+dx)\right]^4 + a \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \right) - \\
& \frac{1}{192 a^2 \left( b - b \tan\left[\frac{1}{2}(c+dx)\right]^4 + a \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \right)} \\
& \left( (a+b) (-9 A b^3 + 128 a^3 B + 24 a b^2 B + 12 a^2 b (13 A + 20 C)) \right. \\
& \quad \text{EllipticE}\left[\text{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] - \\
& \quad 2 a (-3 A b^3 + 24 a^3 (3 A + 4 C) - 4 a^2 b (9 A - 52 B + 12 C) + 2 a b^2 (57 A - 28 B + 96 C)) \\
& \quad \text{EllipticF}\left[\text{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] - \\
& \quad 6 (3 A b^4 + 96 a^3 b B - 8 a b^3 B + 24 a^2 b^2 (A + 2 C) + 16 a^4 (3 A + 4 C)) \text{EllipticPi}\left[ \right. \\
& \quad \left. -1, -\text{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \\
& \quad \sqrt{\frac{1}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \\
& \quad \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^4} - \\
& \quad \left( (-9 A b^3 + 128 a^3 B + 24 a b^2 B + 12 a^2 b (13 A + 20 C)) \tan\left[\frac{1}{2}(c+dx)\right] \right. \\
& \quad \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}} \left( \frac{\sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} + \right. \\
& \quad \left. \left( \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \right) / \\
& \quad \left. \left(1 - \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \right) / \left( 192 a^2 \left( \frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{3/2} \right) + \\
& \quad \left( (-9 A b^3 + 128 a^3 B + 24 a b^2 B + 12 a^2 b (13 A + 20 C)) \tan\left[\frac{1}{2}(c+dx)\right] \right. \\
& \quad \left. \left( \left( -a \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + b \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) / \right. \right. \\
& \quad \left. \left. \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) - \left( \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) /
\end{aligned}$$



$$\begin{aligned}
 & \left( \left( a + b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) / \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) / \\
 & \left( 192 a^2 \sqrt{\frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{\frac{a + b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}} \right) + \\
 & \left( (a+b) (-9Ab^3 + 128a^3B + 24ab^2B + 12a^2b(13A + 20C)) \right. \\
 & \quad \text{EllipticE}\left[\text{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] - \\
 & \quad 2a(-3Ab^3 + 24a^3(3A+4C) - 4a^2b(9A-52B+12C) + 2ab^2(57A-28B+96C)) \\
 & \quad \text{EllipticF}\left[\text{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] - 6(3Ab^4 + 96a^3bB - 8ab^3B + 24a^2b^2 \\
 & \quad (A+2C) + 16a^4(3A+4C)) \text{EllipticPi}\left[-1, -\text{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
 & \quad \sqrt{\frac{a + b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^4} \\
 & \quad \left( \left( -a \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + b \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) / \right. \\
 & \quad \left. \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \left( \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) / \\
 & \quad \left. \left( a + b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) / \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) / \\
 & \left( 192 a^2 \sqrt{\frac{1}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{\frac{a + b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}} \right. \\
 & \quad \left. \left( b - b \tan\left[\frac{1}{2}(c+dx)\right]^4 + a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) \right) + \\
 & \left( \sqrt{\frac{a + b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right. \\
 & \quad \left. \sqrt{\frac{a + b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^4} \right)
 \end{aligned}$$

$$\begin{aligned} & \left( - \left( a (-3 A b^3 + 24 a^3 (3 A + 4 C) - 4 a^2 b (9 A - 52 B + 12 C) + \right. \right. \\ & \quad \left. \left. 2 a b^2 (57 A - 28 B + 96 C) \right) \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \\ & \left( \sqrt{1 - \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2} \sqrt{1 - \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} \right) + \\ & \left( 3 (3 A b^4 + 96 a^3 b B - 8 a b^3 B + 24 a^2 b^2 (A + 2 C) + 16 a^4 (3 A + 4 C)) \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \\ & \left( \sqrt{1 - \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2} \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right) \sqrt{1 - \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} \right) + \\ & \left( (a + b) (-9 A b^3 + 128 a^3 B + 24 a b^2 B + 12 a^2 b (13 A + 20 C)) \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right. \\ & \quad \left. \sqrt{1 - \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} \right) / \left( 2 \sqrt{1 - \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2} \right) \right) / \\ & \left( 96 a^2 \sqrt{\frac{1}{1 - \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}} \left( b - b \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^4 + a \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right)^2 \right) \right) \end{aligned}$$

**Problem 950: Attempted integration timed out after 120 seconds.**

$$\int \operatorname{Sec}[c + d x]^2 (a + b \operatorname{Sec}[c + d x])^{5/2} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 4, 610 leaves, 8 steps):

$$\begin{aligned}
 & \frac{1}{3465 b^4 d} 2 (a-b) \sqrt{a+b} \\
 & (110 a^4 b B - 3069 a^2 b^3 B - 1617 b^5 B - 40 a^5 C - 15 a^3 b^2 (33 A + 17 C) - 15 a b^4 (319 A + 247 C)) \\
 & \operatorname{Cot}[c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \frac{1}{3465 b^3 d} \\
 & 2(a-b) \sqrt{a+b} (10 a^3 b (11 B - 3 C) - 40 a^4 C - 15 a^2 b^2 (33 A - 121 B + 19 C) - \\
 & 3 b^4 (275 A - 539 B + 225 C) + 6 a b^3 (660 A - 209 B + 505 C)) \operatorname{Cot}[c+d x] \\
 & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \\
 & \frac{1}{3465 b^2 d} 2 (110 a^3 b B - 1254 a b^3 B - 40 a^4 C - 75 b^4 (11 A + 9 C) - 15 a^2 b^2 (33 A + 19 C)) \\
 & \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x] - \frac{1}{3465 b^2 d} \\
 & 2 (110 a^2 b B - 539 b^3 B - 40 a^3 C - 5 a b^2 (99 A + 67 C)) (a+b \operatorname{Sec}[c+d x])^{3/2} \operatorname{Tan}[c+d x] + \\
 & \frac{1}{693 b^2 d} 2 (99 A b^2 - 22 a b B + 8 a^2 C + 81 b^2 C) (a+b \operatorname{Sec}[c+d x])^{5/2} \operatorname{Tan}[c+d x] + \\
 & \frac{2 (11 b B - 4 a C) (a+b \operatorname{Sec}[c+d x])^{7/2} \operatorname{Tan}[c+d x]}{99 b^2 d} + \\
 & \frac{2 C \operatorname{Sec}[c+d x] (a+b \operatorname{Sec}[c+d x])^{7/2} \operatorname{Tan}[c+d x]}{11 b d}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 951: Attempted integration timed out after 120 seconds.**

$$\int \operatorname{Sec}[c+d x] (a+b \operatorname{Sec}[c+d x])^{5/2} (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) dx$$

Optimal (type 4, 502 leaves, 7 steps):

$$\begin{aligned}
 & -\frac{1}{315 b^3 d} 2 (a-b) \sqrt{a+b} (45 a^3 b B + 435 a b^3 B - 10 a^4 C + 21 b^4 (9 A + 7 C) + 3 a^2 b^2 (161 A + 93 C)) \\
 & \quad \text{Cot}[c+d x] \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \text{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \quad \sqrt{\frac{b(1-\text{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\text{Sec}[c+d x])}{a-b}} + \frac{1}{315 b^2 d} 2 (a-b) \sqrt{a+b} \\
 & \quad (10 a^3 C + 15 a^2 b (21 A - 3 B + 11 C) - 6 a b^2 (28 A - 60 B + 19 C) + 3 b^3 (63 A - 25 B + 49 C)) \text{Cot}[c+d x] \\
 & \quad \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \text{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\text{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\text{Sec}[c+d x])}{a-b}} + \\
 & \quad \frac{1}{315 b d} 2 (45 a^2 b B + 75 b^3 B - 10 a^3 C + 6 a b^2 (28 A + 19 C)) \sqrt{a+b \text{Sec}[c+d x]} \text{Tan}[c+d x] + \\
 & \quad \frac{1}{315 b d} 2 (63 A b^2 + 45 a b B - 10 a^2 C + 49 b^2 C) (a+b \text{Sec}[c+d x])^{3/2} \text{Tan}[c+d x] + \\
 & \quad \frac{2(9 b B - 2 a C) (a+b \text{Sec}[c+d x])^{5/2} \text{Tan}[c+d x]}{63 b d} + \frac{2 C (a+b \text{Sec}[c+d x])^{7/2} \text{Tan}[c+d x]}{9 b d}
 \end{aligned}$$

Result(type 1, 1 leaves):

???

**Problem 952: Result more than twice size of optimal antiderivative.**

$$\int (a+b \text{Sec}[c+d x])^{5/2} (A+B \text{Sec}[c+d x] + C \text{Sec}[c+d x]^2) dx$$

Optimal (type 4, 521 leaves, 8 steps):

$$\begin{aligned}
 & -\frac{1}{105 b^2 d} 2 (a-b) \sqrt{a+b} (161 a^2 b B + 63 b^3 B + 15 a^3 C + 5 a b^2 (49 A + 29 C)) \\
 & \quad \text{Cot}[c+d x] \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \text{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \quad \sqrt{\frac{b(1-\text{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\text{Sec}[c+d x])}{a-b}} + \frac{1}{105 b d} 2 \sqrt{a+b} \\
 & \quad (15 a^3 (7 B - C) + b^3 (35 A - 63 B + 25 C) + a^2 b (315 A - 161 B + 135 C) - a b^2 (245 A - 119 B + 145 C)) \\
 & \quad \text{Cot}[c+d x] \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \text{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \quad \sqrt{\frac{b(1-\text{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\text{Sec}[c+d x])}{a-b}} - \frac{1}{d} \\
 & \quad 2 a^2 A \sqrt{a+b} \text{Cot}[c+d x] \text{EllipticPi}\left[\frac{a+b}{a}, \text{ArcSin}\left[\frac{\sqrt{a+b \text{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \quad \sqrt{\frac{b(1-\text{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\text{Sec}[c+d x])}{a-b}} + \\
 & \quad \frac{2(35 A b^2 + 56 a b B + 15 a^2 C + 25 b^2 C) \sqrt{a+b \text{Sec}[c+d x]} \text{Tan}[c+d x]}{105 d} + \\
 & \quad \frac{2(7 b B + 5 a C) (a+b \text{Sec}[c+d x])^{3/2} \text{Tan}[c+d x]}{35 d} + \frac{2 C (a+b \text{Sec}[c+d x])^{5/2} \text{Tan}[c+d x]}{7 d}
 \end{aligned}$$

Result (type 4, 1405 leaves):

$$\begin{aligned}
 & -\left( \left( 4 (a+b \text{Sec}[c+d x])^{5/2} (A+B \text{Sec}[c+d x] + C \text{Sec}[c+d x]^2) \sqrt{\frac{1}{1-\text{Tan}\left[\frac{1}{2}(c+d x)\right]^2}} \right. \right. \\
 & \quad \left( 245 a^2 A b^2 \text{Tan}\left[\frac{1}{2}(c+d x)\right] + 245 a A b^3 \text{Tan}\left[\frac{1}{2}(c+d x)\right] + 161 a^3 b B \text{Tan}\left[\frac{1}{2}(c+d x)\right] + \right. \\
 & \quad 161 a^2 b^2 B \text{Tan}\left[\frac{1}{2}(c+d x)\right] + 63 a b^3 B \text{Tan}\left[\frac{1}{2}(c+d x)\right] + 63 b^4 B \text{Tan}\left[\frac{1}{2}(c+d x)\right] + \\
 & \quad 15 a^4 C \text{Tan}\left[\frac{1}{2}(c+d x)\right] + 15 a^3 b C \text{Tan}\left[\frac{1}{2}(c+d x)\right] + 145 a^2 b^2 C \text{Tan}\left[\frac{1}{2}(c+d x)\right] + \\
 & \quad 145 a b^3 C \text{Tan}\left[\frac{1}{2}(c+d x)\right] - 490 a^2 A b^2 \text{Tan}\left[\frac{1}{2}(c+d x)\right]^3 - 322 a^3 b B \text{Tan}\left[\frac{1}{2}(c+d x)\right]^3 - \\
 & \quad 126 a b^3 B \text{Tan}\left[\frac{1}{2}(c+d x)\right]^3 - 30 a^4 C \text{Tan}\left[\frac{1}{2}(c+d x)\right]^3 - 290 a^2 b^2 C \text{Tan}\left[\frac{1}{2}(c+d x)\right]^3 + \\
 & \quad 245 a^2 A b^2 \text{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - 245 a A b^3 \text{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + 161 a^3 b B \text{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - \\
 & \quad \left. \left. 161 a^2 b^2 B \text{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + 63 a b^3 B \text{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - 63 b^4 B \text{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 15 a^4 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - 15 a^3 b C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + 145 a^2 b^2 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - \\
 & 145 a b^3 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + 210 a^3 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right]\right], \\
 & \frac{a-b}{a+b} \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \\
 & 210 a^3 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right]\right], \frac{a-b}{a+b} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \\
 & (a+b)\left(161 a^2 b B+63 b^3 B+15 a^3 C+5 a b^2(49 A+29 C)\right) \operatorname{EllipticE}\left[\right. \\
 & \left. \operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right) \\
 & \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - b(-15 a^3(7 A-7 B-C)+ \\
 & b^3(35 A+63 B+25 C)+a^2 b(315 A+161 B+135 C)+a b^2(245 A+119 B+145 C)) \\
 & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \\
 & \left.\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right) \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}}\right)\right) / \\
 & \left(105 b d(b+a \operatorname{Cos}[c+d x])^{5 / 2}(A+2 C+2 B \operatorname{Cos}[c+d x]+A \operatorname{Cos}[2 c+2 d x])\right. \\
 & \left.\operatorname{Sec}[c+d x]^{9 / 2}\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)^{3 / 2}\right. \\
 & \left.\sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}}\right)\right) + \\
 & \frac{1}{d(b+a \operatorname{Cos}[c+d x])^2(A+2 C+2 B \operatorname{Cos}[c+d x]+A \operatorname{Cos}[2 c+2 d x])} \\
 & \operatorname{Cos}[c+d x]^4 \\
 & (a+b \operatorname{Sec}[c+d x])^{5 / 2} \\
 & (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \\
 & \left(\frac{4(245 a A b^2+161 a^2 b B+63 b^3 B+15 a^3 C+145 a b^2 C) \operatorname{Sin}[c+d x]}{105 b}+\right.
 \end{aligned}$$

$$\frac{4}{35} \operatorname{Sec}[c+dx]^2 (7b^2 B \sin[c+dx] + 15abC \sin[c+dx]) + \frac{4}{105} \operatorname{Sec}[c+dx] \\ (35A b^2 \sin[c+dx] + 77abB \sin[c+dx] + 45a^2 C \sin[c+dx] + 25b^2 C \sin[c+dx]) + \\ \frac{4}{7} b^2 C \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx]$$

### Problem 953: Result more than twice size of optimal antiderivative.

$$\int \cos[c+dx] (a+b \operatorname{Sec}[c+dx])^{5/2} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) dx$$

Optimal (type 4, 505 leaves, 8 steps):

$$-\frac{1}{15bd} (a-b) \sqrt{a+b} (70abB - a^2(15A-46C) + 6b^2(5A+3C)) \\ \operatorname{Cot}[c+dx] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ \sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}} + \frac{1}{15bd} \\ \sqrt{a+b} (a^2b(15A+90B-46C) + 30a^3C - 2b^3(15A-5B+9C) + 2ab^2(45A-35B+17C)) \\ \operatorname{Cot}[c+dx] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ \sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}} - \frac{1}{d} \\ a\sqrt{a+b} (5Ab+2aB) \operatorname{Cot}[c+dx] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ \sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}} + \frac{A(a+b \operatorname{Sec}[c+dx])^{5/2} \sin[c+dx]}{d} - \\ \frac{b(15aA-10bB-16aC) \sqrt{a+b \operatorname{Sec}[c+dx]} \operatorname{Tan}[c+dx]}{15d} - \\ \frac{b(5A-2C) (a+b \operatorname{Sec}[c+dx])^{3/2} \operatorname{Tan}[c+dx]}{5d}$$

Result (type 4, 1498 leaves):

$$\left( 2(a+b \operatorname{Sec}[c+dx])^{5/2} (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \sqrt{\frac{1}{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \right. \\ \left. \left( 15a^3 A \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 15a^2 A b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - 30a A b^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) - \right.$$

$$\begin{aligned}
 & 30 A b^3 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]-70 a^2 b B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]-70 a b^2 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]- \\
 & 46 a^3 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]-46 a^2 b C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]-18 a b^2 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]- \\
 & 18 b^3 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]-30 a^3 A \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3+60 a A b^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3+ \\
 & 140 a^2 b B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3+92 a^3 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3+36 a b^2 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3+ \\
 & 15 a^3 A \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5-15 a^2 A b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5-30 a A b^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5+ \\
 & 30 A b^3 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5-70 a^2 b B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5+70 a b^2 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5- \\
 & 46 a^3 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5+46 a^2 b C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5-18 a b^2 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5+ \\
 & 18 b^3 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5-150 a^2 A b \operatorname{EllipticPi}\left[-1,-\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}}- \\
 & 60 a^3 B \operatorname{EllipticPi}\left[-1,-\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}}- \\
 & 150 a^2 A b \operatorname{EllipticPi}\left[-1,-\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}}- \\
 & 60 a^3 B \operatorname{EllipticPi}\left[-1,-\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}}+ \\
 & (a+b)\left(-70 a b B+a^2(15 A-46 C)-6 b^2(5 A+3 C)\right) \\
 & \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \\
 & \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right) \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}}- \\
 & 2\left(a^2 b(45 A-45 B-23 C)+15 a^3(B-C)-b^3(15 A+5 B+9 C)-a b^2(45 A+35 B+17 C)\right)
 \end{aligned}$$



$$\begin{aligned}
 & \text{EllipticF}\left[\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1+\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b-a\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \Bigg/ \\
 & \left(15d(b+a\text{Cos}[c+dx])^{5/2}(A+2C+2B\text{Cos}[c+dx]+A\text{Cos}[2c+2dx])\right. \\
 & \left.\text{Sec}[c+dx]^{9/2}\left(1+\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^{3/2}\right. \\
 & \left.\sqrt{\frac{a+b-a\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1+\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}}\right)+ \\
 & \left(\text{Cos}[c+dx]^4(a+b\text{Sec}[c+dx])^{5/2}(A+B\text{Sec}[c+dx]+C\text{Sec}[c+dx]^2)\right. \\
 & \left(\frac{4}{15}(15Ab^2+35abB+23a^2C+9b^2C)\text{Sin}[c+dx]+\frac{4}{15}\text{Sec}[c+dx]\right. \\
 & \left.\left(5b^2B\text{Sin}[c+dx]+11abC\text{Sin}[c+dx]\right)+\frac{4}{5}b^2C\text{Sec}[c+dx]\text{Tan}[c+dx]\right) \Bigg) \Bigg/ \\
 & \left(d(b+a\text{Cos}[c+dx])^2(A+2C+2B\text{Cos}[c+dx]+A\text{Cos}[2c+2dx])\right)
 \end{aligned}$$

**Problem 955: Result more than twice size of optimal antiderivative.**

$$\int \text{Cos}[c+dx]^3 (a+b\text{Sec}[c+dx])^{5/2} (A+B\text{Sec}[c+dx]+C\text{Sec}[c+dx]^2) dx$$

Optimal (type 4, 549 leaves, 8 steps):

$$\frac{1}{24 b d} (a-b) \sqrt{a+b} (54 a b B + 3 b^2 (11 A - 16 C) + 8 a^2 (2 A + 3 C)) \operatorname{Cot}[c+d x]$$

$$\operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} +$$

$$\frac{1}{24 d} \sqrt{a+b} (3 b^2 (11 A + 16 (B - C)) + 4 a^2 (4 A + 3 B + 6 C) + 2 a b (13 A + 27 B + 72 C)) \operatorname{Cot}[c+d x]$$

$$\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} -$$

$$\frac{1}{8 a d} \sqrt{a+b} (5 A b^3 + 8 a^3 B + 30 a b^2 B + 20 a^2 b (A + 2 C)) \operatorname{Cot}[c+d x]$$

$$\operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}}$$

$$\sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \frac{(15 A b^2 + 42 a b B + 8 a^2 (2 A + 3 C)) \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{24 d} +$$

$$\frac{(5 A b + 6 a B) \operatorname{Cos}[c+d x] (a+b \operatorname{Sec}[c+d x])^{3/2} \operatorname{Sin}[c+d x]}{12 d} +$$

$$\frac{A \operatorname{Cos}[c+d x]^2 (a+b \operatorname{Sec}[c+d x])^{5/2} \operatorname{Sin}[c+d x]}{3 d}$$

Result (type 4, 2922 leaves):

$$\left( \operatorname{Cos}[c+d x]^4 (a+b \operatorname{Sec}[c+d x])^{5/2} \right.$$

$$\left. (A+B \operatorname{Sec}[c+d x] + C \operatorname{Sec}[c+d x]^2) \left( \frac{1}{6} (a^2 A + 24 b^2 C) \operatorname{Sin}[c+d x] + \right. \right.$$

$$\left. \left. \frac{1}{12} a (13 A b + 6 a B) \operatorname{Sin}[2(c+d x)] + \frac{1}{6} a^2 A \operatorname{Sin}[3(c+d x)] \right) \right) /$$

$$\left( d (b+a \operatorname{Cos}[c+d x])^2 (A+2 C + 2 B \operatorname{Cos}[c+d x] + A \operatorname{Cos}[2 c+2 d x]) \right) +$$

$$\left( \operatorname{Cos}[c+d x]^5 \left( \frac{19 a^2 A b}{6 \sqrt{b+a \operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]}} + \right. \right.$$

$$\frac{2 A b^3}{\sqrt{b+a \operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]}} + \frac{a^3 B}{\sqrt{b+a \operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]}} +$$

$$\frac{6 a b^2 B}{\sqrt{b+a \operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]}} + \frac{6 a^2 b C}{\sqrt{b+a \operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]}} -$$

$$\frac{2 b^3 C}{\sqrt{b+a \operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]}} + \frac{2 a^3 A \sqrt{\operatorname{Sec}[c+d x]}}{3 \sqrt{b+a \operatorname{Cos}[c+d x]}} + \frac{59 a A b^2 \sqrt{\operatorname{Sec}[c+d x]}}{24 \sqrt{b+a \operatorname{Cos}[c+d x]}} \left. \right) +$$

$$\begin{aligned}
 & \frac{11 a^2 b B \sqrt{\sec [c+d x]}}{4 \sqrt{b+a \cos [c+d x]}} + \frac{2 b^3 B \sqrt{\sec [c+d x]}}{\sqrt{b+a \cos [c+d x]}} + \frac{a^3 C \sqrt{\sec [c+d x]}}{\sqrt{b+a \cos [c+d x]}} + \\
 & \frac{4 a b^2 C \sqrt{\sec [c+d x]}}{\sqrt{b+a \cos [c+d x]}} + \frac{2 a^3 A \cos [2 (c+d x)] \sqrt{\sec [c+d x]}}{3 \sqrt{b+a \cos [c+d x]}} + \\
 & \frac{11 a A b^2 \cos [2 (c+d x)] \sqrt{\sec [c+d x]}}{8 \sqrt{b+a \cos [c+d x]}} + \frac{9 a^2 b B \cos [2 (c+d x)] \sqrt{\sec [c+d x]}}{4 \sqrt{b+a \cos [c+d x]}} + \\
 & \left. \frac{a^3 C \cos [2 (c+d x)] \sqrt{\sec [c+d x]}}{\sqrt{b+a \cos [c+d x]}} - \frac{2 a b^2 C \cos [2 (c+d x)] \sqrt{\sec [c+d x]}}{\sqrt{b+a \cos [c+d x]}} \right) \\
 & (a+b \sec [c+d x])^{5/2} (A+B \sec [c+d x]+C \sec [c+d x]^2) \\
 & \left( \frac{1}{\sqrt{\cos [c+d x] \sec \left[\frac{1}{2}(c+d x)\right]^2}} \left( (a+b) (54 a b B+3 b^2 (11 A-16 C)+8 a^2 (2 A+3 C)) \right. \right. \\
 & \quad \text{EllipticE}\left[\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right]-2 (12 a^3 B+a b^2 (-13 A+72 (B-C))+ \\
 & \quad 24 b^3 (A-B-C)+2 a^2 b (19 A-3 B+36 C)) \text{EllipticF}\left[\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \right. \\
 & \quad \left. \frac{a-b}{a+b}\right]-6 (5 A b^3+8 a^3 B+30 a b^2 B+20 a^2 b (A+2 C)) \text{EllipticPi}\left[-1, \right. \\
 & \quad \left. \left. -\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \sqrt{\frac{(b+a \cos [c+d x]) \sec \left[\frac{1}{2}(c+d x)\right]^2}{a+b}} \right. \\
 & \quad \left. \left. (54 a b B+3 b^2 (11 A-16 C)+8 a^2 (2 A+3 C)) (b+a \cos [c+d x]) \text{Tan}\left[\frac{1}{2}(c+d x)\right] \right) \right) / \\
 & \left( 12 d (b+a \cos [c+d x])^3 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right. \\
 & \left. \left( \frac{1}{24 (b+a \cos [c+d x])^{3/2} \sqrt{\sec [c+d x]}} a \sin [c+d x] \left( \frac{1}{\sqrt{\cos [c+d x] \sec \left[\frac{1}{2}(c+d x)\right]^2}} \right. \right. \right. \right. \\
 & \quad \left. \left. \left( (a+b) (54 a b B+3 b^2 (11 A-16 C)+8 a^2 (2 A+3 C)) \text{EllipticE}\left[\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right]-2 (12 a^3 B+a b^2 (-13 A+72 (B-C))+24 b^3 (A-B-C)+ \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right]-2 (12 a^3 B+a b^2 (-13 A+72 (B-C))+24 b^3 (A-B-C)+ \right. \right. \\
 & \quad \left. \left. \left. \frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & 2 a^2 b (19 A - 3 B + 36 C) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] - \\
 & 6\left(5 A b^3+8 a^3 B+30 a b^2 B+20 a^2 b(A+2 C)\right) \operatorname{EllipticPi}\left[-1, \right. \\
 & \left. -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \sqrt{\frac{(b+a \operatorname{Cos}[c+d x]) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \\
 & \left.\left(54 a b B+3 b^2(11 A-16 C)+8 a^2(2 A+3 C)\right)(b+a \operatorname{Cos}[c+d x]) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right) - \\
 & \frac{1}{24 \sqrt{b+a \operatorname{Cos}[c+d x]}} \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x] \left(\frac{1}{\sqrt{\operatorname{Cos}[c+d x] \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2}}\right. \\
 & \left.\left((a+b)\left(54 a b B+3 b^2(11 A-16 C)+8 a^2(2 A+3 C)\right) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right]-2\left(12 a^3 B+a b^2(-13 A+72(B-C))+24 b^3(A-B-C)\right)+\right. \right. \\
 & \left. 2 a^2 b(19 A-3 B+36 C)\right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right]- \\
 & 6\left(5 A b^3+8 a^3 B+30 a b^2 B+20 a^2 b(A+2 C)\right) \operatorname{EllipticPi}\left[-1, \right. \\
 & \left. -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \sqrt{\frac{(b+a \operatorname{Cos}[c+d x]) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \\
 & \left.\left(54 a b B+3 b^2(11 A-16 C)+8 a^2(2 A+3 C)\right)(b+a \operatorname{Cos}[c+d x]) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right) + \\
 & \frac{1}{12 \sqrt{b+a \operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]}} \left(\frac{1}{2}\left(54 a b B+3 b^2(11 A-16 C)+8 a^2(2 A+3 C)\right)\right. \\
 & \left.(b+a \operatorname{Cos}[c+d x]) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2-a\left(54 a b B+3 b^2(11 A-16 C)+8 a^2(2 A+3 C)\right)\right. \\
 & \left.\operatorname{Sin}[c+d x] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]-\frac{1}{2\left(\operatorname{Cos}[c+d x] \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2\right)^{3 / 2}}\right. \\
 & \left.\left((a+b)\left(54 a b B+3 b^2(11 A-16 C)+8 a^2(2 A+3 C)\right) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right]-2\left(12 a^3 B+a b^2(-13 A+72(B-C))+24 b^3(A-B-C)\right)+\right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 a^2 b (19 A - 3 B + 36 C) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] - \\
 & 6\left(5 A b^3+8 a^3 B+30 a b^2 B+20 a^2 b(A+2 C)\right) \operatorname{EllipticPi}\left[-1, \right. \\
 & \quad \left. -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \sqrt{\frac{(b+a \operatorname{Cos}[c+d x]) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \\
 & \quad \left(-\operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Sin}[c+d x]+\operatorname{Cos}[c+d x] \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right) + \\
 & \quad \left(1 / \left(2 \sqrt{\operatorname{Cos}[c+d x] \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{(b+a \operatorname{Cos}[c+d x]) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}}\right)\right) \\
 & \quad \left((a+b)\left(54 a b B+3 b^2(11 A-16 C)+8 a^2(2 A+3 C)\right) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] - 2\left(12 a^3 B+a b^2(-13 A+72(B-C))+24 b^3(A-B-C)\right) + \right. \\
 & \quad 2 a^2 b(19 A-3 B+36 C) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] - \\
 & \quad 6\left(5 A b^3+8 a^3 B+30 a b^2 B+20 a^2 b(A+2 C)\right) \operatorname{EllipticPi}\left[-1, \right. \\
 & \quad \left. -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \left(-\frac{a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Sin}[c+d x]}{a+b} + \right. \\
 & \quad \left. \frac{(b+a \operatorname{Cos}[c+d x]) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{a+b}\right) + \\
 & \quad \left(\sqrt{\frac{(b+a \operatorname{Cos}[c+d x]) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} \left(-\left(\left(12 a^3 B+a b^2(-13 A+72(B-C))+\right.\right.\right. \\
 & \quad \left.\left.\left.24 b^3(A-B-C)+2 a^2 b(19 A-3 B+36 C)\right) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2\right) / \right. \\
 & \quad \left.\left(\sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{1-\frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}}\right)\right) + \\
 & \quad \left(3\left(5 A b^3+8 a^3 B+30 a b^2 B+20 a^2 b(A+2 C)\right) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2\right) / \\
 & \quad \left(\sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right) \right. \\
 & \quad \left.\sqrt{1-\frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}}\right) + \left((a+b)\left(54 a b B+3 b^2(11 A-16 C)\right) + \right.
 \end{aligned}$$

$$8 a^2 (2 A + 3 C) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \sqrt{1 - \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} \left/ \left( \left( 2 \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \right) \right) \right/ \left( \sqrt{\operatorname{Cos}[c+d x] \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2} \right) \right)$$

**Problem 957: Result unnecessarily involves imaginary or complex numbers.**

$$\int \operatorname{Cos}[c+d x]^5 (a+b \operatorname{Sec}[c+d x])^{5/2} (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) dx$$

Optimal (type 4, 774 leaves, 10 steps):

$$\begin{aligned}
 & -\frac{1}{1920 a^2 b d} (a-b) \sqrt{a+b} (45 A b^4 - 2840 a^3 b B - 150 a b^3 B - 256 a^4 (4 A + 5 C) - 12 a^2 b^2 (141 A + 220 C)) \\
 & \quad \text{Cot}[c+d x] \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \text{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \quad \sqrt{\frac{b(1-\text{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\text{Sec}[c+d x])}{a-b}} - \\
 & \frac{1}{1920 a^2 d} \sqrt{a+b} (45 A b^4 - 30 a b^3 (A+5 B) - 16 a^4 (64 A + 45 B + 80 C) - \\
 & \quad 8 a^3 b (193 A + 355 B + 260 C) - 4 a^2 b^2 (423 A + 295 B + 660 C)) \text{Cot}[c+d x] \\
 & \quad \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \text{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\text{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\text{Sec}[c+d x])}{a-b}} - \\
 & \frac{1}{128 a^3 d} \sqrt{a+b} (3 A b^5 + 96 a^5 B + 240 a^3 b^2 B - 10 a b^4 B + 40 a^2 b^3 (A+2 C) + 80 a^4 b (3 A + 4 C)) \\
 & \quad \text{Cot}[c+d x] \text{EllipticPi}\left[\frac{a+b}{a}, \text{ArcSin}\left[\frac{\sqrt{a+b \text{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \quad \sqrt{\frac{b(1-\text{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\text{Sec}[c+d x])}{a-b}} - \frac{1}{1920 a^2 d} \\
 & (45 A b^4 - 2840 a^3 b B - 150 a b^3 B - 256 a^4 (4 A + 5 C) - 12 a^2 b^2 (141 A + 220 C)) \\
 & \quad \sqrt{a+b \text{Sec}[c+d x]} \text{Sin}[c+d x] + \frac{1}{960 a d} \\
 & (15 A b^3 + 360 a^3 B + 590 a b^2 B + 4 a^2 b (193 A + 260 C)) \text{Cos}[c+d x] \sqrt{a+b \text{Sec}[c+d x]} \text{Sin}[c+d x] + \\
 & \frac{1}{240 d} (15 A b^2 + 110 a b B + 16 a^2 (4 A + 5 C)) \text{Cos}[c+d x]^2 \sqrt{a+b \text{Sec}[c+d x]} \text{Sin}[c+d x] + \\
 & \frac{(A b + 2 a B) \text{Cos}[c+d x]^3 (a+b \text{Sec}[c+d x])^{3/2} \text{Sin}[c+d x]}{8 d} + \\
 & \frac{A \text{Cos}[c+d x]^4 (a+b \text{Sec}[c+d x])^{5/2} \text{Sin}[c+d x]}{5 d}
 \end{aligned}$$

Result (type 4, 942 leaves):

$$\begin{aligned}
 & \frac{1}{d (b+a \text{Cos}[c+d x])^2 (A+2 C+2 B \text{Cos}[c+d x]+A \text{Cos}[2 c+2 d x])} \\
 & \quad \text{Cos}[c+d x]^4 (a+b \text{Sec}[c+d x])^{5/2} (A+B \text{Sec}[c+d x]+C \text{Sec}[c+d x]^2) \\
 & \quad \left( \frac{1}{480} (88 a^2 A + 93 A b^2 + 170 a b B + 80 a^2 C) \text{Sin}[c+d x] + \frac{1}{960 a} \right. \\
 & \quad \quad (1024 a^2 A b + 15 A b^3 + 480 a^3 B + 590 a b^2 B + 1040 a^2 b C) \text{Sin}[2(c+d x)] \left. \right) + \\
 & \quad \frac{1}{480} (100 a^2 A + 93 A b^2 + 170 a b B + 80 a^2 C) \text{Sin}[3(c+d x)] + \\
 & \quad \frac{1}{160} a (21 A b + 10 a B) \text{Sin}[4(c+d x)] + \frac{1}{40} a^2 A \text{Sin}[5(c+d x)] \left. \right) -
 \end{aligned}$$

$$\left( (a + b \operatorname{Sec}[c + d x])^{5/2} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right.$$

$$\sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}}$$

$$\left( -(-45 A b^4 + 2840 a^3 b B + 150 a b^3 B + 256 a^4 (4 A + 5 C) + 12 a^2 b^2 (141 A + 220 C)) \right.$$

$$\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] - \frac{1}{\sqrt{\frac{-a+b}{a+b} \left( b - b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^4 + a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 \right)^2 \right)}}$$

$$\operatorname{i} \left( (a - b) (-45 A b^4 + 2840 a^3 b B + 150 a b^3 B + 256 a^4 (4 A + 5 C) + 12 a^2 b^2 (141 A + 220 C)) \right.$$

$$\operatorname{EllipticE}\left[\operatorname{i} \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right], \frac{a+b}{a-b}\right] -$$

$$2(a - b) (-45 A b^4 - 30 a b^3 (A - 5 B) + 720 a^4 B + 4 a^2 b^2 (129 A + 185 B + 180 C) + 8 a^3$$

$$b (161 A + 45 B + 220 C)) \operatorname{EllipticF}\left[\operatorname{i} \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right], \frac{a+b}{a-b}\right] +$$

$$30(3 A b^5 + 96 a^5 B + 240 a^3 b^2 B - 10 a b^4 B + 40 a^2 b^3 (A + 2 C) + 80 a^4 b (3 A + 4 C))$$

$$\operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, \operatorname{i} \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right], \frac{a+b}{a-b}\right]$$

$$\left( -1 - \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 \right) \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}$$

$$\left. \left. \left. \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{a + b}} \right) \right) \right) /$$

$$\left( 960 a^2 d (b + a \operatorname{Cos}[c + d x])^{5/2} (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \right)$$



$$\text{Sec}[c + dx]^{9/2} \sqrt{\frac{1 + \text{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{1 - \text{Tan}\left[\frac{1}{2}(c + dx)\right]^2}}$$

Problem 958: Attempted integration timed out after 120 seconds.

$$\int \frac{\text{Sec}[c + dx]^3 (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2)}{\sqrt{a + b \text{Sec}[c + dx]}} dx$$

Optimal (type 4, 429 leaves, 6 steps):

$$\begin{aligned} & -\frac{1}{105 b^5 d} 2 (a - b) \sqrt{a + b} (56 a^2 b B + 63 b^3 B - 48 a^3 C - 2 a b^2 (35 A + 22 C)) \\ & \quad \text{Cot}[c + dx] \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + dx]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \\ & \quad \sqrt{\frac{b(1 - \text{Sec}[c + dx])}{a + b}} \sqrt{-\frac{b(1 + \text{Sec}[c + dx])}{a - b}} + \frac{1}{105 b^4 d} \\ & 2 \sqrt{a + b} (48 a^3 C - 4 a^2 b (14 B + 3 C) + 2 a b^2 (35 A + 7 B + 22 C) + b^3 (35 A - 63 B + 25 C)) \text{Cot}[c + dx] \\ & \quad \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + dx]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \sqrt{\frac{b(1 - \text{Sec}[c + dx])}{a + b}} \sqrt{-\frac{b(1 + \text{Sec}[c + dx])}{a - b}} + \\ & \quad \frac{2(35 A b^2 - 28 a b B + 24 a^2 C + 25 b^2 C) \sqrt{a + b \text{Sec}[c + dx]} \text{Tan}[c + dx]}{105 b^3 d} + \\ & \quad \frac{2(7 b B - 6 a C) \text{Sec}[c + dx] \sqrt{a + b \text{Sec}[c + dx]} \text{Tan}[c + dx]}{35 b^2 d} + \\ & \quad \frac{2 C \text{Sec}[c + dx]^2 \sqrt{a + b \text{Sec}[c + dx]} \text{Tan}[c + dx]}{7 b d} \end{aligned}$$

Result (type 1, 1 leaves):

???

Problem 959: Attempted integration timed out after 120 seconds.

$$\int \frac{\text{Sec}[c + dx]^2 (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2)}{\sqrt{a + b \text{Sec}[c + dx]}} dx$$

Optimal (type 4, 342 leaves, 5 steps):

$$\begin{aligned}
 & -\frac{1}{15 b^4 d} 2 (a-b) \sqrt{a+b} (15 A b^2 - 10 a b B + 8 a^2 C + 9 b^2 C) \operatorname{Cot}[c+d x] \operatorname{EllipticE}\left[\right. \\
 & \quad \left. \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \\
 & \frac{1}{15 b^3 d} 2 \sqrt{a+b} (15 A b^2 - b^2 (5 B - 9 C) + 8 a^2 C - 2 a b (5 B + C)) \operatorname{Cot}[c+d x] \\
 & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \\
 & \frac{2(5 b B - 4 a C) \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x]}{15 b^2 d} + \frac{2 C \operatorname{Sec}[c+d x] \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x]}{5 b d}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 960: Attempted integration timed out after 120 seconds.**

$$\int \frac{\operatorname{Sec}[c+d x] (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2)}{\sqrt{a+b \operatorname{Sec}[c+d x]}} dx$$

Optimal (type 4, 267 leaves, 4 steps):

$$\begin{aligned}
 & -\frac{1}{3 b^3 d} 2 (a-b) \sqrt{a+b} (3 b B - 2 a C) \operatorname{Cot}[c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \frac{1}{3 b^2 d} \\
 & 2 \sqrt{a+b} (3 A b - b(3 B - C) + 2 a C) \operatorname{Cot}[c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \frac{2 C \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x]}{3 b d}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 961: Result more than twice size of optimal antiderivative.**

$$\int \frac{A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2}{\sqrt{a+b \operatorname{Sec}[c+d x]}} dx$$

Optimal (type 4, 317 leaves, 5 steps):

$$-\frac{1}{b^2 d} 2 (a-b) \sqrt{a+b} C \cot [c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{1}{b d}$$

$$2 \sqrt{a+b} (B-C) \cot [c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} - \frac{1}{a d}$$

$$2 A \sqrt{a+b} \cot [c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}}$$

Result (type 4, 762 leaves):

$$\begin{aligned}
 & \left( 4 C \cos [c+d x] (b+a \cos [c+d x]) (A+B \sec [c+d x]+C \sec [c+d x]^2) \sin [c+d x] \right) / \\
 & \left( b d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{a+b \sec [c+d x]} \right) - \\
 & \left( 4 \sqrt{b+a \cos [c+d x]} (A+B \sec [c+d x]+C \sec [c+d x]^2) \sqrt{\frac{1}{1-\tan \left[\frac{1}{2}(c+d x)\right]^2}} \right. \\
 & \left. \left( a C \tan \left[\frac{1}{2}(c+d x)\right] + b C \tan \left[\frac{1}{2}(c+d x)\right] - 2 a C \tan \left[\frac{1}{2}(c+d x)\right]^3 + a C \tan \left[\frac{1}{2}(c+d x)\right]^5 - \right. \right. \\
 & \left. \left. b C \tan \left[\frac{1}{2}(c+d x)\right]^5 + 2 A b \operatorname{EllipticPi} \left[-1, -\operatorname{ArcSin} \left[\tan \left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \right. \right. \\
 & \left. \left. \sqrt{1-\tan \left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \tan \left[\frac{1}{2}(c+d x)\right]^2+b \tan \left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \right. \right. \\
 & \left. \left. 2 A b \operatorname{EllipticPi} \left[-1, -\operatorname{ArcSin} \left[\tan \left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \tan \left[\frac{1}{2}(c+d x)\right]^2 \right. \right. \\
 & \left. \left. \sqrt{1-\tan \left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \tan \left[\frac{1}{2}(c+d x)\right]^2+b \tan \left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \right. \right. \\
 & \left. \left. (a+b) C \operatorname{EllipticE} \left[\operatorname{ArcSin} \left[\tan \left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\tan \left[\frac{1}{2}(c+d x)\right]^2} \right. \right. \\
 & \left. \left. \left(1+\tan \left[\frac{1}{2}(c+d x)\right]^2\right) \sqrt{\frac{a+b-a \tan \left[\frac{1}{2}(c+d x)\right]^2+b \tan \left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \right. \right. \\
 & \left. \left. b (A-B-C) \operatorname{EllipticF} \left[\operatorname{ArcSin} \left[\tan \left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\tan \left[\frac{1}{2}(c+d x)\right]^2} \right. \right. \\
 & \left. \left. \left(1+\tan \left[\frac{1}{2}(c+d x)\right]^2\right) \sqrt{\frac{a+b-a \tan \left[\frac{1}{2}(c+d x)\right]^2+b \tan \left[\frac{1}{2}(c+d x)\right]^2}{a+b}} \right) \right) \right) / \\
 & \left( b d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sec [c+d x]^{3/2} \sqrt{a+b \sec [c+d x]} \right) \\
 & \left( 1+\tan \left[\frac{1}{2}(c+d x)\right]^2 \right)^{3/2} \sqrt{\frac{a+b-a \tan \left[\frac{1}{2}(c+d x)\right]^2+b \tan \left[\frac{1}{2}(c+d x)\right]^2}{1+\tan \left[\frac{1}{2}(c+d x)\right]^2}} \right)
 \end{aligned}$$

### Problem 962: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x] \left(A+B \sec [c+d x]+C \sec [c+d x]^2\right)}{\sqrt{a+b \sec [c+d x]}} d x$$

Optimal (type 4, 358 leaves, 6 steps):

$$\begin{aligned} & \frac{1}{a b d} A (a-b) \sqrt{a+b} \cot [c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{1}{a b d} \sqrt{a+b} (A b+2 a C) \cot [c+d x] \\ & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \\ & \frac{1}{a^2 d} \sqrt{a+b} (A b-2 a B) \cot [c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{A \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{a d} \end{aligned}$$

Result (type 4, 861 leaves):

$$\begin{aligned} & \left(2 \sqrt{b+a \cos [c+d x]} (B+A \cos [c+d x]+C \sec [c+d x]) \sqrt{\frac{1}{1-\tan \left[\frac{1}{2}(c+d x)\right]^2}}\right. \\ & \left. \left(a A \tan \left[\frac{1}{2}(c+d x)\right]+A b \tan \left[\frac{1}{2}(c+d x)\right]-2 a A \tan \left[\frac{1}{2}(c+d x)\right]^3+a A \tan \left[\frac{1}{2}(c+d x)\right]^5-\right. \right. \\ & \left. \left. A b \tan \left[\frac{1}{2}(c+d x)\right]^5+2 A b \operatorname{EllipticPi}\left[-1,-\operatorname{ArcSin}\left[\tan \left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right]\right) \sqrt{1-\tan \left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \tan \left[\frac{1}{2}(c+d x)\right]^2+b \tan \left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\ & 4 a B \operatorname{EllipticPi}\left[-1,-\operatorname{ArcSin}\left[\tan \left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\tan \left[\frac{1}{2}(c+d x)\right]^2} \\ & \sqrt{\frac{a+b-a \tan \left[\frac{1}{2}(c+d x)\right]^2+b \tan \left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \\ & \left. 2 A b \operatorname{EllipticPi}\left[-1,-\operatorname{ArcSin}\left[\tan \left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \tan \left[\frac{1}{2}(c+d x)\right]^2\right) \end{aligned}$$

$$\begin{aligned}
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 4 a B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & A (a+b) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 2 a (B-C) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \Bigg) \Bigg) / \\
 & \left( a d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{\sec [c + d x]} \right. \\
 & \left. \sqrt{a + b \sec [c + d x]} \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^{3/2} \right. \\
 & \left. \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}} \right)
 \end{aligned}$$

**Problem 963: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\cos [c + d x]^2 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sqrt{a + b \sec [c + d x]}} dx$$

Optimal (type 4, 439 leaves, 7 steps):

$$\begin{aligned}
 & -\frac{1}{4a^2bd} (a-b) \sqrt{a+b} (3Ab-4aB) \operatorname{Cot}[c+dx] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}} - \frac{1}{4a^2d} \\
 & \sqrt{a+b} (3Ab-2a(A+2B)) \operatorname{Cot}[c+dx] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}} - \frac{1}{4a^3d} \sqrt{a+b} (3Ab^2-4aBb+4a^2(A+2C)) \\
 & \operatorname{Cot}[c+dx] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}} - \\
 & \frac{(3Ab-4aB) \sqrt{a+b \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{4a^2d} + \frac{A \operatorname{Cos}[c+dx] \sqrt{a+b \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{2ad}
 \end{aligned}$$

Result (type 4, 1905 leaves):

$$\begin{aligned}
 & \frac{A(b+a \operatorname{Cos}[c+dx]) \operatorname{Sec}[c+dx] \operatorname{Sin}[2(c+dx)]}{4ad \sqrt{a+b \operatorname{Sec}[c+dx]}} + \\
 & \left( \sqrt{b+a \operatorname{Cos}[c+dx]} \sqrt{\operatorname{Sec}[c+dx]} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \right. \\
 & \left. -3aAb \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] -3Ab^2 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & 4a^2 \sqrt{\frac{-a+b}{a+b}} B \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] +4ab \sqrt{\frac{-a+b}{a+b}} B \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \\
 & 6aAb \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3 -8a^2 \sqrt{\frac{-a+b}{a+b}} B \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3 - \\
 & 3aAb \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 +3Ab^2 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 + \\
 & \left. 4a^2 \sqrt{\frac{-a+b}{a+b}} B \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 -4ab \sqrt{\frac{-a+b}{a+b}} B \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 - \right)
 \end{aligned}$$

$$8 \sqrt{a^2} A \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1 - \tan^2\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan^2\left[\frac{1}{2}(c+dx)\right]^2 + b \tan^2\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} -$$

$$6 \sqrt{A b^2} \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1 - \tan^2\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan^2\left[\frac{1}{2}(c+dx)\right]^2 + b \tan^2\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} +$$

$$8 \sqrt{a b} B \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1 - \tan^2\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan^2\left[\frac{1}{2}(c+dx)\right]^2 + b \tan^2\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} -$$

$$16 \sqrt{a^2} C \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1 - \tan^2\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan^2\left[\frac{1}{2}(c+dx)\right]^2 + b \tan^2\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} -$$

$$8 \sqrt{a^2} A \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \tan^2\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{1 - \tan^2\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan^2\left[\frac{1}{2}(c+dx)\right]^2 + b \tan^2\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} -$$

$$6 \sqrt{A b^2} \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \tan^2\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{1 - \tan^2\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan^2\left[\frac{1}{2}(c+dx)\right]^2 + b \tan^2\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + 8 \sqrt{a b} B$$

$$\operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \tan^2\left[\frac{1}{2}(c+dx)\right]^2$$



$$\begin{aligned}
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - 16 i a^2 C \\
 & \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & i (a-b) (-3Ab + 4aB) \text{EllipticE}\left[i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \\
 & \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + 2 i (3Ab^2 - ab(A+4B) + 2a^2(A+2C)) \\
 & \text{EllipticF}\left[i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \Bigg/ \\
 & \left(4a^2 \sqrt{\frac{-a+b}{a+b}} d \sqrt{a+b \sec[c+dx]} \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}} \right. \\
 & \left. \left(a \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) - b \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) \right)
 \end{aligned}$$

**Problem 964: Attempted integration timed out after 120 seconds.**

$$\int \frac{\sec[c+dx]^3 (A+B \sec[c+dx] + C \sec[c+dx]^2)}{(a+b \sec[c+dx])^{3/2}} dx$$

Optimal (type 4, 510 leaves, 6 steps):

$$\frac{1}{15 b^5 \sqrt{a+b} d} 2 (40 a^3 b B - 25 a b^3 B - 6 a^2 b^2 (5 A - 4 C) - 48 a^4 C + 3 b^4 (5 A + 3 C)) \operatorname{Cot}[c+d x]$$

$$\operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} +$$

$$\frac{1}{15 b^4 \sqrt{a+b} d} 2 (a^2 b (40 B - 36 C) - 48 a^3 C - 6 a b^2 (5 A - 5 B + 2 C) - b^3 (15 A - 5 B + 9 C)) \operatorname{Cot}[c+d x]$$

$$\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} -$$

$$\frac{2(A b^2 - a(b B - a C)) \operatorname{Sec}[c+d x]^2 \operatorname{Tan}[c+d x]}{b(a^2 - b^2) d \sqrt{a+b \operatorname{Sec}[c+d x]}} + \frac{1}{15 b^3 (a^2 - b^2) d}$$

$$2(20 a^2 b B - 5 b^3 B - 3 a b^2 (5 A - 3 C) - 24 a^3 C) \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x] +$$

$$\frac{1}{5 b^2 (a^2 - b^2) d} 2(5 A b^2 - 5 a b B + 6 a^2 C - b^2 C) \operatorname{Sec}[c+d x] \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x]$$

Result (type 1, 1 leaves):

???

### Problem 965: Attempted integration timed out after 120 seconds.

$$\int \frac{\operatorname{Sec}[c+d x]^2 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2)}{(a+b \operatorname{Sec}[c+d x])^{3/2}} dx$$

Optimal (type 4, 352 leaves, 5 steps):

$$-\frac{1}{3 b^4 \sqrt{a+b} d} 2 (6 a^2 b B - 3 b^3 B - a b^2 (3 A - 5 C) - 8 a^3 C) \operatorname{Cot}[c+d x] \operatorname{EllipticE}\left[\right.$$

$$\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} +$$

$$\frac{1}{3 b^3 \sqrt{a+b} d} 2 (3 A b^2 - (2 a+b)(b(3 B - C) - 4 a C)) \operatorname{Cot}[c+d x]$$

$$\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} +$$

$$\frac{2 a(A b^2 - a(b B - a C)) \operatorname{Tan}[c+d x]}{b^2 (a^2 - b^2) d \sqrt{a+b \operatorname{Sec}[c+d x]}} + \frac{2 C \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x]}{3 b^2 d}$$

Result (type 1, 1 leaves):

???

**Problem 966: Attempted integration timed out after 120 seconds.**

$$\int \frac{\text{Sec}[c + d x] (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2)}{(a + b \text{Sec}[c + d x])^{3/2}} dx$$

Optimal (type 4, 293 leaves, 4 steps):

$$\begin{aligned}
 & -\frac{1}{b^3 \sqrt{a+b} d} \\
 & 2 (A b^2 - a b B + 2 a^2 C - b^2 C) \text{Cot}[c + d x] \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a+b} \text{Sec}[c + d x]}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1 - \text{Sec}[c + d x])}{a+b}} \sqrt{-\frac{b(1 + \text{Sec}[c + d x])}{a-b}} + \frac{1}{b^2 \sqrt{a+b} d} \\
 & 2 (A b + b(B - C) - 2 a C) \text{Cot}[c + d x] \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a+b} \text{Sec}[c + d x]}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1 - \text{Sec}[c + d x])}{a+b}} \sqrt{-\frac{b(1 + \text{Sec}[c + d x])}{a-b}} - \frac{2 (A b^2 - a (b B - a C)) \text{Tan}[c + d x]}{b (a^2 - b^2) d \sqrt{a+b} \text{Sec}[c + d x]}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 967: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2}{(a + b \text{Sec}[c + d x])^{3/2}} dx$$

Optimal (type 4, 395 leaves, 6 steps):

$$\frac{1}{a b^2 \sqrt{a+b} d} 2 (A b^2 - a (b B - a C)) \operatorname{Cot}[c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b} \operatorname{Sec}[c+d x]}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \frac{1}{a b \sqrt{a+b} d}$$

$$2 (A b - a (B+C)) \operatorname{Cot}[c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b} \operatorname{Sec}[c+d x]}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \frac{1}{a^2 d}$$

$$2 A \sqrt{a+b} \operatorname{Cot}[c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b} \operatorname{Sec}[c+d x]}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \frac{2 (A b^2 - a (b B - a C)) \operatorname{Tan}[c+d x]}{a (a^2 - b^2) d \sqrt{a+b} \operatorname{Sec}[c+d x]}$$

Result (type 4, 1275 leaves):

$$\left( (b+a \operatorname{Cos}[c+d x])^2 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \left( \frac{4 (A b^2 - a b B + a^2 C) \operatorname{Sin}[c+d x]}{a b (-a^2 + b^2)} + \frac{4 (A b^2 \operatorname{Sin}[c+d x] - a b B \operatorname{Sin}[c+d x] + a^2 C \operatorname{Sin}[c+d x])}{a (a^2 - b^2) (b+a \operatorname{Cos}[c+d x])} \right) \right) /$$

$$(d (A+2 C+2 B \operatorname{Cos}[c+d x]+A \operatorname{Cos}[2 c+2 d x]) (a+b \operatorname{Sec}[c+d x])^{3/2}) -$$

$$\left( 4 (b+a \operatorname{Cos}[c+d x])^{3/2} (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \sqrt{\frac{1}{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}} \right.$$

$$\left( a A b^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + A b^3 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] - a^2 b B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] - \right.$$

$$a b^2 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + a^3 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + a^2 b C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] -$$

$$2 a A b^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 + 2 a^2 b B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 - 2 a^3 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 +$$

$$a A b^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - A b^3 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - a^2 b B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 +$$

$$a b^2 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + a^3 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - a^2 b C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 -$$

$$2 a^2 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right]$$

$$\left. \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \right.$$



$$\int \frac{\cos [c+d x] \left(A+B \sec [c+d x]+C \sec [c+d x]^2\right)}{\left(a+b \sec [c+d x]\right)^{3 / 2}} d x$$

Optimal (type 4, 451 leaves, 7 steps):

$$\begin{aligned} & -\frac{1}{a^2 b \sqrt{a+b} d} \\ & \left(3 A b^2-2 a b B-a^2(A-2 C)\right) \cot [c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}}+\frac{1}{a^2 b \sqrt{a+b} d} \\ & \left(3 A b^2+a b(A-2 B)+2 a^2 C\right) \cot [c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}}+\frac{1}{a^3 d} \\ & \sqrt{a+b}(3 A b-2 a B) \cot [c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}}+ \\ & \frac{A \sin [c+d x]}{a d \sqrt{a+b \sec [c+d x]}}-\frac{b\left(3 A b^2-2 a b B-a^2(A-2 C)\right) \tan [c+d x]}{a^2\left(a^2-b^2\right) d \sqrt{a+b \sec [c+d x]}} \end{aligned}$$

Result (type 4, 1814 leaves):

$$\begin{aligned} & \left(\left(b+a \cos [c+d x]\right)^2\left(A+B \sec [c+d x]+C \sec [c+d x]^2\right)\left(\frac{4\left(A b^2-a b B+a^2 C\right) \sin [c+d x]}{a^2\left(a^2-b^2\right)}-\right.\right. \\ & \left.\left.\frac{4\left(A b^3 \sin [c+d x]-a b^2 B \sin [c+d x]+a^2 b C \sin [c+d x]\right)}{a^2\left(a^2-b^2\right)\left(b+a \cos [c+d x]\right)}\right)\right) / \\ & \left(d\left(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]\right)\left(a+b \sec [c+d x]\right)^{3 / 2}\right)- \\ & \left(2\left(b+a \cos [c+d x]\right)^{3 / 2}\left(A+B \sec [c+d x]+C \sec [c+d x]^2\right)\right. \\ & \sqrt{\frac{1}{1-\tan \left[\frac{1}{2}(c+d x)\right]^2}} \sqrt{\frac{a+b-a \tan \left[\frac{1}{2}(c+d x)\right]^2+b \tan \left[\frac{1}{2}(c+d x)\right]^2}{1+\tan \left[\frac{1}{2}(c+d x)\right]^2}} \\ & \left.\left(a^3 A \tan \left[\frac{1}{2}(c+d x)\right]+a^2 A b \tan \left[\frac{1}{2}(c+d x)\right]-3 a A b^2 \tan \left[\frac{1}{2}(c+d x)\right]-\right.\right. \end{aligned}$$

$$\begin{aligned}
 & 3 A b^3 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]+2 a^2 b B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]+2 a b^2 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]- \\
 & 2 a^3 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]-2 a^2 b C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]-2 a^3 A \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3+ \\
 & 6 a A b^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3-4 a^2 b B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3+ \\
 & 4 a^3 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3+a^3 A \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5-a^2 A b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5- \\
 & 3 a A b^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5+3 A b^3 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5+2 a^2 b B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5- \\
 & 2 a b^2 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5-2 a^3 C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5+2 a^2 b C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5+ \\
 & 6 a^2 A b \operatorname{EllipticPi}\left[-1,-\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}}- \\
 & 6 A b^3 \operatorname{EllipticPi}\left[-1,-\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \\
 & \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}}- \\
 & 4 a^3 B \operatorname{EllipticPi}\left[-1,-\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \\
 & \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}}+ \\
 & 4 a b^2 B \operatorname{EllipticPi}\left[-1,-\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}}+ \\
 & 6 a^2 A b \operatorname{EllipticPi}\left[-1,-\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}}- \\
 & 6 A b^3 \operatorname{EllipticPi}\left[-1,-\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 4 a^3 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & 4 a b^2 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & (a+b) (-3 A b^2 + 2 a b B + a^2 (A - 2 C)) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \\
 & \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - 2 a (a+b) (-A b + a (B - C)) \\
 & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left. \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \right) / \\
 & \left( a^2 (a^2 - b^2) d (A + 2 C + 2 B \cos[c+dx] + A \cos[2c+2dx]) \sqrt{\sec[c+dx]} \right. \\
 & (a+b \sec[c+dx])^{3/2} \sqrt{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left. \left( a \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) - b \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \right)
 \end{aligned}$$

**Problem 969:** Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\cos[c+dx]^2 (A + B \sec[c+dx] + C \sec^2[c+dx]^2)}{(a+b \sec[c+dx])^{3/2}} dx$$



Optimal (type 4, 552 leaves, 8 steps):

$$\frac{1}{4 a^3 b \sqrt{a+b} d} (15 A b^3 + 4 a^3 B - 12 a b^2 B - a^2 (7 A b - 8 b C)) \operatorname{Cot}[c+d x]$$

$$\operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}}$$

$$\frac{1}{4 a^3 \sqrt{a+b} d} (15 A b^2 + a b (5 A - 12 B) - 2 a^2 (A + 2 B - 4 C)) \operatorname{Cot}[c+d x]$$

$$\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}}$$

$$\frac{1}{4 a^4 d} \sqrt{a+b} (15 A b^2 - 12 a b B + 4 a^2 (A + 2 C)) \operatorname{Cot}[c+d x]$$

$$\operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \frac{(5 A b - 4 a B) \operatorname{Sin}[c+d x]}{4 a^2 d \sqrt{a+b \operatorname{Sec}[c+d x]}} +$$

$$\frac{A \operatorname{Cos}[c+d x] \operatorname{Sin}[c+d x]}{2 a d \sqrt{a+b \operatorname{Sec}[c+d x]}} + \frac{b(15 A b^3 + 4 a^3 B - 12 a b^2 B - a^2 (7 A b - 8 b C)) \operatorname{Tan}[c+d x]}{4 a^3 (a^2 - b^2) d \sqrt{a+b \operatorname{Sec}[c+d x]}}$$

Result (type 4, 746 leaves):

$$\frac{1}{2} \left( (b + a \operatorname{Cos}[c+d x])^2 \operatorname{Sec}[c+d x]^2 \left( \frac{4 b (A b^2 - a b B + a^2 C) \operatorname{Sin}[c+d x]}{a^3 (-a^2 + b^2)} + \right. \right.$$

$$\left. \left. \frac{(4 (A b^4 \operatorname{Sin}[c+d x] - a b^3 B \operatorname{Sin}[c+d x] + a^2 b^2 C \operatorname{Sin}[c+d x]))}{(a^3 (a^2 - b^2) (b + a \operatorname{Cos}[c+d x])) + \frac{A \operatorname{Sin}[2(c+d x)]}{2 a^2}} \right) \right) /$$

$$(d (a + b \operatorname{Sec}[c+d x])^{3/2}) + \frac{1}{2 a^3 (a^2 - b^2) d (a + b \operatorname{Sec}[c+d x])^{3/2} \sqrt{\frac{1 + \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{1 - \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}}}$$

$$(b + a \operatorname{Cos}[c+d x])^{3/2} \operatorname{Sec}[c+d x]^{3/2} \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}}$$

$$\left( \frac{(15 A b^3 + 4 a^3 B - 12 a b^2 B + a^2 (-7 A b + 8 b C)) \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] - \sqrt{\frac{-a+b}{a+b}} \left(b - b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] + a \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right)^2\right)^2}{1} \right.$$

$$+ i (a - b) \left( (-15 A b^3 - 4 a^3 B + 12 a b^2 B + a^2 b (7 A - 8 C)) \right.$$

$$\operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right], \frac{a+b}{a-b}\right] +$$

$$2 (15 A b^3 + 2 a b^2 (5 A - 6 B) + 2 a^3 (A + 2 C) + a^2 b (A - 8 B + 8 C))$$

$$\operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right], \frac{a+b}{a-b}\right] -$$

$$2 (a + b) (15 A b^2 - 12 a b B + 4 a^2 (A + 2 C)) \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, \right.$$

$$i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right], \frac{a+b}{a-b}\right] \left. \left(-1 - \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right)^2 \right)$$

$$\left. \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2} \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{a + b}} \right)$$

**Problem 970: Attempted integration timed out after 120 seconds.**

$$\int \frac{\operatorname{Sec}[c + d x]^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{(a + b \operatorname{Sec}[c + d x])^{5/2}} dx$$

Optimal (type 4, 549 leaves, 6 steps):

$$\begin{aligned}
 & - \left( \left( 2 (8 a^4 b B - 15 a^2 b^3 B + 3 b^5 B - 2 a^3 b^2 (A - 14 C) + 2 a b^4 (3 A - 4 C) - 16 a^5 C) \right. \right. \\
 & \quad \left. \left. \text{Cot}[c + d x] \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \right. \right. \\
 & \quad \left. \left. \sqrt{\frac{b (1 - \text{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b (1 + \text{Sec}[c + d x])}{a - b}} \right) / \left( 3 b^5 \sqrt{a + b} (a^2 - b^2) d \right) \right) - \\
 & \left( 2 (a^3 b (8 B - 12 C) - 2 a^2 b^2 (A - 3 B - 8 C) - 3 a b^3 (A + 3 B - 3 C) - 16 a^4 C + b^4 (3 A - 3 B + C)) \right. \\
 & \quad \left. \text{Cot}[c + d x] \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \right. \\
 & \quad \left. \sqrt{\frac{b (1 - \text{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b (1 + \text{Sec}[c + d x])}{a - b}} \right) / \left( 3 b^4 \sqrt{a + b} (a^2 - b^2) d \right) - \\
 & \frac{2 (A b^2 - a (b B - a C)) \text{Sec}[c + d x]^2 \text{Tan}[c + d x]}{3 b (a^2 - b^2) d (a + b \text{Sec}[c + d x])^{3/2}} - \\
 & \frac{2 a (4 A b^4 + a (3 a^2 b B - 7 b^3 B - 6 a^3 C + 10 a b^2 C)) \text{Tan}[c + d x]}{3 b^3 (a^2 - b^2)^2 d \sqrt{a + b \text{Sec}[c + d x]}} + \\
 & \frac{2 (A b^2 - a b B + 2 a^2 C - b^2 C) \sqrt{a + b \text{Sec}[c + d x]} \text{Tan}[c + d x]}{3 b^3 (a^2 - b^2) d}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 971: Attempted integration timed out after 120 seconds.**

$$\int \frac{\text{Sec}[c + d x]^2 (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2)}{(a + b \text{Sec}[c + d x])^{5/2}} dx$$

Optimal (type 4, 449 leaves, 5 steps):

$$\left( 2 (2 a^3 b B - 6 a b^3 B + 3 b^4 (A - C) - 8 a^4 C + a^2 b^2 (A + 15 C)) \right. \\ \left. \text{Cot}[c + d x] \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \right. \\ \left. \sqrt{\frac{b (1 - \text{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b (1 + \text{Sec}[c + d x])}{a - b}} \right) / (3 b^4 \sqrt{a + b} (a^2 - b^2) d) + \\ \left( 2 (2 a^2 b (B - 3 C) - 3 b^3 (A + B - C) - 8 a^3 C + a b^2 (A + 3 B + 9 C)) \text{Cot}[c + d x] \text{EllipticF}\left[ \right. \right. \\ \left. \left. \text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \sqrt{\frac{b (1 - \text{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b (1 + \text{Sec}[c + d x])}{a - b}} \right) / \\ (3 b^3 \sqrt{a + b} (a^2 - b^2) d) + \frac{2 a (A b^2 - a (b B - a C)) \text{Tan}[c + d x]}{3 b^2 (a^2 - b^2) d (a + b \text{Sec}[c + d x])^{3/2}} + \\ \frac{2 (3 A b^4 + 2 a^3 b B - 6 a b^3 B - 5 a^4 C + a^2 b^2 (A + 9 C)) \text{Tan}[c + d x]}{3 b^2 (a^2 - b^2)^2 d \sqrt{a + b \text{Sec}[c + d x]}}$$

Result (type 1, 1 leaves):

???

**Problem 972: Attempted integration timed out after 120 seconds.**

$$\int \frac{\text{Sec}[c + d x] (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2)}{(a + b \text{Sec}[c + d x])^{5/2}} dx$$

Optimal (type 4, 416 leaves, 5 steps):

$$\begin{aligned}
 & - \left( \left( 2 (4 a A b^2 - a^2 b B - 3 b^3 B - 2 a^3 C + 6 a b^2 C) \cot [c + d x] \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \operatorname{Sec} [c + d x]}}{\sqrt{a + b}} \right] \right], \right. \right. \\
 & \quad \left. \left. \frac{a + b}{a - b} \sqrt{\frac{b (1 - \operatorname{Sec} [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec} [c + d x])}{a - b}} \right] / \left( 3 (a - b) b^3 (a + b)^{3/2} d \right) \right) + \\
 & \left( 2 (2 a^2 C + a b (3 A + B + 3 C) - b^2 (A + 3 (B + C))) \cot [c + d x] \operatorname{EllipticF} \left[ \right. \right. \\
 & \quad \left. \left. \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \operatorname{Sec} [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \sqrt{\frac{b (1 - \operatorname{Sec} [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec} [c + d x])}{a - b}} \right] / \right. \\
 & \quad \left. \left( 3 b^2 \sqrt{a + b} (a^2 - b^2) d \right) - \frac{2 (A b^2 - a (b B - a C)) \tan [c + d x]}{3 b (a^2 - b^2) d (a + b \operatorname{Sec} [c + d x])^{3/2}} + \right. \\
 & \quad \left. \frac{2 (a^2 b B + 3 b^3 B + 2 a^3 C - 2 a b^2 (2 A + 3 C)) \tan [c + d x]}{3 b (a^2 - b^2)^2 d \sqrt{a + b \operatorname{Sec} [c + d x]}} \right)
 \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 973: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2}{(a + b \operatorname{Sec} [c + d x])^{5/2}} dx$$

Optimal (type 4, 541 leaves, 7 steps):

$$\left( 2 (7 a^2 A b^2 - 3 A b^4 - 4 a^3 b B + a^4 C + 3 a^2 b^2 C) \operatorname{Cot}[c + d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}}\right]\right], \right.$$

$$\left. \frac{a + b}{a - b} \sqrt{\frac{b (1 - \operatorname{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec}[c + d x])}{a - b}} \right) / (3 a^2 (a - b) b^2 (a + b)^{3/2} d) +$$

$$\left( 2 (a A b^2 + 3 A b^3 + a^3 (3 B + C) - a^2 b (6 A + B + 3 C)) \operatorname{Cot}[c + d x] \right.$$

$$\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \sqrt{\frac{b (1 - \operatorname{Sec}[c + d x])}{a + b}}$$

$$\left. \sqrt{-\frac{b (1 + \operatorname{Sec}[c + d x])}{a - b}} \right) / (3 a^2 b \sqrt{a + b} (a^2 - b^2) d) - \frac{1}{a^3 d}$$

$$2 A \sqrt{a + b} \operatorname{Cot}[c + d x] \operatorname{EllipticPi}\left[\frac{a + b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right]$$

$$\sqrt{\frac{b (1 - \operatorname{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec}[c + d x])}{a - b}} +$$

$$\frac{2 (A b^2 - a (b B - a C)) \operatorname{Tan}[c + d x]}{3 a (a^2 - b^2) d (a + b \operatorname{Sec}[c + d x])^{3/2}} -$$

$$\frac{2 (3 A b^4 + 4 a^3 b B - a^4 C - a^2 b^2 (7 A + 3 C)) \operatorname{Tan}[c + d x]}{3 a^2 (a^2 - b^2)^2 d \sqrt{a + b \operatorname{Sec}[c + d x]}}$$

Result (type 4, 1919 leaves):

$$\left( (b + a \operatorname{Cos}[c + d x])^3 \operatorname{Sec}[c + d x] (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right.$$

$$\left( \frac{4 (-7 a^2 A b^2 + 3 A b^4 + 4 a^3 b B - a^4 C - 3 a^2 b^2 C) \operatorname{Sin}[c + d x]}{3 a^2 b (-a^2 + b^2)^2} - \right.$$

$$\left. \frac{4 (A b^3 \operatorname{Sin}[c + d x] - a b^2 B \operatorname{Sin}[c + d x] + a^2 b C \operatorname{Sin}[c + d x])}{3 a^2 (a^2 - b^2) (b + a \operatorname{Cos}[c + d x])^2} + \right.$$

$$\left. (4 (8 a^2 A b^2 \operatorname{Sin}[c + d x] - 4 A b^4 \operatorname{Sin}[c + d x] - 5 a^3 b B \operatorname{Sin}[c + d x] + a b^3 B \operatorname{Sin}[c + d x] + \right.$$

$$\left. 2 a^4 C \operatorname{Sin}[c + d x] + 2 a^2 b^2 C \operatorname{Sin}[c + d x]) \right) / (3 a^2 (a^2 - b^2)^2 (b + a \operatorname{Cos}[c + d x])) \Big) /$$

$$(d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) (a + b \operatorname{Sec}[c + d x])^{5/2}) -$$

$$\left( 4 (b + a \cos [c + d x])^{5/2} \sqrt{\sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right.$$

$$\sqrt{\frac{1}{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}}$$

$$\left( 7 a^3 A b^2 \tan \left[ \frac{1}{2} (c + d x) \right] + 7 a^2 A b^3 \tan \left[ \frac{1}{2} (c + d x) \right] - 3 a A b^4 \tan \left[ \frac{1}{2} (c + d x) \right] - \right.$$

$$3 A b^5 \tan \left[ \frac{1}{2} (c + d x) \right] - 4 a^4 b B \tan \left[ \frac{1}{2} (c + d x) \right] - 4 a^3 b^2 B \tan \left[ \frac{1}{2} (c + d x) \right] +$$

$$a^5 C \tan \left[ \frac{1}{2} (c + d x) \right] + a^4 b C \tan \left[ \frac{1}{2} (c + d x) \right] + 3 a^3 b^2 C \tan \left[ \frac{1}{2} (c + d x) \right] +$$

$$3 a^2 b^3 C \tan \left[ \frac{1}{2} (c + d x) \right] - 14 a^3 A b^2 \tan \left[ \frac{1}{2} (c + d x) \right]^3 + 6 a A b^4 \tan \left[ \frac{1}{2} (c + d x) \right]^3 +$$

$$8 a^4 b B \tan \left[ \frac{1}{2} (c + d x) \right]^3 - 2 a^5 C \tan \left[ \frac{1}{2} (c + d x) \right]^3 - 6 a^3 b^2 C \tan \left[ \frac{1}{2} (c + d x) \right]^3 +$$

$$7 a^3 A b^2 \tan \left[ \frac{1}{2} (c + d x) \right]^5 - 7 a^2 A b^3 \tan \left[ \frac{1}{2} (c + d x) \right]^5 - 3 a A b^4 \tan \left[ \frac{1}{2} (c + d x) \right]^5 +$$

$$3 A b^5 \tan \left[ \frac{1}{2} (c + d x) \right]^5 - 4 a^4 b B \tan \left[ \frac{1}{2} (c + d x) \right]^5 + 4 a^3 b^2 B \tan \left[ \frac{1}{2} (c + d x) \right]^5 +$$

$$a^5 C \tan \left[ \frac{1}{2} (c + d x) \right]^5 - a^4 b C \tan \left[ \frac{1}{2} (c + d x) \right]^5 + 3 a^3 b^2 C \tan \left[ \frac{1}{2} (c + d x) \right]^5 -$$

$$3 a^2 b^3 C \tan \left[ \frac{1}{2} (c + d x) \right]^5 - 6 a^4 A b \operatorname{EllipticPi} \left[ -1, -\operatorname{ArcSin} \left[ \tan \left[ \frac{1}{2} (c + d x) \right] \right] \right], \frac{a - b}{a + b} \right]$$

$$\sqrt{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2} \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} +$$

$$12 a^2 A b^3 \operatorname{EllipticPi} \left[ -1, -\operatorname{ArcSin} \left[ \tan \left[ \frac{1}{2} (c + d x) \right] \right] \right], \frac{a - b}{a + b} \right]$$

$$\sqrt{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2} \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} -$$

$$6 A b^5 \operatorname{EllipticPi} \left[ -1, -\operatorname{ArcSin} \left[ \tan \left[ \frac{1}{2} (c + d x) \right] \right] \right], \frac{a - b}{a + b} \right] \sqrt{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2}$$

$$\sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} -$$

$$6 a^4 A b \operatorname{EllipticPi} \left[ -1, -\operatorname{ArcSin} \left[ \tan \left[ \frac{1}{2} (c + d x) \right] \right] \right], \frac{a - b}{a + b} \right] \tan \left[ \frac{1}{2} (c + d x) \right]^2$$

$$\begin{aligned}
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & 12 a^2 A b^3 \text{EllipticPi}\left[-1, -\text{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 6 A b^5 \text{EllipticPi}\left[-1, -\text{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & (a+b) (-3 A b^4 - 4 a^3 b B + a^4 C + a^2 b^2 (7 A + 3 C)) \\
 & \text{EllipticE}\left[\text{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & a b (a+b) (-2 A b^2 + a^2 (3 A - 3 B + C) + a b (3 A - B + 3 C)) \\
 & \text{EllipticF}\left[\text{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \Bigg) / \\
 & \left( 3 a^2 b (a^2 - b^2)^2 d (A + 2 C + 2 B \cos[c+dx] + A \cos[2c+2dx]) \right. \\
 & (a+b \sec[c+dx])^{5/2} \sqrt{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left. \left( a \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) - b \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \right)
 \end{aligned}$$

**Problem 974: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c+dx] (A+B \sec[c+dx] + C \sec[c+dx]^2)}{(a+b \sec[c+dx])^{5/2}} dx$$



Optimal (type 4, 618 leaves, 8 steps):

$$\begin{aligned}
 & - \left( \left( (26 a^2 A b^2 - 15 A b^4 - 14 a^3 b B + 6 a b^3 B - a^4 (3 A - 8 C)) \right. \right. \\
 & \quad \left. \left. \text{Cot}[c + d x] \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \right. \right. \\
 & \quad \left. \left. \sqrt{\frac{b(1 - \text{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \text{Sec}[c + d x])}{a - b}} \right) / (3 a^3 (a - b) b (a + b)^{3/2} d) \right) - \\
 & \left( (15 A b^4 + a b^3 (5 A - 6 B) - a^2 b^2 (21 A + 2 B) - 6 a^4 C - a^3 b (3 A - 2 (6 B + C))) \text{Cot}[c + d x] \right. \\
 & \quad \left. \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \sqrt{\frac{b(1 - \text{Sec}[c + d x])}{a + b}} \right. \\
 & \quad \left. \sqrt{-\frac{b(1 + \text{Sec}[c + d x])}{a - b}} \right) / (3 a^3 b \sqrt{a + b} (a^2 - b^2) d) + \frac{1}{a^4 d} \\
 & \sqrt{a + b} (5 A b - 2 a B) \text{Cot}[c + d x] \text{EllipticPi}\left[\frac{a + b}{a}, \text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \\
 & \sqrt{\frac{b(1 - \text{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \text{Sec}[c + d x])}{a - b}} + \\
 & \frac{A \text{Sin}[c + d x]}{a d (a + b \text{Sec}[c + d x])^{3/2}} - \frac{b(5 A b^2 - 2 a b B - a^2 (3 A - 2 C)) \text{Tan}[c + d x]}{3 a^2 (a^2 - b^2) d (a + b \text{Sec}[c + d x])^{3/2}} - \\
 & \frac{b(26 a^2 A b^2 - 15 A b^4 - 14 a^3 b B + 6 a b^3 B - a^4 (3 A - 8 C)) \text{Tan}[c + d x]}{3 a^3 (a^2 - b^2)^2 d \sqrt{a + b \text{Sec}[c + d x]}}
 \end{aligned}$$

Result (type 4, 2631 leaves):

$$\begin{aligned}
 & \left( (b + a \text{Cos}[c + d x])^3 \text{Sec}[c + d x] (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) \right. \\
 & \left( -\frac{4(-10 a^2 A b^2 + 6 A b^4 + 7 a^3 b B - 3 a b^3 B - 4 a^4 C) \text{Sin}[c + d x]}{3 a^3 (-a^2 + b^2)^2} + \right. \\
 & \quad \left. \frac{4(A b^4 \text{Sin}[c + d x] - a b^3 B \text{Sin}[c + d x] + a^2 b^2 C \text{Sin}[c + d x])}{3 a^3 (a^2 - b^2) (b + a \text{Cos}[c + d x])^2} + \right. \\
 & \quad \left. (4(-11 a^2 A b^3 \text{Sin}[c + d x] + 7 A b^5 \text{Sin}[c + d x] + 8 a^3 b^2 B \text{Sin}[c + d x] - 4 a b^4 B \text{Sin}[c + d x] - \right. \\
 & \quad \left. \left. 5 a^4 b C \text{Sin}[c + d x] + a^2 b^3 C \text{Sin}[c + d x]) \right) / (3 a^3 (a^2 - b^2)^2 (b + a \text{Cos}[c + d x])) \right) \Big) /
 \end{aligned}$$

$$\begin{aligned}
& \left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) (a + b \sec [c + dx])^{5/2} \right) - \\
& \left( 2 (b + a \cos [c + dx])^{5/2} \sqrt{\sec [c + dx]} (A + B \sec [c + dx] + C \sec [c + dx]^2) \right. \\
& \sqrt{\frac{1}{1 - \tan \left[ \frac{1}{2} (c + dx) \right]^2}} \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + dx) \right]^2 + b \tan \left[ \frac{1}{2} (c + dx) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + dx) \right]^2}} \\
& \left( 3 a^5 A \tan \left[ \frac{1}{2} (c + dx) \right] + 3 a^4 A b \tan \left[ \frac{1}{2} (c + dx) \right] - 26 a^3 A b^2 \tan \left[ \frac{1}{2} (c + dx) \right] - \right. \\
& 26 a^2 A b^3 \tan \left[ \frac{1}{2} (c + dx) \right] + 15 a A b^4 \tan \left[ \frac{1}{2} (c + dx) \right] + 15 A b^5 \tan \left[ \frac{1}{2} (c + dx) \right] + \\
& 14 a^4 b B \tan \left[ \frac{1}{2} (c + dx) \right] + 14 a^3 b^2 B \tan \left[ \frac{1}{2} (c + dx) \right] - 6 a^2 b^3 B \tan \left[ \frac{1}{2} (c + dx) \right] - \\
& 6 a b^4 B \tan \left[ \frac{1}{2} (c + dx) \right] - 8 a^5 C \tan \left[ \frac{1}{2} (c + dx) \right] - 8 a^4 b C \tan \left[ \frac{1}{2} (c + dx) \right] - \\
& 6 a^5 A \tan \left[ \frac{1}{2} (c + dx) \right]^3 + 52 a^3 A b^2 \tan \left[ \frac{1}{2} (c + dx) \right]^3 - 30 a A b^4 \tan \left[ \frac{1}{2} (c + dx) \right]^3 - \\
& 28 a^4 b B \tan \left[ \frac{1}{2} (c + dx) \right]^3 + 12 a^2 b^3 B \tan \left[ \frac{1}{2} (c + dx) \right]^3 + 16 a^5 C \tan \left[ \frac{1}{2} (c + dx) \right]^3 + \\
& 3 a^5 A \tan \left[ \frac{1}{2} (c + dx) \right]^5 - 3 a^4 A b \tan \left[ \frac{1}{2} (c + dx) \right]^5 - 26 a^3 A b^2 \tan \left[ \frac{1}{2} (c + dx) \right]^5 + \\
& 26 a^2 A b^3 \tan \left[ \frac{1}{2} (c + dx) \right]^5 + 15 a A b^4 \tan \left[ \frac{1}{2} (c + dx) \right]^5 - 15 A b^5 \tan \left[ \frac{1}{2} (c + dx) \right]^5 + \\
& 14 a^4 b B \tan \left[ \frac{1}{2} (c + dx) \right]^5 - 14 a^3 b^2 B \tan \left[ \frac{1}{2} (c + dx) \right]^5 - 6 a^2 b^3 B \tan \left[ \frac{1}{2} (c + dx) \right]^5 + \\
& 6 a b^4 B \tan \left[ \frac{1}{2} (c + dx) \right]^5 - 8 a^5 C \tan \left[ \frac{1}{2} (c + dx) \right]^5 + 8 a^4 b C \tan \left[ \frac{1}{2} (c + dx) \right]^5 + \\
& 30 a^4 A b \operatorname{EllipticPi} \left[ -1, -\operatorname{ArcSin} \left[ \tan \left[ \frac{1}{2} (c + dx) \right] \right], \frac{a - b}{a + b} \right] \\
& \sqrt{1 - \tan \left[ \frac{1}{2} (c + dx) \right]^2} \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + dx) \right]^2 + b \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b}} - \\
& 60 a^2 A b^3 \operatorname{EllipticPi} \left[ -1, -\operatorname{ArcSin} \left[ \tan \left[ \frac{1}{2} (c + dx) \right] \right], \frac{a - b}{a + b} \right] \\
& \sqrt{1 - \tan \left[ \frac{1}{2} (c + dx) \right]^2} \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + dx) \right]^2 + b \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b}} + \\
& 30 A b^5 \operatorname{EllipticPi} \left[ -1, -\operatorname{ArcSin} \left[ \tan \left[ \frac{1}{2} (c + dx) \right] \right], \frac{a - b}{a + b} \right]
\end{aligned}$$

$$\begin{aligned}
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 12 & a^5 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 24 & a^3 b^2 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 12 & a b^4 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 30 & a^4 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 60 & a^2 A b^3 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 30 & A b^5 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 12 & a^5 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 24 & a^3 b^2 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2
 \end{aligned}$$



$$\begin{aligned}
 & -\frac{1}{d} 2 (a-b) \sqrt{a+b} C \cot [c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{1}{d} \\
 & 2 b \sqrt{a+b} (B-C) \cot [c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} - \frac{1}{d} \\
 & 2 \sqrt{a+b} (b B-a C) \cot [c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}}
 \end{aligned}$$

Result (type 4, 1232 leaves):

$$\begin{aligned}
 & \left(2 b C \cos [c+d x] \sqrt{a+b \sec [c+d x]} (b B-a C+b C \sec [c+d x]) \sin [c+d x]\right) / \\
 & \left(d (b C+b B \cos [c+d x]-a C \cos [c+d x])\right) + \\
 & \left(2 \sqrt{a+b \sec [c+d x]} (b B-a C+b C \sec [c+d x])\right) \left(a b \sqrt{\frac{-a+b}{a+b}} C \tan \left[\frac{1}{2}(c+d x)\right] + \right. \\
 & b^2 \sqrt{\frac{-a+b}{a+b}} C \tan \left[\frac{1}{2}(c+d x)\right] - 2 a b \sqrt{\frac{-a+b}{a+b}} C \tan \left[\frac{1}{2}(c+d x)\right]^3 + \\
 & a b \sqrt{\frac{-a+b}{a+b}} C \tan \left[\frac{1}{2}(c+d x)\right]^5 - b^2 \sqrt{\frac{-a+b}{a+b}} C \tan \left[\frac{1}{2}(c+d x)\right]^5 + \\
 & 2 i a b B \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan \left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{1-\tan \left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \tan \left[\frac{1}{2}(c+d x)\right]^2+b \tan \left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
 & 2 i a^2 C \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan \left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{1-\tan \left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \tan \left[\frac{1}{2}(c+d x)\right]^2+b \tan \left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + 2 i a b B
 \end{aligned}$$

$$\begin{aligned}
 & \text{EllipticPi}\left[-\frac{a+b}{a-b}, \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a\tan\left[\frac{1}{2}(c+dx)\right]^2+b\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 2 \text{ i } a^2 C \text{EllipticPi}\left[-\frac{a+b}{a-b}, \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a\tan\left[\frac{1}{2}(c+dx)\right]^2+b\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & \text{ i } (a-b) b C \text{EllipticE}\left[\text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} \left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \\
 & \sqrt{\frac{a+b-a\tan\left[\frac{1}{2}(c+dx)\right]^2+b\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \text{ i } (a-b) (aC+b(-B+C)) \\
 & \text{EllipticF}\left[\text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b-a\tan\left[\frac{1}{2}(c+dx)\right]^2+b\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \Big/ \\
 & \left( \sqrt{\frac{-a+b}{a+b}} d \sqrt{b+a \cos[c+dx]} (bC+bB \cos[c+dx]-aC \cos[c+dx]) \right. \\
 & \text{Sec}[c+dx]^{3/2} \sqrt{\frac{1}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}} \\
 & \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^{3/2} \\
 & \left. \sqrt{\frac{a+b-a\tan\left[\frac{1}{2}(c+dx)\right]^2+b\tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}} \right)
 \end{aligned}$$

**Problem 979: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{a b B - a^2 C + b^2 B \operatorname{Sec}[c + d x] + b^2 C \operatorname{Sec}[c + d x]^2}{(a + b \operatorname{Sec}[c + d x])^{5/2}} dx$$

Optimal (type 4, 379 leaves, 7 steps):

$$\begin{aligned} & \frac{1}{a \sqrt{a+b} d} 2 (b B - 2 a C) \operatorname{Cot}[c + d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c + d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1 - \operatorname{Sec}[c + d x])}{a+b}} \sqrt{-\frac{b(1 + \operatorname{Sec}[c + d x])}{a-b}} - \frac{1}{a \sqrt{a+b} d} 2 (b B - 2 a C) \operatorname{Cot}[c + d x] \\ & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c + d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1 - \operatorname{Sec}[c + d x])}{a+b}} \sqrt{-\frac{b(1 + \operatorname{Sec}[c + d x])}{a-b}} - \\ & \frac{1}{a^2 d} 2 \sqrt{a+b} (b B - a C) \operatorname{Cot}[c + d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c + d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1 - \operatorname{Sec}[c + d x])}{a+b}} \sqrt{-\frac{b(1 + \operatorname{Sec}[c + d x])}{a-b}} + \frac{2 b^2 (b B - 2 a C) \operatorname{Tan}[c + d x]}{a (a^2 - b^2) d \sqrt{a+b \operatorname{Sec}[c + d x]}} \end{aligned}$$

Result (type 4, 2090 leaves):

$$\begin{aligned} & \left( (b + a \operatorname{Cos}[c + d x])^2 \operatorname{Sec}[c + d x] (b B - a C + b C \operatorname{Sec}[c + d x]) \right. \\ & \left. \left( \frac{2 b (b B - 2 a C) \operatorname{Sin}[c + d x]}{a (-a^2 + b^2)} - \frac{2 (-b^3 B \operatorname{Sin}[c + d x] + 2 a b^2 C \operatorname{Sin}[c + d x])}{a (a^2 - b^2) (b + a \operatorname{Cos}[c + d x])} \right) \right) / \\ & (d (b C + b B \operatorname{Cos}[c + d x] - a C \operatorname{Cos}[c + d x]) (a + b \operatorname{Sec}[c + d x])^{3/2}) - \\ & \left( 2 (b + a \operatorname{Cos}[c + d x])^{3/2} \sqrt{\operatorname{Sec}[c + d x]} (b B - a C + b C \operatorname{Sec}[c + d x]) \right. \\ & \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}} \\ & \left. \left( -a b^2 \sqrt{\frac{-a+b}{a+b}} B \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] - b^3 \sqrt{\frac{-a+b}{a+b}} B \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] + \right. \right. \\ & \left. \left. 2 a^2 b \sqrt{\frac{-a+b}{a+b}} C \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] + 2 a b^2 \sqrt{\frac{-a+b}{a+b}} C \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] \right) \right) \end{aligned}$$

$$\begin{aligned}
 & 2 a b^2 \sqrt{\frac{-a+b}{a+b}} B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 - 4 a^2 b \sqrt{\frac{-a+b}{a+b}} C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 - \\
 & a b^2 \sqrt{\frac{-a+b}{a+b}} B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + b^3 \sqrt{\frac{-a+b}{a+b}} B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + \\
 & 2 a^2 b \sqrt{\frac{-a+b}{a+b}} C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - 2 a b^2 \sqrt{\frac{-a+b}{a+b}} C \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + \\
 & 2 i a^2 b B \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
 & 2 i b^3 B \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
 & 2 i a^3 C \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \\
 & 2 i a b^2 C \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + 2 i a^2 b B \\
 & \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} -
 \end{aligned}$$



$$\begin{aligned}
 & 2 \, i \, b^3 B \operatorname{EllipticPi} \left[ -\frac{a+b}{a-b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right], \frac{a+b}{a-b} \right] \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \\
 & \sqrt{1 - \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \sqrt{\frac{a+b - a \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} - \\
 & 2 \, i \, a^3 C \operatorname{EllipticPi} \left[ -\frac{a+b}{a-b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right], \frac{a+b}{a-b} \right] \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \\
 & \sqrt{1 - \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \sqrt{\frac{a+b - a \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} + 2 \, i \, a \, b^2 C \\
 & \operatorname{EllipticPi} \left[ -\frac{a+b}{a-b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right], \frac{a+b}{a-b} \right] \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \\
 & \sqrt{1 - \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \sqrt{\frac{a+b - a \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} - \\
 & i (a-b) b (-b B + 2 a C) \operatorname{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right], \frac{a+b}{a-b} \right] \\
 & \sqrt{1 - \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \\
 & \sqrt{\frac{a+b - a \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} + i (a-b) (-2 b^2 B - a b (B - 3 C) + a^2 C) \\
 & \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right], \frac{a+b}{a-b} \right] \sqrt{1 - \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \\
 & \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \sqrt{\frac{a+b - a \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} \right) \Bigg) / \\
 & \left( a \sqrt{\frac{-a+b}{a+b}} (a^2 - b^2) d (b C + b B \operatorname{Cos} [c+dx] - a C \operatorname{Cos} [c+dx]) (a+b \operatorname{Sec} [c+dx])^{3/2} \right. \\
 & \left. (-1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2) \sqrt{\frac{1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{1 - \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}} \right)
 \end{aligned}$$

$$\left( a \left( -1 + \tan \left[ \frac{1}{2} (c + dx) \right] \right)^2 - b \left( 1 + \tan \left[ \frac{1}{2} (c + dx) \right] \right)^2 \right)$$

**Problem 980: Result more than twice size of optimal antiderivative.**

$$\int \frac{a b B - a^2 C + b^2 B \operatorname{Sec}[c + dx] + b^2 C \operatorname{Sec}[c + dx]^2}{(a + b \operatorname{Sec}[c + dx])^{7/2}} dx$$

Optimal (type 4, 519 leaves, 8 steps):

$$\left( 2 (7 a^2 b B - 3 b^3 B - 11 a^3 C + 3 a b^2 C) \operatorname{Cot}[c + dx] \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \operatorname{Sec}[c + dx]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \right. \\ \left. \sqrt{\frac{b (1 - \operatorname{Sec}[c + dx])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec}[c + dx])}{a - b}} \right) / (3 a^2 (a - b) (a + b)^{3/2} d) + \\ \left( 2 (3 b^3 B + a b^2 (B - 3 C) + 9 a^3 C - 2 a^2 b (3 B + C)) \operatorname{Cot}[c + dx] \right. \\ \left. \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \operatorname{Sec}[c + dx]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \sqrt{\frac{b (1 - \operatorname{Sec}[c + dx])}{a + b}} \right. \\ \left. \sqrt{-\frac{b (1 + \operatorname{Sec}[c + dx])}{a - b}} \right) / (3 a^2 \sqrt{a + b} (a^2 - b^2) d) - \frac{1}{a^3 d} \\ 2 \sqrt{a + b} (b B - a C) \operatorname{Cot}[c + dx] \operatorname{EllipticPi} \left[ \frac{a + b}{a}, \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \operatorname{Sec}[c + dx]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \\ \sqrt{\frac{b (1 - \operatorname{Sec}[c + dx])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec}[c + dx])}{a - b}} + \\ \frac{2 b^2 (b B - 2 a C) \operatorname{Tan}[c + dx]}{3 a (a^2 - b^2) d (a + b \operatorname{Sec}[c + dx])^{3/2}} + \frac{2 b^2 (7 a^2 b B - 3 b^3 B - 11 a^3 C + 3 a b^2 C) \operatorname{Tan}[c + dx]}{3 a^2 (a^2 - b^2)^2 d \sqrt{a + b \operatorname{Sec}[c + dx]}}$$

Result (type 4, 4657 leaves):

$$\left( (b + a \operatorname{Cos}[c + dx])^3 \operatorname{Sec}[c + dx]^2 \right. \\ \left. (b B - a C + b C \operatorname{Sec}[c + dx]) \left( \frac{2 b (-7 a^2 b B + 3 b^3 B + 11 a^3 C - 3 a b^2 C) \operatorname{Sin}[c + dx]}{3 a^2 (-a^2 + b^2)^2} - \right. \right. \\ \left. \left. \frac{2 (b^4 B \operatorname{Sin}[c + dx] - 2 a b^3 C \operatorname{Sin}[c + dx])}{3 a^2 (a^2 - b^2) (b + a \operatorname{Cos}[c + dx])^2} - (2 (-8 a^2 b^3 B \operatorname{Sin}[c + dx] + 4 b^5 B \operatorname{Sin}[c + dx] + \right. \right.$$



$$\begin{aligned}
 & \left. \frac{a-b}{a+b} \right) \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \\
 & \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^4} \Big/ \\
 & \left( 3 a^2 (a^2-b^2)^2 \sqrt{\frac{1}{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \right. \\
 & \left. \left( b-b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^4+a\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \right) \right) \Big/ \\
 & \left( d(b C+b B \operatorname{Cos}[c+dx]-a C \operatorname{Cos}[c+dx]) (a+b \operatorname{Sec}[c+dx])^{5/2} \right. \\
 & \left. - \left( \left( b\left(-7 a^2 b B+3 b^3 B+11 a^3 C-3 a b^2 C\right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \right. \\
 & \left. \left. \left. \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \right) \right) \right. \\
 & \left. \left( 3 a^2 (a^2-b^2)^2 \sqrt{\frac{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \right) \right) - \left( 2(a+b) \right. \\
 & \left. -b\left(-7 a^2 b B+3 b^3 B+11 a^3 C-3 a b^2 C\right) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] + \right. \\
 & \left. a\left(2 b^3 B-3 a^2 b(B-2 C)+3 a^3 C-a b^2(3 B+C)\right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \right. \\
 & \left. \frac{a-b}{a+b}\right] + 6(a-b)^2(a+b)(-b B+a C) \operatorname{EllipticPi}\left[-1,-\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \right. \\
 & \left. \frac{a-b}{a+b}\right) \Big/ \\
 & \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \\
 & \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^4} \\
 & \left( -2 b \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3 + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. 2 a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] \left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)\right) \Bigg/ \left(3 a^2\left(a^2-b^2\right)^2\right. \\
 & \left.\sqrt{\frac{1}{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}}\left(b-b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^4+a\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)^2\right)^2\right)- \\
 & \left(2(a+b)\left(-b\left(-7 a^2 b B+3 b^3 B+11 a^3 C-3 a b^2 C\right) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right]\right],\right. \right. \\
 & \quad \left.\frac{a-b}{a+b}\right)+a\left(2 b^3 B-3 a^2 b(B-2 C)+3 a^3 C-a b^2(3 B+C)\right) \\
 & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right]+6(a-b)^2(a+b)(-b B+a C) \\
 & \operatorname{EllipticPi}\left[-1,-\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} \\
 & \left.\sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}}\right) \Bigg/ \\
 & \left(3 a^2\left(a^2-b^2\right)^2 \sqrt{\frac{1}{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}} \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^4}\right. \\
 & \left.\left(b-b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^4+a\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)^2\right)^2\right) \Bigg) + \\
 & \left(\left(-b\left(-7 a^2 b B+3 b^3 B+11 a^3 C-3 a b^2 C\right) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right]\right], \frac{a-b}{a+b}\right)+\right. \\
 & \quad a\left(2 b^3 B-3 a^2 b(B-2 C)+3 a^3 C-a b^2(3 B+C)\right) \\
 & \quad \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right]+ \\
 & \quad 6(a-b)^2(a+b)(-b B+a C) \operatorname{EllipticPi}\left[-1,-\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \\
 & \left.\left(-a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]+b \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right)\right)
 \end{aligned}$$

$$\begin{aligned} & \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}} \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^4} \Big/ \\ & \left( 3 a^2\left(a^2-b^2\right)^2 \sqrt{\frac{1}{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} \right. \\ & \left. \left( b-b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^4+a\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)^2\right) \right) - \\ & \left( 1 / \left( 3 a^2\left(a^2-b^2\right)^2\left(b-b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^4+a\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)^2\right) \right) \right) (a+b) \\ & \left( -b\left(-7 a^2 b B+3 b^3 B+11 a^3 C-3 a b^2 C\right) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right]+ \right. \\ & \quad a\left(2 b^3 B-3 a^2 b(B-2 C)+3 a^3 C-a b^2(3 B+C)\right) \\ & \quad \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right]+ \right. \\ & \quad \left. 6(a-b)^2(a+b)(-b B+a C) \operatorname{EllipticPi}\left[-1,-\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \right) \\ & \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] \sqrt{\frac{1}{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}} \\ & \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} \\ & \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}} \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^4} + \\ & \left( b\left(-7 a^2 b B+3 b^3 B+11 a^3 C-3 a b^2 C\right) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] \right. \\ & \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}} \left( \frac{\operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} + \right. \\ & \left. \left( \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right) \right) \Big/ \right. \\ & \left. \left. \left( 1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)^2 \right) \Big/ \left( 3 a^2\left(a^2-b^2\right)^2\left(\frac{1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}\right)^{3 / 2} \right) \right) - \end{aligned}$$

$$\begin{aligned}
 & \left( b (-7 a^2 b B + 3 b^3 B + 11 a^3 C - 3 a b^2 C) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right. \\
 & \quad \left( \left( -a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + b \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) / \right. \\
 & \quad \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - \left( \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right. \\
 & \quad \left. \left. \left( a + b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) / \\
 & \quad \left( 3 a^2 (a^2 - b^2)^2 \sqrt{\frac{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \right) + \\
 & \quad \left( (a+b) \left( -b (-7 a^2 b B + 3 b^3 B + 11 a^3 C - 3 a b^2 C) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right]\right], \right. \right. \\
 & \quad \left. \left. \frac{a-b}{a+b} \right) + a (2 b^3 B - 3 a^2 b (B - 2 C) + 3 a^3 C - a b^2 (3 B + C)) \right. \\
 & \quad \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b} \right] + \right. \\
 & \quad \left. 6 (a-b)^2 (a+b) (-b B + a C) \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b} \right] \right) \\
 & \quad \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^4} \\
 & \quad \left( \left( -a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + b \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) / \right. \\
 & \quad \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - \left( \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right. \\
 & \quad \left. \left. \left( a + b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) / \\
 & \quad \left( 3 a^2 (a^2 - b^2)^2 \sqrt{\frac{1}{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \right. \\
 & \quad \left. \left( b - b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^4 + a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) \right) + \\
 & \quad \left( 2 (a+b) \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right)
 \end{aligned}$$

$$\begin{aligned} & \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^4} \\ & \left( a \left( 2b^3B-3a^2b(B-2C)+3a^3C-ab^2(3B+C) \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \right) / \\ & \left( 2 \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{1-\frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) - \\ & \left( 3(a-b)^2(a+b)(-bB+aC)\sec\left[\frac{1}{2}(c+dx)\right]^2 \right) / \\ & \left( \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} \left( 1+\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \sqrt{1-\frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) - \\ & \left( b \left( -7a^2bB+3b^3B+11a^3C-3ab^2C \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \\ & \left. \sqrt{1-\frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) / \left( 2 \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} \right) \right) / \left( 3a^2(a^2-b^2)^2 \right. \\ & \left. \left. \left. \left. \left. \sqrt{\frac{1}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} \left( b-b \tan\left[\frac{1}{2}(c+dx)\right]^4+a \left( -1+\tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) \right) \right) \right) \right) \right) \end{aligned}$$

**Problem 981: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sec[c+dx]^{5/2} (a+b \sec[c+dx]) (A+B \sec[c+dx]+C \sec[c+dx]^2) dx$$

Optimal (type 4, 266 leaves, 10 steps):



$$\begin{aligned}
 & -\frac{1}{15d} 2 (9Ab + 9aB + 7bC) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\
 & \frac{1}{21d} 2 (7aA + 5bB + 5aC) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\
 & \frac{2(9Ab + 9aB + 7bC) \sqrt{\sec[c+dx]} \sin[c+dx]}{15d} + \\
 & \frac{2(7aA + 5bB + 5aC) \sec[c+dx]^{3/2} \sin[c+dx]}{21d} + \\
 & \frac{2(9Ab + 9aB + 7bC) \sec[c+dx]^{5/2} \sin[c+dx]}{45d} + \\
 & \frac{2(bB + aC) \sec[c+dx]^{7/2} \sin[c+dx]}{7d} + \frac{2bC \sec[c+dx]^{9/2} \sin[c+dx]}{9d}
 \end{aligned}$$

Result (type 5, 1232 leaves):

$$\begin{aligned}
 & - \left( \left( 6\sqrt{2} AB e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^3 \operatorname{Csc}[c] \right. \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. (a + b \sec[c+dx]) (A + B \sec[c+dx] + C \sec[c+dx]^2) \right) / \\
 & \quad \left. (5d (b + a \cos[c+dx]) (A + 2C + 2B \cos[c+dx] + A \cos[2c + 2dx])) \right) - \\
 & \left( 6\sqrt{2} aB e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^3 \operatorname{Csc}[c] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. (a + b \sec[c+dx]) (A + B \sec[c+dx] + C \sec[c+dx]^2) \right) / \\
 & \quad \left. (5d (b + a \cos[c+dx]) (A + 2C + 2B \cos[c+dx] + A \cos[2c + 2dx])) \right) - \\
 & \left( 14\sqrt{2} bC e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^3 \operatorname{Csc}[c] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. (a + b \sec[c+dx]) (A + B \sec[c+dx] + C \sec[c+dx]^2) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( 15 d (b + a \cos [c + d x]) (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right) + \\
 & \left( 4 a A \cos [c + d x]^{7/2} \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right] \sqrt{\sec [c + d x]} \right. \\
 & \quad \left. (a + b \sec [c + d x]) (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \\
 & \left( 3 d (b + a \cos [c + d x]) (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right) + \\
 & \left( 20 b B \cos [c + d x]^{7/2} \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right] \sqrt{\sec [c + d x]} \right. \\
 & \quad \left. (a + b \sec [c + d x]) (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \\
 & \left( 21 d (b + a \cos [c + d x]) (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right) + \\
 & \left( 20 a C \cos [c + d x]^{7/2} \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right] \sqrt{\sec [c + d x]} \right. \\
 & \quad \left. (a + b \sec [c + d x]) (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \\
 & \left( 21 d (b + a \cos [c + d x]) (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right) + \\
 & \left( (a + b \sec [c + d x]) (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left( \frac{4 (9 A b + 9 a B + 7 b C) \cos [d x] \operatorname{Csc}[c]}{15 d} + \frac{4 b C \sec [c] \sec [c + d x]^4 \sin [d x]}{9 d} + \right. \\
 & \quad \frac{1}{63 d} 4 \sec [c] \sec [c + d x]^3 (7 b C \sin [c] + 9 b B \sin [d x] + 9 a C \sin [d x]) + \frac{1}{315 d} \\
 & \quad 4 \sec [c] \sec [c + d x] (63 A b \sin [c] + 63 a B \sin [c] + 49 b C \sin [c] + 105 a A \sin [d x] + 75 b B \\
 & \quad \sin [d x] + 75 a C \sin [d x]) + \frac{1}{315 d} 4 \sec [c] \sec [c + d x]^2 (45 b B \sin [c] + 45 a C \sin [c] + \\
 & \quad 63 A b \sin [d x] + 63 a B \sin [d x] + 49 b C \sin [d x]) + \left. \left. \frac{4 (7 a A + 5 b B + 5 a C) \operatorname{Tan}[c]}{21 d} \right) \right) / \\
 & \left( (b + a \cos [c + d x]) (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sec [c + d x]^{5/2} \right)
 \end{aligned}$$

**Problem 982: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sec [c + d x]^{3/2} (a + b \sec [c + d x]) (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 4, 230 leaves, 9 steps):

$$\begin{aligned}
 & -\frac{1}{5d} 2 (5aA + 3bB + 3aC) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\
 & \frac{1}{21d} 2 (7Ab + 7aB + 5bC) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\
 & \frac{2(5aA + 3bB + 3aC) \sqrt{\sec[c+dx]} \sin[c+dx]}{5d} + \\
 & \frac{2(7Ab + 7aB + 5bC) \sec[c+dx]^{3/2} \sin[c+dx]}{21d} + \\
 & \frac{2(bB + aC) \sec[c+dx]^{5/2} \sin[c+dx]}{5d} + \frac{2bC \sec[c+dx]^{7/2} \sin[c+dx]}{7d}
 \end{aligned}$$

Result (type 5, 1170 leaves):

$$\begin{aligned}
 & - \left( \left( 2\sqrt{2} a A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^3 \operatorname{Csc}[c] \right. \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. (a + b \sec[c+dx]) (A + B \sec[c+dx] + C \sec[c+dx]^2) \right) / \\
 & \quad \left. (d (b + a \cos[c+dx]) (A + 2C + 2B \cos[c+dx] + A \cos[2c + 2dx])) \right) - \\
 & \left( 6\sqrt{2} b B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^3 \operatorname{Csc}[c] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. (a + b \sec[c+dx]) (A + B \sec[c+dx] + C \sec[c+dx]^2) \right) / \\
 & \quad \left. (5d (b + a \cos[c+dx]) (A + 2C + 2B \cos[c+dx] + A \cos[2c + 2dx])) \right) - \\
 & \left( 6\sqrt{2} a C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^3 \operatorname{Csc}[c] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. (a + b \sec[c+dx]) (A + B \sec[c+dx] + C \sec[c+dx]^2) \right) / \\
 & \quad \left. (5d (b + a \cos[c+dx]) (A + 2C + 2B \cos[c+dx] + A \cos[2c + 2dx])) \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left( 4 A b \cos [c+d x]^{7/2} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]} \right. \\
 & \quad \left. (a+b \sec [c+d x]) (A+B \sec [c+d x]+C \sec [c+d x]^2) \right) / \\
 & (3 d (b+a \cos [c+d x]) (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])) + \\
 & \left( 4 a B \cos [c+d x]^{7/2} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]} \right. \\
 & \quad \left. (a+b \sec [c+d x]) (A+B \sec [c+d x]+C \sec [c+d x]^2) \right) / \\
 & (3 d (b+a \cos [c+d x]) (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])) + \\
 & \left( 20 b C \cos [c+d x]^{7/2} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]} \right. \\
 & \quad \left. (a+b \sec [c+d x]) (A+B \sec [c+d x]+C \sec [c+d x]^2) \right) / \\
 & (21 d (b+a \cos [c+d x]) (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])) + \\
 & \left( (a+b \sec [c+d x]) (A+B \sec [c+d x]+C \sec [c+d x]^2) \right. \\
 & \quad \left( \frac{4(5 a A+3 b B+3 a C) \cos [d x] \operatorname{Csc}[c]}{5 d} + \frac{4 b C \sec [c] \sec [c+d x]^3 \sin [d x]}{7 d} + \right. \\
 & \quad \frac{1}{35 d} 4 \sec [c] \sec [c+d x]^2 (5 b C \sin [c]+7 b B \sin [d x]+7 a C \sin [d x]) + \\
 & \quad \frac{1}{105 d} 4 \sec [c] \sec [c+d x] (21 b B \sin [c]+21 a C \sin [c]+35 A b \sin [d x]+ \\
 & \quad \left. \left. 35 a B \sin [d x]+25 b C \sin [d x]) + \frac{4(7 A b+7 a B+5 b C) \tan [c]}{21 d} \right) \right) / \\
 & ((b+a \cos [c+d x]) (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sec [c+d x]^{5/2})
 \end{aligned}$$

**Problem 983: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sqrt{\sec [c+d x]} (a+b \sec [c+d x]) (A+B \sec [c+d x]+C \sec [c+d x]^2) dx$$

Optimal (type 4, 192 leaves, 8 steps):

$$\begin{aligned}
 & -\frac{1}{5 d} 2(5 A b+5 a B+3 b C) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]} + \\
 & \frac{1}{3 d} 2(b B+a(3 A+C)) \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]} + \\
 & \frac{2(5 A b+5 a B+3 b C) \sqrt{\sec [c+d x]} \sin [c+d x]}{5 d} + \\
 & \frac{2(b B+a C) \sec [c+d x]^{3/2} \sin [c+d x]}{3 d} + \frac{2 b C \sec [c+d x]^{5/2} \sin [c+d x]}{5 d}
 \end{aligned}$$

Result (type 5, 1106 leaves):

$$\begin{aligned}
 & - \left( \left( 2\sqrt{2} A b e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^3 \operatorname{Csc}[c] \right. \right. \\
 & \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. (a+b \operatorname{Sec}[c+dx]) (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad \left. (d(b+a \cos[c+dx]) (A+2C+2B \cos[c+dx] + A \cos[2c+2dx])) \right) - \\
 & \left( 2\sqrt{2} a B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^3 \operatorname{Csc}[c] \right. \\
 & \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. (a+b \operatorname{Sec}[c+dx]) (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad \left. (d(b+a \cos[c+dx]) (A+2C+2B \cos[c+dx] + A \cos[2c+2dx])) \right) - \\
 & \left( 6\sqrt{2} b C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^3 \operatorname{Csc}[c] \right. \\
 & \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. (a+b \operatorname{Sec}[c+dx]) (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad \left. (5d(b+a \cos[c+dx]) (A+2C+2B \cos[c+dx] + A \cos[2c+2dx])) \right) + \\
 & \left( 4a A \cos[c+dx]^{7/2} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\operatorname{Sec}[c+dx]} \right. \\
 & \quad \left. (a+b \operatorname{Sec}[c+dx]) (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad \left. (d(b+a \cos[c+dx]) (A+2C+2B \cos[c+dx] + A \cos[2c+2dx])) \right) + \\
 & \left( 4b B \cos[c+dx]^{7/2} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\operatorname{Sec}[c+dx]} \right. \\
 & \quad \left. (a+b \operatorname{Sec}[c+dx]) (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & \quad \left. (3d(b+a \cos[c+dx]) (A+2C+2B \cos[c+dx] + A \cos[2c+2dx])) \right) + \\
 & \left( 4a C \cos[c+dx]^{7/2} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\operatorname{Sec}[c+dx]} \right. \\
 & \quad \left. (a+b \operatorname{Sec}[c+dx]) (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) /
 \end{aligned}$$

$$\left( 3 d (b + a \cos [c + d x]) (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right) + \left( (a + b \sec [c + d x]) (A + B \sec [c + d x] + C \sec [c + d x]^2) \left( \frac{4 (5 A b + 5 a B + 3 b C) \cos [d x] \csc [c]}{5 d} + \frac{4 b C \sec [c] \sec [c + d x]^2 \sin [d x]}{5 d} + \frac{1}{15 d} \right) \right) / \left( 4 \sec [c] \sec [c + d x] (3 b C \sin [c] + 5 b B \sin [d x] + 5 a C \sin [d x]) + \frac{4 (b B + a C) \tan [c]}{3 d} \right) / \left( (b + a \cos [c + d x]) (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sec [c + d x]^{5/2} \right)$$

**Problem 984: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + b \sec [c + d x]) (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sqrt{\sec [c + d x]}} dx$$

Optimal (type 4, 152 leaves, 7 steps):

$$-\frac{1}{d} 2 (b B - a (A - C)) \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), 2\right] \sqrt{\sec [c + d x]} + \frac{1}{3 d} 2 (3 A b + 3 a B + b C) \sqrt{\cos [c + d x]} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), 2\right] \sqrt{\sec [c + d x]} + \frac{2 (b B + a C) \sqrt{\sec [c + d x]} \sin [c + d x]}{d} + \frac{2 b C \sec [c + d x]^{3/2} \sin [c + d x]}{3 d}$$

Result (type 5, 1074 leaves):

$$\left( 2 \sqrt{2} a A e^{-i (2 c + d x)} \sqrt{\frac{e^{i (c + d x)}}{1 + e^{2 i (c + d x)}}} \cos [c + d x]^3 \csc [c] \left( 1 + e^{2 i (c + d x)} + (-1 + e^{2 i c}) \sqrt{1 + e^{2 i (c + d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c + d x)}\right] \right) (a + b \sec [c + d x]) (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \left( d (b + a \cos [c + d x]) (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right) - \left( 2 \sqrt{2} b B e^{-i (2 c + d x)} \sqrt{\frac{e^{i (c + d x)}}{1 + e^{2 i (c + d x)}}} \cos [c + d x]^3 \csc [c] \left( 1 + e^{2 i (c + d x)} + (-1 + e^{2 i c}) \sqrt{1 + e^{2 i (c + d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c + d x)}\right] \right) (a + b \sec [c + d x]) (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) / \left( d (b + a \cos [c + d x]) (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right) -$$

$$\begin{aligned}
 & \left( 2 \sqrt{2} a C e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^3 \operatorname{Csc}[c] \right. \\
 & \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. (a+b \operatorname{Sec}[c+dx]) (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & (d(b+a \cos[c+dx]) (A+2C+2B \cos[c+dx] + A \cos[2c+2dx])) + \\
 & \left( 4 a b \cos[c+dx]^{7/2} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\operatorname{Sec}[c+dx]} \right. \\
 & \quad \left. (a+b \operatorname{Sec}[c+dx]) (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & (d(b+a \cos[c+dx]) (A+2C+2B \cos[c+dx] + A \cos[2c+2dx])) + \\
 & \left( 4 a b \cos[c+dx]^{7/2} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\operatorname{Sec}[c+dx]} \right. \\
 & \quad \left. (a+b \operatorname{Sec}[c+dx]) (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & (d(b+a \cos[c+dx]) (A+2C+2B \cos[c+dx] + A \cos[2c+2dx])) + \\
 & \left( 4 b c \cos[c+dx]^{7/2} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\operatorname{Sec}[c+dx]} \right. \\
 & \quad \left. (a+b \operatorname{Sec}[c+dx]) (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right) / \\
 & (3 d (b+a \cos[c+dx]) (A+2C+2B \cos[c+dx] + A \cos[2c+2dx])) + \\
 & \left( (a+b \operatorname{Sec}[c+dx]) (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right. \\
 & \quad \left( -\frac{2(aA-2bB-2aC+aA \cos[2c]) \cos[dx] \operatorname{Csc}[c]}{d} + \right. \\
 & \quad \left. \frac{4aA \cos[c] \sin[dx]}{d} + \frac{4bC \operatorname{Sec}[c] \operatorname{Sec}[c+dx] \sin[dx]}{3d} + \frac{4bC \tan[c]}{3d} \right) \right) / \\
 & ((b+a \cos[c+dx]) (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \operatorname{Sec}[c+dx]^{5/2})
 \end{aligned}$$

**Problem 985: Result unnecessarily involves higher level functions.**

$$\int \frac{(a+b \operatorname{Sec}[c+dx]) (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2)}{\operatorname{Sec}[c+dx]^{3/2}} dx$$

Optimal (type 4, 146 leaves, 7 steps):

$$\begin{aligned}
 & \frac{1}{d} 2 (Ab+aB-bC) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\operatorname{Sec}[c+dx]} + \\
 & \frac{1}{3d} 2 (3bB+a(A+3C)) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\operatorname{Sec}[c+dx]} + \\
 & \frac{2aA \sin[c+dx]}{3d \sqrt{\operatorname{Sec}[c+dx]}} + \frac{2bC \sqrt{\operatorname{Sec}[c+dx]} \sin[c+dx]}{d}
 \end{aligned}$$

Result (type 5, 176 leaves):

$$\frac{1}{3d} \sqrt{\sec[c+dx]} \left( -6iAb \cos[c+dx] - 6iaB \cos[c+dx] + 6ibC \cos[c+dx] + 2(3bB+a(A+3C)) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] + 6i(Ab+aB-bC) e^{-i(c+dx)} \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + 6bC \sin[c+dx] + aA \sin[2(c+dx)] \right)$$

**Problem 986: Result unnecessarily involves higher level functions.**

$$\int \frac{(a+b \sec[c+dx]) (A+B \sec[c+dx] + C \sec[c+dx]^2)}{\sec[c+dx]^{5/2}} dx$$

Optimal (type 4, 156 leaves, 7 steps):

$$\frac{1}{5d} 2(3aA+5bB+5aC) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \frac{1}{3d} 2(Ab+aB+3bC) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \frac{2aA \sin[c+dx]}{5d \sec[c+dx]^{3/2}} + \frac{2(Ab+aB) \sin[c+dx]}{3d \sqrt{\sec[c+dx]}}$$

Result (type 5, 173 leaves):

$$\frac{1}{30d} \sqrt{\sec[c+dx]} \left( 20(Ab+aB+3bC) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] + 12i(3aA+5bB+5aC) e^{-i(c+dx)} \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + 2 \cos[c+dx] (-6i(3aA+5bB+5aC) + 10(Ab+aB) \sin[c+dx] + 3aA \sin[2(c+dx)]) \right)$$

**Problem 987: Result unnecessarily involves higher level functions.**

$$\int \frac{(a+b \sec[c+dx]) (A+B \sec[c+dx] + C \sec[c+dx]^2)}{\sec[c+dx]^{7/2}} dx$$

Optimal (type 4, 194 leaves, 8 steps):

$$\frac{1}{5d} 2(3Ab+3aB+5bC) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \frac{1}{21d} 2(5aA+7bB+7aC) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \frac{2aA \sin[c+dx]}{7d \sec[c+dx]^{5/2}} + \frac{2(Ab+aB) \sin[c+dx]}{5d \sec[c+dx]^{3/2}} + \frac{2(5aA+7bB+7aC) \sin[c+dx]}{21d \sqrt{\sec[c+dx]}}$$

Result (type 5, 198 leaves):



$$\frac{1}{420 d} \sqrt{\sec [c+d x]} \left( 40 (5 a A+7 b B+7 a C) \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]+168 i(3 A b+3 a B+5 b C) e^{-i(c+d x)} \sqrt{1+e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right]+2 \cos [c+d x](-84 i(3 A b+3 a B+5 b C)+5(23 a A+28 b B+28 a C) \sin [c+d x]+42(A b+a B) \sin [2(c+d x)]+15 a A \sin [3(c+d x)]) \right)$$

**Problem 988: Result unnecessarily involves higher level functions.**

$$\int \frac{(a+b \sec [c+d x])(A+B \sec [c+d x]+C \sec [c+d x]^2)}{\sec [c+d x]^{9/2}} dx$$

Optimal (type 4, 230 leaves, 9 steps):

$$\frac{1}{15 d} 2(7 a A+9 b B+9 a C) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}+\frac{1}{21 d} 2(5 A b+5 a B+7 b C) \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}+\frac{2 a A \sin [c+d x]}{9 d \sec [c+d x]^{7/2}}+\frac{2(A b+a B) \sin [c+d x]}{7 d \sec [c+d x]^{5/2}}+\frac{2(7 a A+9 b B+9 a C) \sin [c+d x]}{45 d \sec [c+d x]^{3/2}}+\frac{2(5 A b+5 a B+7 b C) \sin [c+d x]}{21 d \sqrt{\sec [c+d x]}}$$

Result (type 5, 229 leaves):

$$\frac{1}{2520 d} \sqrt{\sec [c+d x]} \left( 240 (5 A b+5 a B+7 b C) \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]+336 i(7 a A+9 b B+9 a C) e^{-i(c+d x)} \sqrt{1+e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right]+2 \cos [c+d x](-1176 i a A-1512 i b B-1512 i a C+30(23 A b+23 a B+28 b C) \sin [c+d x]+14(19 a A+18 b B+18 a C) \sin [2(c+d x)]+90 A b \sin [3(c+d x)]+90 a B \sin [3(c+d x)]+35 a A \sin [4(c+d x)]) \right)$$

**Problem 989: Result unnecessarily involves higher level functions.**

$$\int \frac{(a+b \sec [c+d x])(A+B \sec [c+d x]+C \sec [c+d x]^2)}{\sec [c+d x]^{11/2}} dx$$

Optimal (type 4, 266 leaves, 10 steps):

$$\frac{1}{15 d} 2 (7 A b + 7 a B + 9 b C) \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\sec [c + d x]} + \frac{1}{231 d} 10 (9 a A + 11 b B + 11 a C) \sqrt{\cos [c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\sec [c + d x]} + \frac{2 a A \sin [c + d x]}{11 d \sec [c + d x]^{9/2}} + \frac{2 (A b + a B) \sin [c + d x]}{9 d \sec [c + d x]^{7/2}} + \frac{2 (9 a A + 11 b B + 11 a C) \sin [c + d x]}{77 d \sec [c + d x]^{5/2}} + \frac{2 (7 A b + 7 a B + 9 b C) \sin [c + d x]}{45 d \sec [c + d x]^{3/2}} + \frac{10 (9 a A + 11 b B + 11 a C) \sin [c + d x]}{231 d \sqrt{\sec [c + d x]}}$$

Result(type 5, 265 leaves):

$$\frac{1}{55440 d} \sqrt{\sec [c + d x]} \left( 2400 (9 a A + 11 b B + 11 a C) \sqrt{\cos [c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] + 7392 i (7 A b + 7 a B + 9 b C) e^{-i(c+d x)} \sqrt{1 + e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right] + 2 \cos [c + d x] (-25872 i A b - 25872 i a B - 33264 i b C + 30 (435 a A + 506 b B + 506 a C) \sin [c + d x] + 308 (19 A b + 19 a B + 18 b C) \sin [2(c + d x)] + 2565 a A \sin [3(c + d x)] + 1980 b B \sin [3(c + d x)] + 1980 a C \sin [3(c + d x)] + 770 A b \sin [4(c + d x)] + 770 a B \sin [4(c + d x)] + 315 a A \sin [5(c + d x)]) \right)$$

**Problem 1012: Attempted integration timed out after 120 seconds.**

$$\int \frac{\sec [c + d x]^{5/2} (A + B \sec [c + d x] + C \sec [c + d x]^2)}{a + b \sec [c + d x]} dx$$

Optimal (type 4, 296 leaves, 11 steps):

$$-\frac{1}{5 b^3 d} 2 (5 A b^2 - 5 a b B + 5 a^2 C + 3 b^2 C) \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\sec [c + d x]} + \frac{2 (b B - a C) \sqrt{\cos [c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\sec [c + d x]}}{3 b^2 d} - \frac{1}{b^3 (a + b) d} 2 a (A b^2 - a (b B - a C)) \sqrt{\cos [c + d x]} \operatorname{EllipticPi}\left[\frac{2 a}{a + b}, \frac{1}{2}(c + d x), 2\right] \sqrt{\sec [c + d x]} + \frac{2 (5 A b^2 - 5 a b B + 5 a^2 C + 3 b^2 C) \sqrt{\sec [c + d x]} \sin [c + d x]}{5 b^3 d} + \frac{2 (b B - a C) \sec [c + d x]^{3/2} \sin [c + d x]}{3 b^2 d} + \frac{2 C \sec [c + d x]^{5/2} \sin [c + d x]}{5 b d}$$

Result(type 1, 1 leaves):

???

### Problem 1013: Unable to integrate problem.

$$\int \frac{\sec [c+d x]^{3 / 2} (A+B \sec [c+d x]+C \sec [c+d x]^2)}{a+b \sec [c+d x]} d x$$

Optimal (type 4, 218 leaves, 10 steps):

$$\begin{aligned} & -\frac{2(b B-a C) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{b^2 d} + \\ & \frac{2 C \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{3 b d} + \frac{1}{b^2(a+b) d} \\ & 2(A b^2-a(b B-a C)) \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 a}{a+b}, \frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]} + \\ & \frac{2(b B-a C) \sqrt{\sec [c+d x]} \sin [c+d x]}{b^2 d} + \frac{2 C \sec [c+d x]^{3 / 2} \sin [c+d x]}{3 b d} \end{aligned}$$

Result (type 8, 45 leaves):

$$\int \frac{\sec [c+d x]^{3 / 2} (A+B \sec [c+d x]+C \sec [c+d x]^2)}{a+b \sec [c+d x]} d x$$

### Problem 1014: Unable to integrate problem.

$$\int \frac{\sqrt{\sec [c+d x]} (A+B \sec [c+d x]+C \sec [c+d x]^2)}{a+b \sec [c+d x]} d x$$

Optimal (type 4, 178 leaves, 9 steps):

$$\begin{aligned} & -\frac{2 C \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{b d} + \\ & \frac{2 A \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{a d} - \frac{1}{a b(a+b) d} \\ & 2(A b^2-a(b B-a C)) \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 a}{a+b}, \frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]} + \\ & \frac{2 C \sqrt{\sec [c+d x]} \sin [c+d x]}{b d} \end{aligned}$$

Result (type 8, 45 leaves):

$$\int \frac{\sqrt{\sec [c+d x]} (A+B \sec [c+d x]+C \sec [c+d x]^2)}{a+b \sec [c+d x]} d x$$

**Problem 1015: Unable to integrate problem.**

$$\int \frac{A + B \sec [c + d x] + C \sec [c + d x]^2}{\sqrt{\sec [c + d x]} (a + b \sec [c + d x])} dx$$

Optimal (type 4, 157 leaves, 8 steps):

$$\frac{2 A \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\sec [c + d x]}}{a d} -$$

$$\frac{2 (A b - a B) \sqrt{\cos [c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\sec [c + d x]}}{a^2 d} + \frac{1}{a^2 (a + b) d}$$

$$2 (A b^2 - a (b B - a C)) \sqrt{\cos [c + d x]} \operatorname{EllipticPi}\left[\frac{2 a}{a + b}, \frac{1}{2}(c + d x), 2\right] \sqrt{\sec [c + d x]}$$

Result (type 8, 45 leaves):

$$\int \frac{A + B \sec [c + d x] + C \sec [c + d x]^2}{\sqrt{\sec [c + d x]} (a + b \sec [c + d x])} dx$$

**Problem 1016: Unable to integrate problem.**

$$\int \frac{A + B \sec [c + d x] + C \sec [c + d x]^2}{\sec [c + d x]^{3/2} (a + b \sec [c + d x])} dx$$

Optimal (type 4, 207 leaves, 9 steps):

$$-\frac{1}{a^2 d} 2 (A b - a B) \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\sec [c + d x]} + \frac{1}{3 a^3 d}$$

$$2 (3 A b^2 - 3 a b B + a^2 (A + 3 C)) \sqrt{\cos [c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\sec [c + d x]} -$$

$$\frac{1}{a^3 (a + b) d} 2 b (A b^2 - a (b B - a C)) \sqrt{\cos [c + d x]}$$

$$\operatorname{EllipticPi}\left[\frac{2 a}{a + b}, \frac{1}{2}(c + d x), 2\right] \sqrt{\sec [c + d x]} + \frac{2 A \sin [c + d x]}{3 a d \sqrt{\sec [c + d x]}}$$

Result (type 8, 45 leaves):

$$\int \frac{A + B \sec [c + d x] + C \sec [c + d x]^2}{\sec [c + d x]^{3/2} (a + b \sec [c + d x])} dx$$

**Problem 1017: Unable to integrate problem.**

$$\int \frac{A + B \sec [c + d x] + C \sec [c + d x]^2}{\sec [c + d x]^{5/2} (a + b \sec [c + d x])} dx$$

Optimal (type 4, 269 leaves, 10 steps):

$$\begin{aligned} & \frac{1}{5 a^3 d} 2 (5 A b^2 - 5 a b B + a^2 (3 A + 5 C)) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]} - \\ & \frac{1}{3 a^4 d} 2 (3 A b^3 - a^3 B - 3 a b^2 B + a^2 b (A+3 C)) \sqrt{\cos [c+d x]} \\ & \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]} + \frac{1}{a^4 (a+b) d} \\ & 2 b^2 (A b^2 - a (b B - a C)) \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 a}{a+b}, \frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]} + \\ & \frac{2 A \sin [c+d x]}{5 a d \sec [c+d x]^{3 / 2}} - \frac{2 (A b - a B) \sin [c+d x]}{3 a^2 d \sqrt{\sec [c+d x]}} \end{aligned}$$

Result (type 8, 45 leaves):

$$\int \frac{A+B \sec [c+d x]+C \sec [c+d x]^2}{\sec [c+d x]^{5 / 2}(a+b \sec [c+d x])} d x$$

**Problem 1018: Attempted integration timed out after 120 seconds.**

$$\int \frac{A+B \sec [c+d x]+C \sec [c+d x]^2}{\sec [c+d x]^{7 / 2}(a+b \sec [c+d x])} d x$$

Optimal (type 4, 342 leaves, 11 steps):

$$\begin{aligned} & -\frac{1}{5 a^4 d} 2 (5 A b^3 - 3 a^3 B - 5 a b^2 B + a^2 b (3 A + 5 C)) \\ & \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]} + \frac{1}{21 a^5 d} \\ & 2 (21 A b^4 - 7 a^3 b B - 21 a b^3 B + 7 a^2 b^2 (A+3 C) + a^4 (5 A + 7 C)) \sqrt{\cos [c+d x]} \\ & \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]} - \frac{1}{a^5 (a+b) d} \\ & 2 b^3 (A b^2 - a (b B - a C)) \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 a}{a+b}, \frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]} + \\ & \frac{2 A \sin [c+d x]}{7 a d \sec [c+d x]^{5 / 2}} - \frac{2 (A b - a B) \sin [c+d x]}{5 a^2 d \sec [c+d x]^{3 / 2}} + \frac{2 (7 A b^2 - 7 a b B + a^2 (5 A + 7 C)) \sin [c+d x]}{21 a^3 d \sqrt{\sec [c+d x]}} \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 1019: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c+d x]^{5 / 2}(A+B \sec [c+d x]+C \sec [c+d x]^2)}{(a+b \sec [c+d x])^2} d x$$

Optimal (type 4, 447 leaves, 11 steps):

$$\begin{aligned}
 & - \frac{1}{b^3 (a^2 - b^2) d} (3 a^2 b B - 2 b^3 B - a b^2 (A - 4 C) - 5 a^3 C) \\
 & \quad \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\sec [c + d x]} + \frac{1}{3 b^2 (a^2 - b^2) d} \\
 & (3 A b^2 - 3 a b B + 5 a^2 C - 2 b^2 C) \sqrt{\cos [c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\sec [c + d x]} - \\
 & \left( (3 A b^4 + 3 a^3 b B - 5 a b^3 B - a^2 b^2 (A - 7 C) - 5 a^4 C) \sqrt{\cos [c + d x]} \right. \\
 & \quad \left. \operatorname{EllipticPi}\left[\frac{2 a}{a + b}, \frac{1}{2}(c + d x), 2\right] \sqrt{\sec [c + d x]} \right) / \left( (a - b) b^3 (a + b)^2 d \right) + \\
 & \frac{(3 a^2 b B - 2 b^3 B - a b^2 (A - 4 C) - 5 a^3 C) \sqrt{\sec [c + d x]} \sin [c + d x]}{b^3 (a^2 - b^2) d} + \\
 & \frac{(3 A b^2 - 3 a b B + 5 a^2 C - 2 b^2 C) \sec [c + d x]^{3/2} \sin [c + d x]}{3 b^2 (a^2 - b^2) d} - \\
 & \frac{(A b^2 - a (b B - a C)) \sec [c + d x]^{5/2} \sin [c + d x]}{b (a^2 - b^2) d (a + b \sec [c + d x])}
 \end{aligned}$$

Result (type 4, 931 leaves):

$$\begin{aligned}
 & \left( (b + a \cos [c + d x])^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left( - \left( \left( 2 (12 a A b^3 - 24 a^2 b^2 B + 12 b^4 B + 40 a^3 b C - 28 a b^3 C) \cos [c + d x]^2 \right. \right. \right. \\
 & \quad \quad \text{EllipticPi} \left[ -\frac{b}{a}, -\text{ArcSin}[\sqrt{\sec [c + d x]}], -1 \right] (a + b \sec [c + d x]) \\
 & \quad \quad \left. \sqrt{1 - \sec [c + d x]^2} \sin [c + d x] \right) / (a (b + a \cos [c + d x]) (1 - \cos [c + d x]^2)) \Big) + \\
 & \quad \left( 2 (9 a^2 A b^2 - 12 A b^4 - 27 a^3 b B + 30 a b^3 B + 45 a^4 C - 44 a^2 b^2 C - 4 b^4 C) \right. \\
 & \quad \cos [c + d x]^2 \left( \text{EllipticF}[\text{ArcSin}[\sqrt{\sec [c + d x]}], -1] + \right. \\
 & \quad \quad \left. \text{EllipticPi} \left[ -\frac{b}{a}, -\text{ArcSin}[\sqrt{\sec [c + d x]}], -1 \right] \right) (a + b \sec [c + d x]) \\
 & \quad \left. \sqrt{1 - \sec [c + d x]^2} \sin [c + d x] \right) / (b (b + a \cos [c + d x]) (1 - \cos [c + d x]^2)) - \\
 & \quad \left( 2 (3 a^2 A b^2 - 9 a^3 b B + 6 a b^3 B + 15 a^4 C - 12 a^2 b^2 C) \cos [2 (c + d x)] \right. \\
 & \quad (a + b \sec [c + d x]) \left( 2 a b - 2 a b \sec [c + d x]^2 + \right. \\
 & \quad \quad 2 a b \text{EllipticE}[\text{ArcSin}[\sqrt{\sec [c + d x]}], -1] \sqrt{\sec [c + d x]} \sqrt{1 - \sec [c + d x]^2} + \\
 & \quad \quad a (a - 2 b) \text{EllipticF}[\text{ArcSin}[\sqrt{\sec [c + d x]}], -1] \sqrt{\sec [c + d x]} \sqrt{1 - \sec [c + d x]^2} + \\
 & \quad \quad a^2 \text{EllipticPi} \left[ -\frac{b}{a}, -\text{ArcSin}[\sqrt{\sec [c + d x]}], -1 \right] \sqrt{\sec [c + d x]} \sqrt{1 - \sec [c + d x]^2} - \\
 & \quad \quad 2 b^2 \text{EllipticPi} \left[ -\frac{b}{a}, -\text{ArcSin}[\sqrt{\sec [c + d x]}], -1 \right] \\
 & \quad \quad \left. \left. \sqrt{\sec [c + d x]} \sqrt{1 - \sec [c + d x]^2} \right) \sin [c + d x] \right) / \\
 & \quad \left. \left( a^2 b (b + a \cos [c + d x]) (1 - \cos [c + d x]^2) \sqrt{\sec [c + d x]} (2 - \sec [c + d x]^2) \right) \right) / \\
 & \quad \left( 6 (a - b) b^3 (a + b) d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. (a + b \sec [c + d x])^2 \right) + \\
 & \quad \left( (b + a \cos [c + d x])^2 \sqrt{\sec [c + d x]} \right. \\
 & \quad (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \quad \left( \frac{2 (a A b^2 - 3 a^2 b B + 2 b^3 B + 5 a^3 C - 4 a b^2 C) \sin [c + d x]}{b^3 (-a^2 + b^2)} - \right. \\
 & \quad \left. \frac{2 (a A b^2 \sin [c + d x] - a^2 b B \sin [c + d x] + a^3 C \sin [c + d x])}{b^2 (-a^2 + b^2) (b + a \cos [c + d x])} + \frac{4 C \tan [c + d x]}{3 b^2} \right) \Big) / \\
 & \quad \left( d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. (a + b \sec [c + d x])^2 \right)
 \end{aligned}$$

**Problem 1020: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Sec}[c + d x]^{3/2} (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2)}{(a + b \text{Sec}[c + d x])^2} dx$$

Optimal (type 4, 363 leaves, 10 steps):

$$\begin{aligned} & -\frac{1}{b^2 (a^2 - b^2) d} (A b^2 - a b B + 3 a^2 C - 2 b^2 C) \sqrt{\text{Cos}[c + d x]} \text{EllipticE}\left[\frac{1}{2} (c + d x), 2\right] \sqrt{\text{Sec}[c + d x]} - \\ & \frac{1}{a b (a^2 - b^2) d} (A b^2 - a (b B - a C)) \sqrt{\text{Cos}[c + d x]} \text{EllipticF}\left[\frac{1}{2} (c + d x), 2\right] \sqrt{\text{Sec}[c + d x]} + \\ & \left( (A b^4 + a^3 b B - 3 a b^3 B - 3 a^4 C + a^2 b^2 (A + 5 C)) \sqrt{\text{Cos}[c + d x]} \right. \\ & \quad \left. \text{EllipticPi}\left[\frac{2 a}{a + b}, \frac{1}{2} (c + d x), 2\right] \sqrt{\text{Sec}[c + d x]} \right) / (a (a - b) b^2 (a + b)^2 d) + \\ & \frac{(A b^2 - a b B + 3 a^2 C - 2 b^2 C) \sqrt{\text{Sec}[c + d x]} \text{Sin}[c + d x]}{b^2 (a^2 - b^2) d} - \\ & \frac{(A b^2 - a (b B - a C)) \text{Sec}[c + d x]^{3/2} \text{Sin}[c + d x]}{b (a^2 - b^2) d (a + b \text{Sec}[c + d x])} \end{aligned}$$

Result (type 4, 865 leaves):





**Problem 1021: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\text{Sec}[c + d x]} (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2)}{(a + b \text{Sec}[c + d x])^2} dx$$

Optimal (type 4, 299 leaves, 9 steps):

$$\frac{1}{a b (a^2 - b^2) d} (A b^2 - a (b B - a C)) \sqrt{\text{Cos}[c + d x]} \text{EllipticE}\left[\frac{1}{2} (c + d x), 2\right] \sqrt{\text{Sec}[c + d x]} -$$

$$\frac{1}{a^2 (a^2 - b^2) d} (A b^2 + a b B - a^2 (2 A + C)) \sqrt{\text{Cos}[c + d x]} \text{EllipticF}\left[\frac{1}{2} (c + d x), 2\right] \sqrt{\text{Sec}[c + d x]} +$$

$$\left( (A b^4 + a^3 b B + a b^3 B + a^4 C - 3 a^2 b^2 (A + C)) \sqrt{\text{Cos}[c + d x]} \text{EllipticPi}\left[\frac{2 a}{a + b}, \frac{1}{2} (c + d x), 2\right] \right.$$

$$\left. \sqrt{\text{Sec}[c + d x]} \right) / (a^2 (a - b) b (a + b)^2 d) - \frac{(A b^2 - a (b B - a C)) \sqrt{\text{Sec}[c + d x]} \text{Sin}[c + d x]}{b (a^2 - b^2) d (a + b \text{Sec}[c + d x])}$$

Result (type 4, 829 leaves):

$$\begin{aligned}
 & \left( (b + a \cos [c + d x])^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left( - \left( \left( 2 (4 a A b - 4 b^2 B + 4 a b C) \cos [c + d x]^2 \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin} [\sqrt{\sec [c + d x]}], -1 \right] \right. \right. \right. \\
 & \quad \quad \left. \left. \left. (a + b \sec [c + d x]) \sqrt{1 - \sec [c + d x]^2} \sin [c + d x] \right) \right) / \right. \\
 & \quad \left. \left. (a (b + a \cos [c + d x]) (1 - \cos [c + d x]^2)) \right) \right) + \\
 & \quad \left( 2 (-A b^2 + a b B + 3 a^2 C - 4 b^2 C) \cos [c + d x]^2 \left( \operatorname{EllipticF} [\operatorname{ArcSin} [\sqrt{\sec [c + d x]}], -1] + \right. \right. \\
 & \quad \quad \left. \left. \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin} [\sqrt{\sec [c + d x]}], -1 \right] \right) (a + b \sec [c + d x]) \right. \\
 & \quad \left. \sqrt{1 - \sec [c + d x]^2} \sin [c + d x] \right) / (b (b + a \cos [c + d x]) (1 - \cos [c + d x]^2)) - \\
 & \quad \left( 2 (A b^2 - a b B + a^2 C) \cos [2 (c + d x)] (a + b \sec [c + d x]) \left( 2 a b - 2 a b \sec [c + d x]^2 + \right. \right. \\
 & \quad \quad 2 a b \operatorname{EllipticE} [\operatorname{ArcSin} [\sqrt{\sec [c + d x]}], -1] \sqrt{\sec [c + d x]} \sqrt{1 - \sec [c + d x]^2} + \\
 & \quad \quad a (a - 2 b) \operatorname{EllipticF} [\operatorname{ArcSin} [\sqrt{\sec [c + d x]}], -1] \sqrt{\sec [c + d x]} \sqrt{1 - \sec [c + d x]^2} + \\
 & \quad \quad a^2 \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin} [\sqrt{\sec [c + d x]}], -1 \right] \sqrt{\sec [c + d x]} \sqrt{1 - \sec [c + d x]^2} - \\
 & \quad \quad 2 b^2 \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin} [\sqrt{\sec [c + d x]}], -1 \right] \\
 & \quad \quad \left. \left. \sqrt{\sec [c + d x]} \sqrt{1 - \sec [c + d x]^2} \right) \sin [c + d x] \right) / \\
 & \quad \left. \left. \left. \left. (a^2 b (b + a \cos [c + d x]) (1 - \cos [c + d x]^2) \sqrt{\sec [c + d x]} (2 - \sec [c + d x]^2)) \right) \right) \right) \right) / \\
 & \quad \left( 2 (a - b) b (a + b) d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. (a + b \sec [c + d x])^2 \right) + \\
 & \quad \left( (b + a \cos [c + d x])^2 \sqrt{\sec [c + d x]} \right. \\
 & \quad \quad (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \quad \quad \left( \frac{2 (A b^2 - a b B + a^2 C) \sin [c + d x]}{a b (-a^2 + b^2)} + \right. \\
 & \quad \quad \left. \left. \frac{2 (A b^2 \sin [c + d x] - a b B \sin [c + d x] + a^2 C \sin [c + d x])}{a (a^2 - b^2) (b + a \cos [c + d x])} \right) \right) / \\
 & \quad \left( d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. (a + b \sec [c + d x])^2 \right)
 \end{aligned}$$

**Problem 1022: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec [c + d x] + C \sec [c + d x]^2}{\sqrt{\sec [c + d x]} (a + b \sec [c + d x])^2} dx$$

Optimal (type 4, 317 leaves, 9 steps):

$$\begin{aligned}
 & - \frac{1}{a^2 (a^2 - b^2) d} (3 A b^2 - a b B - a^2 (2 A - C)) \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), 2\right] \sqrt{\sec [c + d x]} + \\
 & \frac{1}{a^3 (a^2 - b^2) d} (3 A b^3 + 2 a^3 B - a b^2 B - a^2 b (4 A + C)) \\
 & \sqrt{\cos [c + d x]} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), 2\right] \sqrt{\sec [c + d x]} - \\
 & \left( (3 A b^4 + 3 a^3 b B - a b^3 B - a^4 C - a^2 b^2 (5 A + C)) \sqrt{\cos [c + d x]} \operatorname{EllipticPi}\left[\frac{2 a}{a + b}, \frac{1}{2} (c + d x), 2\right] \right. \\
 & \left. \sqrt{\sec [c + d x]} \right) / \left( a^3 (a - b) (a + b)^2 d \right) + \frac{(A b^2 - a (b B - a C)) \sqrt{\sec [c + d x]} \sin [c + d x]}{a (a^2 - b^2) d (a + b \sec [c + d x])}
 \end{aligned}$$

Result (type 4, 835 leaves):

$$\begin{aligned}
 & \left( (b + a \cos [c + d x])^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left( - \left( \left( 2 (4 a A b - 4 a^2 B + 4 a b C) \cos [c + d x]^2 \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin} [\sqrt{\sec [c + d x]}] \right], -1 \right] \right. \right. \\
 & \quad \quad \left. \left. (a + b \sec [c + d x]) \sqrt{1 - \sec [c + d x]^2} \sin [c + d x] \right) \right) / \\
 & \quad \left. (a (b + a \cos [c + d x]) (1 - \cos [c + d x]^2)) \right) + \\
 & \quad \left( 2 (-2 a^2 A + A b^2 + a b B - a^2 C) \cos [c + d x]^2 \left( \operatorname{EllipticF} [\operatorname{ArcSin} [\sqrt{\sec [c + d x]}] ], -1 \right] + \right. \\
 & \quad \quad \left. \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin} [\sqrt{\sec [c + d x]}] \right], -1 \right) (a + b \sec [c + d x]) \\
 & \quad \left. \sqrt{1 - \sec [c + d x]^2} \sin [c + d x] \right) / (b (b + a \cos [c + d x]) (1 - \cos [c + d x]^2)) - \\
 & \quad \left( 2 (-2 a^2 A + 3 A b^2 - a b B + a^2 C) \cos [2 (c + d x)] (a + b \sec [c + d x]) \right. \\
 & \quad \left. (2 a b - 2 a b \sec [c + d x]^2 + \right. \\
 & \quad \quad 2 a b \operatorname{EllipticE} [\operatorname{ArcSin} [\sqrt{\sec [c + d x]}] ], -1] \sqrt{\sec [c + d x]} \sqrt{1 - \sec [c + d x]^2} + \\
 & \quad \quad a (a - 2 b) \operatorname{EllipticF} [\operatorname{ArcSin} [\sqrt{\sec [c + d x]}] ], -1] \sqrt{\sec [c + d x]} \sqrt{1 - \sec [c + d x]^2} + \\
 & \quad \quad a^2 \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin} [\sqrt{\sec [c + d x]}] \right], -1] \sqrt{\sec [c + d x]} \sqrt{1 - \sec [c + d x]^2} - \\
 & \quad \quad 2 b^2 \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin} [\sqrt{\sec [c + d x]}] \right], -1] \\
 & \quad \quad \left. \left. \sqrt{\sec [c + d x]} \sqrt{1 - \sec [c + d x]^2} \right) \sin [c + d x] \right) / \\
 & \quad \left. \left. (a^2 b (b + a \cos [c + d x]) (1 - \cos [c + d x]^2) \sqrt{\sec [c + d x]} (2 - \sec [c + d x]^2)) \right) \right) / \\
 & \quad \left( 2 a (-a + b) (a + b) d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. (a + b \sec [c + d x])^2 \right) + \\
 & \quad \left( (b + a \cos [c + d x])^2 \sqrt{\sec [c + d x]} \right. \\
 & \quad \quad (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \quad \quad \left( \frac{2 (A b^2 - a b B + a^2 C) \sin [c + d x]}{a^2 (a^2 - b^2)} - \right. \\
 & \quad \quad \left. \left. \frac{2 (A b^3 \sin [c + d x] - a b^2 B \sin [c + d x] + a^2 b C \sin [c + d x])}{a^2 (a^2 - b^2) (b + a \cos [c + d x])} \right) \right) / \\
 & \quad \left( d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. (a + b \sec [c + d x])^2 \right)
 \end{aligned}$$

**Problem 1023: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2}{\operatorname{Sec}[c + d x]^{3/2} (a + b \operatorname{Sec}[c + d x])^2} dx$$

Optimal (type 4, 406 leaves, 10 steps):

$$\frac{1}{a^3 (a^2 - b^2) d} (5 A b^3 + 2 a^3 B - 3 a b^2 B - a^2 b (4 A - C)) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]} - \frac{1}{3 a^4 (a^2 - b^2) d} (15 A b^4 + 12 a^3 b B - 9 a b^3 B - a^2 b^2 (16 A - 3 C) - 2 a^4 (A + 3 C)) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]} + \left(b (5 A b^4 + 5 a^3 b B - 3 a b^3 B - a^2 b^2 (7 A - C) - 3 a^4 C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticPi}\left[\frac{2 a}{a + b}, \frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}\right) / (a^4 (a - b) (a + b)^2 d) - \frac{(5 A b^2 - 3 a b B - a^2 (2 A - 3 C)) \operatorname{Sin}[c + d x]}{3 a^2 (a^2 - b^2) d \sqrt{\operatorname{Sec}[c + d x]}} + \frac{(A b^2 - a (b B - a C)) \operatorname{Sin}[c + d x]}{a (a^2 - b^2) d \sqrt{\operatorname{Sec}[c + d x]} (a + b \operatorname{Sec}[c + d x])}$$

Result (type 4, 887 leaves):

$$\begin{aligned}
 & \left( (b + a \cos [c + d x])^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left( - \left( \left( 2 (4 a^3 A + 8 a A b^2 - 12 a^2 b B + 12 a^3 C) \cos [c + d x]^2 \right. \right. \right. \\
 & \quad \quad \text{EllipticPi} \left[ -\frac{b}{a}, -\text{ArcSin}[\sqrt{\sec [c + d x]}], -1 \right] (a + b \sec [c + d x]) \\
 & \quad \quad \left. \sqrt{1 - \sec [c + d x]^2} \sin [c + d x] \right) / (a (b + a \cos [c + d x]) (1 - \cos [c + d x]^2)) \Big) + \\
 & \quad \left( 2 (-8 a^2 A b + 5 A b^3 + 6 a^3 B - 3 a b^2 B - 3 a^2 b C) \cos [c + d x]^2 \right. \\
 & \quad \left( \text{EllipticF}[\text{ArcSin}[\sqrt{\sec [c + d x]}], -1] + \right. \\
 & \quad \quad \left. \text{EllipticPi} \left[ -\frac{b}{a}, -\text{ArcSin}[\sqrt{\sec [c + d x]}], -1 \right] \right) (a + b \sec [c + d x]) \\
 & \quad \left. \sqrt{1 - \sec [c + d x]^2} \sin [c + d x] \right) / (b (b + a \cos [c + d x]) (1 - \cos [c + d x]^2)) - \\
 & \quad \left( 2 (-12 a^2 A b + 15 A b^3 + 6 a^3 B - 9 a b^2 B + 3 a^2 b C) \cos [2 (c + d x)] \right. \\
 & \quad (a + b \sec [c + d x]) \left( 2 a b - 2 a b \sec [c + d x]^2 + \right. \\
 & \quad \quad 2 a b \text{EllipticE}[\text{ArcSin}[\sqrt{\sec [c + d x]}], -1] \sqrt{\sec [c + d x]} \sqrt{1 - \sec [c + d x]^2} + \\
 & \quad \quad a (a - 2 b) \text{EllipticF}[\text{ArcSin}[\sqrt{\sec [c + d x]}], -1] \sqrt{\sec [c + d x]} \sqrt{1 - \sec [c + d x]^2} + \\
 & \quad \quad a^2 \text{EllipticPi} \left[ -\frac{b}{a}, -\text{ArcSin}[\sqrt{\sec [c + d x]}], -1 \right] \sqrt{\sec [c + d x]} \sqrt{1 - \sec [c + d x]^2} - \\
 & \quad \quad 2 b^2 \text{EllipticPi} \left[ -\frac{b}{a}, -\text{ArcSin}[\sqrt{\sec [c + d x]}], -1 \right] \\
 & \quad \quad \left. \left. \left. \sqrt{\sec [c + d x]} \sqrt{1 - \sec [c + d x]^2} \right) \sin [c + d x] \right) / \right. \\
 & \quad \left. \left. \left. \left( a^2 b (b + a \cos [c + d x]) (1 - \cos [c + d x]^2) \sqrt{\sec [c + d x]} (2 - \sec [c + d x]^2) \right) \right) \right) / \right. \\
 & \quad \left( 6 a^2 (a - b) (a + b) d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. (a + b \sec [c + d x])^2 \right) + \\
 & \quad \left( (b + a \cos [c + d x])^2 \sqrt{\sec [c + d x]} \right. \\
 & \quad (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \quad \left( \frac{2 b (A b^2 - a b B + a^2 C) \sin [c + d x]}{a^3 (-a^2 + b^2)} + \right. \\
 & \quad \quad \left. \frac{2 (A b^4 \sin [c + d x] - a b^3 B \sin [c + d x] + a^2 b^2 C \sin [c + d x])}{a^3 (a^2 - b^2) (b + a \cos [c + d x])} + \frac{2 A \sin [2 (c + d x)]}{3 a^2} \right) \Big) / \right. \\
 & \quad \left( d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. (a + b \sec [c + d x])^2 \right)
 \end{aligned}$$

**Problem 1027: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Sec}[c + d x]^{3/2} (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2)}{(a + b \text{Sec}[c + d x])^3} dx$$

Optimal (type 4, 469 leaves, 10 steps):

$$\begin{aligned} & - \left( (A b^4 - a^3 b B - 5 a b^3 B - 3 a^4 C + a^2 b^2 (5 A + 9 C)) \sqrt{\text{Cos}[c + d x]} \right. \\ & \quad \left. \text{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\text{Sec}[c + d x]} \right) / (4 a b^2 (a^2 - b^2)^2 d) + \\ & \quad \frac{1}{4 a^2 b (a^2 - b^2)^2 d} (A b^4 + 3 a^3 b B + 3 a b^3 B + a^4 C - 7 a^2 b^2 (A + C)) \sqrt{\text{Cos}[c + d x]} \\ & \quad \text{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\text{Sec}[c + d x]} - \\ & \quad \left( (A b^6 - a^5 b B + 10 a^3 b^3 B + 3 a b^5 B - 3 a^4 b^2 (A - 2 C) - 3 a^6 C - 5 a^2 b^4 (2 A + 3 C)) \right. \\ & \quad \left. \sqrt{\text{Cos}[c + d x]} \text{EllipticPi}\left[\frac{2 a}{a + b}, \frac{1}{2}(c + d x), 2\right] \sqrt{\text{Sec}[c + d x]} \right) / \\ & \quad (4 a^2 (a - b)^2 b^2 (a + b)^3 d) - \frac{(A b^2 - a (b B - a C)) \text{Sec}[c + d x]^{3/2} \text{Sin}[c + d x]}{2 b (a^2 - b^2) d (a + b \text{Sec}[c + d x])^2} + \\ & \quad \left( (A b^4 - a^3 b B - 5 a b^3 B - 3 a^4 C + a^2 b^2 (5 A + 9 C)) \sqrt{\text{Sec}[c + d x]} \text{Sin}[c + d x] \right) / \\ & \quad (4 b^2 (a^2 - b^2)^2 d (a + b \text{Sec}[c + d x])) \end{aligned}$$

Result (type 4, 1051 leaves):



$$\begin{aligned}
 & \left( (b+a \cos [c+d x])^3 \sec [c+d x] (A+B \sec [c+d x]+C \sec [c+d x]^2) \right. \\
 & \quad \left( - \left( \left( 2(-24 a A b^3+8 a^2 b^2 B+16 b^4 B+8 a^3 b C-32 a b^3 C) \cos [c+d x]^2 \right. \right. \right. \\
 & \quad \quad \left. \left. \left. \text{EllipticPi}\left[-\frac{b}{a},-\text{ArcSin}\left[\sqrt{\sec [c+d x]}\right],-1\right](a+b \sec [c+d x]) \right. \right. \right. \\
 & \quad \quad \left. \left. \left. \sqrt{1-\sec [c+d x]^2} \sin [c+d x] \right) \right) / (a(b+a \cos [c+d x])(1-\cos [c+d x]^2)) \right) + \\
 & \quad \left( 2\left(a^2 A b^2+5 A b^4+3 a^3 b B-9 a b^3 B+9 a^4 C-19 a^2 b^2 C+16 b^4 C\right) \cos [c+d x]^2 \right. \\
 & \quad \left( \left( \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\sec [c+d x]}\right],-1\right]+ \right. \right. \\
 & \quad \quad \left. \left. \text{EllipticPi}\left[-\frac{b}{a},-\text{ArcSin}\left[\sqrt{\sec [c+d x]}\right],-1\right] \right)(a+b \sec [c+d x]) \right. \\
 & \quad \left. \left. \sqrt{1-\sec [c+d x]^2} \sin [c+d x] \right) \right) / (b(b+a \cos [c+d x])(1-\cos [c+d x]^2)) - \\
 & \quad \left( 2\left(-5 a^2 A b^2-A b^4+a^3 b B+5 a b^3 B+3 a^4 C-9 a^2 b^2 C\right) \cos [2(c+d x)] \right. \\
 & \quad \left( a+b \sec [c+d x] \right)\left( 2 a b-2 a b \sec [c+d x]^2+ \right. \\
 & \quad \quad 2 a b \text{EllipticE}\left[\text{ArcSin}\left[\sqrt{\sec [c+d x]}\right],-1\right] \sqrt{\sec [c+d x]} \sqrt{1-\sec [c+d x]^2} + \\
 & \quad \quad a(a-2 b) \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\sec [c+d x]}\right],-1\right] \sqrt{\sec [c+d x]} \sqrt{1-\sec [c+d x]^2} + \\
 & \quad \quad a^2 \text{EllipticPi}\left[-\frac{b}{a},-\text{ArcSin}\left[\sqrt{\sec [c+d x]}\right],-1\right] \sqrt{\sec [c+d x]} \sqrt{1-\sec [c+d x]^2} - \\
 & \quad \quad 2 b^2 \text{EllipticPi}\left[-\frac{b}{a},-\text{ArcSin}\left[\sqrt{\sec [c+d x]}\right],-1\right] \\
 & \quad \quad \left. \left. \left. \sqrt{\sec [c+d x]} \sqrt{1-\sec [c+d x]^2} \right) \sin [c+d x] \right) \right) / \\
 & \quad \left. \left( a^2 b(b+a \cos [c+d x])(1-\cos [c+d x]^2) \sqrt{\sec [c+d x]}(2-\sec [c+d x]^2) \right) \right) \Bigg) / \\
 & \quad \left( 8(a-b)^2 b^2(a+b)^2 d(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right. \\
 & \quad \left. (a+b \sec [c+d x])^3 \right) + \\
 & \quad \left( (b+a \cos [c+d x])^3 \sec [c+d x]^{3/2} \right. \\
 & \quad \left( A+B \sec [c+d x]+C \sec [c+d x]^2 \right) \\
 & \quad \left( \frac{\left( 5 a^2 A b^2+A b^4-a^3 b B-5 a b^3 B-3 a^4 C+9 a^2 b^2 C\right) \sin [c+d x]}{2 a b^2\left(-a^2+b^2\right)^2} + \right. \\
 & \quad \quad \left. \frac{A b^2 \sin [c+d x]-a b B \sin [c+d x]+a^2 C \sin [c+d x]}{a\left(a^2-b^2\right)(b+a \cos [c+d x])^2} + \right. \\
 & \quad \quad \left. \left( -7 a^2 A b^2 \sin [c+d x]+A b^4 \sin [c+d x]+3 a^3 b B \sin [c+d x]+3 a b^3 B \sin [c+d x]+ \right. \right. \\
 & \quad \quad \left. \left. a^4 C \sin [c+d x]-7 a^2 b^2 C \sin [c+d x] \right) \right) / \left( 2 a b\left(-a^2+b^2\right)^2(b+a \cos [c+d x]) \right) \Bigg) \Bigg) / \\
 & \quad \left( d(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])(a+b \sec [c+d x])^3 \right)
 \end{aligned}$$

**Problem 1028: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\text{Sec}[c + d x]} (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2)}{(a + b \text{Sec}[c + d x])^3} dx$$

Optimal (type 4, 478 leaves, 10 steps):

$$\begin{aligned} & - \left( \left( (3 A b^4 + 5 a^3 b B + a b^3 B - a^4 C - a^2 b^2 (9 A + 5 C)) \sqrt{\text{Cos}[c + d x]} \right. \right. \\ & \quad \left. \left. \text{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\text{Sec}[c + d x]} \right) / (4 a^2 b (a^2 - b^2)^2 d) \right) + \\ & \frac{1}{4 a^3 (a^2 - b^2)^2 d} (3 A b^4 - 7 a^3 b B + a b^3 B - a^2 b^2 (5 A - 3 C) + a^4 (8 A + 3 C)) \\ & \sqrt{\text{Cos}[c + d x]} \text{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\text{Sec}[c + d x]} - \\ & \left( (3 A b^6 - 3 a^5 b B - 10 a^3 b^3 B + a b^5 B - 3 a^2 b^4 (2 A - C) - a^6 C + 5 a^4 b^2 (3 A + 2 C)) \right. \\ & \quad \left. \sqrt{\text{Cos}[c + d x]} \text{EllipticPi}\left[\frac{2 a}{a + b}, \frac{1}{2}(c + d x), 2\right] \sqrt{\text{Sec}[c + d x]} \right) / \\ & (4 a^3 (a - b)^2 b (a + b)^3 d) - \frac{(A b^2 - a (b B - a C)) \sqrt{\text{Sec}[c + d x]} \text{Sin}[c + d x]}{2 b (a^2 - b^2) d (a + b \text{Sec}[c + d x])^2} + \\ & \left( (A b^4 + 3 a^3 b B + 3 a b^3 B + a^4 C - 7 a^2 b^2 (A + C)) \sqrt{\text{Sec}[c + d x]} \text{Sin}[c + d x] \right) / \\ & (4 a b (a^2 - b^2)^2 d (a + b \text{Sec}[c + d x])) \end{aligned}$$

Result (type 4, 1051 leaves):

$$\begin{aligned}
 & \left( (b+a \cos [c+d x])^3 \sec [c+d x] (A+B \sec [c+d x]+C \sec [c+d x]^2) \right. \\
 & \quad \left( - \left( \left( 2 (16 a^3 A b+8 a A b^3-24 a^2 b^2 B+8 a^3 b C+16 a b^3 C) \cos [c+d x]^2 \right. \right. \right. \\
 & \quad \quad \left. \left. \left. \operatorname{EllipticPi}\left[-\frac{b}{a},-\operatorname{ArcSin}\left[\sqrt{\sec [c+d x]}\right],-1\right](a+b \sec [c+d x]) \right. \right. \right. \\
 & \quad \quad \left. \left. \left. \sqrt{1-\sec [c+d x]^2} \sin [c+d x]\right) / (a(b+a \cos [c+d x])\left(1-\cos [c+d x]^2\right)) \right) \right) + \\
 & \quad \left( 2(-5 a^2 A b^2-A b^4+a^3 b B+5 a b^3 B+3 a^4 C-9 a^2 b^2 C) \cos [c+d x]^2 \right. \\
 & \quad \left( \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\sec [c+d x]}\right],-1\right]+ \right. \\
 & \quad \left. \left. \operatorname{EllipticPi}\left[-\frac{b}{a},-\operatorname{ArcSin}\left[\sqrt{\sec [c+d x]}\right],-1\right]\right)(a+b \sec [c+d x]) \right. \\
 & \quad \left. \left. \sqrt{1-\sec [c+d x]^2} \sin [c+d x]\right) / (b(b+a \cos [c+d x])\left(1-\cos [c+d x]^2\right)) - \right. \\
 & \quad \left( 2(9 a^2 A b^2-3 A b^4-5 a^3 b B-a b^3 B+a^4 C+5 a^2 b^2 C) \cos [2(c+d x)] \right. \\
 & \quad \left( a+b \sec [c+d x]\right)\left(2 a b-2 a b \sec [c+d x]^2+\right. \\
 & \quad 2 a b \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\sec [c+d x]}\right],-1\right] \sqrt{\sec [c+d x]} \sqrt{1-\sec [c+d x]^2}+ \\
 & \quad a(a-2 b) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\sec [c+d x]}\right],-1\right] \sqrt{\sec [c+d x]} \sqrt{1-\sec [c+d x]^2}+ \\
 & \quad a^2 \operatorname{EllipticPi}\left[-\frac{b}{a},-\operatorname{ArcSin}\left[\sqrt{\sec [c+d x]}\right],-1\right] \sqrt{\sec [c+d x]} \sqrt{1-\sec [c+d x]^2}- \\
 & \quad 2 b^2 \operatorname{EllipticPi}\left[-\frac{b}{a},-\operatorname{ArcSin}\left[\sqrt{\sec [c+d x]}\right],-1\right] \\
 & \quad \left. \left. \left. \sqrt{\sec [c+d x]} \sqrt{1-\sec [c+d x]^2}\right) \sin [c+d x]\right) / \right. \\
 & \quad \left. \left. \left. \left( a^2 b(b+a \cos [c+d x])\left(1-\cos [c+d x]^2\right) \sqrt{\sec [c+d x]}\left(2-\sec [c+d x]^2\right) \right) \right) \right) / \right. \\
 & \quad \left( 8 a(a-b)^2 b(a+b)^2 d(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right. \\
 & \quad \left. (a+b \sec [c+d x])^3\right)+ \\
 & \quad \left( (b+a \cos [c+d x])^3 \sec [c+d x]^{3/2} \right. \\
 & \quad (A+B \sec [c+d x]+C \sec [c+d x]^2) \\
 & \quad \left( \frac{(-9 a^2 A b^2+3 A b^4+5 a^3 b B+a b^3 B-a^4 C-5 a^2 b^2 C) \sin [c+d x]}{2 a^2 b\left(-a^2+b^2\right)^2} - \right. \\
 & \quad \left. \frac{A b^3 \sin [c+d x]-a b^2 B \sin [c+d x]+a^2 b C \sin [c+d x]}{a^2\left(a^2-b^2\right)(b+a \cos [c+d x])^2} + \right. \\
 & \quad \left. \left. \left. \left( 11 a^2 A b^2 \sin [c+d x]-5 A b^4 \sin [c+d x]-7 a^3 b B \sin [c+d x]+a b^3 B \sin [c+d x]+ \right. \right. \right. \\
 & \quad \left. \left. \left. 3 a^4 C \sin [c+d x]+3 a^2 b^2 C \sin [c+d x]\right) / \left( 2 a^2\left(a^2-b^2\right)^2(b+a \cos [c+d x]) \right) \right) \right) / \right. \\
 & \quad \left. \left. \left. \left( d(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])\right)(a+b \sec [c+d x])^3 \right) \right) \right) /
 \end{aligned}$$

**Problem 1029: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2}{\sqrt{\operatorname{Sec}[c + dx]} (a + b \operatorname{Sec}[c + dx])^3} dx$$

Optimal (type 4, 486 leaves, 10 steps):

$$\frac{1}{4 a^3 (a^2 - b^2)^2 d} (15 A b^4 + 9 a^3 b B - 3 a b^3 B + a^4 (8 A - 5 C) - a^2 b^2 (29 A + C))$$

$$\sqrt{\operatorname{Cos}[c + dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\operatorname{Sec}[c + dx]} - \frac{1}{4 a^4 (a^2 - b^2)^2 d}$$

$$(15 A b^5 - 8 a^5 B + 5 a^3 b^2 B - 3 a b^4 B - a^2 b^3 (33 A + C) + a^4 b (24 A + 7 C))$$

$$\sqrt{\operatorname{Cos}[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\operatorname{Sec}[c + dx]} +$$

$$\left( (15 A b^6 - 15 a^5 b B + 6 a^3 b^3 B - 3 a b^5 B + 3 a^6 C - a^2 b^4 (38 A + C) + 5 a^4 b^2 (7 A + 2 C)) \right.$$

$$\left. \sqrt{\operatorname{Cos}[c + dx]} \operatorname{EllipticPi}\left[\frac{2 a}{a + b}, \frac{1}{2}(c + dx), 2\right] \sqrt{\operatorname{Sec}[c + dx]} \right) /$$

$$(4 a^4 (a - b)^2 (a + b)^3 d) + \frac{(A b^2 - a (b B - a C)) \sqrt{\operatorname{Sec}[c + dx]} \operatorname{Sin}[c + dx]}{2 a (a^2 - b^2) d (a + b \operatorname{Sec}[c + dx])^2} -$$

$$\left( (5 A b^4 + 7 a^3 b B - a b^3 B - 3 a^4 C - a^2 b^2 (11 A + 3 C)) \sqrt{\operatorname{Sec}[c + dx]} \operatorname{Sin}[c + dx] \right) /$$

$$(4 a^2 (a^2 - b^2)^2 d (a + b \operatorname{Sec}[c + dx]))$$

Result (type 4, 1064 leaves):

$$\begin{aligned}
 & \left( (b+a \cos [c+d x])^3 \sec [c+d x] (A+B \sec [c+d x]+C \sec [c+d x]^2) \right. \\
 & \quad \left( - \left( \left( 2(-32 a^3 A b+8 a A b^3+16 a^4 B+8 a^2 b^2 B-24 a^3 b C) \cos [c+d x]^2 \right. \right. \right. \\
 & \quad \quad \left. \left. \left. \text{EllipticPi}\left[-\frac{b}{a}, -\text{ArcSin}\left[\sqrt{\sec [c+d x]}\right], -1\right] (a+b \sec [c+d x]) \right. \right. \right. \\
 & \quad \quad \left. \left. \left. \sqrt{1-\sec [c+d x]^2} \sin [c+d x] \right) / (a(b+a \cos [c+d x]) (1-\cos [c+d x]^2)) \right) \right) + \\
 & \quad \left( 2(8 a^4 A-7 a^2 A b^2+5 A b^4-5 a^3 b B-a b^3 B+a^4 C+5 a^2 b^2 C) \cos [c+d x]^2 \right. \\
 & \quad \left( \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\sec [c+d x]}\right], -1\right] + \right. \\
 & \quad \quad \left. \left. \text{EllipticPi}\left[-\frac{b}{a}, -\text{ArcSin}\left[\sqrt{\sec [c+d x]}\right], -1\right] \right) (a+b \sec [c+d x]) \right. \\
 & \quad \left. \left. \sqrt{1-\sec [c+d x]^2} \sin [c+d x] \right) / (b(b+a \cos [c+d x]) (1-\cos [c+d x]^2)) - \right. \\
 & \quad \left( 2(8 a^4 A-29 a^2 A b^2+15 A b^4+9 a^3 b B-3 a b^3 B-5 a^4 C-a^2 b^2 C) \cos [2(c+d x)] \right. \\
 & \quad \left. (a+b \sec [c+d x]) \left( 2 a b-2 a b \sec [c+d x]^2 + \right. \right. \\
 & \quad \quad 2 a b \text{EllipticE}\left[\text{ArcSin}\left[\sqrt{\sec [c+d x]}\right], -1\right] \sqrt{\sec [c+d x]} \sqrt{1-\sec [c+d x]^2} + \\
 & \quad \quad a(a-2 b) \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\sec [c+d x]}\right], -1\right] \sqrt{\sec [c+d x]} \sqrt{1-\sec [c+d x]^2} + \\
 & \quad \quad a^2 \text{EllipticPi}\left[-\frac{b}{a}, -\text{ArcSin}\left[\sqrt{\sec [c+d x]}\right], -1\right] \sqrt{\sec [c+d x]} \sqrt{1-\sec [c+d x]^2} - \\
 & \quad \quad 2 b^2 \text{EllipticPi}\left[-\frac{b}{a}, -\text{ArcSin}\left[\sqrt{\sec [c+d x]}\right], -1\right] \\
 & \quad \quad \left. \left. \left. \sqrt{\sec [c+d x]} \sqrt{1-\sec [c+d x]^2} \right) \sin [c+d x] \right) / \right. \\
 & \quad \left. \left. \left. \left( a^2 b(b+a \cos [c+d x]) (1-\cos [c+d x]^2) \sqrt{\sec [c+d x]} (2-\sec [c+d x]^2) \right) \right) \right) / \right. \\
 & \quad \left( 8 a^2(a-b)^2(a+b)^2 d(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right. \\
 & \quad \left. (a+b \sec [c+d x])^3 \right) + \\
 & \quad \left( (b+a \cos [c+d x])^3 \sec [c+d x]^{3/2} \right. \\
 & \quad (A+B \sec [c+d x]+C \sec [c+d x]^2) \\
 & \quad \left( - \left( \left( (-13 a^2 A b^2+7 A b^4+9 a^3 b B-3 a b^3 B-5 a^4 C-a^2 b^2 C) \sin [c+d x] \right) / \left( 2 a^3(-a^2+b^2)^2 \right) \right) - \right. \\
 & \quad \quad \left. \frac{-A b^4 \sin [c+d x]+a b^3 B \sin [c+d x]-a^2 b^2 C \sin [c+d x]}{a^3(a^2-b^2)(b+a \cos [c+d x])^2} + \right. \\
 & \quad \quad \left. (-15 a^2 A b^3 \sin [c+d x]+9 A b^5 \sin [c+d x]+11 a^3 b^2 B \sin [c+d x]-5 a b^4 B \sin [c+d x]- \right. \\
 & \quad \quad \left. \left. 7 a^4 b C \sin [c+d x]+a^2 b^3 C \sin [c+d x] \right) / \left( 2 a^3(a^2-b^2)^2(b+a \cos [c+d x]) \right) \right) \right) / \right. \\
 & \quad \left. \left( d(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) (a+b \sec [c+d x])^3 \right) \right)
 \end{aligned}$$

**Problem 1031: Result unnecessarily involves imaginary or complex numbers.**

$$\int \text{Sec}[c + d x]^{3/2} \sqrt{a + b \text{Sec}[c + d x]} (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) dx$$

Optimal (type 4, 447 leaves, 14 steps):

$$\left( (24 A b^2 + 18 a b B - a^2 C + 16 b^2 C) \sqrt{\frac{b + a \text{Cos}[c + d x]}{a + b}} \right. \\ \left. \text{EllipticF}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \sqrt{\text{Sec}[c + d x]} \right) / (24 b d \sqrt{a + b \text{Sec}[c + d x]}) - \\ \left( (2 a^2 b B - 8 b^3 B - a^3 C - 4 a b^2 (2 A + C)) \sqrt{\frac{b + a \text{Cos}[c + d x]}{a + b}} \right. \\ \left. \text{EllipticPi}\left[2, \frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \sqrt{\text{Sec}[c + d x]} \right) / (8 b^2 d \sqrt{a + b \text{Sec}[c + d x]}) - \\ \left( (24 A b^2 + 6 a b B - 3 a^2 C + 16 b^2 C) \text{EllipticE}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \text{Sec}[c + d x]} \right) / \\ \left( 24 b^2 d \sqrt{\frac{b + a \text{Cos}[c + d x]}{a + b}} \sqrt{\text{Sec}[c + d x]} \right) + \frac{1}{24 b^2 d} \\ (24 A b^2 + 6 a b B - 3 a^2 C + 16 b^2 C) \sqrt{\text{Sec}[c + d x]} \sqrt{a + b \text{Sec}[c + d x]} \text{Sin}[c + d x] + \\ \frac{(6 b B + a C) \text{Sec}[c + d x]^{3/2} \sqrt{a + b \text{Sec}[c + d x]} \text{Sin}[c + d x]}{12 b d} + \\ \frac{C \text{Sec}[c + d x]^{5/2} \sqrt{a + b \text{Sec}[c + d x]} \text{Sin}[c + d x]}{3 d}$$

Result (type 4, 782 leaves):

$$\left( \sqrt{a + b \text{Sec}[c + d x]} (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) \right. \\ \left. \frac{2 (24 a b^2 B + 4 a^2 b C) \sqrt{\frac{b + a \text{Cos}[c + d x]}{a + b}} \text{EllipticF}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right]}{\sqrt{b + a \text{Cos}[c + d x]}} + \right. \\ \left. 2 (24 a A b^2 - 18 a^2 b B + 48 b^3 B + 9 a^3 C + 8 a b^2 C) \sqrt{\frac{b + a \text{Cos}[c + d x]}{a + b}} \right)$$

$$\begin{aligned}
 & \left. \left( \text{EllipticPi} \left[ 2, \frac{1}{2} (c+dx), \frac{2a}{a+b} \right] / \left( \sqrt{b+a \cos[c+dx]} \right) + \right. \right. \\
 & \left. \left( 2i (-24aAb^2 - 6a^2bB + 3a^3C - 16ab^2C) \sqrt{\frac{a-a \cos[c+dx]}{a+b}} \sqrt{\frac{a+a \cos[c+dx]}{a-b}} \cos \left[ \right. \right. \right. \\
 & \left. \left. 2(c+dx) \right] \left[ -2b(a+b) \text{EllipticE} \left[ i \text{ArcSinh} \left[ \sqrt{\frac{1}{a-b}} \sqrt{b+a \cos[c+dx]} \right], \frac{-a+b}{a+b} \right] + \right. \right. \\
 & \left. \left. a \left[ 2b \text{EllipticF} \left[ i \text{ArcSinh} \left[ \sqrt{\frac{1}{a-b}} \sqrt{b+a \cos[c+dx]} \right], \frac{-a+b}{a+b} \right] + \right. \right. \right. \\
 & \left. \left. \left. a \text{EllipticPi} \left[ 1 - \frac{a}{b}, i \text{ArcSinh} \left[ \sqrt{\frac{1}{a-b}} \sqrt{b+a \cos[c+dx]} \right], \frac{-a+b}{a+b} \right] \right] \right) \right) \\
 & \left. \sin[c+dx] \right) / \left( \sqrt{\frac{1}{a-b}} b \sqrt{1 - \cos[c+dx]^2} \sqrt{\frac{a^2 - a^2 \cos[c+dx]^2}{a^2}} \right. \\
 & \left. \left. \left. \left( -a^2 + 2b^2 - 4b(b+a \cos[c+dx]) + 2(b+a \cos[c+dx])^2 \right) \right) \right) \\
 & \left( 48b^2 d \sqrt{b+a \cos[c+dx]} (A+2C+2B \cos[c+dx]+A \cos[2c+2dx]) \right. \\
 & \left. \sec[c+dx]^{5/2} \right) + \\
 & \left( \sqrt{a+b \sec[c+dx]} (A+B \sec[c+dx]+C \sec[c+dx]^2) \right. \\
 & \left( \frac{\sec[c+dx]^2 (6bB \sin[c+dx]+aC \sin[c+dx])}{6b} + \frac{1}{12b^2} \sec[c+dx] \right. \\
 & \left. (24Ab^2 \sin[c+dx]+6abB \sin[c+dx]-3a^2C \sin[c+dx]+16b^2C \sin[c+dx]) + \right. \\
 & \left. \frac{2}{3} C \sec[c+dx]^2 \tan[c+dx] \right) / \\
 & \left( d(A+2C+2B \cos[c+dx]+A \cos[2c+2dx]) \sec[c+dx]^{5/2} \right)
 \end{aligned}$$

**Problem 1032:** Result unnecessarily involves imaginary or complex numbers.

$$\int \sqrt{\sec[c+dx]} \sqrt{a+b \sec[c+dx]} (A+B \sec[c+dx]+C \sec[c+dx]^2) dx$$

Optimal (type 4, 346 leaves, 13 steps):

$$\begin{aligned} & \left( (8 a A + 4 b B + 3 a C) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b} \sqrt{\sec [c + d x]}\right] \right) / \\ & (4 d \sqrt{a + b \sec [c + d x]}) + \left( (8 A b^2 + 4 a b B - a^2 C + 4 b^2 C) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \\ & \left. \operatorname{EllipticPi}\left[2, \frac{1}{2}(c + d x), \frac{2 a}{a + b} \sqrt{\sec [c + d x]}\right] \right) / (4 b d \sqrt{a + b \sec [c + d x]}) - \\ & \frac{(4 b B + a C) \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b} \sqrt{a + b \sec [c + d x]}\right]}{4 b d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \sqrt{\sec [c + d x]}} + \\ & \frac{(4 b B + a C) \sqrt{\sec [c + d x]} \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{4 b d} + \\ & \frac{C \sec [c + d x]^{3/2} \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{2 d} \end{aligned}$$

Result (type 4, 683 leaves):

$$\begin{aligned} & - \left( \left( \sqrt{a + b \sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \right. \\ & \left. \left( 2 (-16 a A b - 4 a b C) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right) / \right. \\ & \left. (\sqrt{b + a \cos [c + d x]}) + \left( 2 (-16 A b^2 - 4 a b B + 3 a^2 C - 8 b^2 C) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \right. \\ & \left. \left. \operatorname{EllipticPi}\left[2, \frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right) / (\sqrt{b + a \cos [c + d x]}) + \right. \\ & \left. \left( 2 i (4 a b B + a^2 C) \sqrt{\frac{a - a \cos [c + d x]}{a + b}} \sqrt{\frac{a + a \cos [c + d x]}{a - b}} \cos [2(c + d x)] \right) \right. \\ & \left. \left( -2 b (a + b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \cos [c + d x]}\right], \frac{-a + b}{a + b}\right] + \right. \right. \\ & \left. \left. a \left( 2 b \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \cos [c + d x]}\right], \frac{-a + b}{a + b}\right] + \right. \right. \end{aligned}$$





$$\frac{(2 a B + b C) \sqrt{\frac{b+a \operatorname{Cos}[c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{\operatorname{Sec}[c+d x]}}{d \sqrt{a+b \operatorname{Sec}[c+d x]}} +$$

$$\left( (2 b B + a C) \sqrt{\frac{b+a \operatorname{Cos}[c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{\operatorname{Sec}[c+d x]} \right) /$$

$$\left( d \sqrt{a+b \operatorname{Sec}[c+d x]} \right) + \frac{(2 A - C) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \operatorname{Sec}[c+d x]}}{d \sqrt{\frac{b+a \operatorname{Cos}[c+d x]}{a+b}} \sqrt{\operatorname{Sec}[c+d x]}} +$$

$$\frac{C \sqrt{\operatorname{Sec}[c+d x]} \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{d}$$

Result (type 4, 624 leaves):



**Problem 1034: Unable to integrate problem.**

$$\int \frac{\sqrt{a + b \operatorname{Sec}[c + d x]} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[c + d x]^{3/2}} dx$$

Optimal (type 4, 277 leaves, 12 steps):

$$\begin{aligned} & - \left( \left( 2 (A b^2 - a^2 (A + 3 C)) \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{\operatorname{Sec}[c + d x]} \right) / \right. \\ & \quad \left. (3 a d \sqrt{a + b \operatorname{Sec}[c + d x]}) \right) + \\ & \frac{2 b C \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \operatorname{EllipticPi}\left[2, \frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{\operatorname{Sec}[c + d x]}}{d \sqrt{a + b \operatorname{Sec}[c + d x]}} + \\ & \frac{2 (A b + 3 a B) \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \operatorname{Sec}[c + d x]}}{3 a d \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \sqrt{\operatorname{Sec}[c + d x]}} + \\ & \frac{2 A \sqrt{a + b \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{3 d \sqrt{\operatorname{Sec}[c + d x]}} \end{aligned}$$

Result (type 8, 47 leaves):

$$\int \frac{\sqrt{a + b \operatorname{Sec}[c + d x]} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[c + d x]^{3/2}} dx$$

**Problem 1035: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{a + b \operatorname{Sec}[c + d x]} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[c + d x]^{5/2}} dx$$

Optimal (type 4, 273 leaves, 9 steps):

$$\begin{aligned}
 & - \left( \left( 2 (a^2 - b^2) (2 A b - 5 a B) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), \frac{2 a}{a + b} \right] \sqrt{\sec [c + d x]} \right) / \right. \\
 & \quad \left. (15 a^2 d \sqrt{a + b \sec [c + d x]}) \right) - \\
 & \left( 2 (2 A b^2 - 5 a b B - 3 a^2 (3 A + 5 C)) \operatorname{EllipticE} \left[ \frac{1}{2} (c + d x), \frac{2 a}{a + b} \right] \sqrt{a + b \sec [c + d x]} \right) / \\
 & \left( 15 a^2 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \sqrt{\sec [c + d x]} \right) + \\
 & \frac{2 A \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{5 d \sec [c + d x]^{3/2}} + \frac{2 (A b + 5 a B) \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{15 a d \sqrt{\sec [c + d x]}}
 \end{aligned}$$

Result (type 6, 3426 leaves):

$$\begin{aligned}
 & \left( \sqrt{a + b \sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left( - \frac{4 (9 a^2 A - 2 A b^2 + 5 a b B + 15 a^2 C) \cot [c]}{15 a^2 d} + \frac{4 (A b + 5 a B) \cos [d x] \sin [c]}{15 a d} + \right. \\
 & \quad \left. \frac{2 A \cos [2 d x] \sin [2 c]}{5 d} + \frac{4 (A b + 5 a B) \cos [c] \sin [d x]}{15 a d} + \frac{2 A \cos [2 c] \sin [2 d x]}{5 d} \right) \Big) / \\
 & \left( (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sec [c + d x]^{5/2} \right) - \\
 & \left( 28 A b \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c]}{a \sqrt{1 + \cot [c]^2}} \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right) \right] \right. \\
 & \quad \left. \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right] \csc [c] \\
 & \quad \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( -1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right) \\
 & \sqrt{a + b \sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) \sec [d x - \operatorname{ArcTan} [\cot [c]]] \\
 & \sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \operatorname{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \operatorname{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}}
 \end{aligned}$$

$$\left. \sqrt{b - a \sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]} \right/$$

$$\left( 15 a d \sqrt{b + a \cos[c + dx]} (A + 2 C + 2 B \cos[c + dx] + A \cos[2c + 2 dx]) \sqrt{1 + \cot[c]^2} \sec[c + dx]^{5/2} - \right.$$

$$\left( 4 B \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc[c] (b - a \sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]])}{a \sqrt{1 + \cot[c]^2} \left( 1 + \frac{b \csc[c]}{a \sqrt{1 + \cot[c]^2}} \right)} \right], \right.$$

$$\left. \frac{\csc[c] (b - a \sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]])}{a \sqrt{1 + \cot[c]^2} \left( -1 + \frac{b \csc[c]}{a \sqrt{1 + \cot[c]^2}} \right)} \right] \csc[c]$$

$$\sqrt{a + b \sec[c + dx]} (A + B \sec[c + dx] + C \sec[c + dx]^2) \sec[dx - \text{ArcTan}[\cot[c]]]$$

$$\sqrt{\frac{a \sqrt{1 + \cot[c]^2} - a \sqrt{1 + \cot[c]^2} \sin[dx - \text{ArcTan}[\cot[c]]]}{a \sqrt{1 + \cot[c]^2} - b \csc[c]}}$$

$$\sqrt{\frac{a \sqrt{1 + \cot[c]^2} + a \sqrt{1 + \cot[c]^2} \sin[dx - \text{ArcTan}[\cot[c]]]}{a \sqrt{1 + \cot[c]^2} + b \csc[c]}}$$

$$\left. \sqrt{b - a \sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]} \right/$$

$$\left( 3 d \sqrt{b + a \cos[c + dx]} (A + 2 C + 2 B \cos[c + dx] + A \cos[2c + 2 dx]) \sqrt{1 + \cot[c]^2} \sec[c + dx]^{5/2} - \right.$$

$$\left( 4 b C \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc[c] (b - a \sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]])}{a \sqrt{1 + \cot[c]^2} \left( 1 + \frac{b \csc[c]}{a \sqrt{1 + \cot[c]^2}} \right)} \right], \right.$$

$$\left. \frac{\csc[c] (b - a \sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]])}{a \sqrt{1 + \cot[c]^2} \left( -1 + \frac{b \csc[c]}{a \sqrt{1 + \cot[c]^2}} \right)} \right] \csc[c]$$

$$\sqrt{a + b \sec[c + dx]} (A + B \sec[c + dx] + C \sec[c + dx]^2) \sec[dx - \text{ArcTan}[\cot[c]]]$$

$$\begin{aligned}
 & \sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}} \\
 & \left. \sqrt{b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]]} \right) / \\
 & \left( a d \sqrt{b + a \cos [c + d x]} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. \sqrt{1 + \cot [c]^2} \sec [c + d x]^{5/2} \right) - \\
 & \left( 6 a A \csc [c] \sqrt{a + b \sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left. \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \sec [c] (b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]) \right) \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \tan [c]^2} \right) \right) \right) / \left( a \sqrt{1 + \tan [c]^2} \left( 1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right), \\
 & \quad - \left( \left( \sec [c] (b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]) \right) \sqrt{1 + \tan [c]^2} \right) \right) / \\
 & \quad \left( a \sqrt{1 + \tan [c]^2} \left( -1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \left. \right) \sin [d x + \text{ArcTan} [\tan [c]]] \tan [c] \Big) / \\
 & \left( \sqrt{1 + \tan [c]^2} \sqrt{\left( (a \sqrt{1 + \tan [c]^2} - a \cos [d x + \text{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) \right) /} \\
 & \quad \left( b \sec [c] + a \sqrt{1 + \tan [c]^2} \right) \sqrt{\left( (a \sqrt{1 + \tan [c]^2} + \right. \\
 & \quad \left. a \cos [d x + \text{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) /} \left( -b \sec [c] + a \sqrt{1 + \tan [c]^2} \right) \Big) \\
 & \quad \left. \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2}} \right) - \\
 & \left( \frac{\sin [d x + \text{ArcTan} [\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \left( 2 a \cos [c] (b + a \cos [c] \cos [ \right. \right.
 \end{aligned}$$





$$\begin{aligned}
 & \left( 2 b B \operatorname{Csc}[c] \sqrt{a+b \operatorname{Sec}[c+d x]} (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \right. \\
 & \left. \left( \left( \operatorname{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, -\left(\operatorname{Sec}[c] \left(b+a \operatorname{Cos}[c] \operatorname{Cos}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]\right]\right)\right.\right.\right. \right. \\
 & \left. \left. \left. \sqrt{1+\operatorname{Tan}[c]^2}\right)\right)\right) / \left(a \sqrt{1+\operatorname{Tan}[c]^2} \left(1-\frac{b \operatorname{Sec}[c]}{a \sqrt{1+\operatorname{Tan}[c]^2}}\right)\right) \right), \\
 & - \left( \left(\operatorname{Sec}[c] \left(b+a \operatorname{Cos}[c] \operatorname{Cos}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]\right]\right) \sqrt{1+\operatorname{Tan}[c]^2}\right) / \right. \\
 & \left. \left(a \sqrt{1+\operatorname{Tan}[c]^2} \left(-1-\frac{b \operatorname{Sec}[c]}{a \sqrt{1+\operatorname{Tan}[c]^2}}\right)\right) \right) \operatorname{Sin}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] / \\
 & \left( \sqrt{1+\operatorname{Tan}[c]^2} \sqrt{\left(\left(a \sqrt{1+\operatorname{Tan}[c]^2}-a \operatorname{Cos}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]\right] \sqrt{1+\operatorname{Tan}[c]^2}\right) / \right. \right. \\
 & \left. \left. \left(b \operatorname{Sec}[c]+a \sqrt{1+\operatorname{Tan}[c]^2}\right)\right) \sqrt{\left(\left(a \sqrt{1+\operatorname{Tan}[c]^2}+ \right.\right. \right. \\
 & \left. \left. \left. a \operatorname{Cos}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]\right] \sqrt{1+\operatorname{Tan}[c]^2}\right) / \left(-b \operatorname{Sec}[c]+a \sqrt{1+\operatorname{Tan}[c]^2}\right)\right) \right) \\
 & \left. \sqrt{b+a \operatorname{Cos}[c] \operatorname{Cos}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1+\operatorname{Tan}[c]^2}} \right) - \\
 & \left( \frac{\operatorname{Sin}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1+\operatorname{Tan}[c]^2}} + \left(2 a \operatorname{Cos}[c] \left(b+a \operatorname{Cos}[c] \operatorname{Cos}[ \right. \right. \right. \\
 & \left. \left. \left. d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]\right] \sqrt{1+\operatorname{Tan}[c]^2}\right) / \left(a^2 \operatorname{Cos}[c]^2+a^2 \operatorname{Sin}[c]^2\right) \right) / \\
 & \left. \left(\sqrt{b+a \operatorname{Cos}[c] \operatorname{Cos}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1+\operatorname{Tan}[c]^2}}\right) \right) / \\
 & \left(3 d \sqrt{b+a \operatorname{Cos}[c+d x]} (A+2 C+2 B \operatorname{Cos}[c+d x]+A \operatorname{Cos}[2 c+2 d x]) \right. \\
 & \left. \operatorname{Sec}[c+d x]^{5/2}\right) - \\
 & \left( 2 a C \operatorname{Csc}[c] \sqrt{a+b \operatorname{Sec}[c+d x]} (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \right. \\
 & \left. \left( \left( \operatorname{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, -\left(\operatorname{Sec}[c] \left(b+a \operatorname{Cos}[c] \operatorname{Cos}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]\right]\right)\right.\right.\right. \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & \left( 2 (a^2 - b^2) (25 a^2 A + 8 A b^2 - 14 a b B + 35 a^2 C) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \\
 & \quad \left. \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{\sec [c + d x]} \right) / \left( 105 a^3 d \sqrt{a + b \sec [c + d x]} \right) + \\
 & \left( 2 (8 A b^3 + 63 a^3 B - 14 a b^2 B + a^2 b (19 A + 35 C)) \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right. \\
 & \quad \left. \sqrt{a + b \sec [c + d x]} \right) / \left( 105 a^3 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \sqrt{\sec [c + d x]} \right) + \\
 & \frac{2 A \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{7 d \sec [c + d x]^{5/2}} + \frac{2 (A b + 7 a B) \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{35 a d \sec [c + d x]^{3/2}} - \\
 & \frac{2 (4 A b^2 - 7 a b B - 5 a^2 (5 A + 7 C)) \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{105 a^2 d \sqrt{\sec [c + d x]}}
 \end{aligned}$$

Result (type 6, 4441 leaves):

$$\begin{aligned}
 & \left( \sqrt{a + b \sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left( - \frac{4 (19 a^2 A b + 8 A b^3 + 63 a^3 B - 14 a b^2 B + 35 a^2 b C) \cot [c]}{105 a^3 d} + \right. \\
 & \quad \frac{(115 a^2 A - 16 A b^2 + 28 a b B + 140 a^2 C) \cos [d x] \sin [c]}{105 a^2 d} + \frac{2 (A b + 7 a B) \cos [2 d x] \sin [2 c]}{35 a d} + \\
 & \quad \frac{A \cos [3 d x] \sin [3 c]}{7 d} + \frac{(115 a^2 A - 16 A b^2 + 28 a b B + 140 a^2 C) \cos [c] \sin [d x]}{105 a^2 d} + \\
 & \quad \left. \left. \frac{2 (A b + 7 a B) \cos [2 c] \sin [2 d x]}{35 a d} + \frac{A \cos [3 c] \sin [3 d x]}{7 d} \right) \right) / \\
 & \left( (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sec [c + d x]^{5/2} \right) - \\
 & \left( 20 A \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]] \right)}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right. \\
 & \quad \left. \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]] \right)}{a \sqrt{1 + \cot [c]^2} \left( -1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right] \csc [c] \right) \\
 & \sqrt{a + b \sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) \sec [d x - \operatorname{ArcTan} [\cot [c]]] \\
 & \sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \operatorname{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}}
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{\sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}}}{\sqrt{b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]]}} \right) / \\
 & \left( 21 d \sqrt{b + a \cos [c + d x]} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. \sqrt{1 + \cot [c]^2} \sec [c + d x]^{5/2} \right) - \\
 & \left( 8 A b^2 \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right. \\
 & \quad \left. \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( -1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right] \csc [c] \\
 & \sqrt{a + b \sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) \sec [d x - \text{ArcTan} [\cot [c]]] \\
 & \left( \frac{\sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}}}{\sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}} \right) / \\
 & \left( 105 a^2 d \sqrt{b + a \cos [c + d x]} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. \sqrt{1 + \cot [c]^2} \sec [c + d x]^{5/2} \right) - \\
 & \left( 28 b B \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( -1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \text{Csc}[c] \\
 & \sqrt{a + b \text{Sec}[c + dx]} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \\
 & \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} - b \text{Csc}[c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} + a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} + b \text{Csc}[c]}} \\
 & \left. \sqrt{b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right/ \\
 & \left( 15 a d \sqrt{b + a \text{Cos}[c + dx]} (A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2 c + 2 dx]) \right. \\
 & \quad \left. \sqrt{1 + \text{Cot}[c]^2} \text{Sec}[c + dx]^{5/2} \right) - \\
 & \left( 4 \text{C AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( 1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \right], \right. \\
 & \quad \left. \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( -1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \text{Csc}[c] \right) \\
 & \sqrt{a + b \text{Sec}[c + dx]} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \\
 & \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} - b \text{Csc}[c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} + a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} + b \text{Csc}[c]}} \\
 & \left. \sqrt{b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right/
 \end{aligned}$$

$$\begin{aligned}
 & \left( 3 d \sqrt{b + a \cos [c + d x]} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. \sqrt{1 + \cot [c]^2} \sec [c + d x]^{5/2} \right) - \\
 & \left( 38 A b \csc [c] \sqrt{a + b \sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left( \left( \operatorname{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, -\left( \sec [c] (b + a \cos [c] \cos [d x + \operatorname{ArcTan} [\tan [c]]) \right) \right] \right. \right. \\
 & \quad \left. \left. \sqrt{1 + \tan [c]^2} \right) \right) / \left( a \sqrt{1 + \tan [c]^2} \left( 1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right), \\
 & \quad - \left( \left( \sec [c] (b + a \cos [c] \cos [d x + \operatorname{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) \right) / \\
 & \quad \left( a \sqrt{1 + \tan [c]^2} \left( -1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right) \sin [d x + \operatorname{ArcTan} [\tan [c]]] \tan [c] \Big/ \\
 & \quad \left( \sqrt{1 + \tan [c]^2} \sqrt{\left( (a \sqrt{1 + \tan [c]^2} - a \cos [d x + \operatorname{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) / \right. \\
 & \quad \left. (b \sec [c] + a \sqrt{1 + \tan [c]^2}) \right) \sqrt{\left( (a \sqrt{1 + \tan [c]^2} + \right. \\
 & \quad \left. a \cos [d x + \operatorname{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) / (-b \sec [c] + a \sqrt{1 + \tan [c]^2}) \Big/ \\
 & \quad \left. \sqrt{b + a \cos [c] \cos [d x + \operatorname{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2}} \right) - \\
 & \quad \left( \frac{\sin [d x + \operatorname{ArcTan} [\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \left( 2 a \cos [c] (b + a \cos [c] \cos [ \right. \right. \\
 & \quad \left. \left. d x + \operatorname{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) \right) / (a^2 \cos [c]^2 + a^2 \sin [c]^2) \Big/ \\
 & \quad \left( \sqrt{b + a \cos [c] \cos [d x + \operatorname{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2}} \right) \Big/ \\
 & \left. \left( 105 d \sqrt{b + a \cos [c + d x]} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sec [c + d x]^{5/2} \right) - \right. \\
 & \left. \left( 16 A b^3 \csc [c] \sqrt{a + b \sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \right] \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \text{Tan}[c]^2} \right) \right) \right) / \left( a \sqrt{1 + \text{Tan}[c]^2} \left( 1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right), \\
 & - \left( \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \right] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \\
 & \quad \left( a \sqrt{1 + \text{Tan}[c]^2} \left( -1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] \Big) / \\
 & \left( \sqrt{1 + \text{Tan}[c]^2} \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} - a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \sqrt{1 + \text{Tan}[c]^2} \right) \right) /} \\
 & \quad \left( b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} + \right. \right. \\
 & \quad \left. \left. a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \sqrt{1 + \text{Tan}[c]^2} \right) / \left( -b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right)} \\
 & \quad \left. \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) - \\
 & \left( \frac{\text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \left( 2 a \text{Cos}[c] \left( b + a \text{Cos}[c] \text{Cos}[ \right. \right. \right. \\
 & \quad \left. \left. \left. dx + \text{ArcTan}[\text{Tan}[c]] \right) \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a^2 \text{Cos}[c]^2 + a^2 \text{Sin}[c]^2 \right) \Big) / \\
 & \quad \left( \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) \Big) / \\
 & \left( 105 a^2 d \sqrt{b + a \text{Cos}[c + dx]} \left( A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2 c + 2 dx] \right) \text{Sec}[c + dx]^{5/2} \right) - \\
 & \left( 6 a B \text{Csc}[c] \sqrt{a + b \text{Sec}[c + dx]} \left( A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2 \right) \right. \\
 & \left. \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \right) \right. \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \text{Tan}[c]^2} \right) \right) \right) / \left( a \sqrt{1 + \text{Tan}[c]^2} \left( 1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \Big) ,
 \end{aligned}$$

$$\begin{aligned}
 & - \left( \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \right. \\
 & \quad \left. \left( a \sqrt{1 + \text{Tan}[c]^2} \left( -1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] / \\
 & \left( \sqrt{1 + \text{Tan}[c]^2} \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} - a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) / \right. \right. \\
 & \quad \left. \left( b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} + \right. \right. \\
 & \quad \left. \left. a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) / \left( -b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) } \\
 & \left. \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) - \\
 & \left( \frac{\text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \left( 2 a \text{Cos}[c] \left( b + a \text{Cos}[c] \text{Cos}[ \right. \right. \right. \\
 & \quad \left. \left. \left. dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a^2 \text{Cos}[c]^2 + a^2 \text{Sin}[c]^2 \right) \right) / \\
 & \left( \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) / \\
 & \left( 5 d \sqrt{b + a \text{Cos}[c + dx]} \left( A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2 c + 2 dx] \right) \right. \\
 & \quad \left. \text{Sec}[c + dx]^{5/2} \right) + \\
 & \left( 4 b^2 B \text{Csc}[c] \sqrt{a + b \text{Sec}[c + dx]} \left( A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2 \right) \right. \\
 & \left. \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \right) \right) \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a \sqrt{1 + \text{Tan}[c]^2} \left( 1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \right), \\
 & - \left( \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \right. \\
 & \quad \left. \left( a \sqrt{1 + \text{Tan}[c]^2} \left( -1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] /
 \end{aligned}$$



$$\begin{aligned}
 & \left( \sqrt{1 + \tan[c]^2} \sqrt{\left( (a \sqrt{1 + \tan[c]^2} - a \cos[d x + \text{ArcTan}[\tan[c]]) \sqrt{1 + \tan[c]^2} \right) / \right.} \\
 & \quad \left. \left( b \sec[c] + a \sqrt{1 + \tan[c]^2} \right) \sqrt{\left( (a \sqrt{1 + \tan[c]^2} + \right.} \right. \\
 & \quad \left. \left. a \cos[d x + \text{ArcTan}[\tan[c]]) \sqrt{1 + \tan[c]^2} \right) / \left( -b \sec[c] + a \sqrt{1 + \tan[c]^2} \right) \right) \\
 & \quad \left. \sqrt{b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]) \sqrt{1 + \tan[c]^2} \right) -} \\
 & \left( \frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \left( 2 a \cos[c] \left( b + a \cos[c] \cos[ \right. \right. \right. \\
 & \quad \left. \left. \left. d x + \text{ArcTan}[\tan[c]]) \sqrt{1 + \tan[c]^2} \right) \right) / \left( a^2 \cos[c]^2 + a^2 \sin[c]^2 \right) \right) / \\
 & \left( \sqrt{b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]) \sqrt{1 + \tan[c]^2} \right) \right) / \\
 & \left( 15 a d \sqrt{b + a \cos[c + d x]} \left( A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x] \right) \right. \\
 & \quad \left. \sec[c + d x]^{5/2} \right) - \\
 & \left( 2 b C \csc[c] \sqrt{a + b \sec[c + d x]} \left( A + B \sec[c + d x] + C \sec[c + d x]^2 \right) \right. \\
 & \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \sec[c] \left( b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]) \right) \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \tan[c]^2} \right) \right) / \left( a \sqrt{1 + \tan[c]^2} \left( 1 - \frac{b \sec[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \right) \right) , \\
 & \quad - \left( \left( \sec[c] \left( b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]) \sqrt{1 + \tan[c]^2} \right) \right) / \right. \\
 & \quad \left. \left( a \sqrt{1 + \tan[c]^2} \left( -1 - \frac{b \sec[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \right) \left. \sin[d x + \text{ArcTan}[\tan[c]]] \tan[c] \right) / \\
 & \left( \sqrt{1 + \tan[c]^2} \sqrt{\left( (a \sqrt{1 + \tan[c]^2} - a \cos[d x + \text{ArcTan}[\tan[c]]) \sqrt{1 + \tan[c]^2} \right) / \right.} \\
 & \quad \left. \left( b \sec[c] + a \sqrt{1 + \tan[c]^2} \right) \sqrt{\left( (a \sqrt{1 + \tan[c]^2} + \right.} \right. \\
 & \quad \left. \left. a \cos[d x + \text{ArcTan}[\tan[c]]) \sqrt{1 + \tan[c]^2} \right) / \left( -b \sec[c] + a \sqrt{1 + \tan[c]^2} \right) \right)
 \end{aligned}$$

$$\left( \sqrt{b+a \cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2} \right) -$$

$$\left( \frac{\sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}} + \left( 2 a \cos [c] \left( b+a \cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2} \right) \right) / \left( a^2 \cos [c]^2+a^2 \sin [c]^2 \right) \right) /$$

$$\left( \sqrt{b+a \cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2} \right) /$$

$$\left( 3 d \sqrt{b+a \cos [c+d x]} \left( A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x] \right) \operatorname{Sec}[c+d x]^{5 / 2} \right)$$

**Problem 1037: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{a+b \operatorname{Sec}[c+d x]} \left( A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2 \right)}{\operatorname{Sec}[c+d x]^{9 / 2}} d x$$

Optimal (type 4, 457 leaves, 11 steps):

$$- \left( \left( 2 \left( a^2-b^2 \right) \left( 16 A b^3-75 a^3 B-24 a b^2 B+6 a^2 b \left( 6 A+7 C \right) \right) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \right. \right.$$

$$\left. \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{\operatorname{Sec}[c+d x]} \right) / \left( 315 a^4 d \sqrt{a+b \operatorname{Sec}[c+d x]} \right) -$$

$$\left( 2 \left( 16 A b^4-57 a^3 b B-24 a b^3 B+6 a^2 b^2 \left( 4 A+7 C \right)-21 a^4 \left( 7 A+9 C \right) \right) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \right.$$

$$\left. \sqrt{a+b \operatorname{Sec}[c+d x]} \right) / \left( 315 a^4 d \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \sqrt{\operatorname{Sec}[c+d x]} \right) +$$

$$\frac{2 A \sqrt{a+b \operatorname{Sec}[c+d x]} \sin [c+d x]}{9 d \operatorname{Sec}[c+d x]^{7 / 2}} + \frac{2 \left( A b+9 a B \right) \sqrt{a+b \operatorname{Sec}[c+d x]} \sin [c+d x]}{63 a d \operatorname{Sec}[c+d x]^{5 / 2}} -$$

$$\frac{2 \left( 6 A b^2-9 a b B-7 a^2 \left( 7 A+9 C \right) \right) \sqrt{a+b \operatorname{Sec}[c+d x]} \sin [c+d x]}{315 a^2 d \operatorname{Sec}[c+d x]^{3 / 2}} +$$

$$\left( 2 \left( 8 A b^3+75 a^3 B-12 a b^2 B+a^2 b \left( 13 A+21 C \right) \right) \sqrt{a+b \operatorname{Sec}[c+d x]} \sin [c+d x] \right) /$$

$$\left( 315 a^3 d \sqrt{\operatorname{Sec}[c+d x]} \right)$$

Result (type 6, 5993 leaves):

$$\begin{aligned}
 & \frac{1}{(A+2C+2B \cos [c+dx]+A \cos [2c+2dx]) \sec [c+dx]^{5/2}} \\
 & \sqrt{a+b \sec [c+dx]} (A+B \sec [c+dx]+C \sec [c+dx]^2) \\
 & \left( -\frac{1}{315 a^4 d} 4 (147 a^4 A-24 a^2 A b^2-16 A b^4+57 a^3 b B+24 a b^3 B+189 a^4 C-42 a^2 b^2 C) \cot [c]+ \right. \\
 & \quad \frac{1}{315 a^3 d} (57 a^2 A b+32 A b^3+345 a^3 B-48 a b^2 B+84 a^2 b C) \cos [d x] \sin [c]+ \\
 & \quad \frac{(133 a^2 A-12 A b^2+18 a b B+126 a^2 C) \cos [2 d x] \sin [2 c]}{315 a^2 d} + \frac{(A b+9 a B) \cos [3 d x] \sin [3 c]}{63 a d} + \\
 & \quad \frac{A \cos [4 d x] \sin [4 c]}{18 d} + \frac{1}{315 a^3 d} (57 a^2 A b+32 A b^3+345 a^3 B-48 a b^2 B+84 a^2 b C) \\
 & \quad \cos [c] \sin [d x]+ \frac{(133 a^2 A-12 A b^2+18 a b B+126 a^2 C) \cos [2 c] \sin [2 d x]}{315 a^2 d} + \\
 & \quad \left. \frac{(A b+9 a B) \cos [3 c] \sin [3 d x]}{63 a d} + \frac{A \cos [4 c] \sin [4 d x]}{18 d} \right) - \\
 & \left( 148 A b \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] \left(b-a \sqrt{1+\cot [c]^2} \sin [c] \sin [d x]-\operatorname{ArcTan}[\cot [c]]\right)}{a \sqrt{1+\cot [c]^2} \left(1+\frac{b \csc [c]}{a \sqrt{1+\cot [c]^2}}\right)}\right], \right. \\
 & \quad \left. \frac{\csc [c] \left(b-a \sqrt{1+\cot [c]^2} \sin [c] \sin [d x]-\operatorname{ArcTan}[\cot [c]]\right)}{a \sqrt{1+\cot [c]^2} \left(-1+\frac{b \csc [c]}{a \sqrt{1+\cot [c]^2}}\right)} \right] \csc [c] \\
 & \sqrt{a+b \sec [c+dx]} (A+B \sec [c+dx]+C \sec [c+dx]^2) \sec [d x-\operatorname{ArcTan}[\cot [c]]] \\
 & \sqrt{\frac{a \sqrt{1+\cot [c]^2}-a \sqrt{1+\cot [c]^2} \sin [d x-\operatorname{ArcTan}[\cot [c]]]}{a \sqrt{1+\cot [c]^2}-b \csc [c]}} \\
 & \sqrt{\frac{a \sqrt{1+\cot [c]^2}+a \sqrt{1+\cot [c]^2} \sin [d x-\operatorname{ArcTan}[\cot [c]]]}{a \sqrt{1+\cot [c]^2}+b \csc [c]}} \\
 & \left. \sqrt{b-a \sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]]} \right) / \\
 & \left( 105 a d \sqrt{b+a \cos [c+dx]} (A+2 C+2 B \cos [c+dx]+A \cos [2 c+2 d x]) \right. \\
 & \quad \left. \sqrt{1+\cot [c]^2} \sec [c+dx]^{5/2} \right) +
 \end{aligned}$$

$$\left( 16 A b^3 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\operatorname{Csc}[c] \left( b - a \sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \right)}{a \sqrt{1 + \operatorname{Cot}[c]^2} \left( 1 + \frac{b \operatorname{Csc}[c]}{a \sqrt{1 + \operatorname{Cot}[c]^2} \right)} \right], \right.$$

$$\left. \frac{\operatorname{Csc}[c] \left( b - a \sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \right)}{a \sqrt{1 + \operatorname{Cot}[c]^2} \left( -1 + \frac{b \operatorname{Csc}[c]}{a \sqrt{1 + \operatorname{Cot}[c]^2} \right)} \right] \operatorname{Csc}[c]$$

$$\sqrt{a + b \operatorname{Sec}[c + d x]} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]$$

$$\sqrt{\frac{a \sqrt{1 + \operatorname{Cot}[c]^2} - a \sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}{a \sqrt{1 + \operatorname{Cot}[c]^2} - b \operatorname{Csc}[c]}}$$

$$\sqrt{\frac{a \sqrt{1 + \operatorname{Cot}[c]^2} + a \sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}{a \sqrt{1 + \operatorname{Cot}[c]^2} + b \operatorname{Csc}[c]}}$$

$$\left. \sqrt{b - a \sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) /$$

$$\left( 315 a^3 d \sqrt{b + a \operatorname{Cos}[c + d x]} (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sec}[c + d x]^{5/2} \right) -$$

$$\left( 20 B \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\operatorname{Csc}[c] \left( b - a \sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \right)}{a \sqrt{1 + \operatorname{Cot}[c]^2} \left( 1 + \frac{b \operatorname{Csc}[c]}{a \sqrt{1 + \operatorname{Cot}[c]^2} \right)} \right], \right.$$

$$\left. \frac{\operatorname{Csc}[c] \left( b - a \sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \right)}{a \sqrt{1 + \operatorname{Cot}[c]^2} \left( -1 + \frac{b \operatorname{Csc}[c]}{a \sqrt{1 + \operatorname{Cot}[c]^2} \right)} \right] \operatorname{Csc}[c]$$

$$\sqrt{a + b \operatorname{Sec}[c + d x]} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]$$

$$\sqrt{\frac{a \sqrt{1 + \operatorname{Cot}[c]^2} - a \sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}{a \sqrt{1 + \operatorname{Cot}[c]^2} - b \operatorname{Csc}[c]}}$$

$$\sqrt{\frac{a \sqrt{1 + \operatorname{Cot}[c]^2} + a \sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}{a \sqrt{1 + \operatorname{Cot}[c]^2} + b \operatorname{Csc}[c]}}$$

$$\left. \sqrt{b - a \sqrt{1 + \cot[c]^2} \sin[c] \sin[d x - \text{ArcTan}[\cot[c]]]} \right/$$

$$\left( 21 d \sqrt{b + a \cos[c + d x]} (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) \sqrt{1 + \cot[c]^2} \sec[c + d x]^{5/2} - \right.$$

$$\left. \left( 8 b^2 B \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc[c] \left( b - a \sqrt{1 + \cot[c]^2} \sin[c] \sin[d x - \text{ArcTan}[\cot[c]]] \right)}{a \sqrt{1 + \cot[c]^2} \left( 1 + \frac{b \csc[c]}{a \sqrt{1 + \cot[c]^2}} \right)} \right], \right. \right.$$

$$\left. \frac{\csc[c] \left( b - a \sqrt{1 + \cot[c]^2} \sin[c] \sin[d x - \text{ArcTan}[\cot[c]]] \right)}{a \sqrt{1 + \cot[c]^2} \left( -1 + \frac{b \csc[c]}{a \sqrt{1 + \cot[c]^2}} \right)} \right] \csc[c]$$

$$\sqrt{a + b \sec[c + d x]} (A + B \sec[c + d x] + C \sec[c + d x]^2) \sec[d x - \text{ArcTan}[\cot[c]]]$$

$$\sqrt{\frac{a \sqrt{1 + \cot[c]^2} - a \sqrt{1 + \cot[c]^2} \sin[d x - \text{ArcTan}[\cot[c]]]}{a \sqrt{1 + \cot[c]^2} - b \csc[c]}}$$

$$\sqrt{\frac{a \sqrt{1 + \cot[c]^2} + a \sqrt{1 + \cot[c]^2} \sin[d x - \text{ArcTan}[\cot[c]]]}{a \sqrt{1 + \cot[c]^2} + b \csc[c]}}$$

$$\left. \sqrt{b - a \sqrt{1 + \cot[c]^2} \sin[c] \sin[d x - \text{ArcTan}[\cot[c]]]} \right/$$

$$\left( 105 a^2 d \sqrt{b + a \cos[c + d x]} (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) \sqrt{1 + \cot[c]^2} \sec[c + d x]^{5/2} - \right.$$

$$\left. \left( 28 b C \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc[c] \left( b - a \sqrt{1 + \cot[c]^2} \sin[c] \sin[d x - \text{ArcTan}[\cot[c]]] \right)}{a \sqrt{1 + \cot[c]^2} \left( 1 + \frac{b \csc[c]}{a \sqrt{1 + \cot[c]^2}} \right)} \right], \right. \right.$$

$$\left. \frac{\csc[c] \left( b - a \sqrt{1 + \cot[c]^2} \sin[c] \sin[d x - \text{ArcTan}[\cot[c]]] \right)}{a \sqrt{1 + \cot[c]^2} \left( -1 + \frac{b \csc[c]}{a \sqrt{1 + \cot[c]^2}} \right)} \right] \csc[c]$$

$$\sqrt{a + b \sec[c + d x]} (A + B \sec[c + d x] + C \sec[c + d x]^2) \sec[d x - \text{ArcTan}[\cot[c]]]$$

$$\sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}}$$

$$\sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}}$$

$$\sqrt{b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]]} \Big/$$

$$\left( 15 a d \sqrt{b + a \cos [c + d x]} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right.$$

$$\left. \sqrt{1 + \cot [c]^2} \sec [c + d x]^{5/2} \right) -$$

$$\left( 14 a A \csc [c] \sqrt{a + b \sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right.$$

$$\left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \sec [c] (b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]) \right) \right. \right. \right.$$

$$\left. \left. \left. \sqrt{1 + \tan [c]^2} \right) \right) \Big/ \left( a \sqrt{1 + \tan [c]^2} \left( 1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right),$$

$$- \left( \left( \sec [c] (b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]) \right) \sqrt{1 + \tan [c]^2} \right) \Big/$$

$$\left( a \sqrt{1 + \tan [c]^2} \left( -1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \Big] \sin [d x + \text{ArcTan} [\tan [c]]] \tan [c] \Big/$$

$$\left( \sqrt{1 + \tan [c]^2} \sqrt{\left( (a \sqrt{1 + \tan [c]^2} - a \cos [d x + \text{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) \Big/ \right.$$

$$\left( b \sec [c] + a \sqrt{1 + \tan [c]^2} \right) \sqrt{\left( (a \sqrt{1 + \tan [c]^2} + \right.$$

$$\left. \left. a \cos [d x + \text{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) \Big/ \left( -b \sec [c] + a \sqrt{1 + \tan [c]^2} \right) \right)}$$

$$\sqrt{b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2}} \Big) -$$

$$\left( \frac{\sin [d x + \text{ArcTan} [\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \left( 2 a \cos [c] (b + a \cos [c] \cos [c + d x]) \right. \right.$$



$$\begin{aligned}
 & \left( 32 A b^4 \operatorname{Csc}[c] \sqrt{a+b \operatorname{Sec}[c+d x]} (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \right. \\
 & \left. \left( \left( \operatorname{AppellF1}\left[-\frac{1}{2},-\frac{1}{2},-\frac{1}{2},\frac{1}{2},-\left(\operatorname{Sec}[c]\left(b+a \operatorname{Cos}[c] \operatorname{Cos}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]\right)\right.\right.\right.\right. \right. \right. \\
 & \left. \left. \left. \left. \sqrt{1+\operatorname{Tan}[c]^2}\right)\right)\right) / \left(a \sqrt{1+\operatorname{Tan}[c]^2}\left(1-\frac{b \operatorname{Sec}[c]}{a \sqrt{1+\operatorname{Tan}[c]^2}}\right)\right) \right), \\
 & -\left(\left(\operatorname{Sec}[c]\left(b+a \operatorname{Cos}[c] \operatorname{Cos}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]\right)\right) \sqrt{1+\operatorname{Tan}[c]^2}\right) / \\
 & \left.\left(a \sqrt{1+\operatorname{Tan}[c]^2}\left(-1-\frac{b \operatorname{Sec}[c]}{a \sqrt{1+\operatorname{Tan}[c]^2}}\right)\right)\right) \operatorname{Sin}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] \Big/ \\
 & \left(\sqrt{1+\operatorname{Tan}[c]^2} \sqrt{\left(\left(a \sqrt{1+\operatorname{Tan}[c]^2}-a \operatorname{Cos}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]\right)\right) \sqrt{1+\operatorname{Tan}[c]^2}\right) /} \\
 & \left.\left(b \operatorname{Sec}[c]+a \sqrt{1+\operatorname{Tan}[c]^2}\right)\right) \sqrt{\left(\left(a \sqrt{1+\operatorname{Tan}[c]^2}+ \right. \right. \\
 & \left. \left. a \operatorname{Cos}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]\right)\right) \sqrt{1+\operatorname{Tan}[c]^2}} / \left(-b \operatorname{Sec}[c]+a \sqrt{1+\operatorname{Tan}[c]^2}\right) \Big) \\
 & \left.\sqrt{b+a \operatorname{Cos}[c] \operatorname{Cos}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1+\operatorname{Tan}[c]^2}}\right) - \\
 & \left(\frac{\operatorname{Sin}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1+\operatorname{Tan}[c]^2}}+\left(2 a \operatorname{Cos}[c]\left(b+a \operatorname{Cos}[c] \operatorname{Cos}[ \right. \right. \right. \\
 & \left. \left. \left. d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]\right)\right) \sqrt{1+\operatorname{Tan}[c]^2}\right) / \left(a^2 \operatorname{Cos}[c]^2+a^2 \operatorname{Sin}[c]^2\right) \Big) / \\
 & \left.\left(\sqrt{b+a \operatorname{Cos}[c] \operatorname{Cos}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1+\operatorname{Tan}[c]^2}}\right)\right) \Big/ \\
 & \left(315 a^3 d \sqrt{b+a \operatorname{Cos}[c+d x]}(A+2 C+2 B \operatorname{Cos}[c+d x]+A \operatorname{Cos}[2 c+2 d x]) \right. \\
 & \left. \operatorname{Sec}[c+d x]^{5 / 2}\right) - \\
 & \left(38 b B \operatorname{Csc}[c] \sqrt{a+b \operatorname{Sec}[c+d x]}(A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \right. \\
 & \left. \left(\left(\operatorname{AppellF1}\left[-\frac{1}{2},-\frac{1}{2},-\frac{1}{2},\frac{1}{2},-\left(\operatorname{Sec}[c]\left(b+a \operatorname{Cos}[c] \operatorname{Cos}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]\right)\right)\right.\right.\right.\right. \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & \left. \left. \left. \left. \left. \sqrt{1 + \tan[c]^2} \right) \right) \right) \right) \left/ \left( a \sqrt{1 + \tan[c]^2} \left( 1 - \frac{b \sec[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \right), \\
 & - \left( \left( \sec[c] \left( b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2} \right) \right) \right) \left/ \right. \\
 & \left. \left( a \sqrt{1 + \tan[c]^2} \left( -1 - \frac{b \sec[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \right) \left. \sin[d x + \text{ArcTan}[\tan[c]]] \tan[c] \right) \left/ \right. \\
 & \left( \sqrt{1 + \tan[c]^2} \sqrt{\left( \left( a \sqrt{1 + \tan[c]^2} - a \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2} \right) \right) \right) \left/ \right. \\
 & \left. \left( b \sec[c] + a \sqrt{1 + \tan[c]^2} \right) \sqrt{\left( \left( a \sqrt{1 + \tan[c]^2} + \right. \right. \right. \\
 & \left. \left. \left. a \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2} \right) \right) \right) \left/ \left( -b \sec[c] + a \sqrt{1 + \tan[c]^2} \right) \right) \\
 & \left. \sqrt{b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}} \right) - \\
 & \left( \frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \left( 2 a \cos[c] \left( b + a \cos[c] \cos \right. \right. \right. \\
 & \left. \left. \left. d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2} \right) \right) \right) \left/ \left( a^2 \cos[c]^2 + a^2 \sin[c]^2 \right) \right) \left/ \right. \\
 & \left. \left( \sqrt{b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}} \right) \right) \right) \left/ \right. \\
 & \left( 105 d \sqrt{b + a \cos[c + d x]} \left( A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x] \right) \right. \\
 & \left. \sec[c + d x]^{5/2} \right) - \\
 & \left( 16 b^3 B \csc[c] \sqrt{a + b \sec[c + d x]} \left( A + B \sec[c + d x] + C \sec[c + d x]^2 \right) \right. \\
 & \left. \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \sec[c] \left( b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \right) \right) \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \sqrt{1 + \tan[c]^2} \right) \right) \right) \right) \left/ \left( a \sqrt{1 + \tan[c]^2} \left( 1 - \frac{b \sec[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \right) \right) \right), \\
 & - \left( \left( \sec[c] \left( b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2} \right) \right) \right) \left/ \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( a \sqrt{1 + \tan^2[c]} \left( -1 - \frac{b \sec[c]}{a \sqrt{1 + \tan^2[c]}} \right) \right) \left[ \sin[d x + \text{ArcTan}[\tan[c]]] \tan[c] \right] / \\
 & \left( \sqrt{1 + \tan^2[c]} \sqrt{\left( \left( a \sqrt{1 + \tan^2[c]} - a \cos[d x + \text{ArcTan}[\tan[c]]] \right) \sqrt{1 + \tan^2[c]} \right) / \right. \\
 & \left. \left( b \sec[c] + a \sqrt{1 + \tan^2[c]} \right) \sqrt{\left( \left( a \sqrt{1 + \tan^2[c]} + \right. \right. \right. \\
 & \left. \left. \left. a \cos[d x + \text{ArcTan}[\tan[c]]] \right) \sqrt{1 + \tan^2[c]} \right) / \left( -b \sec[c] + a \sqrt{1 + \tan^2[c]} \right) \right) \\
 & \left. \sqrt{b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan^2[c]}} \right) - \\
 & \left( \frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan^2[c]}} + \left( 2 a \cos[c] \left( b + a \cos[c] \cos[ \right. \right. \right. \\
 & \left. \left. \left. d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan^2[c]} \right) \right) / \left( a^2 \cos^2[c] + a^2 \sin^2[c] \right) \right) / \\
 & \left( \sqrt{b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan^2[c]}} \right) \left. \right) \left. \right) / \\
 & \left( 105 a^2 d \sqrt{b + a \cos[c + d x]} \left( A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x] \right) \right. \\
 & \left. \sec[c + d x]^{5/2} \right) - \\
 & \left( 6 a C \csc[c] \sqrt{a + b \sec[c + d x]} \left( A + B \sec[c + d x] + C \sec[c + d x]^2 \right) \right. \\
 & \left. \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \sec[c] \left( b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \right) \right) \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \sqrt{1 + \tan^2[c]} \right) \right) / \left( a \sqrt{1 + \tan^2[c]} \left( 1 - \frac{b \sec[c]}{a \sqrt{1 + \tan^2[c]}} \right) \right) \right) \right) , \\
 & - \left( \left( \sec[c] \left( b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \right) \sqrt{1 + \tan^2[c]} \right) \right) / \\
 & \left( a \sqrt{1 + \tan^2[c]} \left( -1 - \frac{b \sec[c]}{a \sqrt{1 + \tan^2[c]}} \right) \right) \left[ \sin[d x + \text{ArcTan}[\tan[c]]] \tan[c] \right] / \\
 & \left( \sqrt{1 + \tan^2[c]} \sqrt{\left( \left( a \sqrt{1 + \tan^2[c]} - a \cos[d x + \text{ArcTan}[\tan[c]]] \right) \sqrt{1 + \tan^2[c]} \right) / \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( b \sec [c] + a \sqrt{1 + \tan [c]^2} \right) \sqrt{\left( \left( a \sqrt{1 + \tan [c]^2} + \right. \right. \\
 & \quad \left. \left. a \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2} \right) / \left( -b \sec [c] + a \sqrt{1 + \tan [c]^2} \right) \right)} \\
 & \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2}} \Big) - \\
 & \left( \frac{\sin [d x + \text{ArcTan} [\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \left( 2 a \cos [c] \left( b + a \cos [c] \cos [ \right. \right. \right. \\
 & \quad \left. \left. \left. d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2} \right) \right) / \left( a^2 \cos [c]^2 + a^2 \sin [c]^2 \right) \right) / \\
 & \left( \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2}} \right) \Big) / \\
 & \left( 5 d \sqrt{b + a \cos [c + d x]} \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \right. \\
 & \quad \left. \sec [c + d x]^{5/2} \right) + \\
 & \left( 4 b^2 C \csc [c] \sqrt{a + b \sec [c + d x]} \left( A + B \sec [c + d x] + C \sec [c + d x]^2 \right) \right. \\
 & \left. \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \sec [c] \left( b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]] \right) \right) \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \tan [c]^2} \right) \right) / \left( a \sqrt{1 + \tan [c]^2} \left( 1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right) \Big), \\
 & - \left( \left( \sec [c] \left( b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2} \right) \right) / \right. \\
 & \quad \left. \left( a \sqrt{1 + \tan [c]^2} \left( -1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right) \Big) \sin [d x + \text{ArcTan} [\tan [c]]] \tan [c] \Big) / \\
 & \left( \sqrt{1 + \tan [c]^2} \sqrt{\left( \left( a \sqrt{1 + \tan [c]^2} - a \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2} \right) / \right. \right. \\
 & \quad \left. \left. \left( b \sec [c] + a \sqrt{1 + \tan [c]^2} \right) \right) \sqrt{\left( \left( a \sqrt{1 + \tan [c]^2} + \right. \right. \right. \\
 & \quad \left. \left. \left. a \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2} \right) \right) / \left( -b \sec [c] + a \sqrt{1 + \tan [c]^2} \right) \right)} \\
 & \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2}} \Big) -
 \end{aligned}$$

$$\left( \frac{\sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \left( 2 a \text{Cos}[c] \left( b + a \text{Cos}[c] \text{Cos} [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a^2 \text{Cos}[c]^2 + a^2 \text{Sin}[c]^2 \right) \right) / \left( \sqrt{b + a \text{Cos}[c] \text{Cos} [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) / \left( 15 a d \sqrt{b + a \text{Cos}[c + d x]} \left( A + 2 C + 2 B \text{Cos}[c + d x] + A \text{Cos}[2 c + 2 d x] \right) \text{Sec}[c + d x]^{5/2} \right)$$

**Problem 1038: Result unnecessarily involves imaginary or complex numbers.**

$$\int \text{Sec}[c + d x]^{3/2} (a + b \text{Sec}[c + d x])^{3/2} (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) dx$$

Optimal (type 4, 551 leaves, 15 steps):

$$\left( (136 a^2 b B + 128 b^3 B - 3 a^3 C + 12 a b^2 (28 A + 19 C)) \sqrt{\frac{b + a \text{Cos}[c + d x]}{a + b}} \text{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{\text{Sec}[c + d x]} \right) / (192 b d \sqrt{a + b \text{Sec}[c + d x]}) - \left( (8 a^3 b B - 96 a b^3 B - 3 a^4 C - 24 a^2 b^2 (2 A + C) - 16 b^4 (4 A + 3 C)) \sqrt{\frac{b + a \text{Cos}[c + d x]}{a + b}} \text{EllipticPi}\left[2, \frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{\text{Sec}[c + d x]} \right) / (64 b^2 d \sqrt{a + b \text{Sec}[c + d x]}) - \left( (24 a^2 b B + 128 b^3 B - 9 a^3 C + 12 a b^2 (20 A + 13 C)) \text{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \text{Sec}[c + d x]} \right) / \left( 192 b^2 d \sqrt{\frac{b + a \text{Cos}[c + d x]}{a + b}} \sqrt{\text{Sec}[c + d x]} \right) + \frac{1}{192 b^2 d} (24 a^2 b B + 128 b^3 B - 9 a^3 C + 12 a b^2 (20 A + 13 C)) \sqrt{\text{Sec}[c + d x]} \sqrt{a + b \text{Sec}[c + d x]} \text{Sin}[c + d x] + \frac{1}{96 b d} (48 A b^2 + 56 a b B + 3 a^2 C + 36 b^2 C) \text{Sec}[c + d x]^{3/2} \sqrt{a + b \text{Sec}[c + d x]} \text{Sin}[c + d x] + \frac{(8 b B + 3 a C) \text{Sec}[c + d x]^{5/2} \sqrt{a + b \text{Sec}[c + d x]} \text{Sin}[c + d x]}{24 d} + \frac{C \text{Sec}[c + d x]^{5/2} (a + b \text{Sec}[c + d x])^{3/2} \text{Sin}[c + d x]}{4 d}$$



$$\left( (a + b \operatorname{Sec}[c + d x])^{3/2} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \left( \frac{1}{12} \operatorname{Sec}[c + d x]^3 (8 b B \operatorname{Sin}[c + d x] + 9 a C \operatorname{Sin}[c + d x]) + \frac{1}{48 b} \operatorname{Sec}[c + d x]^2 (48 A b^2 \operatorname{Sin}[c + d x] + 56 a b B \operatorname{Sin}[c + d x] + 3 a^2 C \operatorname{Sin}[c + d x] + 36 b^2 C \operatorname{Sin}[c + d x]) + \frac{1}{96 b^2} \operatorname{Sec}[c + d x] (240 a A b^2 \operatorname{Sin}[c + d x] + 24 a^2 b B \operatorname{Sin}[c + d x] + 128 b^3 B \operatorname{Sin}[c + d x] - 9 a^3 C \operatorname{Sin}[c + d x] + 156 a b^2 C \operatorname{Sin}[c + d x]) + \frac{1}{2} b C \operatorname{Sec}[c + d x]^3 \operatorname{Tan}[c + d x] \right) \right) / \left( d (b + a \operatorname{Cos}[c + d x]) (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \operatorname{Sec}[c + d x]^{7/2} \right)$$

**Problem 1039: Result unnecessarily involves imaginary or complex numbers.**

$$\int \sqrt{\operatorname{Sec}[c + d x]} (a + b \operatorname{Sec}[c + d x])^{3/2} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 4, 446 leaves, 14 steps):

$$\left( (42 a b B + 8 b^2 (3 A + 2 C) + a^2 (48 A + 17 C)) \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b} \sqrt{\operatorname{Sec}[c + d x]}\right] \right) / (24 d \sqrt{a + b \operatorname{Sec}[c + d x]}) + \left( (6 a^2 b B + 8 b^3 B - a^3 C + 12 a b^2 (2 A + C)) \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \operatorname{EllipticPi}\left[2, \frac{1}{2} (c + d x), \frac{2 a}{a + b} \sqrt{\operatorname{Sec}[c + d x]}\right] \right) / (8 b d \sqrt{a + b \operatorname{Sec}[c + d x]}) - \left( (24 A b^2 + 30 a b B + 3 a^2 C + 16 b^2 C) \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b} \sqrt{a + b \operatorname{Sec}[c + d x]}\right] \right) / \left( 24 b d \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \sqrt{\operatorname{Sec}[c + d x]} \right) + \frac{1}{24 b d} (24 A b^2 + 30 a b B + 3 a^2 C + 16 b^2 C) \sqrt{\operatorname{Sec}[c + d x]} \sqrt{a + b \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x] + \frac{(2 b B + a C) \operatorname{Sec}[c + d x]^{3/2} \sqrt{a + b \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{4 d} + \frac{C \operatorname{Sec}[c + d x]^{3/2} (a + b \operatorname{Sec}[c + d x])^{3/2} \operatorname{Sin}[c + d x]}{3 d}$$

Result (type 4, 800 leaves):

$$\begin{aligned}
 & - \left( \left( (a + b \operatorname{Sec}[c + d x])^{3/2} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \right. \\
 & \left. \left( 2 (-96 a^2 A b - 24 a b^2 B - 28 a^2 b C) \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right) \right) / \\
 & \left( \sqrt{b + a \operatorname{Cos}[c + d x]} \right) + \left( 2 (-120 a A b^2 - 6 a^2 b B - 48 b^3 B + 9 a^3 C - 56 a b^2 C) \right. \\
 & \left. \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right) / \left( \sqrt{b + a \operatorname{Cos}[c + d x]} \right) + \\
 & \left( 2 i (24 a A b^2 + 30 a^2 b B + 3 a^3 C + 16 a b^2 C) \sqrt{\frac{a - a \operatorname{Cos}[c + d x]}{a + b}} \sqrt{\frac{a + a \operatorname{Cos}[c + d x]}{a - b}} \right. \\
 & \left. \operatorname{Cos}[2(c + d x)] \left( -2 b (a + b) \operatorname{EllipticE}\left[ i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \operatorname{Cos}[c + d x]}\right], \right. \right. \right. \\
 & \left. \left. \frac{-a + b}{a + b} \right] + a \left( 2 b \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \operatorname{Cos}[c + d x]}\right], \frac{-a + b}{a + b}\right] + \right. \right. \\
 & \left. \left. a \operatorname{EllipticPi}\left[1 - \frac{a}{b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \operatorname{Cos}[c + d x]}\right], \frac{-a + b}{a + b}\right] \right) \right) \right) \\
 & \left. \operatorname{Sin}[c + d x] \right) / \left( \sqrt{\frac{1}{a - b}} b \sqrt{1 - \operatorname{Cos}[c + d x]^2} \sqrt{\frac{a^2 - a^2 \operatorname{Cos}[c + d x]^2}{a^2}} \right. \\
 & \left. \left. \left( -a^2 + 2 b^2 - 4 b (b + a \operatorname{Cos}[c + d x]) + 2 (b + a \operatorname{Cos}[c + d x])^2 \right) \right) \right) / \\
 & \left( 48 b d (b + a \operatorname{Cos}[c + d x])^{3/2} (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \right. \\
 & \left. \operatorname{Sec}[c + d x]^{7/2} \right) + \\
 & \left( (a + b \operatorname{Sec}[c + d x])^{3/2} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \left( \frac{1}{6} \operatorname{Sec}[c + d x]^2 (6 b B \operatorname{Sin}[c + d x] + 7 a C \operatorname{Sin}[c + d x]) + \frac{1}{12 b} \operatorname{Sec}[c + d x] \right. \\
 & \left. (24 A b^2 \operatorname{Sin}[c + d x] + 30 a b B \operatorname{Sin}[c + d x] + 3 a^2 C \operatorname{Sin}[c + d x] + 16 b^2 C \operatorname{Sin}[c + d x]) + \right. \\
 & \left. \frac{2}{3} b C \operatorname{Sec}[c + d x]^2 \operatorname{Tan}[c + d x] \right) \right) /
 \end{aligned}$$

$$\frac{(d (b + a \cos [c + d x]) (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sec [c + d x]^{7/2})}{\sec [c + d x]^{7/2}}$$

**Problem 1040: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(a + b \sec [c + d x])^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sqrt{\sec [c + d x]}} dx$$

Optimal (type 4, 353 leaves, 13 steps):

$$\left( (8 a^2 B + 4 b^2 B + a b (8 A + 7 C)) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b} \sqrt{\sec [c + d x]}\right] / (4 d \sqrt{a + b \sec [c + d x]}) + \right. \\ \left. \left( (8 A b^2 + 12 a b B + 3 a^2 C + 4 b^2 C) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticPi}\left[2, \frac{1}{2} (c + d x), \frac{2 a}{a + b} \sqrt{\sec [c + d x]}\right] / (4 d \sqrt{a + b \sec [c + d x]}) + \right. \right. \\ \left. \left. \frac{(8 a A - 4 b B - 5 a C) \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b} \sqrt{a + b \sec [c + d x]}\right]}{4 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \sqrt{\sec [c + d x]}} + \right. \right. \\ \left. \left. \frac{(4 b B + 3 a C) \sqrt{\sec [c + d x]} \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{4 d} + \right. \right. \\ \left. \left. \frac{C \sqrt{\sec [c + d x]} (a + b \sec [c + d x])^{3/2} \sin [c + d x]}{2 d} \right) \right]$$

Result (type 4, 709 leaves):





twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Sec}[c + d x])^{3/2} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[c + d x]^{3/2}} dx$$

Optimal (type 4, 340 leaves, 13 steps):

$$\left( (6 a b B - b^2 (2 A - 3 C) + 2 a^2 (A + 3 C)) \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b} \sqrt{\operatorname{Sec}[c + d x]}\right] \right) / (3 d \sqrt{a + b \operatorname{Sec}[c + d x]}) +$$

$$\left( b (2 b B + 3 a C) \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \operatorname{EllipticPi}\left[2, \frac{1}{2} (c + d x), \frac{2 a}{a + b} \sqrt{\operatorname{Sec}[c + d x]}\right] \right) /$$

$$(d \sqrt{a + b \operatorname{Sec}[c + d x]}) + \frac{(8 A b + 6 a B - 3 b C) \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b} \sqrt{a + b \operatorname{Sec}[c + d x]}\right]}{3 d \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \sqrt{\operatorname{Sec}[c + d x]}}$$

$$\frac{b (2 A - 3 C) \sqrt{\operatorname{Sec}[c + d x]} \sqrt{a + b \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{3 d} +$$

$$\frac{2 A (a + b \operatorname{Sec}[c + d x])^{3/2} \operatorname{Sin}[c + d x]}{3 d \sqrt{\operatorname{Sec}[c + d x]}}$$

Result (type 4, 685 leaves):



### Problem 1042: Unable to integrate problem.

$$\int \frac{(a + b \operatorname{Sec}[c + d x])^{3/2} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[c + d x]^{5/2}} dx$$

Optimal (type 4, 356 leaves, 13 steps):

$$\begin{aligned} & - \left( \left( 2 (3 A b^3 - 5 a^3 B + 5 a b^2 B - 3 a^2 b (A + 5 C)) \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \right. \right. \\ & \quad \left. \left. \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{\operatorname{Sec}[c + d x]} \right) / \left( 15 a d \sqrt{a + b \operatorname{Sec}[c + d x]} \right) \right) + \\ & \frac{2 b^2 C \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \operatorname{EllipticPi}\left[2, \frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{\operatorname{Sec}[c + d x]}}{d \sqrt{a + b \operatorname{Sec}[c + d x]}} + \\ & \left( 2 (3 A b^2 + 20 a b B + 3 a^2 (3 A + 5 C)) \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \operatorname{Sec}[c + d x]} \right) / \\ & \left( 15 a d \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \sqrt{\operatorname{Sec}[c + d x]} \right) + \\ & \frac{2 (3 A b + 5 a B) \sqrt{a + b \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{15 d \sqrt{\operatorname{Sec}[c + d x]}} + \\ & \frac{2 A (a + b \operatorname{Sec}[c + d x])^{3/2} \operatorname{Sin}[c + d x]}{5 d \operatorname{Sec}[c + d x]^{3/2}} \end{aligned}$$

Result (type 8, 47 leaves):

$$\int \frac{(a + b \operatorname{Sec}[c + d x])^{3/2} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[c + d x]^{5/2}} dx$$

### Problem 1043: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Sec}[c + d x])^{3/2} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[c + d x]^{7/2}} dx$$

Optimal (type 4, 359 leaves, 10 steps):

$$\begin{aligned}
 & \left( 2 (a^2 - b^2) (25 a^2 A - 6 A b^2 + 21 a b B + 35 a^2 C) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \\
 & \quad \left. \text{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{\sec [c + d x]} \right) / \left( 105 a^2 d \sqrt{a + b \sec [c + d x]} \right) - \\
 & \left( 2 (6 A b^3 - 63 a^3 B - 21 a b^2 B - 2 a^2 b (41 A + 70 C)) \text{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right. \\
 & \quad \left. \sqrt{a + b \sec [c + d x]} \right) / \left( 105 a^2 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \sqrt{\sec [c + d x]} \right) + \\
 & \frac{2 (3 A b + 7 a B) \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{35 d \sec [c + d x]^{3/2}} + \\
 & \frac{2 (3 A b^2 + 42 a b B + 5 a^2 (5 A + 7 C)) \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{105 a d \sqrt{\sec [c + d x]}} + \\
 & \frac{2 A (a + b \sec [c + d x])^{3/2} \sin [c + d x]}{7 d \sec [c + d x]^{5/2}}
 \end{aligned}$$

Result (type 6, 4862 leaves):

$$\begin{aligned}
 & \left( (a + b \sec [c + d x])^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left( - \frac{4 (82 a^2 A b - 6 A b^3 + 63 a^3 B + 21 a b^2 B + 140 a^2 b C) \cot [c]}{105 a^2 d} + \right. \\
 & \quad \frac{(115 a^2 A + 12 A b^2 + 168 a b B + 140 a^2 C) \cos [d x] \sin [c]}{105 a d} + \\
 & \quad \frac{2 (8 A b + 7 a B) \cos [2 d x] \sin [2 c]}{35 d} + \frac{a A \cos [3 d x] \sin [3 c]}{7 d} + \\
 & \quad \frac{(115 a^2 A + 12 A b^2 + 168 a b B + 140 a^2 C) \cos [c] \sin [d x]}{105 a d} + \\
 & \quad \left. \left. \frac{2 (8 A b + 7 a B) \cos [2 c] \sin [2 d x]}{35 d} + \frac{a A \cos [3 c] \sin [3 d x]}{7 d} \right) \right) / \\
 & \left( (b + a \cos [c + d x]) (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sec [c + d x]^{7/2} \right) - \\
 & \left( 20 a A \text{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] (b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan}[\cot [c]])]}{a \sqrt{1 + \cot [c]^2} \left(1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}\right)}\right], \right. \\
 & \quad \left. \frac{\csc [c] (b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan}[\cot [c]])]}{a \sqrt{1 + \cot [c]^2} \left(-1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}\right)}\right] \csc [c] \right) \\
 & (a + b \sec [c + d x])^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \sec [d x - \text{ArcTan}[\cot [c]]]
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}} \\
 & \left. \sqrt{b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]]} \right) / \\
 & \left( 21 d (b + a \cos [c + d x])^{3/2} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \left. \sqrt{1 + \cot [c]^2} \sec [c + d x]^{7/2} \right) - \\
 & \left( 68 A b^2 \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right. \\
 & \left. \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( -1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right] \csc [c] \\
 & (a + b \sec [c + d x])^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \sec [d x - \text{ArcTan} [\cot [c]]] \\
 & \sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}} \\
 & \left. \sqrt{b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]]} \right) / \\
 & \left( 35 a d (b + a \cos [c + d x])^{3/2} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \left. \sqrt{1 + \cot [c]^2} \sec [c + d x]^{7/2} \right) -
 \end{aligned}$$

$$\left( 16 b B \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]] \right]}{a \sqrt{1 + \text{Cot}[c]^2} \left( 1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2} \right)} \right)} \right], \right.$$

$$\left. \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]] \right]}{a \sqrt{1 + \text{Cot}[c]^2} \left( -1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2} \right)} \right)}{\left( a + b \text{Sec}[c + dx] \right)^{3/2} \left( A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2 \right) \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right)$$

$$\sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} - b \text{Csc}[c]}}$$

$$\sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} + a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} + b \text{Csc}[c]}}$$

$$\left. \sqrt{b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right) /$$

$$\left( 5 d \left( b + a \text{Cos}[c + dx] \right)^{3/2} \left( A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2 c + 2 dx] \right) \sqrt{1 + \text{Cot}[c]^2} \text{Sec}[c + dx]^{7/2} \right) -$$

$$\left( 4 a C \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]] \right]}{a \sqrt{1 + \text{Cot}[c]^2} \left( 1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2} \right)} \right)} \right], \right.$$

$$\left. \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]] \right]}{a \sqrt{1 + \text{Cot}[c]^2} \left( -1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2} \right)} \right)}{\left( a + b \text{Sec}[c + dx] \right)^{3/2} \left( A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2 \right) \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right)$$

$$\sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} - b \text{Csc}[c]}}$$

$$\sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} + a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} + b \text{Csc}[c]}}$$

$$\left. \sqrt{b - a \sqrt{1 + \cot^2[c]} \sin[c] \sin[d x - \text{ArcTan}[\cot[c]]]} \right/$$

$$\left( 3 d (b + a \cos[c + d x])^{3/2} (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) \sqrt{1 + \cot^2[c]} \sec[c + d x]^{7/2} \right) -$$

$$\left( 4 b^2 C \text{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc[c] \left( b - a \sqrt{1 + \cot^2[c]} \sin[c] \sin[d x - \text{ArcTan}[\cot[c]]] \right)}{a \sqrt{1 + \cot^2[c]} \left( 1 + \frac{b \csc[c]}{a \sqrt{1 + \cot^2[c]}} \right)}\right], \right.$$

$$\left. \frac{\csc[c] \left( b - a \sqrt{1 + \cot^2[c]} \sin[c] \sin[d x - \text{ArcTan}[\cot[c]]] \right)}{a \sqrt{1 + \cot^2[c]} \left( -1 + \frac{b \csc[c]}{a \sqrt{1 + \cot^2[c]}} \right)} \right] \csc[c]$$

$$(a + b \sec[c + d x])^{3/2} (A + B \sec[c + d x] + C \sec[c + d x]^2) \sec[d x - \text{ArcTan}[\cot[c]]]$$

$$\sqrt{\frac{a \sqrt{1 + \cot^2[c]} - a \sqrt{1 + \cot^2[c]} \sin[d x - \text{ArcTan}[\cot[c]]]}{a \sqrt{1 + \cot^2[c]} - b \csc[c]}}$$

$$\sqrt{\frac{a \sqrt{1 + \cot^2[c]} + a \sqrt{1 + \cot^2[c]} \sin[d x - \text{ArcTan}[\cot[c]]]}{a \sqrt{1 + \cot^2[c]} + b \csc[c]}}$$

$$\left. \sqrt{b - a \sqrt{1 + \cot^2[c]} \sin[c] \sin[d x - \text{ArcTan}[\cot[c]]]} \right/$$

$$\left( a d (b + a \cos[c + d x])^{3/2} (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) \sqrt{1 + \cot^2[c]} \sec[c + d x]^{7/2} \right) -$$

$$\left( 164 a A b \csc[c] (a + b \sec[c + d x])^{3/2} (A + B \sec[c + d x] + C \sec[c + d x]^2) \right.$$

$$\left. \left( \left( \text{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, -\left( \sec[c] \left( b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \right) \sqrt{1 + \tan^2[c]} \right) \right] \right) \right) \right) \left( a \sqrt{1 + \tan^2[c]} \left( 1 - \frac{b \sec[c]}{a \sqrt{1 + \tan^2[c]}} \right) \right) \right),$$



$$\begin{aligned}
 & - \left( \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \right. \\
 & \quad \left. \left( a \sqrt{1 + \text{Tan}[c]^2} \left( -1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] / \\
 & \left( \sqrt{1 + \text{Tan}[c]^2} \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} - a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \right. \\
 & \quad \left. \left( b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} + \right. \right. \\
 & \quad \left. \left. a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) / \left( -b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) \\
 & \quad \left. \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) - \\
 & \left( \frac{\text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \left( 2 a \text{Cos}[c] \left( b + a \text{Cos}[c] \text{Cos}[ \right. \right. \right. \\
 & \quad \left. \left. \left. dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a^2 \text{Cos}[c]^2 + a^2 \text{Sin}[c]^2 \right) \right) / \\
 & \quad \left( \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \\
 & \left( 105 d (b + a \text{Cos}[c + dx])^{3/2} (A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2 c + 2 dx]) \text{Sec}[c + dx]^{7/2} \right) + \\
 & \left( 4 A b^3 \text{Csc}[c] (a + b \text{Sec}[c + dx])^{3/2} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \right. \\
 & \quad \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \right) \right) \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a \sqrt{1 + \text{Tan}[c]^2} \left( 1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \right), \\
 & - \left( \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \right. \\
 & \quad \left. \left( a \sqrt{1 + \text{Tan}[c]^2} \left( -1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] /
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{1 + \tan[c]^2} \sqrt{\left( \left( a \sqrt{1 + \tan[c]^2} - a \cos[d x + \text{ArcTan}[\tan[c]] \right] \sqrt{1 + \tan[c]^2} \right) / \right. \\
 & \quad \left. \left( b \sec[c] + a \sqrt{1 + \tan[c]^2} \right) \right) \sqrt{\left( \left( a \sqrt{1 + \tan[c]^2} + \right. \right. \\
 & \quad \left. \left. a \cos[d x + \text{ArcTan}[\tan[c]] \right] \sqrt{1 + \tan[c]^2} \right) / \left( -b \sec[c] + a \sqrt{1 + \tan[c]^2} \right) } \\
 & \quad \left. \sqrt{b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}} \right) - \\
 & \left( \frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \left( 2 a \cos[c] \left( b + a \cos[c] \cos[ \right. \right. \right. \\
 & \quad \left. \left. \left. d x + \text{ArcTan}[\tan[c]] \right] \sqrt{1 + \tan[c]^2} \right) \right) / \left( a^2 \cos[c]^2 + a^2 \sin[c]^2 \right) \right) / \\
 & \left( \sqrt{b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}} \right) \Big) / \\
 & \left( 35 a d (b + a \cos[c + d x])^{3/2} (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) \sec[c + d x]^{7/2} \right) - \\
 & \left( 6 a^2 B \csc[c] (a + b \sec[c + d x])^{3/2} (A + B \sec[c + d x] + C \sec[c + d x]^2) \right. \\
 & \left. \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \sec[c] \left( b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]] \right] \right. \right. \right. \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \tan[c]^2} \right) \right) \right) / \left( a \sqrt{1 + \tan[c]^2} \left( 1 - \frac{b \sec[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \right) \Big), \\
 & - \left( \left( \sec[c] \left( b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2} \right) \right) / \right. \\
 & \quad \left. \left( a \sqrt{1 + \tan[c]^2} \left( -1 - \frac{b \sec[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \right) \Big) \sin[d x + \text{ArcTan}[\tan[c]]] \tan[c] \Big) / \\
 & \left( \sqrt{1 + \tan[c]^2} \sqrt{\left( \left( a \sqrt{1 + \tan[c]^2} - a \cos[d x + \text{ArcTan}[\tan[c]] \right] \sqrt{1 + \tan[c]^2} \right) / \right. \\
 & \quad \left. \left( b \sec[c] + a \sqrt{1 + \tan[c]^2} \right) \right) \sqrt{\left( \left( a \sqrt{1 + \tan[c]^2} + \right. \right. \\
 & \quad \left. \left. a \cos[d x + \text{ArcTan}[\tan[c]] \right] \sqrt{1 + \tan[c]^2} \right) / \left( -b \sec[c] + a \sqrt{1 + \tan[c]^2} \right) } \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \sqrt{b+a \cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}} \right) - \\
 & \left( \frac{\sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}} + \left( 2 a \cos [c] \left( b+a \cos [c] \cos [ \right. \right. \right. \\
 & \quad \left. \left. \left. d x+\operatorname{ArcTan}[\tan [c]] \right] \sqrt{1+\tan [c]^2} \right) \right) / \left( a^2 \cos [c]^2+a^2 \sin [c]^2 \right) \right) / \\
 & \left( \sqrt{b+a \cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}} \right) \Big) / \\
 & \left( 5 d (b+a \cos [c+d x])^{3 / 2} (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right. \\
 & \quad \left. \sec [c+d x]^{7 / 2} \right) - \\
 & \left( 2 b^2 B \csc [c] (a+b \sec [c+d x])^{3 / 2} (A+B \sec [c+d x]+C \sec [c+d x]^2) \right. \\
 & \quad \left. \left( \left( \operatorname{AppellF1}\left[-\frac{1}{2},-\frac{1}{2},-\frac{1}{2}, \frac{1}{2},-\left(\sec [c] \left(b+a \cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]\right] \right. \right. \right. \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1+\tan [c]^2}\right)\right) / \left(a \sqrt{1+\tan [c]^2} \left(1-\frac{b \sec [c]}{a \sqrt{1+\tan [c]^2}}\right)\right) \right) \right), \\
 & - \left( \left( \sec [c] \left(b+a \cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}\right) \right) / \right. \\
 & \quad \left. \left( a \sqrt{1+\tan [c]^2} \left(-1-\frac{b \sec [c]}{a \sqrt{1+\tan [c]^2}}\right) \right) \right) \sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c] \Big) / \\
 & \left( \sqrt{1+\tan [c]^2} \sqrt{\left(\left(a \sqrt{1+\tan [c]^2}-a \cos [d x+\operatorname{ArcTan}[\tan [c]]\right] \sqrt{1+\tan [c]^2}\right) / \right. \\
 & \quad \left. \left(b \sec [c]+a \sqrt{1+\tan [c]^2}\right) \right) \sqrt{\left(\left(a \sqrt{1+\tan [c]^2}+ \right. \right. \\
 & \quad \left. \left. a \cos [d x+\operatorname{ArcTan}[\tan [c]]\right] \sqrt{1+\tan [c]^2}\right) / \left(-b \sec [c]+a \sqrt{1+\tan [c]^2}\right) \right) \Big) \\
 & \left. \sqrt{b+a \cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}} \right) - \\
 & \left( \frac{\sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}} + \left( 2 a \cos [c] \left( b+a \cos [c] \cos [ \right. \right. \right.
 \end{aligned}$$



$$\sec [c + d x]^{7/2}$$

Problem 1044: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(a + b \sec [c + d x])^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sec [c + d x]^{9/2}} dx$$

Optimal (type 4, 455 leaves, 11 steps):

$$\begin{aligned} & \left( 2 (a^2 - b^2) (8 A b^3 + 75 a^3 B - 18 a b^2 B + a^2 (39 A b + 63 b C)) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \\ & \quad \left. \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b} \sqrt{\sec [c + d x]}\right] \right) / (315 a^3 d \sqrt{a + b \sec [c + d x]}) + \\ & \left( 2 (8 A b^4 + 246 a^3 b B - 18 a b^3 B + 21 a^4 (7 A + 9 C) + 3 a^2 b^2 (11 A + 21 C)) \right. \\ & \quad \left. \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b} \sqrt{a + b \sec [c + d x]}\right] \right) / \\ & \left( 315 a^3 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \sqrt{\sec [c + d x]} \right) + \frac{2 (A b + 3 a B) \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{21 d \sec [c + d x]^{5/2}} + \\ & \frac{2 (3 A b^2 + 72 a b B + 7 a^2 (7 A + 9 C)) \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{315 a d \sec [c + d x]^{3/2}} - \\ & \left( 2 (4 A b^3 - 75 a^3 B - 9 a b^2 B - 2 a^2 b (44 A + 63 C)) \sqrt{a + b \sec [c + d x]} \sin [c + d x] \right) / \\ & \left( 315 a^2 d \sqrt{\sec [c + d x]} \right) + \frac{2 A (a + b \sec [c + d x])^{3/2} \sin [c + d x]}{9 d \sec [c + d x]^{7/2}} \end{aligned}$$

Result (type 6, 5997 leaves):

$$\begin{aligned} & \left( (a + b \sec [c + d x])^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\ & \quad \left( -\frac{1}{315 a^3 d} 4 (147 a^4 A + 33 a^2 A b^2 + 8 A b^4 + 246 a^3 b B - 18 a b^3 B + 189 a^4 C + 63 a^2 b^2 C) \cot [c] + \right. \\ & \quad \frac{1}{315 a^2 d} (402 a^2 A b - 16 A b^3 + 345 a^3 B + 36 a b^2 B + 504 a^2 b C) \cos [d x] \sin [c] + \\ & \quad \frac{(133 a^2 A + 6 A b^2 + 144 a b B + 126 a^2 C) \cos [2 d x] \sin [2 c]}{315 a d} + \\ & \quad \frac{(10 A b + 9 a B) \cos [3 d x] \sin [3 c]}{63 d} + \frac{a A \cos [4 d x] \sin [4 c]}{18 d} + \frac{1}{315 a^2 d} \\ & \quad \left. \left. (402 a^2 A b - 16 A b^3 + 345 a^3 B + 36 a b^2 B + 504 a^2 b C) \cos [c] \sin [d x] + \right. \right. \\ & \quad \left. \left. \frac{(133 a^2 A + 6 A b^2 + 144 a b B + 126 a^2 C) \cos [2 c] \sin [2 d x]}{315 a d} \right) \right. \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{(10 A b + 9 a B) \cos[3 c] \sin[3 d x]}{63 d} + \frac{a A \cos[4 c] \sin[4 d x]}{18 d} \right) / \\
 & \left( (b + a \cos[c + d x]) (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) \sec[c + d x]^{7/2} \right) - \\
 & \left( 248 A b \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc[c] \left( b - a \sqrt{1 + \cot[c]^2} \sin[c] \sin[d x - \operatorname{ArcTan}[\cot[c]]] \right)}{a \sqrt{1 + \cot[c]^2} \left( 1 + \frac{b \csc[c]}{a \sqrt{1 + \cot[c]^2}} \right)} \right], \right. \\
 & \left. \frac{\csc[c] \left( b - a \sqrt{1 + \cot[c]^2} \sin[c] \sin[d x - \operatorname{ArcTan}[\cot[c]]] \right)}{a \sqrt{1 + \cot[c]^2} \left( -1 + \frac{b \csc[c]}{a \sqrt{1 + \cot[c]^2}} \right)} \right] \csc[c] \\
 & (a + b \sec[c + d x])^{3/2} (A + B \sec[c + d x] + C \sec[c + d x]^2) \sec[d x - \operatorname{ArcTan}[\cot[c]]] \\
 & \sqrt{\frac{a \sqrt{1 + \cot[c]^2} - a \sqrt{1 + \cot[c]^2} \sin[d x - \operatorname{ArcTan}[\cot[c]]]}{a \sqrt{1 + \cot[c]^2} - b \csc[c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \cot[c]^2} + a \sqrt{1 + \cot[c]^2} \sin[d x - \operatorname{ArcTan}[\cot[c]]]}{a \sqrt{1 + \cot[c]^2} + b \csc[c]}} \\
 & \left. \sqrt{b - a \sqrt{1 + \cot[c]^2} \sin[c] \sin[d x - \operatorname{ArcTan}[\cot[c]]]} \right) / \\
 & \left( 105 d (b + a \cos[c + d x])^{3/2} (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) \right. \\
 & \left. \sqrt{1 + \cot[c]^2} \sec[c + d x]^{7/2} \right) - \\
 & \left( 8 A b^3 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc[c] \left( b - a \sqrt{1 + \cot[c]^2} \sin[c] \sin[d x - \operatorname{ArcTan}[\cot[c]]] \right)}{a \sqrt{1 + \cot[c]^2} \left( 1 + \frac{b \csc[c]}{a \sqrt{1 + \cot[c]^2}} \right)} \right], \right. \\
 & \left. \frac{\csc[c] \left( b - a \sqrt{1 + \cot[c]^2} \sin[c] \sin[d x - \operatorname{ArcTan}[\cot[c]]] \right)}{a \sqrt{1 + \cot[c]^2} \left( -1 + \frac{b \csc[c]}{a \sqrt{1 + \cot[c]^2}} \right)} \right] \csc[c] \\
 & (a + b \sec[c + d x])^{3/2} (A + B \sec[c + d x] + C \sec[c + d x]^2) \sec[d x - \operatorname{ArcTan}[\cot[c]]] \\
 & \sqrt{\frac{a \sqrt{1 + \cot[c]^2} - a \sqrt{1 + \cot[c]^2} \sin[d x - \operatorname{ArcTan}[\cot[c]]]}{a \sqrt{1 + \cot[c]^2} - b \csc[c]}}
 \end{aligned}$$

$$\left( \frac{\sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}}}{\sqrt{b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]]}} \right) /$$

$$\left( 315 a^2 d (b + a \cos [c + d x])^{3/2} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} \sec [c + d x]^{7/2} \right) -$$

$$\left( 20 a B \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] (b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]])}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right.$$

$$\left. \frac{\csc [c] (b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]])}{a \sqrt{1 + \cot [c]^2} \left( -1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right] \csc [c]$$

$$(a + b \sec [c + d x])^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \sec [d x - \text{ArcTan} [\cot [c]]]$$

$$\left( \frac{\sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}}}{\sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}}} \right) /$$

$$\left( 21 d (b + a \cos [c + d x])^{3/2} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} \sec [c + d x]^{7/2} \right) -$$

$$\left( 68 b^2 B \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] (b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]])}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right.$$

$$\begin{aligned}
 & \left. \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( -1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \right] \text{Csc}[c] \\
 & (a + b \text{Sec}[c + dx])^{3/2} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \\
 & \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} - b \text{Csc}[c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} + a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} + b \text{Csc}[c]}} \\
 & \left. \sqrt{b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right) / \\
 & \left( 35 a d (b + a \text{Cos}[c + dx])^{3/2} (A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2 c + 2 dx]) \right. \\
 & \left. \sqrt{1 + \text{Cot}[c]^2} \text{Sec}[c + dx]^{7/2} \right) - \\
 & \left( 16 b C \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( 1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \right], \right. \\
 & \left. \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( -1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \right] \text{Csc}[c] \\
 & (a + b \text{Sec}[c + dx])^{3/2} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \\
 & \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} - b \text{Csc}[c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} + a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} + b \text{Csc}[c]}} \\
 & \left. \sqrt{b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right) /
 \end{aligned}$$



$$\begin{aligned}
 & \left( 5 d (b + a \cos [c + d x])^{3/2} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. \sqrt{1 + \cot [c]^2} \sec [c + d x]^{7/2} \right) - \\
 & \left( 14 a^2 A \csc [c] (a + b \sec [c + d x])^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left( \left( \operatorname{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, -\left( \sec [c] (b + a \cos [c] \cos [d x + \operatorname{ArcTan} [\tan [c]]) \right) \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \tan [c]^2} \right) \right] \right) / \left( a \sqrt{1 + \tan [c]^2} \left( 1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right), \\
 & \quad - \left( \left( \sec [c] (b + a \cos [c] \cos [d x + \operatorname{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) \right) / \\
 & \quad \left( a \sqrt{1 + \tan [c]^2} \left( -1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \left. \right) \sin [d x + \operatorname{ArcTan} [\tan [c]]] \tan [c] \Bigg) / \\
 & \quad \left( \sqrt{1 + \tan [c]^2} \sqrt{\left( (a \sqrt{1 + \tan [c]^2} - a \cos [d x + \operatorname{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) / \right. \\
 & \quad \left. (b \sec [c] + a \sqrt{1 + \tan [c]^2}) \right) \sqrt{\left( (a \sqrt{1 + \tan [c]^2} + \right. \\
 & \quad \left. a \cos [d x + \operatorname{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) / (-b \sec [c] + a \sqrt{1 + \tan [c]^2}) \right) \\
 & \quad \left. \sqrt{b + a \cos [c] \cos [d x + \operatorname{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2}} \right) - \\
 & \quad \left( \frac{\sin [d x + \operatorname{ArcTan} [\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \left( 2 a \cos [c] (b + a \cos [c] \cos [ \right. \right. \\
 & \quad \left. \left. d x + \operatorname{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) \right) / (a^2 \cos [c]^2 + a^2 \sin [c]^2) \Bigg) / \\
 & \quad \left( \sqrt{b + a \cos [c] \cos [d x + \operatorname{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2}} \right) \Bigg) / \\
 & \left( 15 d (b + a \cos [c + d x])^{3/2} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sec [c + d x]^{7/2} \right) - \\
 & \left( 22 A b^2 \csc [c] (a + b \sec [c + d x])^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \right] \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \text{Tan}[c]^2} \right) \right) \right) / \left( a \sqrt{1 + \text{Tan}[c]^2} \left( 1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right), \\
 & - \left( \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \right. \\
 & \quad \left. \left( a \sqrt{1 + \text{Tan}[c]^2} \left( -1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] \Bigg) / \\
 & \left( \sqrt{1 + \text{Tan}[c]^2} \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} - a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right] \sqrt{1 + \text{Tan}[c]^2} \right) / \right. \right. \\
 & \quad \left. \left( b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} + \right. \right. \right. \\
 & \quad \left. \left. \left. a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right] \sqrt{1 + \text{Tan}[c]^2} \right) / \left( -b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) \right) \\
 & \quad \left. \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) - \\
 & \left( \frac{\text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \left( 2 a \text{Cos}[c] \left( b + a \text{Cos}[c] \text{Cos}[ \right. \right. \right. \\
 & \quad \left. \left. \left. dx + \text{ArcTan}[\text{Tan}[c]] \right] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a^2 \text{Cos}[c]^2 + a^2 \text{Sin}[c]^2 \right) \Bigg) / \\
 & \left( \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) \Bigg) / \\
 & \left( 105 d (b + a \text{Cos}[c + dx])^{3/2} (A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2 c + 2 dx]) \text{Sec}[c + dx]^{7/2} \right) - \\
 & \left( 16 A b^4 \text{Csc}[c] (a + b \text{Sec}[c + dx])^{3/2} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \right. \\
 & \left. \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \right] \right. \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \text{Tan}[c]^2} \right) \right) \right) / \left( a \sqrt{1 + \text{Tan}[c]^2} \left( 1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \Bigg),
 \end{aligned}$$

$$\begin{aligned}
 & - \left( \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \right. \\
 & \quad \left. \left( a \sqrt{1 + \text{Tan}[c]^2} \left( -1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] / \\
 & \left( \sqrt{1 + \text{Tan}[c]^2} \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} - a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) / \right. \right. \\
 & \quad \left. \left( b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} + \right. \right. \\
 & \quad \left. \left. a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) / \left( -b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) } \\
 & \quad \left. \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) - \\
 & \left( \frac{\text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \left( 2 a \text{Cos}[c] \left( b + a \text{Cos}[c] \text{Cos}[ \right. \right. \right. \\
 & \quad \left. \left. \left. dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a^2 \text{Cos}[c]^2 + a^2 \text{Sin}[c]^2 \right) \right) / \\
 & \left( \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) / \\
 & \left( 315 a^2 d (b + a \text{Cos}[c + dx])^{3/2} (A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2 c + 2 dx]) \right. \\
 & \quad \left. \text{Sec}[c + dx]^{7/2} \right) - \\
 & \left( 164 a b B \text{Csc}[c] (a + b \text{Sec}[c + dx])^{3/2} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \right. \\
 & \quad \left. \left( \left( \text{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, -\left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \right) \right) \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a \sqrt{1 + \text{Tan}[c]^2} \left( 1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \right), \\
 & - \left( \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \right. \\
 & \quad \left. \left( a \sqrt{1 + \text{Tan}[c]^2} \left( -1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] /
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{1 + \tan[c]^2} \sqrt{\left( (a \sqrt{1 + \tan[c]^2} - a \cos[d x + \text{ArcTan}[\tan[c]]) \sqrt{1 + \tan[c]^2} \right) / \right.} \\
 & \quad \left. \left( b \sec[c] + a \sqrt{1 + \tan[c]^2} \right) \sqrt{\left( (a \sqrt{1 + \tan[c]^2} + \right.} \right. \\
 & \quad \left. \left. a \cos[d x + \text{ArcTan}[\tan[c]]) \sqrt{1 + \tan[c]^2} \right) / \left( -b \sec[c] + a \sqrt{1 + \tan[c]^2} \right) \right) \\
 & \quad \left. \sqrt{b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]) \sqrt{1 + \tan[c]^2} \right) -} \\
 & \left( \frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \left( 2 a \cos[c] \left( b + a \cos[c] \cos[ \right. \right. \right. \\
 & \quad \left. \left. \left. d x + \text{ArcTan}[\tan[c]]) \sqrt{1 + \tan[c]^2} \right) \right) / \left( a^2 \cos[c]^2 + a^2 \sin[c]^2 \right) \right) / \\
 & \left( \sqrt{b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]) \sqrt{1 + \tan[c]^2} \right) \right) / \\
 & \left( 105 d (b + a \cos[c + d x])^{3/2} (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) \right. \\
 & \quad \left. \sec[c + d x]^{7/2} \right) + \\
 & \left( 4 b^3 B \csc[c] (a + b \sec[c + d x])^{3/2} (A + B \sec[c + d x] + C \sec[c + d x]^2) \right. \\
 & \left. \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \sec[c] \left( b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]) \right) \right. \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \tan[c]^2} \right) \right) / \left( a \sqrt{1 + \tan[c]^2} \left( 1 - \frac{b \sec[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \right) \right), \\
 & \quad - \left( \left( \sec[c] \left( b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]) \sqrt{1 + \tan[c]^2} \right) \right) / \right. \\
 & \quad \left. \left( a \sqrt{1 + \tan[c]^2} \left( -1 - \frac{b \sec[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \right) \sin[d x + \text{ArcTan}[\tan[c]]] \tan[c] \right) / \\
 & \left( \sqrt{1 + \tan[c]^2} \sqrt{\left( (a \sqrt{1 + \tan[c]^2} - a \cos[d x + \text{ArcTan}[\tan[c]]) \sqrt{1 + \tan[c]^2} \right) / \right.} \\
 & \quad \left. \left( b \sec[c] + a \sqrt{1 + \tan[c]^2} \right) \sqrt{\left( (a \sqrt{1 + \tan[c]^2} + \right.} \right. \\
 & \quad \left. \left. a \cos[d x + \text{ArcTan}[\tan[c]]) \sqrt{1 + \tan[c]^2} \right) / \left( -b \sec[c] + a \sqrt{1 + \tan[c]^2} \right) \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \sqrt{b+a \cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}} \right) - \\
 & \left( \frac{\sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}} + \left( 2 a \cos [c] \left( b+a \cos [c] \cos [ \right. \right. \right. \\
 & \quad \left. \left. \left. d x+\operatorname{ArcTan}[\tan [c]] \right] \sqrt{1+\tan [c]^2} \right) \right) / \left( a^2 \cos [c]^2+a^2 \sin [c]^2 \right) \right) / \\
 & \left( \left( \sqrt{b+a \cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}} \right) \right) / \\
 & \left( 35 a d (b+a \cos [c+d x])^{3 / 2} (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right. \\
 & \quad \left. \sec [c+d x]^{7 / 2} \right) - \\
 & \left( 6 a^2 C \csc [c] (a+b \sec [c+d x])^{3 / 2} (A+B \sec [c+d x]+C \sec [c+d x]^2) \right. \\
 & \quad \left( \left( \operatorname{AppellF1}\left[-\frac{1}{2},-\frac{1}{2},-\frac{1}{2}, \frac{1}{2},-\left(\sec [c] \left(b+a \cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]\right] \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1+\tan [c]^2}\right)\right) / \left(a \sqrt{1+\tan [c]^2} \left(1-\frac{b \sec [c]}{a \sqrt{1+\tan [c]^2}}\right)\right) \right) \right), \\
 & \quad - \left( \left( \sec [c] \left(b+a \cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]\right] \sqrt{1+\tan [c]^2} \right) \right) / \\
 & \quad \left( a \sqrt{1+\tan [c]^2} \left(-1-\frac{b \sec [c]}{a \sqrt{1+\tan [c]^2}}\right) \right) \right) \sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c] \Big) / \\
 & \left( \sqrt{1+\tan [c]^2} \sqrt{\left(\left(a \sqrt{1+\tan [c]^2}-a \cos [d x+\operatorname{ArcTan}[\tan [c]]\right] \sqrt{1+\tan [c]^2}\right) / \right. \\
 & \quad \left. \left(b \sec [c]+a \sqrt{1+\tan [c]^2}\right) \right) \sqrt{\left(\left(a \sqrt{1+\tan [c]^2}+ \right. \right. \\
 & \quad \left. \left. a \cos [d x+\operatorname{ArcTan}[\tan [c]]\right] \sqrt{1+\tan [c]^2}\right) / \left(-b \sec [c]+a \sqrt{1+\tan [c]^2}\right) \right) \Big) \\
 & \left. \sqrt{b+a \cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}} \right) - \\
 & \left( \frac{\sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}} + \left( 2 a \cos [c] \left( b+a \cos [c] \cos [ \right. \right. \right.
 \end{aligned}$$



$$\sec [c + d x]^{7/2}$$

**Problem 1045: Result unnecessarily involves imaginary or complex numbers.**

$$\int \sqrt{\sec [c + d x]} (a + b \sec [c + d x])^{5/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 4, 550 leaves, 15 steps):

$$\begin{aligned} & \left( (472 a^2 b B + 128 b^3 B + 4 a b^2 (132 A + 89 C) + a^3 (384 A + 133 C)) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \\ & \quad \left. \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \sqrt{\sec [c + d x]} \right) / (192 d \sqrt{a + b \sec [c + d x]}) + \\ & \left( (40 a^3 b B + 160 a b^3 B - 5 a^4 C + 120 a^2 b^2 (2 A + C) + 16 b^4 (4 A + 3 C)) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \\ & \quad \left. \operatorname{EllipticPi}\left[2, \frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \sqrt{\sec [c + d x]} \right) / (64 b d \sqrt{a + b \sec [c + d x]}) - \\ & \left( (264 a^2 b B + 128 b^3 B + 15 a^3 C + 4 a b^2 (108 A + 71 C)) \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right. \\ & \quad \left. \sqrt{a + b \sec [c + d x]} \right) / \left( 192 b d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \sqrt{\sec [c + d x]} \right) + \frac{1}{192 b d} \\ & \left( (264 a^2 b B + 128 b^3 B + 15 a^3 C + 4 a b^2 (108 A + 71 C)) \sqrt{\sec [c + d x]} \sqrt{a + b \sec [c + d x]} \sin [c + d x] + \right. \\ & \quad \frac{1}{32 d} (16 A b^2 + 24 a b B + 5 a^2 C + 12 b^2 C) \sec [c + d x]^{3/2} \sqrt{a + b \sec [c + d x]} \sin [c + d x] + \\ & \quad \left. \frac{(8 b B + 5 a C) \sec [c + d x]^{3/2} (a + b \sec [c + d x])^{3/2} \sin [c + d x]}{24 d} + \right. \\ & \quad \left. \frac{C \sec [c + d x]^{3/2} (a + b \sec [c + d x])^{5/2} \sin [c + d x]}{4 d} \right) \end{aligned}$$

Result (type 4, 925 leaves):

$$\begin{aligned} & - \left( (a + b \sec [c + d x])^{5/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\ & \quad \left. \left( 2 (-768 a^3 A b - 192 a A b^3 - 416 a^2 b^2 B - 236 a^3 b C - 144 a b^3 C) \right) \right) \end{aligned}$$





$$\frac{1}{96 b} \operatorname{Sec}[c+d x] \left( 432 a A b^2 \operatorname{Sin}[c+d x] + 264 a^2 b B \operatorname{Sin}[c+d x] + 128 b^3 B \operatorname{Sin}[c+d x] + 15 a^3 C \operatorname{Sin}[c+d x] + 284 a b^2 C \operatorname{Sin}[c+d x] \right) + \frac{1}{2} b^2 C \operatorname{Sec}[c+d x]^3 \operatorname{Tan}[c+d x] \Big) \Big/ \left( d (b+a \operatorname{Cos}[c+d x])^2 (A+2 C+2 B \operatorname{Cos}[c+d x]+A \operatorname{Cos}[2 c+2 d x]) \operatorname{Sec}[c+d x]^{9/2} \right)$$

**Problem 1046: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{(a+b \operatorname{Sec}[c+d x])^{5/2} (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2)}{\sqrt{\operatorname{Sec}[c+d x]}} dx$$

Optimal (type 4, 453 leaves, 14 steps):

$$\left( (48 a^3 B + 66 a b^2 B + 8 b^3 (3 A + 2 C) + a^2 b (96 A + 59 C)) \sqrt{\frac{b+a \operatorname{Cos}[c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b} \sqrt{\operatorname{Sec}[c+d x]}\right] \right) \Big/ (24 d \sqrt{a+b \operatorname{Sec}[c+d x]}) + \left( (30 a^2 b B + 8 b^3 B + 5 a^3 C + 20 a b^2 (2 A + C)) \sqrt{\frac{b+a \operatorname{Cos}[c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b} \sqrt{\operatorname{Sec}[c+d x]}\right] \right) \Big/ (8 d \sqrt{a+b \operatorname{Sec}[c+d x]}) - \left( (54 a b B - a^2 (48 A - 33 C) + 8 b^2 (3 A + 2 C)) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b} \sqrt{a+b \operatorname{Sec}[c+d x]}\right] \right) \Big/ \left( 24 d \sqrt{\frac{b+a \operatorname{Cos}[c+d x]}{a+b}} \sqrt{\operatorname{Sec}[c+d x]} \right) + \frac{1}{24 d} (24 A b^2 + 42 a b B + 15 a^2 C + 16 b^2 C) \sqrt{\operatorname{Sec}[c+d x]} \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x] + \frac{(6 b B + 5 a C) \sqrt{\operatorname{Sec}[c+d x]} (a+b \operatorname{Sec}[c+d x])^{3/2} \operatorname{Sin}[c+d x]}{12 d} + \frac{C \sqrt{\operatorname{Sec}[c+d x]} (a+b \operatorname{Sec}[c+d x])^{5/2} \operatorname{Sin}[c+d x]}{3 d}$$

Result (type 4, 817 leaves):

$$\left( (a+b \operatorname{Sec}[c+d x])^{5/2} (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \right)$$



$$\left( \frac{2}{3} b^2 C \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx] \right) / \left( d (b+a \operatorname{Cos}[c+dx])^2 (A+2C+2B \operatorname{Cos}[c+dx]+A \operatorname{Cos}[2c+2dx]) \operatorname{Sec}[c+dx]^{9/2} \right)$$

**Problem 1047: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{(a+b \operatorname{Sec}[c+dx])^{5/2} (A+B \operatorname{Sec}[c+dx]+C \operatorname{Sec}[c+dx]^2)}{\operatorname{Sec}[c+dx]^{3/2}} dx$$

Optimal (type 4, 427 leaves, 14 steps):

$$\left( (48 a^2 b B + 12 b^3 B + 8 a^3 (A + 3 C) + a b^2 (16 A + 33 C)) \sqrt{\frac{b + a \operatorname{Cos}[c+dx]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), \frac{2a}{a+b} \sqrt{\operatorname{Sec}[c+dx]}\right] / (12 d \sqrt{a+b \operatorname{Sec}[c+dx]}) + \left( b (8 A b^2 + 20 a b B + 15 a^2 C + 4 b^2 C) \sqrt{\frac{b + a \operatorname{Cos}[c+dx]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+dx), \frac{2a}{a+b}\right] \sqrt{\operatorname{Sec}[c+dx]} \right) / (4 d \sqrt{a+b \operatorname{Sec}[c+dx]}) + \left( (24 a^2 B - 12 b^2 B + a b (56 A - 27 C)) \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), \frac{2a}{a+b} \sqrt{a+b \operatorname{Sec}[c+dx]}\right] / \left( 12 d \sqrt{\frac{b + a \operatorname{Cos}[c+dx]}{a+b}} \sqrt{\operatorname{Sec}[c+dx]} \right) - \frac{1}{12 d} b (8 a A - 12 b B - 21 a C) \sqrt{\operatorname{Sec}[c+dx]} \sqrt{a+b \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx] - \frac{b (4 A - 3 C) \sqrt{\operatorname{Sec}[c+dx]} (a+b \operatorname{Sec}[c+dx])^{3/2} \operatorname{Sin}[c+dx]}{6 d} + \frac{2 A (a+b \operatorname{Sec}[c+dx])^{5/2} \operatorname{Sin}[c+dx]}{3 d \sqrt{\operatorname{Sec}[c+dx]}} \right)$$

Result (type 4, 766 leaves):

$$\left( (a+b \operatorname{Sec}[c+dx])^{5/2} (A+B \operatorname{Sec}[c+dx]+C \operatorname{Sec}[c+dx]^2) \left( \left( 2 (16 a^3 A + 144 a A b^2 + 144 a^2 b B + 48 a^3 C + 12 a b^2 C) \sqrt{\frac{b + a \operatorname{Cos}[c+dx]}{a+b}} \right) \right) \right)$$



$$\int \frac{(a + b \operatorname{Sec}[c + d x])^{5/2} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[c + d x]^{5/2}} dx$$

Optimal (type 4, 419 leaves, 14 steps):

$$\left( (10 a^3 B + 20 a b^2 B - b^3 (16 A - 15 C) + 4 a^2 b (4 A + 15 C)) \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \right. \\ \left. \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \sqrt{\operatorname{Sec}[c + d x]} \right) / (15 d \sqrt{a + b \operatorname{Sec}[c + d x]}) + \\ \left( b^2 (2 b B + 5 a C) \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \sqrt{\operatorname{Sec}[c + d x]} \right) / \\ (d \sqrt{a + b \operatorname{Sec}[c + d x]}) + \\ \left( (70 a b B + b^2 (46 A - 15 C) + 6 a^2 (3 A + 5 C)) \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \operatorname{Sec}[c + d x]} \right) / \\ \left( 15 d \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \sqrt{\operatorname{Sec}[c + d x]} \right) - \frac{1}{15 d} \\ b (16 A b + 10 a B - 15 b C) \sqrt{\operatorname{Sec}[c + d x]} \sqrt{a + b \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x] + \\ \frac{2 (A b + a B) (a + b \operatorname{Sec}[c + d x])^{3/2} \operatorname{Sin}[c + d x]}{3 d \sqrt{\operatorname{Sec}[c + d x]}} + \frac{2 A (a + b \operatorname{Sec}[c + d x])^{5/2} \operatorname{Sin}[c + d x]}{5 d \operatorname{Sec}[c + d x]^{3/2}}$$

Result (type 4, 755 leaves):

$$\left( (a + b \operatorname{Sec}[c + d x])^{5/2} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\ \left( \left( 2 (68 a^2 A b + 60 A b^3 + 20 a^3 B + 180 a b^2 B + 180 a^2 b C) \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \right. \right. \\ \left. \left. \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right) / (\sqrt{b + a \operatorname{Cos}[c + d x]}) + \right. \\ \left( 2 (18 a^3 A + 46 a A b^2 + 70 a^2 b B + 60 b^3 B + 30 a^3 C + 135 a b^2 C) \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \right. \\ \left. \left. \operatorname{EllipticPi}\left[2, \frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right) / (\sqrt{b + a \operatorname{Cos}[c + d x]}) + \right.$$



$$\begin{aligned}
 & - \left( \left( 2 (15 A b^4 - 56 a^3 b B + 56 a b^3 B + 10 a^2 b^2 (A - 7 C) - 5 a^4 (5 A + 7 C)) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \right. \\
 & \quad \left. \left. \text{EllipticF} \left[ \frac{1}{2} (c + d x), \frac{2 a}{a + b} \right] \sqrt{\sec [c + d x]} \right) / \left( 105 a d \sqrt{a + b \sec [c + d x]} \right) \right) + \\
 & \frac{2 b^3 C \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \text{EllipticPi} \left[ 2, \frac{1}{2} (c + d x), \frac{2 a}{a + b} \right] \sqrt{\sec [c + d x]}}{d \sqrt{a + b \sec [c + d x]}} + \\
 & \left( 2 (15 A b^3 + 63 a^3 B + 161 a b^2 B + 5 a^2 b (29 A + 49 C)) \text{EllipticE} \left[ \frac{1}{2} (c + d x), \frac{2 a}{a + b} \right] \right. \\
 & \quad \left. \sqrt{a + b \sec [c + d x]} \right) / \left( 105 a d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \sqrt{\sec [c + d x]} \right) + \\
 & \frac{2 (15 A b^2 + 56 a b B + 5 a^2 (5 A + 7 C)) \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{105 d \sqrt{\sec [c + d x]}} + \\
 & \frac{2 (5 A b + 7 a B) (a + b \sec [c + d x])^{3/2} \sin [c + d x]}{35 d \sec [c + d x]^{3/2}} + \\
 & \frac{2 A (a + b \sec [c + d x])^{5/2} \sin [c + d x]}{7 d \sec [c + d x]^{5/2}}
 \end{aligned}$$

Result (type 8, 47 leaves):

$$\int \frac{(a + b \sec [c + d x])^{5/2} (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sec [c + d x]^{7/2}} dx$$

**Problem 1050: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + b \sec [c + d x])^{5/2} (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sec [c + d x]^{9/2}} dx$$

Optimal (type 4, 452 leaves, 11 steps):

$$\begin{aligned}
 & - \left( \left( 2 (a^2 - b^2) (10 A b^3 - 75 a^3 B - 45 a b^2 B - 6 a^2 b (19 A + 28 C)) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \right. \\
 & \quad \left. \left. \text{EllipticF} \left[ \frac{1}{2} (c + d x), \frac{2 a}{a + b} \right] \sqrt{\sec [c + d x]} \right) / (315 a^2 d \sqrt{a + b \sec [c + d x]}) \right) - \\
 & \left( 2 (10 A b^4 - 435 a^3 b B - 45 a b^3 B - 21 a^4 (7 A + 9 C) - 3 a^2 b^2 (93 A + 161 C)) \right. \\
 & \quad \left. \text{EllipticE} \left[ \frac{1}{2} (c + d x), \frac{2 a}{a + b} \right] \sqrt{a + b \sec [c + d x]} \right) / \\
 & \left( 315 a^2 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \sqrt{\sec [c + d x]} \right) + \\
 & \frac{2 (15 A b^2 + 90 a b B + 7 a^2 (7 A + 9 C)) \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{315 d \sec [c + d x]^{3/2}} + \\
 & \left( 2 (5 A b^3 + 75 a^3 B + 135 a b^2 B + a^2 b (163 A + 231 C)) \sqrt{a + b \sec [c + d x]} \sin [c + d x] \right) / \\
 & \left( 315 a d \sqrt{\sec [c + d x]} \right) + \\
 & \frac{2 (5 A b + 9 a B) (a + b \sec [c + d x])^{3/2} \sin [c + d x]}{63 d \sec [c + d x]^{5/2}} + \frac{2 A (a + b \sec [c + d x])^{5/2} \sin [c + d x]}{9 d \sec [c + d x]^{7/2}}
 \end{aligned}$$

Result (type 6, 6410 leaves):

$$\begin{aligned}
 & \left( (a + b \sec [c + d x])^{5/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left( - \frac{1}{315 a^2 d} 4 (147 a^4 A + 279 a^2 A b^2 - 10 A b^4 + 435 a^3 b B + 45 a b^3 B + 189 a^4 C + 483 a^2 b^2 C) \cot [c] + \right. \\
 & \quad \frac{1}{315 a d} (747 a^2 A b + 20 A b^3 + 345 a^3 B + 540 a b^2 B + 924 a^2 b C) \cos [d x] \sin [c] + \\
 & \quad \frac{(133 a^2 A + 150 A b^2 + 270 a b B + 126 a^2 C) \cos [2 d x] \sin [2 c]}{315 d} + \\
 & \quad \frac{a (19 A b + 9 a B) \cos [3 d x] \sin [3 c]}{63 d} + \frac{a^2 A \cos [4 d x] \sin [4 c]}{18 d} + \frac{1}{315 a d} \\
 & \quad (747 a^2 A b + 20 A b^3 + 345 a^3 B + 540 a b^2 B + 924 a^2 b C) \cos [c] \sin [d x] + \\
 & \quad \left. \frac{(133 a^2 A + 150 A b^2 + 270 a b B + 126 a^2 C) \cos [2 c] \sin [2 d x]}{315 d} \right) / \\
 & \left( (b + a \cos [c + d x])^2 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sec [c + d x]^{9/2} \right) - \\
 & \left( 116 a b \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c]}{a \sqrt{1 + \cot [c]^2}} \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x] - \text{ArcTan} [\cot [c]] \right) \right] \right) / \\
 & \quad a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)
 \end{aligned}$$



$$\begin{aligned}
 & \left. \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( -1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \right] \text{Csc}[c] \\
 & (a + b \text{Sec}[c + dx])^{5/2} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \\
 & \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} - b \text{Csc}[c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} + a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} + b \text{Csc}[c]}} \\
 & \left. \sqrt{b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right) / \\
 & \left( 35 d (b + a \text{Cos}[c + dx])^{5/2} (A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2c + 2dx]) \right. \\
 & \left. \sqrt{1 + \text{Cot}[c]^2} \text{Sec}[c + dx]^{9/2} \right) - \\
 & \left( 124 A b^3 \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( 1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \right], \right. \\
 & \left. \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( -1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \right] \text{Csc}[c] \\
 & (a + b \text{Sec}[c + dx])^{5/2} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \\
 & \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} - b \text{Csc}[c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} + a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} + b \text{Csc}[c]}} \\
 & \left. \sqrt{b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( 63 a d (b + a \cos [c + d x])^{5/2} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. \sqrt{1 + \cot [c]^2} \sec [c + d x]^{9/2} \right) - \\
 & \left( 20 a^2 B \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right. \\
 & \quad \left. \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( -1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right] \csc [c] \\
 & (a + b \sec [c + d x])^{5/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \sec [d x - \operatorname{ArcTan} [\cot [c]]] \\
 & \sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \operatorname{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \operatorname{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}} \\
 & \left. \sqrt{b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]]} \right) / \\
 & \left( 21 d (b + a \cos [c + d x])^{5/2} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. \sqrt{1 + \cot [c]^2} \sec [c + d x]^{9/2} \right) - \\
 & \left( 36 b^2 B \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right. \\
 & \quad \left. \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( -1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right] \csc [c] \\
 & (a + b \sec [c + d x])^{5/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \sec [d x - \operatorname{ArcTan} [\cot [c]]] \\
 & \sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \operatorname{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}}
 \end{aligned}$$

$$\left( \frac{\sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}}}{\sqrt{b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]]}} \right) /$$

$$\left( 7 d (b + a \cos [c + d x])^{5/2} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} \sec [c + d x]^{9/2} \right) -$$

$$\left( 68 a b C \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right.$$

$$\left. \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( -1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right] \csc [c]$$

$$(a + b \sec [c + d x])^{5/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \sec [d x - \text{ArcTan} [\cot [c]]]$$

$$\left( \frac{\sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}}}{\sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}}} \right) /$$

$$\left( 15 d (b + a \cos [c + d x])^{5/2} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} \sec [c + d x]^{9/2} \right) -$$

$$\left( 4 b^3 C \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right.$$

$$\frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( -1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \text{Csc}[c]$$

$$(a + b \text{Sec}[c + dx])^{5/2} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]]$$

$$\sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} - b \text{Csc}[c]}}$$

$$\sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} + a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} + b \text{Csc}[c]}}$$

$$\left. \sqrt{b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right/$$

$$\left( a d (b + a \text{Cos}[c + dx])^{5/2} (A + 2C + 2B \text{Cos}[c + dx] + A \text{Cos}[2c + 2dx]) \right.$$

$$\left. \sqrt{1 + \text{Cot}[c]^2} \text{Sec}[c + dx]^{9/2} \right) -$$

$$\left( 14 a^3 A \text{Csc}[c] (a + b \text{Sec}[c + dx])^{5/2} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \right.$$

$$\left( \left( \text{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, -\left( \text{Sec}[c] (b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]) \right. \right. \right. \right.$$

$$\left. \left. \left. \sqrt{1 + \text{Tan}[c]^2} \right) \right) \right) / \left( a \sqrt{1 + \text{Tan}[c]^2} \left( 1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right),$$

$$- \left( \left( \text{Sec}[c] (b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]) \sqrt{1 + \text{Tan}[c]^2} \right) \right) /$$

$$\left( a \sqrt{1 + \text{Tan}[c]^2} \left( -1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] \left. \right/$$

$$\left( \sqrt{1 + \text{Tan}[c]^2} \sqrt{\left( (a \sqrt{1 + \text{Tan}[c]^2} - a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]) \sqrt{1 + \text{Tan}[c]^2} \right) \right) /$$

$$\left( b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \sqrt{\left( (a \sqrt{1 + \text{Tan}[c]^2} + \right.$$

$$\left. a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]) \sqrt{1 + \text{Tan}[c]^2} \right) / \left( -b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right)$$

$$\begin{aligned}
 & \left. \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}} \right) - \\
 & \left( \frac{\sin [d x + \text{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \left( 2 a \cos [c] \left( b + a \cos [c] \cos [ \right. \right. \right. \\
 & \quad \left. \left. \left. d x + \text{ArcTan}[\tan [c]] \right] \sqrt{1 + \tan [c]^2} \right) \right) / \left( a^2 \cos [c]^2 + a^2 \sin [c]^2 \right) \right) / \\
 & \left( \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}} \right) \Bigg) / \\
 & \left( 15 d (b + a \cos [c + d x])^{5/2} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sec [c + d x]^{9/2} \right) - \\
 & \left( 62 a A b^2 \csc [c] (a + b \sec [c + d x])^{5/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \left. \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \sec [c] \left( b + a \cos [c] \cos [d x + \text{ArcTan}[\tan [c]] \right] \right. \right. \right. \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \tan [c]^2} \right) \right) \right) / \left( a \sqrt{1 + \tan [c]^2} \left( 1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right) \Bigg), \\
 & - \left( \left( \sec [c] \left( b + a \cos [c] \cos [d x + \text{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2} \right) \right) \right) / \\
 & \left( a \sqrt{1 + \tan [c]^2} \left( -1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \Bigg) \sin [d x + \text{ArcTan}[\tan [c]]] \tan [c] \Bigg) / \\
 & \left( \sqrt{1 + \tan [c]^2} \sqrt{\left( \left( a \sqrt{1 + \tan [c]^2} - a \cos [d x + \text{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2} \right) \right. \right. \\
 & \quad \left. \left. \left( b \sec [c] + a \sqrt{1 + \tan [c]^2} \right) \right) \sqrt{\left( \left( a \sqrt{1 + \tan [c]^2} + \right. \right. \right. \\
 & \quad \left. \left. \left. a \cos [d x + \text{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2} \right) \right) / \left( -b \sec [c] + a \sqrt{1 + \tan [c]^2} \right) \right) \right) \\
 & \left. \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}} \right) - \\
 & \left( \frac{\sin [d x + \text{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \left( 2 a \cos [c] \left( b + a \cos [c] \cos [ \right. \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & \left( 58 a^2 b B \operatorname{Csc}[c] (a + b \operatorname{Sec}[c + d x])^{5/2} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \left( \left( \operatorname{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, -\left(\operatorname{Sec}[c] (b + a \operatorname{Cos}[c] \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]])]\right)\right.\right. \right. \\
 & \left. \left. \left. \sqrt{1 + \operatorname{Tan}[c]^2}\right)\right) / \left(a \sqrt{1 + \operatorname{Tan}[c]^2} \left(1 - \frac{b \operatorname{Sec}[c]}{a \sqrt{1 + \operatorname{Tan}[c]^2}}\right)\right) \right), \\
 & - \left( \left( \operatorname{Sec}[c] (b + a \operatorname{Cos}[c] \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]])] \sqrt{1 + \operatorname{Tan}[c]^2} \right) / \right. \\
 & \left. \left( a \sqrt{1 + \operatorname{Tan}[c]^2} \left(-1 - \frac{b \operatorname{Sec}[c]}{a \sqrt{1 + \operatorname{Tan}[c]^2}}\right) \right) \right) \operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] \Big/ \\
 & \left( \sqrt{1 + \operatorname{Tan}[c]^2} \sqrt{\left(\left(a \sqrt{1 + \operatorname{Tan}[c]^2} - a \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]\right] \sqrt{1 + \operatorname{Tan}[c]^2}\right) / \right. \\
 & \left. \left(b \operatorname{Sec}[c] + a \sqrt{1 + \operatorname{Tan}[c]^2}\right) \sqrt{\left(\left(a \sqrt{1 + \operatorname{Tan}[c]^2} + \right.\right.} \right. \\
 & \left. \left. a \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]\right] \sqrt{1 + \operatorname{Tan}[c]^2}\right) / \left(-b \operatorname{Sec}[c] + a \sqrt{1 + \operatorname{Tan}[c]^2}\right) \right) \\
 & \left. \sqrt{b + a \operatorname{Cos}[c] \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}} \right) - \\
 & \left( \frac{\operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1 + \operatorname{Tan}[c]^2}} + \left( 2 a \operatorname{Cos}[c] (b + a \operatorname{Cos}[c] \operatorname{Cos}[ \right. \right. \\
 & \left. \left. d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]\right] \sqrt{1 + \operatorname{Tan}[c]^2} \right) / (a^2 \operatorname{Cos}[c]^2 + a^2 \operatorname{Sin}[c]^2) \Big/ \\
 & \left. \left( \sqrt{b + a \operatorname{Cos}[c] \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}} \right) \right) \Big/ \\
 & \left( 21 d (b + a \operatorname{Cos}[c + d x])^{5/2} (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \right. \\
 & \left. \operatorname{Sec}[c + d x]^{9/2} \right) - \\
 & \left( 2 b^3 B \operatorname{Csc}[c] (a + b \operatorname{Sec}[c + d x])^{5/2} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \left( \left( \operatorname{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, -\left(\operatorname{Sec}[c] (b + a \operatorname{Cos}[c] \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]])]\right)\right.\right. \right.
 \end{aligned}$$





$$\begin{aligned}
 & \left( a \sqrt{1 + \tan^2[c]} \left( -1 - \frac{b \sec[c]}{a \sqrt{1 + \tan^2[c]}} \right) \right) \left( \sin[dx + \arctan[\tan[c]]] \tan[c] \right) / \\
 & \left( \sqrt{1 + \tan^2[c]} \sqrt{\left( \left( a \sqrt{1 + \tan^2[c]} - a \cos[dx + \arctan[\tan[c]]] \right) \sqrt{1 + \tan^2[c]} \right)} / \right. \\
 & \left. \left( b \sec[c] + a \sqrt{1 + \tan^2[c]} \right) \sqrt{\left( \left( a \sqrt{1 + \tan^2[c]} + \right. \right. \right. \\
 & \left. \left. \left. a \cos[dx + \arctan[\tan[c]]] \right) \sqrt{1 + \tan^2[c]} \right)} / \left( -b \sec[c] + a \sqrt{1 + \tan^2[c]} \right) \right) \\
 & \left. \sqrt{b + a \cos[c] \cos[dx + \arctan[\tan[c]]] \sqrt{1 + \tan^2[c]}} \right) - \\
 & \left( \frac{\sin[dx + \arctan[\tan[c]]] \tan[c]}{\sqrt{1 + \tan^2[c]}} + \left( 2 a \cos[c] \left( b + a \cos[c] \cos[ \right. \right. \right. \\
 & \left. \left. \left. dx + \arctan[\tan[c]] \right] \sqrt{1 + \tan^2[c]} \right) \right) / \left( a^2 \cos^2[c] + a^2 \sin^2[c] \right) \right) / \\
 & \left( \sqrt{b + a \cos[c] \cos[dx + \arctan[\tan[c]]] \sqrt{1 + \tan^2[c]}} \right) \left. \right) / \\
 & \left( 5 d \left( b + a \cos[c + dx] \right)^{5/2} \left( A + 2 C + 2 B \cos[c + dx] + A \cos[2c + 2dx] \right) \right. \\
 & \left. \sec[c + dx]^{9/2} \right) - \\
 & \left( 46 a b^2 C \csc[c] \left( a + b \sec[c + dx] \right)^{5/2} \left( A + B \sec[c + dx] + C \sec[c + dx]^2 \right) \right. \\
 & \left. \left( \left( \operatorname{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \sec[c] \left( b + a \cos[c] \cos[dx + \arctan[\tan[c]]] \right) \right) \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \sqrt{1 + \tan^2[c]} \right) \right) \right) / \left( a \sqrt{1 + \tan^2[c]} \left( 1 - \frac{b \sec[c]}{a \sqrt{1 + \tan^2[c]}} \right) \right) \right) \left. \right), \\
 & - \left( \left( \sec[c] \left( b + a \cos[c] \cos[dx + \arctan[\tan[c]]] \right) \sqrt{1 + \tan^2[c]} \right) \right) / \\
 & \left( a \sqrt{1 + \tan^2[c]} \left( -1 - \frac{b \sec[c]}{a \sqrt{1 + \tan^2[c]}} \right) \right) \left( \sin[dx + \arctan[\tan[c]]] \tan[c] \right) / \\
 & \left( \sqrt{1 + \tan^2[c]} \sqrt{\left( \left( a \sqrt{1 + \tan^2[c]} - a \cos[dx + \arctan[\tan[c]]] \right) \sqrt{1 + \tan^2[c]} \right)} / \right.
 \end{aligned}$$

$$\left( \left( b \operatorname{Sec}[c] + a \sqrt{1 + \operatorname{Tan}[c]^2} \right) \sqrt{\left( \left( a \sqrt{1 + \operatorname{Tan}[c]^2} + a \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2} \right) / \left( -b \operatorname{Sec}[c] + a \sqrt{1 + \operatorname{Tan}[c]^2} \right) \right)} - \sqrt{b + a \operatorname{Cos}[c] \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}} \right) - \left( \frac{\operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1 + \operatorname{Tan}[c]^2}} + \left( 2 a \operatorname{Cos}[c] \left( b + a \operatorname{Cos}[c] \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2} \right) / \left( a^2 \operatorname{Cos}[c]^2 + a^2 \operatorname{Sin}[c]^2 \right) \right) \right) / \left( \sqrt{b + a \operatorname{Cos}[c] \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}} \right) \right) / \left( 15 d \left( b + a \operatorname{Cos}[c + d x] \right)^{5/2} \left( A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x] \right) \operatorname{Sec}[c + d x]^{9/2} \right)$$

**Problem 1051: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + b \operatorname{Sec}[c + d x])^{5/2} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[c + d x]^{11/2}} dx$$

Optimal (type 4, 565 leaves, 12 steps):

$$\begin{aligned}
 & \left( 2 (a^2 - b^2) (40 A b^4 + 1254 a^3 b B - 110 a b^3 B + 75 a^4 (9 A + 11 C) + 15 a^2 b^2 (19 A + 33 C)) \right. \\
 & \quad \left. \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{\sec [c + d x]} \right) / \\
 & \quad (3465 a^3 d \sqrt{a + b \sec [c + d x]}) + \\
 & \quad \left( 2 (40 A b^5 + 1617 a^5 B + 3069 a^3 b^2 B - 110 a b^4 B + 15 a^2 b^3 (17 A + 33 C) + 15 a^4 b (247 A + 319 C)) \right. \\
 & \quad \left. \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \sec [c + d x]} \right) / \\
 & \quad \left( 3465 a^3 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \sqrt{\sec [c + d x]} \right) + \\
 & \quad \frac{2 (5 A b^2 + 44 a b B + 3 a^2 (9 A + 11 C)) \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{231 d \sec [c + d x]^{5/2}} + \\
 & \quad \left( 2 (15 A b^3 + 539 a^3 B + 825 a b^2 B + 5 a^2 b (229 A + 297 C)) \sqrt{a + b \sec [c + d x]} \sin [c + d x] \right) / \\
 & \quad (3465 a d \sec [c + d x]^{3/2}) - \\
 & \quad \left( 2 (20 A b^4 - 1793 a^3 b B - 55 a b^3 B - 75 a^4 (9 A + 11 C) - 5 a^2 b^2 (205 A + 297 C)) \right. \\
 & \quad \left. \sqrt{a + b \sec [c + d x]} \sin [c + d x] \right) / (3465 a^2 d \sqrt{\sec [c + d x]}) + \\
 & \quad \frac{2 (5 A b + 11 a B) (a + b \sec [c + d x])^{3/2} \sin [c + d x]}{99 d \sec [c + d x]^{7/2}} + \frac{2 A (a + b \sec [c + d x])^{5/2} \sin [c + d x]}{11 d \sec [c + d x]^{9/2}}
 \end{aligned}$$

Result (type 6, 7479 leaves):

$$\begin{aligned}
 & \left( (a + b \sec [c + d x])^{5/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left( -\frac{1}{3465 a^3 d} (3705 a^4 A b + 255 a^2 A b^3 + 40 A b^5 + 1617 a^5 B + \right. \\
 & \quad \quad 3069 a^3 b^2 B - 110 a b^4 B + 4785 a^4 b C + 495 a^2 b^3 C) \cot [c] + \frac{1}{6930 a^2 d} \\
 & \quad (6525 a^4 A + 9330 a^2 A b^2 - 160 A b^4 + 16434 a^3 b B + 440 a b^3 B + 7590 a^4 C + 11880 a^2 b^2 C) \\
 & \quad \cos [d x] \sin [c] + \frac{1}{3465 a d} (3095 a^2 A b + 30 A b^3 + 1463 a^3 B + 1650 a b^2 B + 2970 a^2 b C) \\
 & \quad \cos [2 d x] \sin [2 c] + \frac{(513 a^2 A + 452 A b^2 + 836 a b B + 396 a^2 C) \cos [3 d x] \sin [3 c]}{2772 d} + \\
 & \quad \frac{a (23 A b + 11 a B) \cos [4 d x] \sin [4 c]}{198 d} + \frac{a^2 A \cos [5 d x] \sin [5 c]}{44 d} + \frac{1}{6930 a^2 d} \\
 & \quad (6525 a^4 A + 9330 a^2 A b^2 - 160 A b^4 + 16434 a^3 b B + 440 a b^3 B + 7590 a^4 C + 11880 a^2 b^2 C) \\
 & \quad \cos [c] \sin [d x] + \frac{1}{3465 a d} (3095 a^2 A b + 30 A b^3 + 1463 a^3 B + 1650 a b^2 B + 2970 a^2 b C) \\
 & \quad \left. \left. \cos [2 c] \sin [2 d x] + \frac{(513 a^2 A + 452 A b^2 + 836 a b B + 396 a^2 C) \cos [3 c] \sin [3 d x]}{2772 d} \right) \right)
 \end{aligned}$$

$$\left( \frac{a (23 A b + 11 a B) \cos [4 c] \sin [4 d x]}{198 d} + \frac{a^2 A \cos [5 c] \sin [5 d x]}{44 d} \right) /$$

$$\left( (b + a \cos [c + d x])^2 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sec [c + d x]^{9/2} \right) -$$

$$\left( 60 a^2 A \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right.$$

$$\left. \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( -1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right] \csc [c]$$

$$(a + b \sec [c + d x])^{5/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \sec [d x - \operatorname{ArcTan} [\cot [c]]]$$

$$\sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \operatorname{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}}$$

$$\sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \operatorname{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}}$$

$$\left. \sqrt{b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]]} \right) /$$

$$\left( 77 d (b + a \cos [c + d x])^{5/2} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right.$$

$$\left. \sqrt{1 + \cot [c]^2} \sec [c + d x]^{9/2} \right) -$$

$$\left( 884 A b^2 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right.$$

$$\left. \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( -1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right] \csc [c]$$

$$(a + b \sec [c + d x])^{5/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \sec [d x - \operatorname{ArcTan} [\cot [c]]]$$

$$\sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \operatorname{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}}$$

$$\left( \frac{\sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}}}{\sqrt{b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]]}} \right) /$$

$$\left( 231 d (b + a \cos [c + d x])^{5/2} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} \sec [c + d x]^{9/2} \right) -$$

$$\left( 8 A b^4 \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] (b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]])}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right.$$

$$\left. \frac{\csc [c] (b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]])}{a \sqrt{1 + \cot [c]^2} \left( -1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right] \csc [c]$$

$$(a + b \sec [c + d x])^{5/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \sec [d x - \text{ArcTan} [\cot [c]]]$$

$$\left( \frac{\sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}}}{\sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}}} \right) /$$

$$\left( 693 a^2 d (b + a \cos [c + d x])^{5/2} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} \sec [c + d x]^{9/2} \right) -$$

$$\left( 116 a b B \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] (b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]])}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right.$$

$$\begin{aligned}
 & \left. \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( -1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \right] \text{Csc}[c] \\
 & (a + b \text{Sec}[c + dx])^{5/2} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \\
 & \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} - b \text{Csc}[c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} + a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} + b \text{Csc}[c]}} \\
 & \left. \sqrt{b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right) / \\
 & \left( 35 d (b + a \text{Cos}[c + dx])^{5/2} (A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2c + 2dx]) \right. \\
 & \left. \sqrt{1 + \text{Cot}[c]^2} \text{Sec}[c + dx]^{9/2} \right) - \\
 & \left( 124 b^3 B \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( 1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \right], \right. \\
 & \left. \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( -1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \right] \text{Csc}[c] \\
 & (a + b \text{Sec}[c + dx])^{5/2} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \\
 & \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} - b \text{Csc}[c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} + a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} + b \text{Csc}[c]}} \\
 & \left. \sqrt{b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( 63 a d (b + a \cos [c + d x])^{5/2} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. \sqrt{1 + \cot [c]^2} \sec [c + d x]^{9/2} \right) - \\
 & \left( 20 a^2 C \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right. \\
 & \quad \left. \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( -1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right] \csc [c] \\
 & (a + b \sec [c + d x])^{5/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \sec [d x - \operatorname{ArcTan} [\cot [c]]] \\
 & \sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \operatorname{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \operatorname{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}} \\
 & \left. \sqrt{b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]]} \right) / \\
 & \left( 21 d (b + a \cos [c + d x])^{5/2} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. \sqrt{1 + \cot [c]^2} \sec [c + d x]^{9/2} \right) - \\
 & \left( 36 b^2 C \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right. \\
 & \quad \left. \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( -1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right] \csc [c] \\
 & (a + b \sec [c + d x])^{5/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \sec [d x - \operatorname{ArcTan} [\cot [c]]] \\
 & \sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \operatorname{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}}
 \end{aligned}$$

$$\left( \frac{\sqrt{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}}{a \sqrt{1 + \cot [c]^2} + b \csc [c]} \right. \\ \left. \sqrt{b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]]} \right) / \\ \left( 7 d (b + a \cos [c + d x])^{5/2} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\ \left. \sqrt{1 + \cot [c]^2} \sec [c + d x]^{9/2} \right) - \\ \left( 494 a^2 A b \csc [c] (a + b \sec [c + d x])^{5/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\ \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \sec [c] (b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]) \right) \right. \right. \right. \\ \left. \left. \left. \sqrt{1 + \tan [c]^2} \right) \right] \right) / \left( a \sqrt{1 + \tan [c]^2} \left( 1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right) \\ - \left( \left( \sec [c] (b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) \right) / \\ \left( a \sqrt{1 + \tan [c]^2} \left( -1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right) \sin [d x + \text{ArcTan} [\tan [c]]] \tan [c] \left. \right) / \\ \left( \sqrt{1 + \tan [c]^2} \sqrt{\left( (a \sqrt{1 + \tan [c]^2} - a \cos [d x + \text{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) / \right. \\ \left. (b \sec [c] + a \sqrt{1 + \tan [c]^2}) \right) \sqrt{\left( (a \sqrt{1 + \tan [c]^2} + \right. \\ \left. a \cos [d x + \text{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) / (-b \sec [c] + a \sqrt{1 + \tan [c]^2}) \right) \\ \left. \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2}} \right) - \\ \left( \frac{\sin [d x + \text{ArcTan} [\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \left( 2 a \cos [c] (b + a \cos [c] \cos [ \right. \right. \\ \left. \left. d x + \text{ArcTan} [\tan [c]] \right) \sqrt{1 + \tan [c]^2} \right) / (a^2 \cos [c]^2 + a^2 \sin [c]^2) \right) /$$



$$\begin{aligned}
 & \left( \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]]} \sqrt{1 + \tan [c]^2} \right) \Bigg) \Bigg) \Bigg) / \\
 & \left( 231 d (b + a \cos [c + d x])^{5/2} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sec [c + d x]^{9/2} \right) - \\
 & \left( 34 A b^3 \csc [c] (a + b \sec [c + d x])^{5/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \left. \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, -\left( \sec [c] (b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]) \right) \right. \right. \right. \right. \\
 & \left. \left. \left. \sqrt{1 + \tan [c]^2} \right) \right) \right) / \left( a \sqrt{1 + \tan [c]^2} \left( 1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right) \Bigg) \Bigg) \Bigg) / \\
 & - \left( \left( \sec [c] (b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) \right) \Bigg) \Bigg) / \\
 & \left( a \sqrt{1 + \tan [c]^2} \left( -1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \Bigg) \Bigg) \left[ \sin [d x + \text{ArcTan} [\tan [c]]] \tan [c] \right] \Bigg) \Bigg) / \\
 & \left( \sqrt{1 + \tan [c]^2} \sqrt{\left( \left( a \sqrt{1 + \tan [c]^2} - a \cos [d x + \text{ArcTan} [\tan [c]]] \right) \sqrt{1 + \tan [c]^2} \right) \right) \Bigg) \Bigg) / \\
 & \left( b \sec [c] + a \sqrt{1 + \tan [c]^2} \right) \sqrt{\left( \left( a \sqrt{1 + \tan [c]^2} + \right. \right. \\
 & \left. \left. a \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2} \right) \right) \Bigg) \Bigg) / \left( -b \sec [c] + a \sqrt{1 + \tan [c]^2} \right) \Bigg) \\
 & \left. \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]]} \sqrt{1 + \tan [c]^2} \right) \Bigg) - \\
 & \left( \frac{\sin [d x + \text{ArcTan} [\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \left( 2 a \cos [c] (b + a \cos [c] \cos [ \right. \right. \\
 & \left. \left. d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2} \right) \right) \Bigg) \Bigg) / \left( a^2 \cos [c]^2 + a^2 \sin [c]^2 \right) \Bigg) \Bigg) / \\
 & \left( \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]]} \sqrt{1 + \tan [c]^2} \right) \Bigg) \Bigg) \Bigg) \Bigg) / \\
 & \left( 231 d (b + a \cos [c + d x])^{5/2} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sec [c + d x]^{9/2} \right) - \\
 & \left( 16 A b^5 \csc [c] (a + b \sec [c + d x])^{5/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \right] \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \text{Tan}[c]^2} \right) \right) \right) / \left( a \sqrt{1 + \text{Tan}[c]^2} \left( 1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right), \\
 & - \left( \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \right] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \\
 & \quad \left( a \sqrt{1 + \text{Tan}[c]^2} \left( -1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] \Big) / \\
 & \left( \sqrt{1 + \text{Tan}[c]^2} \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} - a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \sqrt{1 + \text{Tan}[c]^2} \right) \right.} \\
 & \quad \left. \left( b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} + \right. \right.} \\
 & \quad \left. \left. a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \sqrt{1 + \text{Tan}[c]^2} \right) / \left( -b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \Big)} \\
 & \quad \left. \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) - \\
 & \left( \frac{\text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \left( 2 a \text{Cos}[c] \left( b + a \text{Cos}[c] \text{Cos}[ \right. \right. \right. \\
 & \quad \left. \left. \left. dx + \text{ArcTan}[\text{Tan}[c]] \right) \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a^2 \text{Cos}[c]^2 + a^2 \text{Sin}[c]^2 \right) \Big) / \\
 & \quad \left( \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \Big) \Big) / \\
 & \left( 693 a^2 d (b + a \text{Cos}[c + dx])^{5/2} (A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2 c + 2 dx]) \right. \\
 & \quad \left. \text{Sec}[c + dx]^{9/2} \right) - \\
 & \left( 14 a^3 B \text{Csc}[c] (a + b \text{Sec}[c + dx])^{5/2} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \right. \\
 & \quad \left. \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \right) \right] \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \text{Tan}[c]^2} \right) \right) \right) / \left( a \sqrt{1 + \text{Tan}[c]^2} \left( 1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \Big)
 \end{aligned}$$

$$\begin{aligned}
 & - \left( \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \right. \\
 & \quad \left. \left( a \sqrt{1 + \text{Tan}[c]^2} \left( -1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] / \\
 & \left( \sqrt{1 + \text{Tan}[c]^2} \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} - a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) / \right. \right. \\
 & \quad \left. \left( b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} + \right. \right. \\
 & \quad \left. \left. a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) / \left( -b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) } \\
 & \quad \left. \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) - \\
 & \left( \frac{\text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \left( 2 a \text{Cos}[c] \left( b + a \text{Cos}[c] \text{Cos}[ \right. \right. \right. \\
 & \quad \left. \left. \left. dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a^2 \text{Cos}[c]^2 + a^2 \text{Sin}[c]^2 \right) \right) / \\
 & \left( \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) / \\
 & \left( 15 d (b + a \text{Cos}[c + dx])^{5/2} (A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2 c + 2 dx]) \right. \\
 & \quad \left. \text{Sec}[c + dx]^{9/2} \right) - \\
 & \left( 62 a b^2 B \text{Csc}[c] (a + b \text{Sec}[c + dx])^{5/2} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \right. \\
 & \quad \left( \left( \text{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, -\left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \right) \right) \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a \sqrt{1 + \text{Tan}[c]^2} \left( 1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \right), \\
 & - \left( \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \right. \\
 & \quad \left. \left( a \sqrt{1 + \text{Tan}[c]^2} \left( -1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] /
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{1 + \tan[c]^2} \sqrt{\left( (a \sqrt{1 + \tan[c]^2} - a \cos[d x + \text{ArcTan}[\tan[c]]) \sqrt{1 + \tan[c]^2} \right) / \right.} \\
 & \quad \left. \left( b \sec[c] + a \sqrt{1 + \tan[c]^2} \right) \sqrt{\left( (a \sqrt{1 + \tan[c]^2} + \right.} \right. \\
 & \quad \left. \left. a \cos[d x + \text{ArcTan}[\tan[c]]) \sqrt{1 + \tan[c]^2} \right) / \left( -b \sec[c] + a \sqrt{1 + \tan[c]^2} \right) \right) \\
 & \quad \left. \sqrt{b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]) \sqrt{1 + \tan[c]^2}} \right) - \\
 & \left( \frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \left( 2 a \cos[c] \left( b + a \cos[c] \cos \left[ \right. \right. \right. \right. \\
 & \quad \left. \left. \left. d x + \text{ArcTan}[\tan[c]] \right] \sqrt{1 + \tan[c]^2} \right) \right) / \left( a^2 \cos[c]^2 + a^2 \sin[c]^2 \right) \right) / \\
 & \left( \sqrt{b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]) \sqrt{1 + \tan[c]^2}} \right) / \\
 & \left( 35 d (b + a \cos[c + d x])^{5/2} (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) \right. \\
 & \quad \left. \sec[c + d x]^{9/2} \right) + \\
 & \left( 4 b^4 B \csc[c] (a + b \sec[c + d x])^{5/2} (A + B \sec[c + d x] + C \sec[c + d x]^2) \right. \\
 & \left. \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \sec[c] \left( b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]) \right) \right. \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \tan[c]^2} \right) \right) / \left( a \sqrt{1 + \tan[c]^2} \left( 1 - \frac{b \sec[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \right) \right), \\
 & - \left( \left( \sec[c] \left( b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]) \sqrt{1 + \tan[c]^2} \right) \right) / \right. \\
 & \quad \left. \left( a \sqrt{1 + \tan[c]^2} \left( -1 - \frac{b \sec[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \right) \sin[d x + \text{ArcTan}[\tan[c]]] \tan[c] \right) / \\
 & \left( \sqrt{1 + \tan[c]^2} \sqrt{\left( (a \sqrt{1 + \tan[c]^2} - a \cos[d x + \text{ArcTan}[\tan[c]]) \sqrt{1 + \tan[c]^2} \right) / \right.} \\
 & \quad \left. \left( b \sec[c] + a \sqrt{1 + \tan[c]^2} \right) \sqrt{\left( (a \sqrt{1 + \tan[c]^2} + \right.} \right. \\
 & \quad \left. \left. a \cos[d x + \text{ArcTan}[\tan[c]]) \sqrt{1 + \tan[c]^2} \right) / \left( -b \sec[c] + a \sqrt{1 + \tan[c]^2} \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \sqrt{b+a \cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}} \right) - \\
 & \left( \frac{\sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}} + \left( 2 a \cos [c] \left( b+a \cos [c] \cos [ \right. \right. \right. \\
 & \quad \left. \left. \left. d x+\operatorname{ArcTan}[\tan [c]] \right] \sqrt{1+\tan [c]^2} \right) \right) / \left( a^2 \cos [c]^2+a^2 \sin [c]^2 \right) \right) / \\
 & \left( \left( \sqrt{b+a \cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}} \right) \right) / \\
 & \left( 63 a d \left( b+a \cos [c+d x] \right)^{5 / 2} \left( A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x] \right) \right. \\
 & \quad \left. \sec [c+d x]^{9 / 2} \right) - \\
 & \left( 58 a^2 b C \csc [c] \left( a+b \sec [c+d x] \right)^{5 / 2} \left( A+B \sec [c+d x]+C \sec [c+d x]^2 \right) \right. \\
 & \quad \left( \left( \operatorname{AppellF1}\left[-\frac{1}{2},-\frac{1}{2},-\frac{1}{2}, \frac{1}{2},-\left( \sec [c] \left( b+a \cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]] \right) \right) \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1+\tan [c]^2} \right) \right) \right) / \left( a \sqrt{1+\tan [c]^2} \left( 1-\frac{b \sec [c]}{a \sqrt{1+\tan [c]^2}} \right) \right) \right) \right), \\
 & - \left( \left( \sec [c] \left( b+a \cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2} \right) \right) \right) / \\
 & \quad \left( a \sqrt{1+\tan [c]^2} \left( -1-\frac{b \sec [c]}{a \sqrt{1+\tan [c]^2}} \right) \right) \right) \sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c] \Big) / \\
 & \left( \sqrt{1+\tan [c]^2} \sqrt{\left( \left( a \sqrt{1+\tan [c]^2}-a \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2} \right) \right) / \right. \\
 & \quad \left. \left( b \sec [c]+a \sqrt{1+\tan [c]^2} \right) \right) \sqrt{\left( \left( a \sqrt{1+\tan [c]^2}+ \right. \right. \\
 & \quad \left. \left. a \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2} \right) \right) / \left( -b \sec [c]+a \sqrt{1+\tan [c]^2} \right) \right) \\
 & \left. \sqrt{b+a \cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}} \right) - \\
 & \left( \frac{\sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}} + \left( 2 a \cos [c] \left( b+a \cos [c] \cos [ \right. \right. \right.
 \end{aligned}$$



$$\text{Sec}[c + d x]^{9/2}$$

**Problem 1052: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\text{Sec}[c + d x]^{3/2} (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2)}{\sqrt{a + b \text{Sec}[c + d x]}} dx$$

Optimal (type 4, 350 leaves, 13 steps):

$$\frac{(4 b B - a C) \sqrt{\frac{b+a \text{Cos}[c+d x]}{a+b}} \text{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{\text{Sec}[c+d x]}}{4 b d \sqrt{a+b \text{Sec}[c+d x]}} +$$

$$\left( (8 A b^2 - 4 a b B + 3 a^2 C + 4 b^2 C) \sqrt{\frac{b+a \text{Cos}[c+d x]}{a+b}} \right.$$

$$\left. \text{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{\text{Sec}[c+d x]} \right) / (4 b^2 d \sqrt{a+b \text{Sec}[c+d x]}) -$$

$$\frac{(4 b B - 3 a C) \text{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \text{Sec}[c+d x]}}{4 b^2 d \sqrt{\frac{b+a \text{Cos}[c+d x]}{a+b}} \sqrt{\text{Sec}[c+d x]}} +$$

$$\frac{(4 b B - 3 a C) \sqrt{\text{Sec}[c+d x]} \sqrt{a+b \text{Sec}[c+d x]} \text{Sin}[c+d x]}{4 b^2 d} +$$

$$\frac{C \text{Sec}[c+d x]^{3/2} \sqrt{a+b \text{Sec}[c+d x]} \text{Sin}[c+d x]}{2 b d}$$

Result (type 4, 690 leaves):

$$\left( \sqrt{b+a \text{Cos}[c+d x]} (A + B \text{Sec}[c+d x] + C \text{Sec}[c+d x]^2) \right.$$

$$\left. \frac{8 a b C \sqrt{\frac{b+a \text{Cos}[c+d x]}{a+b}} \text{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{\sqrt{b+a \text{Cos}[c+d x]}} + \left( 2 (16 A b^2 - 12 a b B + 9 a^2 C + 8 b^2 C) \right. \right.$$

$$\left. \left. \sqrt{\frac{b+a \text{Cos}[c+d x]}{a+b}} \text{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \right) / (\sqrt{b+a \text{Cos}[c+d x]}) +$$

$$\left( 2 i (-4 a b B + 3 a^2 C) \sqrt{\frac{a - a \cos [c + d x]}{a + b}} \sqrt{\frac{a + a \cos [c + d x]}{a - b}} \cos [2 (c + d x)] \right. \\ \left( -2 b (a + b) \operatorname{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \sqrt{\frac{1}{a - b}} \sqrt{b + a \cos [c + d x]} \right], \frac{-a + b}{a + b} \right] + \right. \\ \left. a \left( 2 b \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \sqrt{\frac{1}{a - b}} \sqrt{b + a \cos [c + d x]} \right], \frac{-a + b}{a + b} \right] + \right. \right. \\ \left. \left. a \operatorname{EllipticPi} \left[ 1 - \frac{a}{b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{1}{a - b}} \sqrt{b + a \cos [c + d x]} \right], \frac{-a + b}{a + b} \right] \right) \right) \\ \sin [c + d x] \Bigg/ \left( \sqrt{\frac{1}{a - b}} b \sqrt{1 - \cos [c + d x]}^2 \sqrt{\frac{a^2 - a^2 \cos [c + d x]^2}{a^2}} \right. \\ \left. \left( -a^2 + 2 b^2 - 4 b (b + a \cos [c + d x]) + 2 (b + a \cos [c + d x])^2 \right) \right) \Bigg/ \\ \left( 8 b^2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sec [c + d x]^{3/2} \sqrt{a + b \sec [c + d x]} \right) + \\ \left( (b + a \cos [c + d x]) (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\ \left. \left( \frac{\sec [c + d x] (4 b B \sin [c + d x] - 3 a C \sin [c + d x])}{2 b^2} + \frac{C \sec [c + d x] \tan [c + d x]}{b} \right) \right) \Bigg/ \\ \left( d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sec [c + d x]^{3/2} \sqrt{a + b \sec [c + d x]} \right)$$

**Problem 1053: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sqrt{a + b \sec [c + d x]}} dx$$

Optimal (type 4, 260 leaves, 12 steps):



$$\begin{aligned}
 & \frac{(2A + C) \sqrt{\frac{b+a \cos[c+dx]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), \frac{2a}{a+b}\right] \sqrt{\sec[c+dx]}}{d \sqrt{a+b \sec[c+dx]}} + \\
 & \left( (2bB - aC) \sqrt{\frac{b+a \cos[c+dx]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+dx), \frac{2a}{a+b}\right] \sqrt{\sec[c+dx]} \right) / \\
 & (bd \sqrt{a+b \sec[c+dx]}) - \frac{C \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), \frac{2a}{a+b}\right] \sqrt{a+b \sec[c+dx]}}{bd \sqrt{\frac{b+a \cos[c+dx]}{a+b}} \sqrt{\sec[c+dx]}} + \\
 & \frac{C \sqrt{\sec[c+dx]} \sqrt{a+b \sec[c+dx]} \sin[c+dx]}{bd}
 \end{aligned}$$

Result(type 4, 623 leaves):



### Problem 1054: Unable to integrate problem.

$$\int \frac{A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2}{\sqrt{\operatorname{Sec}[c + d x]} \sqrt{a + b \operatorname{Sec}[c + d x]}} dx$$

Optimal (type 4, 219 leaves, 11 steps):

$$\begin{aligned} & - \left( \left( 2 (A b - a B) \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \sqrt{\operatorname{Sec}[c + d x]} \right) / \right. \\ & \left. \left( a d \sqrt{a + b \operatorname{Sec}[c + d x]} \right) \right) + \frac{2 C \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \sqrt{\operatorname{Sec}[c + d x]}}{d \sqrt{a + b \operatorname{Sec}[c + d x]}} + \\ & \frac{2 A \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \operatorname{Sec}[c + d x]}}{a d \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \sqrt{\operatorname{Sec}[c + d x]}} \end{aligned}$$

Result (type 8, 47 leaves):

$$\int \frac{A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2}{\sqrt{\operatorname{Sec}[c + d x]} \sqrt{a + b \operatorname{Sec}[c + d x]}} dx$$

### Problem 1055: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2}{\operatorname{Sec}[c + d x]^{3/2} \sqrt{a + b \operatorname{Sec}[c + d x]}} dx$$

Optimal (type 4, 216 leaves, 8 steps):

$$\begin{aligned} & \left( 2 (2 A b^2 - 3 a b B + a^2 (A + 3 C)) \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \right. \\ & \left. \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \sqrt{\operatorname{Sec}[c + d x]} \right) / \left( 3 a^2 d \sqrt{a + b \operatorname{Sec}[c + d x]} \right) - \\ & \frac{2 (2 A b - 3 a B) \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \operatorname{Sec}[c + d x]}}{3 a^2 d \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \sqrt{\operatorname{Sec}[c + d x]}} + \\ & \frac{2 A \sqrt{a + b \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{3 a d \sqrt{\operatorname{Sec}[c + d x]}} \end{aligned}$$

Result (type 6, 1959 leaves):

$$\begin{aligned}
 & \left( (b + a \cos [c + d x]) (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left. \left( -\frac{4(-2Ab + 3aB) \cot [c]}{3a^2 d} + \frac{4A \cos [dx] \sin [c]}{3ad} + \frac{4A \cos [c] \sin [dx]}{3ad} \right) \right) / \\
 & \left( (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sec [c + dx]^{3/2} \sqrt{a + b \sec [c + dx]} \right) - \\
 & \left( 4A \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [dx - \operatorname{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right. \\
 & \quad \left. \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [dx - \operatorname{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( -1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right] \sqrt{b + a \cos [c + dx]} \\
 & \quad \csc [c] (A + B \sec [c + dx] + C \sec [c + dx]^2) \sec [dx - \operatorname{ArcTan} [\cot [c]]] \\
 & \quad \sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [dx - \operatorname{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}} \\
 & \quad \sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [dx - \operatorname{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}} \\
 & \quad \left. \sqrt{b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [dx - \operatorname{ArcTan} [\cot [c]]]} \right) / \\
 & \left( 3ad (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sqrt{1 + \cot [c]^2} \right. \\
 & \quad \left. \sec [c + dx]^{3/2} \sqrt{a + b \sec [c + dx]} \right) - \\
 & \left( 4C \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [dx - \operatorname{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right. \\
 & \quad \left. \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [dx - \operatorname{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( -1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right] \sqrt{b + a \cos [c + dx]} \\
 & \quad \csc [c] (A + B \sec [c + dx] + C \sec [c + dx]^2) \sec [dx - \operatorname{ArcTan} [\cot [c]]]
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}} \\
 & \left. \sqrt{b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]]} \right) / \\
 & \left( a d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} \right. \\
 & \quad \left. \sec [c + d x]^{3/2} \sqrt{a + b \sec [c + d x]} \right) + \\
 & \left( 4 A b \sqrt{b + a \cos [c + d x]} \csc [c] (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left. \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \sec [c] (b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]) \right) \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \tan [c]^2} \right) \right) / \left( a \sqrt{1 + \tan [c]^2} \left( 1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right) \right), \\
 & \quad - \left( \left( \sec [c] (b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) \right) / \\
 & \quad \left( a \sqrt{1 + \tan [c]^2} \left( -1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right) \sin [d x + \text{ArcTan} [\tan [c]]] \tan [c] \Big) / \\
 & \left( \sqrt{1 + \tan [c]^2} \sqrt{\left( \left( a \sqrt{1 + \tan [c]^2} - a \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2} \right) \right) / \right. \\
 & \quad \left. \left( b \sec [c] + a \sqrt{1 + \tan [c]^2} \right) \right) \sqrt{\left( \left( a \sqrt{1 + \tan [c]^2} + \right. \right. \\
 & \quad \left. \left. a \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2} \right) \right) / \left( -b \sec [c] + a \sqrt{1 + \tan [c]^2} \right) \Big) \\
 & \quad \left. \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2}} \right) - \\
 & \left( \frac{\sin [d x + \text{ArcTan} [\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \left( 2 a \cos [c] (b + a \cos [c] \cos [c] \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left( dx + \text{ArcTan}[\text{Tan}[c]] \sqrt{1 + \text{Tan}[c]^2} \right) / (a^2 \text{Cos}[c]^2 + a^2 \text{Sin}[c]^2) \right) / \\
 & \left( \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) / \\
 & (3 a d (A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2 c + 2 dx]) \text{Sec}[c + dx]^{3/2} \sqrt{a + b \text{Sec}[c + dx]}) - \\
 & \left( 2 B \sqrt{b + a \text{Cos}[c + dx]} \text{Csc}[c] (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \right. \\
 & \left. \left( \left( \text{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, -\left(\text{Sec}[c] \left(b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]\right] \right. \right. \right. \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \left. \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a \sqrt{1 + \text{Tan}[c]^2} \left( 1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \right) \right), \\
 & - \left( \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \right. \\
 & \left. \left( a \sqrt{1 + \text{Tan}[c]^2} \left( -1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] \Big) / \\
 & \left( \sqrt{1 + \text{Tan}[c]^2} \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} - a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) / \right. \right. \\
 & \left. \left( b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} + \right. \right. \\
 & \left. \left. a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) / \left( -b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) } \\
 & \left. \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) - \\
 & \left( \frac{\text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + (2 a \text{Cos}[c] (b + a \text{Cos}[c] \text{Cos}[ \right. \\
 & \left. dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}) / (a^2 \text{Cos}[c]^2 + a^2 \text{Sin}[c]^2) \right) / \\
 & \left( \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) / \\
 & (d (A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2 c + 2 dx]) \text{Sec}[c + dx]^{3/2}
 \end{aligned}$$

$$\sqrt{a + b \operatorname{Sec}[c + d x]})$$

**Problem 1056: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2}{\operatorname{Sec}[c + d x]^{5/2} \sqrt{a + b \operatorname{Sec}[c + d x]}} dx$$

Optimal (type 4, 291 leaves, 9 steps):

$$\begin{aligned} & - \left( \left( 2 (8 A b^3 - 5 a^3 B - 10 a b^2 B + a^2 b (7 A + 15 C)) \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \right. \right. \\ & \quad \left. \left. \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \sqrt{\operatorname{Sec}[c + d x]} \right) / \left( 15 a^3 d \sqrt{a + b \operatorname{Sec}[c + d x]} \right) \right) + \\ & \left( 2 (8 A b^2 - 10 a b B + 3 a^2 (3 A + 5 C)) \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \operatorname{Sec}[c + d x]} \right) / \\ & \left( 15 a^3 d \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \sqrt{\operatorname{Sec}[c + d x]} \right) + \\ & \frac{2 A \sqrt{a + b \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{5 a d \operatorname{Sec}[c + d x]^{3/2}} - \frac{2 (4 A b - 5 a B) \sqrt{a + b \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{15 a^2 d \sqrt{\operatorname{Sec}[c + d x]}} \end{aligned}$$

Result (type 6, 3039 leaves):

$$\begin{aligned} & \left( (b + a \operatorname{Cos}[c + d x]) (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\ & \quad \left( - \frac{4 (9 a^2 A + 8 A b^2 - 10 a b B + 15 a^2 C) \operatorname{Cot}[c]}{15 a^3 d} + \frac{4 (-4 A b + 5 a B) \operatorname{Cos}[d x] \operatorname{Sin}[c]}{15 a^2 d} + \right. \\ & \quad \left. \frac{2 A \operatorname{Cos}[2 d x] \operatorname{Sin}[2 c]}{5 a d} + \frac{4 (-4 A b + 5 a B) \operatorname{Cos}[c] \operatorname{Sin}[d x]}{15 a^2 d} + \frac{2 A \operatorname{Cos}[2 c] \operatorname{Sin}[2 d x]}{5 a d} \right) \Big) / \\ & \left( (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \operatorname{Sec}[c + d x]^{3/2} \sqrt{a + b \operatorname{Sec}[c + d x]} \right) - \\ & \left( 8 A b \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\operatorname{Csc}[c] (b - a \sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]])]}{a \sqrt{1 + \operatorname{Cot}[c]^2} \left(1 + \frac{b \operatorname{Csc}[c]}{a \sqrt{1 + \operatorname{Cot}[c]^2}\right)}\right)} \right. \right. \\ & \quad \left. \left. \frac{\operatorname{Csc}[c] (b - a \sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]])]}{a \sqrt{1 + \operatorname{Cot}[c]^2} \left(-1 + \frac{b \operatorname{Csc}[c]}{a \sqrt{1 + \operatorname{Cot}[c]^2}\right)}\right)}{\sqrt{b + a \operatorname{Cos}[c + d x]}} \right) \right. \\ & \left. \operatorname{Csc}[c] (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \right) \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}} \\
 & \left. \sqrt{b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]]} \right) / \\
 & \left( 15 a^2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} \right. \\
 & \quad \left. \sec [c + d x]^{3/2} \sqrt{a + b \sec [c + d x]} \right) - \\
 & \left( 4 B \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] (b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]])}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right. \\
 & \quad \left. \frac{\csc [c] (b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]])}{a \sqrt{1 + \cot [c]^2} \left( -1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right] \sqrt{b + a \cos [c + d x]} \\
 & \csc [c] (A + B \sec [c + d x] + C \sec [c + d x]^2) \sec [d x - \text{ArcTan} [\cot [c]]] \\
 & \sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}} \\
 & \left. \sqrt{b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]]} \right) / \\
 & \left( 3 a d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} \right. \\
 & \quad \left. \sec [c + d x]^{3/2} \sqrt{a + b \sec [c + d x]} \right) - \\
 & \left( 6 A \sqrt{b + a \cos [c + d x]} \csc [c] (A + B \sec [c + d x] + C \sec [c + d x]^2) \right)
 \end{aligned}$$



$$\begin{aligned}
 & \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \right] \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \text{Tan}[c]^2} \right) \right) \right) / \left( a \sqrt{1 + \text{Tan}[c]^2} \left( 1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right), \\
 & - \left( \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \right] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \\
 & \quad \left( a \sqrt{1 + \text{Tan}[c]^2} \left( -1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] \Big) / \\
 & \left( \sqrt{1 + \text{Tan}[c]^2} \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} - a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \sqrt{1 + \text{Tan}[c]^2} \right) \right) /} \\
 & \quad \left( b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} + \right. \right. \\
 & \quad \left. \left. a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \sqrt{1 + \text{Tan}[c]^2} \right) / \left( -b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right)} \\
 & \quad \left. \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) - \\
 & \left( \frac{\text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \left( 2 a \text{Cos}[c] \left( b + a \text{Cos}[c] \text{Cos}[ \right. \right. \right. \\
 & \quad \left. \left. \left. dx + \text{ArcTan}[\text{Tan}[c]] \right) \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a^2 \text{Cos}[c]^2 + a^2 \text{Sin}[c]^2 \right) \Big) / \\
 & \quad \left( \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) \Big) / \\
 & \left( 5 d (A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2 c + 2 dx]) \text{Sec}[c + dx]^{3/2} \sqrt{a + b \text{Sec}[c + dx]} \right) - \\
 & \left( 16 A b^2 \sqrt{b + a \text{Cos}[c + dx]} \text{Csc}[c] (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \right) \\
 & \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \right) \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \text{Tan}[c]^2} \right) \right) \right) / \left( a \sqrt{1 + \text{Tan}[c]^2} \left( 1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right),
 \end{aligned}$$

$$\begin{aligned}
 & - \left( \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \right. \\
 & \quad \left. \left( a \sqrt{1 + \text{Tan}[c]^2} \left( -1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] / \\
 & \left( \sqrt{1 + \text{Tan}[c]^2} \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} - a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) / \right. \right. \\
 & \quad \left. \left( b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} + \right. \right. \\
 & \quad \left. \left. a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) / \left( -b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) } \\
 & \left. \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) - \\
 & \left( \frac{\text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \left( 2 a \text{Cos}[c] \left( b + a \text{Cos}[c] \text{Cos}[ \right. \right. \right. \\
 & \quad \left. \left. \left. dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a^2 \text{Cos}[c]^2 + a^2 \text{Sin}[c]^2 \right) \right) / \\
 & \left( \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) / \\
 & \left( 15 a^2 d \left( A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2 c + 2 dx] \right) \text{Sec}[c + dx]^{3/2} \right. \\
 & \quad \left. \sqrt{a + b \text{Sec}[c + dx]} \right) + \\
 & \left( 4 b B \sqrt{b + a \text{Cos}[c + dx]} \text{Csc}[c] \left( A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2 \right) \right. \\
 & \left. \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \right) \right) \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a \sqrt{1 + \text{Tan}[c]^2} \left( 1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \right), \\
 & - \left( \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \right. \\
 & \quad \left. \left( a \sqrt{1 + \text{Tan}[c]^2} \left( -1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] /
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{1 + \tan[c]^2} \sqrt{\left( (a \sqrt{1 + \tan[c]^2} - a \cos[d x + \text{ArcTan}[\tan[c]]) \sqrt{1 + \tan[c]^2} \right) / \right.} \\
 & \quad \left. \left( b \sec[c] + a \sqrt{1 + \tan[c]^2} \right) \sqrt{\left( (a \sqrt{1 + \tan[c]^2} + \right.} \right. \\
 & \quad \left. \left. a \cos[d x + \text{ArcTan}[\tan[c]]) \sqrt{1 + \tan[c]^2} \right) / \left( -b \sec[c] + a \sqrt{1 + \tan[c]^2} \right) \right) \\
 & \quad \left. \sqrt{b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]) \sqrt{1 + \tan[c]^2} \right) -} \\
 & \left( \frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \left( 2 a \cos[c] \left( b + a \cos[c] \cos \left[ \right. \right. \right. \right. \\
 & \quad \left. \left. \left. d x + \text{ArcTan}[\tan[c]] \right] \sqrt{1 + \tan[c]^2} \right) \right) / \left( a^2 \cos[c]^2 + a^2 \sin[c]^2 \right) \right) / \\
 & \left( \sqrt{b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]) \sqrt{1 + \tan[c]^2} \right) \right) / \\
 & \left( 3 a d \left( A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x] \right) \sec[c + d x]^{3/2} \right. \\
 & \quad \left. \sqrt{a + b \sec[c + d x]} \right) - \\
 & \left( 2 C \sqrt{b + a \cos[c + d x]} \csc[c] \left( A + B \sec[c + d x] + C \sec[c + d x]^2 \right) \right. \\
 & \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \sec[c] \left( b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]) \right) \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \tan[c]^2} \right) \right) / \left( a \sqrt{1 + \tan[c]^2} \left( 1 - \frac{b \sec[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \right) \right) , \\
 & - \left( \left( \sec[c] \left( b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]) \sqrt{1 + \tan[c]^2} \right) \right) / \right. \\
 & \quad \left. \left( a \sqrt{1 + \tan[c]^2} \left( -1 - \frac{b \sec[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \right) \sin[d x + \text{ArcTan}[\tan[c]]] \tan[c] \right) / \\
 & \left( \sqrt{1 + \tan[c]^2} \sqrt{\left( (a \sqrt{1 + \tan[c]^2} - a \cos[d x + \text{ArcTan}[\tan[c]]) \sqrt{1 + \tan[c]^2} \right) / \right.} \\
 & \quad \left. \left( b \sec[c] + a \sqrt{1 + \tan[c]^2} \right) \sqrt{\left( (a \sqrt{1 + \tan[c]^2} + \right.} \right. \\
 & \quad \left. \left. a \cos[d x + \text{ArcTan}[\tan[c]]) \sqrt{1 + \tan[c]^2} \right) / \left( -b \sec[c] + a \sqrt{1 + \tan[c]^2} \right) \right)
 \end{aligned}$$

$$\left( \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan}[\tan [c]]]} \sqrt{1 + \tan [c]^2} \right) - \left( \frac{\sin [d x + \text{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \left( 2 a \cos [c] \left( b + a \cos [c] \cos [d x + \text{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2} \right) \right) / \left( a^2 \cos [c]^2 + a^2 \sin [c]^2 \right) \right) / \left( \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan}[\tan [c]]]} \sqrt{1 + \tan [c]^2} \right) / \left( d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sec [c + d x]^{3/2} \sqrt{a + b \sec [c + d x]} \right)$$

**Problem 1057: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec [c + d x] + C \sec [c + d x]^2}{\sec [c + d x]^{7/2} \sqrt{a + b \sec [c + d x]}} dx$$

Optimal (type 4, 380 leaves, 10 steps):

$$\left( 2 (48 A b^4 - 49 a^3 b B - 56 a b^3 B + 5 a^4 (5 A + 7 C) + 2 a^2 b^2 (16 A + 35 C)) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \text{EllipticF} \left[ \frac{1}{2} (c + d x), \frac{2 a}{a + b} \sqrt{\sec [c + d x]} \right] / \left( 105 a^4 d \sqrt{a + b \sec [c + d x]} \right) - \left( 2 (48 A b^3 - 63 a^3 B - 56 a b^2 B + a^2 (44 A b + 70 b C)) \text{EllipticE} \left[ \frac{1}{2} (c + d x), \frac{2 a}{a + b} \sqrt{a + b \sec [c + d x]} \right] / \left( 105 a^4 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \sqrt{\sec [c + d x]} \right) + \frac{2 A \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{7 a d \sec [c + d x]^{5/2}} - \frac{2 (6 A b - 7 a B) \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{35 a^2 d \sec [c + d x]^{3/2}} + \frac{2 (24 A b^2 - 28 a b B + 5 a^2 (5 A + 7 C)) \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{105 a^3 d \sqrt{\sec [c + d x]}} \right)$$

Result (type 6, 4470 leaves):

$$\left( (b + a \cos [c + d x]) (A + B \sec [c + d x] + C \sec [c + d x]^2) \right)$$

$$\begin{aligned}
 & \left( -\frac{4(-44a^2Ab - 48Ab^3 + 63a^3B + 56a^2b^2B - 70a^2bC) \operatorname{Cot}[c]}{105a^4d} + \right. \\
 & \quad \frac{(115a^2A + 96Ab^2 - 112abB + 140a^2C) \operatorname{Cos}[dx] \operatorname{Sin}[c]}{105a^3d} + \\
 & \quad \frac{2(-6Ab + 7aB) \operatorname{Cos}[2dx] \operatorname{Sin}[2c]}{35a^2d} + \frac{A \operatorname{Cos}[3dx] \operatorname{Sin}[3c]}{7ad} + \\
 & \quad \left. \frac{(115a^2A + 96Ab^2 - 112abB + 140a^2C) \operatorname{Cos}[c] \operatorname{Sin}[dx]}{105a^3d} + \right. \\
 & \quad \left. \frac{2(-6Ab + 7aB) \operatorname{Cos}[2c] \operatorname{Sin}[2dx]}{35a^2d} + \frac{A \operatorname{Cos}[3c] \operatorname{Sin}[3dx]}{7ad} \right) / \\
 & \left( (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) \operatorname{Sec}[c + dx]^{3/2} \sqrt{a + b \operatorname{Sec}[c + dx]} \right) - \\
 & \left( 20A \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\operatorname{Csc}[c] \left( b - a \sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \right)}{a \sqrt{1 + \operatorname{Cot}[c]^2} \left( 1 + \frac{b \operatorname{Csc}[c]}{a \sqrt{1 + \operatorname{Cot}[c]^2} \right)} \right], \right. \\
 & \quad \left. \frac{\operatorname{Csc}[c] \left( b - a \sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \right)}{a \sqrt{1 + \operatorname{Cot}[c]^2} \left( -1 + \frac{b \operatorname{Csc}[c]}{a \sqrt{1 + \operatorname{Cot}[c]^2} \right)} \right] \sqrt{b + a \operatorname{Cos}[c + dx]} \right. \\
 & \quad \left. \operatorname{Csc}[c] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \right. \\
 & \quad \sqrt{\frac{a \sqrt{1 + \operatorname{Cot}[c]^2} - a \sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}{a \sqrt{1 + \operatorname{Cot}[c]^2} - b \operatorname{Csc}[c]}} \\
 & \quad \sqrt{\frac{a \sqrt{1 + \operatorname{Cot}[c]^2} + a \sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}{a \sqrt{1 + \operatorname{Cot}[c]^2} + b \operatorname{Csc}[c]}} \\
 & \quad \left. \sqrt{b - a \sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) / \\
 & \left( 21ad (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) \sqrt{1 + \operatorname{Cot}[c]^2} \right. \\
 & \quad \left. \operatorname{Sec}[c + dx]^{3/2} \sqrt{a + b \operatorname{Sec}[c + dx]} \right) + \\
 & \left( 16A b^2 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\operatorname{Csc}[c] \left( b - a \sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \right)}{a \sqrt{1 + \operatorname{Cot}[c]^2} \left( 1 + \frac{b \operatorname{Csc}[c]}{a \sqrt{1 + \operatorname{Cot}[c]^2} \right)} \right], \right.
 \end{aligned}$$

$$\frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( -1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \sqrt{b + a \text{Cos}[c + dx]}$$

$$\text{Csc}[c] \left( A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2 \right) \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]]$$

$$\sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} - b \text{Csc}[c]}}$$

$$\sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} + a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} + b \text{Csc}[c]}}$$

$$\sqrt{b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} /$$

$$\left( 35 a^3 d \left( A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2c + 2dx] \right) \sqrt{1 + \text{Cot}[c]^2} \text{Sec}[c + dx]^{3/2} \sqrt{a + b \text{Sec}[c + dx]} \right) -$$

$$\left( 8 b B \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( 1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \right], \right.$$

$$\left. \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( -1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \sqrt{b + a \text{Cos}[c + dx]} \right)$$

$$\text{Csc}[c] \left( A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2 \right) \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]]$$

$$\sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} - b \text{Csc}[c]}}$$

$$\sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} + a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} + b \text{Csc}[c]}}$$

$$\sqrt{b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} /$$

$$\begin{aligned}
 & \left( 15 a^2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} \right. \\
 & \quad \left. \sec [c + d x]^{3/2} \sqrt{a + b \sec [c + d x]} \right) - \\
 & \left( 4 C \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]] \right)}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right. \\
 & \quad \left. \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]] \right)}{a \sqrt{1 + \cot [c]^2} \left( -1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right] \sqrt{b + a \cos [c + d x]} \right) \\
 & \csc [c] (A + B \sec [c + d x] + C \sec [c + d x]^2) \sec [d x - \operatorname{ArcTan} [\cot [c]]] \\
 & \sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \operatorname{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \operatorname{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}} \\
 & \left. \sqrt{b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]]} \right) / \\
 & \left( 3 a d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} \right. \\
 & \quad \left. \sec [c + d x]^{3/2} \sqrt{a + b \sec [c + d x]} \right) + \\
 & \left( 88 A b \sqrt{b + a \cos [c + d x]} \csc [c] (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left( \left( \operatorname{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \sec [c] \left( b + a \cos [c] \cos [d x + \operatorname{ArcTan} [\tan [c]] \right) \right) \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \tan [c]^2} \right) \right) / \left( a \sqrt{1 + \tan [c]^2} \left( 1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right) \right), \\
 & \quad \left. - \left( \sec [c] \left( b + a \cos [c] \cos [d x + \operatorname{ArcTan} [\tan [c]] \right) \sqrt{1 + \tan [c]^2} \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( a \sqrt{1 + \tan[c]^2} \left( -1 - \frac{b \sec[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \sin[d x + \text{ArcTan}[\tan[c]]] \tan[c] \Big/ \\
 & \left( \sqrt{1 + \tan[c]^2} \sqrt{\left( \left( a \sqrt{1 + \tan[c]^2} - a \cos[d x + \text{ArcTan}[\tan[c]]] \right) \sqrt{1 + \tan[c]^2} \right) \right. \\
 & \left. \left( b \sec[c] + a \sqrt{1 + \tan[c]^2} \right) \sqrt{\left( \left( a \sqrt{1 + \tan[c]^2} + \right. \right. \right. \\
 & \left. \left. \left. a \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2} \right) \right) \right) \Big/ \left( -b \sec[c] + a \sqrt{1 + \tan[c]^2} \right) \\
 & \left. \sqrt{b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}} \right) - \\
 & \left( \frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \left( 2 a \cos[c] \left( b + a \cos[c] \cos[ \right. \right. \right. \\
 & \left. \left. \left. d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2} \right) \right) \Big/ \left( a^2 \cos[c]^2 + a^2 \sin[c]^2 \right) \right) \Big/ \\
 & \left( \sqrt{b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}} \right) \Big/ \\
 & \left( 105 a d \left( A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x] \right) \sec[c + d x]^{3/2} \sqrt{a + b \sec[c + d x]} \right) + \\
 & \left( 32 A b^3 \sqrt{b + a \cos[c + d x]} \csc[c] \left( A + B \sec[c + d x] + C \sec[c + d x]^2 \right) \right. \\
 & \left. \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \sec[c] \left( b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \right) \right) \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \sqrt{1 + \tan[c]^2} \right) \right) \Big/ \left( a \sqrt{1 + \tan[c]^2} \left( 1 - \frac{b \sec[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \right) \Big/ \\
 & - \left( \left( \sec[c] \left( b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2} \right) \right) \Big/ \right. \\
 & \left. \left( a \sqrt{1 + \tan[c]^2} \left( -1 - \frac{b \sec[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \right) \sin[d x + \text{ArcTan}[\tan[c]]] \tan[c] \Big/ \\
 & \left( \sqrt{1 + \tan[c]^2} \sqrt{\left( \left( a \sqrt{1 + \tan[c]^2} - a \cos[d x + \text{ArcTan}[\tan[c]]] \right) \sqrt{1 + \tan[c]^2} \right) \right. \\
 & \left. \left( b \sec[c] + a \sqrt{1 + \tan[c]^2} \right) \sqrt{\left( \left( a \sqrt{1 + \tan[c]^2} + \right. \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & \left( \frac{a \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}}{-b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2}} \right) \\
 & \left( \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) - \\
 & \left( \frac{\sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \left( 2 a \cos [c] \left( b + a \cos [c] \cos [ \right. \right. \right. \\
 & \left. \left. \left. d x + \text{ArcTan}[\text{Tan}[c]] \right] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a^2 \cos [c]^2 + a^2 \sin [c]^2 \right) \right) / \\
 & \left( \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) \Big) / \\
 & \left( 35 a^3 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \text{Sec}[c + d x]^{3/2} \sqrt{a + b \text{Sec}[c + d x]} \right) - \\
 & \left( 6 B \sqrt{b + a \cos [c + d x]} \text{Csc}[c] (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) \right. \\
 & \left. \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \text{Sec}[c] \left( b + a \cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]] \right) \right. \right. \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a \sqrt{1 + \text{Tan}[c]^2} \left( 1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \right), \\
 & - \left( \left( \text{Sec}[c] \left( b + a \cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \right. \\
 & \left. \left( a \sqrt{1 + \text{Tan}[c]^2} \left( -1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \Big) \sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] \Big) / \\
 & \left( \sqrt{1 + \text{Tan}[c]^2} \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} - a \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) / \right. \right. \\
 & \left. \left. \left( b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} + \right. \right. \right. \\
 & \left. \left. \left. a \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( -b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) \Big) \\
 & \left( \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) - \\
 & \left( \frac{\sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \left( 2 a \cos [c] \left( b + a \cos [c] \cos [ \right. \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & \sqrt{a + b \sec [c + d x]} + \\
 & \left( 4 b C \sqrt{b + a \cos [c + d x]} \operatorname{Csc}[c] (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \left. \left( \left( \operatorname{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2} \right] - \left( \sec [c] (b + a \cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]) \right] \right) \right. \right. \\
 & \left. \left. \sqrt{1 + \tan [c]^2} \right) \right) / \left( a \sqrt{1 + \tan [c]^2} \left( 1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right), \\
 & - \left( \left( \sec [c] (b + a \cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]) \right) \sqrt{1 + \tan [c]^2} \right) / \\
 & \left( a \sqrt{1 + \tan [c]^2} \left( -1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right) \sin [d x + \operatorname{ArcTan}[\tan [c]]] \tan [c] \Big/ \\
 & \left( \sqrt{1 + \tan [c]^2} \sqrt{\left( (a \sqrt{1 + \tan [c]^2} - a \cos [d x + \operatorname{ArcTan}[\tan [c]]) \sqrt{1 + \tan [c]^2} \right) / \right. \\
 & \left. (b \sec [c] + a \sqrt{1 + \tan [c]^2}) \right) \sqrt{\left( (a \sqrt{1 + \tan [c]^2} + \right. \\
 & \left. a \cos [d x + \operatorname{ArcTan}[\tan [c]]) \sqrt{1 + \tan [c]^2} \right) / (-b \sec [c] + a \sqrt{1 + \tan [c]^2}) \Big/ \\
 & \left. \sqrt{b + a \cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}} \right) - \\
 & \left( \frac{\sin [d x + \operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \left( 2 a \cos [c] (b + a \cos [c] \cos [ \right. \right. \\
 & \left. \left. d x + \operatorname{ArcTan}[\tan [c]] \right) \sqrt{1 + \tan [c]^2} \right) \Big/ (a^2 \cos [c]^2 + a^2 \sin [c]^2) \Big/ \\
 & \left. \left( \sqrt{b + a \cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}} \right) \right) \Big/ \\
 & \left( 3 a d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sec [c + d x]^{3/2} \right. \\
 & \left. \sqrt{a + b \sec [c + d x]} \right)
 \end{aligned}$$

**Problem 1058:** Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{\text{Sec}[c + d x]} (a A + (A b + a B) \text{Sec}[c + d x] + b B \text{Sec}[c + d x]^2)}{\sqrt{a + b \text{Sec}[c + d x]}} dx$$

Optimal (type 4, 253 leaves, 13 steps):

$$\frac{(2 a A + b B) \sqrt{\frac{b+a \text{Cos}[c+d x]}{a+b}} \text{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{\text{Sec}[c+d x]}}{d \sqrt{a+b \text{Sec}[c+d x]}} +$$

$$\left( (2 A b + a B) \sqrt{\frac{b+a \text{Cos}[c+d x]}{a+b}} \text{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{\text{Sec}[c+d x]} \right) /$$

$$\left( d \sqrt{a+b \text{Sec}[c+d x]} \right) - \frac{B \text{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \text{Sec}[c+d x]}}{d \sqrt{\frac{b+a \text{Cos}[c+d x]}{a+b}} \sqrt{\text{Sec}[c+d x]}} +$$

$$\frac{B \sqrt{\text{Sec}[c+d x]} \sqrt{a+b \text{Sec}[c+d x]} \text{Sin}[c+d x]}{d}$$

Result (type 4, 521 leaves):

$$\begin{aligned}
 & \frac{B (b + a \cos [c + d x]) \sec [c + d x]^{3/2} \sin [c + d x]}{d \sqrt{a + b \sec [c + d x]}} + \frac{1}{4 d \sqrt{a + b \sec [c + d x]}} \\
 & \frac{\sqrt{b + a \cos [c + d x]} \sqrt{\sec [c + d x]}}{\left( \frac{8 a A \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{\sqrt{b+a \cos [c+d x]}} + \right. \\
 & \frac{2 (4 A b + a B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{\sqrt{b+a \cos [c+d x]}} - \\
 & \left( 2 i a B \sqrt{\frac{a-a \cos [c+d x]}{a+b}} \sqrt{\frac{a+a \cos [c+d x]}{a-b}} \cos [2(c+d x)] \right. \\
 & \left. \left( -2 b (a+b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] + \right. \right. \\
 & \left. \left. a \left( 2 b \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] + \right. \right. \right. \\
 & \left. \left. \left. a \operatorname{EllipticPi}\left[1 - \frac{a}{b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] \right) \right) \right) \\
 & \left. \frac{\sin [c+d x]}{\left( \sqrt{\frac{1}{a-b}} b \sqrt{1 - \cos [c+d x]}^2 \sqrt{\frac{a^2 - a^2 \cos [c+d x]^2}{a^2}} \right.} \right. \\
 & \left. \left. \left. \left( -a^2 + 2 b^2 - 4 b (b + a \cos [c+d x]) + 2 (b + a \cos [c+d x])^2 \right) \right) \right) \right)
 \end{aligned}$$

**Problem 1059: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\sec [c + d x]^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2)}{(a + b \sec [c + d x])^{3/2}} dx$$

Optimal (type 4, 393 leaves, 13 steps):

$$\begin{aligned}
 & C \frac{\sqrt{\frac{b+a \operatorname{Cos}[c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{\operatorname{Sec}[c+d x]}}{b d \sqrt{a+b \operatorname{Sec}[c+d x]}} + \\
 & \left( (2 b B - 3 a C) \sqrt{\frac{b+a \operatorname{Cos}[c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{\operatorname{Sec}[c+d x]} \right) / \\
 & \left( b^2 d \sqrt{a+b \operatorname{Sec}[c+d x]} \right) - \\
 & \left( (2 A b^2 - 2 a b B + 3 a^2 C - b^2 C) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \operatorname{Sec}[c+d x]} \right) / \\
 & \left( b^2 (a^2 - b^2) d \sqrt{\frac{b+a \operatorname{Cos}[c+d x]}{a+b}} \sqrt{\operatorname{Sec}[c+d x]} \right) - \\
 & \frac{2 (A b^2 - a (b B - a C)) \operatorname{Sec}[c+d x]^{3/2} \operatorname{Sin}[c+d x]}{b (a^2 - b^2) d \sqrt{a+b \operatorname{Sec}[c+d x]}} + \frac{1}{b^2 (a^2 - b^2) d} \\
 & (2 A b^2 - 2 a b B + 3 a^2 C - b^2 C) \sqrt{\operatorname{Sec}[c+d x]} \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]
 \end{aligned}$$

Result (type 4, 774 leaves):



### Problem 1060: Unable to integrate problem.

$$\int \frac{\sqrt{\text{Sec}[c + d x]} (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2)}{(a + b \text{Sec}[c + d x])^{3/2}} dx$$

Optimal (type 4, 311 leaves, 12 steps):

$$\begin{aligned} & \frac{2 A \sqrt{\frac{b+a \text{Cos}[c+d x]}{a+b}} \text{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{\text{Sec}[c+d x]}}{a d \sqrt{a+b \text{Sec}[c+d x]}} + \\ & \frac{2 C \sqrt{\frac{b+a \text{Cos}[c+d x]}{a+b}} \text{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{\text{Sec}[c+d x]}}{b d \sqrt{a+b \text{Sec}[c+d x]}} + \\ & \left( 2 (A b^2 - a (b B - a C)) \text{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \text{Sec}[c+d x]} \right) / \\ & \left( a b (a^2 - b^2) d \sqrt{\frac{b+a \text{Cos}[c+d x]}{a+b}} \sqrt{\text{Sec}[c+d x]} \right) - \\ & \frac{2 (A b^2 - a (b B - a C)) \sqrt{\text{Sec}[c+d x]} \text{Sin}[c+d x]}{b (a^2 - b^2) d \sqrt{a+b \text{Sec}[c+d x]}} \end{aligned}$$

Result (type 8, 47 leaves):

$$\int \frac{\sqrt{\text{Sec}[c + d x]} (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2)}{(a + b \text{Sec}[c + d x])^{3/2}} dx$$

### Problem 1061: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2}{\sqrt{\text{Sec}[c + d x]} (a + b \text{Sec}[c + d x])^{3/2}} dx$$

Optimal (type 4, 249 leaves, 8 steps):



$$\begin{aligned}
 & - \left( \left( 2 (2 A b - a B) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), \frac{2 a}{a + b} \right] \sqrt{\sec [c + d x]} \right) / \right. \\
 & \quad \left. \left( a^2 d \sqrt{a + b \sec [c + d x]} \right) \right) - \\
 & \left( 2 (2 A b^2 - a b B - a^2 (A - C)) \operatorname{EllipticE} \left[ \frac{1}{2} (c + d x), \frac{2 a}{a + b} \right] \sqrt{a + b \sec [c + d x]} \right) / \\
 & \left( a^2 (a^2 - b^2) d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \sqrt{\sec [c + d x]} \right) + \\
 & \frac{2 (A b^2 - a (b B - a C)) \sqrt{\sec [c + d x]} \sin [c + d x]}{a (a^2 - b^2) d \sqrt{a + b \sec [c + d x]}}
 \end{aligned}$$

Result (type 6, 3541 leaves):

$$\begin{aligned}
 & \left( (b + a \cos [c + d x])^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left( - \frac{1}{a^2 (a^2 - b^2) d} 2 (a^2 A - 3 A b^2 + 2 a b B - 2 a^2 C + a^2 A \cos [2 c] - A b^2 \cos [2 c]) \operatorname{Csc} [c] \operatorname{Sec} [c] - \right. \\
 & \quad \left. (4 \operatorname{Sec} [c] (A b^3 \sin [c] - a b^2 B \sin [c] + a^2 b C \sin [c] - A a b^2 \sin [d x] + \right. \\
 & \quad \left. a^2 b B \sin [d x] - a^3 C \sin [d x])) / (a^2 (a^2 - b^2) d (b + a \cos [c + d x])) \right) \Bigg) / \\
 & \left( (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{\sec [c + d x]} (a + b \sec [c + d x])^{3/2} + \right. \\
 & \left. \left( 4 A b \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\operatorname{Csc} [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \operatorname{Csc} [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right] \right) \right. \\
 & \quad \left. \frac{\operatorname{Csc} [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( -1 + \frac{b \operatorname{Csc} [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right) (b + a \cos [c + d x])^{3/2} \\
 & \operatorname{Csc} [c] (A + B \sec [c + d x] + C \sec [c + d x]^2) \operatorname{Sec} [d x - \operatorname{ArcTan} [\cot [c]]] \\
 & \sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \operatorname{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \operatorname{Csc} [c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \operatorname{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \operatorname{Csc} [c]}}
 \end{aligned}$$

$$\left. \sqrt{b - a \sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]} \right/$$

$$\left( (a^2 - b^2) d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{1 + \cot[c]^2} \right.$$

$$\left. \sqrt{\sec[c + dx]} (a + b \sec[c + dx])^{3/2} \right) -$$

$$\left( 4 B \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc[c] \left( b - a \sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]] \right)}{a \sqrt{1 + \cot[c]^2} \left( 1 + \frac{b \csc[c]}{a \sqrt{1 + \cot[c]^2}} \right)} \right], \right.$$

$$\left. \frac{\csc[c] \left( b - a \sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]] \right)}{a \sqrt{1 + \cot[c]^2} \left( -1 + \frac{b \csc[c]}{a \sqrt{1 + \cot[c]^2}} \right)} \right] (b + a \cos[c + dx])^{3/2}$$

$$\csc[c] (A + B \sec[c + dx] + C \sec[c + dx]^2) \sec[dx - \text{ArcTan}[\cot[c]]]$$

$$\sqrt{\frac{a \sqrt{1 + \cot[c]^2} - a \sqrt{1 + \cot[c]^2} \sin[dx - \text{ArcTan}[\cot[c]]]}{a \sqrt{1 + \cot[c]^2} - b \csc[c]}}$$

$$\sqrt{\frac{a \sqrt{1 + \cot[c]^2} + a \sqrt{1 + \cot[c]^2} \sin[dx - \text{ArcTan}[\cot[c]]]}{a \sqrt{1 + \cot[c]^2} + b \csc[c]}}$$

$$\left. \sqrt{b - a \sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]} \right/$$

$$\left( (a^2 - b^2) d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{1 + \cot[c]^2} \right.$$

$$\left. \sqrt{\sec[c + dx]} (a + b \sec[c + dx])^{3/2} \right) +$$

$$\left( 4 b C \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc[c] \left( b - a \sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]] \right)}{a \sqrt{1 + \cot[c]^2} \left( 1 + \frac{b \csc[c]}{a \sqrt{1 + \cot[c]^2}} \right)} \right], \right.$$

$$\left. \frac{\csc[c] \left( b - a \sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]] \right)}{a \sqrt{1 + \cot[c]^2} \left( -1 + \frac{b \csc[c]}{a \sqrt{1 + \cot[c]^2}} \right)} \right] (b + a \cos[c + dx])^{3/2}$$

$$\csc[c] (A + B \sec[c + dx] + C \sec[c + dx]^2) \sec[dx - \text{ArcTan}[\cot[c]]]$$

$$\begin{aligned}
 & \sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}} \\
 & \left. \sqrt{b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]]} \right) / \\
 & \left( a (a^2 - b^2) d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} \right. \\
 & \quad \left. \sqrt{\sec [c + d x]} (a + b \sec [c + d x])^{3/2} \right) - \\
 & \left( 2 a A (b + a \cos [c + d x])^{3/2} \csc [c] (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left. \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \sec [c] (b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]) \right) \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \tan [c]^2} \right) \right) / \left( a \sqrt{1 + \tan [c]^2} \left( 1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right) \right), \\
 & \quad - \left( \left( \sec [c] (b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) \right) / \\
 & \quad \left( a \sqrt{1 + \tan [c]^2} \left( -1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right) \sin [d x + \text{ArcTan} [\tan [c]]] \tan [c] \Big) / \\
 & \left( \sqrt{1 + \tan [c]^2} \sqrt{\left( (a \sqrt{1 + \tan [c]^2} - a \cos [d x + \text{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) / \right. \\
 & \quad \left. (b \sec [c] + a \sqrt{1 + \tan [c]^2}) \right) \sqrt{\left( (a \sqrt{1 + \tan [c]^2} + \right. \\
 & \quad \left. a \cos [d x + \text{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) / (-b \sec [c] + a \sqrt{1 + \tan [c]^2}) \Big)} \\
 & \quad \left. \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2}} \right) - \\
 & \left( \frac{\sin [d x + \text{ArcTan} [\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \left( 2 a \cos [c] (b + a \cos [c] \cos [c] \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \left. \left. d x + \text{ArcTan}[\text{Tan}[c]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) \right) \right) \Big/ \left( a^2 \text{Cos}[c]^2 + a^2 \text{Sin}[c]^2 \right) \Big/ \\
 & \left( \sqrt{\left( \sqrt{b + a \text{Cos}[c] \text{Cos}[d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \text{Tan}[c]^2} \right)} \right) \Big/ \\
 & \left( (a^2 - b^2) d (A + 2 C + 2 B \text{Cos}[c + d x] + A \text{Cos}[2 c + 2 d x]) \sqrt{\text{Sec}[c + d x]} (a + b \text{Sec}[c + d x])^{3/2} \right) + \\
 & \left( 4 A b^2 (b + a \text{Cos}[c + d x])^{3/2} \text{Csc}[c] (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) \right. \\
 & \left. \left( \left( \text{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, -\left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[d x + \text{ArcTan}[\text{Tan}[c]] \right) \right. \right. \right. \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \left. \sqrt{1 + \text{Tan}[c]^2} \right) \right) \right) \right) \right) \Big/ \left( a \sqrt{1 + \text{Tan}[c]^2} \left( 1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \Big/ \\
 & - \left( \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[d x + \text{ArcTan}[\text{Tan}[c]]] \right) \sqrt{1 + \text{Tan}[c]^2} \right) \right) \Big/ \\
 & \left( a \sqrt{1 + \text{Tan}[c]^2} \left( -1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \Big/ \left. \left. \left. \left. \left. \left. \left. \left. \left. \left. \left. \text{Sin}[d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] \right) \right) \right) \right) \right) \right) \right) \Big/ \\
 & \left( \sqrt{1 + \text{Tan}[c]^2} \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} - a \text{Cos}[d x + \text{ArcTan}[\text{Tan}[c]]] \right) \sqrt{1 + \text{Tan}[c]^2} \right)} \Big/ \right. \\
 & \left( b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \Big/ \left( \left( a \sqrt{1 + \text{Tan}[c]^2} + \right. \right. \\
 & \left. \left. a \text{Cos}[d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \Big/ \left( -b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) \\
 & \left. \left. \left. \left. \left. \left. \left. \left. \left. \left. \left. \left. \left. \left. \left. \left. \left. \left. \left. \sqrt{b + a \text{Cos}[c] \text{Cos}[d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \text{Tan}[c]^2} \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) - \\
 & \left( \frac{\text{Sin}[d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \left( 2 a \text{Cos}[c] \left( b + a \text{Cos}[c] \text{Cos}[ \right. \right. \right. \\
 & \left. \left. \left. d x + \text{ArcTan}[\text{Tan}[c]] \right) \sqrt{1 + \text{Tan}[c]^2} \right) \right) \Big/ \left( a^2 \text{Cos}[c]^2 + a^2 \text{Sin}[c]^2 \right) \Big/ \\
 & \left( \sqrt{\left( \sqrt{b + a \text{Cos}[c] \text{Cos}[d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \text{Tan}[c]^2} \right)} \right) \Big/ \\
 & \left( a (a^2 - b^2) d (A + 2 C + 2 B \text{Cos}[c + d x] + A \text{Cos}[2 c + 2 d x]) \sqrt{\text{Sec}[c + d x]} \right. \\
 & \left. (a + b \text{Sec}[c + d x])^{3/2} \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2 b B (b + a \cos [c + d x])^{3/2} \operatorname{Csc}[c] (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \left( \left( \operatorname{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, -\left(\operatorname{Sec}[c] (b + a \cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]])\right)\right.\right. \right. \\
 & \left. \left. \left. \sqrt{1 + \tan [c]^2}\right)\right] / \left(a \sqrt{1 + \tan [c]^2} \left(1 - \frac{b \operatorname{Sec}[c]}{a \sqrt{1 + \tan [c]^2}}\right)\right) \right) \right), \\
 & - \left( \left( \operatorname{Sec}[c] (b + a \cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]) \sqrt{1 + \tan [c]^2}\right) \right) / \\
 & \left( a \sqrt{1 + \tan [c]^2} \left(-1 - \frac{b \operatorname{Sec}[c]}{a \sqrt{1 + \tan [c]^2}}\right) \right) \right) \operatorname{Sin}[d x + \operatorname{ArcTan}[\tan [c]]] \operatorname{Tan}[c] \Big/ \\
 & \left( \sqrt{1 + \tan [c]^2} \sqrt{\left(\left(a \sqrt{1 + \tan [c]^2} - a \cos [d x + \operatorname{ArcTan}[\tan [c]]\right] \sqrt{1 + \tan [c]^2}\right) \right) /} \\
 & \left( b \operatorname{Sec}[c] + a \sqrt{1 + \tan [c]^2} \right) \sqrt{\left(\left(a \sqrt{1 + \tan [c]^2} + \right. \right. \\
 & \left. \left. a \cos [d x + \operatorname{ArcTan}[\tan [c]]\right] \sqrt{1 + \tan [c]^2}\right) / \left(-b \operatorname{Sec}[c] + a \sqrt{1 + \tan [c]^2}\right)} \\
 & \left. \sqrt{b + a \cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}} \right) - \\
 & \left( \frac{\operatorname{Sin}[d x + \operatorname{ArcTan}[\tan [c]]] \operatorname{Tan}[c]}{\sqrt{1 + \tan [c]^2}} + \left( 2 a \cos [c] (b + a \cos [c] \cos [ \right. \right. \\
 & \left. \left. d x + \operatorname{ArcTan}[\tan [c]]\right] \sqrt{1 + \tan [c]^2} \right) / \left(a^2 \cos [c]^2 + a^2 \sin [c]^2\right) \right) \Big/ \\
 & \left( \sqrt{b + a \cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}} \right) \Big/ \\
 & \left( (a^2 - b^2) d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{\operatorname{Sec}[c + d x]} \right. \\
 & \left. (a + b \operatorname{Sec}[c + d x])^{3/2} \right) + \\
 & \left( 2 a C (b + a \cos [c + d x])^{3/2} \operatorname{Csc}[c] (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \left( \left( \operatorname{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, -\left(\operatorname{Sec}[c] (b + a \cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]])\right)\right.\right. \right. \right.
 \end{aligned}$$

$$\begin{aligned} & \left. \left( \sqrt{1 + \tan[c]^2} \right) \right) / \left( a \sqrt{1 + \tan[c]^2} \left( 1 - \frac{b \sec[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right), \\ & - \left( \left( \sec[c] \left( b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2} \right) \right) / \right. \\ & \left. \left( a \sqrt{1 + \tan[c]^2} \left( -1 - \frac{b \sec[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \right) \sin[d x + \text{ArcTan}[\tan[c]]] \tan[c] / \\ & \left( \sqrt{1 + \tan[c]^2} \sqrt{\left( \left( a \sqrt{1 + \tan[c]^2} - a \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2} \right) / \right. \right. \\ & \left. \left. \left( b \sec[c] + a \sqrt{1 + \tan[c]^2} \right) \right) \sqrt{\left( \left( a \sqrt{1 + \tan[c]^2} + \right. \right. \right. \\ & \left. \left. \left. a \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2} \right) / \left( -b \sec[c] + a \sqrt{1 + \tan[c]^2} \right) \right) \right. \\ & \left. \left. \sqrt{b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}} \right) - \right. \\ & \left. \left( \frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \left( 2 a \cos[c] \left( b + a \cos[c] \cos \right. \right. \right. \right. \\ & \left. \left. \left. d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2} \right) \right) / \left( a^2 \cos[c]^2 + a^2 \sin[c]^2 \right) \right) / \\ & \left. \left( \sqrt{b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}} \right) \right) / \\ & \left( (a^2 - b^2) d (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) \right. \\ & \left. \sqrt{\sec[c + d x]} \right. \\ & \left. (a + b \sec[c + d x])^{3/2} \right) \end{aligned}$$

**Problem 1062: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec[c + d x] + C \sec[c + d x]^2}{\sec[c + d x]^{3/2} (a + b \sec[c + d x])^{3/2}} dx$$

Optimal (type 4, 350 leaves, 9 steps):

$$\begin{aligned}
 & \left( 2 (8 A b^2 - 6 a b B + a^2 (A + 3 C)) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \\
 & \quad \left. \text{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b} \sqrt{\sec [c + d x]}\right] \right) / \left( 3 a^3 d \sqrt{a + b \sec [c + d x]} \right) + \\
 & \left( 2 (8 A b^3 + 3 a^3 B - 6 a b^2 B - a^2 (5 A b - 3 b C)) \text{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b} \sqrt{a + b \sec [c + d x]}\right] \right) / \\
 & \left( 3 a^3 (a^2 - b^2) d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \sqrt{\sec [c + d x]} \right) + \\
 & \frac{2 (A b^2 - a (b B - a C)) \sin [c + d x]}{a (a^2 - b^2) d \sqrt{\sec [c + d x]} \sqrt{a + b \sec [c + d x]}} - \\
 & \frac{2 (4 A b^2 - 3 a b B - a^2 (A - 3 C)) \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{3 a^2 (a^2 - b^2) d \sqrt{\sec [c + d x]}}
 \end{aligned}$$

Result (type 6, 4557 leaves):

$$\begin{aligned}
 & \left( (b + a \cos [c + d x])^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left( -\frac{1}{3 a^3 (a^2 - b^2) d} 2 (-5 a^2 A b + 11 A b^3 + 3 a^3 B - 9 a b^2 B + 6 a^2 b C - 5 a^2 A b \cos [2 c] + \right. \\
 & \quad \quad 5 A b^3 \cos [2 c] + 3 a^3 B \cos [2 c] - 3 a b^2 B \cos [2 c]) \csc [c] \sec [c] + \frac{4 A \cos [d x] \sin [c]}{3 a^2 d} + \\
 & \quad \quad \frac{4 A \cos [c] \sin [d x]}{3 a^2 d} + (4 \sec [c] (A b^4 \sin [c] - a b^3 B \sin [c] + a^2 b^2 C \sin [c] - a A b^3 \sin [d x] + \\
 & \quad \quad \left. a^2 b^2 B \sin [d x] - a^3 b C \sin [d x])) / (a^3 (a^2 - b^2) d (b + a \cos [c + d x])) \right) \Bigg) / \\
 & \left( (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{\sec [c + d x]} (a + b \sec [c + d x])^{3/2} \right) - \\
 & \left( 4 A \text{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] (b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan}[\cot [c]])]}{a \sqrt{1 + \cot [c]^2} \left(1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}}\right)}\right], \right. \\
 & \quad \left. \frac{\csc [c] (b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan}[\cot [c]])]}{a \sqrt{1 + \cot [c]^2} \left(-1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}}\right)} \right] (b + a \cos [c + d x])^{3/2} \right) \\
 & \csc [c] (A + B \sec [c + d x] + C \sec [c + d x]^2) \sec [d x - \text{ArcTan}[\cot [c]]] \\
 & \sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan}[\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}}
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{\sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}}}{\sqrt{\frac{b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]]}{}}} \right) \\
 & \left( 3 (a^2 - b^2) d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} \right. \\
 & \quad \left. \sqrt{\sec [c + d x]} (a + b \sec [c + d x])^{3/2} \right) - \\
 & \left( 8 A b^2 \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right. \\
 & \quad \left. \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( -1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right] (b + a \cos [c + d x])^{3/2} \\
 & \csc [c] (A + B \sec [c + d x] + C \sec [c + d x]^2) \sec [d x - \text{ArcTan} [\cot [c]]] \\
 & \left( \frac{\sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}}}{\sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}}} \right) \\
 & \left( \frac{\sqrt{b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]]}}{\sqrt{3 a^2 (a^2 - b^2) d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])}} \right) \\
 & \quad \sqrt{1 + \cot [c]^2} \sqrt{\sec [c + d x]} (a + b \sec [c + d x])^{3/2} + \\
 & \left( 4 b B \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right.
 \end{aligned}$$



$$\frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( -1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \left( b + a \text{Cos}[c + dx] \right)^{3/2}$$

$$\text{Csc}[c] \left( A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2 \right) \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]]$$

$$\sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} - b \text{Csc}[c]}}$$

$$\sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} + a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} + b \text{Csc}[c]}}$$

$$\sqrt{b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \Big/$$

$$\left( a (a^2 - b^2) d (A + 2C + 2B \text{Cos}[c + dx] + A \text{Cos}[2c + 2dx]) \sqrt{1 + \text{Cot}[c]^2} \sqrt{\text{Sec}[c + dx]} (a + b \text{Sec}[c + dx])^{3/2} \right) -$$

$$\left( 4 \text{C AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( 1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \right], \right.$$

$$\left. \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( -1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \right] \left( b + a \text{Cos}[c + dx] \right)^{3/2}$$

$$\text{Csc}[c] \left( A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2 \right) \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]]$$

$$\sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} - b \text{Csc}[c]}}$$

$$\sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} + a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} + b \text{Csc}[c]}}$$

$$\sqrt{b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \Big/$$

$$\begin{aligned}
 & \left( (a^2 - b^2) d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{1 + \cot[c]^2} \right. \\
 & \quad \left. \sqrt{\sec[c + dx]} (a + b \sec[c + dx])^{3/2} \right) + \\
 & \left( 10Ab (b + a \cos[c + dx])^{3/2} \operatorname{Csc}[c] (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\
 & \quad \left( \left( \operatorname{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \sec[c] (b + a \cos[c] \cos[dx + \operatorname{ArcTan}[\tan[c]])] \right) \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \tan[c]^2} \right) \right) / \left( a \sqrt{1 + \tan[c]^2} \left( 1 - \frac{b \sec[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \right), \\
 & \quad - \left( \left( \sec[c] (b + a \cos[c] \cos[dx + \operatorname{ArcTan}[\tan[c]])] \sqrt{1 + \tan[c]^2} \right) / \right. \\
 & \quad \left. \left( a \sqrt{1 + \tan[c]^2} \left( -1 - \frac{b \sec[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \right) \sin[dx + \operatorname{ArcTan}[\tan[c]]] \tan[c] \Big/ \\
 & \quad \left( \sqrt{1 + \tan[c]^2} \sqrt{\left( (a \sqrt{1 + \tan[c]^2} - a \cos[dx + \operatorname{ArcTan}[\tan[c]])] \sqrt{1 + \tan[c]^2} \right) / \right. \\
 & \quad \left. (b \sec[c] + a \sqrt{1 + \tan[c]^2}) \right) \sqrt{\left( (a \sqrt{1 + \tan[c]^2} + \right. \\
 & \quad \left. a \cos[dx + \operatorname{ArcTan}[\tan[c]])] \sqrt{1 + \tan[c]^2} \right) / (-b \sec[c] + a \sqrt{1 + \tan[c]^2})} \\
 & \quad \left. \sqrt{b + a \cos[c] \cos[dx + \operatorname{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}} \right) - \\
 & \quad \left( \frac{\sin[dx + \operatorname{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \left( 2a \cos[c] (b + a \cos[c] \cos[ \right. \right. \\
 & \quad \left. \left. dx + \operatorname{ArcTan}[\tan[c]])] \sqrt{1 + \tan[c]^2} \right) / (a^2 \cos[c]^2 + a^2 \sin[c]^2) \right) \Big/ \\
 & \quad \left( \sqrt{b + a \cos[c] \cos[dx + \operatorname{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}} \right) \Big/ \\
 & \left( 3(a^2 - b^2) d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{\sec[c + dx]} (a + b \sec[c + dx])^{3/2} \right) - \\
 & \left( 16Ab^3 (b + a \cos[c + dx])^{3/2} \operatorname{Csc}[c] (A + B \sec[c + dx] + C \sec[c + dx]^2) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \right] \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \text{Tan}[c]^2} \right) \right) \right) / \left( a \sqrt{1 + \text{Tan}[c]^2} \left( 1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right), \\
 & - \left( \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \right] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \\
 & \quad \left( a \sqrt{1 + \text{Tan}[c]^2} \left( -1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] \Big/ \\
 & \left( \sqrt{1 + \text{Tan}[c]^2} \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} - a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \sqrt{1 + \text{Tan}[c]^2} \right) \right.} \\
 & \quad \left. \left( b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} + \right. \right.} \\
 & \quad \left. \left. a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \sqrt{1 + \text{Tan}[c]^2} \right) \Big/ \left( -b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right)} \\
 & \quad \left. \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) - \\
 & \left( \frac{\text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \left( 2 a \text{Cos}[c] \left( b + a \text{Cos}[c] \text{Cos}[ \right. \right. \right. \\
 & \quad \left. \left. \left. dx + \text{ArcTan}[\text{Tan}[c]] \right) \sqrt{1 + \text{Tan}[c]^2} \right) \right) \Big/ \left( a^2 \text{Cos}[c]^2 + a^2 \text{Sin}[c]^2 \right) \Big/ \\
 & \quad \left( \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) \Big/ \\
 & \left( 3 a^2 (a^2 - b^2) d (A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2 c + 2 dx]) \sqrt{\text{Sec}[c + dx]} \right. \\
 & \quad \left. (a + b \text{Sec}[c + dx])^{3/2} \right) - \\
 & \left( 2 a B (b + a \text{Cos}[c + dx])^{3/2} \text{Csc}[c] (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \right. \\
 & \left. \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \right) \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \text{Tan}[c]^2} \right) \right) \right) / \left( a \sqrt{1 + \text{Tan}[c]^2} \left( 1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \Big/
 \end{aligned}$$

$$\begin{aligned}
 & - \left( \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \right. \\
 & \quad \left. \left( a \sqrt{1 + \text{Tan}[c]^2} \left( -1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] / \\
 & \left( \sqrt{1 + \text{Tan}[c]^2} \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} - a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) / \right. \right. \\
 & \quad \left. \left( b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} + \right. \right. \\
 & \quad \left. \left. a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) / \left( -b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) } \\
 & \quad \left. \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) - \\
 & \left( \frac{\text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \left( 2 a \text{Cos}[c] \left( b + a \text{Cos}[c] \text{Cos}[ \right. \right. \right. \\
 & \quad \left. \left. \left. dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a^2 \text{Cos}[c]^2 + a^2 \text{Sin}[c]^2 \right) \right) / \\
 & \left( \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) / \\
 & \left( (a^2 - b^2) d (A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2 c + 2 dx]) \sqrt{\text{Sec}[c + dx]} \right. \\
 & \quad \left. (a + b \text{Sec}[c + dx])^{3/2} \right) + \\
 & \left( 4 b^2 B (b + a \text{Cos}[c + dx])^{3/2} \text{Csc}[c] (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \right. \\
 & \quad \left. \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \right) \right) \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a \sqrt{1 + \text{Tan}[c]^2} \left( 1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \right), \\
 & - \left( \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \right. \\
 & \quad \left. \left( a \sqrt{1 + \text{Tan}[c]^2} \left( -1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] /
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{1 + \tan[c]^2} \sqrt{\left( \left( a \sqrt{1 + \tan[c]^2} - a \cos[d x + \text{ArcTan}[\tan[c]] \right] \sqrt{1 + \tan[c]^2} \right) / \right.} \\
 & \quad \left. \left( b \sec[c] + a \sqrt{1 + \tan[c]^2} \right) \right) \sqrt{\left( \left( a \sqrt{1 + \tan[c]^2} + \right.} \right. \\
 & \quad \left. \left. a \cos[d x + \text{ArcTan}[\tan[c]] \right] \sqrt{1 + \tan[c]^2} \right) / \left( -b \sec[c] + a \sqrt{1 + \tan[c]^2} \right)} \\
 & \quad \left. \sqrt{b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}} \right) - \\
 & \left( \frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \left( 2 a \cos[c] \left( b + a \cos[c] \cos[ \right. \right. \right. \\
 & \quad \left. \left. \left. d x + \text{ArcTan}[\tan[c]] \right] \sqrt{1 + \tan[c]^2} \right) \right) / \left( a^2 \cos[c]^2 + a^2 \sin[c]^2 \right) \right) / \\
 & \left( \sqrt{b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}} \right) \Bigg) / \\
 & \left( a (a^2 - b^2) d (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) \sqrt{\sec[c + d x]} \right. \\
 & \quad \left. (a + b \sec[c + d x])^{3/2} \right) - \\
 & \left( 2 b C (b + a \cos[c + d x])^{3/2} \csc[c] (A + B \sec[c + d x] + C \sec[c + d x]^2) \right. \\
 & \quad \left. \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \sec[c] \left( b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]] \right] \right) \right. \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \tan[c]^2} \right) \right) / \left( a \sqrt{1 + \tan[c]^2} \left( 1 - \frac{b \sec[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \right) \right) , \\
 & \quad - \left( \left( \sec[c] \left( b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2} \right) \right) / \right. \\
 & \quad \left. \left( a \sqrt{1 + \tan[c]^2} \left( -1 - \frac{b \sec[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \right) \sin[d x + \text{ArcTan}[\tan[c]]] \tan[c] \Bigg) / \\
 & \left( \sqrt{1 + \tan[c]^2} \sqrt{\left( \left( a \sqrt{1 + \tan[c]^2} - a \cos[d x + \text{ArcTan}[\tan[c]] \right] \sqrt{1 + \tan[c]^2} \right) / \right.} \\
 & \quad \left. \left( b \sec[c] + a \sqrt{1 + \tan[c]^2} \right) \right) \sqrt{\left( \left( a \sqrt{1 + \tan[c]^2} + \right. \right. \\
 & \quad \left. \left. a \cos[d x + \text{ArcTan}[\tan[c]] \right] \sqrt{1 + \tan[c]^2} \right) / \left( -b \sec[c] + a \sqrt{1 + \tan[c]^2} \right)} \Bigg)
 \end{aligned}$$

$$\left( \sqrt{b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]]} \sqrt{1 + \tan[c]^2} \right) - \left( \frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \left( 2 a \cos[c] \left( b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2} \right) \right) / \left( a^2 \cos[c]^2 + a^2 \sin[c]^2 \right) \right) / \left( \sqrt{b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]]} \sqrt{1 + \tan[c]^2} \right) / \left( (a^2 - b^2) d (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) \sqrt{\sec[c + d x]} (a + b \sec[c + d x])^{3/2} \right)$$

**Problem 1063: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec[c + d x] + C \sec[c + d x]^2}{\sec[c + d x]^{5/2} (a + b \sec[c + d x])^{3/2}} dx$$

Optimal (type 4, 461 leaves, 10 steps):

$$\begin{aligned}
 & - \left( \left( 2 (48 A b^3 - 5 a^3 B - 40 a b^2 B + 6 a^2 b (2 A + 5 C)) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \right. \\
 & \quad \left. \left. \text{EllipticF} \left[ \frac{1}{2} (c + d x), \frac{2 a}{a + b} \right] \sqrt{\sec [c + d x]} \right) / \left( 15 a^4 d \sqrt{a + b \sec [c + d x]} \right) \right) - \\
 & \left( 2 (48 A b^4 + 25 a^3 b B - 40 a b^3 B - 6 a^2 b^2 (4 A - 5 C) - 3 a^4 (3 A + 5 C)) \right. \\
 & \quad \left. \text{EllipticE} \left[ \frac{1}{2} (c + d x), \frac{2 a}{a + b} \right] \sqrt{a + b \sec [c + d x]} \right) / \\
 & \left( 15 a^4 (a^2 - b^2) d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \sqrt{\sec [c + d x]} \right) + \\
 & \frac{2 (A b^2 - a (b B - a C)) \sin [c + d x]}{a (a^2 - b^2) d \sec [c + d x]^{3/2} \sqrt{a + b \sec [c + d x]}} - \\
 & \frac{2 (6 A b^2 - 5 a b B - a^2 (A - 5 C)) \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{5 a^2 (a^2 - b^2) d \sec [c + d x]^{3/2}} + \\
 & \left( \frac{2 (24 A b^3 + 5 a^3 B - 20 a b^2 B - a^2 (9 A b - 15 b C)) \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{15 a^3 (a^2 - b^2) d \sqrt{\sec [c + d x]}} \right) /
 \end{aligned}$$

Result (type 6, 6134 leaves):

$$\begin{aligned}
 & \left( (b + a \cos [c + d x])^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \left( - \left( (2 (9 a^4 A + 24 a^2 A b^2 - 63 A b^4 - 25 a^3 b B + 55 a b^3 B + 15 a^4 C - 45 a^2 b^2 C + 9 a^4 A \cos [2 c] + \right. \right. \\
 & \quad 24 a^2 A b^2 \cos [2 c] - 33 A b^4 \cos [2 c] - 25 a^3 b B \cos [2 c] + 25 a b^3 B \cos [2 c] + \\
 & \quad 15 a^4 C \cos [2 c] - 15 a^2 b^2 C \cos [2 c]) \csc [c] \sec [c] / (15 a^4 (a^2 - b^2) d) + \\
 & \quad \frac{4 (-9 A b + 5 a B) \cos [d x] \sin [c]}{15 a^3 d} + \frac{2 A \cos [2 d x] \sin [2 c]}{5 a^2 d} + \\
 & \quad \frac{4 (-9 A b + 5 a B) \cos [c] \sin [d x]}{15 a^3 d} - \\
 & \quad \left. (4 \sec [c] (A b^5 \sin [c] - a b^4 B \sin [c] + a^2 b^3 C \sin [c] - a A b^4 \sin [d x] + a^2 b^3 B \sin [d x] - \right. \\
 & \quad \left. a^3 b^2 C \sin [d x])) / (a^4 (a^2 - b^2) d (b + a \cos [c + d x])) + \frac{2 A \cos [2 c] \sin [2 d x]}{5 a^2 d} \right) \left. \right) / \\
 & \left( (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{\sec [c + d x]} \right. \\
 & \quad \left. (a + b \sec [c + d x])^{3/2} \right) + \\
 & \left( 4 A b \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan}[\cot [c]] \right)}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right] \right) \right) /
 \end{aligned}$$

$$\frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( -1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)}$$

$$(b + a \text{Cos}[c + dx])^{3/2} \text{Csc}[c] (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]]$$

$$\sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} - b \text{Csc}[c]}}$$

$$\sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} + a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} + b \text{Csc}[c]}}$$

$$\left. \sqrt{b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right/$$

$$\left( 5 a (a^2 - b^2) d (A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2 c + 2 dx]) \right.$$

$$\left. \sqrt{1 + \text{Cot}[c]^2} \sqrt{\text{Sec}[c + dx]} (a + b \text{Sec}[c + dx])^{3/2} \right) +$$

$$\left( 16 A b^3 \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( 1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \right], \right.$$

$$\left. \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( -1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \right] (b + a \text{Cos}[c + dx])^{3/2}$$

$$\text{Csc}[c] (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]]$$

$$\sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} - b \text{Csc}[c]}}$$

$$\sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} + a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} + b \text{Csc}[c]}}$$

$$\left. \sqrt{b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right/$$



$$\begin{aligned}
 & \left( 5 a^3 (a^2 - b^2) d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. \sqrt{1 + \cot [c]^2} \sqrt{\sec [c + d x]} (a + b \sec [c + d x])^{3/2} \right) - \\
 & \left( 4 B \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right. \\
 & \quad \left. \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( -1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right] (b + a \cos [c + d x])^{3/2} \\
 & \quad \csc [c] (A + B \sec [c + d x] + C \sec [c + d x]^2) \sec [d x - \operatorname{ArcTan} [\cot [c]]] \\
 & \quad \sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \operatorname{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}} \\
 & \quad \sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \operatorname{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}} \\
 & \quad \left. \sqrt{b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]]} \right) / \\
 & \left( 3 (a^2 - b^2) d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} \right. \\
 & \quad \left. \sqrt{\sec [c + d x]} (a + b \sec [c + d x])^{3/2} \right) - \\
 & \left( 8 b^2 B \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right. \\
 & \quad \left. \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( -1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right] (b + a \cos [c + d x])^{3/2} \\
 & \quad \csc [c] (A + B \sec [c + d x] + C \sec [c + d x]^2) \sec [d x - \operatorname{ArcTan} [\cot [c]]] \\
 & \quad \sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \operatorname{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}}
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{\sqrt{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}}{a \sqrt{1 + \cot [c]^2} + b \csc [c]} \right. \\
 & \left. \frac{\sqrt{b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]]}}{\right) / \\
 & \left( 3 a^2 (a^2 - b^2) d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \left. \sqrt{1 + \cot [c]^2} \sqrt{\sec [c + d x]} (a + b \sec [c + d x])^{3/2} \right) + \\
 & \left( 4 b C \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right. \\
 & \left. \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( -1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right] (b + a \cos [c + d x])^{3/2} \\
 & \csc [c] (A + B \sec [c + d x] + C \sec [c + d x]^2) \sec [d x - \text{ArcTan} [\cot [c]]] \\
 & \left( \frac{\sqrt{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}}{a \sqrt{1 + \cot [c]^2} - b \csc [c]} \right. \\
 & \left. \frac{\sqrt{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}}{a \sqrt{1 + \cot [c]^2} + b \csc [c]} \right. \\
 & \left. \frac{\sqrt{b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]]}}{\right) / \\
 & \left( a (a^2 - b^2) d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} \right. \\
 & \left. \sqrt{\sec [c + d x]} (a + b \sec [c + d x])^{3/2} \right) - \\
 & \left( 6 a A (b + a \cos [c + d x])^{3/2} \csc [c] (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \left. \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \sec [c] (b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]) \right) \right] \right) \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \left. \left. \sqrt{1 + \tan[c]^2} \right) \right) \right) \right) \left/ \left( a \sqrt{1 + \tan[c]^2} \left( 1 - \frac{b \sec[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \right), \\
 & - \left( \left( \sec[c] \left( b + a \cos[c] \cos[d x + \operatorname{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2} \right) \right) \right) \left/ \right. \\
 & \left. \left( a \sqrt{1 + \tan[c]^2} \left( -1 - \frac{b \sec[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \right) \left. \sin[d x + \operatorname{ArcTan}[\tan[c]]] \tan[c] \right) \left/ \right. \\
 & \left( \sqrt{1 + \tan[c]^2} \sqrt{\left( \left( a \sqrt{1 + \tan[c]^2} - a \cos[d x + \operatorname{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2} \right) \right) \right) \left/ \right. \\
 & \left. \left( b \sec[c] + a \sqrt{1 + \tan[c]^2} \right) \right) \sqrt{\left( \left( a \sqrt{1 + \tan[c]^2} + \right. \right. \\
 & \left. \left. a \cos[d x + \operatorname{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2} \right) \right) \left/ \left( -b \sec[c] + a \sqrt{1 + \tan[c]^2} \right) \right) \\
 & \left. \sqrt{b + a \cos[c] \cos[d x + \operatorname{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}} \right) - \\
 & \left( \frac{\sin[d x + \operatorname{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \left( 2 a \cos[c] \left( b + a \cos[c] \cos \right. \right. \right. \\
 & \left. \left. \left. d x + \operatorname{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2} \right) \right) \left/ \left( a^2 \cos[c]^2 + a^2 \sin[c]^2 \right) \right) \left/ \right. \\
 & \left. \left( \sqrt{b + a \cos[c] \cos[d x + \operatorname{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}} \right) \right) \left. \right) \left/ \right. \\
 & \left( 5 (a^2 - b^2) d (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) \sqrt{\sec[c + d x]} (a + b \sec[c + d x])^{3/2} \right) - \\
 & \left( 16 A b^2 (b + a \cos[c + d x])^{3/2} \operatorname{Csc}[c] (A + B \sec[c + d x] + C \sec[c + d x]^2) \right. \\
 & \left. \left( \left( \operatorname{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \sec[c] \left( b + a \cos[c] \cos[d x + \operatorname{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2} \right) \right) \right] \right) \right) \right. \right. \\
 & \left. \left. \sqrt{1 + \tan[c]^2} \right) \right) \left/ \left( a \sqrt{1 + \tan[c]^2} \left( 1 - \frac{b \sec[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \right), \\
 & - \left( \left( \sec[c] \left( b + a \cos[c] \cos[d x + \operatorname{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2} \right) \right) \right) \left/ \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( a \sqrt{1 + \tan[c]^2} \left( -1 - \frac{b \operatorname{Sec}[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \left[ \sin[d x + \operatorname{ArcTan}[\tan[c]]] \tan[c] \right] / \\
 & \left( \sqrt{1 + \tan[c]^2} \sqrt{\left( \left( a \sqrt{1 + \tan[c]^2} - a \cos[d x + \operatorname{ArcTan}[\tan[c]]] \right) \sqrt{1 + \tan[c]^2} \right) / \right. \\
 & \left. \left( b \operatorname{Sec}[c] + a \sqrt{1 + \tan[c]^2} \right) \sqrt{\left( \left( a \sqrt{1 + \tan[c]^2} + \right. \right. \right. \\
 & \left. \left. \left. a \cos[d x + \operatorname{ArcTan}[\tan[c]]] \right) \sqrt{1 + \tan[c]^2} \right) / \left( -b \operatorname{Sec}[c] + a \sqrt{1 + \tan[c]^2} \right) \right) \\
 & \left. \sqrt{b + a \cos[c] \cos[d x + \operatorname{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}} \right) - \\
 & \left( \frac{\sin[d x + \operatorname{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \left( 2 a \cos[c] \left( b + a \cos[c] \cos[ \right. \right. \right. \\
 & \left. \left. \left. d x + \operatorname{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2} \right) \right) / \left( a^2 \cos[c]^2 + a^2 \sin[c]^2 \right) \right) / \\
 & \left( \sqrt{b + a \cos[c] \cos[d x + \operatorname{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}} \right) \left. \right) \left. \right) / \\
 & \left( 5 a \left( a^2 - b^2 \right) d \left( A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x] \right) \sqrt{\operatorname{Sec}[c + d x]} \right. \\
 & \left. \left( a + b \operatorname{Sec}[c + d x] \right)^{3/2} \right) + \\
 & \left( 32 A b^4 \left( b + a \cos[c + d x] \right)^{3/2} \operatorname{Csc}[c] \left( A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2 \right) \right. \\
 & \left. \left( \left( \operatorname{AppellF1}\left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, -\left( \operatorname{Sec}[c] \left( b + a \cos[c] \cos[d x + \operatorname{ArcTan}[\tan[c]]] \right) \right) \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \sqrt{1 + \tan[c]^2} \right) \right) / \left( a \sqrt{1 + \tan[c]^2} \left( 1 - \frac{b \operatorname{Sec}[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \right) \right) \left. \right) \left. \right) / \\
 & - \left( \left( \operatorname{Sec}[c] \left( b + a \cos[c] \cos[d x + \operatorname{ArcTan}[\tan[c]]] \right) \sqrt{1 + \tan[c]^2} \right) \right) / \\
 & \left( a \sqrt{1 + \tan[c]^2} \left( -1 - \frac{b \operatorname{Sec}[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \left[ \sin[d x + \operatorname{ArcTan}[\tan[c]]] \tan[c] \right] / \\
 & \left( \sqrt{1 + \tan[c]^2} \sqrt{\left( \left( a \sqrt{1 + \tan[c]^2} - a \cos[d x + \operatorname{ArcTan}[\tan[c]]] \right) \sqrt{1 + \tan[c]^2} \right) / \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( b \operatorname{Sec}[c] + a \sqrt{1 + \operatorname{Tan}[c]^2} \right) \sqrt{\left( \left( a \sqrt{1 + \operatorname{Tan}[c]^2} + \right. \right. \\
 & \quad \left. \left. a \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2} \right) / \left( -b \operatorname{Sec}[c] + a \sqrt{1 + \operatorname{Tan}[c]^2} \right) \right)} \\
 & \sqrt{b + a \operatorname{Cos}[c] \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}} \Big) - \\
 & \left( \frac{\operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1 + \operatorname{Tan}[c]^2}} + \left( 2 a \operatorname{Cos}[c] \left( b + a \operatorname{Cos}[c] \operatorname{Cos}[ \right. \right. \right. \\
 & \quad \left. \left. \left. d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2} \right) \right) / \left( a^2 \operatorname{Cos}[c]^2 + a^2 \operatorname{Sin}[c]^2 \right) \right) / \\
 & \left( \sqrt{b + a \operatorname{Cos}[c] \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}} \right) \Big) / \\
 & \left( 5 a^3 (a^2 - b^2) d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{\operatorname{Sec}[c + d x]} \right. \\
 & \quad \left. (a + b \operatorname{Sec}[c + d x])^{3/2} \right) + \\
 & \left( 10 b B (b + a \operatorname{Cos}[c + d x])^{3/2} \operatorname{Csc}[c] (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \left. \left( \left( \operatorname{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, -\left( \operatorname{Sec}[c] \left( b + a \operatorname{Cos}[c] \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \right) \right) \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \operatorname{Tan}[c]^2} \right) \right) / \left( a \sqrt{1 + \operatorname{Tan}[c]^2} \left( 1 - \frac{b \operatorname{Sec}[c]}{a \sqrt{1 + \operatorname{Tan}[c]^2}} \right) \right) \right) \Big), \\
 & - \left( \left( \operatorname{Sec}[c] \left( b + a \operatorname{Cos}[c] \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2} \right) \right) / \right. \\
 & \quad \left. \left( a \sqrt{1 + \operatorname{Tan}[c]^2} \left( -1 - \frac{b \operatorname{Sec}[c]}{a \sqrt{1 + \operatorname{Tan}[c]^2}} \right) \right) \right) \operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] \Big) / \\
 & \left( \sqrt{1 + \operatorname{Tan}[c]^2} \sqrt{\left( \left( a \sqrt{1 + \operatorname{Tan}[c]^2} - a \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2} \right) / \right. \right. \\
 & \quad \left. \left. \left( b \operatorname{Sec}[c] + a \sqrt{1 + \operatorname{Tan}[c]^2} \right) \right) \sqrt{\left( \left( a \sqrt{1 + \operatorname{Tan}[c]^2} + \right. \right. \right. \\
 & \quad \left. \left. \left. a \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2} \right) / \left( -b \operatorname{Sec}[c] + a \sqrt{1 + \operatorname{Tan}[c]^2} \right) \right) \right)} \\
 & \sqrt{b + a \operatorname{Cos}[c] \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}} \Big) -
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{\sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \left( 2 a \cos [c] \left( b + a \cos [c] \cos [ \right. \right. \right. \\
 & \quad \left. \left. \left. d x + \text{ArcTan}[\text{Tan}[c]] \right] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a^2 \cos [c]^2 + a^2 \sin [c]^2 \right) \Bigg) / \\
 & \left( \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) \Bigg) / \\
 & \left( 3 \left( a^2 - b^2 \right) d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \sqrt{\text{Sec}[c + d x]} \right. \\
 & \quad \left. (a + b \text{Sec}[c + d x])^{3/2} \right) - \\
 & \left( 16 b^3 B \left( b + a \cos [c + d x] \right)^{3/2} \text{Csc}[c] \left( A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2 \right) \right. \\
 & \quad \left. \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \text{Sec}[c] \left( b + a \cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]] \right] \right) \right. \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a \sqrt{1 + \text{Tan}[c]^2} \left( 1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \Bigg), \\
 & \quad - \left( \left( \text{Sec}[c] \left( b + a \cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \right. \\
 & \quad \left. \left( a \sqrt{1 + \text{Tan}[c]^2} \left( -1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \Bigg] \sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] \Bigg) / \\
 & \left( \sqrt{1 + \text{Tan}[c]^2} \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} - a \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) / \right. \right. \\
 & \quad \left. \left. \left( b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} + \right. \right. \right. \\
 & \quad \left. \left. \left. a \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( -b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) \right) \\
 & \quad \left. \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) - \\
 & \left( \frac{\sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \left( 2 a \cos [c] \left( b + a \cos [c] \cos [ \right. \right. \right. \\
 & \quad \left. \left. \left. d x + \text{ArcTan}[\text{Tan}[c]] \right] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a^2 \cos [c]^2 + a^2 \sin [c]^2 \right) \Bigg) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]]} \sqrt{1 + \tan [c]^2} \right) \Bigg) \Bigg) \Bigg) / \\
 & \left( 3 a^2 (a^2 - b^2) d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. \sqrt{\sec [c + d x]} \right. \\
 & \quad \left. (a + b \sec [c + d x])^{3/2} \right) - \\
 & \left( 2 a C (b + a \cos [c + d x])^{3/2} \csc [c] (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \sec [c] (b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]) \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. \sqrt{1 + \tan [c]^2} \right) \right) \right] / \left( a \sqrt{1 + \tan [c]^2} \left( 1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right) \Bigg) \Bigg) \Bigg) / \\
 & \quad - \left( \left( \sec [c] (b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) \right) \Bigg) \Bigg) / \\
 & \quad \left( a \sqrt{1 + \tan [c]^2} \left( -1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \Bigg) \Bigg) \left[ \sin [d x + \text{ArcTan} [\tan [c]]] \tan [c] \right] \Bigg) \Bigg) / \\
 & \quad \left( \sqrt{1 + \tan [c]^2} \sqrt{\left( (a \sqrt{1 + \tan [c]^2} - a \cos [d x + \text{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) \right) \Bigg) \Bigg) / \\
 & \quad \left( b \sec [c] + a \sqrt{1 + \tan [c]^2} \right) \sqrt{\left( (a \sqrt{1 + \tan [c]^2} + \right. \\
 & \quad \left. a \cos [d x + \text{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) \Bigg) \Bigg) / \left( -b \sec [c] + a \sqrt{1 + \tan [c]^2} \right) \Bigg) \Bigg) \\
 & \quad \left. \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]]} \sqrt{1 + \tan [c]^2} \right) \Bigg) - \\
 & \quad \left( \frac{\sin [d x + \text{ArcTan} [\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \left( 2 a \cos [c] (b + a \cos [c] \cos [ \right. \right. \\
 & \quad \left. \left. d x + \text{ArcTan} [\tan [c]] \right) \sqrt{1 + \tan [c]^2} \right) \Bigg) \Bigg) / (a^2 \cos [c]^2 + a^2 \sin [c]^2) \Bigg) \Bigg) \Bigg) / \\
 & \quad \left( \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]]} \sqrt{1 + \tan [c]^2} \right) \Bigg) \Bigg) \Bigg) / \\
 & \left( (a^2 - b^2) d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. \sqrt{\sec [c + d x]} \right. \\
 & \quad \left. (a + b \sec [c + d x])^{3/2} \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left( 4 b^2 C (b + a \cos [c + d x])^{3/2} \operatorname{Csc}[c] (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \left. \left( \left( \operatorname{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, -\left(\operatorname{Sec}[c] (b + a \cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]])\right)\right] \right. \right. \right. \\
 & \left. \left. \left. \sqrt{1 + \tan [c]^2} \right) \right) / \left( a \sqrt{1 + \tan [c]^2} \left( 1 - \frac{b \operatorname{Sec}[c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right), \\
 & - \left( \left( \operatorname{Sec}[c] (b + a \cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]) \sqrt{1 + \tan [c]^2} \right) \right) / \\
 & \left( a \sqrt{1 + \tan [c]^2} \left( -1 - \frac{b \operatorname{Sec}[c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right) \operatorname{Sin}[d x + \operatorname{ArcTan}[\tan [c]]] \operatorname{Tan}[c] \Big/ \\
 & \left( \sqrt{1 + \tan [c]^2} \sqrt{\left( (a \sqrt{1 + \tan [c]^2} - a \cos [d x + \operatorname{ArcTan}[\tan [c]]) \sqrt{1 + \tan [c]^2} \right) \right) / \\
 & \left( b \operatorname{Sec}[c] + a \sqrt{1 + \tan [c]^2} \right) \sqrt{\left( (a \sqrt{1 + \tan [c]^2} + \right. \\
 & \left. a \cos [d x + \operatorname{ArcTan}[\tan [c]]) \sqrt{1 + \tan [c]^2} \right) / \left( -b \operatorname{Sec}[c] + a \sqrt{1 + \tan [c]^2} \right) \Big)} \\
 & \left. \sqrt{b + a \cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]) \sqrt{1 + \tan [c]^2}} \right) - \\
 & \left( \frac{\operatorname{Sin}[d x + \operatorname{ArcTan}[\tan [c]]] \operatorname{Tan}[c]}{\sqrt{1 + \tan [c]^2}} + \left( 2 a \cos [c] (b + a \cos [c] \cos [ \right. \right. \\
 & \left. \left. d x + \operatorname{ArcTan}[\tan [c]]) \sqrt{1 + \tan [c]^2} \right) \right) / \left( a^2 \cos [c]^2 + a^2 \sin [c]^2 \right) \Big/ \\
 & \left( \sqrt{b + a \cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]) \sqrt{1 + \tan [c]^2}} \right) \Big/ \\
 & \left( a (a^2 - b^2) d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \left. \sqrt{\operatorname{Sec}[c + d x]} \right. \\
 & \left. (a + b \operatorname{Sec}[c + d x])^{3/2} \right)
 \end{aligned}$$

**Problem 1064: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\operatorname{Sec}[c + d x]^{5/2} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{(a + b \operatorname{Sec}[c + d x])^{5/2}} dx$$



Optimal (type 4, 563 leaves, 14 steps):

$$\begin{aligned}
 & \left( (2 A b^2 - 2 a b B + 5 a^2 C - 3 b^2 C) \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \right. \\
 & \quad \left. \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \sqrt{\operatorname{Sec}[c + d x]} \right) / \left( 3 b^2 (a^2 - b^2) d \sqrt{a + b \operatorname{Sec}[c + d x]} \right) + \\
 & \left( (2 b B - 5 a C) \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \sqrt{\operatorname{Sec}[c + d x]} \right) / \\
 & \quad \left( b^3 d \sqrt{a + b \operatorname{Sec}[c + d x]} \right) + \\
 & \left( (8 A b^4 + 6 a^3 b B - 14 a b^3 B - 15 a^4 C + 26 a^2 b^2 C - 3 b^4 C) \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right. \\
 & \quad \left. \sqrt{a + b \operatorname{Sec}[c + d x]} \right) / \left( 3 b^3 (a^2 - b^2)^2 d \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \sqrt{\operatorname{Sec}[c + d x]} \right) - \\
 & \frac{2 (A b^2 - a (b B - a C)) \operatorname{Sec}[c + d x]^{5/2} \operatorname{Sin}[c + d x]}{3 b (a^2 - b^2) d (a + b \operatorname{Sec}[c + d x])^{3/2}} + \\
 & \left( 2 (3 A b^4 + 2 a^3 b B - 6 a b^3 B - 5 a^4 C + a^2 b^2 (A + 9 C)) \operatorname{Sec}[c + d x]^{3/2} \operatorname{Sin}[c + d x] \right) / \\
 & \quad \left( 3 b^2 (a^2 - b^2)^2 d \sqrt{a + b \operatorname{Sec}[c + d x]} \right) - \frac{1}{3 b^3 (a^2 - b^2)^2 d} \\
 & \frac{(8 A b^4 + 6 a^3 b B - 14 a b^3 B - 15 a^4 C + 26 a^2 b^2 C - 3 b^4 C)}{\sqrt{\operatorname{Sec}[c + d x]} \sqrt{a + b \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}
 \end{aligned}$$

Result (type 4, 938 leaves):

$$\begin{aligned}
 & - \left( \left( (b + a \operatorname{Cos}[c + d x])^{5/2} \sqrt{\operatorname{Sec}[c + d x]} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \right. \\
 & \quad \left. \left( 2 (-4 a^2 A b^3 - 12 A b^5 - 8 a^3 b^2 B + 24 a b^4 B + 20 a^4 b C - 36 a^2 b^3 C) \right. \right. \\
 & \quad \left. \left. \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right) / \left( \sqrt{b + a \operatorname{Cos}[c + d x]} \right) + \right. \\
 & \quad \left. \left( 2 (-8 a A b^4 - 18 a^4 b B + 38 a^2 b^3 B - 12 b^5 B + 45 a^5 C - 86 a^3 b^2 C + 33 a b^4 C) \right. \right. \\
 & \quad \left. \left. \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right) / \left( \sqrt{b + a \operatorname{Cos}[c + d x]} \right) + \right.
 \end{aligned}$$

$$\left( 2 i \left( -8 a A b^4 - 6 a^4 b B + 14 a^2 b^3 B + 15 a^5 C - 26 a^3 b^2 C + 3 a b^4 C \right) \right. \\ \left. \sqrt{\frac{a - a \cos [c + d x]}{a + b}} \sqrt{\frac{a + a \cos [c + d x]}{a - b}} \cos [2 (c + d x)] \right. \\ \left. \left( -2 b (a + b) \operatorname{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \sqrt{\frac{1}{a - b}} \sqrt{b + a \cos [c + d x]} \right], \frac{-a + b}{a + b} \right] + \right. \right. \\ \left. \left. a \left( 2 b \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \sqrt{\frac{1}{a - b}} \sqrt{b + a \cos [c + d x]} \right], \frac{-a + b}{a + b} \right] + \right. \right. \right. \\ \left. \left. \left. a \operatorname{EllipticPi} \left[ 1 - \frac{a}{b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{1}{a - b}} \sqrt{b + a \cos [c + d x]} \right], \frac{-a + b}{a + b} \right] \right) \right) \right) \\ \left. \sin [c + d x] \right) / \left( \sqrt{\frac{1}{a - b}} b \sqrt{1 - \cos [c + d x]}^2 \sqrt{\frac{a^2 - a^2 \cos [c + d x]^2}{a^2}} \right. \\ \left. \left( -a^2 + 2 b^2 - 4 b (b + a \cos [c + d x]) + 2 (b + a \cos [c + d x])^2 \right) \right) / \\ \left( 6 (a - b)^2 b^3 (a + b)^2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\ \left. (a + b \sec [c + d x])^{5/2} \right) + \\ \left( (b + a \cos [c + d x])^3 \sqrt{\sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\ \left( -\frac{4 (a A b^2 \sin [c + d x] - a^2 b B \sin [c + d x] + a^3 C \sin [c + d x])}{3 b^2 (-a^2 + b^2) (b + a \cos [c + d x])^2} - \right. \\ \left. (4 (4 a A b^4 \sin [c + d x] + 3 a^4 b B \sin [c + d x] - 7 a^2 b^3 B \sin [c + d x] - 6 a^5 C \sin [c + d x] + \right. \\ \left. 10 a^3 b^2 C \sin [c + d x])) / (3 b^3 (-a^2 + b^2)^2 (b + a \cos [c + d x])) + \frac{2 C \tan [c + d x]}{b^3} \right) / \\ \left. (d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^{5/2}) \right) /$$

**Problem 1065: Unable to integrate problem.**

$$\int \frac{\sec [c + d x]^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2)}{(a + b \sec [c + d x])^{5/2}} dx$$

Optimal (type 4, 447 leaves, 13 steps):

$$\begin{aligned}
 & - \left( \left( 2 (A b^2 - a (b B - a C)) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{\sec [c + d x]} \right) / \right. \\
 & \quad \left. (3 a b (a^2 - b^2) d \sqrt{a + b \sec [c + d x]}) \right) + \\
 & \frac{2 C \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticPi}\left[2, \frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{\sec [c + d x]}}{b^2 d \sqrt{a + b \sec [c + d x]}} - \\
 & \left( 2 (A b^4 - 4 a b^3 B - 3 a^4 C + a^2 b^2 (3 A + 7 C)) \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \sec [c + d x]} \right) / \\
 & \left( 3 a b^2 (a^2 - b^2)^2 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \sqrt{\sec [c + d x]} \right) - \\
 & \frac{2 (A b^2 - a (b B - a C)) \sec [c + d x]^{3/2} \sin [c + d x]}{3 b (a^2 - b^2) d (a + b \sec [c + d x])^{3/2}} + \\
 & \left( 2 (A b^4 - 4 a b^3 B - 3 a^4 C + a^2 b^2 (3 A + 7 C)) \sqrt{\sec [c + d x]} \sin [c + d x] \right) / \\
 & \left( 3 b^2 (a^2 - b^2)^2 d \sqrt{a + b \sec [c + d x]} \right)
 \end{aligned}$$

Result (type 8, 47 leaves):

$$\int \frac{\sec [c + d x]^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2)}{(a + b \sec [c + d x])^{5/2}} dx$$

**Problem 1066: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2)}{(a + b \sec [c + d x])^{5/2}} dx$$

Optimal (type 4, 378 leaves, 9 steps):

$$\begin{aligned}
 & - \left( \left( 2 (2 A b^2 + a b B - a^2 (3 A + C)) \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \right. \right. \\
 & \quad \left. \left. \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \sqrt{\operatorname{Sec}[c + d x]} \right) / \left( 3 a^2 (a^2 - b^2) d \sqrt{a + b \operatorname{Sec}[c + d x]} \right) \right) - \\
 & \left( 2 (2 A b^3 + 3 a^3 B + a b^2 B - 2 a^2 b (3 A + 2 C)) \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \operatorname{Sec}[c + d x]} \right) / \\
 & \left( 3 a^2 (a^2 - b^2)^2 d \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \sqrt{\operatorname{Sec}[c + d x]} \right) - \\
 & \frac{2 (A b^2 - a (b B - a C)) \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{3 b (a^2 - b^2) d (a + b \operatorname{Sec}[c + d x])^{3/2}} + \\
 & \left( 2 (A b^4 + 2 a^3 b B + 2 a b^3 B + a^4 C - 5 a^2 b^2 (A + C)) \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x] \right) / \\
 & \left( 3 a b (a^2 - b^2)^2 d \sqrt{a + b \operatorname{Sec}[c + d x]} \right)
 \end{aligned}$$

Result (type 6, 5040 leaves):

$$\begin{aligned}
 & \frac{1}{(A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) (a + b \operatorname{Sec}[c + d x])^{5/2}} \\
 & (b + a \operatorname{Cos}[c + d x])^3 \sqrt{\operatorname{Sec}[c + d x]} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\
 & \left( \frac{4 (-6 a^2 A b + 2 A b^3 + 3 a^3 B + a b^2 B - 4 a^2 b C) \operatorname{Csc}[c] \operatorname{Sec}[c]}{3 a^2 (a^2 - b^2)^2 d} - \right. \\
 & \quad (4 \operatorname{Sec}[c] (A b^3 \operatorname{Sin}[c] - a b^2 B \operatorname{Sin}[c] + a^2 b C \operatorname{Sin}[c] - a A b^2 \operatorname{Sin}[d x] + \\
 & \quad \quad a^2 b B \operatorname{Sin}[d x] - a^3 C \operatorname{Sin}[d x])) / (3 a^2 (a^2 - b^2) d (b + a \operatorname{Cos}[c + d x])^2) + \\
 & \quad (4 \operatorname{Sec}[c] (7 a^2 A b^2 \operatorname{Sin}[c] - 3 A b^4 \operatorname{Sin}[c] - 4 a^3 b B \operatorname{Sin}[c] + a^4 C \operatorname{Sin}[c] + \\
 & \quad \quad 3 a^2 b^2 C \operatorname{Sin}[c] - 6 a^3 A b \operatorname{Sin}[d x] + 2 a A b^3 \operatorname{Sin}[d x] + 3 a^4 B \operatorname{Sin}[d x] + \\
 & \quad \quad a^2 b^2 B \operatorname{Sin}[d x] - 4 a^3 b C \operatorname{Sin}[d x])) / (3 a^2 (a^2 - b^2)^2 d (b + a \operatorname{Cos}[c + d x])) \left. \right) - \\
 & \left( 4 a A \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\operatorname{Csc}[c] (b - a \sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]])]}{a \sqrt{1 + \operatorname{Cot}[c]^2} \left(1 + \frac{b \operatorname{Csc}[c]}{a \sqrt{1 + \operatorname{Cot}[c]^2}\right)}\right]}{a \sqrt{1 + \operatorname{Cot}[c]^2} \left(-1 + \frac{b \operatorname{Csc}[c]}{a \sqrt{1 + \operatorname{Cot}[c]^2}\right)}\right]} \right) \\
 & \frac{\operatorname{Csc}[c] (b - a \sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]])]}{a \sqrt{1 + \operatorname{Cot}[c]^2} \left(-1 + \frac{b \operatorname{Csc}[c]}{a \sqrt{1 + \operatorname{Cot}[c]^2}\right)}\right)}{(b + a \operatorname{Cos}[c + d x])^{5/2} \operatorname{Csc}[c] \sqrt{\operatorname{Sec}[c + d x]} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}
 \end{aligned}$$

$$\begin{aligned}
 & \left. \begin{aligned}
 & \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} - b \text{Csc}[c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} + a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} + b \text{Csc}[c]}} \\
 & \sqrt{b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \Big/
 \end{aligned} \right) \\
 & \left( (a^2 - b^2)^2 d (A + 2C + 2B \text{Cos}[c + dx] + A \text{Cos}[2c + 2dx]) \sqrt{1 + \text{Cot}[c]^2} (a + b \text{Sec}[c + dx])^{5/2} \right) - \\
 & \left( 4 A b^2 \text{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( 1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2} \right)}\right], \right. \\
 & \left. \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( -1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2} \right)} \right) \right] \\
 & (b + a \text{Cos}[c + dx])^{5/2} \text{Csc}[c] \sqrt{\text{Sec}[c + dx]} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \\
 & \left. \begin{aligned}
 & \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} - b \text{Csc}[c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} + a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} + b \text{Csc}[c]}} \\
 & \sqrt{b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \Big/
 \end{aligned} \right) \\
 & \left( 3 a (a^2 - b^2)^2 d (A + 2C + 2B \text{Cos}[c + dx] + A \text{Cos}[2c + 2dx]) \sqrt{1 + \text{Cot}[c]^2} (a + b \text{Sec}[c + dx])^{5/2} \right) + \\
 & \left( 16 b B \text{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( 1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2} \right)}\right], \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( -1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \right] \\
 & (b + a \text{Cos}[c + dx])^{5/2} \text{Csc}[c] \sqrt{\text{Sec}[c + dx]} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \\
 & \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} - b \text{Csc}[c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} + a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} + b \text{Csc}[c]}} \\
 & \left. \sqrt{b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right) / \\
 & \left( 3 (a^2 - b^2)^2 d (A + 2C + 2B \text{Cos}[c + dx] + A \text{Cos}[2c + 2dx]) \sqrt{1 + \text{Cot}[c]^2} (a + b \text{Sec}[c + dx])^{5/2} \right) - \\
 & \left( 4 a \text{C AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( 1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \right], \right. \\
 & \left. \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( -1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \right] \\
 & (b + a \text{Cos}[c + dx])^{5/2} \text{Csc}[c] \sqrt{\text{Sec}[c + dx]} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \\
 & \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} - b \text{Csc}[c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} + a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} + b \text{Csc}[c]}} \\
 & \left. \sqrt{b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right) / \\
 & \left( 3 (a^2 - b^2)^2 d (A + 2C + 2B \text{Cos}[c + dx] + A \text{Cos}[2c + 2dx]) \sqrt{1 + \text{Cot}[c]^2} (a + b \text{Sec}[c + dx])^{5/2} \right) -
 \end{aligned}$$

$$\left( 4 b^2 C \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\operatorname{Csc}[c] \left( b - a \sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \right)}{a \sqrt{1 + \operatorname{Cot}[c]^2} \left( 1 + \frac{b \operatorname{Csc}[c]}{a \sqrt{1 + \operatorname{Cot}[c]^2}} \right)} \right], \right.$$

$$\left. \frac{\operatorname{Csc}[c] \left( b - a \sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \right)}{a \sqrt{1 + \operatorname{Cot}[c]^2} \left( -1 + \frac{b \operatorname{Csc}[c]}{a \sqrt{1 + \operatorname{Cot}[c]^2}} \right)} \right]$$

$$(b + a \operatorname{Cos}[c + d x])^{5/2} \operatorname{Csc}[c] \sqrt{\operatorname{Sec}[c + d x]} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)$$

$$\operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{\frac{a \sqrt{1 + \operatorname{Cot}[c]^2} - a \sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}{a \sqrt{1 + \operatorname{Cot}[c]^2} - b \operatorname{Csc}[c]}}$$

$$\sqrt{\frac{a \sqrt{1 + \operatorname{Cot}[c]^2} + a \sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}{a \sqrt{1 + \operatorname{Cot}[c]^2} + b \operatorname{Csc}[c]}}$$

$$\sqrt{b - a \sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \Big/$$

$$\left( a (a^2 - b^2)^2 d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2} (a + b \operatorname{Sec}[c + d x])^{5/2} \right) -$$

$$\left( 4 a A b (b + a \operatorname{Cos}[c + d x])^{5/2} \operatorname{Csc}[c] \sqrt{\operatorname{Sec}[c + d x]} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right.$$

$$\left. \left( \left( \operatorname{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \operatorname{Sec}[c] \left( b + a \operatorname{Cos}[c] \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \right) \sqrt{1 + \operatorname{Tan}[c]^2} \right) \right] \right) \Big/ \left( a \sqrt{1 + \operatorname{Tan}[c]^2} \left( 1 - \frac{b \operatorname{Sec}[c]}{a \sqrt{1 + \operatorname{Tan}[c]^2}} \right) \right) \right) \right),$$

$$- \left( \left( \operatorname{Sec}[c] \left( b + a \operatorname{Cos}[c] \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \right) \sqrt{1 + \operatorname{Tan}[c]^2} \right) \right) \Big/$$

$$\left( a \sqrt{1 + \operatorname{Tan}[c]^2} \left( -1 - \frac{b \operatorname{Sec}[c]}{a \sqrt{1 + \operatorname{Tan}[c]^2}} \right) \right) \Big] \operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] \Big/$$

$$\left( \sqrt{1 + \operatorname{Tan}[c]^2} \sqrt{\left( \left( a \sqrt{1 + \operatorname{Tan}[c]^2} - a \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \right) \sqrt{1 + \operatorname{Tan}[c]^2} \right)} \Big/$$

$$\left( b \operatorname{Sec}[c] + a \sqrt{1 + \operatorname{Tan}[c]^2} \right) \Big] \sqrt{\left( \left( a \sqrt{1 + \operatorname{Tan}[c]^2} + \right. \right.$$

$$\begin{aligned}
 & \left( \frac{a \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}}{-b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2}} \right) \\
 & \left( \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) - \\
 & \left( \frac{\sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \left( 2 a \cos [c] \left( b + a \cos [c] \cos [ \right. \right. \right. \\
 & \left. \left. \left. d x + \text{ArcTan}[\text{Tan}[c]] \right] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a^2 \cos [c]^2 + a^2 \sin [c]^2 \right) \right) / \\
 & \left( \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) \Big) / \\
 & \left( (a^2 - b^2)^2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \text{Sec}[c + d x])^{5/2} + \right. \\
 & \left. 4 A b^3 (b + a \cos [c + d x])^{5/2} \text{Csc}[c] \sqrt{\text{Sec}[c + d x]} (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) \right. \\
 & \left. \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \text{Sec}[c] \left( b + a \cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]] \right] \right. \right. \right. \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a \sqrt{1 + \text{Tan}[c]^2} \left( 1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \Big), \\
 & - \left( \left( \text{Sec}[c] \left( b + a \cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \right. \\
 & \left. \left( a \sqrt{1 + \text{Tan}[c]^2} \left( -1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \Big) \sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] \Big) / \\
 & \left( \sqrt{1 + \text{Tan}[c]^2} \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} - a \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) / \right. \right. \\
 & \left. \left. \left( b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} + \right. \right. \right. \\
 & \left. \left. \left. a \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( -b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) \Big) \\
 & \left( \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) - \\
 & \left( \frac{\sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \left( 2 a \cos [c] \left( b + a \cos [c] \cos [ \right. \right. \right.
 \end{aligned}$$





$$\begin{aligned}
 & \left( 2 b^2 B (b + a \cos [c + d x])^{5/2} \operatorname{Csc}[c] \sqrt{\operatorname{Sec}[c + d x]} \right. \\
 & \quad \left. (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \quad \left( \left( \operatorname{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, -\left( \operatorname{Sec}[c] \left( b + a \cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]] \right) \right) \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \operatorname{Tan}[c]^2} \right) \right) \right) / \left( a \sqrt{1 + \operatorname{Tan}[c]^2} \left( 1 - \frac{b \operatorname{Sec}[c]}{a \sqrt{1 + \operatorname{Tan}[c]^2}} \right) \right) \right), \\
 & \quad - \left( \left( \operatorname{Sec}[c] \left( b + a \cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]] \right) \right) \sqrt{1 + \operatorname{Tan}[c]^2} \right) / \right. \\
 & \quad \left. \left( a \sqrt{1 + \operatorname{Tan}[c]^2} \left( -1 - \frac{b \operatorname{Sec}[c]}{a \sqrt{1 + \operatorname{Tan}[c]^2}} \right) \right) \right) \operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] \Big/ \\
 & \quad \left( \sqrt{1 + \operatorname{Tan}[c]^2} \sqrt{\left( \left( a \sqrt{1 + \operatorname{Tan}[c]^2} - a \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]] \right) \sqrt{1 + \operatorname{Tan}[c]^2} \right) / \right. \\
 & \quad \left. \left( b \operatorname{Sec}[c] + a \sqrt{1 + \operatorname{Tan}[c]^2} \right) \right) \sqrt{\left( \left( a \sqrt{1 + \operatorname{Tan}[c]^2} + \right. \right. \\
 & \quad \left. \left. a \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]] \right) \sqrt{1 + \operatorname{Tan}[c]^2} \right) / \left( -b \operatorname{Sec}[c] + a \sqrt{1 + \operatorname{Tan}[c]^2} \right) \right) \\
 & \quad \left. \sqrt{b + a \cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}} \right) - \\
 & \quad \left( \frac{\operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1 + \operatorname{Tan}[c]^2}} + \left( 2 a \cos [c] \left( b + a \cos [c] \cos [ \right. \right. \right. \\
 & \quad \left. \left. \left. d x + \operatorname{ArcTan}[\operatorname{Tan}[c]] \right) \sqrt{1 + \operatorname{Tan}[c]^2} \right) \right) / \left( a^2 \cos [c]^2 + a^2 \sin [c]^2 \right) \Big/ \\
 & \quad \left( \sqrt{b + a \cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}} \right) \Big/ \\
 & \quad \left( 3 (a^2 - b^2)^2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. (a + b \operatorname{Sec}[c + d x])^{5/2} \right) - \\
 & \quad \left( 8 a b C (b + a \cos [c + d x])^{5/2} \operatorname{Csc}[c] \sqrt{\operatorname{Sec}[c + d x]} \right. \\
 & \quad \left. (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \right] \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a \sqrt{1 + \text{Tan}[c]^2} \left( 1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right), \\
 & - \left( \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \right] \sqrt{1 + \text{Tan}[c]^2} \right) / \right. \\
 & \quad \left. \left( a \sqrt{1 + \text{Tan}[c]^2} \left( -1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] \Big/ \\
 & \left( \sqrt{1 + \text{Tan}[c]^2} \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} - a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \sqrt{1 + \text{Tan}[c]^2} \right) / \right. \\
 & \quad \left. \left( b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} + \right. \right. \right. \\
 & \quad \left. \left. \left. a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \sqrt{1 + \text{Tan}[c]^2} \right) / \left( -b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) \\
 & \quad \left. \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) - \\
 & \left( \frac{\text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \left( 2 a \text{Cos}[c] \left( b + a \text{Cos}[c] \text{Cos}[ \right. \right. \right. \\
 & \quad \left. \left. \left. dx + \text{ArcTan}[\text{Tan}[c]] \right) \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a^2 \text{Cos}[c]^2 + a^2 \text{Sin}[c]^2 \right) \Big/ \\
 & \quad \left. \left( \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) \Big/ \\
 & \left( 3 (a^2 - b^2)^2 d (A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2 c + 2 dx]) \right. \\
 & \quad \left. (a + b \text{Sec}[c + dx])^{5/2} \right)
 \end{aligned}$$

**Problem 1067: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2}{\sqrt{\text{Sec}[c + dx]} (a + b \text{Sec}[c + dx])^{5/2}} dx$$

Optimal (type 4, 401 leaves, 9 steps):

$$\left( 2 (8 A b^3 + 3 a^3 B - 2 a b^2 B - a^2 b (9 A + C)) \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b} \sqrt{\operatorname{Sec}[c + d x]}\right] \right) / \left( 3 a^3 (a^2 - b^2) d \sqrt{a + b \operatorname{Sec}[c + d x]} \right) +$$

$$\left( 2 (8 A b^4 + 6 a^3 b B - 2 a b^3 B + 3 a^4 (A - C) - a^2 b^2 (15 A + C)) \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b} \sqrt{a + b \operatorname{Sec}[c + d x]}\right] \right) / \left( 3 a^3 (a^2 - b^2)^2 d \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \sqrt{\operatorname{Sec}[c + d x]} \right) +$$

$$\frac{2 (A b^2 - a (b B - a C)) \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{3 a (a^2 - b^2) d (a + b \operatorname{Sec}[c + d x])^{3/2}} -$$

$$\left( 2 (4 A b^4 + 5 a^3 b B - a b^3 B - 2 a^4 C - 2 a^2 b^2 (4 A + C)) \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x] \right) / \left( 3 a^2 (a^2 - b^2)^2 d \sqrt{a + b \operatorname{Sec}[c + d x]} \right)$$

Result (type 6, 6142 leaves):

$$\frac{1}{(A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) (a + b \operatorname{Sec}[c + d x])^{5/2} (b + a \operatorname{Cos}[c + d x])^3 \sqrt{\operatorname{Sec}[c + d x]} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x])^2}$$

$$\left( -\frac{1}{3 a^3 (a^2 - b^2)^2 d} (3 a^4 A - 24 a^2 A b^2 + 13 A b^4 + 12 a^3 b B - 4 a b^3 B - 6 a^4 C - 2 a^2 b^2 C + 3 a^4 A \operatorname{Cos}[2 c] - 6 a^2 A b^2 \operatorname{Cos}[2 c] + 3 A b^4 \operatorname{Cos}[2 c]) \operatorname{Csc}[c] \operatorname{Sec}[c] + (4 \operatorname{Sec}[c] (A b^4 \operatorname{Sin}[c] - a b^3 B \operatorname{Sin}[c] + a^2 b^2 C \operatorname{Sin}[c] - a A b^3 \operatorname{Sin}[d x] + a^2 b^2 B \operatorname{Sin}[d x] - a^3 b C \operatorname{Sin}[d x])) / (3 a^3 (a^2 - b^2) d (b + a \operatorname{Cos}[c + d x])^2) - (4 \operatorname{Sec}[c] (10 a^2 A b^3 \operatorname{Sin}[c] - 6 A b^5 \operatorname{Sin}[c] - 7 a^3 b^2 B \operatorname{Sin}[c] + 3 a b^4 B \operatorname{Sin}[c] + 4 a^4 b C \operatorname{Sin}[c] - 9 a^3 A b^2 \operatorname{Sin}[d x] + 5 a A b^4 \operatorname{Sin}[d x] + 6 a^4 b B \operatorname{Sin}[d x] - 2 a^2 b^3 B \operatorname{Sin}[d x] - 3 a^5 C \operatorname{Sin}[d x] - a^3 b^2 C \operatorname{Sin}[d x])) / (3 a^3 (a^2 - b^2)^2 d (b + a \operatorname{Cos}[c + d x])) \right) +$$

$$\left( 8 A b \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\operatorname{Csc}[c] (b - a \sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]])]}{a \sqrt{1 + \operatorname{Cot}[c]^2} \left(1 + \frac{b \operatorname{Csc}[c]}{a \sqrt{1 + \operatorname{Cot}[c]^2}\right)}\right)}{a \sqrt{1 + \operatorname{Cot}[c]^2} \left(-1 + \frac{b \operatorname{Csc}[c]}{a \sqrt{1 + \operatorname{Cot}[c]^2}\right)}\right] \right)$$

$$\frac{\operatorname{Csc}[c] (b - a \sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]])]}{a \sqrt{1 + \operatorname{Cot}[c]^2} \left(-1 + \frac{b \operatorname{Csc}[c]}{a \sqrt{1 + \operatorname{Cot}[c]^2}\right)}$$

$$(b + a \operatorname{Cos}[c + d x])^{5/2} \operatorname{Csc}[c] \sqrt{\operatorname{Sec}[c + d x]} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x])^2 \operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]$$

$$\begin{aligned}
 & \left( \frac{\sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}}}{\sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}}} \right. \\
 & \left. \sqrt{b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]]} \right) / \\
 & \left( (a^2 - b^2)^2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} (a + b \sec [c + d x])^{5/2} \right) - \\
 & \left( 8 A b^3 \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right. \\
 & \left. \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( -1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right) \\
 & (b + a \cos [c + d x])^{5/2} \csc [c] \sqrt{\sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \sec [d x - \text{ArcTan} [\cot [c]]] \sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}} \\
 & \left( \frac{\sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}}}{\sqrt{b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]]} \right) / \\
 & \left( 3 a^2 (a^2 - b^2)^2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \left. \sqrt{1 + \cot [c]^2} (a + b \sec [c + d x])^{5/2} \right) - \\
 & \left( 4 a B \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( -1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \right] \\
 & (b + a \text{Cos}[c + dx])^{5/2} \text{Csc}[c] \sqrt{\text{Sec}[c + dx]} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \\
 & \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} - b \text{Csc}[c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} + a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} + b \text{Csc}[c]}} \\
 & \left. \sqrt{b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right) / \\
 & \left( (a^2 - b^2)^2 d (A + 2C + 2B \text{Cos}[c + dx] + A \text{Cos}[2c + 2dx]) \sqrt{1 + \text{Cot}[c]^2} (a + b \text{Sec}[c + dx])^{5/2} \right) - \\
 & \left( 4 b^2 \text{B AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( 1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \right], \right. \\
 & \left. \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( -1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \right] \\
 & (b + a \text{Cos}[c + dx])^{5/2} \text{Csc}[c] \sqrt{\text{Sec}[c + dx]} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \\
 & \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} - b \text{Csc}[c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} + a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} + b \text{Csc}[c]}} \\
 & \left. \sqrt{b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right) / \\
 & (3 a (a^2 - b^2)^2 d (A + 2C + 2B \text{Cos}[c + dx] + A \text{Cos}[2c + 2dx])
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{1 + \cot [c]^2} (a + b \sec [c + d x])^{5/2} + \\
 & \left( 16 b C \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]] \right)}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right. \\
 & \left. \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]] \right)}{a \sqrt{1 + \cot [c]^2} \left( -1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right) \right] \\
 & (b + a \cos [c + d x])^{5/2} \csc [c] \sqrt{\sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \sec [d x - \operatorname{ArcTan} [\cot [c]]] \sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \operatorname{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \operatorname{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}} \\
 & \left. \sqrt{b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]]} \right) / \\
 & \left( 3 (a^2 - b^2)^2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} (a + b \sec [c + d x])^{5/2} \right) - \\
 & \left( 2 a^2 A (b + a \cos [c + d x])^{5/2} \csc [c] \sqrt{\sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \left. \left( \left( \operatorname{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, -\left( \sec [c] \left( b + a \cos [c] \cos [d x + \operatorname{ArcTan} [\tan [c]] \right) \right) \right] \right. \right. \right. \\
 & \left. \left. \left. \sqrt{1 + \tan [c]^2} \right) \right) / \left( a \sqrt{1 + \tan [c]^2} \left( 1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right) \right) , \\
 & - \left( \left( \sec [c] \left( b + a \cos [c] \cos [d x + \operatorname{ArcTan} [\tan [c]] \right) \right) \sqrt{1 + \tan [c]^2} \right) / \\
 & \left( a \sqrt{1 + \tan [c]^2} \left( -1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right) \sin [d x + \operatorname{ArcTan} [\tan [c]]] \tan [c] \Big) / \\
 & \left( \sqrt{1 + \tan [c]^2} \sqrt{\left( \left( a \sqrt{1 + \tan [c]^2} - a \cos [d x + \operatorname{ArcTan} [\tan [c]] \right) \sqrt{1 + \tan [c]^2} \right) / \right.}
 \end{aligned}$$

$$\begin{aligned}
 & \left( b \operatorname{Sec}[c] + a \sqrt{1 + \operatorname{Tan}[c]^2} \right) \sqrt{\left( \left( a \sqrt{1 + \operatorname{Tan}[c]^2} + \right. \right. \\
 & \quad \left. \left. a \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2} \right) / \left( -b \operatorname{Sec}[c] + a \sqrt{1 + \operatorname{Tan}[c]^2} \right) \right)} \\
 & \sqrt{b + a \operatorname{Cos}[c] \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}} \Big) - \\
 & \left( \frac{\operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1 + \operatorname{Tan}[c]^2}} + \left( 2 a \operatorname{Cos}[c] \left( b + a \operatorname{Cos}[c] \operatorname{Cos}[ \right. \right. \right. \\
 & \quad \left. \left. \left. d x + \operatorname{ArcTan}[\operatorname{Tan}[c]] \right] \sqrt{1 + \operatorname{Tan}[c]^2} \right) \right) / \left( a^2 \operatorname{Cos}[c]^2 + a^2 \operatorname{Sin}[c]^2 \right) \right) / \\
 & \left( \sqrt{b + a \operatorname{Cos}[c] \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}} \right) \Big) / \\
 & \left( (a^2 - b^2)^2 d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) (a + b \operatorname{Sec}[c + d x])^{5/2} \right) + \\
 & \left( 10 A b^2 (b + a \operatorname{Cos}[c + d x])^{5/2} \operatorname{Csc}[c] \sqrt{\operatorname{Sec}[c + d x]} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \left. \left( \left( \operatorname{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, -\left( \operatorname{Sec}[c] \left( b + a \operatorname{Cos}[c] \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \right) \right) \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \operatorname{Tan}[c]^2} \right) \right) / \left( a \sqrt{1 + \operatorname{Tan}[c]^2} \left( 1 - \frac{b \operatorname{Sec}[c]}{a \sqrt{1 + \operatorname{Tan}[c]^2}} \right) \right) \right) \right), \\
 & - \left( \left( \operatorname{Sec}[c] \left( b + a \operatorname{Cos}[c] \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2} \right) \right) / \right. \\
 & \quad \left. \left( a \sqrt{1 + \operatorname{Tan}[c]^2} \left( -1 - \frac{b \operatorname{Sec}[c]}{a \sqrt{1 + \operatorname{Tan}[c]^2}} \right) \right) \right) \left. \operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] \right) / \\
 & \left( \sqrt{1 + \operatorname{Tan}[c]^2} \sqrt{\left( \left( a \sqrt{1 + \operatorname{Tan}[c]^2} - a \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2} \right) / \right. \right. \\
 & \quad \left. \left. \left( b \operatorname{Sec}[c] + a \sqrt{1 + \operatorname{Tan}[c]^2} \right) \right) \sqrt{\left( \left( a \sqrt{1 + \operatorname{Tan}[c]^2} + \right. \right. \right. \\
 & \quad \left. \left. \left. a \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2} \right) / \left( -b \operatorname{Sec}[c] + a \sqrt{1 + \operatorname{Tan}[c]^2} \right) \right) \right)} \\
 & \sqrt{b + a \operatorname{Cos}[c] \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}} \Big) -
 \end{aligned}$$



$$\begin{aligned}
 & \left( \frac{\sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \left( 2 a \cos [c] \left( b + a \cos [c] \cos [ \right. \right. \right. \\
 & \quad \left. \left. \left. d x + \text{ArcTan}[\text{Tan}[c]] \right] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a^2 \cos [c]^2 + a^2 \sin [c]^2 \right) \Bigg) / \\
 & \left( \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) \Bigg) / \\
 & \left( (a^2 - b^2)^2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^{5/2} - \right. \\
 & \left. 16 A b^4 (b + a \cos [c + d x])^{5/2} \text{Csc}[c] \sqrt{\sec [c + d x]} \right. \\
 & \quad \left. (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \left. \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \sec [c] \left( b + a \cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]] \right] \right. \right. \right. \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a \sqrt{1 + \text{Tan}[c]^2} \left( 1 - \frac{b \sec [c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \right) \Bigg) , \\
 & - \left( \left( \sec [c] \left( b + a \cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \right. \\
 & \quad \left. \left( a \sqrt{1 + \text{Tan}[c]^2} \left( -1 - \frac{b \sec [c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \Bigg) \sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] \Bigg) / \\
 & \left( \sqrt{1 + \text{Tan}[c]^2} \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} - a \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) / \right. \right. \\
 & \quad \left. \left. \left( b \sec [c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} + \right. \right. \right. \\
 & \quad \left. \left. \left. a \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) / \left( -b \sec [c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) \right. \\
 & \quad \left. \left. \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) - \right. \\
 & \left. \left( \frac{\sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \left( 2 a \cos [c] \left( b + a \cos [c] \cos [ \right. \right. \right. \right. \\
 & \quad \left. \left. \left. d x + \text{ArcTan}[\text{Tan}[c]] \right] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a^2 \cos [c]^2 + a^2 \sin [c]^2 \right) \Bigg) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]]} \sqrt{1 + \tan [c]^2} \right) \Bigg) \Bigg) \Bigg) / \\
 & \left( 3 a^2 (a^2 - b^2)^2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. (a + b \sec [c + d x])^{5/2} \right) - \\
 & \left( 4 a b B (b + a \cos [c + d x])^{5/2} \text{Csc} [c] \sqrt{\sec [c + d x]} \right. \\
 & \quad \left. (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left. \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, -\left( \sec [c] (b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]) \right. \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. \sqrt{1 + \tan [c]^2} \right) \right) \right] / \left( a \sqrt{1 + \tan [c]^2} \left( 1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right) \right) \Bigg) \Bigg) / \\
 & \quad - \left( \left( \sec [c] (b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) \right) \Bigg) \Bigg) / \\
 & \quad \left( a \sqrt{1 + \tan [c]^2} \left( -1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \Bigg) \Bigg) \sin [d x + \text{ArcTan} [\tan [c]]] \tan [c] \Bigg) \Bigg) / \\
 & \left( \sqrt{1 + \tan [c]^2} \sqrt{\left( (a \sqrt{1 + \tan [c]^2} - a \cos [d x + \text{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) \right) \Bigg) \Bigg) / \\
 & \quad \left( b \sec [c] + a \sqrt{1 + \tan [c]^2} \right) \sqrt{\left( (a \sqrt{1 + \tan [c]^2} + \right. \\
 & \quad \left. a \cos [d x + \text{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) \Bigg) \Bigg) / \left( -b \sec [c] + a \sqrt{1 + \tan [c]^2} \right) \Bigg) \Bigg) \\
 & \quad \left. \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]]} \sqrt{1 + \tan [c]^2} \right) \Bigg) - \\
 & \left( \frac{\sin [d x + \text{ArcTan} [\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \left( 2 a \cos [c] (b + a \cos [c] \cos [ \right. \right. \\
 & \quad \left. \left. d x + \text{ArcTan} [\tan [c]] \right) \sqrt{1 + \tan [c]^2} \right) \Bigg) \Bigg) / \left( a^2 \cos [c]^2 + a^2 \sin [c]^2 \right) \Bigg) \Bigg) / \\
 & \left( \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]]} \sqrt{1 + \tan [c]^2} \right) \Bigg) \Bigg) \Bigg) / \\
 & \left( (a^2 - b^2)^2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. (a + b \sec [c + d x])^{5/2} \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left( 4 b^3 B (b + a \cos [c + d x])^{5/2} \csc [c] \sqrt{\sec [c + d x]} \right. \\
 & \quad \left. (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left( \left( \operatorname{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, -\left( \sec [c] (b + a \cos [c] \cos [d x + \operatorname{ArcTan} [\tan [c]]) \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. \sqrt{1 + \tan [c]^2} \right) \right) \right] / \left( a \sqrt{1 + \tan [c]^2} \left( 1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right), \\
 & \quad - \left( \left( \sec [c] (b + a \cos [c] \cos [d x + \operatorname{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) \right) / \\
 & \quad \left( a \sqrt{1 + \tan [c]^2} \left( -1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right) \sin [d x + \operatorname{ArcTan} [\tan [c]]] \tan [c] \Big/ \\
 & \quad \left( \sqrt{1 + \tan [c]^2} \sqrt{\left( (a \sqrt{1 + \tan [c]^2} - a \cos [d x + \operatorname{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) \right.} \\
 & \quad \left. (b \sec [c] + a \sqrt{1 + \tan [c]^2}) \right) \sqrt{\left( (a \sqrt{1 + \tan [c]^2} + \right.} \\
 & \quad \left. a \cos [d x + \operatorname{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) / (-b \sec [c] + a \sqrt{1 + \tan [c]^2})} \\
 & \quad \left. \sqrt{b + a \cos [c] \cos [d x + \operatorname{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2}} \right) - \\
 & \quad \left( \frac{\sin [d x + \operatorname{ArcTan} [\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \left( 2 a \cos [c] (b + a \cos [c] \cos [ \right. \right. \\
 & \quad \left. \left. d x + \operatorname{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) \right) / (a^2 \cos [c]^2 + a^2 \sin [c]^2) \Big/ \\
 & \quad \left( \sqrt{b + a \cos [c] \cos [d x + \operatorname{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2}} \right) \Big/ \\
 & \quad \left( 3 a (a^2 - b^2)^2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. (a + b \sec [c + d x])^{5/2} \right) + \\
 & \quad \left( 2 a^2 C (b + a \cos [c + d x])^{5/2} \csc [c] \sqrt{\sec [c + d x]} \right. \\
 & \quad \left. (A + B \sec [c + d x] + C \sec [c + d x]^2) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \right] \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \text{Tan}[c]^2} \right) \right) \right) / \left( a \sqrt{1 + \text{Tan}[c]^2} \left( 1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right), \\
 & - \left( \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \right] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \\
 & \quad \left( a \sqrt{1 + \text{Tan}[c]^2} \left( -1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] \Big) / \\
 & \left( \sqrt{1 + \text{Tan}[c]^2} \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} - a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \sqrt{1 + \text{Tan}[c]^2} \right) \right. \right. \\
 & \quad \left. \left. \left( b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} + \right. \right. \right. \\
 & \quad \left. \left. \left. a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( -b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) \\
 & \quad \left. \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) - \\
 & \left( \frac{\text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \left( 2 a \text{Cos}[c] \left( b + a \text{Cos}[c] \text{Cos}[ \right. \right. \right. \\
 & \quad \left. \left. \left. dx + \text{ArcTan}[\text{Tan}[c]] \right) \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a^2 \text{Cos}[c]^2 + a^2 \text{Sin}[c]^2 \right) \Big) / \\
 & \quad \left( \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \Big) \Big) / \\
 & \left( (a^2 - b^2)^2 d (A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2 c + 2 dx]) \right. \\
 & \quad \left. (a + b \text{Sec}[c + dx])^{5/2} \right) + \\
 & \left( 2 b^2 C (b + a \text{Cos}[c + dx])^{5/2} \text{Csc}[c] \sqrt{\text{Sec}[c + dx]} \right. \\
 & \quad \left. (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \right. \\
 & \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \right) \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \text{Tan}[c]^2} \right) \right) \right) / \left( a \sqrt{1 + \text{Tan}[c]^2} \left( 1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \Big)
 \end{aligned}$$

$$\begin{aligned}
 & - \left( \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) \right) / \\
 & \left( a \sqrt{1 + \text{Tan}[c]^2} \left( -1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \left] \text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] \right) / \\
 & \left( \sqrt{1 + \text{Tan}[c]^2} \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} - a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) \right) / \\
 & \left( b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} + \right. \right. \\
 & \left. \left. a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( -b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) \\
 & \left. \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) - \\
 & \left( \frac{\text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \left( 2 a \text{Cos}[c] \left( b + a \text{Cos}[c] \text{Cos}[ \right. \right. \right. \\
 & \left. \left. \left. dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a^2 \text{Cos}[c]^2 + a^2 \text{Sin}[c]^2 \right) \right) / \\
 & \left( \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) \right) / \\
 & \left( 3 (a^2 - b^2)^2 d (A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2 c + 2 dx]) \right. \\
 & \left. (a + b \text{Sec}[c + dx])^{5/2} \right)
 \end{aligned}$$

**Problem 1068: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2}{\text{Sec}[c + dx]^{3/2} (a + b \text{Sec}[c + dx])^{5/2}} dx$$

Optimal (type 4, 521 leaves, 10 steps):

$$\begin{aligned}
 & - \left( \left( 2 (16 A b^4 + 9 a^3 b B - 8 a b^3 B - 2 a^2 b^2 (8 A - C) - a^4 (A + 3 C)) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \right. \\
 & \quad \left. \left. \text{EllipticF} \left[ \frac{1}{2} (c + d x), \frac{2 a}{a + b} \right] \sqrt{\sec [c + d x]} \right) / \left( 3 a^4 (a^2 - b^2) d \sqrt{a + b \sec [c + d x]} \right) \right) - \\
 & \left( 2 (16 A b^5 - 3 a^5 B + 15 a^3 b^2 B - 8 a b^4 B - 2 a^2 b^3 (14 A - C) + a^4 (8 A b - 6 b C)) \right. \\
 & \quad \left. \text{EllipticE} \left[ \frac{1}{2} (c + d x), \frac{2 a}{a + b} \right] \sqrt{a + b \sec [c + d x]} \right) / \\
 & \left( 3 a^4 (a^2 - b^2)^2 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \sqrt{\sec [c + d x]} \right) + \\
 & \frac{2 (A b^2 - a (b B - a C)) \sin [c + d x]}{3 a (a^2 - b^2) d \sqrt{\sec [c + d x]} (a + b \sec [c + d x])^{3/2}} + \\
 & \frac{2 (10 a^2 A b^2 - 6 A b^4 - 7 a^3 b B + 3 a b^3 B + 4 a^4 C) \sin [c + d x]}{3 a^2 (a^2 - b^2)^2 d \sqrt{\sec [c + d x]} \sqrt{a + b \sec [c + d x]}} + \\
 & \left( 2 (8 A b^4 + 8 a^3 b B - 4 a b^3 B + a^4 (A - 5 C) - a^2 b^2 (13 A - C)) \sqrt{a + b \sec [c + d x]} \sin [c + d x] \right) / \\
 & \left( 3 a^3 (a^2 - b^2)^2 d \sqrt{\sec [c + d x]} \right)
 \end{aligned}$$

Result (type 6, 7608 leaves):

$$\begin{aligned}
 & \frac{1}{(A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^{5/2}} \\
 & (b + a \cos [c + d x])^3 \sqrt{\sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x])^2 \\
 & \left( - \frac{1}{3 a^4 (a^2 - b^2)^2 d} (-8 a^4 A b + 40 a^2 A b^3 - 24 A b^5 + 3 a^5 B - 24 a^3 b^2 B + 13 a b^4 B + 12 a^4 b C - \right. \\
 & \quad 4 a^2 b^3 C - 8 a^4 A b \cos [2 c] + 16 a^2 A b^3 \cos [2 c] - 8 A b^5 \cos [2 c] + 3 a^5 B \cos [2 c] - \\
 & \quad \left. 6 a^3 b^2 B \cos [2 c] + 3 a b^4 B \cos [2 c]) \csc [c] \sec [c] + \frac{4 A \cos [d x] \sin [c]}{3 a^3 d} + \right. \\
 & \quad \left. \frac{4 A \cos [c] \sin [d x]}{3 a^3 d} - (4 \sec [c] (A b^5 \sin [c] - a b^4 B \sin [c] + a^2 b^3 C \sin [c] - a A b^4 \sin [d x] + \right. \\
 & \quad \left. a^2 b^3 B \sin [d x] - a^3 b^2 C \sin [d x])) / (3 a^4 (a^2 - b^2) d (b + a \cos [c + d x])^2) + \right. \\
 & \quad \left. (4 \sec [c] (13 a^2 A b^4 \sin [c] - 9 A b^6 \sin [c] - 10 a^3 b^3 B \sin [c] + 6 a b^5 B \sin [c] + \right. \\
 & \quad \left. 7 a^4 b^2 C \sin [c] - 3 a^2 b^4 C \sin [c] - 12 a^3 A b^3 \sin [d x] + 8 a A b^5 \sin [d x] + \right. \\
 & \quad \left. 9 a^4 b^2 B \sin [d x] - 5 a^2 b^4 B \sin [d x] - 6 a^5 b C \sin [d x] + 2 a^3 b^3 C \sin [d x])) / \right. \\
 & \quad \left. (3 a^4 (a^2 - b^2)^2 d (b + a \cos [c + d x])) \right) - \left( 4 a A \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2} \right. \right.
 \end{aligned}$$

$$\frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( 1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)},$$

$$\frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( -1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)}$$

$$(b + a \text{Cos}[c + dx])^{5/2} \text{Csc}[c] \sqrt{\text{Sec}[c + dx]}$$

$$(A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2)$$

$$\text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]]$$

$$\sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} - b \text{Csc}[c]}}$$

$$\sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} + a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} + b \text{Csc}[c]}}$$

$$\left. \sqrt{b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right/$$

$$\left( 3 (a^2 - b^2)^2 d (A + 2C + 2B \text{Cos}[c + dx] + A \text{Cos}[2c + 2dx]) \right.$$

$$\left. \sqrt{1 + \text{Cot}[c]^2} (a + b \text{Sec}[c + dx])^{5/2} \right) -$$

$$\left( 28 A b^2 \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( 1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \right], \right.$$

$$\left. \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( -1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \right]$$

$$(b + a \text{Cos}[c + dx])^{5/2} \text{Csc}[c] \sqrt{\text{Sec}[c + dx]} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2)$$

$$\text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} - b \text{Csc}[c]}}$$

$$\begin{aligned}
 & \left( \frac{\sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}}}{\sqrt{b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]]}} \right) / \\
 & \left( 3 a (a^2 - b^2)^2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. \sqrt{1 + \cot [c]^2} (a + b \sec [c + d x])^{5/2} \right) + \\
 & \left( 16 A b^4 \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] (b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]])}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right. \\
 & \quad \left. \frac{\csc [c] (b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]])}{a \sqrt{1 + \cot [c]^2} \left( -1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right) ] \\
 & (b + a \cos [c + d x])^{5/2} \csc [c] \sqrt{\sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \sec [d x - \text{ArcTan} [\cot [c]]] \sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}} \\
 & \left( \frac{\sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}}}{\sqrt{b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]]}} \right) / \\
 & \left( 3 a^3 (a^2 - b^2)^2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. \sqrt{1 + \cot [c]^2} (a + b \sec [c + d x])^{5/2} \right) + \\
 & \left( 8 b B \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] (b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]])}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right.
 \end{aligned}$$



$$\begin{aligned}
 & \left. \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( -1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \right] \\
 & (b + a \text{Cos}[c + dx])^{5/2} \text{Csc}[c] \sqrt{\text{Sec}[c + dx]} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \\
 & \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} - b \text{Csc}[c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} + a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} + b \text{Csc}[c]}} \\
 & \left. \sqrt{b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right) / \\
 & \left( (a^2 - b^2)^2 d (A + 2C + 2B \text{Cos}[c + dx] + A \text{Cos}[2c + 2dx]) \sqrt{1 + \text{Cot}[c]^2} (a + b \text{Sec}[c + dx])^{5/2} \right) - \\
 & \left( 8 b^3 \text{B AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( 1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \right], \right. \\
 & \left. \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( -1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \right] \\
 & (b + a \text{Cos}[c + dx])^{5/2} \text{Csc}[c] \sqrt{\text{Sec}[c + dx]} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \\
 & \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} - b \text{Csc}[c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} + a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} + b \text{Csc}[c]}} \\
 & \left. \sqrt{b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right) / \\
 & (3 a^2 (a^2 - b^2)^2 d (A + 2C + 2B \text{Cos}[c + dx] + A \text{Cos}[2c + 2dx])
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{1 + \cot [c]^2} (a + b \sec [c + d x])^{5/2} - \\
 & \left( 4 a C \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]] \right)}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right. \\
 & \left. \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]] \right)}{a \sqrt{1 + \cot [c]^2} \left( -1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right) \right] \\
 & (b + a \cos [c + d x])^{5/2} \csc [c] \sqrt{\sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \sec [d x - \operatorname{ArcTan} [\cot [c]]] \sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \operatorname{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \operatorname{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}} \\
 & \left. \sqrt{b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]]} \right) / \\
 & \left( (a^2 - b^2)^2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} (a + b \sec [c + d x])^{5/2} - \right. \\
 & \left. 4 b^2 C \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]] \right)}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right. \\
 & \left. \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]] \right)}{a \sqrt{1 + \cot [c]^2} \left( -1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right) \right] \\
 & (b + a \cos [c + d x])^{5/2} \csc [c] \sqrt{\sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \sec [d x - \operatorname{ArcTan} [\cot [c]]] \sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \operatorname{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \operatorname{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}}
 \end{aligned}$$

$$\begin{aligned}
 & \left. \sqrt{b - a \sqrt{1 + \cot^2[c]} \sin[c] \sin[d x - \text{ArcTan}[\cot[c]]]} \right) / \\
 & \left( 3 a (a^2 - b^2)^2 d (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) \right. \\
 & \quad \left. \sqrt{1 + \cot^2[c]} (a + b \sec[c + d x])^{5/2} \right) + \\
 & \left( 16 a A b (b + a \cos[c + d x])^{5/2} \csc[c] \sqrt{\sec[c + d x]} (A + B \sec[c + d x] + C \sec^2[c + d x])^2 \right. \\
 & \quad \left( \left( \text{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, -\left(\sec[c] (b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]])\right)\right.\right.\right. \\
 & \quad \left.\left.\left. \sqrt{1 + \tan^2[c]}\right)\right) / \left(a \sqrt{1 + \tan^2[c]} \left(1 - \frac{b \sec[c]}{a \sqrt{1 + \tan^2[c]}}\right)\right) \right) \right) , \\
 & \quad - \left( \left( \sec[c] (b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]) \sqrt{1 + \tan^2[c]} \right) / \right. \\
 & \quad \left. \left( a \sqrt{1 + \tan^2[c]} \left(-1 - \frac{b \sec[c]}{a \sqrt{1 + \tan^2[c]}}\right) \right) \right) \sin[d x + \text{ArcTan}[\tan[c]]] \tan[c] \Big) / \\
 & \quad \left( \sqrt{1 + \tan^2[c]} \sqrt{\left( (a \sqrt{1 + \tan^2[c]} - a \cos[d x + \text{ArcTan}[\tan[c]]) \sqrt{1 + \tan^2[c]} \right) / \right. \\
 & \quad \left. (b \sec[c] + a \sqrt{1 + \tan^2[c]}) \sqrt{\left( (a \sqrt{1 + \tan^2[c]} + \right. \right. \\
 & \quad \left. \left. a \cos[d x + \text{ArcTan}[\tan[c]]) \sqrt{1 + \tan^2[c]} \right) / (-b \sec[c] + a \sqrt{1 + \tan^2[c]}) \right) \Big) \\
 & \quad \left. \sqrt{b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan^2[c]}} \right) - \\
 & \quad \left( \frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan^2[c]}} + \left( 2 a \cos[c] (b + a \cos[c] \cos[ \right. \right. \\
 & \quad \left. \left. d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan^2[c]} \right) / (a^2 \cos^2[c] + a^2 \sin^2[c]) \right) / \\
 & \quad \left( \sqrt{b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan^2[c]}} \right) \Big) / \\
 & \left( 3 (a^2 - b^2)^2 d (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) (a + b \sec[c + d x])^{5/2} \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \left( 56 A b^3 (b + a \cos [c + d x])^{5/2} \operatorname{Csc}[c] \sqrt{\operatorname{Sec}[c + d x]} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \left( \left( \operatorname{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, -\left(\operatorname{Sec}[c] (b + a \cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]])\right)\right.\right.\right. \\
 & \left.\left.\left.\sqrt{1 + \operatorname{Tan}[c]^2}\right)\right)\right] / \left(a \sqrt{1 + \operatorname{Tan}[c]^2} \left(1 - \frac{b \operatorname{Sec}[c]}{a \sqrt{1 + \operatorname{Tan}[c]^2}}\right)\right) \right), \\
 & - \left( \left(\operatorname{Sec}[c] (b + a \cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]])\right) \sqrt{1 + \operatorname{Tan}[c]^2}\right) / \\
 & \left(a \sqrt{1 + \operatorname{Tan}[c]^2} \left(-1 - \frac{b \operatorname{Sec}[c]}{a \sqrt{1 + \operatorname{Tan}[c]^2}}\right)\right) \left[\sin [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]\right] / \\
 & \left(\sqrt{1 + \operatorname{Tan}[c]^2} \sqrt{\left(\left(a \sqrt{1 + \operatorname{Tan}[c]^2} - a \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]\right) \sqrt{1 + \operatorname{Tan}[c]^2}\right) / \right. \\
 & \left.\left(b \operatorname{Sec}[c] + a \sqrt{1 + \operatorname{Tan}[c]^2}\right)\right) \sqrt{\left(\left(a \sqrt{1 + \operatorname{Tan}[c]^2} + \right.\right. \\
 & \left.\left.a \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]\right) \sqrt{1 + \operatorname{Tan}[c]^2}\right) / \left(-b \operatorname{Sec}[c] + a \sqrt{1 + \operatorname{Tan}[c]^2}\right)} \\
 & \left.\sqrt{b + a \cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}}\right) - \\
 & \left(\frac{\sin [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1 + \operatorname{Tan}[c]^2}} + \left(2 a \cos [c] (b + a \cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}) / \left(a^2 \cos [c]^2 + a^2 \sin [c]^2\right)\right) / \right. \\
 & \left.\left(\sqrt{b + a \cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}}\right)\right) / \\
 & \left(3 a (a^2 - b^2)^2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \operatorname{Sec}[c + d x])^{5/2} + \right. \\
 & \left. 32 A b^5 (b + a \cos [c + d x])^{5/2} \operatorname{Csc}[c] \sqrt{\operatorname{Sec}[c + d x]} \right. \\
 & \left. (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \left. \left( \left( \operatorname{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, -\left(\operatorname{Sec}[c] (b + a \cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]])\right)\right.\right.\right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \sqrt{1 + \tan [c]^2} \right) / \left( a \sqrt{1 + \tan [c]^2} \left( 1 - \frac{b \operatorname{Sec}[c]}{a \sqrt{1 + \tan [c]^2}} \right) \right), \\
 & - \left( \left( \operatorname{Sec}[c] \left( b + a \operatorname{Cos}[c] \operatorname{Cos}[dx + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2} \right) \right) / \right. \\
 & \quad \left. \left( a \sqrt{1 + \tan [c]^2} \left( -1 - \frac{b \operatorname{Sec}[c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right) \operatorname{Sin}[dx + \operatorname{ArcTan}[\tan [c]]] \operatorname{Tan}[c] / \\
 & \quad \left( \sqrt{1 + \tan [c]^2} \sqrt{\left( \left( a \sqrt{1 + \tan [c]^2} - a \operatorname{Cos}[dx + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2} \right) / \right. \right. \\
 & \quad \left. \left( b \operatorname{Sec}[c] + a \sqrt{1 + \tan [c]^2} \right) \right) \sqrt{\left( \left( a \sqrt{1 + \tan [c]^2} + \right. \right. \\
 & \quad \left. \left. a \operatorname{Cos}[dx + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2} \right) / \left( -b \operatorname{Sec}[c] + a \sqrt{1 + \tan [c]^2} \right) \right) } \\
 & \quad \left. \sqrt{b + a \operatorname{Cos}[c] \operatorname{Cos}[dx + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}} \right) - \\
 & \quad \left( \frac{\operatorname{Sin}[dx + \operatorname{ArcTan}[\tan [c]]] \operatorname{Tan}[c]}{\sqrt{1 + \tan [c]^2}} + \left( 2 a \operatorname{Cos}[c] \left( b + a \operatorname{Cos}[c] \operatorname{Cos}[ \right. \right. \right. \\
 & \quad \left. \left. \left. dx + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2} \right) \right) / \left( a^2 \operatorname{Cos}[c]^2 + a^2 \operatorname{Sin}[c]^2 \right) \right) / \\
 & \quad \left( \sqrt{b + a \operatorname{Cos}[c] \operatorname{Cos}[dx + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}} \right) \right) / \\
 & \left( 3 a^3 (a^2 - b^2)^2 d (A + 2 C + 2 B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2 c + 2 dx]) (a + b \operatorname{Sec}[c + dx])^{5/2} - \right. \\
 & \left. \left( 2 a^2 B (b + a \operatorname{Cos}[c + dx])^{5/2} \operatorname{Csc}[c] \sqrt{\operatorname{Sec}[c + dx]} \right. \right. \\
 & \quad \left. \left. (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right. \right. \\
 & \quad \left. \left. \left( \operatorname{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, -\left( \operatorname{Sec}[c] \left( b + a \operatorname{Cos}[c] \operatorname{Cos}[dx + \operatorname{ArcTan}[\tan [c]]] \right) \right) \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \tan [c]^2} \right) \right) \right) / \left( a \sqrt{1 + \tan [c]^2} \left( 1 - \frac{b \operatorname{Sec}[c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right), \\
 & - \left( \left( \operatorname{Sec}[c] \left( b + a \operatorname{Cos}[c] \operatorname{Cos}[dx + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2} \right) \right) / \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( a \sqrt{1 + \tan[c]^2} \left( -1 - \frac{b \operatorname{Sec}[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \left[ \sin[d x + \operatorname{ArcTan}[\tan[c]]] \tan[c] \right] / \\
 & \left( \sqrt{1 + \tan[c]^2} \sqrt{\left( \left( a \sqrt{1 + \tan[c]^2} - a \cos[d x + \operatorname{ArcTan}[\tan[c]]] \right) \sqrt{1 + \tan[c]^2} \right) / \right. \\
 & \left. \left( b \operatorname{Sec}[c] + a \sqrt{1 + \tan[c]^2} \right) \sqrt{\left( \left( a \sqrt{1 + \tan[c]^2} + \right. \right. \right. \\
 & \left. \left. \left. a \cos[d x + \operatorname{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2} \right) / \left( -b \operatorname{Sec}[c] + a \sqrt{1 + \tan[c]^2} \right) \right) \right. \\
 & \left. \sqrt{b + a \cos[c] \cos[d x + \operatorname{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}} \right) - \\
 & \left( \frac{\sin[d x + \operatorname{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \left( 2 a \cos[c] \left( b + a \cos[c] \cos[ \right. \right. \right. \\
 & \left. \left. \left. d x + \operatorname{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2} \right) \right) / \left( a^2 \cos[c]^2 + a^2 \sin[c]^2 \right) \right) / \\
 & \left( \sqrt{b + a \cos[c] \cos[d x + \operatorname{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}} \right) \left. \right) / \\
 & \left( (a^2 - b^2)^2 d (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) (a + b \operatorname{Sec}[c + d x])^{5/2} \right) + \\
 & \left( 10 b^2 B (b + a \cos[c + d x])^{5/2} \operatorname{Csc}[c] \sqrt{\operatorname{Sec}[c + d x]} \right. \\
 & \left. (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \left. \left( \left( \operatorname{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, -\left( \operatorname{Sec}[c] \left( b + a \cos[c] \cos[d x + \operatorname{ArcTan}[\tan[c]]] \right) \right) \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \sqrt{1 + \tan[c]^2} \right) \right) / \left( a \sqrt{1 + \tan[c]^2} \left( 1 - \frac{b \operatorname{Sec}[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \right) \right), \\
 & - \left( \left( \operatorname{Sec}[c] \left( b + a \cos[c] \cos[d x + \operatorname{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2} \right) \right) / \right. \\
 & \left. \left( a \sqrt{1 + \tan[c]^2} \left( -1 - \frac{b \operatorname{Sec}[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \right) \left[ \sin[d x + \operatorname{ArcTan}[\tan[c]]] \tan[c] \right] / \\
 & \left( \sqrt{1 + \tan[c]^2} \sqrt{\left( \left( a \sqrt{1 + \tan[c]^2} - a \cos[d x + \operatorname{ArcTan}[\tan[c]]] \right) \sqrt{1 + \tan[c]^2} \right) / \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( b \sec [c] + a \sqrt{1 + \tan [c]^2} \right) \sqrt{\left( \left( a \sqrt{1 + \tan [c]^2} + \right. \right. \\
 & \quad \left. \left. a \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2} \right) / \left( -b \sec [c] + a \sqrt{1 + \tan [c]^2} \right) \right)} \\
 & \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2}} \Big) - \\
 & \left( \frac{\sin [d x + \text{ArcTan} [\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \left( 2 a \cos [c] \left( b + a \cos [c] \cos [ \right. \right. \right. \\
 & \quad \left. \left. \left. d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2} \right) \right) / \left( a^2 \cos [c]^2 + a^2 \sin [c]^2 \right) \right) / \\
 & \left( \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2}} \right) \Big) / \\
 & \left( (a^2 - b^2)^2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^{5/2} \right) - \\
 & \left( 16 b^4 B (b + a \cos [c + d x])^{5/2} \text{Csc} [c] \sqrt{\sec [c + d x]} \right. \\
 & \quad \left. (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \left. \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \sec [c] \left( b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]] \right) \right) \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \tan [c]^2} \right) \right) / \left( a \sqrt{1 + \tan [c]^2} \left( 1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right) \Big), \\
 & - \left( \left( \sec [c] \left( b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2} \right) \right) / \right. \\
 & \quad \left. \left( a \sqrt{1 + \tan [c]^2} \left( -1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right) \sin [d x + \text{ArcTan} [\tan [c]]] \tan [c] \Big) / \\
 & \left( \sqrt{1 + \tan [c]^2} \sqrt{\left( \left( a \sqrt{1 + \tan [c]^2} - a \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2} \right) / \right. \right. \\
 & \quad \left. \left. \left( b \sec [c] + a \sqrt{1 + \tan [c]^2} \right) \right) \sqrt{\left( \left( a \sqrt{1 + \tan [c]^2} + \right. \right. \right. \\
 & \quad \left. \left. \left. a \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2} \right) / \left( -b \sec [c] + a \sqrt{1 + \tan [c]^2} \right) \right)} \right. \\
 & \quad \left. \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2}} \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{\sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \left( 2 a \cos [c] \left( b + a \cos [c] \cos [ \right. \right. \right. \\
 & \quad \left. \left. \left. d x + \text{ArcTan}[\text{Tan}[c]] \right] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a^2 \cos [c]^2 + a^2 \sin [c]^2 \right) \Bigg) / \\
 & \left( \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) \Bigg) / \\
 & \left( 3 a^2 \left( a^2 - b^2 \right)^2 d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \right. \\
 & \quad \left. \left( a + b \sec [c + d x] \right)^{5/2} \right) - \\
 & \left( 4 a b C \left( b + a \cos [c + d x] \right)^{5/2} \text{Csc}[c] \sqrt{\sec [c + d x]} \right. \\
 & \quad \left. \left( A + B \sec [c + d x] + C \sec [c + d x]^2 \right) \right. \\
 & \quad \left. \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \sec [c] \left( b + a \cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]] \right) \right) \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \text{Tan}[c]^2} \right) \right) \right) / \left( a \sqrt{1 + \text{Tan}[c]^2} \left( 1 - \frac{b \sec [c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \Bigg) , \\
 & - \left( \left( \sec [c] \left( b + a \cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) \right) / \\
 & \quad \left( a \sqrt{1 + \text{Tan}[c]^2} \left( -1 - \frac{b \sec [c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \Bigg) \sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] \Bigg) / \\
 & \left( \sqrt{1 + \text{Tan}[c]^2} \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} - a \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \right. \\
 & \quad \left. \left( b \sec [c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} + \right. \right. \\
 & \quad \left. \left. a \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( -b \sec [c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \Bigg) \\
 & \quad \left. \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) - \\
 & \left( \frac{\sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \left( 2 a \cos [c] \left( b + a \cos [c] \cos [ \right. \right. \right. \\
 & \quad \left. \left. \left. d x + \text{ArcTan}[\text{Tan}[c]] \right] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a^2 \cos [c]^2 + a^2 \sin [c]^2 \right) \Bigg) /
 \end{aligned}$$



$$\begin{aligned}
 & \left( \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2}} \right) \Bigg) \Bigg) \Bigg) / \\
 & \left( (a^2 - b^2)^2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. (a + b \sec [c + d x])^{5/2} \right) + \\
 & \left( 4 b^3 C (b + a \cos [c + d x])^{5/2} \csc [c] \sqrt{\sec [c + d x]} \right. \\
 & \quad \left. (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left. \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \sec [c] (b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]) \right. \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. \sqrt{1 + \tan [c]^2} \right) \right) \right] / \left( a \sqrt{1 + \tan [c]^2} \left( 1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right) \right) \Bigg) \Bigg) \Bigg) / \\
 & \quad - \left( \left( \sec [c] (b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) \right) \Bigg) \Bigg) \Bigg) / \\
 & \quad \left( a \sqrt{1 + \tan [c]^2} \left( -1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \Bigg) \Bigg) \left[ \sin [d x + \text{ArcTan} [\tan [c]]] \tan [c] \right] \Bigg) \Bigg) / \\
 & \left( \sqrt{1 + \tan [c]^2} \sqrt{\left( (a \sqrt{1 + \tan [c]^2} - a \cos [d x + \text{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) \right) \Bigg) \Bigg) \Bigg) / \\
 & \quad \left( b \sec [c] + a \sqrt{1 + \tan [c]^2} \right) \sqrt{\left( (a \sqrt{1 + \tan [c]^2} + \right. \\
 & \quad \left. a \cos [d x + \text{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) \Bigg) \Bigg) \Bigg) / \left( -b \sec [c] + a \sqrt{1 + \tan [c]^2} \right) \Bigg) \Bigg) \\
 & \quad \left( \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2}} \right) \Bigg) \Bigg) \Bigg) - \\
 & \left( \frac{\sin [d x + \text{ArcTan} [\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \left( 2 a \cos [c] (b + a \cos [c] \cos [ \right. \right. \\
 & \quad \left. \left. d x + \text{ArcTan} [\tan [c]] \right) \sqrt{1 + \tan [c]^2} \right) \Bigg) \Bigg) \Bigg) / \left( a^2 \cos [c]^2 + a^2 \sin [c]^2 \right) \Bigg) \Bigg) \Bigg) / \\
 & \left( \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2}} \right) \Bigg) \Bigg) \Bigg) \Bigg) / \\
 & \left( 3 a (a^2 - b^2)^2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. (a + b \sec [c + d x])^{5/2} \right)
 \end{aligned}$$

**Problem 1069: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec [c + d x] + C \sec [c + d x]^2}{\sec [c + d x]^{5/2} (a + b \sec [c + d x])^{5/2}} dx$$

Optimal (type 4, 663 leaves, 11 steps):

$$\left( 2 (128 A b^5 + 5 a^5 B + 80 a^3 b^2 B - 80 a b^4 B - 4 a^2 b^3 (29 A - 10 C) - a^4 b (17 A + 45 C)) \right. \\ \left. \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{\sec [c + d x]} \right) / \\ (15 a^5 (a^2 - b^2) d \sqrt{a + b \sec [c + d x]}) + \\ \left( 2 (128 A b^6 - 40 a^5 b B + 140 a^3 b^3 B - 80 a b^5 B + 5 a^4 b^2 (11 A - 15 C) - 4 a^2 b^4 (53 A - 10 C) + \right. \\ \left. 3 a^6 (3 A + 5 C)) \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \sec [c + d x]} \right) / \\ \left( 15 a^5 (a^2 - b^2)^2 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \sqrt{\sec [c + d x]} \right) + \\ \frac{2 (A b^2 - a (b B - a C)) \sin [c + d x]}{3 a (a^2 - b^2) d \sec [c + d x]^{3/2} (a + b \sec [c + d x])^{3/2}} - \\ \frac{2 (8 A b^4 + 9 a^3 b B - 5 a b^3 B - 2 a^2 b^2 (6 A - C) - 6 a^4 C) \sin [c + d x]}{3 a^2 (a^2 - b^2)^2 d \sec [c + d x]^{3/2} \sqrt{a + b \sec [c + d x]}} + \\ \left( 2 (48 A b^4 + 50 a^3 b B - 30 a b^3 B + a^4 (3 A - 35 C) - a^2 b^2 (71 A - 15 C)) \right. \\ \left. \sqrt{a + b \sec [c + d x]} \sin [c + d x] \right) / (15 a^3 (a^2 - b^2)^2 d \sec [c + d x]^{3/2}) - \\ \left( 2 (64 A b^5 - 5 a^5 B + 65 a^3 b^2 B - 40 a b^4 B + 2 a^4 b (7 A - 20 C) - 2 a^2 b^3 (49 A - 10 C)) \right. \\ \left. \sqrt{a + b \sec [c + d x]} \sin [c + d x] \right) / (15 a^4 (a^2 - b^2)^2 d \sqrt{\sec [c + d x]})$$

Result (type 6, 9192 leaves):

$$\frac{1}{(A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \sec [c + d x])^{5/2}} \\ (b + a \cos [c + d x])^3 \sqrt{\sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) \\ \left( - \frac{1}{15 a^5 (a^2 - b^2)^2 d} 2 (9 a^6 A + 55 a^4 A b^2 - 287 a^2 A b^4 + 183 A b^6 - 40 a^5 b B + 200 a^3 b^3 B - 120 a b^5 B + \right. \\ \left. 15 a^6 C - 120 a^4 b^2 C + 65 a^2 b^4 C + 9 a^6 A \cos [2 c] + 55 a^4 A b^2 \cos [2 c] - 137 a^2 A b^4 \cos [2 c] + \right. \\ \left. 73 A b^6 \cos [2 c] - 40 a^5 b B \cos [2 c] + 80 a^3 b^3 B \cos [2 c] - 40 a b^5 B \cos [2 c] + \right. \\ \left. 15 a^6 C \cos [2 c] - 30 a^4 b^2 C \cos [2 c] + 15 a^2 b^4 C \cos [2 c]) \operatorname{Csc}[c] \operatorname{Sec}[c] + \right.$$

$$\begin{aligned}
 & \frac{4(-14Ab + 5aB) \cos[dx] \sin[c]}{15a^4d} + \frac{2A \cos[2dx] \sin[2c]}{5a^3d} + \\
 & \frac{4(-14Ab + 5aB) \cos[c] \sin[dx]}{15a^4d} + \\
 & \left( 4 \sec[c] (Ab^6 \sin[c] - ab^5 B \sin[c] + a^2 b^4 C \sin[c] - aAb^5 \sin[dx] + \right. \\
 & \quad \left. a^2 b^4 B \sin[dx] - a^3 b^3 C \sin[dx]) \right) / \left( 3a^5 (a^2 - b^2) d (b + a \cos[c + dx])^2 \right) - \\
 & \left( 4 \sec[c] (16a^2 Ab^5 \sin[c] - 12Ab^7 \sin[c] - 13a^3 b^4 B \sin[c] + 9ab^6 B \sin[c] + \right. \\
 & \quad \left. 10a^4 b^3 C \sin[c] - 6a^2 b^5 C \sin[c] - 15a^3 Ab^4 \sin[dx] + 11aAb^6 \sin[dx] + \right. \\
 & \quad \left. 12a^4 b^3 B \sin[dx] - 8a^2 b^5 B \sin[dx] - 9a^5 b^2 C \sin[dx] + 5a^3 b^4 C \sin[dx]) \right) / \\
 & \left( 3a^5 (a^2 - b^2)^2 d (b + a \cos[c + dx]) \right) + \frac{2A \cos[2c] \sin[2dx]}{5a^3d} \Bigg) + \\
 & \left( 32Ab \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc[c] (b - a \sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]])]}{a \sqrt{1 + \cot[c]^2} \left( 1 + \frac{b \csc[c]}{a \sqrt{1 + \cot[c]^2}} \right)} \right], \right. \\
 & \quad \left. \frac{\csc[c] (b - a \sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]])]}{a \sqrt{1 + \cot[c]^2} \left( -1 + \frac{b \csc[c]}{a \sqrt{1 + \cot[c]^2}} \right)} \right] \Bigg) \\
 & (b + a \cos[c + dx])^{5/2} \csc[c] \sqrt{\sec[c + dx]} \\
 & (A + B \sec[c + dx] + C \sec[c + dx]^2) \\
 & \sec[dx - \operatorname{ArcTan}[\cot[c]]] \\
 & \sqrt{\frac{a \sqrt{1 + \cot[c]^2} - a \sqrt{1 + \cot[c]^2} \sin[dx - \operatorname{ArcTan}[\cot[c]]]}{a \sqrt{1 + \cot[c]^2} - b \csc[c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \cot[c]^2} + a \sqrt{1 + \cot[c]^2} \sin[dx - \operatorname{ArcTan}[\cot[c]]]}{a \sqrt{1 + \cot[c]^2} + b \csc[c]}} \\
 & \left. \sqrt{b - a \sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]]]} \right) / \\
 & \left( 15(a^2 - b^2)^2 d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \right. \\
 & \quad \left. \sqrt{1 + \cot[c]^2} (a + b \sec[c + dx])^{5/2} \right) + \\
 & \left( 176Ab^3 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc[c] (b - a \sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]])]}{a \sqrt{1 + \cot[c]^2} \left( 1 + \frac{b \csc[c]}{a \sqrt{1 + \cot[c]^2}} \right)} \right], \right. \\
 & \quad \left. \frac{\csc[c] (b - a \sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]])]}{a \sqrt{1 + \cot[c]^2} \left( 1 + \frac{b \csc[c]}{a \sqrt{1 + \cot[c]^2}} \right)} \right] \Bigg) ,
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( -1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \right] \\
 & (b + a \text{Cos}[c + dx])^{5/2} \text{Csc}[c] \sqrt{\text{Sec}[c + dx]} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \\
 & \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} - b \text{Csc}[c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} + a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} + b \text{Csc}[c]}} \\
 & \left. \sqrt{b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right) / \\
 & (15 a^2 (a^2 - b^2)^2 d (A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2 c + 2 dx]) \\
 & \sqrt{1 + \text{Cot}[c]^2} (a + b \text{Sec}[c + dx])^{5/2}) - \\
 & \left( 128 A b^5 \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( 1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \right], \right. \\
 & \left. \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( -1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \right] \\
 & (b + a \text{Cos}[c + dx])^{5/2} \text{Csc}[c] \sqrt{\text{Sec}[c + dx]} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \\
 & \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} - b \text{Csc}[c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} + a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} + b \text{Csc}[c]}} \\
 & \left. \sqrt{b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( 15 a^4 (a^2 - b^2)^2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. \sqrt{1 + \cot [c]^2} (a + b \sec [c + d x])^{5/2} \right) - \\
 & \left( 4 a B \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right. \\
 & \quad \left. \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( -1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right] \\
 & (b + a \cos [c + d x])^{5/2} \csc [c] \sqrt{\sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \sec [d x - \operatorname{ArcTan} [\cot [c]]] \sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \operatorname{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \operatorname{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}} \\
 & \left. \sqrt{b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]]} \right) / \\
 & \left( 3 (a^2 - b^2)^2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} (a + b \sec [c + d x])^{5/2} \right) - \\
 & \left( 28 b^2 B \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right. \\
 & \quad \left. \frac{\csc [c] \left( b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right)}{a \sqrt{1 + \cot [c]^2} \left( -1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right] \\
 & (b + a \cos [c + d x])^{5/2} \csc [c] \sqrt{\sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \sec [d x - \operatorname{ArcTan} [\cot [c]]] \sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \operatorname{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}}
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}} \\
 & \sqrt{\frac{b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]]}{}} \Big/ \\
 & \left( 3 a (a^2 - b^2)^2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. \sqrt{1 + \cot [c]^2} (a + b \sec [c + d x])^{5/2} \right) + \\
 & \left( 16 b^4 B \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] (b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]])}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right. \\
 & \quad \left. \frac{\csc [c] (b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]])}{a \sqrt{1 + \cot [c]^2} \left( -1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right) \\
 & (b + a \cos [c + d x])^{5/2} \csc [c] \sqrt{\sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \sec [d x - \text{ArcTan} [\cot [c]]] \sqrt{\frac{a \sqrt{1 + \cot [c]^2} - a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} - b \csc [c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \cot [c]^2} + a \sqrt{1 + \cot [c]^2} \sin [d x - \text{ArcTan} [\cot [c]]]}{a \sqrt{1 + \cot [c]^2} + b \csc [c]}} \\
 & \sqrt{\frac{b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]]}{}} \Big/ \\
 & \left( 3 a^3 (a^2 - b^2)^2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. \sqrt{1 + \cot [c]^2} (a + b \sec [c + d x])^{5/2} \right) + \\
 & \left( 8 b C \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\csc [c] (b - a \sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]])}{a \sqrt{1 + \cot [c]^2} \left( 1 + \frac{b \csc [c]}{a \sqrt{1 + \cot [c]^2}} \right)} \right], \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( -1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \right] \\
 & (b + a \text{Cos}[c + dx])^{5/2} \text{Csc}[c] \sqrt{\text{Sec}[c + dx]} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \\
 & \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} - b \text{Csc}[c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} + a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} + b \text{Csc}[c]}} \\
 & \left. \sqrt{b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right) / \\
 & \left( (a^2 - b^2)^2 d (A + 2C + 2B \text{Cos}[c + dx] + A \text{Cos}[2c + 2dx]) \sqrt{1 + \text{Cot}[c]^2} (a + b \text{Sec}[c + dx])^{5/2} \right) - \\
 & \left( 8 b^3 \text{C AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( 1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \right], \right. \\
 & \left. \frac{\text{Csc}[c] \left( b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \right)}{a \sqrt{1 + \text{Cot}[c]^2} \left( -1 + \frac{b \text{Csc}[c]}{a \sqrt{1 + \text{Cot}[c]^2}} \right)} \right] \\
 & (b + a \text{Cos}[c + dx])^{5/2} \text{Csc}[c] \sqrt{\text{Sec}[c + dx]} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \\
 & \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} - b \text{Csc}[c]}} \\
 & \sqrt{\frac{a \sqrt{1 + \text{Cot}[c]^2} + a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}{a \sqrt{1 + \text{Cot}[c]^2} + b \text{Csc}[c]}} \\
 & \left. \sqrt{b - a \sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right) / \\
 & (3 a^2 (a^2 - b^2)^2 d (A + 2C + 2B \text{Cos}[c + dx] + A \text{Cos}[2c + 2dx])
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{1 + \cot [c]^2} (a + b \operatorname{Sec}[c + d x])^{5/2} - \\
 & \left( 6 a^2 A (b + a \cos [c + d x])^{5/2} \operatorname{Csc}[c] \sqrt{\operatorname{Sec}[c + d x]} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \left. \left( \left( \operatorname{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, -\left(\operatorname{Sec}[c] (b + a \cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]])\right)\right] \right. \right. \right. \\
 & \left. \left. \left. \sqrt{1 + \tan [c]^2} \right) \right) / \left( a \sqrt{1 + \tan [c]^2} \left( 1 - \frac{b \operatorname{Sec}[c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right), \\
 & - \left( \left( \operatorname{Sec}[c] (b + a \cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]) \sqrt{1 + \tan [c]^2} \right) \right) / \\
 & \left( a \sqrt{1 + \tan [c]^2} \left( -1 - \frac{b \operatorname{Sec}[c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \left. \right) \sin [d x + \operatorname{ArcTan}[\tan [c]]] \tan [c] \Bigg) / \\
 & \left( \sqrt{1 + \tan [c]^2} \sqrt{\left( \left( a \sqrt{1 + \tan [c]^2} - a \cos [d x + \operatorname{ArcTan}[\tan [c]]] \right) \sqrt{1 + \tan [c]^2} \right) / \right. \\
 & \left. \left( b \operatorname{Sec}[c] + a \sqrt{1 + \tan [c]^2} \right) \sqrt{\left( \left( a \sqrt{1 + \tan [c]^2} + \right. \right. \right. \\
 & \left. \left. \left. a \cos [d x + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2} \right) \right) / \left( -b \operatorname{Sec}[c] + a \sqrt{1 + \tan [c]^2} \right) \right) \\
 & \left. \sqrt{b + a \cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}} \right) - \\
 & \left( \frac{\sin [d x + \operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \left( 2 a \cos [c] (b + a \cos [c] \cos [ \right. \right. \\
 & \left. \left. d x + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2} \right) \right) / \left( a^2 \cos [c]^2 + a^2 \sin [c]^2 \right) \Bigg) / \\
 & \left( \sqrt{b + a \cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}} \right) \Bigg) / \\
 & \left( 5 (a^2 - b^2)^2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + b \operatorname{Sec}[c + d x])^{5/2} - \right. \\
 & \left. 22 A b^2 (b + a \cos [c + d x])^{5/2} \operatorname{Csc}[c] \sqrt{\operatorname{Sec}[c + d x]} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \left. \left( \left( \operatorname{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, -\left(\operatorname{Sec}[c] (b + a \cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]])\right)\right] \right) \right. \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & \left. \left. \left. \left. \left. \sqrt{1 + \tan[c]^2} \right) \right) \right) \right) \right) \left/ \left( a \sqrt{1 + \tan[c]^2} \left( 1 - \frac{b \sec[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \right), \\
 & - \left( \left( \sec[c] \left( b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2} \right) \right) \right) \right) \left/ \right. \\
 & \left. \left. \left. \left. \left. \left( a \sqrt{1 + \tan[c]^2} \left( -1 - \frac{b \sec[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \right) \right) \right) \right) \left[ \sin[d x + \text{ArcTan}[\tan[c]]] \tan[c] \right] \left/ \right. \\
 & \left. \left. \left. \left. \left. \sqrt{1 + \tan[c]^2} \sqrt{\left( \left( a \sqrt{1 + \tan[c]^2} - a \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2} \right) \right) \right) \right) \right) \right) \right/ \\
 & \left. \left. \left. \left. \left. \left( b \sec[c] + a \sqrt{1 + \tan[c]^2} \right) \right) \right) \right) \right) \sqrt{\left( \left( a \sqrt{1 + \tan[c]^2} + \right. \right. \right. \\
 & \left. \left. \left. a \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2} \right) \right) \right) \right) \left/ \left( -b \sec[c] + a \sqrt{1 + \tan[c]^2} \right) \right) \\
 & \left. \left. \left. \left. \left. \sqrt{b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}} \right) \right) \right) \right) \right) - \\
 & \left( \frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \left( 2 a \cos[c] \left( b + a \cos[c] \cos \right. \right. \right. \\
 & \left. \left. \left. d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2} \right) \right) \right) \left/ \left( a^2 \cos[c]^2 + a^2 \sin[c]^2 \right) \right) \left/ \right. \\
 & \left. \left. \left. \left. \left. \left( \sqrt{b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}} \right) \right) \right) \right) \right) \right) \left/ \right. \\
 & \left( 3 (a^2 - b^2)^2 d (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) (a + b \sec[c + d x])^{5/2} \right) + \\
 & \left( 424 A b^4 (b + a \cos[c + d x])^{5/2} \text{Csc}[c] \sqrt{\sec[c + d x]} (A + B \sec[c + d x] + C \sec[c + d x]^2) \right) \\
 & \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \sec[c] \left( b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \right) \right) \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \left. \sqrt{1 + \tan[c]^2} \right) \right) \right) \right) \right) \left/ \left( a \sqrt{1 + \tan[c]^2} \left( 1 - \frac{b \sec[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \right) \right), \\
 & - \left( \left( \sec[c] \left( b + a \cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2} \right) \right) \right) \left/ \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( a \sqrt{1 + \tan[c]^2} \left( -1 - \frac{b \operatorname{Sec}[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \left[ \sin[dx + \operatorname{ArcTan}[\tan[c]]] \tan[c] \right] / \\
 & \left( \sqrt{1 + \tan[c]^2} \sqrt{\left( \left( a \sqrt{1 + \tan[c]^2} - a \cos[dx + \operatorname{ArcTan}[\tan[c]]] \right) \sqrt{1 + \tan[c]^2} \right) / \right. \\
 & \left. \left( b \operatorname{Sec}[c] + a \sqrt{1 + \tan[c]^2} \right) \sqrt{\left( \left( a \sqrt{1 + \tan[c]^2} + \right. \right. \right. \\
 & \left. \left. \left. a \cos[dx + \operatorname{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2} \right) / \left( -b \operatorname{Sec}[c] + a \sqrt{1 + \tan[c]^2} \right) \right) \right. \\
 & \left. \sqrt{b + a \cos[c] \cos[dx + \operatorname{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}} \right) - \\
 & \left( \frac{\sin[dx + \operatorname{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \left( 2 a \cos[c] \left( b + a \cos[c] \cos[ \right. \right. \right. \\
 & \left. \left. \left. dx + \operatorname{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2} \right) \right) / \left( a^2 \cos[c]^2 + a^2 \sin[c]^2 \right) \right) / \\
 & \left( \sqrt{b + a \cos[c] \cos[dx + \operatorname{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}} \right) \left. \right) / \\
 & \left( 15 a^2 (a^2 - b^2)^2 d (A + 2 C + 2 B \cos[c + dx] + A \cos[2c + 2dx]) (a + b \operatorname{Sec}[c + dx])^{5/2} \right) - \\
 & \left( 256 A b^6 (b + a \cos[c + dx])^{5/2} \operatorname{Csc}[c] \sqrt{\operatorname{Sec}[c + dx]} \right. \\
 & \left. (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right. \\
 & \left. \left( \left( \operatorname{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \operatorname{Sec}[c] \left( b + a \cos[c] \cos[dx + \operatorname{ArcTan}[\tan[c]]] \right) \right) \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \sqrt{1 + \tan[c]^2} \right) \right) / \left( a \sqrt{1 + \tan[c]^2} \left( 1 - \frac{b \operatorname{Sec}[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \right) \right), \\
 & - \left( \left( \operatorname{Sec}[c] \left( b + a \cos[c] \cos[dx + \operatorname{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2} \right) \right) / \right. \\
 & \left. \left( a \sqrt{1 + \tan[c]^2} \left( -1 - \frac{b \operatorname{Sec}[c]}{a \sqrt{1 + \tan[c]^2}} \right) \right) \right) \left[ \sin[dx + \operatorname{ArcTan}[\tan[c]]] \tan[c] \right] / \\
 & \left( \sqrt{1 + \tan[c]^2} \sqrt{\left( \left( a \sqrt{1 + \tan[c]^2} - a \cos[dx + \operatorname{ArcTan}[\tan[c]]] \right) \sqrt{1 + \tan[c]^2} \right) / \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( b \operatorname{Sec}[c] + a \sqrt{1 + \operatorname{Tan}[c]^2} \right) \sqrt{\left( \left( a \sqrt{1 + \operatorname{Tan}[c]^2} + \right. \right. \\
 & \quad \left. \left. a \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2} \right) / \left( -b \operatorname{Sec}[c] + a \sqrt{1 + \operatorname{Tan}[c]^2} \right) \right)} \\
 & \left. \sqrt{b + a \operatorname{Cos}[c] \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}} \right) - \\
 & \left( \frac{\operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1 + \operatorname{Tan}[c]^2}} + \left( 2 a \operatorname{Cos}[c] \left( b + a \operatorname{Cos}[c] \operatorname{Cos}[ \right. \right. \right. \\
 & \quad \left. \left. \left. d x + \operatorname{ArcTan}[\operatorname{Tan}[c]] \right] \sqrt{1 + \operatorname{Tan}[c]^2} \right) \right) / \left( a^2 \operatorname{Cos}[c]^2 + a^2 \operatorname{Sin}[c]^2 \right) \right) / \\
 & \left( \sqrt{b + a \operatorname{Cos}[c] \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}} \right) \Big) / \\
 & \left( 15 a^4 (a^2 - b^2)^2 d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) (a + b \operatorname{Sec}[c + d x])^{5/2} \right) + \\
 & \left( 16 a b B (b + a \operatorname{Cos}[c + d x])^{5/2} \operatorname{Csc}[c] \sqrt{\operatorname{Sec}[c + d x]} \right. \\
 & \quad \left. (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \left. \left( \left( \operatorname{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, -\left( \operatorname{Sec}[c] \left( b + a \operatorname{Cos}[c] \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \right) \right) \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \operatorname{Tan}[c]^2} \right) \right) / \left( a \sqrt{1 + \operatorname{Tan}[c]^2} \left( 1 - \frac{b \operatorname{Sec}[c]}{a \sqrt{1 + \operatorname{Tan}[c]^2}} \right) \right) \right) \right), \\
 & - \left( \left( \operatorname{Sec}[c] \left( b + a \operatorname{Cos}[c] \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2} \right) \right) / \right. \\
 & \quad \left. \left( a \sqrt{1 + \operatorname{Tan}[c]^2} \left( -1 - \frac{b \operatorname{Sec}[c]}{a \sqrt{1 + \operatorname{Tan}[c]^2}} \right) \right) \right) \operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] \Big) / \\
 & \left( \sqrt{1 + \operatorname{Tan}[c]^2} \sqrt{\left( \left( a \sqrt{1 + \operatorname{Tan}[c]^2} - a \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2} \right) / \right. \right. \\
 & \quad \left. \left. \left( b \operatorname{Sec}[c] + a \sqrt{1 + \operatorname{Tan}[c]^2} \right) \right) \sqrt{\left( \left( a \sqrt{1 + \operatorname{Tan}[c]^2} + \right. \right. \right. \\
 & \quad \left. \left. \left. a \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2} \right) / \left( -b \operatorname{Sec}[c] + a \sqrt{1 + \operatorname{Tan}[c]^2} \right) \right) \right)} \\
 & \left. \sqrt{b + a \operatorname{Cos}[c] \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}} \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{\sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \left( 2 a \text{Cos}[c] \left( b + a \text{Cos}[c] \text{Cos} [ \right. \right. \right. \\
 & \quad \left. \left. \left. d x + \text{ArcTan}[\text{Tan}[c]] \right] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a^2 \text{Cos}[c]^2 + a^2 \text{Sin}[c]^2 \right) \Bigg) / \\
 & \left( \sqrt{b + a \text{Cos}[c] \text{Cos} [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) \Bigg) / \\
 & \left( 3 \left( a^2 - b^2 \right)^2 d \left( A + 2 C + 2 B \text{Cos}[c + d x] + A \text{Cos}[2 c + 2 d x] \right) \left( a + b \text{Sec}[c + d x] \right)^{5/2} - \right. \\
 & \left. 56 b^3 B \left( b + a \text{Cos}[c + d x] \right)^{5/2} \text{Csc}[c] \sqrt{\text{Sec}[c + d x]} \right. \\
 & \left. \left( A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2 \right) \right. \\
 & \left. \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos} [d x + \text{ArcTan}[\text{Tan}[c]]] \right) \right. \right. \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a \sqrt{1 + \text{Tan}[c]^2} \left( 1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \Bigg), \\
 & - \left( \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos} [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \right. \\
 & \quad \left. \left( a \sqrt{1 + \text{Tan}[c]^2} \left( -1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \Bigg) \sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] \Bigg) / \\
 & \left( \sqrt{1 + \text{Tan}[c]^2} \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} - a \text{Cos} [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) / \right. \right. \\
 & \quad \left. \left. \left( b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} + \right. \right. \right. \\
 & \quad \left. \left. \left. a \text{Cos} [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) / \left( -b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) \right) \\
 & \quad \left. \sqrt{b + a \text{Cos}[c] \text{Cos} [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) - \\
 & \left( \frac{\sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \left( 2 a \text{Cos}[c] \left( b + a \text{Cos}[c] \text{Cos} [ \right. \right. \right. \\
 & \quad \left. \left. \left. d x + \text{ArcTan}[\text{Tan}[c]] \right] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a^2 \text{Cos}[c]^2 + a^2 \text{Sin}[c]^2 \right) \Bigg) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]]} \sqrt{1 + \tan [c]^2} \right) \Bigg) \Bigg) \Bigg) / \\
 & \left( 3 a (a^2 - b^2)^2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. (a + b \sec [c + d x])^{5/2} \right) + \\
 & \left( 32 b^5 B (b + a \cos [c + d x])^{5/2} \csc [c] \sqrt{\sec [c + d x]} \right. \\
 & \quad \left. (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left. \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, -\left( \sec [c] (b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]) \right. \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. \sqrt{1 + \tan [c]^2} \right) \right) \right] / \left( a \sqrt{1 + \tan [c]^2} \left( 1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right) \right) \Bigg) \Bigg) \Bigg) / \\
 & \quad - \left( \left( \sec [c] (b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) \right) \Bigg) \Bigg) \Bigg) / \\
 & \quad \left( a \sqrt{1 + \tan [c]^2} \left( -1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \Bigg) \Bigg) \left[ \sin [d x + \text{ArcTan} [\tan [c]]] \tan [c] \right] \Bigg) \Bigg) \Bigg) / \\
 & \quad \left( \sqrt{1 + \tan [c]^2} \sqrt{\left( (a \sqrt{1 + \tan [c]^2} - a \cos [d x + \text{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) \right) \Bigg) \Bigg) \Bigg) / \\
 & \quad \left( b \sec [c] + a \sqrt{1 + \tan [c]^2} \right) \sqrt{\left( (a \sqrt{1 + \tan [c]^2} + \right. \\
 & \quad \left. a \cos [d x + \text{ArcTan} [\tan [c]]) \sqrt{1 + \tan [c]^2} \right) \Bigg) \Bigg) \Bigg) / \left( -b \sec [c] + a \sqrt{1 + \tan [c]^2} \right) \Bigg) \Bigg) \Bigg) / \\
 & \quad \left( \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]]} \sqrt{1 + \tan [c]^2} \right) \Bigg) \Bigg) \Bigg) - \\
 & \quad \left( \frac{\sin [d x + \text{ArcTan} [\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \left( 2 a \cos [c] (b + a \cos [c] \cos [ \right. \right. \\
 & \quad \left. \left. d x + \text{ArcTan} [\tan [c]] \right) \sqrt{1 + \tan [c]^2} \right) \Bigg) \Bigg) \Bigg) / (a^2 \cos [c]^2 + a^2 \sin [c]^2) \Bigg) \Bigg) \Bigg) \Bigg) / \\
 & \quad \left( \sqrt{b + a \cos [c] \cos [d x + \text{ArcTan} [\tan [c]]]} \sqrt{1 + \tan [c]^2} \right) \Bigg) \Bigg) \Bigg) \Bigg) / \\
 & \left( 3 a^3 (a^2 - b^2)^2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. (a + b \sec [c + d x])^{5/2} \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2 a^2 C (b + a \cos [c + d x])^{5/2} \operatorname{Csc}[c] \sqrt{\sec [c + d x]} \right. \\
 & \quad \left. (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left( \left( \operatorname{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, -\left( \sec [c] (b + a \cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]) \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \tan [c]^2} \right) \right] \right) / \left( a \sqrt{1 + \tan [c]^2} \left( 1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right), \\
 & \quad - \left( \left( \sec [c] (b + a \cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]) \sqrt{1 + \tan [c]^2} \right) \right) / \\
 & \quad \left( a \sqrt{1 + \tan [c]^2} \left( -1 - \frac{b \sec [c]}{a \sqrt{1 + \tan [c]^2}} \right) \right) \right) \sin [d x + \operatorname{ArcTan}[\tan [c]]] \tan [c] \Big/ \\
 & \quad \left( \sqrt{1 + \tan [c]^2} \sqrt{\left( \left( a \sqrt{1 + \tan [c]^2} - a \cos [d x + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2} \right) \right. \right. \\
 & \quad \left. \left. (b \sec [c] + a \sqrt{1 + \tan [c]^2}) \right) \sqrt{\left( \left( a \sqrt{1 + \tan [c]^2} + \right. \right. \right. \\
 & \quad \left. \left. a \cos [d x + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2} \right) \right) / \left( -b \sec [c] + a \sqrt{1 + \tan [c]^2} \right)} \\
 & \quad \left. \sqrt{b + a \cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}} \right) - \\
 & \quad \left( \frac{\sin [d x + \operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \left( 2 a \cos [c] (b + a \cos [c] \cos [ \right. \right. \\
 & \quad \left. \left. d x + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2} \right) \right) / \left( a^2 \cos [c]^2 + a^2 \sin [c]^2 \right) \Big/ \\
 & \quad \left( \sqrt{b + a \cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}} \right) \Big/ \\
 & \quad \left( (a^2 - b^2)^2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\
 & \quad \left. (a + b \sec [c + d x])^{5/2} \right) + \\
 & \left. 10 b^2 C (b + a \cos [c + d x])^{5/2} \operatorname{Csc}[c] \sqrt{\sec [c + d x]} \right. \\
 & \quad \left. (A + B \sec [c + d x] + C \sec [c + d x]^2) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \right] \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \text{Tan}[c]^2} \right) \right) \right) / \left( a \sqrt{1 + \text{Tan}[c]^2} \left( 1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right), \\
 & - \left( \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \right] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \\
 & \quad \left( a \sqrt{1 + \text{Tan}[c]^2} \left( -1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] \Big) / \\
 & \left( \sqrt{1 + \text{Tan}[c]^2} \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} - a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \sqrt{1 + \text{Tan}[c]^2} \right) \right. \right. \\
 & \quad \left. \left. \left( b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} + \right. \right. \right. \\
 & \quad \left. \left. \left. a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( -b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \right) \\
 & \quad \left. \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) - \\
 & \left( \frac{\text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \left( 2 a \text{Cos}[c] \left( b + a \text{Cos}[c] \text{Cos}[ \right. \right. \right. \\
 & \quad \left. \left. \left. dx + \text{ArcTan}[\text{Tan}[c]] \right) \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a^2 \text{Cos}[c]^2 + a^2 \text{Sin}[c]^2 \right) \Big) / \\
 & \quad \left( \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \Big) \Big) / \\
 & \left( (a^2 - b^2)^2 d (A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2c + 2dx]) \right. \\
 & \quad \left. (a + b \text{Sec}[c + dx])^{5/2} \right) - \\
 & \left( 16 b^4 C (b + a \text{Cos}[c + dx])^{5/2} \text{Csc}[c] \sqrt{\text{Sec}[c + dx]} \right. \\
 & \quad \left. (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \right. \\
 & \left( \left( \text{AppellF1} \left[ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, - \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]] \right) \right) \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1 + \text{Tan}[c]^2} \right) \right) \right) / \left( a \sqrt{1 + \text{Tan}[c]^2} \left( 1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \right) \Big) \Big)
 \end{aligned}$$

$$\begin{aligned}
 & - \left( \left( \text{Sec}[c] \left( b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) \right) / \\
 & \left( a \sqrt{1 + \text{Tan}[c]^2} \left( -1 - \frac{b \text{Sec}[c]}{a \sqrt{1 + \text{Tan}[c]^2}} \right) \right) \left( \text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] \right) / \\
 & \left( \sqrt{1 + \text{Tan}[c]^2} \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} - a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) \right) / \\
 & \left( b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \sqrt{\left( \left( a \sqrt{1 + \text{Tan}[c]^2} + \right. \right. \\
 & \left. \left. a \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( -b \text{Sec}[c] + a \sqrt{1 + \text{Tan}[c]^2} \right) \\
 & \left. \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) - \\
 & \left( \frac{\text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \left( 2 a \text{Cos}[c] \left( b + a \text{Cos}[c] \text{Cos}[ \right. \right. \right. \\
 & \left. \left. \left. dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \right) \right) / \left( a^2 \text{Cos}[c]^2 + a^2 \text{Sin}[c]^2 \right) \right) / \\
 & \left( \sqrt{b + a \text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right) \right) / \\
 & \left( 3 a^2 (a^2 - b^2)^2 d (A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2 c + 2 dx]) \right. \\
 & \left. (a + b \text{Sec}[c + dx])^{5/2} \right)
 \end{aligned}$$

**Problem 1070: Attempted integration timed out after 120 seconds.**

$$\int (a + b \text{Sec}[c + dx])^{2/3} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) dx$$

Optimal (type 8, 248 leaves, 8 steps):



$$\left( \sqrt{2} (a+b) C \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, -\frac{5}{3}, \frac{3}{2}, \frac{1}{2} (1 - \sec [c + d x]), \frac{b (1 - \sec [c + d x])}{a + b} \right] \right. \\ \left. (a + b \sec [c + d x])^{2/3} \tan [c + d x] \right) / \left( b d \sqrt{1 + \sec [c + d x]} \left( \frac{a + b \sec [c + d x]}{a + b} \right)^{2/3} \right) + \\ \left( \sqrt{2} (b B - a C) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, -\frac{2}{3}, \frac{3}{2}, \frac{1}{2} (1 - \sec [c + d x]), \frac{b (1 - \sec [c + d x])}{a + b} \right] \right. \\ \left. (a + b \sec [c + d x])^{2/3} \tan [c + d x] \right) / \\ \left( b d \sqrt{1 + \sec [c + d x]} \left( \frac{a + b \sec [c + d x]}{a + b} \right)^{2/3} \right) + A \operatorname{Int} [ (a + b \sec [c + d x])^{2/3}, x]$$

Result (type 1, 1 leaves):

???

**Problem 1072: Attempted integration timed out after 120 seconds.**

$$\int \frac{A + B \sec [c + d x] + C \sec [c + d x]^2}{(a + b \sec [c + d x])^{1/3}} dx$$

Optimal (type 8, 245 leaves, 8 steps):

$$\left( \sqrt{2} C \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, -\frac{2}{3}, \frac{3}{2}, \frac{1}{2} (1 - \sec [c + d x]), \frac{b (1 - \sec [c + d x])}{a + b} \right] \right. \\ \left. (a + b \sec [c + d x])^{2/3} \tan [c + d x] \right) / \left( b d \sqrt{1 + \sec [c + d x]} \left( \frac{a + b \sec [c + d x]}{a + b} \right)^{2/3} \right) + \\ \left( \sqrt{2} (b B - a C) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{3}, \frac{3}{2}, \frac{1}{2} (1 - \sec [c + d x]), \frac{b (1 - \sec [c + d x])}{a + b} \right] \right. \\ \left. \left( \frac{a + b \sec [c + d x]}{a + b} \right)^{1/3} \tan [c + d x] \right) / \\ \left( b d \sqrt{1 + \sec [c + d x]} (a + b \sec [c + d x])^{1/3} \right) + A \operatorname{Int} \left[ \frac{1}{(a + b \sec [c + d x])^{1/3}}, x \right]$$

Result (type 1, 1 leaves):

???

**Problem 1078: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c + d x]^{3/2} (A + C \sec [c + d x]^2) dx$$

Optimal (type 4, 48 leaves, 3 steps):

$$\frac{2 (A + 3 C) \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right]}{3 d} + \frac{2 A \sqrt{\cos [c + d x]} \sin [c + d x]}{3 d}$$

Result (type 5, 124 leaves):

$$- \left( \left( 4 \sqrt{\cos [c+d x]} (C+A \cos [c+d x])^2 \sin [c] \right. \right. \\ \left. \left. \left( (A+3 C) \sqrt{\cos [d x-\operatorname{ArcTan}[\cot [c]]^2} \sqrt{\csc [c]^2} \operatorname{HypergeometricPFQ} \left[ \right. \right. \right. \right. \\ \left. \left. \left. \left. \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]^2] \sec [d x-\operatorname{ArcTan}[\cot [c]]] \right\} - \right. \right. \right. \right. \\ \left. \left. \left. \left. \left. A \csc [c] \sin [c+d x] \right) \right) \right) \right) / \left( 3 d (A+2 C+A \cos [2(c+d x)]) \right)$$

**Problem 1079: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sqrt{\cos [c+d x]} (A+C \sec [c+d x])^2 dx$$

Optimal (type 4, 44 leaves, 3 steps):

$$\frac{2(A-C) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{d} + \frac{2 C \sin [c+d x]}{d \sqrt{\cos [c+d x]}}$$

Result (type 5, 289 leaves):

$$\left( \cos [c+d x]^2 (A+C \sec [c+d x])^2 \left( -\frac{4((A-2 C) \cos [d x]+A \cos [2 c+d x]) \csc [c]}{d \sqrt{\cos [c+d x]}} + \right. \right. \\ \left. \left( 2(A-C) \csc \left[\frac{c}{2}\right] \left( 3 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x}(\cos [c]+i \sin [c])^2\right] + \right. \right. \right. \\ \left. \left. \left. e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x}(\cos [c]+i \sin [c])^2\right] \right) \right) \right. \\ \left. \left. \sec \left[\frac{c}{2}\right] \sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)} \right. \right. \\ \left. \left. \sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]} \right) \right) / \left( 3 d\left(\left(1+e^{2 i d x}\right) \cos [c]+i\left(-1+e^{2 i d x}\right) \sin [c]\right)\right) / \left( 2(A+2 C+A \cos [2(c+d x)]) \right)$$

**Problem 1083: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c+d x]^{9 / 2}(a+a \sec [c+d x])(A+C \sec [c+d x])^2 dx$$

Optimal (type 4, 165 leaves, 8 steps):

$$\frac{2a(7A+9C) \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{15d} + \frac{2a(5A+7C) \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{21d} +$$

$$\frac{2a(5A+7C) \sqrt{\cos[c+dx]} \sin[c+dx]}{21d} + \frac{2a(7A+9C) \cos[c+dx]^{3/2} \sin[c+dx]}{45d} +$$

$$\frac{2aA \cos[c+dx]^{5/2} \sin[c+dx]}{7d} + \frac{2aA \cos[c+dx]^{7/2} \sin[c+dx]}{9d}$$

Result(type 5, 918 leaves):

$$a \left( \sqrt{\cos[c+dx]} \left(1 + \cos[c+dx]\right) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \right.$$

$$\left( -\frac{(7A+9C) \cot[c]}{15d} + \frac{(23A+28C) \cos[dx] \sin[c]}{84d} + \frac{(19A+18C) \cos[2dx] \sin[2c]}{180d} + \right.$$

$$\frac{A \cos[3dx] \sin[3c]}{28d} + \frac{A \cos[4dx] \sin[4c]}{72d} + \frac{(23A+28C) \cos[c] \sin[dx]}{84d} +$$

$$\left. \frac{(19A+18C) \cos[2c] \sin[2dx]}{180d} + \frac{A \cos[3c] \sin[3dx]}{28d} + \frac{A \cos[4c] \sin[4dx]}{72d} \right) -$$

$$\left( 5A(1 + \cos[c+dx]) \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\cot[c]]]\right]^2 \right.$$

$$\operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Sec}[dx - \operatorname{ArcTan}[\cot[c]]] \sqrt{1 - \sin[dx - \operatorname{ArcTan}[\cot[c]]]}$$

$$\sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]]]}$$

$$\left. \sqrt{1 + \sin[dx - \operatorname{ArcTan}[\cot[c]]]} \right) / \left( 21d \sqrt{1 + \cot[c]^2} \right) -$$

$$\left( C(1 + \cos[c+dx]) \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\cot[c]]]\right]^2 \right.$$

$$\operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Sec}[dx - \operatorname{ArcTan}[\cot[c]]] \sqrt{1 - \sin[dx - \operatorname{ArcTan}[\cot[c]]]}$$

$$\left. \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]]]} \sqrt{1 + \sin[dx - \operatorname{ArcTan}[\cot[c]]]} \right) /$$

$$\left( 3d \sqrt{1 + \cot[c]^2} \right) - \frac{1}{30d} 7A(1 + \cos[c+dx]) \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2$$

$$\left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos[dx + \operatorname{ArcTan}[\tan[c]]]\right]^2 \right)$$

$$\begin{aligned}
 & \left( \frac{\sin [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1 - \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]}} \right) / \\
 & \left( \frac{\sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \tan [c]^2} \sqrt{1 + \tan [c]^2}}{\frac{\sin [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}} \right) - \\
 & \left. \frac{1}{10 d} \right) \\
 & 3 C (1 + \cos [c + d x]) \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \right. \right. \\
 & \left. \left. \left\{\frac{3}{4}\right\}, \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]^2\right] \sin [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] \right) / \\
 & \left( \frac{\sin [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1 - \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]}} \right) / \\
 & \left( \frac{\sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \tan [c]^2} \sqrt{1 + \tan [c]^2}}{\frac{\sin [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}} \right) - \\
 & \left. \frac{1}{10 d} \right)
 \end{aligned}$$

**Problem 1084: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c + d x]^{7/2} (a + a \operatorname{Sec}[c + d x]) (A + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 4, 134 leaves, 7 steps):

$$\frac{2a(3A+5C) \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{5d} + \frac{2a(5A+7C) \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{21d} + \frac{2a(5A+7C) \sqrt{\cos[c+dx]} \sin[c+dx]}{21d} + \frac{2aA \cos[c+dx]^{3/2} \sin[c+dx]}{5d} + \frac{2aA \cos[c+dx]^{5/2} \sin[c+dx]}{7d}$$

Result (type 5, 872 leaves):

$$a \left( \sqrt{\cos[c+dx]} (1 + \cos[c+dx]) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \left( -\frac{(3A+5C) \cot[c]}{5d} + \frac{(23A+28C) \cos[dx] \sin[c]}{84d} + \frac{A \cos[2dx] \sin[2c]}{10d} + \frac{A \cos[3dx] \sin[3c]}{28d} + \frac{(23A+28C) \cos[c] \sin[dx]}{84d} + \frac{A \cos[2c] \sin[2dx]}{10d} + \frac{A \cos[3c] \sin[3dx]}{28d} \right) - \left( 5A(1 + \cos[c+dx]) \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\cot[c]]]\right]^2 \right) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Sec}[dx - \operatorname{ArcTan}[\cot[c]]] \sqrt{1 - \sin[dx - \operatorname{ArcTan}[\cot[c]]]} \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]]]} \sqrt{1 + \sin[dx - \operatorname{ArcTan}[\cot[c]]]} \right) / \left( 21d \sqrt{1 + \cot[c]^2} \right) - \left( C(1 + \cos[c+dx]) \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\cot[c]]]\right]^2 \right) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Sec}[dx - \operatorname{ArcTan}[\cot[c]]] \sqrt{1 - \sin[dx - \operatorname{ArcTan}[\cot[c]]]} \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]]]} \sqrt{1 + \sin[dx - \operatorname{ArcTan}[\cot[c]]]} \right) / \left( 3d \sqrt{1 + \cot[c]^2} \right) - \frac{1}{10d} 3A(1 + \cos[c+dx]) \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos[dx + \operatorname{ArcTan}[\tan[c]]]\right]^2 \right) \sin[dx + \operatorname{ArcTan}[\tan[c]]] \tan[c] \right) /$$

$$\left( \frac{\sqrt{1 - \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2} \sqrt{1 + \tan [c]^2}}{\frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]] \text{Tan} [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\text{Tan} [c]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2}}} \right) - \frac{1}{2 d}$$

$$C (1 + \cos [c + d x]) \text{Csc} [c] \text{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \right. \right.$$

$$\left. \left. \frac{\cos [d x + \text{ArcTan} [\text{Tan} [c]]]^2 \sin [d x + \text{ArcTan} [\text{Tan} [c]] \text{Tan} [c]}{\sqrt{1 - \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2} \sqrt{1 + \tan [c]^2}} \right] \right) - \frac{1}{2 d}$$

Problem 1085: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \cos [c + d x]^{5/2} (a + a \text{Sec} [c + d x]) (A + C \text{Sec} [c + d x]^2) dx$$

Optimal (type 4, 101 leaves, 6 steps):

$$\frac{2 a (3 A + 5 C) \text{EllipticE} \left[ \frac{1}{2} (c + d x), 2 \right]}{3 d} + \frac{2 a (A + 3 C) \text{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right]}{3 d} + \frac{2 a A \sqrt{\cos [c + d x]} \sin [c + d x]}{3 d} + \frac{2 a A \cos [c + d x]^{3/2} \sin [c + d x]}{5 d}$$

Result (type 5, 824 leaves):

$$\begin{aligned}
 & a \left( \sqrt{\cos [c+d x]} (1+\cos [c+d x]) \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \left(-\frac{(3 A+5 C) \cot [c]}{5 d}+\frac{A \cos [d x] \sin [c]}{3 d}+\right. \right. \\
 & \quad \left. \left. \frac{A \cos [2 d x] \sin [2 c]}{10 d}+\frac{A \cos [c] \sin [d x]}{3 d}+\frac{A \cos [2 c] \sin [2 d x]}{10 d}\right)-\right. \\
 & \quad \left. \left( A (1+\cos [c+d x]) \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]\right]^2\right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \operatorname{Sec}[d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \right. \\
 & \quad \left. \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]}} \right) / \\
 & \quad \left( 3 d \sqrt{1+\cot [c]^2} \right)-\frac{1}{d \sqrt{1+\cot [c]^2}} C (1+\cos [c+d x]) \operatorname{Csc}[c] \\
 & \quad \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]\right]^2 \\
 & \quad \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \operatorname{Sec}[d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \\
 & \quad \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} - \\
 & \quad \frac{1}{10 d} 3 A (1+\cos [c+d x]) \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \\
 & \quad \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\tan [c]]]\right]^2\right) \\
 & \quad \left. \sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c] \right) / \\
 & \quad \left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \right. \\
 & \quad \left. \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2} \sqrt{1+\tan [c]^2} \right)- \\
 & \quad \left. \frac{\frac{\sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}}+\frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}{\cos [c]^2+\sin [c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2}} \right)-\frac{1}{2 d}
 \end{aligned}$$

$$C (1 + \cos [c + d x]) \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \right.\right.$$

$$\left. \left. \frac{\cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]}{\sin [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]} \right] \right) /$$

$$\left( \sqrt{1 - \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right.$$

$$\left. \sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \operatorname{Tan}[c]^2} \sqrt{1 + \operatorname{Tan}[c]^2} \right) -$$

$$\left( \frac{\frac{\sin [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1 + \operatorname{Tan}[c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \operatorname{Tan}[c]^2}} \right)$$

**Problem 1086: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c + d x]^{3/2} (a + a \operatorname{Sec}[c + d x]) (A + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 4, 95 leaves, 6 steps):

$$\frac{2 a (A - C) \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), 2\right]}{d} + \frac{2 a (A + 3 C) \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), 2\right]}{3 d} +$$

$$\frac{2 a C \sin [c + d x]}{d \sqrt{\cos [c + d x]}} + \frac{2 a A \sqrt{\cos [c + d x]} \sin [c + d x]}{3 d}$$

Result (type 5, 813 leaves):

$$a \left( \sqrt{\cos [c + d x]} (1 + \cos [c + d x]) \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \left( -\frac{(A - 2 C + A \cos [2 c]) \operatorname{Csc}[c] \operatorname{Sec}[c]}{2 d} + \right. \right.$$

$$\left. \frac{A \cos [d x] \sin [c]}{3 d} + \frac{A \cos [c] \sin [d x]}{3 d} + \frac{C \operatorname{Sec}[c] \operatorname{Sec}[c + d x] \sin [d x]}{d} \right) -$$

$$\left( A (1 + \cos [c + d x]) \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2 \right] \right)$$

$$\operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}$$



$$\begin{aligned}
 & \left. \sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]} \sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]} \right) / \\
 & \left( 3d \sqrt{1+\cot[c]^2} \right) - \frac{1}{d \sqrt{1+\cot[c]^2}} C (1+\cos[c+dx]) \csc[c] \\
 & \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\cot[c]]]^2\right] \\
 & \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sec[dx - \text{ArcTan}[\cot[c]]] \sqrt{1-\sin[dx - \text{ArcTan}[\cot[c]]]} \\
 & \sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]} \sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]} - \\
 & \frac{1}{2d} A (1+\cos[c+dx]) \csc[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \\
 & \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos[dx + \text{ArcTan}[\tan[c]]]^2\right] \right. \\
 & \left. \sin[dx + \text{ArcTan}[\tan[c]]] \tan[c] \right) / \left( \sqrt{1-\cos[dx + \text{ArcTan}[\tan[c]]]} \right. \\
 & \left. \sqrt{1+\cos[dx + \text{ArcTan}[\tan[c]]]} \sqrt{\cos[c] \cos[dx + \text{ArcTan}[\tan[c]]]} \sqrt{1+\tan[c]^2} \right. \\
 & \left. \sqrt{1+\tan[c]^2} \right) - \frac{\frac{\sin[dx + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1+\tan[c]^2}} + \frac{2 \cos[c]^2 \cos[dx + \text{ArcTan}[\tan[c]]] \sqrt{1+\tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[dx + \text{ArcTan}[\tan[c]]]} \sqrt{1+\tan[c]^2}} \Bigg) + \\
 & \frac{1}{2d} C (1+\cos[c+dx]) \csc[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \right. \right. \\
 & \left. \left. \left\{\frac{3}{4}\right\}, \cos[dx + \text{ArcTan}[\tan[c]]]^2\right] \sin[dx + \text{ArcTan}[\tan[c]]] \tan[c] \right) / \\
 & \left( \sqrt{1-\cos[dx + \text{ArcTan}[\tan[c]]]} \sqrt{1+\cos[dx + \text{ArcTan}[\tan[c]]]} \right. \\
 & \left. \sqrt{\cos[c] \cos[dx + \text{ArcTan}[\tan[c]]]} \sqrt{1+\tan[c]^2} \sqrt{1+\tan[c]^2} \right) -
 \end{aligned}$$

$$\left( \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \right)$$

**Problem 1087: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sqrt{\cos[c + d x]} (a + a \sec[c + d x]) (A + C \sec[c + d x]^2) dx$$

Optimal (type 4, 95 leaves, 6 steps):

$$\frac{2 a (A - C) \text{EllipticE}\left[\frac{1}{2} (c + d x), 2\right]}{d} + \frac{2 a (3 A + C) \text{EllipticF}\left[\frac{1}{2} (c + d x), 2\right]}{3 d} + \frac{2 a C \sin[c + d x]}{3 d \cos[c + d x]^{3/2}} + \frac{2 a C \sin[c + d x]}{d \sqrt{\cos[c + d x]}}$$

Result (type 5, 817 leaves):

$$a \left( \sqrt{\cos[c + d x]} (1 + \cos[c + d x]) \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \left( -\frac{(A - 2 C + A \cos[2 c]) \csc[c] \sec[c]}{2 d} + \frac{C \sec[c] \sec[c + d x]^2 \sin[d x]}{3 d} + \frac{\sec[c] \sec[c + d x] (C \sin[c] + 3 C \sin[d x])}{3 d} \right) - \frac{1}{d \sqrt{1 + \cot[c]^2}} \right. \\ A (1 + \cos[c + d x]) \csc[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[d x - \text{ArcTan}[\cot[c]]]\right]^2 \\ \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \sec[d x - \text{ArcTan}[\cot[c]]] \sqrt{1 - \sin[d x - \text{ArcTan}[\cot[c]]]} \\ \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[d x - \text{ArcTan}[\cot[c]]] \sqrt{1 + \sin[d x - \text{ArcTan}[\cot[c]]]} - \\ \left. \left( C (1 + \cos[c + d x]) \csc[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[d x - \text{ArcTan}[\cot[c]]]\right]^2 \right. \right. \\ \left. \left. \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \sec[d x - \text{ArcTan}[\cot[c]]] \sqrt{1 - \sin[d x - \text{ArcTan}[\cot[c]]]} \right. \right. \\ \left. \left. \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[d x - \text{ArcTan}[\cot[c]]] \sqrt{1 + \sin[d x - \text{ArcTan}[\cot[c]]]} \right) \right) /$$

$$\begin{aligned}
 & \left( 3 d \sqrt{1 + \cot [c]^2} \right) - \frac{1}{2 d} A (1 + \cos [c + d x]) \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \\
 & \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]^2\right] \right. \\
 & \left. \operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] \right) / \left( \sqrt{1 - \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right) \\
 & \sqrt{1 + \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \tan [c]^2} \\
 & \left. \sqrt{1 + \tan [c]^2} \right) - \frac{\frac{\operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \tan [c]^2}} \left. \right) + \\
 & \frac{1}{2 d} C (1 + \cos [c + d x]) \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \right. \right. \\
 & \left. \left. \left\{\frac{3}{4}\right\}, \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]^2\right] \operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] \right) / \\
 & \left( \sqrt{1 - \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right) \\
 & \left. \sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \tan [c]^2} \sqrt{1 + \tan [c]^2} \right) - \\
 & \left. \frac{\frac{\operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \tan [c]^2}} \right) \left. \right)
 \end{aligned}$$

**Problem 1088: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \operatorname{Sec}[c + d x]) (A + C \operatorname{Sec}[c + d x]^2)}{\sqrt{\cos [c + d x]}} dx$$

Optimal (type 4, 132 leaves, 7 steps):

$$-\frac{2 a (5 A+3 C) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 d}+\frac{2 a (3 A+C) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{3 d}+\frac{2 a C \sin [c+d x]}{5 d \cos [c+d x]^{5 / 2}}+\frac{2 a C \sin [c+d x]}{3 d \cos [c+d x]^{3 / 2}}+\frac{2 a (5 A+3 C) \sin [c+d x]}{5 d \sqrt{\cos [c+d x]}}$$

Result (type 5, 851 leaves):

$$a \left( \sqrt{\cos [c+d x]} \left(1+\cos [c+d x]\right) \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \left(\frac{(5 A+3 C) \operatorname{Csc}[c] \operatorname{Sec}[c]}{5 d}+\frac{C \operatorname{Sec}[c] \operatorname{Sec}[c+d x]^3 \sin [d x]}{5 d}+\frac{\operatorname{Sec}[c] \operatorname{Sec}[c+d x]^2(3 C \sin [c]+5 C \sin [d x])}{15 d}+\frac{\operatorname{Sec}[c] \operatorname{Sec}[c+d x](5 C \sin [c]+15 A \sin [d x]+9 C \sin [d x])}{15 d}\right)-\frac{1}{d \sqrt{1+\cot [c]^2}}\right. \\ A(1+\cos [c+d x]) \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]\right]^2 \\ \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \operatorname{Sec}[d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \\ \left. \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]]} \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]}-\right. \\ \left. \left(C(1+\cos [c+d x]) \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]\right]^2\right. \right. \\ \left. \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \operatorname{Sec}[d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \right. \\ \left. \left. \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]]} \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]}\right) \right) / \\ \left(3 d \sqrt{1+\cot [c]^2}\right)+\frac{1}{2 d} A(1+\cos [c+d x]) \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \\ \left(\operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\tan [c]]]\right]^2\right. \\ \left. \operatorname{Sin}[d x+\operatorname{ArcTan}[\tan [c]]] \tan [c]\right) / \\ \left(\sqrt{1-\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\cos [d x+\operatorname{ArcTan}[\tan [c]]]}\right)$$

$$\begin{aligned}
 & \left( \sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]]} \sqrt{1 + \tan[c]^2} \sqrt{1 + \tan[c]^2} \right) - \\
 & \left( \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]]} \sqrt{1 + \tan[c]^2}} \right) + \frac{1}{10 d} \\
 & 3 C (1 + \cos[c + d x]) \text{Csc}[c] \text{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \right. \right. \\
 & \left. \left. \left\{\frac{3}{4}\right\}, \cos[d x + \text{ArcTan}[\tan[c]]]^2 \sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]\right\} \right) / \\
 & \left( \sqrt{1 - \cos[d x + \text{ArcTan}[\tan[c]]]} \sqrt{1 + \cos[d x + \text{ArcTan}[\tan[c]]]} \right) \\
 & \left( \sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]]} \sqrt{1 + \tan[c]^2} \sqrt{1 + \tan[c]^2} \right) - \\
 & \left( \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]]} \sqrt{1 + \tan[c]^2}} \right)
 \end{aligned}$$

**Problem 1089: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \sec[c + d x]) (A + C \sec[c + d x]^2)}{\cos[c + d x]^{3/2}} dx$$

Optimal (type 4, 165 leaves, 8 steps):

$$\begin{aligned}
 & -\frac{2 a (5 A + 3 C) \text{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{5 d} + \frac{2 a (7 A + 5 C) \text{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{21 d} + \\
 & \frac{2 a C \sin[c + d x]}{7 d \cos[c + d x]^{7/2}} + \frac{2 a C \sin[c + d x]}{5 d \cos[c + d x]^{5/2}} + \frac{2 a (7 A + 5 C) \sin[c + d x]}{21 d \cos[c + d x]^{3/2}} + \frac{2 a (5 A + 3 C) \sin[c + d x]}{5 d \sqrt{\cos[c + d x]}}
 \end{aligned}$$

Result (type 5, 895 leaves):

$$\begin{aligned}
 & a \left( \sqrt{\cos [c+d x]} (1+\cos [c+d x]) \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \left(\frac{(5 A+3 C) \operatorname{Csc}[c] \operatorname{Sec}[c]}{5 d}+\right.\right. \\
 & \quad \left.\left.\frac{C \operatorname{Sec}[c] \operatorname{Sec}[c+d x]^4 \operatorname{Sin}[d x]}{7 d}+\frac{\operatorname{Sec}[c] \operatorname{Sec}[c+d x]^3(5 C \operatorname{Sin}[c]+7 C \operatorname{Sin}[d x])}{35 d}+\frac{1}{105 d} \operatorname{Sec}[c] \operatorname{Sec}[c+d x]^2(21 C \operatorname{Sin}[c]+35 A \operatorname{Sin}[d x]+25 C \operatorname{Sin}[d x])+\frac{1}{105 d} \right.\right. \\
 & \quad \left.\left.\operatorname{Sec}[c] \operatorname{Sec}[c+d x](35 A \operatorname{Sin}[c]+25 C \operatorname{Sin}[c]+105 A \operatorname{Sin}[d x]+63 C \operatorname{Sin}[d x])\right)\right) - \\
 & \left( A(1+\cos [c+d x]) \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2\right) \\
 & \quad \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \operatorname{Sec}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1-\operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \quad \sqrt{-\sqrt{1+\operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \quad \left. \sqrt{1+\operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) / \left(3 d \sqrt{1+\operatorname{Cot}[c]^2}\right) - \\
 & \left( 5 C(1+\cos [c+d x]) \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2\right) \\
 & \quad \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \operatorname{Sec}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1-\operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \quad \left. \sqrt{-\sqrt{1+\operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1+\operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) / \\
 & \quad \left(21 d \sqrt{1+\operatorname{Cot}[c]^2}\right) + \frac{1}{2 d} A(1+\cos [c+d x]) \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \\
 & \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \operatorname{Cos}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]\right]^2\right) \\
 & \quad \left. \operatorname{Sin}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] \right) / \\
 & \left( \sqrt{1-\operatorname{Cos}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1+\operatorname{Cos}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right. \\
 & \quad \left. \sqrt{\operatorname{Cos}[c] \operatorname{Cos}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1+\operatorname{Tan}[c]^2} \sqrt{1+\operatorname{Tan}[c]^2} \right) -
 \end{aligned}$$

$$\left. \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \right) + \frac{1}{10 d}$$

$$3 C (1 + \cos[c + d x]) \text{Csc}[c] \text{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos[d x + \text{ArcTan}[\tan[c]]]^2\right] \sin[d x + \text{ArcTan}[\tan[c]]] \tan[c] \right) /$$

$$\left( \frac{\sqrt{1 - \cos[d x + \text{ArcTan}[\tan[c]]]} \sqrt{1 + \cos[d x + \text{ArcTan}[\tan[c]]]}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}} \sqrt{1 + \tan[c]^2}} \right) -$$

$$\left. \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \right)$$

**Problem 1090: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c + d x]^{11/2} (a + a \sec[c + d x])^2 (A + C \sec[c + d x]^2) dx$$

Optimal (type 4, 230 leaves, 10 steps):

$$\frac{4 a^2 (7 A + 9 C) \text{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{15 d} + \frac{8 a^2 (25 A + 33 C) \text{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{231 d} +$$

$$\frac{8 a^2 (25 A + 33 C) \sqrt{\cos[c + d x]} \sin[c + d x]}{231 d} + \frac{4 a^2 (7 A + 9 C) \cos[c + d x]^{3/2} \sin[c + d x]}{45 d} +$$

$$\frac{2 a^2 (89 A + 99 C) \cos[c + d x]^{5/2} \sin[c + d x]}{693 d} + \frac{2 A \cos[c + d x]^{5/2} (a + a \cos[c + d x])^2 \sin[c + d x]}{11 d} +$$

$$\frac{8 A \cos[c + d x]^{5/2} (a^2 + a^2 \cos[c + d x]) \sin[c + d x]}{99 d}$$

Result (type 5, 976 leaves):

$$\begin{aligned}
 & a^2 \left( \sqrt{\cos [c+d x]} (1+\cos [c+d x])^2 \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 \right. \\
 & \left. -\frac{(7 A+9 C) \cot [c]}{15 d}+\frac{(941 A+1122 C) \cos [d x] \sin [c]}{3696 d}+\frac{(19 A+18 C) \cos [2 d x] \sin [2 c]}{180 d}+\right. \\
 & \left. \frac{(101 A+44 C) \cos [3 d x] \sin [3 c]}{2464 d}+\frac{A \cos [4 d x] \sin [4 c]}{72 d}+\frac{A \cos [5 d x] \sin [5 c]}{352 d}+\right. \\
 & \left. \frac{(941 A+1122 C) \cos [c] \sin [d x]}{3696 d}+\frac{(19 A+18 C) \cos [2 c] \sin [2 d x]}{180 d}+\right. \\
 & \left. \frac{(101 A+44 C) \cos [3 c] \sin [3 d x]}{2464 d}+\frac{A \cos [4 c] \sin [4 d x]}{72 d}+\frac{A \cos [5 c] \sin [5 d x]}{352 d}\right) - \\
 & \left( 50 A(1+\cos [c+d x])^2 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]\right]^2 \right) \\
 & \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 \operatorname{Sec}[d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \\
 & \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]]} \\
 & \left. \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \right) / \left( 231 d \sqrt{1+\cot [c]^2} \right) - \\
 & \left( 2 C(1+\cos [c+d x])^2 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]\right]^2 \right) \\
 & \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 \operatorname{Sec}[d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \\
 & \left. \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]]} \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \right) / \\
 & \left( 7 d \sqrt{1+\cot [c]^2} \right) -\frac{1}{30 d} 7 A(1+\cos [c+d x])^2 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 \\
 & \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\tan [c]]]\right]^2 \right) \\
 & \left. \sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c] \right) / \\
 & \left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \right)
 \end{aligned}$$



$$\begin{aligned}
 & \left( \sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]]} \sqrt{1 + \tan[c]^2} \sqrt{1 + \tan[c]^2} \right) - \\
 & \left( \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]]} \sqrt{1 + \tan[c]^2}} \right) - \frac{1}{10 d} \\
 & 3 C (1 + \cos[c + d x])^2 \text{Csc}[c] \text{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^4 \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \right. \right. \\
 & \left. \left. \left\{\frac{3}{4}\right\}, \cos[d x + \text{ArcTan}[\tan[c]]]^2 \sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]\right\} \right) / \\
 & \left( \sqrt{1 - \cos[d x + \text{ArcTan}[\tan[c]]]} \sqrt{1 + \cos[d x + \text{ArcTan}[\tan[c]]]} \right) \\
 & \left( \sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]]} \sqrt{1 + \tan[c]^2} \sqrt{1 + \tan[c]^2} \right) - \\
 & \left( \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]]} \sqrt{1 + \tan[c]^2}} \right)
 \end{aligned}$$

**Problem 1091: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c + d x]^{9/2} (a + a \sec[c + d x])^2 (A + C \sec[c + d x])^2 dx$$

Optimal (type 4, 197 leaves, 9 steps):

$$\begin{aligned}
 & \frac{16 a^2 (2 A + 3 C) \text{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{15 d} + \frac{4 a^2 (5 A + 7 C) \text{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{21 d} + \\
 & \frac{4 a^2 (5 A + 7 C) \sqrt{\cos[c + d x]} \sin[c + d x]}{21 d} + \frac{2 a^2 (19 A + 21 C) \cos[c + d x]^{3/2} \sin[c + d x]}{105 d} + \\
 & \frac{2 A \cos[c + d x]^{3/2} (a + a \cos[c + d x])^2 \sin[c + d x]}{9 d} + \\
 & \frac{8 A \cos[c + d x]^{3/2} (a^2 + a^2 \cos[c + d x]) \sin[c + d x]}{63 d}
 \end{aligned}$$

Result (type 5, 1118 leaves):

$$\left( \cos [c+d x]^{9/2} \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a+a \sec [c+d x])^2 (A+C \sec [c+d x])^2 \right. \\ \left( -\frac{8(2 A+3 C) \cot [c]}{15 d} + \frac{(23 A+28 C) \cos [d x] \sin [c]}{42 d} + \frac{(37 A+18 C) \cos [2 d x] \sin [2 c]}{180 d} + \right. \\ \left. \frac{A \cos [3 d x] \sin [3 c]}{14 d} + \frac{A \cos [4 d x] \sin [4 c]}{72 d} + \frac{(23 A+28 C) \cos [c] \sin [d x]}{42 d} + \right. \\ \left. \frac{(37 A+18 C) \cos [2 c] \sin [2 d x]}{180 d} + \frac{A \cos [3 c] \sin [3 d x]}{14 d} + \frac{A \cos [4 c] \sin [4 d x]}{72 d} \right) \Bigg) / \\ (A+2 C+A \cos [2 c+2 d x]) - \frac{1}{21 d (A+2 C+A \cos [2 c+2 d x]) \sqrt{1+\cot [c]^2}} \\ 10 A \cos [c+d x]^4 \csc [c] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan}[\cot [c]]] \right]^2 \\ \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a+a \sec [c+d x])^2 (A+C \sec [c+d x])^2 \\ \sec [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\cot [c]]]} \\ \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x - \operatorname{ArcTan}[\cot [c]]]} -} \\ \frac{1}{3 d (A+2 C+A \cos [2 c+2 d x]) \sqrt{1+\cot [c]^2}} \\ 2 C \cos [c+d x]^4 \csc [c] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan}[\cot [c]]] \right]^2 \\ \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a+a \sec [c+d x])^2 (A+C \sec [c+d x])^2 \\ \sec [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\cot [c]]]} \\ \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x - \operatorname{ArcTan}[\cot [c]]]} -} \\ \left( 8 A \cos [c+d x]^4 \csc [c] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a+a \sec [c+d x])^2 (A+C \sec [c+d x])^2 \right) \\ \left( \operatorname{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \operatorname{ArcTan}[\tan [c]]] \right]^2 \right) \\ \left( \sin [d x + \operatorname{ArcTan}[\tan [c]]] \tan [c] \right) / \left( \sqrt{1 - \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \right) \\ \sqrt{1 + \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \sqrt{1 + \tan [c]^2}$$

$$\left. \left. \left. \left. \sqrt{1 + \tan[c]^2} \right) - \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \right) \right) \right) /$$

$$(15 d (A + 2 C + A \cos[2 c + 2 d x])) - \left( 4 C \cos[c + d x]^4 \csc[c] \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^4 \right.$$

$$\left. \left. \left. \left. (a + a \sec[c + d x])^2 (A + C \sec[c + d x])^2 \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \right. \right. \right. \right. \right. \right.$$

$$\left. \left. \left. \left. \left\{\frac{3}{4}\right\}, \cos[d x + \text{ArcTan}[\tan[c]]]^2 \right] \sin[d x + \text{ArcTan}[\tan[c]]] \tan[c] \right) \right) \right) /$$

$$\left( \sqrt{1 - \cos[d x + \text{ArcTan}[\tan[c]]]} \sqrt{1 + \cos[d x + \text{ArcTan}[\tan[c]]]} \right.$$

$$\left. \left. \left. \left. \sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}} \sqrt{1 + \tan[c]^2} \right) - \right. \right.$$

$$\left. \left. \left. \left. \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \right) \right) \right) / (5 d (A +$$

$$2 C + A \cos[2 c + 2 d x]))$$

Problem 1092: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \cos[c + d x]^{7/2} (a + a \sec[c + d x])^2 (A + C \sec[c + d x])^2 dx$$

Optimal (type 4, 164 leaves, 8 steps):

$$\frac{4 a^2 (3 A + 5 C) \text{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{5 d} + \frac{8 a^2 (3 A + 7 C) \text{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{21 d} +$$

$$\frac{2 a^2 (33 A + 35 C) \sqrt{\cos[c + d x]} \sin[c + d x]}{105 d} + \frac{2 A \sqrt{\cos[c + d x]} (a + a \cos[c + d x])^2 \sin[c + d x]}{7 d} +$$

$$\frac{8 A \sqrt{\cos[c + d x]} (a^2 + a^2 \cos[c + d x]) \sin[c + d x]}{35 d}$$

Result (type 5, 1070 leaves):

$$\left( \cos [c+d x]^{9/2} \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2 (A+C \operatorname{Sec}[c+d x]^2) \left( -\frac{2(3 A+5 C) \operatorname{Cot}[c]}{5 d} + \frac{(51 A+28 C) \cos [d x] \sin [c]}{84 d} + \frac{A \cos [2 d x] \sin [2 c]}{5 d} + \frac{A \cos [3 d x] \sin [3 c]}{28 d} + \frac{(51 A+28 C) \cos [c] \sin [d x]}{84 d} + \frac{A \cos [2 c] \sin [2 d x]}{5 d} + \frac{A \cos [3 c] \sin [3 d x]}{28 d} \right) \right) /$$

$$(A+2 C+A \cos [2 c+2 d x]) - \frac{1}{7 d (A+2 C+A \cos [2 c+2 d x]) \sqrt{1+\operatorname{Cot}[c]^2}}$$

$$4 A \cos [c+d x]^4 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2$$

$$\operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2 (A+C \operatorname{Sec}[c+d x]^2)$$

$$\operatorname{Sec}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]}$$

$$\sqrt{-\sqrt{1+\operatorname{Cot}[c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} - \frac{1}{3 d (A+2 C+A \cos [2 c+2 d x]) \sqrt{1+\operatorname{Cot}[c]^2}}$$

$$4 C \cos [c+d x]^4 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2$$

$$\operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2 (A+C \operatorname{Sec}[c+d x]^2)$$

$$\operatorname{Sec}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]}$$

$$\sqrt{-\sqrt{1+\operatorname{Cot}[c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} - \left( 3 A \cos [c+d x]^4 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2 (A+C \operatorname{Sec}[c+d x]^2) \right.$$

$$\left. \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]\right]^2 \right) \right) / \left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right.$$

$$\left. \sqrt{1+\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1+\operatorname{Tan}[c]^2} \right)$$

$$\left. \left( \sqrt{1 + \tan[c]^2} \right) - \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \right) /$$

$$(5 d (A + 2 C + A \cos[2 c + 2 d x])) - \left( C \cos[c + d x]^4 \csc[c] \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^4 (a + a \sec[c + d x])^2 \right.$$

$$(A + C \sec[c + d x]^2) \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos[d x + \text{ArcTan}[\tan[c]]]\right]^2 \right)$$

$$\left. \frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 - \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \cos[d x + \text{ArcTan}[\tan[c]]]}}} \right) /$$

$$\left( \sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}} \sqrt{1 + \tan[c]^2} \right) -$$

$$\left. \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \right) / (d (A +$$

$$2 C + A \cos[2 c + 2 d x]))$$

**Problem 1093: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c + d x]^{5/2} (a + a \sec[c + d x])^2 (A + C \sec[c + d x])^2 dx$$

Optimal (type 4, 158 leaves, 8 steps):

$$\frac{16 a^2 A \text{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{5 d} + \frac{4 a^2 (A + 3 C) \text{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{3 d} +$$

$$\frac{2 a^2 (7 A - 15 C) \sqrt{\cos[c + d x]} \sin[c + d x]}{15 d} + \frac{2 C (a + a \cos[c + d x])^2 \sin[c + d x]}{d \sqrt{\cos[c + d x]}} +$$

$$\frac{2 (A - 5 C) \sqrt{\cos[c + d x]} (a^2 + a^2 \cos[c + d x]) \sin[c + d x]}{5 d}$$

Result (type 5, 799 leaves):

$$\left( \cos [c+d x]^{9/2} \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2 \right. \\ \left. (A+C \operatorname{Sec}[c+d x])^2 \left( -\frac{(8 A-5 C+8 A \cos [2 c]+5 C \cos [2 c]) \operatorname{Csc}[c] \operatorname{Sec}[c]}{10 d} + \right. \right. \\ \left. \frac{2 A \cos [d x] \sin [c]}{3 d} + \frac{A \cos [2 d x] \sin [2 c]}{10 d} + \frac{2 A \cos [c] \sin [d x]}{3 d} + \right. \\ \left. \left. \frac{C \operatorname{Sec}[c] \operatorname{Sec}[c+d x] \sin [d x]}{d} + \frac{A \cos [2 c] \sin [2 d x]}{10 d} \right) \right) / \\ (A+2 C+A \cos [2 c+2 d x]) - \frac{1}{3 d (A+2 C+A \cos [2 c+2 d x]) \sqrt{1+\cot [c]^2}} \\ 2 A \cos [c+d x]^4 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right] \\ \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2 (A+C \operatorname{Sec}[c+d x])^2 \\ \operatorname{Sec}[d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \\ \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]]} \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} - \\ \frac{1}{d (A+2 C+A \cos [2 c+2 d x]) \sqrt{1+\cot [c]^2}} \\ 2 C \cos [c+d x]^4 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right] \\ \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2 (A+C \operatorname{Sec}[c+d x])^2 \\ \operatorname{Sec}[d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \\ \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]]} \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} - \\ \left( 4 A \cos [c+d x]^4 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2 (A+C \operatorname{Sec}[c+d x])^2 \right. \\ \left. \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\tan [c]]]^2\right] \sin [d x+\operatorname{ArcTan}[\tan [c]]] \right. \right. \\ \left. \left. \operatorname{Tan}[c] \right) \right) / \left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \right)$$

$$\left( \sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]]} \sqrt{1 + \tan[c]^2} \sqrt{1 + \tan[c]^2} \right) - \left( \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]]} \sqrt{1 + \tan[c]^2}} \right) / (5 d (A + 2 C + A \cos[2 c + 2 d x]))$$

**Problem 1094: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c + d x]^{3/2} (a + a \sec[c + d x])^2 (A + C \sec[c + d x])^2 dx$$

Optimal (type 4, 154 leaves, 8 steps):

$$\frac{4 a^2 (A - C) \text{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{d} + \frac{8 a^2 (A + C) \text{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{3 d} + \frac{2 a^2 (A - 5 C) \sqrt{\cos[c + d x]} \sin[c + d x]}{3 d} + \frac{2 C (a + a \cos[c + d x])^2 \sin[c + d x]}{3 d \cos[c + d x]^{3/2}} + \frac{8 C (a^2 + a^2 \cos[c + d x]) \sin[c + d x]}{3 d \sqrt{\cos[c + d x]}}$$

Result (type 5, 1040 leaves):

$$\left( \cos[c + d x]^{9/2} \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^4 (a + a \sec[c + d x])^2 (A + C \sec[c + d x])^2 \left( -\frac{(A - 2 C + A \cos[2 c]) \csc[c] \sec[c]}{d} + \frac{A \cos[d x] \sin[c]}{3 d} + \frac{A \cos[c] \sin[d x]}{3 d} + \frac{C \sec[c] \sec[c + d x]^2 \sin[d x]}{3 d} + \frac{\sec[c] \sec[c + d x] (C \sin[c] + 6 C \sin[d x])}{3 d} \right) \right) / (A + 2 C + A \cos[2 c + 2 d x]) - \frac{1}{3 d (A + 2 C + A \cos[2 c + 2 d x]) \sqrt{1 + \cot[c]^2}} - 4 A \cos[c + d x]^4 \csc[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[d x - \text{ArcTan}[\cot[c]]]^2\right] \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^4 (a + a \sec[c + d x])^2 (A + C \sec[c + d x])^2 \sec[d x - \text{ArcTan}[\cot[c]]] \sqrt{1 - \sin[d x - \text{ArcTan}[\cot[c]]]} \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[d x - \text{ArcTan}[\cot[c]]]} \sqrt{1 + \sin[d x - \text{ArcTan}[\cot[c]]]} - \frac{1}{3 d (A + 2 C + A \cos[2 c + 2 d x]) \sqrt{1 + \cot[c]^2}}$$

$$4 C \cos [c+d x]^4 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right]$$

$$\operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2 (A+C \operatorname{Sec}[c+d x]^2)$$

$$\operatorname{Sec}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]}$$

$$\sqrt{-\sqrt{1+\operatorname{Cot}[c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} -$$

$$\left( A \cos [c+d x]^4 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2 (A+C \operatorname{Sec}[c+d x]^2) \right.$$

$$\left. \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]^2\right] \right) \right.$$

$$\left. \sin [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] \right) / \left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right.$$

$$\left. \sqrt{1+\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1+\operatorname{Tan}[c]^2} \right.$$

$$\left. \left. \sqrt{1+\operatorname{Tan}[c]^2} \right) - \frac{\frac{\sin [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1+\operatorname{Tan}[c]^2}} + \frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1+\operatorname{Tan}[c]^2}}{\cos [c]^2+\sin [c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1+\operatorname{Tan}[c]^2}} \right) /$$

$$(d(A+2 C+A \cos [2 c+2 d x])) + \left( C \cos [c+d x]^4 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2 \right.$$

$$\left. (A+C \operatorname{Sec}[c+d x]^2) \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]^2\right] \right) \right.$$

$$\left. \sin [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] \right) /$$

$$\left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1+\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right)$$



$$\left( \sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]]} \sqrt{1 + \tan[c]^2} \sqrt{1 + \tan[c]^2} \right) - \left( \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]]} \sqrt{1 + \tan[c]^2}} \right) / (d (A + 2 C + A \cos[2 c + 2 d x]))$$

**Problem 1095: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sqrt{\cos[c + d x]} (a + a \sec[c + d x])^2 (A + C \sec[c + d x])^2 dx$$

Optimal (type 4, 156 leaves, 8 steps):

$$\begin{aligned} & -\frac{16 a^2 C \text{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{5 d} + \\ & \frac{4 a^2 (3 A + C) \text{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{3 d} + \frac{2 a^2 (15 A + 17 C) \sin[c + d x]}{15 d \sqrt{\cos[c + d x]}} + \\ & \frac{2 C (a + a \cos[c + d x])^2 \sin[c + d x]}{5 d \cos[c + d x]^{5/2}} + \frac{8 C (a^2 + a^2 \cos[c + d x]) \sin[c + d x]}{15 d \cos[c + d x]^{3/2}} \end{aligned}$$

Result (type 5, 800 leaves):

$$\begin{aligned} & \left( \cos[c + d x]^{9/2} \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^4 (a + a \sec[c + d x])^2 \right. \\ & \quad (A + C \sec[c + d x])^2 \left( -\frac{(-5 A - 16 C + 5 A \cos[2 c]) \csc[c] \sec[c]}{10 d} + \right. \\ & \quad \left. \frac{C \sec[c] \sec[c + d x]^3 \sin[d x]}{5 d} + \frac{\sec[c] \sec[c + d x]^2 (3 C \sin[c] + 10 C \sin[d x])}{15 d} + \right. \\ & \quad \left. \left. \frac{1}{15 d} \sec[c] \sec[c + d x] (10 C \sin[c] + 15 A \sin[d x] + 24 C \sin[d x]) \right) \right) / \\ & (A + 2 C + A \cos[2 c + 2 d x]) - \frac{1}{d (A + 2 C + A \cos[2 c + 2 d x]) \sqrt{1 + \cot[c]^2}} \\ & 2 A \cos[c + d x]^4 \csc[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[d x - \text{ArcTan}[\cot[c]]]^2\right] \\ & \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^4 (a + a \sec[c + d x])^2 (A + C \sec[c + d x])^2 \\ & \sec[d x - \text{ArcTan}[\cot[c]]] \sqrt{1 - \sin[d x - \text{ArcTan}[\cot[c]]]} \\ & \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[d x - \text{ArcTan}[\cot[c]]]} \sqrt{1 + \sin[d x - \text{ArcTan}[\cot[c]]]} - \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{3 d (A + 2 C + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2}} \\
 & 2 C \cos [c + d x]^4 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\cot [c]]]^2\right] \\
 & \sec \left[\frac{c}{2} + \frac{d x}{2}\right]^4 (a + a \sec [c + d x])^2 (A + C \sec [c + d x]^2) \\
 & \sec [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\cot [c]]]} \\
 & \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\cot [c]]]} +} \\
 & \left( 4 C \cos [c + d x]^4 \csc [c] \sec \left[\frac{c}{2} + \frac{d x}{2}\right]^4 (a + a \sec [c + d x])^2 (A + C \sec [c + d x]^2) \right. \\
 & \left. \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos [d x + \operatorname{ArcTan}[\tan [c]]]^2\right] \sin [d x + \operatorname{ArcTan}[\tan [c]]] \right. \right. \\
 & \left. \left. \tan [c] \right) \right) / \left( \sqrt{1 - \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \sqrt{1 + \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \right. \\
 & \left. \sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \sqrt{1 + \tan [c]^2} \sqrt{1 + \tan [c]^2} \right) - \\
 & \left. \frac{\frac{\sin [d x + \operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \sqrt{1 + \tan [c]^2}} \right) / (5 d (A + \\
 & 2 C + A \cos [2 c + 2 d x]))
 \end{aligned}$$

**Problem 1096: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \sec [c + d x])^2 (A + C \sec [c + d x]^2)}{\sqrt{\cos [c + d x]}} dx$$

Optimal (type 4, 197 leaves, 9 steps):

$$\begin{aligned}
 & - \frac{4 a^2 (5 A+3 C) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 d} + \frac{8 a^2 (7 A+3 C) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{21 d} + \\
 & \frac{2 a^2 (35 A+33 C) \operatorname{Sin}[c+d x]}{105 d \operatorname{Cos}[c+d x]^{3 / 2}} + \frac{4 a^2 (5 A+3 C) \operatorname{Sin}[c+d x]}{5 d \sqrt{\operatorname{Cos}[c+d x]}} + \\
 & \frac{2 C(a+a \operatorname{Cos}[c+d x])^2 \operatorname{Sin}[c+d x]}{7 d \operatorname{Cos}[c+d x]^{7 / 2}} + \frac{8 C\left(a^2+a^2 \operatorname{Cos}[c+d x]\right) \operatorname{Sin}[c+d x]}{35 d \operatorname{Cos}[c+d x]^{5 / 2}}
 \end{aligned}$$

Result (type 5, 1092 leaves):

$$\begin{aligned}
 & \left( \operatorname{Cos}[c+d x]^{9 / 2} \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2 \right. \\
 & \quad (A+C \operatorname{Sec}[c+d x])^2 \left( \frac{2(5 A+3 C) \operatorname{Csc}[c] \operatorname{Sec}[c]}{5 d} + \frac{C \operatorname{Sec}[c] \operatorname{Sec}[c+d x]^4 \operatorname{Sin}[d x]}{7 d} + \right. \\
 & \quad \left. \frac{\operatorname{Sec}[c] \operatorname{Sec}[c+d x]^3 (5 C \operatorname{Sin}[c]+14 C \operatorname{Sin}[d x])}{35 d} + \frac{1}{105 d} \right. \\
 & \quad \left. \left. \operatorname{Sec}[c] \operatorname{Sec}[c+d x]^2 (42 C \operatorname{Sin}[c]+35 A \operatorname{Sin}[d x]+60 C \operatorname{Sin}[d x]) + \frac{1}{105 d} \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}[c] \operatorname{Sec}[c+d x] (35 A \operatorname{Sin}[c]+60 C \operatorname{Sin}[c]+210 A \operatorname{Sin}[d x]+126 C \operatorname{Sin}[d x]) \right) \right) / \\
 & \quad (A+2 C+A \operatorname{Cos}[2 c+2 d x]) - \frac{1}{3 d(A+2 C+A \operatorname{Cos}[2 c+2 d x]) \sqrt{1+\operatorname{Cot}[c]^2}} \\
 & \quad 4 A \operatorname{Cos}[c+d x]^4 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \\
 & \quad \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2 (A+C \operatorname{Sec}[c+d x])^2 \\
 & \quad \operatorname{Sec}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1-\operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \quad \sqrt{-\sqrt{1+\operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1+\operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} - \\
 & \quad \frac{1}{7 d(A+2 C+A \operatorname{Cos}[2 c+2 d x]) \sqrt{1+\operatorname{Cot}[c]^2}} \\
 & \quad 4 C \operatorname{Cos}[c+d x]^4 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \\
 & \quad \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2 (A+C \operatorname{Sec}[c+d x])^2 \\
 & \quad \operatorname{Sec}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1-\operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \quad \sqrt{-\sqrt{1+\operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1+\operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} + \\
 & \quad \left( A \operatorname{Cos}[c+d x]^4 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2 (A+C \operatorname{Sec}[c+d x])^2 \right.
 \end{aligned}$$

$$\left( \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \right]^2 \right) \right.$$

$$\left. \left. \frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 - \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \right) \right) / \left( \sqrt{1 + \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \text{Tan} [c]^2} \right.$$

$$\left. \left. \left. \left. \sqrt{1 + \text{Tan} [c]^2} \right) - \frac{\frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 + \text{Tan} [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \sqrt{1 + \text{Tan} [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \text{Tan} [c]^2}} \right) \right) \right) /$$

$$\left( d (A + 2 C + A \cos [2 c + 2 d x]) \right) + \left( 3 C \cos [c + d x]^4 \csc [c] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a + a \sec [c + d x])^2 \right.$$

$$\left. \left. \left( A + C \sec [c + d x]^2 \right) \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \right]^2 \right) \right) \right)$$

$$\left. \left. \frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 - \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \right) \right) /$$

$$\left( \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \text{Tan} [c]^2} \sqrt{1 + \text{Tan} [c]^2} \right) -$$

$$\left. \left. \frac{\frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 + \text{Tan} [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \sqrt{1 + \text{Tan} [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \text{Tan} [c]^2}} \right) \right) / (5 d (A +$$

$$2 C + A \cos [2 c + 2 d x])$$

Problem 1097: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(a + a \sec [c + d x])^2 (A + C \sec [c + d x]^2)}{\cos [c + d x]^{3/2}} dx$$

Optimal (type 4, 230 leaves, 10 steps):

$$\begin{aligned} & - \frac{16 a^2 (3 A + 2 C) \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{15 d} + \frac{4 a^2 (7 A + 5 C) \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{21 d} + \\ & \frac{2 a^2 (21 A + 19 C) \sin [c + d x]}{105 d \cos [c + d x]^{5/2}} + \frac{4 a^2 (7 A + 5 C) \sin [c + d x]}{21 d \cos [c + d x]^{3/2}} + \frac{16 a^2 (3 A + 2 C) \sin [c + d x]}{15 d \sqrt{\cos [c + d x]}} + \\ & \frac{2 C (a + a \cos [c + d x])^2 \sin [c + d x]}{9 d \cos [c + d x]^{9/2}} + \frac{8 C (a^2 + a^2 \cos [c + d x]) \sin [c + d x]}{63 d \cos [c + d x]^{7/2}} \end{aligned}$$

Result (type 5, 1137 leaves):

$$\begin{aligned} & \frac{1}{A + 2 C + A \cos [2 c + 2 d x]} \cos [c + d x]^{9/2} \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \\ & \left( (a + a \sec [c + d x])^2 (A + C \sec [c + d x]^2) \left( \frac{8 (3 A + 2 C) \csc [c] \sec [c]}{15 d} + \right. \right. \\ & \quad \left. \frac{C \sec [c] \sec [c + d x]^5 \sin [d x]}{9 d} + \frac{\sec [c] \sec [c + d x]^4 (7 C \sin [c] + 18 C \sin [d x])}{63 d} \right) + \\ & \quad \frac{1}{105 d} 2 \sec [c] \sec [c + d x] (35 A \sin [c] + 25 C \sin [c] + 84 A \sin [d x] + 56 C \sin [d x]) + \\ & \quad \left. \frac{1}{315 d} \sec [c] \sec [c + d x]^3 (90 C \sin [c] + 63 A \sin [d x] + 112 C \sin [d x]) + \frac{1}{315 d} \right. \\ & \quad \left. \sec [c] \sec [c + d x]^2 (63 A \sin [c] + 112 C \sin [c] + 210 A \sin [d x] + 150 C \sin [d x]) \right) - \\ & \frac{1}{3 d (A + 2 C + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2}} 2 A \cos [c + d x]^4 \csc [c] \\ & \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\cot [c]]]^2\right] \\ & \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a + a \sec [c + d x])^2 (A + C \sec [c + d x]^2) \\ & \sec [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\cot [c]]]} \\ & \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\cot [c]]]} - \\ & \frac{1}{21 d (A + 2 C + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2}} \\ & 10 C \cos [c + d x]^4 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\cot [c]]]^2\right] \\ & \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a + a \sec [c + d x])^2 (A + C \sec [c + d x]^2) \\ & \sec [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\cot [c]]]} \\ & \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\cot [c]]]} + \end{aligned}$$

$$\left( 4 A \cos [c+d x]^4 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2 (A+C \operatorname{Sec}[c+d x])^2 \right.$$

$$\left. \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]\right]^2 \right) \right.$$

$$\left. \left. \operatorname{Sin}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]\right) / \left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right) \right.$$

$$\left. \left. \sqrt{1+\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1+\operatorname{Tan}[c]^2} \right. \right.$$

$$\left. \left. \left. \left. \sqrt{1+\operatorname{Tan}[c]^2} \right) - \frac{\frac{\operatorname{Sin}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1+\operatorname{Tan}[c]^2}} + \frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1+\operatorname{Tan}[c]^2}}{\cos [c]^2+\operatorname{Sin}[c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1+\operatorname{Tan}[c]^2}} \right) \right) / \right.$$

$$\left. \left. \left( 5 d (A+2 C+A \cos [2 c+2 d x]) \right) + \left( 8 C \cos [c+d x]^4 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2 \right) \right. \right.$$

$$\left. \left. \left( A+C \operatorname{Sec}[c+d x]^2 \right) \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]\right]^2 \right) \right. \right.$$

$$\left. \left. \left. \left. \operatorname{Sin}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]\right) / \right. \right.$$

$$\left. \left. \left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1+\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right. \right.$$

$$\left. \left. \left. \left. \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1+\operatorname{Tan}[c]^2} \sqrt{1+\operatorname{Tan}[c]^2} \right) - \right. \right.$$

$$\left. \left. \left. \left. \frac{\frac{\operatorname{Sin}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1+\operatorname{Tan}[c]^2}} + \frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1+\operatorname{Tan}[c]^2}}{\cos [c]^2+\operatorname{Sin}[c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1+\operatorname{Tan}[c]^2}} \right) \right) / (15 d (A + \right.$$

$$\left. \left. 2 C+A \cos [2 c+2 d x]) \right) \right)$$

Problem 1098: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \cos [c+d x]^{13 / 2} (a+a \sec [c+d x])^3 (A+C \sec [c+d x]^2) d x$$

Optimal (type 4, 279 leaves, 11 steps):

$$\begin{aligned} & \frac{4 a^3 (175 A+221 C) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{195 d} + \\ & \frac{4 a^3 (95 A+121 C) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{231 d} + \frac{4 a^3 (95 A+121 C) \sqrt{\cos [c+d x]} \sin [c+d x]}{231 d} + \\ & \frac{4 a^3 (175 A+221 C) \cos [c+d x]^{3 / 2} \sin [c+d x]}{585 d} + \frac{40 a^3 (118 A+143 C) \cos [c+d x]^{5 / 2} \sin [c+d x]}{9009 d} + \\ & \frac{2 A \cos [c+d x]^{5 / 2} (a+a \cos [c+d x])^3 \sin [c+d x]}{13 d} + \\ & \frac{12 A \cos [c+d x]^{5 / 2} (a^2+a^2 \cos [c+d x])^2 \sin [c+d x]}{143 a d} + \\ & \frac{2 (145 A+143 C) \cos [c+d x]^{5 / 2} (a^3+a^3 \cos [c+d x]) \sin [c+d x]}{1287 d} \end{aligned}$$

Result (type 5, 1022 leaves):

$$\begin{aligned} & a^3 \left( \sqrt{\cos [c+d x]} (1+\cos [c+d x])^3 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \right. \\ & \left( - \frac{(175 A+221 C) \cot [c]}{390 d} + \frac{(1811 A+2134 C) \cos [d x] \sin [c]}{7392 d} + \right. \\ & \frac{(7825 A+7592 C) \cos [2 d x] \sin [2 c]}{74880 d} + \frac{(215 A+132 C) \cos [3 d x] \sin [3 c]}{4928 d} + \\ & \frac{(59 A+13 C) \cos [4 d x] \sin [4 c]}{3744 d} + \frac{3 A \cos [5 d x] \sin [5 c]}{704 d} + \\ & \frac{A \cos [6 d x] \sin [6 c]}{1664 d} + \frac{(1811 A+2134 C) \cos [c] \sin [d x]}{7392 d} + \\ & \frac{(7825 A+7592 C) \cos [2 c] \sin [2 d x]}{74880 d} + \frac{(215 A+132 C) \cos [3 c] \sin [3 d x]}{4928 d} + \\ & \left. \left. \frac{(59 A+13 C) \cos [4 c] \sin [4 d x]}{3744 d} + \frac{3 A \cos [5 c] \sin [5 d x]}{704 d} + \frac{A \cos [6 c] \sin [6 d x]}{1664 d} \right) - \right. \\ & \left. \left( 95 A (1+\cos [c+d x])^3 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\cot [c]]]^2\right] \right) \right. \\ & \left. \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \sec [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\cot [c]]]} \right) \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{\sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]}}{\sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]}} \right) / \left( 462 d \sqrt{1+\cot[c]^2} \right) - \\
 & \left( 11 C (1+\cos[c+dx])^3 \text{Csc}[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\cot[c]]]^2\right] \right. \\
 & \quad \left. \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \text{Sec}[dx - \text{ArcTan}[\cot[c]]] \sqrt{1-\sin[dx - \text{ArcTan}[\cot[c]]]} \right. \\
 & \quad \left. \sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]} \sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]} \right) / \\
 & \left( 42 d \sqrt{1+\cot[c]^2} \right) - \frac{1}{156 d} 35 A (1+\cos[c+dx])^3 \text{Csc}[c] \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \\
 & \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos[dx + \text{ArcTan}[\tan[c]]]^2\right] \right. \\
 & \quad \left. \sin[dx + \text{ArcTan}[\tan[c]]] \tan[c] \right) / \\
 & \left( \sqrt{1-\cos[dx + \text{ArcTan}[\tan[c]]]} \sqrt{1+\cos[dx + \text{ArcTan}[\tan[c]]]} \right. \\
 & \quad \left. \sqrt{\cos[c] \cos[dx + \text{ArcTan}[\tan[c]]]} \sqrt{1+\tan[c]^2} \sqrt{1+\tan[c]^2} \right) - \\
 & \left( \frac{\frac{\sin[dx + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1+\tan[c]^2}} + \frac{2 \cos[c]^2 \cos[dx + \text{ArcTan}[\tan[c]]] \sqrt{1+\tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[dx + \text{ArcTan}[\tan[c]]]} \sqrt{1+\tan[c]^2}} \right) - \\
 & \frac{1}{60 d} 17 C (1+\cos[c+dx])^3 \text{Csc}[c] \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \\
 & \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos[dx + \text{ArcTan}[\tan[c]]]^2\right] \right. \\
 & \quad \left. \sin[dx + \text{ArcTan}[\tan[c]]] \tan[c] \right) /
 \end{aligned}$$



$$\left( \frac{\sqrt{1 - \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2} \sqrt{1 + \tan [c]^2}}{\frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]] \text{Tan} [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\text{Tan} [c]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2}}} \right)$$

**Problem 1099: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c + d x]^{11/2} (a + a \sec [c + d x])^3 (A + C \sec [c + d x]^2) dx$$

Optimal (type 4, 246 leaves, 10 steps):

$$\frac{4 a^3 (5 A + 7 C) \text{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{5 d} + \frac{4 a^3 (105 A + 143 C) \text{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{231 d} +$$

$$\frac{4 a^3 (105 A + 143 C) \sqrt{\cos [c + d x]} \sin [c + d x]}{231 d} + \frac{8 a^3 (35 A + 44 C) \cos [c + d x]^{3/2} \sin [c + d x]}{385 d} +$$

$$\frac{2 A \cos [c + d x]^{3/2} (a + a \cos [c + d x])^3 \sin [c + d x]}{11 d} +$$

$$\frac{4 A \cos [c + d x]^{3/2} (a^2 + a^2 \cos [c + d x])^2 \sin [c + d x]}{33 a d} +$$

$$\frac{2 (35 A + 33 C) \cos [c + d x]^{3/2} (a^3 + a^3 \cos [c + d x]) \sin [c + d x]}{231 d}$$

Result (type 5, 976 leaves):

$$a^3 \left( \sqrt{\cos [c + d x]} (1 + \cos [c + d x])^3 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \right.$$

$$\left( - \frac{(5 A + 7 C) \cot [c]}{10 d} + \frac{(1953 A + 2354 C) \cos [d x] \sin [c]}{7392 d} + \frac{(25 A + 18 C) \cos [2 d x] \sin [2 c]}{240 d} + \right.$$

$$\frac{(189 A + 44 C) \cos [3 d x] \sin [3 c]}{4928 d} + \frac{A \cos [4 d x] \sin [4 c]}{96 d} + \frac{A \cos [5 d x] \sin [5 c]}{704 d} +$$

$$\frac{(1953 A + 2354 C) \cos [c] \sin [d x]}{7392 d} + \frac{(25 A + 18 C) \cos [2 c] \sin [2 d x]}{240 d} +$$

$$\left. \frac{(189 A + 44 C) \cos [3 c] \sin [3 d x]}{4928 d} + \frac{A \cos [4 c] \sin [4 d x]}{96 d} + \frac{A \cos [5 c] \sin [5 d x]}{704 d} \right) -$$

$$\left( 5 A (1 + \cos [c + d x])^3 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2 \right. \\ \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 \operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right. \\ \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right. \\ \left. \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) / \left( 22 d \sqrt{1 + \operatorname{Cot}[c]^2} \right) -$$

$$\left( 13 C (1 + \cos [c + d x])^3 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2 \right. \\ \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 \operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right. \\ \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) /$$

$$\left( 42 d \sqrt{1 + \operatorname{Cot}[c]^2} \right) - \frac{1}{4 d} A (1 + \cos [c + d x])^3 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6$$

$$\left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]\right]^2 \right)$$

$$\operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] \Big/$$

$$\left( \sqrt{1 - \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right.$$

$$\left. \sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \operatorname{Tan}[c]^2} \sqrt{1 + \operatorname{Tan}[c]^2} \right) -$$

$$\left( \frac{\frac{\operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1 + \operatorname{Tan}[c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \operatorname{Tan}[c]^2}} \right) - \frac{1}{20 d}$$

$$7 C (1 + \cos [c + d x])^3 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \right.$$

$$\left\{ \frac{3}{4}, \cos [d x + \text{ArcTan} [\text{Tan} [c]]]^2 \sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c] \right\} /$$

$$\left( \sqrt{1 - \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \right.$$

$$\left. \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \text{Tan} [c]^2} \sqrt{1 + \text{Tan} [c]^2} \right) -$$

$$\left( \frac{\frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 + \text{Tan} [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \sqrt{1 + \text{Tan} [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \text{Tan} [c]^2}} \right)$$

**Problem 1100: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c + d x]^{9/2} (a + a \sec [c + d x])^3 (A + C \sec [c + d x]^2) dx$$

Optimal (type 4, 213 leaves, 9 steps):

$$\frac{4 a^3 (17 A + 27 C) \text{EllipticE} \left[ \frac{1}{2} (c + d x), 2 \right]}{15 d} + \frac{4 a^3 (11 A + 21 C) \text{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right]}{21 d} +$$

$$\frac{8 a^3 (16 A + 21 C) \sqrt{\cos [c + d x]} \sin [c + d x]}{105 d} + \frac{2 A \sqrt{\cos [c + d x]} (a + a \cos [c + d x])^3 \sin [c + d x]}{9 d} +$$

$$\frac{4 A \sqrt{\cos [c + d x]} (a^2 + a^2 \cos [c + d x])^2 \sin [c + d x]}{21 a d} +$$

$$\frac{2 (73 A + 63 C) \sqrt{\cos [c + d x]} (a^3 + a^3 \cos [c + d x]) \sin [c + d x]}{315 d}$$

Result (type 5, 1116 leaves):

$$\left( \cos [c + d x]^{11/2} \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 (a + a \sec [c + d x])^3 (A + C \sec [c + d x]^2) \right.$$

$$\left( - \frac{(17 A + 27 C) \cot [c]}{15 d} + \frac{(97 A + 84 C) \cos [d x] \sin [c]}{168 d} + \frac{(73 A + 18 C) \cos [2 d x] \sin [2 c]}{360 d} + \right.$$

$$\frac{3 A \cos [3 d x] \sin [3 c]}{56 d} + \frac{A \cos [4 d x] \sin [4 c]}{144 d} + \frac{(97 A + 84 C) \cos [c] \sin [d x]}{168 d} +$$

$$\left. \left. \frac{(73 A + 18 C) \cos [2 c] \sin [2 d x]}{360 d} + \frac{3 A \cos [3 c] \sin [3 d x]}{56 d} + \frac{A \cos [4 c] \sin [4 d x]}{144 d} \right) \right) /$$

$$(A + 2 C + A \cos [2 c + 2 d x]) - \frac{1}{21 d (A + 2 C + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2}}$$

$$11 A \cos [c + d x]^5 \csc [c] \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \text{ArcTan} [\cot [c]]]^2 \right]$$

$$\begin{aligned}
 & \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \text{Sec}[c + dx])^3 (A + C \text{Sec}[c + dx]^2) \\
 & \frac{\text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}}{\sqrt{-\sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] - \sqrt{1 + \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}} - 1} \\
 & d (A + 2C + A \text{Cos}[2c + 2dx]) \sqrt{1 + \text{Cot}[c]^2} \\
 & C \text{Cos}[c + dx]^5 \text{Csc}[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]^2\right] \\
 & \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \text{Sec}[c + dx])^3 (A + C \text{Sec}[c + dx]^2) \\
 & \frac{\text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}}{\sqrt{-\sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] - \sqrt{1 + \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]}} - 1} \\
 & \left( 17 A \text{Cos}[c + dx]^5 \text{Csc}[c] \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \text{Sec}[c + dx])^3 (A + C \text{Sec}[c + dx]^2) \right. \\
 & \left. \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]]^2\right] \right) \right. \\
 & \left. \left. \frac{\text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 - \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]]}} \right) \right. \\
 & \left. \frac{\sqrt{1 + \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{\text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \text{Tan}[c]^2}}{\sqrt{1 + \text{Tan}[c]^2} - \frac{\frac{\text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \frac{2 \text{Cos}[c]^2 \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}}{\text{Cos}[c]^2 + \text{Sin}[c]^2}}{\sqrt{\text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \text{Tan}[c]^2}}} \right) \left. \right) \\
 & (30 d (A + 2C + A \text{Cos}[2c + 2dx])) - \left( 9 C \text{Cos}[c + dx]^5 \text{Csc}[c] \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \right.
 \end{aligned}$$

$$\begin{aligned}
 & (a + a \operatorname{Sec}[c + d x])^3 (A + C \operatorname{Sec}[c + d x]^2) \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \right. \right. \\
 & \quad \left. \left. \left\{\frac{3}{4}\right\}, \cos[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]^2 \operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]\right] \right) / \\
 & \left( \sqrt{1 - \cos[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \cos[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right. \\
 & \quad \left. \sqrt{\cos[c] \cos[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \tan[c]^2} \sqrt{1 + \tan[c]^2} \right) - \\
 & \left. \frac{\frac{\operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \tan[c]^2}} \right) / (10 d (A + \\
 & 2 C + A \cos[2 c + 2 d x]))
 \end{aligned}$$

**Problem 1101: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c + d x]^{7/2} (a + a \operatorname{Sec}[c + d x])^3 (A + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 4, 215 leaves, 9 steps):

$$\begin{aligned}
 & \frac{4 a^3 (7 A + 5 C) \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{5 d} + \frac{4 a^3 (13 A + 35 C) \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{21 d} + \\
 & \frac{4 a^3 (41 A - 35 C) \sqrt{\cos[c + d x]} \operatorname{Sin}[c + d x]}{105 d} + \frac{2 C (a + a \cos[c + d x])^3 \operatorname{Sin}[c + d x]}{d \sqrt{\cos[c + d x]}} + \\
 & \frac{2 (A - 7 C) \sqrt{\cos[c + d x]} (a^2 + a^2 \cos[c + d x])^2 \operatorname{Sin}[c + d x]}{7 a d} + \\
 & \frac{2 (11 A - 35 C) \sqrt{\cos[c + d x]} (a^3 + a^3 \cos[c + d x]) \operatorname{Sin}[c + d x]}{35 d}
 \end{aligned}$$

Result (type 5, 1108 leaves):

$$\begin{aligned}
 & \left( \cos[c + d x]^{11/2} \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \operatorname{Sec}[c + d x])^3 (A + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \quad \left( - \frac{(14 A + 5 C + 14 A \cos[2 c] + 15 C \cos[2 c]) \operatorname{Csc}[c] \operatorname{Sec}[c]}{20 d} + \frac{(107 A + 28 C) \cos[d x] \operatorname{Sin}[c]}{168 d} + \right. \\
 & \quad \left. \frac{3 A \cos[2 d x] \operatorname{Sin}[2 c]}{20 d} + \frac{A \cos[3 d x] \operatorname{Sin}[3 c]}{56 d} + \frac{(107 A + 28 C) \cos[c] \operatorname{Sin}[d x]}{168 d} + \right.
 \end{aligned}$$

$$\left( \frac{C \operatorname{Sec}[c] \operatorname{Sec}[c+dx] \operatorname{Sin}[dx]}{2d} + \frac{3A \operatorname{Cos}[2c] \operatorname{Sin}[2dx]}{20d} + \frac{A \operatorname{Cos}[3c] \operatorname{Sin}[3dx]}{56d} \right) /$$

$$(A+2C+A \operatorname{Cos}[2c+2dx]) - \frac{1}{21d(A+2C+A \operatorname{Cos}[2c+2dx]) \sqrt{1+\operatorname{Cot}[c]^2}}$$

$$13A \operatorname{Cos}[c+dx]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right]$$

$$\operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3 (A+C \operatorname{Sec}[c+dx]^2)$$

$$\operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}$$

$$\frac{\sqrt{-\sqrt{1+\operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1+\operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} - 1}{3d(A+2C+A \operatorname{Cos}[2c+2dx]) \sqrt{1+\operatorname{Cot}[c]^2}}$$

$$5C \operatorname{Cos}[c+dx]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right]$$

$$\operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3 (A+C \operatorname{Sec}[c+dx]^2)$$

$$\operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}$$

$$\frac{\sqrt{-\sqrt{1+\operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1+\operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} - 1}{7A \operatorname{Cos}[c+dx]^5 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3 (A+C \operatorname{Sec}[c+dx]^2)}$$

$$\left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \operatorname{Cos}[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]]^2\right] \right)$$

$$\operatorname{Sin}[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] \Big/ \left( \sqrt{1 - \operatorname{Cos}[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right)$$

$$\frac{\sqrt{1+\operatorname{Cos}[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{\operatorname{Cos}[c] \operatorname{Cos}[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1+\operatorname{Tan}[c]^2}}{\sqrt{1+\operatorname{Tan}[c]^2} - \frac{\frac{\operatorname{Sin}[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1+\operatorname{Tan}[c]^2}} + \frac{2 \operatorname{Cos}[c]^2 \operatorname{Cos}[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1+\operatorname{Tan}[c]^2}}{\operatorname{Cos}[c]^2 + \operatorname{Sin}[c]^2}}{\sqrt{\operatorname{Cos}[c] \operatorname{Cos}[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1+\operatorname{Tan}[c]^2}}} \Big/$$

$$\begin{aligned}
 & (10 d (A + 2 C + A \cos [2 c + 2 d x])) - \left( C \cos [c + d x]^5 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \operatorname{Sec}[c + d x])^3 \right. \\
 & (A + C \operatorname{Sec}[c + d x]^2) \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]\right]^2 \right) \\
 & \left. \operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] \right) / \\
 & \left( \sqrt{1 - \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right. \\
 & \left. \sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \tan [c]^2} \sqrt{1 + \tan [c]^2} \right) - \\
 & \left. \frac{\frac{\operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \tan [c]^2}} \right) / (2 d (A + \\
 & 2 C + A \cos [2 c + 2 d x]))
 \end{aligned}$$

**Problem 1102: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c + d x]^{5/2} (a + a \operatorname{Sec}[c + d x])^3 (A + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 4, 211 leaves, 9 steps):

$$\begin{aligned}
 & \frac{4 a^3 (9 A - 5 C) \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{5 d} + \\
 & \frac{4 a^3 (3 A + 5 C) \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{3 d} + \frac{8 a^3 (3 A - 10 C) \sqrt{\cos [c + d x]} \operatorname{Sin}[c + d x]}{15 d} + \\
 & \frac{2 C (a + a \cos [c + d x])^3 \operatorname{Sin}[c + d x]}{3 d \cos [c + d x]^{3/2}} + \frac{4 C (a^2 + a^2 \cos [c + d x])^2 \operatorname{Sin}[c + d x]}{a d \sqrt{\cos [c + d x]}} + \\
 & \frac{2 (3 A - 35 C) \sqrt{\cos [c + d x]} (a^3 + a^3 \cos [c + d x]) \operatorname{Sin}[c + d x]}{15 d}
 \end{aligned}$$

Result (type 5, 1089 leaves):

$$\begin{aligned}
 & \left( \cos [c+d x]^{11/2} \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^3 (A+C \operatorname{Sec}[c+d x]^2) \right. \\
 & \quad \left( -\frac{(18 A-25 C+18 A \cos [2 c]+5 C \cos [2 c]) \operatorname{Csc}[c] \operatorname{Sec}[c]}{20 d}+\frac{A \cos [d x] \operatorname{Sin}[c]}{2 d} \right. \\
 & \quad \frac{A \cos [2 d x] \operatorname{Sin}[2 c]}{20 d}+\frac{A \cos [c] \operatorname{Sin}[d x]}{2 d}+\frac{C \operatorname{Sec}[c] \operatorname{Sec}[c+d x]^2 \operatorname{Sin}[d x]}{6 d} \\
 & \quad \left. \left. \frac{\operatorname{Sec}[c] \operatorname{Sec}[c+d x](C \operatorname{Sin}[c]+9 C \operatorname{Sin}[d x])}{6 d}+\frac{A \cos [2 c] \operatorname{Sin}[2 d x]}{20 d} \right) \right) / \\
 & (A+2 C+A \cos [2 c+2 d x])-\frac{1}{d(A+2 C+A \cos [2 c+2 d x]) \sqrt{1+\operatorname{Cot}[c]^2}} \\
 & A \cos [c+d x]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \\
 & \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^3 (A+C \operatorname{Sec}[c+d x]^2) \\
 & \operatorname{Sec}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1-\operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \sqrt{-\sqrt{1+\operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1+\operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} - \\
 & \frac{1}{3 d(A+2 C+A \cos [2 c+2 d x]) \sqrt{1+\operatorname{Cot}[c]^2}} \\
 & 5 C \cos [c+d x]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \\
 & \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^3 (A+C \operatorname{Sec}[c+d x]^2) \\
 & \operatorname{Sec}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1-\operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \sqrt{-\sqrt{1+\operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1+\operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} - \\
 & \left( 9 A \cos [c+d x]^5 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^3 (A+C \operatorname{Sec}[c+d x]^2) \right. \\
 & \quad \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]^2\right] \right. \\
 & \quad \left. \left. \operatorname{Sin}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] \right) \right) / \left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right. \\
 & \quad \left. \sqrt{1+\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1+\operatorname{Tan}[c]^2} \right)
 \end{aligned}$$



$$\left. \left( \sqrt{1 + \tan[c]^2} \right) - \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \right) /$$

$$(10 d (A + 2 C + A \cos[2 c + 2 d x])) + \left( C \cos[c + d x]^5 \csc[c] \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \sec[c + d x])^3 \right.$$

$$(A + C \sec[c + d x]^2) \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos[d x + \text{ArcTan}[\tan[c]]]^2\right] \right.$$

$$\left. \left. \frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 - \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \cos[d x + \text{ArcTan}[\tan[c]]]}} \right) / \right.$$

$$\left. \left. \frac{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}}{\sqrt{1 + \tan[c]^2}} \right) - \right.$$

$$\left. \left. \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \right) / (2 d (A + \right.$$

$$\left. \left. 2 C + A \cos[2 c + 2 d x] \right) \right)$$

**Problem 1103: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c + d x]^{3/2} (a + a \sec[c + d x])^3 (A + C \sec[c + d x]^2) dx$$

Optimal (type 4, 213 leaves, 9 steps):

$$\frac{4 a^3 (5 A - 9 C) \text{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{5 d} + \frac{4 a^3 (5 A + 3 C) \text{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{3 d} -$$

$$\frac{4 a^3 (5 A + 21 C) \sqrt{\cos[c + d x]} \sin[c + d x]}{15 d} + \frac{2 C (a + a \cos[c + d x])^3 \sin[c + d x]}{5 d \cos[c + d x]^{5/2}} +$$

$$\frac{4 C (a^2 + a^2 \cos[c + d x])^2 \sin[c + d x]}{5 a d \cos[c + d x]^{3/2}} + \frac{2 (5 A + 11 C) (a^3 + a^3 \cos[c + d x]) \sin[c + d x]}{5 d \sqrt{\cos[c + d x]}}$$

Result (type 5, 1085 leaves):

$$\left( \cos [c+d x]^{11 / 2} \sec \left[ \frac{c}{2}+\frac{d x}{2} \right]^6 (a+a \sec [c+d x])^3 (A+C \sec [c+d x]^2) \right. \\ \left. \left( -\frac{(5 A-36 C+15 A \cos [2 c]) \csc [c] \sec [c]}{20 d}+\frac{A \cos [d x] \sin [c]}{6 d}+\frac{A \cos [c] \sin [d x]}{6 d}+\frac{C \sec [c] \sec [c+d x]^3 \sin [d x]}{10 d}+\frac{\sec [c] \sec [c+d x]^2 (C \sin [c]+5 C \sin [d x])}{10 d}+\frac{\sec [c] \sec [c+d x] (5 C \sin [c]+5 A \sin [d x]+18 C \sin [d x])}{10 d} \right) \right) / \\ (A+2 C+A \cos [2 c+2 d x])-\frac{1}{3 d(A+2 C+A \cos [2 c+2 d x]) \sqrt{1+\cot [c]^2}} \\ 5 A \cos [c+d x]^5 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]\right]^2 \\ \sec \left[ \frac{c}{2}+\frac{d x}{2} \right]^6 (a+a \sec [c+d x])^3 (A+C \sec [c+d x]^2) \\ \sec [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \\ \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]}-1} \\ d(A+2 C+A \cos [2 c+2 d x]) \sqrt{1+\cot [c]^2} \\ C \cos [c+d x]^5 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]\right]^2 \\ \sec \left[ \frac{c}{2}+\frac{d x}{2} \right]^6 (a+a \sec [c+d x])^3 (A+C \sec [c+d x]^2) \\ \sec [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \\ \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]}-1} \\ \left( A \cos [c+d x]^5 \csc [c] \sec \left[ \frac{c}{2}+\frac{d x}{2} \right]^6 (a+a \sec [c+d x])^3 (A+C \sec [c+d x]^2) \right. \\ \left. \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\tan [c]]]\right]^2 \right. \right. \\ \left. \left. \sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c] \right) \right) / \sqrt{1-\cos [d x+\operatorname{ArcTan}[\tan [c]]]^2}$$

$$\begin{aligned}
 & \left. \left( \sqrt{1 + \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2} \right. \right. \\
 & \left. \left. \sqrt{1 + \tan [c]^2} \right) - \frac{\frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2}} \right) / \\
 & (2 d (A + 2 C + A \cos [2 c + 2 d x])) + \left( 9 C \cos [c + d x]^5 \text{Csc} [c] \text{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 (a + a \text{Sec} [c + d x])^3 \right. \\
 & \left. (A + C \text{Sec} [c + d x]^2) \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \text{ArcTan} [\text{Tan} [c]] \right]^2 \right) \right. \\
 & \left. \frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 + \tan [c]^2}} \right) / \\
 & \left( \frac{\sqrt{1 - \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \right. \\
 & \left. \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2} \sqrt{1 + \tan [c]^2} \right) - \\
 & \left. \frac{\frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2}} \right) / (10 d (A + \\
 & 2 C + A \cos [2 c + 2 d x]))
 \end{aligned}$$

**Problem 1104: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sqrt{\cos [c + d x]} (a + a \text{Sec} [c + d x])^3 (A + C \text{Sec} [c + d x]^2) dx$$

Optimal (type 4, 213 leaves, 9 steps):

$$\begin{aligned}
 & - \frac{4 a^3 (5 A+7 C) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 d} + \frac{4 a^3 (35 A+13 C) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{21 d} + \\
 & \frac{8 a^3 (70 A+53 C) \sin [c+d x]}{105 d \sqrt{\cos [c+d x]}} + \frac{2 C (a+a \cos [c+d x])^3 \sin [c+d x]}{7 d \cos [c+d x]^{7 / 2}} + \\
 & \frac{12 C (a^2+a^2 \cos [c+d x])^2 \sin [c+d x]}{35 a d \cos [c+d x]^{5 / 2}} + \frac{2 (5 A+7 C) (a^3+a^3 \cos [c+d x]) \sin [c+d x]}{15 d \cos [c+d x]^{3 / 2}}
 \end{aligned}$$

Result (type 5, 1102 leaves):

$$\begin{aligned}
 & \left( \cos [c+d x]^{11 / 2} \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^3 \right. \\
 & \quad (A+C \operatorname{Sec}[c+d x])^2 \left( -\frac{(-25 A-28 C+5 A \cos [2 c]) \operatorname{Csc}[c] \operatorname{Sec}[c]}{20 d} + \right. \\
 & \quad \quad \frac{C \operatorname{Sec}[c] \operatorname{Sec}[c+d x]^4 \sin [d x]}{14 d} + \frac{\operatorname{Sec}[c] \operatorname{Sec}[c+d x]^3 (5 C \sin [c]+21 C \sin [d x])}{70 d} + \\
 & \quad \quad \frac{1}{210 d} \operatorname{Sec}[c] \operatorname{Sec}[c+d x]^2 (63 C \sin [c]+35 A \sin [d x]+130 C \sin [d x]) + \frac{1}{210 d} \\
 & \quad \quad \left. \left. \operatorname{Sec}[c] \operatorname{Sec}[c+d x] (35 A \sin [c]+130 C \sin [c]+315 A \sin [d x]+294 C \sin [d x]) \right) \right) \right) / \\
 & (A+2 C+A \cos [2 c+2 d x]) - \frac{1}{3 d (A+2 C+A \cos [2 c+2 d x]) \sqrt{1+\operatorname{Cot}[c]^2}} \\
 & 5 A \cos [c+d x]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \\
 & \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^3 (A+C \operatorname{Sec}[c+d x])^2 \\
 & \operatorname{Sec}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \sqrt{-\sqrt{1+\operatorname{Cot}[c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1+\sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} - \\
 & \frac{1}{21 d (A+2 C+A \cos [2 c+2 d x]) \sqrt{1+\operatorname{Cot}[c]^2}} \\
 & 13 C \cos [c+d x]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \\
 & \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^3 (A+C \operatorname{Sec}[c+d x])^2 \\
 & \operatorname{Sec}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \sqrt{-\sqrt{1+\operatorname{Cot}[c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1+\sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} + \\
 & \left( A \cos [c+d x]^5 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^3 (A+C \operatorname{Sec}[c+d x])^2 \right.
 \end{aligned}$$

$$\left( \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \right]^2 \right) \right.$$

$$\left. \left. \frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 - \cos [d x + \text{ArcTan} [\text{Tan} [c]]]}} \right) \right)$$

$$\left. \left. \frac{\sqrt{1 + \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \text{Tan} [c]^2}}{\sqrt{1 + \text{Tan} [c]^2}} \right) \right)$$

$$\left. \left. \left( \frac{\frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 + \text{Tan} [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \sqrt{1 + \text{Tan} [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \text{Tan} [c]^2}} \right) \right) \right)$$

$$\left( 2 d (A + 2 C + A \cos [2 c + 2 d x]) \right) + \left( 7 C \cos [c + d x]^5 \csc [c] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 (a + a \sec [c + d x])^3 \right)$$

$$(A + C \sec [c + d x]^2) \left( \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \right]^2 \right) \right)$$

$$\left( \frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 - \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \right)$$

$$\left( \frac{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \text{Tan} [c]^2} \sqrt{1 + \text{Tan} [c]^2}}{\sqrt{1 + \text{Tan} [c]^2}} \right) -$$

$$\left( \frac{\frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 + \text{Tan} [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \sqrt{1 + \text{Tan} [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \text{Tan} [c]^2}} \right) \left( 10 d (A + \right.$$

$$\left. 2 C + A \cos [2 c + 2 d x]) \right)$$

Problem 1105: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(a + a \operatorname{Sec}[c + d x])^3 (A + C \operatorname{Sec}[c + d x]^2)}{\sqrt{\operatorname{Cos}[c + d x]}} dx$$

Optimal (type 4, 246 leaves, 10 steps):

$$\begin{aligned} & - \frac{4 a^3 (27 A + 17 C) \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{15 d} + \\ & \frac{4 a^3 (21 A + 11 C) \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{21 d} + \frac{8 a^3 (21 A + 16 C) \operatorname{Sin}[c + d x]}{105 d \operatorname{Cos}[c + d x]^{3/2}} + \\ & \frac{4 a^3 (27 A + 17 C) \operatorname{Sin}[c + d x]}{15 d \sqrt{\operatorname{Cos}[c + d x]}} + \frac{2 C (a + a \operatorname{Cos}[c + d x])^3 \operatorname{Sin}[c + d x]}{9 d \operatorname{Cos}[c + d x]^{9/2}} + \\ & \frac{4 C (a^2 + a^2 \operatorname{Cos}[c + d x])^2 \operatorname{Sin}[c + d x]}{21 a d \operatorname{Cos}[c + d x]^{7/2}} + \frac{2 (63 A + 73 C) (a^3 + a^3 \operatorname{Cos}[c + d x]) \operatorname{Sin}[c + d x]}{315 d \operatorname{Cos}[c + d x]^{5/2}} \end{aligned}$$

Result (type 5, 1135 leaves):

$$\begin{aligned} & \frac{1}{A + 2 C + A \operatorname{Cos}[2 c + 2 d x]} \operatorname{Cos}[c + d x]^{11/2} \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 \\ & \left( (a + a \operatorname{Sec}[c + d x])^3 (A + C \operatorname{Sec}[c + d x]^2) \left( \frac{(27 A + 17 C) \operatorname{Csc}[c] \operatorname{Sec}[c]}{15 d} + \right. \right. \\ & \quad \frac{C \operatorname{Sec}[c] \operatorname{Sec}[c + d x]^5 \operatorname{Sin}[d x]}{18 d} + \left. \frac{\operatorname{Sec}[c] \operatorname{Sec}[c + d x]^4 (7 C \operatorname{Sin}[c] + 27 C \operatorname{Sin}[d x])}{126 d} \right) + \\ & \quad \frac{1}{630 d} \operatorname{Sec}[c] \operatorname{Sec}[c + d x]^3 (135 C \operatorname{Sin}[c] + 63 A \operatorname{Sin}[d x] + 238 C \operatorname{Sin}[d x]) + \frac{1}{210 d} \\ & \quad \operatorname{Sec}[c] \operatorname{Sec}[c + d x] (105 A \operatorname{Sin}[c] + 110 C \operatorname{Sin}[c] + 378 A \operatorname{Sin}[d x] + 238 C \operatorname{Sin}[d x]) + \frac{1}{630 d} \\ & \quad \left. \operatorname{Sec}[c] \operatorname{Sec}[c + d x]^2 (63 A \operatorname{Sin}[c] + 238 C \operatorname{Sin}[c] + 315 A \operatorname{Sin}[d x] + 330 C \operatorname{Sin}[d x]) \right) - \\ & \frac{1}{d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2}} A \operatorname{Cos}[c + d x]^5 \operatorname{Csc}[c] \\ & \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \\ & \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \operatorname{Sec}[c + d x])^3 (A + C \operatorname{Sec}[c + d x]^2) \\ & \operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\ & \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1 + \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} - \\ & \frac{1}{21 d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2}} \\ & 11 C \operatorname{Cos}[c + d x]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \\ & \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \operatorname{Sec}[c + d x])^3 (A + C \operatorname{Sec}[c + d x]^2) \\ & \operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \end{aligned}$$

$$\begin{aligned}
 & \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]]} \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} + \\
 & \left( 9 A \cos [c+d x]^5 \csc [c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 (A+C \sec [c+d x]^2) \right. \\
 & \left. \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\tan [c]]]^2\right] \right) \right. \\
 & \left. \sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c] \right) / \left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \right. \\
 & \left. \sqrt{1+\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2} \right. \\
 & \left. \left. \sqrt{1+\tan [c]^2} \right) - \frac{\frac{\sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}{\cos [c]^2+\sin [c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2}}} \right) / \\
 & (10 d (A+2 C+A \cos [2 c+2 d x])) + \left( 17 C \cos [c+d x]^5 \csc [c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 \right. \\
 & \left. (a+a \sec [c+d x])^3 (A+C \sec [c+d x]^2) \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\}, \right. \right. \right. \\
 & \left. \left. \left. \left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\tan [c]]]^2\right] \sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c] \right) \right) / \\
 & \left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \right. \\
 & \left. \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2} \sqrt{1+\tan [c]^2} \right) -
 \end{aligned}$$

$$\left. \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}}}{\right) / (30 d (A + 2 C + A \cos[2 c + 2 d x]))$$

**Problem 1106: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \sec[c + d x])^3 (A + C \sec[c + d x]^2)}{\cos[c + d x]^{3/2}} dx$$

Optimal (type 4, 279 leaves, 11 steps):

$$\begin{aligned} & - \frac{4 a^3 (7 A + 5 C) \text{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{5 d} + \frac{4 a^3 (143 A + 105 C) \text{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{231 d} + \\ & \frac{8 a^3 (44 A + 35 C) \sin[c + d x]}{385 d \cos[c + d x]^{5/2}} + \frac{4 a^3 (143 A + 105 C) \sin[c + d x]}{231 d \cos[c + d x]^{3/2}} + \\ & \frac{4 a^3 (7 A + 5 C) \sin[c + d x]}{5 d \sqrt{\cos[c + d x]}} + \frac{2 C (a + a \cos[c + d x])^3 \sin[c + d x]}{11 d \cos[c + d x]^{11/2}} + \\ & \frac{4 C (a^2 + a^2 \cos[c + d x])^2 \sin[c + d x]}{33 a d \cos[c + d x]^{9/2}} + \frac{2 (33 A + 35 C) (a^3 + a^3 \cos[c + d x]) \sin[c + d x]}{231 d \cos[c + d x]^{7/2}} \end{aligned}$$

Result (type 5, 1179 leaves):

$$\begin{aligned} & \frac{1}{A + 2 C + A \cos[2 c + 2 d x]} \cos[c + d x]^{11/2} \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^6 \\ & (a + a \sec[c + d x])^3 (A + C \sec[c + d x]^2) \left( \frac{(7 A + 5 C) \csc[c] \sec[c]}{5 d} + \right. \\ & \frac{C \sec[c] \sec[c + d x]^6 \sin[d x]}{22 d} + \frac{\sec[c] \sec[c + d x]^5 (3 C \sin[c] + 11 C \sin[d x])}{66 d} + \\ & \frac{1}{462 d} \sec[c] \sec[c + d x]^4 (77 C \sin[c] + 33 A \sin[d x] + 126 C \sin[d x]) + \frac{1}{2310 d} \\ & \sec[c] \sec[c + d x]^3 (165 A \sin[c] + 630 C \sin[c] + 693 A \sin[d x] + 770 C \sin[d x]) + \frac{1}{2310 d} \\ & \sec[c] \sec[c + d x]^2 (693 A \sin[c] + 770 C \sin[c] + 1430 A \sin[d x] + 1050 C \sin[d x]) + \\ & \left. \frac{1}{1155 d} \sec[c] \sec[c + d x] (715 A \sin[c] + 525 C \sin[c] + 1617 A \sin[d x] + 1155 C \sin[d x]) \right) - \\ & \frac{1}{21 d (A + 2 C + A \cos[2 c + 2 d x]) \sqrt{1 + \cot[c]^2}} 13 A \cos[c + d x]^5 \csc[c] \\ & \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[d x - \text{ArcTan}[\cot[c]]]^2\right] \\ & \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \sec[c + d x])^3 (A + C \sec[c + d x]^2) \end{aligned}$$



$$\begin{aligned}
 & \frac{\sec [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\cot [c]]]} \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\cot [c]]]} \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\cot [c]]]} - 1}{11 d (A + 2 C + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2}} \\
 & 5 C \cos [c + d x]^5 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\cot [c]]]^2\right] \\
 & \sec \left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \sec [c + d x])^3 (A + C \sec [c + d x]^2) \\
 & \frac{\sec [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\cot [c]]]} \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\cot [c]]]} \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\cot [c]]]} + 7 A \cos [c + d x]^5 \csc [c] \sec \left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \sec [c + d x])^3 (A + C \sec [c + d x]^2)}{\left(\operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos [d x + \operatorname{ArcTan}[\tan [c]]]^2\right]\right) \left(\sin [d x + \operatorname{ArcTan}[\tan [c]]] \tan [c]\right) / \left(\sqrt{1 - \cos [d x + \operatorname{ArcTan}[\tan [c]]]}\right)} \\
 & \left. \frac{\sqrt{1 + \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \sqrt{1 + \tan [c]^2}}{\sqrt{1 + \tan [c]^2}} - \frac{\frac{\sin [d x + \operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \sqrt{1 + \tan [c]^2}} \right) / \\
 & (10 d (A + 2 C + A \cos [2 c + 2 d x])) + \left( C \cos [c + d x]^5 \csc [c] \sec \left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \sec [c + d x])^3 \right. \\
 & \left. (A + C \sec [c + d x]^2) \left(\operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos [d x + \operatorname{ArcTan}[\tan [c]]]^2\right]\right) \right)
 \end{aligned}$$

$$\left( \frac{\sin [d x + \operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1 - \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \sqrt{1 + \cos [d x + \operatorname{ArcTan}[\tan [c]]]}} - \frac{\sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \sqrt{1 + \tan [c]^2} \sqrt{1 + \tan [c]^2}}{\sqrt{1 + \tan [c]^2}} - \frac{\frac{\sin [d x + \operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \sqrt{1 + \tan [c]^2}} \right) / (2 d (A + 2 C + A \cos [2 c + 2 d x]))$$

**Problem 1107: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\cos [c + d x]^{7/2} (A + C \sec [c + d x]^2)}{a + a \sec [c + d x]} dx$$

Optimal (type 4, 192 leaves, 8 steps):

$$\begin{aligned} & - \frac{3 (7 A + 5 C) \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), 2\right]}{5 a d} + \frac{5 (9 A + 7 C) \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), 2\right]}{21 a d} + \\ & \frac{5 (9 A + 7 C) \sqrt{\cos [c + d x]} \sin [c + d x]}{21 a d} - \frac{(7 A + 5 C) \cos [c + d x]^{3/2} \sin [c + d x]}{5 a d} + \\ & \frac{(9 A + 7 C) \cos [c + d x]^{5/2} \sin [c + d x]}{7 a d} - \frac{(A + C) \cos [c + d x]^{7/2} \sin [c + d x]}{d (a + a \cos [c + d x])} \end{aligned}$$

Result (type 5, 1393 leaves):

$$\begin{aligned} & - \frac{1}{10 (A + 2 C + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])} \\ & 21 i A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \cos [c + d x] \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} \right] (A + C \sec [c + d x]^2) \\ & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \right. \\ & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\ & \quad (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) - \\ & \quad \left. \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \right. \\ & \quad \left. \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) \right) \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{1 + e^{2ix} \cos[2c] + i e^{2ix} \sin[2c]} \right) / \\
 & \left( -i d (1 + e^{2ix}) \cos[c] + d (-1 + e^{2ix}) \sin[c] \right) - \\
 & \frac{1}{2 (A + 2C + A \cos[2c + 2dx]) (a + a \sec[c + dx])} \\
 & 3 \\
 & i \\
 & C \\
 & \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \\
 & \cos[c + dx] \\
 & \csc\left[\frac{c}{2}\right] \\
 & \sec\left[\frac{c}{2}\right] \\
 & (A + C \sec[c + dx]^2) \\
 & \left( \left( 2 e^{2ix} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix} (\cos[c] + i \sin[c])^2\right] \right. \right. \\
 & \quad \left. \left. \frac{\sqrt{e^{-ix} (2 (1 + e^{2ix}) \cos[c] + 2i (-1 + e^{2ix}) \sin[c])}}{\sqrt{1 + e^{2ix} \cos[2c] + i e^{2ix} \sin[2c]}} \right) / \right. \\
 & \quad \left. (3 i d (1 + e^{2ix}) \cos[c] - 3 d (-1 + e^{2ix}) \sin[c]) - \right. \\
 & \quad \left. \left( 2 \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix} (\cos[c] + i \sin[c])^2\right] \right. \right. \\
 & \quad \left. \left. \frac{\sqrt{e^{-ix} (2 (1 + e^{2ix}) \cos[c] + 2i (-1 + e^{2ix}) \sin[c])}}{\sqrt{1 + e^{2ix} \cos[2c] + i e^{2ix} \sin[2c]}} \right) / \right. \\
 & \quad \left. \left. (-i d (1 + e^{2ix}) \cos[c] + d (-1 + e^{2ix}) \sin[c]) \right) \right) + \\
 & \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c + dx]^{3/2} (A + C \sec[c + dx]^2) \right. \\
 & \quad \left( \frac{4 (5A + 5C + 16A \cos[c] + 10C \cos[c]) \csc[c]}{5d} + \right. \\
 & \quad \frac{2 (51A + 28C) \cos[dx] \sin[c]}{21d} - \frac{4A \cos[2dx] \sin[2c]}{5d} + \\
 & \quad \frac{2A \cos[3dx] \sin[3c]}{7d} + \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right] (A \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{d} + \\
 & \quad \left. \left. \frac{2 (51A + 28C) \cos[c] \sin[dx]}{21d} - \frac{4A \cos[2c] \sin[2dx]}{5d} + \frac{2A \cos[3c] \sin[3dx]}{7d} \right) \right) / \\
 & ((A + 2C + A \cos[2c + 2dx]) (a + a \sec[c + dx])) -
 \end{aligned}$$

$$\left( \begin{aligned} &30 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c + dx] \operatorname{Csc}\left[\frac{c}{2}\right] \\ &\operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \\ &\operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c + dx]^2) \operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \\ &\sqrt{1 - \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\ &\sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\ &\sqrt{1 + \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \end{aligned} \right) /$$

$$\left( 7 d (A + 2 C + A \cos[2c + 2dx]) \sqrt{1 + \operatorname{Cot}[c]^2} (a + a \operatorname{Sec}[c + dx]) \right) -$$

$$\left( \begin{aligned} &10 C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c + dx] \operatorname{Csc}\left[\frac{c}{2}\right] \\ &\operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \operatorname{Sec}\left[\frac{c}{2}\right] \\ &(A + C \operatorname{Sec}[c + dx]^2) \operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\ &\sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1 + \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \end{aligned} \right) /$$

$$\left( 3 d (A + 2 C + A \cos[2c + 2dx]) \sqrt{1 + \operatorname{Cot}[c]^2} (a + a \operatorname{Sec}[c + dx]) \right)$$

**Problem 1108: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c + dx]^{5/2} (A + C \operatorname{Sec}[c + dx]^2)}{a + a \operatorname{Sec}[c + dx]} dx$$

Optimal (type 4, 159 leaves, 7 steps):

$$\frac{3 (7 A + 5 C) \operatorname{EllipticE}\left[\frac{1}{2} (c + dx), 2\right]}{5 a d} - \frac{(5 A + 3 C) \operatorname{EllipticF}\left[\frac{1}{2} (c + dx), 2\right]}{3 a d} - \frac{(5 A + 3 C) \sqrt{\cos[c + dx]} \sin[c + dx]}{3 a d} + \frac{(7 A + 5 C) \cos[c + dx]^{3/2} \sin[c + dx]}{5 a d} - \frac{(A + C) \cos[c + dx]^{5/2} \sin[c + dx]}{d (a + a \cos[c + dx])}$$

Result (type 5, 1345 leaves):

$$\frac{1}{10 (A + 2 C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])} {}_{21}F_1 \left[ A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c + dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \right]$$

$$\begin{aligned}
 & (A + C \operatorname{Sec}[c + d x]^2) \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])\right]^2 \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])}}{\sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]}} \right) / \\
 & \quad (3 i d (1 + e^{2 i d x}) \cos[c] - 3 d (-1 + e^{2 i d x}) \sin[c]) - \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])\right]^2 \right) \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])}}{\sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2 i d x}) \cos[c] + d (-1 + e^{2 i d x}) \sin[c]) \right) + \\
 & \frac{1}{2 (A + 2 C + A \cos[2 c + 2 d x]) (a + a \operatorname{Sec}[c + d x])} \\
 & 3 \\
 & i \\
 & C \\
 & \cos\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \\
 & \cos[c + d x] \\
 & \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \\
 & (A + C \operatorname{Sec}[c + d x]^2) \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])\right]^2 \right) \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])}}{\sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]}} \right) / \\
 & \quad (3 i d (1 + e^{2 i d x}) \cos[c] - 3 d (-1 + e^{2 i d x}) \sin[c]) - \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])\right]^2 \right) \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])}}{\sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2 i d x}) \cos[c] + d (-1 + e^{2 i d x}) \sin[c]) \right) + \\
 & \left( \cos\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \cos[c + d x]^{3/2} (A + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \quad \left( -\frac{4 (5 A + 5 C + 16 A \cos[c] + 10 C \cos[c]) \operatorname{Csc}[c]}{5 d} - \frac{8 A \cos[d x] \sin[c]}{3 d} + \right. \\
 & \quad \left. \frac{4 A \cos[2 d x] \sin[2 c]}{5 d} - \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right] (A \sin\left[\frac{d x}{2}\right] + C \sin\left[\frac{d x}{2}\right])}{d} \right)
 \end{aligned}$$

$$\left. \left( \frac{8 A \cos [c] \sin [d x]}{3 d} + \frac{4 A \cos [2 c] \sin [2 d x]}{5 d} \right) \right) /$$

$$\left( (A + 2 C + A \cos [2 c + 2 d x]) (a + a \sec [c + d x]) \right) +$$

$$\left( 10 A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \cos [c + d x] \operatorname{Csc} \left[ \frac{c}{2} \right] \right.$$

$$\operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]^2 \right]$$

$$\operatorname{Sec} \left[ \frac{c}{2} \right] (A + C \sec [c + d x]^2) \operatorname{Sec} [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]$$

$$\sqrt{1 - \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]}$$

$$\sqrt{-\sqrt{1 + \operatorname{Cot} [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]}$$

$$\left. \sqrt{1 + \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \right) /$$

$$\left( 3 d (A + 2 C + A \cos [2 c + 2 d x]) \sqrt{1 + \operatorname{Cot} [c]^2} (a + a \sec [c + d x]) \right) +$$

$$\left( 2 C \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \cos [c + d x] \operatorname{Csc} \left[ \frac{c}{2} \right] \right.$$

$$\operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]^2 \right] \operatorname{Sec} \left[ \frac{c}{2} \right]$$

$$(A + C \sec [c + d x]^2) \operatorname{Sec} [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]}$$

$$\left. \sqrt{-\sqrt{1 + \operatorname{Cot} [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \sqrt{1 + \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \right) /$$

$$\left( d (A + 2 C + A \cos [2 c + 2 d x]) \sqrt{1 + \operatorname{Cot} [c]^2} (a + a \sec [c + d x]) \right)$$

**Problem 1109: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\cos [c + d x]^{3/2} (A + C \sec [c + d x]^2)}{a + a \sec [c + d x]} dx$$

Optimal (type 4, 122 leaves, 6 steps):

$$- \frac{(3 A + C) \operatorname{EllipticE} \left[ \frac{1}{2} (c + d x), 2 \right]}{a d} + \frac{(5 A + 3 C) \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right]}{3 a d} +$$

$$\frac{(5 A + 3 C) \sqrt{\cos [c + d x]} \sin [c + d x]}{3 a d} - \frac{(A + C) \cos [c + d x]^{3/2} \sin [c + d x]}{d (a + a \cos [c + d x])}$$

Result (type 5, 1300 leaves):

$$\begin{aligned}
 & - \frac{1}{2 (A + 2 C + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])} 3 i i A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \cos [c + d x] \csc \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} \right] \\
 & (A + C \sec [c + d x]^2) \left( \left( 2 e^{2 i d x} \text{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \right. \\
 & \quad \left. \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) \right) / \\
 & (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) - \\
 & \left( 2 \text{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) \right) / \\
 & \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) - \\
 & \frac{1}{2 (A + 2 C + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])} \\
 & i \\
 & C \\
 & \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \\
 & \cos [c + d x] \\
 & \csc \left[ \frac{c}{2} \right] \\
 & \sec \left[ \frac{c}{2} \right] \\
 & (A + C \sec [c + d x]^2) \\
 & \left( \left( 2 e^{2 i d x} \text{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \right. \\
 & \quad \left. \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) \right) / \\
 & (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) - \\
 & \left( 2 \text{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) \right) / \\
 & \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) + \\
 & \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \cos [c + d x]^{3/2} (A + C \sec [c + d x]^2) \right. \\
 & \quad \left. \left( \frac{4 (A + C + 2 A \cos [c]) \csc [c]}{d} + \frac{8 A \cos [d x] \sin [c]}{3 d} \right) + \right.
 \end{aligned}$$

$$\left( \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] \left(A \operatorname{Sin}\left[\frac{dx}{2}\right] + C \operatorname{Sin}\left[\frac{dx}{2}\right]\right)}{d} + \frac{8 A \operatorname{Cos}[c] \operatorname{Sin}[dx]}{3 d} \right) /$$

$$\left( (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) (a + a \operatorname{Sec}[c + d x]) \right) -$$

$$\left( 10 A \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Cos}[c + d x] \operatorname{Csc}\left[\frac{c}{2}\right] \right.$$

$$\operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right]$$

$$\operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c + d x]^2) \operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]$$

$$\sqrt{1 - \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}$$

$$\sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}$$

$$\left. \sqrt{1 + \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) /$$

$$\left( 3 d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2} (a + a \operatorname{Sec}[c + d x]) \right) -$$

$$\left( 2 C \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Cos}[c + d x] \operatorname{Csc}\left[\frac{c}{2}\right] \right.$$

$$\operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \operatorname{Sec}\left[\frac{c}{2}\right]$$

$$(A + C \operatorname{Sec}[c + d x]^2) \operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}$$

$$\sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}$$

$$\left. \sqrt{1 + \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) /$$

$$\left( d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2} (a + a \operatorname{Sec}[c + d x]) \right)$$

**Problem 1110: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\operatorname{Cos}[c + d x]} (A + C \operatorname{Sec}[c + d x]^2)}{a + a \operatorname{Sec}[c + d x]} dx$$

Optimal (type 4, 84 leaves, 5 steps):



$$\frac{(3A+C) \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{ad} - \frac{(A-C) \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{ad} - \frac{(A+C) \sqrt{\cos[c+dx]} \sin[c+dx]}{d(a+a \cos[c+dx])}$$

Result (type 5, 1270 leaves):

$$\frac{1}{2(A+2C+A \cos[2c+2dx]) (a+a \sec[c+dx])} \left( 3i A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c+dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \right. \\ \left. (A+C \sec[c+dx]^2) \left( \left( 2 e^{2i dx} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2i dx} (\cos[c] + i \sin[c])^2\right] \right. \right. \right. \\ \left. \left. \sqrt{e^{-i dx} (2(1+e^{2i dx}) \cos[c] + 2i(-1+e^{2i dx}) \sin[c])} \right. \right. \\ \left. \left. \sqrt{1+e^{2i dx} \cos[2c] + i e^{2i dx} \sin[2c]} \right) \right) / \\ \left( 3i d (1+e^{2i dx}) \cos[c] - 3d (-1+e^{2i dx}) \sin[c] \right) - \\ \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i dx} (\cos[c] + i \sin[c])^2\right] \right. \\ \left. \sqrt{e^{-i dx} (2(1+e^{2i dx}) \cos[c] + 2i(-1+e^{2i dx}) \sin[c])} \right. \\ \left. \sqrt{1+e^{2i dx} \cos[2c] + i e^{2i dx} \sin[2c]} \right) / \\ \left. \left( -i d (1+e^{2i dx}) \cos[c] + d (-1+e^{2i dx}) \sin[c] \right) \right) + \\ \frac{1}{2(A+2C+A \cos[2c+2dx]) (a+a \sec[c+dx])} \\ i \\ C \\ \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \\ \cos[c+dx] \\ \operatorname{Csc}\left[\frac{c}{2}\right] \\ \operatorname{Sec}\left[\frac{c}{2}\right] \\ (A+C \sec[c+dx]^2) \\ \left( \left( 2 e^{2i dx} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2i dx} (\cos[c] + i \sin[c])^2\right] \right. \right. \\ \left. \left. \sqrt{e^{-i dx} (2(1+e^{2i dx}) \cos[c] + 2i(-1+e^{2i dx}) \sin[c])} \right. \right. \\ \left. \left. \sqrt{1+e^{2i dx} \cos[2c] + i e^{2i dx} \sin[2c]} \right) \right) / \\ \left( 3i d (1+e^{2i dx}) \cos[c] - 3d (-1+e^{2i dx}) \sin[c] \right) - \\ \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i dx} (\cos[c] + i \sin[c])^2\right] \right. \\ \left. \sqrt{e^{-i dx} (2(1+e^{2i dx}) \cos[c] + 2i(-1+e^{2i dx}) \sin[c])} \right. \\ \left. \sqrt{1+e^{2i dx} \cos[2c] + i e^{2i dx} \sin[2c]} \right) /$$

$$\begin{aligned}
 & \left( -i d (1 + e^{2 i d x}) \operatorname{Cos}[c] + d (-1 + e^{2 i d x}) \operatorname{Sin}[c] \right) + \\
 & \left( \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \operatorname{Cos}[c + d x]^{3/2} (A + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \left. \left( -\frac{4 (A + C + 2 A \operatorname{Cos}[c]) \operatorname{Csc}[c]}{d} - \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right] (A \operatorname{Sin}\left[\frac{d x}{2}\right] + C \operatorname{Sin}\left[\frac{d x}{2}\right])}{d} \right) \right) / \\
 & \left( (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) (a + a \operatorname{Sec}[c + d x]) \right) + \\
 & \left( 2 A \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \operatorname{Cos}[c + d x] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \operatorname{Sec}\left[\frac{c}{2}\right] \right. \\
 & \left. (A + C \operatorname{Sec}[c + d x]^2) \operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right. \\
 & \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right. \\
 & \left. \sqrt{1 + \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) / \\
 & \left( d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2} (a + a \operatorname{Sec}[c + d x]) \right) - \\
 & \left( 2 C \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \operatorname{Cos}[c + d x] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \operatorname{Sec}\left[\frac{c}{2}\right] \right. \\
 & \left. (A + C \operatorname{Sec}[c + d x]^2) \operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right. \\
 & \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1 + \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) / \\
 & \left( d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2} (a + a \operatorname{Sec}[c + d x]) \right)
 \end{aligned}$$

**Problem 1111: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + C \operatorname{Sec}[c + d x]^2}{\sqrt{\operatorname{Cos}[c + d x]} (a + a \operatorname{Sec}[c + d x])} dx$$

Optimal (type 4, 112 leaves, 6 steps):

$$\begin{aligned}
 & - \frac{(A+3C) \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{ad} + \frac{(A-C) \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{ad} + \\
 & \frac{(A+3C) \operatorname{Sin}[c+dx]}{ad \sqrt{\operatorname{Cos}[c+dx]}} - \frac{(A+C) \operatorname{Sin}[c+dx]}{d \sqrt{\operatorname{Cos}[c+dx]} (a+a \operatorname{Cos}[c+dx])}
 \end{aligned}$$

Result (type 5, 1304 leaves):

$$\begin{aligned}
 & - \frac{1}{2(A+2C+A \operatorname{Cos}[2c+2dx]) (a+a \operatorname{Sec}[c+dx])} i A \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Cos}[c+dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \\
 & (A+C \operatorname{Sec}[c+dx]^2) \left( \left( 2 e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right. \right. \\
 & \quad \left. \left. \frac{\sqrt{e^{-ix} (2(1+e^{2ix}) \operatorname{Cos}[c] + 2i(-1+e^{2ix}) \operatorname{Sin}[c])}}{\sqrt{1+e^{2ix} \operatorname{Cos}[2c] + i e^{2ix} \operatorname{Sin}[2c]}} \right) / \right. \\
 & \quad \left. (3id(1+e^{2ix}) \operatorname{Cos}[c] - 3d(-1+e^{2ix}) \operatorname{Sin}[c]) - \right. \\
 & \quad \left. \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right) \right. \\
 & \quad \left. \frac{\sqrt{e^{-ix} (2(1+e^{2ix}) \operatorname{Cos}[c] + 2i(-1+e^{2ix}) \operatorname{Sin}[c])}}{\sqrt{1+e^{2ix} \operatorname{Cos}[2c] + i e^{2ix} \operatorname{Sin}[2c]}} \right) / \right. \\
 & \quad \left. (-id(1+e^{2ix}) \operatorname{Cos}[c] + d(-1+e^{2ix}) \operatorname{Sin}[c]) \right) - \\
 & \frac{1}{2(A+2C+A \operatorname{Cos}[2c+2dx]) (a+a \operatorname{Sec}[c+dx])} \\
 & 3 \\
 & i \\
 & C \\
 & \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \\
 & \operatorname{Cos}[c+dx] \\
 & \operatorname{Csc}\left[\frac{c}{2}\right] \\
 & \operatorname{Sec}\left[\frac{c}{2}\right] \\
 & (A+C \operatorname{Sec}[c+dx]^2) \\
 & \left( \left( 2 e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right) \right. \\
 & \quad \left. \frac{\sqrt{e^{-ix} (2(1+e^{2ix}) \operatorname{Cos}[c] + 2i(-1+e^{2ix}) \operatorname{Sin}[c])}}{\sqrt{1+e^{2ix} \operatorname{Cos}[2c] + i e^{2ix} \operatorname{Sin}[2c]}} \right) / \right. \\
 & \quad \left. (3id(1+e^{2ix}) \operatorname{Cos}[c] - 3d(-1+e^{2ix}) \operatorname{Sin}[c]) - \right. \\
 & \quad \left. \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right) \right. \\
 & \quad \left. \frac{\sqrt{e^{-ix} (2(1+e^{2ix}) \operatorname{Cos}[c] + 2i(-1+e^{2ix}) \operatorname{Sin}[c])}}{\sqrt{1+e^{2ix} \operatorname{Cos}[2c] + i e^{2ix} \operatorname{Sin}[2c]}} \right) / \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( -i d (1 + e^{2 i d x}) \operatorname{Cos}[c] + d (-1 + e^{2 i d x}) \operatorname{Sin}[c] \right) + \\
 & \left( \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \operatorname{Cos}[c + d x]^{3/2} (A + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \left( \frac{2 (2 C + A \operatorname{Cos}[c] + C \operatorname{Cos}[c]) \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c]}{d} + \right. \\
 & \left. \left. \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right] (A \operatorname{Sin}\left[\frac{d x}{2}\right] + C \operatorname{Sin}\left[\frac{d x}{2}\right])}{d} + \frac{8 C \operatorname{Sec}[c] \operatorname{Sec}[c + d x] \operatorname{Sin}[d x]}{d} \right) \right) / \\
 & \left( (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) (a + a \operatorname{Sec}[c + d x]) \right) - \\
 & \left( 2 A \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \operatorname{Cos}[c + d x] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \\
 & \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c + d x]^2) \operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \\
 & \sqrt{1 - \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \left. \sqrt{1 + \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) / \\
 & \left( d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2} (a + a \operatorname{Sec}[c + d x]) \right) + \\
 & \left( 2 C \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \operatorname{Cos}[c + d x] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \operatorname{Sec}\left[\frac{c}{2}\right] \\
 & (A + C \operatorname{Sec}[c + d x]^2) \operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1 + \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) / \\
 & \left( d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2} (a + a \operatorname{Sec}[c + d x]) \right)
 \end{aligned}$$

**Problem 1112: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + C \operatorname{Sec}[c + d x]^2}{\operatorname{Cos}[c + d x]^{3/2} (a + a \operatorname{Sec}[c + d x])} dx$$

Optimal (type 4, 150 leaves, 7 steps):

$$\frac{(A+3C) \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{ad} + \frac{(3A+5C) \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{3ad} +$$

$$\frac{(3A+5C) \operatorname{Sin}[c+dx]}{3ad \operatorname{Cos}[c+dx]^{3/2}} - \frac{(A+3C) \operatorname{Sin}[c+dx]}{ad \sqrt{\operatorname{Cos}[c+dx]}} - \frac{(A+C) \operatorname{Sin}[c+dx]}{d \operatorname{Cos}[c+dx]^{3/2} (a+a \operatorname{Cos}[c+dx])}$$

Result (type 5, 1337 leaves):

$$\frac{1}{2(A+2C+A \operatorname{Cos}[2c+2dx]) (a+a \operatorname{Sec}[c+dx])} i A \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Cos}[c+dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right]$$

$$(A+C \operatorname{Sec}[c+dx]^2) \left( \left( 2 e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right. \right.$$

$$\left. \frac{\sqrt{e^{-ix} (2(1+e^{2ix}) \operatorname{Cos}[c] + 2i(-1+e^{2ix}) \operatorname{Sin}[c])}}{\sqrt{1+e^{2ix} \operatorname{Cos}[2c] + i e^{2ix} \operatorname{Sin}[2c]}} \right) /$$

$$(3id(1+e^{2ix}) \operatorname{Cos}[c] - 3d(-1+e^{2ix}) \operatorname{Sin}[c]) -$$

$$\left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right.$$

$$\left. \frac{\sqrt{e^{-ix} (2(1+e^{2ix}) \operatorname{Cos}[c] + 2i(-1+e^{2ix}) \operatorname{Sin}[c])}}{\sqrt{1+e^{2ix} \operatorname{Cos}[2c] + i e^{2ix} \operatorname{Sin}[2c]}} \right) /$$

$$\left. (-id(1+e^{2ix}) \operatorname{Cos}[c] + d(-1+e^{2ix}) \operatorname{Sin}[c]) \right) +$$

$$\frac{1}{2(A+2C+A \operatorname{Cos}[2c+2dx]) (a+a \operatorname{Sec}[c+dx])}$$

$$3$$

$$i$$

$$C$$

$$\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^2$$

$$\operatorname{Cos}[c+dx]$$

$$\operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right]$$

$$(A+C \operatorname{Sec}[c+dx]^2)$$

$$\left( \left( 2 e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right. \right.$$

$$\left. \frac{\sqrt{e^{-ix} (2(1+e^{2ix}) \operatorname{Cos}[c] + 2i(-1+e^{2ix}) \operatorname{Sin}[c])}}{\sqrt{1+e^{2ix} \operatorname{Cos}[2c] + i e^{2ix} \operatorname{Sin}[2c]}} \right) /$$

$$(3id(1+e^{2ix}) \operatorname{Cos}[c] - 3d(-1+e^{2ix}) \operatorname{Sin}[c]) -$$

$$\left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right.$$

$$\left. \frac{\sqrt{e^{-ix} (2(1+e^{2ix}) \operatorname{Cos}[c] + 2i(-1+e^{2ix}) \operatorname{Sin}[c])}}{\sqrt{1+e^{2ix} \operatorname{Cos}[2c] + i e^{2ix} \operatorname{Sin}[2c]}} \right) /$$

$$\begin{aligned}
 & \left( -i d (1 + e^{2 i d x}) \operatorname{Cos}[c] + d (-1 + e^{2 i d x}) \operatorname{Sin}[c] \right) + \\
 & \left( \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \operatorname{Cos}[c + d x]^{3/2} (A + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \left( -\frac{2 (2 C + A \operatorname{Cos}[c] + C \operatorname{Cos}[c]) \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c]}{d} - \right. \\
 & \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right] (A \operatorname{Sin}\left[\frac{d x}{2}\right] + C \operatorname{Sin}\left[\frac{d x}{2}\right])}{d} + \frac{8 C \operatorname{Sec}[c] \operatorname{Sec}[c + d x]^2 \operatorname{Sin}[d x]}{3 d} + \\
 & \left. \left. \frac{8 \operatorname{Sec}[c] \operatorname{Sec}[c + d x] (C \operatorname{Sin}[c] - 3 C \operatorname{Sin}[d x])}{3 d} \right) \right) / \\
 & \left( (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) (a + a \operatorname{Sec}[c + d x]) \right) - \\
 & \left( 2 A \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \operatorname{Cos}[c + d x] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \\
 & \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c + d x]^2) \operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \\
 & \frac{\sqrt{1 - \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}}{\sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \\
 & \left. \frac{\sqrt{1 + \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}}{\sqrt{1 + \operatorname{Cot}[c]^2}} \right) / \\
 & \left( d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2} (a + a \operatorname{Sec}[c + d x]) \right) - \\
 & \left( 10 C \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \operatorname{Cos}[c + d x] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \operatorname{Sec}\left[\frac{c}{2}\right] \\
 & (A + C \operatorname{Sec}[c + d x]^2) \operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \left. \frac{\sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1 + \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}}{\sqrt{1 + \operatorname{Cot}[c]^2}} \right) / \\
 & \left( 3 d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2} (a + a \operatorname{Sec}[c + d x]) \right)
 \end{aligned}$$

**Problem 1113:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{A + C \operatorname{Sec}[c + d x]^2}{\operatorname{Cos}[c + d x]^{5/2} (a + a \operatorname{Sec}[c + d x])} dx$$

Optimal (type 4, 192 leaves, 8 steps):

$$\frac{3 (5 A + 7 C) \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), 2\right]}{5 a d} - \frac{(3 A + 5 C) \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), 2\right]}{3 a d} + \frac{(5 A + 7 C) \operatorname{Sin}[c + d x]}{5 a d \operatorname{Cos}[c + d x]^{5/2}} - \frac{(3 A + 5 C) \operatorname{Sin}[c + d x]}{3 a d \operatorname{Cos}[c + d x]^{3/2}} + \frac{3 (5 A + 7 C) \operatorname{Sin}[c + d x]}{5 a d \sqrt{\operatorname{Cos}[c + d x]}} - \frac{(A + C) \operatorname{Sin}[c + d x]}{d \operatorname{Cos}[c + d x]^{5/2} (a + a \operatorname{Cos}[c + d x])}$$

Result (type 5, 1382 leaves):

$$\frac{1}{2 (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) (a + a \operatorname{Sec}[c + d x])} \frac{3 i A \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \operatorname{Cos}[c + d x] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c + d x]^2) \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])} \sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]} \right) / \left( 3 i d (1 + e^{2 i d x}) \operatorname{Cos}[c] - 3 d (-1 + e^{2 i d x}) \operatorname{Sin}[c] \right) - \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])} \sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]} \right) / \left( -i d (1 + e^{2 i d x}) \operatorname{Cos}[c] + d (-1 + e^{2 i d x}) \operatorname{Sin}[c] \right) \right) - 1}{10 (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) (a + a \operatorname{Sec}[c + d x])} \frac{21 i C \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \operatorname{Cos}[c + d x] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c + d x]^2) \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])} \sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]} \right) / \right.$$

$$\begin{aligned}
 & \left( 3 i d (1 + e^{2 i d x}) \operatorname{Cos}[c] - 3 d (-1 + e^{2 i d x}) \operatorname{Sin}[c] \right) - \\
 & \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]}} \right) / \\
 & \left. (-i d (1 + e^{2 i d x}) \operatorname{Cos}[c] + d (-1 + e^{2 i d x}) \operatorname{Sin}[c]) \right) + \\
 & \left( \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \operatorname{Cos}[c + d x]^{3/2} (A + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \quad \left( \frac{2 (10 A + 16 C + 5 A \operatorname{Cos}[c] + 5 C \operatorname{Cos}[c]) \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c]}{5 d} + \right. \\
 & \quad \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right] (A \operatorname{Sin}\left[\frac{d x}{2}\right] + C \operatorname{Sin}\left[\frac{d x}{2}\right])}{d} + \frac{8 C \operatorname{Sec}[c] \operatorname{Sec}[c + d x]^3 \operatorname{Sin}[d x]}{5 d} - \\
 & \quad \left. \frac{1}{15 d} 8 \operatorname{Sec}[c] \operatorname{Sec}[c + d x] (5 C \operatorname{Sin}[c] - 15 A \operatorname{Sin}[d x] - 24 C \operatorname{Sin}[d x]) + \right. \\
 & \quad \left. \left. \frac{8 \operatorname{Sec}[c] \operatorname{Sec}[c + d x]^2 (3 C \operatorname{Sin}[c] - 5 C \operatorname{Sin}[d x])}{15 d} \right) \right) / \\
 & \left( (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) (a + a \operatorname{Sec}[c + d x]) \right) + \\
 & \left( 2 A \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \operatorname{Cos}[c + d x] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \\
 & \quad \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c + d x]^2) \operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \\
 & \quad \frac{\sqrt{1 - \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}}{\sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \\
 & \quad \left. \frac{\sqrt{1 + \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}}{\sqrt{1 + \operatorname{Cot}[c]^2}} \right) / \\
 & \left( d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2} (a + a \operatorname{Sec}[c + d x]) \right) + \\
 & \left( 10 C \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \operatorname{Cos}[c + d x] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \operatorname{Sec}\left[\frac{c}{2}\right] \\
 & \quad \left. (A + C \operatorname{Sec}[c + d x]^2) \operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right)
 \end{aligned}$$



$$\frac{\sqrt{-\sqrt{1+\cot^2[c]} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]} \sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]}}{\left(3d(A+2C+A \cos[2c+2dx]) \sqrt{1+\cot^2[c]} (a+a \sec[c+dx])\right)}$$

**Problem 1114: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c+dx]^{5/2} (A+C \sec[c+dx]^2)}{(a+a \sec[c+dx])^2} dx$$

Optimal (type 4, 196 leaves, 8 steps):

$$\frac{4(14A+5C) \text{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{5a^2d} - \frac{5(3A+C) \text{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{3a^2d} - \frac{5(3A+C) \sqrt{\cos[c+dx]} \sin[c+dx]}{3a^2d} + \frac{4(14A+5C) \cos[c+dx]^{3/2} \sin[c+dx]}{15a^2d} - \frac{(3A+C) \cos[c+dx]^{5/2} \sin[c+dx]}{a^2d(1+\cos[c+dx])} - \frac{(A+C) \cos[c+dx]^{7/2} \sin[c+dx]}{3d(a+a \cos[c+dx])^2}$$

Result (type 5, 1398 leaves):

$$\frac{1}{5(A+2C+A \cos[2c+2dx]) (a+a \sec[c+dx])^2} \left( 56i A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \csc\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right] \right. \\ \left. (A+C \sec[c+dx]^2) \left( \left( 2e^{2idx} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2idx} (\cos[c] + i \sin[c])^2\right] \right. \right. \right. \\ \left. \left. \frac{\sqrt{e^{-idx} (2(1+e^{2idx}) \cos[c] + 2i(-1+e^{2idx}) \sin[c])}}{\sqrt{1+e^{2idx} \cos[2c] + i e^{2idx} \sin[2c]}} \right) \right. \right. \\ \left. \left. (3i d (1+e^{2idx}) \cos[c] - 3d(-1+e^{2idx}) \sin[c]) - \right. \right. \\ \left. \left. \left( 2 \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2idx} (\cos[c] + i \sin[c])^2\right] \right. \right. \right. \\ \left. \left. \frac{\sqrt{e^{-idx} (2(1+e^{2idx}) \cos[c] + 2i(-1+e^{2idx}) \sin[c])}}{\sqrt{1+e^{2idx} \cos[2c] + i e^{2idx} \sin[2c]}} \right) \right. \right. \\ \left. \left. (-i d (1+e^{2idx}) \cos[c] + d(-1+e^{2idx}) \sin[c]) \right) \right) + \\ \frac{1}{4(A+2C+A \cos[2c+2dx]) (a+a \sec[c+dx])^2} \\ i \\ C$$

$$\begin{aligned}
 & \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \\
 & \csc\left[\frac{c}{2}\right] \\
 & \sec\left[\frac{c}{2}\right] \\
 & (A + C \sec[c + dx]^2) \\
 & \left( \left( 2 e^{2 i dx} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i dx} (\cos[c] + i \sin[c])^2\right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \cos[c] + 2 i (-1 + e^{2 i dx}) \sin[c])}}{\sqrt{1 + e^{2 i dx} \cos[2 c] + i e^{2 i dx} \sin[2 c]}} \right) / \\
 & \quad (3 i d (1 + e^{2 i dx}) \cos[c] - 3 d (-1 + e^{2 i dx}) \sin[c]) - \\
 & \quad \left. \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i dx} (\cos[c] + i \sin[c])^2\right] \right) \right. \\
 & \quad \left. \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \cos[c] + 2 i (-1 + e^{2 i dx}) \sin[c])}}{\sqrt{1 + e^{2 i dx} \cos[2 c] + i e^{2 i dx} \sin[2 c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2 i dx}) \cos[c] + d (-1 + e^{2 i dx}) \sin[c]) \right) + \\
 & \left( 20 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \csc\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\cot[c]]]\right]^2 \right) \\
 & \quad \sec\left[\frac{c}{2}\right] (A + C \sec[c + dx]^2) \sec[dx - \operatorname{ArcTan}[\cot[c]]] \\
 & \quad \frac{\sqrt{1 - \sin[dx - \operatorname{ArcTan}[\cot[c]]]}}{\sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]]]}} \\
 & \quad \left. \frac{\sqrt{1 + \sin[dx - \operatorname{ArcTan}[\cot[c]]]}}{\sqrt{1 + \cot[c]^2} (a + a \sec[c + dx]^2)} \right) + \\
 & \left( 20 C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \csc\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\cot[c]]]\right]^2 \right) \\
 & \quad \sec\left[\frac{c}{2}\right] (A + C \sec[c + dx]^2) \sec[dx - \operatorname{ArcTan}[\cot[c]]] \\
 & \quad \frac{\sqrt{1 - \sin[dx - \operatorname{ArcTan}[\cot[c]]]}}{\sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]]]}} \\
 & \quad \left. \frac{\sqrt{1 + \sin[dx - \operatorname{ArcTan}[\cot[c]]]}}{\sqrt{1 + \cot[c]^2} (a + a \sec[c + dx]^2)} \right) + \\
 & \left( 3 d (A + 2 C + A \cos[2 c + 2 dx]) \sqrt{1 + \cot[c]^2} (a + a \sec[c + dx]^2) \right) +
 \end{aligned}$$

$$\left( \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 \sqrt{\cos [c + dx]} (A + C \sec [c + dx])^2 \right. \\ \left( - \frac{16 (10A + 5C + 18A \cos [c] + 5C \cos [c]) \operatorname{Csc} [c]}{5d} - \frac{32A \cos [dx] \sin [c]}{3d} + \right. \\ \frac{8A \cos [2dx] \sin [2c]}{5d} + \frac{4 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^3 (A \sin \left[ \frac{dx}{2} \right] + C \sin \left[ \frac{dx}{2} \right])}{3d} - \\ \frac{16 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{dx}{2} \right] (2A \sin \left[ \frac{dx}{2} \right] + C \sin \left[ \frac{dx}{2} \right])}{d} - \frac{32A \cos [c] \sin [dx]}{3d} + \\ \left. \left. \frac{8A \cos [2c] \sin [2dx]}{5d} + \frac{4(A + C) \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \tan \left[ \frac{c}{2} \right]}{3d} \right) \right) / \\ \left( (A + 2C + A \cos [2c + 2dx]) (a + a \sec [c + dx])^2 \right)$$

**Problem 1115: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\cos [c + dx]^{3/2} (A + C \sec [c + dx])^2}{(a + a \sec [c + dx])^2} dx$$

Optimal (type 4, 161 leaves, 7 steps):

$$- \frac{(7A + C) \operatorname{EllipticE} \left[ \frac{1}{2} (c + dx), 2 \right]}{a^2 d} + \\ \frac{2(5A + C) \operatorname{EllipticF} \left[ \frac{1}{2} (c + dx), 2 \right]}{3a^2 d} + \frac{2(5A + C) \sqrt{\cos [c + dx]} \sin [c + dx]}{3a^2 d} - \\ \frac{(7A + C) \cos [c + dx]^{3/2} \sin [c + dx]}{3a^2 d (1 + \cos [c + dx])} - \frac{(A + C) \cos [c + dx]^{5/2} \sin [c + dx]}{3d (a + a \cos [c + dx])^2}$$

Result (type 5, 1355 leaves):

$$- \frac{1}{(A + 2C + A \cos [2c + 2dx]) (a + a \sec [c + dx])^2} \frac{7i A \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 \operatorname{Csc} \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} \right]}{(A + C \sec [c + dx])^2} \left( \left( 2 e^{2i dx} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2i dx} (\cos [c] + i \sin [c])^2 \right] \right. \right. \\ \left. \left. \frac{\sqrt{e^{-i dx} (2(1 + e^{2i dx}) \cos [c] + 2i(-1 + e^{2i dx}) \sin [c])}}{\sqrt{1 + e^{2i dx} \cos [2c] + i e^{2i dx} \sin [2c]}} \right) \right) / \\ (3i d (1 + e^{2i dx}) \cos [c] - 3d (-1 + e^{2i dx}) \sin [c]) - \\ \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i dx} (\cos [c] + i \sin [c])^2 \right] \right. \\ \left. \frac{\sqrt{e^{-i dx} (2(1 + e^{2i dx}) \cos [c] + 2i(-1 + e^{2i dx}) \sin [c])}}{\sqrt{1 + e^{2i dx} \cos [2c] + i e^{2i dx} \sin [2c]}} \right) \right)$$

$$\frac{\left( \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \left( -i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c] \right) - 1}{(A + 2 C + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^2}$$

$$\frac{i C \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} \right] (A + C \sec [c + d x])^2}{\left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c]) \right]^2 \right) \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \left( 3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c] \right) - \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c]) \right]^2 \right) \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \left( -i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c] \right) \right) - \left( 40 A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \right]^2 \right) \operatorname{Sec} \left[ \frac{c}{2} \right] (A + C \sec [c + d x])^2 \operatorname{Sec} [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \sqrt{-\sqrt{1 + \operatorname{Cot} [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \sqrt{1 + \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \right) / \left( 3 d (A + 2 C + A \cos [2 c + 2 d x]) \sqrt{1 + \operatorname{Cot} [c]^2} (a + a \sec [c + d x])^2 \right) - \left( 8 C \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \right]^2 \right) \operatorname{Sec} \left[ \frac{c}{2} \right] (A + C \sec [c + d x])^2 \operatorname{Sec} [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \right)$$

$$\begin{aligned}
 & \left. \frac{\sqrt{1 - \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \sqrt{-\sqrt{1 + \text{Cot} [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \sqrt{1 + \sin [d x - \text{ArcTan} [\text{Cot} [c]]}}}{\left( 3 d (A + 2 C + A \cos [2 c + 2 d x]) \sqrt{1 + \text{Cot} [c]^2} (a + a \sec [c + d x])^2 \right) +} \right. \\
 & \left. \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \sqrt{\cos [c + d x]} (A + C \sec [c + d x])^2 \right) \left( \frac{8 (3 A + C + 4 A \cos [c]) \text{Csc} [c]}{d} + \right. \right. \\
 & \left. \left. \frac{16 A \cos [d x] \sin [c]}{3 d} - \frac{4 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^3 (A \sin \left[ \frac{d x}{2} \right] + C \sin \left[ \frac{d x}{2} \right])}{3 d} + \right. \right. \\
 & \left. \left. \frac{8 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right] (3 A \sin \left[ \frac{d x}{2} \right] + C \sin \left[ \frac{d x}{2} \right])}{d} + \right. \right. \\
 & \left. \left. \frac{16 A \cos [c] \sin [d x]}{3 d} - \frac{4 (A + C) \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \tan \left[ \frac{c}{2} \right]}{3 d} \right) \right) \left. \right) / \\
 & \left( (A + 2 C + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^2 \right)
 \end{aligned}$$

**Problem 1116: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\cos [c + d x]} (A + C \sec [c + d x])^2}{(a + a \sec [c + d x])^2} dx$$

Optimal (type 4, 130 leaves, 6 steps):

$$\frac{4 A \text{EllipticE} \left[ \frac{1}{2} (c + d x), 2 \right]}{a^2 d} - \frac{(5 A - C) \text{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right]}{3 a^2 d} - \frac{(5 A - C) \sqrt{\cos [c + d x]} \sin [c + d x]}{3 a^2 d (1 + \cos [c + d x])} - \frac{(A + C) \cos [c + d x]^{3/2} \sin [c + d x]}{3 d (a + a \cos [c + d x])^2}$$

Result (type 5, 934 leaves):

$$\begin{aligned}
 & \frac{1}{(A + 2 C + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^2} 4 i A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \text{Csc} \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} \right] \\
 & (A + C \sec [c + d x])^2 \left( \left( 2 e^{2 i d x} \text{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \right. \\
 & \left. \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) \right) / \\
 & (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) -
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \\
 & \quad \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \Bigg) / \\
 & \quad \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) + \\
 & \left( 2 \theta A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right]^2 \right) \\
 & \quad \operatorname{Sec} \left[ \frac{c}{2} \right] (A + C \sec [c + d x]^2) \operatorname{Sec} [d x - \operatorname{ArcTan} [\cot [c]]] \\
 & \quad \frac{\sqrt{1 - \sin [d x - \operatorname{ArcTan} [\cot [c]]]}}{\sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]]}} \\
 & \quad \left. \frac{\sqrt{1 + \sin [d x - \operatorname{ArcTan} [\cot [c]]]}}{\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]]}} \right) / \\
 & \left( 3 d (A + 2 C + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} (a + a \sec [c + d x])^2 \right) - \\
 & \left( 4 C \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right]^2 \right) \\
 & \quad \operatorname{Sec} \left[ \frac{c}{2} \right] (A + C \sec [c + d x]^2) \operatorname{Sec} [d x - \operatorname{ArcTan} [\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan} [\cot [c]]]}} \\
 & \quad \left. \frac{\sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]]}}{\sqrt{1 + \sin [d x - \operatorname{ArcTan} [\cot [c]]]}} \right) / \\
 & \left( 3 d (A + 2 C + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} (a + a \sec [c + d x])^2 \right) + \\
 & \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \sqrt{\cos [c + d x]} (A + C \sec [c + d x]^2) \right. \\
 & \quad \left( -\frac{16 A \cot \left[ \frac{c}{2} \right]}{d} - \frac{16 A \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right] \sin \left[ \frac{d x}{2} \right]}{d} + \right. \\
 & \quad \left. \frac{4 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^3 (A \sin \left[ \frac{d x}{2} \right] + C \sin \left[ \frac{d x}{2} \right])}{3 d} + \frac{4 (A + C) \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \tan \left[ \frac{c}{2} \right]}{3 d} \right) \Bigg) / \\
 & \left( (A + 2 C + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^2 \right)
 \end{aligned}$$

**Problem 1117: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + C \operatorname{Sec}[c + d x]^2}{\sqrt{\operatorname{Cos}[c + d x]} (a + a \operatorname{Sec}[c + d x])^2} dx$$

Optimal (type 4, 125 leaves, 6 steps):

$$-\frac{(A-C) \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{a^2 d} + \frac{2(A+C) \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{3 a^2 d} +$$

$$\frac{(A-C) \sqrt{\operatorname{Cos}[c+dx]} \operatorname{Sin}[c+dx]}{a^2 d (1+\operatorname{Cos}[c+dx])} - \frac{(A+C) \sqrt{\operatorname{Cos}[c+dx]} \operatorname{Sin}[c+dx]}{3 d (a+a \operatorname{Cos}[c+dx])^2}$$

Result (type 5, 1322 leaves):

$$-\frac{1}{(A+2C+A \operatorname{Cos}[2c+2dx]) (a+a \operatorname{Sec}[c+dx])^2} i A \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right]$$

$$(A+C \operatorname{Sec}[c+dx]^2) \left( \left( 2 e^{2 i dx} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i dx} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right. \right.$$

$$\left. \frac{\sqrt{e^{-i dx} (2 (1+e^{2 i dx}) \operatorname{Cos}[c] + 2 i (-1+e^{2 i dx}) \operatorname{Sin}[c])}}{\sqrt{1+e^{2 i dx} \operatorname{Cos}[2c] + i e^{2 i dx} \operatorname{Sin}[2c]}} \right) /$$

$$(3 i d (1+e^{2 i dx}) \operatorname{Cos}[c] - 3 d (-1+e^{2 i dx}) \operatorname{Sin}[c]) -$$

$$\left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i dx} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right.$$

$$\left. \frac{\sqrt{e^{-i dx} (2 (1+e^{2 i dx}) \operatorname{Cos}[c] + 2 i (-1+e^{2 i dx}) \operatorname{Sin}[c])}}{\sqrt{1+e^{2 i dx} \operatorname{Cos}[2c] + i e^{2 i dx} \operatorname{Sin}[2c]}} \right) /$$

$$\left. (-i d (1+e^{2 i dx}) \operatorname{Cos}[c] + d (-1+e^{2 i dx}) \operatorname{Sin}[c]) \right) +$$

$$\frac{1}{(A+2C+A \operatorname{Cos}[2c+2dx]) (a+a \operatorname{Sec}[c+dx])^2}$$

$$i$$

$$C$$

$$\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^4$$

$$\operatorname{Csc}\left[\frac{c}{2}\right]$$

$$\operatorname{Sec}\left[\frac{c}{2}\right]$$

$$(A+C \operatorname{Sec}[c+dx]^2)$$

$$\left( \left( 2 e^{2 i dx} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i dx} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right. \right.$$

$$\left. \frac{\sqrt{e^{-i dx} (2 (1+e^{2 i dx}) \operatorname{Cos}[c] + 2 i (-1+e^{2 i dx}) \operatorname{Sin}[c])}}{\sqrt{1+e^{2 i dx} \operatorname{Cos}[2c] + i e^{2 i dx} \operatorname{Sin}[2c]}} \right) /$$

$$(3 i d (1+e^{2 i dx}) \operatorname{Cos}[c] - 3 d (-1+e^{2 i dx}) \operatorname{Sin}[c]) -$$

$$\left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i dx} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right.$$

$$\begin{aligned} & \left( \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \cos [c] + 2 i (-1 + e^{2 i dx}) \sin [c])}}{\sqrt{1 + e^{2 i dx} \cos [2 c] + i e^{2 i dx} \sin [2 c]}} \right) / \\ & \left( -i d (1 + e^{2 i dx}) \cos [c] + d (-1 + e^{2 i dx}) \sin [c] \right) - \\ & \left( 8 A \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [dx - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \right]^2 \right) \\ & \operatorname{Sec} \left[ \frac{c}{2} \right] (A + C \operatorname{Sec} [c + dx]^2) \operatorname{Sec} [dx - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \\ & \sqrt{1 - \sin [dx - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \\ & \sqrt{-\sqrt{1 + \operatorname{Cot} [c]^2} \sin [c] \sin [dx - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \\ & \sqrt{1 + \sin [dx - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \Big) / \\ & \left( 3 d (A + 2 C + A \cos [2 c + 2 dx]) \sqrt{1 + \operatorname{Cot} [c]^2} (a + a \operatorname{Sec} [c + dx])^2 \right) - \\ & \left( 8 C \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [dx - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \right]^2 \right) \\ & \operatorname{Sec} \left[ \frac{c}{2} \right] (A + C \operatorname{Sec} [c + dx]^2) \operatorname{Sec} [dx - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \\ & \sqrt{1 - \sin [dx - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \\ & \sqrt{-\sqrt{1 + \operatorname{Cot} [c]^2} \sin [c] \sin [dx - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \\ & \sqrt{1 + \sin [dx - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \Big) / \\ & \left( 3 d (A + 2 C + A \cos [2 c + 2 dx]) \sqrt{1 + \operatorname{Cot} [c]^2} (a + a \operatorname{Sec} [c + dx])^2 \right) + \\ & \left( \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 \sqrt{\cos [c + dx]} (A + C \operatorname{Sec} [c + dx]^2) \right. \\ & \left( \frac{8 (A - C) \operatorname{Csc} [c]}{d} + \frac{8 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right] (A \sin \left[ \frac{dx}{2} \right] - C \sin \left[ \frac{dx}{2} \right])}{d} - \right. \\ & \left. \frac{4 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right]^3 (A \sin \left[ \frac{dx}{2} \right] + C \sin \left[ \frac{dx}{2} \right])}{3 d} - \frac{4 (A + C) \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \operatorname{Tan} \left[ \frac{c}{2} \right]}{3 d} \right) \Big) / \\ & \left( (A + 2 C + A \cos [2 c + 2 dx]) (a + a \operatorname{Sec} [c + dx])^2 \right) \end{aligned}$$

Problem 1118: Result unnecessarily involves higher level functions and more



than twice size of optimal antiderivative.

$$\int \frac{A + C \operatorname{Sec}[c + dx]^2}{\operatorname{Cos}[c + dx]^{3/2} (a + a \operatorname{Sec}[c + dx])^2} dx$$

Optimal (type 4, 151 leaves, 7 steps):

$$-\frac{4 C \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right]}{a^2 d} + \frac{(A - 5 C) \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right]}{3 a^2 d} + \frac{4 C \operatorname{Sin}[c + dx]}{a^2 d \sqrt{\operatorname{Cos}[c + dx]}} + \frac{(A - 5 C) \operatorname{Sin}[c + dx]}{3 a^2 d \sqrt{\operatorname{Cos}[c + dx]} (1 + \operatorname{Cos}[c + dx])} - \frac{(A + C) \operatorname{Sin}[c + dx]}{3 d \sqrt{\operatorname{Cos}[c + dx]} (a + a \operatorname{Cos}[c + dx])^2}$$

Result (type 5, 954 leaves):

$$-\frac{1}{(A + 2 C + A \operatorname{Cos}[2 c + 2 dx]) (a + a \operatorname{Sec}[c + dx])^2} 4 i C \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c + dx]^2) \left( \left( 2 e^{2 i dx} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i dx} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i dx}) \operatorname{Sin}[c])} \sqrt{1 + e^{2 i dx} \operatorname{Cos}[2 c] + i e^{2 i dx} \operatorname{Sin}[2 c]} \right) / \left( 3 i d (1 + e^{2 i dx}) \operatorname{Cos}[c] - 3 d (-1 + e^{2 i dx}) \operatorname{Sin}[c] \right) - \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i dx} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i dx}) \operatorname{Sin}[c])} \sqrt{1 + e^{2 i dx} \operatorname{Cos}[2 c] + i e^{2 i dx} \operatorname{Sin}[2 c]} \right) / \left( -i d (1 + e^{2 i dx}) \operatorname{Cos}[c] + d (-1 + e^{2 i dx}) \operatorname{Sin}[c] \right) \right) - \left( 4 A \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2 \right) \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c + dx]^2) \operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1 + \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) / \left( 3 d (A + 2 C + A \operatorname{Cos}[2 c + 2 dx]) \sqrt{1 + \operatorname{Cot}[c]^2} (a + a \operatorname{Sec}[c + dx])^2 \right) + \left( 20 C \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2 \right)$$

$$\begin{aligned} & \left. \begin{aligned} & \text{Sec}\left[\frac{c}{2}\right] (A + C \text{Sec}[c + dx]^2) \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \\ & \sqrt{1 - \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \\ & \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \\ & \sqrt{1 + \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \end{aligned} \right) / \\ & \left( 3d (A + 2C + A \text{Cos}[2c + 2dx]) \sqrt{1 + \text{Cot}[c]^2} (a + a \text{Sec}[c + dx])^2 \right) + \\ & \left( \text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\text{Cos}[c + dx]} (A + C \text{Sec}[c + dx]^2) \left( \frac{16C \text{Cot}\left[\frac{c}{2}\right] \text{Sec}[c]}{d} + \right. \right. \\ & \quad \left. \frac{16C \text{Sec}\left[\frac{c}{2}\right] \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] \text{Sin}\left[\frac{dx}{2}\right]}{d} + \frac{4 \text{Sec}\left[\frac{c}{2}\right] \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (A \text{Sin}\left[\frac{dx}{2}\right] + C \text{Sin}\left[\frac{dx}{2}\right])}{3d} + \right. \\ & \quad \left. \left. \frac{16C \text{Sec}[c] \text{Sec}[c + dx] \text{Sin}[dx]}{d} + \frac{4(A + C) \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \text{Tan}\left[\frac{c}{2}\right]}{3d} \right) \right) / \\ & \left( (A + 2C + A \text{Cos}[2c + 2dx]) (a + a \text{Sec}[c + dx])^2 \right) \end{aligned}$$

**Problem 1119: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + C \text{Sec}[c + dx]^2}{\text{Cos}[c + dx]^{5/2} (a + a \text{Sec}[c + dx])^2} dx$$

Optimal (type 4, 189 leaves, 8 steps):

$$\begin{aligned} & \frac{(A + 7C) \text{EllipticE}\left[\frac{1}{2}(c + dx), 2\right]}{a^2 d} + \frac{2(A + 5C) \text{EllipticF}\left[\frac{1}{2}(c + dx), 2\right]}{3a^2 d} + \\ & \frac{2(A + 5C) \text{Sin}[c + dx]}{3a^2 d \text{Cos}[c + dx]^{3/2}} - \frac{(A + 7C) \text{Sin}[c + dx]}{a^2 d \sqrt{\text{Cos}[c + dx]}} - \\ & \frac{(A + 7C) \text{Sin}[c + dx]}{3a^2 d \text{Cos}[c + dx]^{3/2} (1 + \text{Cos}[c + dx])} - \frac{(A + C) \text{Sin}[c + dx]}{3d \text{Cos}[c + dx]^{3/2} (a + a \text{Cos}[c + dx])^2} \end{aligned}$$

Result (type 5, 1391 leaves):

$$\begin{aligned} & \frac{1}{(A + 2C + A \text{Cos}[2c + 2dx]) (a + a \text{Sec}[c + dx])^2} \text{I} A \text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \text{Csc}\left[\frac{c}{2}\right] \text{Sec}\left[\frac{c}{2}\right] \\ & (A + C \text{Sec}[c + dx]^2) \left( \left( 2e^{2ix} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix} (\text{Cos}[c] + \text{I} \text{Sin}[c])^2\right] \right. \right. \\ & \quad \left. \left. \sqrt{e^{-ix} (2(1 + e^{2ix}) \text{Cos}[c] + 2(-1 + e^{2ix}) \text{Sin}[c])} \right. \right. \\ & \quad \left. \left. \sqrt{1 + e^{2ix} \text{Cos}[2c] + \text{I} e^{2ix} \text{Sin}[2c]} \right) \right) / \end{aligned}$$

$$\begin{aligned}
 & \left( 3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c] \right) - \\
 & \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) + \\
 & \frac{1}{(A + 2 C + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^2} \\
 & 7 \\
 & i \\
 & C \\
 & \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \\
 & \operatorname{Csc} \left[ \frac{c}{2} \right] \\
 & \operatorname{Sec} \left[ \frac{c}{2} \right] \\
 & (A + C \sec [c + d x]^2) \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \left. (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) - \right. \\
 & \left. \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) - \\
 & \left( 8 A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]^2 \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[ \frac{c}{2} \right] (A + C \sec [c + d x]^2) \operatorname{Sec} [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \right. \\
 & \quad \left. \frac{\sqrt{1 - \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]}}{\sqrt{-\sqrt{1 + \operatorname{Cot} [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]}} \right. \\
 & \quad \left. \frac{\sqrt{1 + \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]}}{\sqrt{1 + \operatorname{Cot} [c]^2}} \right) / \\
 & \left( 3 d (A + 2 C + A \cos [2 c + 2 d x]) \sqrt{1 + \operatorname{Cot} [c]^2} (a + a \sec [c + d x])^2 \right) -
 \end{aligned}$$

$$\left( 40 C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin\left[dx - \operatorname{ArcTan}\left[\operatorname{Cot}[c]\right]\right]\right]^2 \right. \\ \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + C \operatorname{Sec}[c + dx]^2) \operatorname{Sec}\left[dx - \operatorname{ArcTan}\left[\operatorname{Cot}[c]\right]\right] \right. \\ \left. \sqrt{1 - \sin\left[dx - \operatorname{ArcTan}\left[\operatorname{Cot}[c]\right]\right]} \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin[c] \sin\left[dx - \operatorname{ArcTan}\left[\operatorname{Cot}[c]\right]\right]} \right. \\ \left. \sqrt{1 + \sin\left[dx - \operatorname{ArcTan}\left[\operatorname{Cot}[c]\right]\right]} \right) / \\ \left( 3d (A + 2C + A \cos[2c + 2dx]) \sqrt{1 + \operatorname{Cot}[c]^2} (a + a \operatorname{Sec}[c + dx]^2) \right) + \\ \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c + dx]} (A + C \operatorname{Sec}[c + dx]^2) \right. \\ \left( -\frac{4(4C + A \cos[c] + 3C \cos[c]) \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c]}{d} - \right. \\ \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (A \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{3d} - \\ \frac{8 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] (A \sin\left[\frac{dx}{2}\right] + 3C \sin\left[\frac{dx}{2}\right])}{d} + \frac{16C \operatorname{Sec}[c] \operatorname{Sec}[c + dx]^2 \sin[dx]}{3d} + \\ \left. \left. \frac{16 \operatorname{Sec}[c] \operatorname{Sec}[c + dx] (C \sin[c] - 6C \sin[dx])}{3d} - \frac{4(A + C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Tan}\left[\frac{c}{2}\right]}{3d} \right) \right) / \\ \left( (A + 2C + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx]^2) \right)$$

**Problem 1120: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c + dx]^{5/2} (A + C \operatorname{Sec}[c + dx]^2)}{(a + a \operatorname{Sec}[c + dx])^3} dx$$

Optimal (type 4, 250 leaves, 9 steps):

$$\begin{aligned}
 & \frac{7 (33 A + 7 C) \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{10 a^3 d} - \\
 & \frac{(63 A + 13 C) \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{6 a^3 d} - \frac{(63 A + 13 C) \sqrt{\cos[c + d x]} \sin[c + d x]}{6 a^3 d} + \\
 & \frac{7 (33 A + 7 C) \cos[c + d x]^{3/2} \sin[c + d x]}{30 a^3 d} - \frac{(A + C) \cos[c + d x]^{9/2} \sin[c + d x]}{5 d (a + a \cos[c + d x])^3} - \\
 & \frac{2 (6 A + C) \cos[c + d x]^{7/2} \sin[c + d x]}{15 a d (a + a \cos[c + d x])^2} - \frac{(63 A + 13 C) \cos[c + d x]^{5/2} \sin[c + d x]}{10 d (a^3 + a^3 \cos[c + d x])}
 \end{aligned}$$

Result (type 5, 1507 leaves):

$$\begin{aligned}
 & \frac{1}{5 (A + 2 C + A \cos[2 c + 2 d x]) (a + a \sec[c + d x])^3} 231 i A \cos\left[\frac{c}{2} + \frac{d x}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c + d x] \\
 & \left( (A + C \sec[c + d x])^2 \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right. \right. \right. \\
 & \quad \left. \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])}}{\sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]}} \right) \right. \\
 & \quad \left. (3 i d (1 + e^{2 i d x}) \cos[c] - 3 d (-1 + e^{2 i d x}) \sin[c]) - \right. \\
 & \quad \left. \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right) \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])}}{\sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]}} \right) \right. \\
 & \quad \left. (-i d (1 + e^{2 i d x}) \cos[c] + d (-1 + e^{2 i d x}) \sin[c]) \right) + \\
 & \frac{1}{5 (A + 2 C + A \cos[2 c + 2 d x]) (a + a \sec[c + d x])^3} \\
 & 49 \\
 & i \\
 & C \\
 & \cos\left[\frac{c}{2} + \frac{d x}{2}\right]^6 \\
 & \operatorname{Csc}\left[\frac{c}{2}\right] \\
 & \operatorname{Sec}\left[\frac{c}{2}\right] \\
 & \operatorname{Sec}[c + d x] \\
 & (A + C \sec[c + d x])^2 \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right) \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])}}{\sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]}} \right) \right. \\
 & \quad \left. (3 i d (1 + e^{2 i d x}) \cos[c] - 3 d (-1 + e^{2 i d x}) \sin[c]) - \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \\
 & \quad \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \Bigg) / \\
 & \quad \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) + \\
 & \left( 84 A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \right]^2 \right. \\
 & \quad \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} [c + d x] (A + C \operatorname{Sec} [c + d x]^2) \\
 & \quad \operatorname{Sec} [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \\
 & \quad \left. \sqrt{-\sqrt{1 + \operatorname{Cot} [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \right. \\
 & \quad \left. \sqrt{1 + \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \right) / \\
 & \quad \left( d (A + 2 C + A \cos [2 c + 2 d x]) \sqrt{1 + \operatorname{Cot} [c]^2} (a + a \operatorname{Sec} [c + d x])^3 \right) + \\
 & \left( 52 C \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \right]^2 \right. \\
 & \quad \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} [c + d x] (A + C \operatorname{Sec} [c + d x]^2) \\
 & \quad \operatorname{Sec} [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \\
 & \quad \left. \sqrt{-\sqrt{1 + \operatorname{Cot} [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \sqrt{1 + \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \right) / \\
 & \quad \left( 3 d (A + 2 C + A \cos [2 c + 2 d x]) \sqrt{1 + \operatorname{Cot} [c]^2} (a + a \operatorname{Sec} [c + d x])^3 \right) + \\
 & \quad \frac{1}{\sqrt{\cos [c + d x]} (A + 2 C + A \cos [2 c + 2 d x]) (a + a \operatorname{Sec} [c + d x])^3} \\
 & \quad \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 (A + C \operatorname{Sec} [c + d x]^2) \\
 & \quad \left( -\frac{8 (99 A + 29 C + 132 A \cos [c] + 20 C \cos [c]) \operatorname{Csc} [c]}{5 d} - \frac{32 A \cos [d x] \sin [c]}{d} + \right. \\
 & \quad \frac{16 A \cos [2 d x] \sin [2 c]}{5 d} - \frac{4 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^5 (A \sin \left[ \frac{d x}{2} \right] + C \sin \left[ \frac{d x}{2} \right])}{5 d} + \\
 & \quad \left. \frac{16 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^3 (12 A \sin \left[ \frac{d x}{2} \right] + 7 C \sin \left[ \frac{d x}{2} \right])}{15 d} \right) -
 \end{aligned}$$

$$\frac{8 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] \left(99 A \operatorname{Sin}\left[\frac{dx}{2}\right] + 29 C \operatorname{Sin}\left[\frac{dx}{2}\right]\right)}{5 d} -$$

$$\frac{32 A \operatorname{Cos}[c] \operatorname{Sin}[dx]}{d} + \frac{16 A \operatorname{Cos}[2c] \operatorname{Sin}[2dx]}{5 d} +$$

$$\frac{16 (12 A + 7 C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Tan}\left[\frac{c}{2}\right]}{15 d} - \frac{4 (A + C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Tan}\left[\frac{c}{2}\right]}{5 d}$$

**Problem 1121: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Cos}[c + dx]^{3/2} (A + C \operatorname{Sec}[c + dx]^2)}{(a + a \operatorname{Sec}[c + dx])^3} dx$$

Optimal (type 4, 209 leaves, 8 steps):

$$- \frac{(119 A + 9 C) \operatorname{EllipticE}\left[\frac{1}{2} (c + dx), 2\right]}{10 a^3 d} + \frac{(11 A + C) \operatorname{EllipticF}\left[\frac{1}{2} (c + dx), 2\right]}{2 a^3 d} +$$

$$\frac{(11 A + C) \sqrt{\operatorname{Cos}[c + dx]} \operatorname{Sin}[c + dx]}{2 a^3 d} - \frac{(A + C) \operatorname{Cos}[c + dx]^{7/2} \operatorname{Sin}[c + dx]}{5 d (a + a \operatorname{Cos}[c + dx])^3} -$$

$$\frac{2 A \operatorname{Cos}[c + dx]^{5/2} \operatorname{Sin}[c + dx]}{3 a d (a + a \operatorname{Cos}[c + dx])^2} - \frac{(119 A + 9 C) \operatorname{Cos}[c + dx]^{3/2} \operatorname{Sin}[c + dx]}{30 d (a^3 + a^3 \operatorname{Cos}[c + dx])}$$

Result (type 5, 1470 leaves):

$$- \frac{1}{5 (A + 2 C + A \operatorname{Cos}[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^3}$$

$$119 i A \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c + dx] (A + C \operatorname{Sec}[c + dx]^2)$$

$$\left( \left( 2 e^{2 i dx} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i dx} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right. \right.$$

$$\left. \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i dx}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i dx} \operatorname{Cos}[2c] + i e^{2 i dx} \operatorname{Sin}[2c]}} \right) /$$

$$(3 i d (1 + e^{2 i dx}) \operatorname{Cos}[c] - 3 d (-1 + e^{2 i dx}) \operatorname{Sin}[c]) -$$

$$\left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i dx} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right.$$

$$\left. \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i dx}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i dx} \operatorname{Cos}[2c] + i e^{2 i dx} \operatorname{Sin}[2c]}} \right) /$$

$$\left. (-i d (1 + e^{2 i dx}) \operatorname{Cos}[c] + d (-1 + e^{2 i dx}) \operatorname{Sin}[c]) \right) -$$

$$\frac{1}{5 (A + 2 C + A \operatorname{Cos}[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^3}$$

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$$\begin{aligned}
 & i \\
 & C \\
 & \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \\
 & \csc\left[\frac{c}{2}\right] \\
 & \sec\left[\frac{c}{2}\right] \\
 & \sec[c + dx] \\
 & (A + C \sec[c + dx]^2) \\
 & \left( \left( 2 e^{2 i dx} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i dx} (\cos[c] + i \sin[c])^2\right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \cos[c] + 2 i (-1 + e^{2 i dx}) \sin[c])}}{\sqrt{1 + e^{2 i dx} \cos[2 c] + i e^{2 i dx} \sin[2 c]}} \right) / \\
 & \quad (3 i d (1 + e^{2 i dx}) \cos[c] - 3 d (-1 + e^{2 i dx}) \sin[c]) - \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i dx} (\cos[c] + i \sin[c])^2\right] \right. \\
 & \quad \left. \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \cos[c] + 2 i (-1 + e^{2 i dx}) \sin[c])}}{\sqrt{1 + e^{2 i dx} \cos[2 c] + i e^{2 i dx} \sin[2 c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2 i dx}) \cos[c] + d (-1 + e^{2 i dx}) \sin[c]) \right) - \\
 & \left( 44 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \csc\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\cot[c]]]\right]^2 \right) \\
 & \quad \sec\left[\frac{c}{2}\right] \sec[c + dx] (A + C \sec[c + dx]^2) \\
 & \quad \frac{\sec[dx - \operatorname{ArcTan}[\cot[c]]] \sqrt{1 - \sin[dx - \operatorname{ArcTan}[\cot[c]]]}}{\sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]]]}} \\
 & \quad \left. \frac{\sqrt{1 + \sin[dx - \operatorname{ArcTan}[\cot[c]]]}}{\sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]]]}} \right) / \\
 & \quad \left( d (A + 2 C + A \cos[2 c + 2 dx]) \sqrt{1 + \cot[c]^2} (a + a \sec[c + dx])^3 \right) - \\
 & \left( 4 C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \csc\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\cot[c]]]\right]^2 \right) \\
 & \quad \sec\left[\frac{c}{2}\right] \sec[c + dx] (A + C \sec[c + dx]^2) \\
 & \quad \frac{\sec[dx - \operatorname{ArcTan}[\cot[c]]] \sqrt{1 - \sin[dx - \operatorname{ArcTan}[\cot[c]]]}}{\sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]]]}} \\
 & \quad \left. \frac{\sqrt{1 + \sin[dx - \operatorname{ArcTan}[\cot[c]]]}}{\sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]]]}} \right)
 \end{aligned}$$



$$\left. \begin{aligned} & \sqrt{1 + \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \Bigg/ \\ & \left( d (A + 2 C + A \cos [2 c + 2 d x]) \sqrt{1 + \text{Cot} [c]^2} (a + a \sec [c + d x])^3 \right) + \\ & \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 (A + C \sec [c + d x]^2) \left( \frac{8 (59 A + 9 C + 60 A \cos [c]) \text{Csc} [c]}{5 d} + \right. \right. \\ & \quad \frac{32 A \cos [d x] \sin [c]}{3 d} + \frac{4 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^5 (A \sin \left[ \frac{d x}{2} \right] + C \sin \left[ \frac{d x}{2} \right])}{5 d} - \\ & \quad \frac{8 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^3 (19 A \sin \left[ \frac{d x}{2} \right] + 9 C \sin \left[ \frac{d x}{2} \right])}{15 d} + \\ & \quad \left. \frac{8 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right] (59 A \sin \left[ \frac{d x}{2} \right] + 9 C \sin \left[ \frac{d x}{2} \right])}{5 d} + \frac{32 A \cos [c] \sin [d x]}{3 d} - \right. \\ & \quad \left. \frac{8 (19 A + 9 C) \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \tan \left[ \frac{c}{2} \right]}{15 d} + \frac{4 (A + C) \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \tan \left[ \frac{c}{2} \right]}{5 d} \right) \Bigg/ \\ & \left( \sqrt{\cos [c + d x]} (A + 2 C + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^3 \right) \end{aligned} \right.$$

**Problem 1122: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\cos [c + d x]} (A + C \sec [c + d x]^2)}{(a + a \sec [c + d x])^3} dx$$

Optimal (type 4, 186 leaves, 7 steps):

$$\begin{aligned} & \frac{(49 A - C) \text{EllipticE} \left[ \frac{1}{2} (c + d x), 2 \right]}{10 a^3 d} - \\ & \frac{(13 A - C) \text{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right]}{6 a^3 d} - \frac{(A + C) \cos [c + d x]^{5/2} \sin [c + d x]}{5 d (a + a \cos [c + d x])^3} - \\ & \frac{2 (4 A - C) \cos [c + d x]^{3/2} \sin [c + d x]}{15 a d (a + a \cos [c + d x])^2} - \frac{(13 A - C) \sqrt{\cos [c + d x]} \sin [c + d x]}{6 d (a^3 + a^3 \cos [c + d x])} \end{aligned}$$

Result (type 5, 1446 leaves):

$$\begin{aligned} & \frac{1}{5 (A + 2 C + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^3} 49 i A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \text{Csc} \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} \right] \sec [c + d x] \\ & (A + C \sec [c + d x]^2) \left( \left( 2 e^{2 i d x} \text{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \right. \\ & \quad \left. \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \right. \right. \\ & \quad \left. \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) \right) \Bigg/ \end{aligned}$$

$$\begin{aligned}
 & \left( 3 i d (1 + e^{2 i d x}) \operatorname{Cos}[c] - 3 d (-1 + e^{2 i d x}) \operatorname{Sin}[c] \right) - \\
 & \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]}} \right) / \\
 & \left. (-i d (1 + e^{2 i d x}) \operatorname{Cos}[c] + d (-1 + e^{2 i d x}) \operatorname{Sin}[c]) \right) - \\
 & \frac{1}{5 (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) (a + a \operatorname{Sec}[c + d x])^3} \\
 & i \\
 & C \\
 & \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 \\
 & \operatorname{Csc}\left[\frac{c}{2}\right] \\
 & \operatorname{Sec}\left[\frac{c}{2}\right] \\
 & \operatorname{Sec}[c + d x] \\
 & (A + C \operatorname{Sec}[c + d x]^2) \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]}} \right) / \\
 & \left. (3 i d (1 + e^{2 i d x}) \operatorname{Cos}[c] - 3 d (-1 + e^{2 i d x}) \operatorname{Sin}[c]) - \right. \\
 & \left. \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]}} \right) / \\
 & \left. (-i d (1 + e^{2 i d x}) \operatorname{Cos}[c] + d (-1 + e^{2 i d x}) \operatorname{Sin}[c]) \right) + \\
 & \left( 52 A \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right. \\
 & \quad \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c + d x] (A + C \operatorname{Sec}[c + d x]^2) \\
 & \quad \operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \quad \left. \frac{\sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}}{\sqrt{1 + \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right) / \\
 & \left( 3 d (A + 2 C + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2} (a + a \operatorname{Sec}[c + d x])^3 \right) -
 \end{aligned}$$

$$\left( 4 C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin\left[dx - \operatorname{ArcTan}\left[\operatorname{Cot}\left[\frac{c}{2}\right]\right]\right]^2\right] \right. \\
 \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[c + dx\right] \left(A + C \operatorname{Sec}\left[c + dx\right]^2\right) \right. \\
 \left. \operatorname{Sec}\left[dx - \operatorname{ArcTan}\left[\operatorname{Cot}\left[\frac{c}{2}\right]\right]\right] \sqrt{1 - \sin\left[dx - \operatorname{ArcTan}\left[\operatorname{Cot}\left[\frac{c}{2}\right]\right]\right]} \right. \\
 \left. \sqrt{-\sqrt{1 + \operatorname{Cot}\left[\frac{c}{2}\right]^2} \sin\left[\frac{c}{2}\right] \sin\left[dx - \operatorname{ArcTan}\left[\operatorname{Cot}\left[\frac{c}{2}\right]\right]\right] \sqrt{1 + \sin\left[dx - \operatorname{ArcTan}\left[\operatorname{Cot}\left[\frac{c}{2}\right]\right]\right]}} \right) / \\
 \left( 3 d \left(A + 2 C + A \cos\left[2c + 2dx\right]\right) \sqrt{1 + \operatorname{Cot}\left[\frac{c}{2}\right]^2} \left(a + a \operatorname{Sec}\left[c + dx\right]\right)^3 \right) + \\
 \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \left(A + C \operatorname{Sec}\left[c + dx\right]^2\right) \right. \\
 \left( -\frac{8 \left(29 A - C + 20 A \cos\left[\frac{c}{2}\right]\right) \operatorname{Csc}\left[\frac{c}{2}\right]}{5 d} - \frac{8 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] \left(29 A \sin\left[\frac{dx}{2}\right] - C \sin\left[\frac{dx}{2}\right]\right)}{5 d} \right. \\
 \left. \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^5 \left(A \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right]\right)}{5 d} + \right. \\
 \left. \frac{16 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 \left(7 A \sin\left[\frac{dx}{2}\right] + 2 C \sin\left[\frac{dx}{2}\right]\right)}{15 d} + \right. \\
 \left. \frac{16 \left(7 A + 2 C\right) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Tan}\left[\frac{c}{2}\right]}{15 d} - \frac{4 \left(A + C\right) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Tan}\left[\frac{c}{2}\right]}{5 d} \right) \left. \right) / \\
 \left( \sqrt{\cos\left[c + dx\right]} \left(A + 2 C + A \cos\left[2c + 2dx\right]\right) \left(a + a \operatorname{Sec}\left[c + dx\right]\right)^3 \right)$$

**Problem 1123: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + C \operatorname{Sec}\left[c + dx\right]^2}{\sqrt{\cos\left[c + dx\right]} \left(a + a \operatorname{Sec}\left[c + dx\right]\right)^3} dx$$

Optimal (type 4, 184 leaves, 7 steps):

$$-\frac{(9A - C) \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right]}{10 a^3 d} + \\
 \frac{(3A + C) \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right]}{6 a^3 d} - \frac{(A + C) \cos\left[c + dx\right]^{3/2} \sin\left[c + dx\right]}{5 d \left(a + a \cos\left[c + dx\right]\right)^3} - \\
 \frac{2(3A - 2C) \sqrt{\cos\left[c + dx\right]} \sin\left[c + dx\right]}{15 a d \left(a + a \cos\left[c + dx\right]\right)^2} + \frac{(9A - C) \sqrt{\cos\left[c + dx\right]} \sin\left[c + dx\right]}{10 d \left(a^3 + a^3 \cos\left[c + dx\right]\right)}$$

Result (type 5, 1439 leaves):

$$\begin{aligned}
 & - \frac{1}{5 (A + 2 C + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^3} 9 i A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \csc \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} \right] \sec [c + d x] \\
 & \quad (A + C \sec [c + d x]^2) \left( \left( 2 e^{2 i d x} \text{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \quad (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) - \\
 & \quad \left( 2 \text{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right) \\
 & \quad \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) + \\
 & \frac{1}{5 (A + 2 C + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^3} \\
 & \quad i \\
 & \quad C \\
 & \quad \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \\
 & \quad \csc \left[ \frac{c}{2} \right] \\
 & \quad \sec \left[ \frac{c}{2} \right] \\
 & \quad \sec [c + d x] \\
 & \quad (A + C \sec [c + d x]^2) \\
 & \quad \left( \left( 2 e^{2 i d x} \text{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right) \right. \\
 & \quad \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \quad (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) - \\
 & \quad \left( 2 \text{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right) \\
 & \quad \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) - \\
 & \quad \left( 4 A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \csc \left[ \frac{c}{2} \right] \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \text{ArcTan} [\text{Cot} [c]]] \right]^2 \right) \\
 & \quad \sec \left[ \frac{c}{2} \right] \sec [c + d x] (A + C \sec [c + d x]^2) \\
 & \quad \sec [d x - \text{ArcTan} [\text{Cot} [c]]] \sqrt{1 - \sin [d x - \text{ArcTan} [\text{Cot} [c]]]}
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{\sqrt{-\sqrt{1+\cot^2[c]} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]}}{\sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]}} \right) / \\
 & \left( d (A+2C+A \cos[2c+2dx]) \sqrt{1+\cot^2[c]} (a+a \sec[c+dx])^3 \right) - \\
 & \left( 4C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \csc\left[\frac{c}{2}\right] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\cot[c]]]^2\right] \right. \\
 & \quad \sec\left[\frac{c}{2}\right] \sec[c+dx] (A+C \sec[c+dx])^2 \\
 & \quad \sec[dx - \text{ArcTan}[\cot[c]]] \sqrt{1-\sin[dx - \text{ArcTan}[\cot[c]]]} \\
 & \quad \left. \frac{\sqrt{-\sqrt{1+\cot^2[c]} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]}}{\sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]}} \right) / \\
 & \left( 3d (A+2C+A \cos[2c+2dx]) \sqrt{1+\cot^2[c]} (a+a \sec[c+dx])^3 \right) + \\
 & \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (A+C \sec[c+dx])^2 \right. \\
 & \quad \left( \frac{8(9A-C) \csc[c]}{5d} + \frac{8 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right] (9A \sin\left[\frac{dx}{2}\right] - C \sin\left[\frac{dx}{2}\right])}{5d} \right) - \\
 & \quad \frac{8 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (9A \sin\left[\frac{dx}{2}\right] - C \sin\left[\frac{dx}{2}\right])}{15d} + \\
 & \quad \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^5 (A \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{5d} - \\
 & \quad \left. \left. \frac{8(9A-C) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{15d} + \frac{4(A+C) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \tan\left[\frac{c}{2}\right]}{5d} \right) \right) / \\
 & \left( \sqrt{\cos[c+dx]} (A+2C+A \cos[2c+2dx]) (a+a \sec[c+dx])^3 \right)
 \end{aligned}$$

**Problem 1124:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{A+C \sec[c+dx]^2}{\cos[c+dx]^{3/2} (a+a \sec[c+dx])^3} dx$$

Optimal (type 4, 180 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{(A-9C) \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{10a^3d} + \\
 & \frac{(A+3C) \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{6a^3d} - \frac{(A+C) \sqrt{\cos[c+dx]} \sin[c+dx]}{5d(a+a\cos[c+dx])^3} + \\
 & \frac{2(2A-3C) \sqrt{\cos[c+dx]} \sin[c+dx]}{15ad(a+a\cos[c+dx])^2} + \frac{(A-9C) \sqrt{\cos[c+dx]} \sin[c+dx]}{10d(a^3+a^3\cos[c+dx])}
 \end{aligned}$$

Result (type 5, 1436 leaves):

$$\begin{aligned}
 & - \frac{1}{5(A+2C+A\cos[2c+2dx])(a+a\sec[c+dx])^3} \operatorname{Im} A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx] \\
 & \quad (A+C\sec[c+dx])^2 \left( \left( 2e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix}(\cos[c] + i\sin[c])^2\right] \right. \right. \\
 & \quad \left. \left. \frac{\sqrt{e^{-ix}(2(1+e^{2ix})\cos[c] + 2i(-1+e^{2ix})\sin[c])}}{\sqrt{1+e^{2ix}\cos[2c] + ie^{2ix}\sin[2c]}} \right) / \right. \\
 & \quad \left. (3id(1+e^{2ix})\cos[c] - 3d(-1+e^{2ix})\sin[c]) - \right. \\
 & \quad \left. \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix}(\cos[c] + i\sin[c])^2\right] \right. \right. \\
 & \quad \left. \left. \frac{\sqrt{e^{-ix}(2(1+e^{2ix})\cos[c] + 2i(-1+e^{2ix})\sin[c])}}{\sqrt{1+e^{2ix}\cos[2c] + ie^{2ix}\sin[2c]}} \right) / \right. \\
 & \quad \left. (-id(1+e^{2ix})\cos[c] + d(-1+e^{2ix})\sin[c]) \right) + \\
 & \quad \frac{1}{5(A+2C+A\cos[2c+2dx])(a+a\sec[c+dx])^3} \\
 & \quad 9 \\
 & \quad i \\
 & \quad C \\
 & \quad \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \\
 & \quad \operatorname{Csc}\left[\frac{c}{2}\right] \\
 & \quad \operatorname{Sec}\left[\frac{c}{2}\right] \\
 & \quad \operatorname{Sec}[c+dx] \\
 & \quad (A+C\sec[c+dx])^2 \\
 & \quad \left( \left( 2e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix}(\cos[c] + i\sin[c])^2\right] \right. \right. \\
 & \quad \left. \left. \frac{\sqrt{e^{-ix}(2(1+e^{2ix})\cos[c] + 2i(-1+e^{2ix})\sin[c])}}{\sqrt{1+e^{2ix}\cos[2c] + ie^{2ix}\sin[2c]}} \right) / \right. \\
 & \quad \left. (3id(1+e^{2ix})\cos[c] - 3d(-1+e^{2ix})\sin[c]) - \right. \\
 & \quad \left. \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix}(\cos[c] + i\sin[c])^2\right] \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \cos [c] + 2 i (-1 + e^{2 i dx}) \sin [c])}}{\sqrt{1 + e^{2 i dx} \cos [2 c] + i e^{2 i dx} \sin [2 c]}} \right) / \\
 & \left( -i d (1 + e^{2 i dx}) \cos [c] + d (-1 + e^{2 i dx}) \sin [c] \right) - \\
 & \left( 4 A \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^6 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [dx - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \right]^2 \right) \\
 & \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} [c + dx] (A + C \operatorname{Sec} [c + dx]^2) \\
 & \operatorname{Sec} [dx - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \sqrt{1 - \sin [dx - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \\
 & \sqrt{-\sqrt{1 + \operatorname{Cot} [c]^2} \sin [c] \sin [dx - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \\
 & \left. \sqrt{1 + \sin [dx - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \right) / \\
 & \left( 3 d (A + 2 C + A \cos [2 c + 2 dx]) \sqrt{1 + \operatorname{Cot} [c]^2} (a + a \operatorname{Sec} [c + dx])^3 \right) - \\
 & \left( 4 C \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^6 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [dx - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \right]^2 \right) \\
 & \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} [c + dx] (A + C \operatorname{Sec} [c + dx]^2) \\
 & \operatorname{Sec} [dx - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \sqrt{1 - \sin [dx - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \\
 & \sqrt{-\sqrt{1 + \operatorname{Cot} [c]^2} \sin [c] \sin [dx - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \\
 & \left. \sqrt{1 + \sin [dx - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \right) / \\
 & \left( d (A + 2 C + A \cos [2 c + 2 dx]) \sqrt{1 + \operatorname{Cot} [c]^2} (a + a \operatorname{Sec} [c + dx])^3 \right) + \\
 & \left( \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^6 (A + C \operatorname{Sec} [c + dx]^2) \right. \\
 & \left( \frac{8 (A - 9 C) \operatorname{Csc} [c]}{5 d} + \frac{8 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right] (A \sin \left[ \frac{dx}{2} \right] - 9 C \sin \left[ \frac{dx}{2} \right])}{5 d} \right) + \\
 & \frac{16 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right]^3 (2 A \sin \left[ \frac{dx}{2} \right] - 3 C \sin \left[ \frac{dx}{2} \right])}{15 d} - \\
 & \frac{4 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right]^5 (A \sin \left[ \frac{dx}{2} \right] + C \sin \left[ \frac{dx}{2} \right])}{5 d} + \\
 & \left. \left. \frac{16 (2 A - 3 C) \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \operatorname{Tan} \left[ \frac{c}{2} \right]}{15 d} - \frac{4 (A + C) \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 \operatorname{Tan} \left[ \frac{c}{2} \right]}{5 d} \right) \right) /
 \end{aligned}$$

$$\left(\sqrt{\cos [c+d x]} (A+2 C+A \cos [2 c+2 d x]) (a+a \sec [c+d x])^3\right)$$

**Problem 1125: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A+C \sec [c+d x]^2}{\cos [c+d x]^{5/2} (a+a \sec [c+d x])^3} dx$$

Optimal (type 4, 209 leaves, 8 steps):

$$\frac{(A-49 C) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{10 a^3 d} + \frac{(A-13 C) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{6 a^3 d} -$$

$$\frac{(A-49 C) \sin [c+d x]}{10 a^3 d \sqrt{\cos [c+d x]}} - \frac{(A+C) \sin [c+d x]}{5 d \sqrt{\cos [c+d x]} (a+a \cos [c+d x])^3} +$$

$$\frac{2(A-4 C) \sin [c+d x]}{15 a d \sqrt{\cos [c+d x]} (a+a \cos [c+d x])^2} + \frac{(A-13 C) \sin [c+d x]}{6 d \sqrt{\cos [c+d x]} (a^3+a^3 \cos [c+d x])}$$

Result (type 5, 1473 leaves):

$$\frac{1}{5(A+2 C+A \cos [2 c+2 d x]) (a+a \sec [c+d x])^3} i A \cos \left[\frac{c}{2}+\frac{d x}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+d x]$$

$$(A+C \sec [c+d x]^2) \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c]+i \sin [c])^2\right] \right. \right.$$

$$\left. \frac{\sqrt{e^{-i d x} (2(1+e^{2 i d x}) \cos [c]+2 i(-1+e^{2 i d x}) \sin [c])}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}} \right) /$$

$$(3 i d(1+e^{2 i d x}) \cos [c]-3 d(-1+e^{2 i d x}) \sin [c]) -$$

$$\left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c]+i \sin [c])^2\right] \right.$$

$$\left. \frac{\sqrt{e^{-i d x} (2(1+e^{2 i d x}) \cos [c]+2 i(-1+e^{2 i d x}) \sin [c])}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}} \right) /$$

$$\left. (-i d(1+e^{2 i d x}) \cos [c]+d(-1+e^{2 i d x}) \sin [c]) \right) -$$

$$\frac{1}{5(A+2 C+A \cos [2 c+2 d x]) (a+a \sec [c+d x])^3}$$

49  
i  
C  
Cos [c/2 + dx/2]^6  
Csc [c/2]  
Sec [c/2]  
Sec [c + dx]



$$\begin{aligned}
 & (A + C \operatorname{Sec}[c + dx]^2) \\
 & \left( \left( 2 e^{2i dx} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2i dx} (\cos[c] + i \sin[c])\right]^2 \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i dx} (2 (1 + e^{2i dx}) \cos[c] + 2i (-1 + e^{2i dx}) \sin[c])}}{\sqrt{1 + e^{2i dx} \cos[2c] + i e^{2i dx} \sin[2c]}} \right) / \\
 & \quad \left( 3 i d (1 + e^{2i dx}) \cos[c] - 3 d (-1 + e^{2i dx}) \sin[c] \right) - \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i dx} (\cos[c] + i \sin[c])\right]^2 \right. \\
 & \quad \left. \frac{\sqrt{e^{-i dx} (2 (1 + e^{2i dx}) \cos[c] + 2i (-1 + e^{2i dx}) \sin[c])}}{\sqrt{1 + e^{2i dx} \cos[2c] + i e^{2i dx} \sin[2c]}} \right) / \\
 & \quad \left. \left. (-i d (1 + e^{2i dx}) \cos[c] + d (-1 + e^{2i dx}) \sin[c]) \right) \right) - \\
 & \left( 4 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2 \right) \\
 & \quad \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c + dx] (A + C \operatorname{Sec}[c + dx]^2) \\
 & \quad \operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \quad \left. \frac{\sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}}{\sqrt{1 + \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right) / \\
 & \quad \left( 3 d (A + 2 C + A \cos[2c + 2dx]) \sqrt{1 + \operatorname{Cot}[c]^2} (a + a \operatorname{Sec}[c + dx])^3 \right) + \\
 & \left( 52 C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2 \right) \\
 & \quad \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c + dx] (A + C \operatorname{Sec}[c + dx]^2) \\
 & \quad \operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \quad \left. \frac{\sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}}}{\sqrt{1 + \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right) / \\
 & \quad \left( 3 d (A + 2 C + A \cos[2c + 2dx]) \sqrt{1 + \operatorname{Cot}[c]^2} (a + a \operatorname{Sec}[c + dx])^3 \right) + \\
 & \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (A + C \operatorname{Sec}[c + dx]^2) \left( -\frac{4 (-20 C + A \cos[c] - 29 C \cos[c]) \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c]}{5 d} \right. \right. \\
 & \quad \left. \left. \frac{8 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] (A \sin\left[\frac{dx}{2}\right] - 29 C \sin\left[\frac{dx}{2}\right])}{5 d} \right) + \right.
 \end{aligned}$$

$$\frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^5 \left(A \operatorname{Sin}\left[\frac{dx}{2}\right] + C \operatorname{Sin}\left[\frac{dx}{2}\right]\right)}{5 d} +$$

$$\frac{8 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 \left(A \operatorname{Sin}\left[\frac{dx}{2}\right] + 11 C \operatorname{Sin}\left[\frac{dx}{2}\right]\right)}{15 d} + \frac{32 C \operatorname{Sec}[c] \operatorname{Sec}[c + dx] \operatorname{Sin}[dx]}{d} +$$

$$\left. \frac{8 (A + 11 C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Tan}\left[\frac{c}{2}\right]}{15 d} + \frac{4 (A + C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Tan}\left[\frac{c}{2}\right]}{5 d} \right) \Bigg/$$

$$\left(\sqrt{\operatorname{Cos}[c + dx]} (A + 2 C + A \operatorname{Cos}[2 c + 2 dx]) (a + a \operatorname{Sec}[c + dx])^3\right)$$

**Problem 1126: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + C \operatorname{Sec}[c + dx]^2}{\operatorname{Cos}[c + dx]^{7/2} (a + a \operatorname{Sec}[c + dx])^3} dx$$

Optimal (type 4, 242 leaves, 9 steps):

$$\frac{(9 A + 119 C) \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right]}{10 a^3 d} + \frac{(A + 11 C) \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right]}{2 a^3 d} +$$

$$\frac{(A + 11 C) \operatorname{Sin}[c + dx]}{2 a^3 d \operatorname{Cos}[c + dx]^{3/2}} - \frac{(9 A + 119 C) \operatorname{Sin}[c + dx]}{10 a^3 d \sqrt{\operatorname{Cos}[c + dx]}} - \frac{(A + C) \operatorname{Sin}[c + dx]}{5 d \operatorname{Cos}[c + dx]^{3/2} (a + a \operatorname{Cos}[c + dx])^3} -$$

$$\frac{2 C \operatorname{Sin}[c + dx]}{3 a d \operatorname{Cos}[c + dx]^{3/2} (a + a \operatorname{Cos}[c + dx])^2} - \frac{(9 A + 119 C) \operatorname{Sin}[c + dx]}{30 d \operatorname{Cos}[c + dx]^{3/2} (a^3 + a^3 \operatorname{Cos}[c + dx])}$$

Result (type 5, 1505 leaves):

$$\frac{1}{5 (A + 2 C + A \operatorname{Cos}[2 c + 2 dx]) (a + a \operatorname{Sec}[c + dx])^3} 9 i A \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c + dx]$$

$$\left( (A + C \operatorname{Sec}[c + dx]^2) \left( \left( 2 e^{2 i dx} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i dx} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right. \right. \right.$$

$$\left. \left. \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i dx}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i dx} \operatorname{Cos}[2 c] + i e^{2 i dx} \operatorname{Sin}[2 c]}} \right) \right) \Bigg/$$

$$(3 i d (1 + e^{2 i dx}) \operatorname{Cos}[c] - 3 d (-1 + e^{2 i dx}) \operatorname{Sin}[c]) -$$

$$\left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i dx} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right.$$

$$\left. \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i dx}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i dx} \operatorname{Cos}[2 c] + i e^{2 i dx} \operatorname{Sin}[2 c]}} \right) \Bigg/$$

$$\left. (-i d (1 + e^{2 i dx}) \operatorname{Cos}[c] + d (-1 + e^{2 i dx}) \operatorname{Sin}[c]) \right) +$$

$$\frac{1}{5 (A + 2 C + A \operatorname{Cos}[2 c + 2 dx]) (a + a \operatorname{Sec}[c + dx])^3}$$

$$\begin{aligned}
 & i \\
 & C \\
 & \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \\
 & \csc\left[\frac{c}{2}\right] \\
 & \sec\left[\frac{c}{2}\right] \\
 & \sec[c + dx] \\
 & (A + C \sec[c + dx]^2) \\
 & \left( \left( 2 e^{2 i dx} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i dx} (\cos[c] + i \sin[c])^2\right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \cos[c] + 2 i (-1 + e^{2 i dx}) \sin[c])}}{\sqrt{1 + e^{2 i dx} \cos[2 c] + i e^{2 i dx} \sin[2 c]}} \right) / \\
 & \quad (3 i d (1 + e^{2 i dx}) \cos[c] - 3 d (-1 + e^{2 i dx}) \sin[c]) - \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i dx} (\cos[c] + i \sin[c])^2\right] \right. \\
 & \quad \left. \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \cos[c] + 2 i (-1 + e^{2 i dx}) \sin[c])}}{\sqrt{1 + e^{2 i dx} \cos[2 c] + i e^{2 i dx} \sin[2 c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2 i dx}) \cos[c] + d (-1 + e^{2 i dx}) \sin[c]) \right) - \\
 & \left( 4 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \csc\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\cot[c]]]\right]^2 \right) \\
 & \quad \sec\left[\frac{c}{2}\right] \sec[c + dx] (A + C \sec[c + dx]^2) \\
 & \quad \frac{\sec[dx - \operatorname{ArcTan}[\cot[c]]] \sqrt{1 - \sin[dx - \operatorname{ArcTan}[\cot[c]]]}}{\sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]]]}} \\
 & \quad \left. \frac{\sqrt{1 + \sin[dx - \operatorname{ArcTan}[\cot[c]]]}}{\sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]]]} \right) / \\
 & \quad \left( d (A + 2 C + A \cos[2 c + 2 dx]) \sqrt{1 + \cot[c]^2} (a + a \sec[c + dx])^3 \right) - \\
 & \left( 44 C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \csc\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\cot[c]]]\right]^2 \right) \\
 & \quad \sec\left[\frac{c}{2}\right] \sec[c + dx] (A + C \sec[c + dx]^2) \\
 & \quad \frac{\sec[dx - \operatorname{ArcTan}[\cot[c]]] \sqrt{1 - \sin[dx - \operatorname{ArcTan}[\cot[c]]]}}{\sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]]]} \sqrt{1 + \sin[dx - \operatorname{ArcTan}[\cot[c]]]}} \right) /
 \end{aligned}$$

$$\left( \frac{d (A + 2C + A \cos[2c + 2dx]) \sqrt{1 + \cot^2[c]} (a + a \sec[c + dx])^3}{1} + \frac{\sqrt{\cos[c + dx]} (A + 2C + A \cos[2c + 2dx]) (a + a \sec[c + dx])^3}{\cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (A + C \sec[c + dx])^2} \right. \\ \left. - \frac{4 (60C + 9A \cos[c] + 59C \cos[c]) \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c]}{5d} - \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^5 (A \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{5d} - \frac{16 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (3A \sin\left[\frac{dx}{2}\right] + 8C \sin\left[\frac{dx}{2}\right])}{15d} - \frac{8 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] (9A \sin\left[\frac{dx}{2}\right] + 59C \sin\left[\frac{dx}{2}\right])}{5d} + \frac{32C \operatorname{Sec}[c] \operatorname{Sec}[c + dx]^2 \sin[dx]}{3d} + \frac{32 \operatorname{Sec}[c] \operatorname{Sec}[c + dx] (C \sin[c] - 9C \sin[dx])}{3d} - \frac{16 (3A + 8C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Tan}\left[\frac{c}{2}\right]}{15d} - \frac{4 (A + C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Tan}\left[\frac{c}{2}\right]}{5d} \right)$$

**Problem 1130: Result unnecessarily involves higher level functions.**

$$\int \cos[c + dx]^{3/2} \sqrt{a + a \sec[c + dx]} (A + C \sec[c + dx])^2 dx$$

Optimal (type 3, 136 leaves, 5 steps):

$$\frac{2 \sqrt{a} C \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c + dx]}{\sqrt{a + a \sec[c + dx]}}\right] \sqrt{\cos[c + dx]} \sqrt{\sec[c + dx]}}{d} + \frac{2aA \sin[c + dx]}{3d \sqrt{\cos[c + dx]} \sqrt{a + a \sec[c + dx]}} + \frac{2A \sqrt{\cos[c + dx]} \sqrt{a + a \sec[c + dx]} \sin[c + dx]}{3d}$$

Result (type 5, 174 leaves):

$$\left( 2 \sqrt{\cos[c + dx]} (C + A \cos[c + dx])^2 \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right] \sqrt{a (1 + \sec[c + dx])} \left( -6 i C e^{\frac{1}{2} i (c + dx)} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i (c + dx)}\right] - 2 i C e^{\frac{3}{2} i (c + dx)} \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i (c + dx)}\right] + A \left( 3 \sin\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{3}{2}(c + dx)\right] \right) \right) \right) / (3d (A + 2C + A \cos[2(c + dx)]))$$

**Problem 1131: Result unnecessarily involves higher level functions.**

$$\int \frac{\sqrt{\cos [c+d x]} \sqrt{a+a \sec [c+d x]} (A+C \sec [c+d x]^2) d x}{d}$$

Optimal (type 3, 135 leaves, 5 steps):

$$\frac{\sqrt{a} C \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan [c+d x]}{\sqrt{a+a \sec [c+d x]}}\right] \sqrt{\cos [c+d x]} \sqrt{\sec [c+d x]}}{d} + \frac{a(2 A-C) \sin [c+d x]}{d \sqrt{\cos [c+d x]} \sqrt{a+a \sec [c+d x]}} + \frac{C \sqrt{a+a \sec [c+d x]} \sin [c+d x]}{d \sqrt{\cos [c+d x]}}$$

Result (type 5, 184 leaves):

$$\left(2(C+A \cos [c+d x]^2) \sec \left[\frac{1}{2}(c+d x)\right] \sqrt{a(1+\sec [c+d x])} - \left(-3 i C e^{\frac{1}{2} i(c+d x)} \cos [c+d x] \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i(c+d x)}\right] - i C e^{\frac{3}{2} i(c+d x)} \cos [c+d x] \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i(c+d x)}\right] + 3(C+2 A \cos [c+d x]) \sin \left[\frac{1}{2}(c+d x)\right]\right) / \left(3 d \sqrt{\cos [c+d x]} (A+2 C+A \cos [2(c+d x)])\right)$$

**Problem 1132: Result unnecessarily involves higher level functions.**

$$\int \frac{\sqrt{a+a \sec [c+d x]} (A+C \sec [c+d x]^2) d x}{\sqrt{\cos [c+d x]}}$$

Optimal (type 3, 144 leaves, 5 steps):

$$\frac{\sqrt{a} (8 A+3 C) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan [c+d x]}{\sqrt{a+a \sec [c+d x]}}\right] \sqrt{\cos [c+d x]} \sqrt{\sec [c+d x]}}{4 d} + \frac{a C \sin [c+d x]}{4 d \cos [c+d x]^{3/2} \sqrt{a+a \sec [c+d x]}} + \frac{C \sqrt{a+a \sec [c+d x]} \sin [c+d x]}{2 d \cos [c+d x]^{3/2}}$$

Result (type 5, 161 leaves):

$$\frac{1}{12 d} \sqrt{\cos [c+d x]} \sec \left[\frac{1}{2}(c+d x)\right] \sqrt{a(1+\sec [c+d x])} - \left(-3 i (8 A+3 C) e^{\frac{1}{2} i(c+d x)} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i(c+d x)}\right] - i (8 A+3 C) e^{\frac{3}{2} i(c+d x)} \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i(c+d x)}\right] + 3 C \sec [c+d x] (3+2 \sec [c+d x]) \sin \left[\frac{1}{2}(c+d x)\right]\right)$$

**Problem 1133: Result unnecessarily involves higher level functions.**

$$\int \frac{\sqrt{a + a \operatorname{Sec}[c + d x]} (A + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Cos}[c + d x]^{3/2}} dx$$

Optimal (type 3, 189 leaves, 6 steps):

$$\frac{\sqrt{a} (8 A + 5 C) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c + d x]}{\sqrt{a + a \operatorname{Sec}[c + d x]}}\right] \sqrt{\operatorname{Cos}[c + d x]} \sqrt{\operatorname{Sec}[c + d x]}}{8 d} +$$

$$\frac{a C \operatorname{Sin}[c + d x]}{12 d \operatorname{Cos}[c + d x]^{5/2} \sqrt{a + a \operatorname{Sec}[c + d x]}} +$$

$$\frac{a (8 A + 5 C) \operatorname{Sin}[c + d x]}{8 d \operatorname{Cos}[c + d x]^{3/2} \sqrt{a + a \operatorname{Sec}[c + d x]}} + \frac{C \sqrt{a + a \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{3 d \operatorname{Cos}[c + d x]^{5/2}}$$

Result (type 5, 176 leaves):

$$\frac{1}{24 d} \sqrt{\operatorname{Cos}[c + d x]} \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right] \sqrt{a (1 + \operatorname{Sec}[c + d x])}$$

$$\left( -3 i (8 A + 5 C) e^{\frac{1}{2} i (c + d x)} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i (c + d x)}\right] - \right.$$

$$\left. i (8 A + 5 C) e^{\frac{3}{2} i (c + d x)} \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i (c + d x)}\right] + \right.$$

$$\left. \operatorname{Sec}[c + d x] (24 A + 15 C + 10 C \operatorname{Sec}[c + d x] + 8 C \operatorname{Sec}[c + d x]^2) \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)$$

**Problem 1134: Result unnecessarily involves higher level functions.**

$$\int \frac{\sqrt{a + a \operatorname{Sec}[c + d x]} (A + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Cos}[c + d x]^{5/2}} dx$$

Optimal (type 3, 234 leaves, 7 steps):

$$\frac{\sqrt{a} (48 A + 35 C) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c + d x]}{\sqrt{a + a \operatorname{Sec}[c + d x]}}\right] \sqrt{\operatorname{Cos}[c + d x]} \sqrt{\operatorname{Sec}[c + d x]}}{64 d} +$$

$$\frac{a C \operatorname{Sin}[c + d x]}{24 d \operatorname{Cos}[c + d x]^{7/2} \sqrt{a + a \operatorname{Sec}[c + d x]}} + \frac{a (48 A + 35 C) \operatorname{Sin}[c + d x]}{96 d \operatorname{Cos}[c + d x]^{5/2} \sqrt{a + a \operatorname{Sec}[c + d x]}} +$$

$$\frac{a (48 A + 35 C) \operatorname{Sin}[c + d x]}{64 d \operatorname{Cos}[c + d x]^{3/2} \sqrt{a + a \operatorname{Sec}[c + d x]}} + \frac{C \sqrt{a + a \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{4 d \operatorname{Cos}[c + d x]^{7/2}}$$

Result (type 5, 195 leaves):

$$\frac{1}{192 d} \sqrt{\cos [c+d x]} \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right] \sqrt{a\left(1+\operatorname{Sec}[c+d x]\right)} \left(-3 i(48 A+35 C) e^{\frac{1}{2} i(c+d x)} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i(c+d x)}\right]-i(48 A+35 C) e^{\frac{3}{2} i(c+d x)} \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i(c+d x)}\right]+\operatorname{Sec}[c+d x]\left(3(48 A+35 C)+(96 A+70 C) \operatorname{Sec}[c+d x]+56 C \operatorname{Sec}[c+d x]^2+48 C \operatorname{Sec}[c+d x]^3\right) \sin\left[\frac{1}{2}(c+d x)\right]\right)$$

**Problem 1138: Result unnecessarily involves higher level functions.**

$$\int \cos [c+d x]^{5 / 2}(a+a \operatorname{Sec}[c+d x])^{3 / 2}(A+C \operatorname{Sec}[c+d x]^2) d x$$

Optimal (type 3, 183 leaves, 6 steps):

$$\frac{2 a^{3 / 2} C \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right] \sqrt{\cos [c+d x]} \sqrt{\operatorname{Sec}[c+d x]}}{d} + \frac{2 a^2(4 A+5 C) \sin [c+d x]}{5 d \sqrt{\cos [c+d x]} \sqrt{a+a \operatorname{Sec}[c+d x]}} + \frac{2 a A \sqrt{\cos [c+d x]} \sqrt{a+a \operatorname{Sec}[c+d x]} \sin [c+d x]}{5 d} + \frac{2 A \cos [c+d x]^{3 / 2}(a+a \operatorname{Sec}[c+d x])^{3 / 2} \sin [c+d x]}{5 d}$$

Result (type 5, 198 leaves):

$$\frac{1}{30 d(A+2 C+A \cos [2(c+d x)])} a \sqrt{\cos [c+d x]}(1+\cos [c+d x])(C+A \cos [c+d x]^2) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^3 \sqrt{a(1+\operatorname{Sec}[c+d x])}\left(-60 i C e^{\frac{1}{2} i(c+d x)} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i(c+d x)}\right]-20 i C e^{\frac{3}{2} i(c+d x)} \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i(c+d x)}\right]+6(13 A+10 C+6 A \cos [c+d x]+A \cos [2(c+d x)]) \sin\left[\frac{1}{2}(c+d x)\right]\right)$$

**Problem 1139: Result unnecessarily involves higher level functions.**

$$\int \cos [c+d x]^{3 / 2}(a+a \operatorname{Sec}[c+d x])^{3 / 2}(A+C \operatorname{Sec}[c+d x]^2) d x$$

Optimal (type 3, 189 leaves, 6 steps):

$$\frac{3 a^{3/2} C \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right] \sqrt{\operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]}}{d} +$$

$$\frac{a^2 (8 A-3 C) \operatorname{Sin}[c+d x]}{3 d \sqrt{\operatorname{Cos}[c+d x]} \sqrt{a+a \operatorname{Sec}[c+d x]}} - \frac{a (2 A-3 C) \sqrt{a+a \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{3 d \sqrt{\operatorname{Cos}[c+d x]}} +$$

$$\frac{2 A \sqrt{\operatorname{Cos}[c+d x]} (a+a \operatorname{Sec}[c+d x])^{3/2} \operatorname{Sin}[c+d x]}{3 d}$$

Result (type 5, 207 leaves):

$$\frac{1}{3 d \sqrt{\operatorname{Cos}[c+d x]} (A+2 C+A \operatorname{Cos}[2(c+d x)])}$$

$$a (1+\operatorname{Cos}[c+d x]) (C+A \operatorname{Cos}[c+d x]^2) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^3 \sqrt{a(1+\operatorname{Sec}[c+d x])}$$

$$\left(-9 i C e^{\frac{1}{2} i(c+d x)} \operatorname{Cos}[c+d x] \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i(c+d x)}\right] -\right.$$

$$\left.3 i C e^{\frac{3}{2} i(c+d x)} \operatorname{Cos}[c+d x] \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i(c+d x)}\right] +\right.$$

$$\left.(A+3 C+10 A \operatorname{Cos}[c+d x]+A \operatorname{Cos}[2(c+d x)]) \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)$$

Problem 1140: Result unnecessarily involves higher level functions.

$$\int \sqrt{\operatorname{Cos}[c+d x]} (a+a \operatorname{Sec}[c+d x])^{3/2} (A+C \operatorname{Sec}[c+d x]^2) dx$$

Optimal (type 3, 191 leaves, 6 steps):

$$\frac{a^{3/2} (8 A+7 C) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right] \sqrt{\operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]}}{4 d} +$$

$$\frac{a^2 (8 A-5 C) \operatorname{Sin}[c+d x]}{4 d \sqrt{\operatorname{Cos}[c+d x]} \sqrt{a+a \operatorname{Sec}[c+d x]}} +$$

$$\frac{3 a C \sqrt{a+a \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{4 d \sqrt{\operatorname{Cos}[c+d x]}} + \frac{C (a+a \operatorname{Sec}[c+d x])^{3/2} \operatorname{Sin}[c+d x]}{2 d \sqrt{\operatorname{Cos}[c+d x]}}$$

Result (type 5, 224 leaves):



$$\frac{1}{12 d \cos [c+d x]^{3/2} (A+2 C+A \cos [2(c+d x)])}$$

$$a(1+\cos [c+d x])(C+A \cos [c+d x]^2) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^3 \sqrt{a(1+\operatorname{Sec}[c+d x])}$$

$$\left(-3 i(8 A+7 C) e^{\frac{1}{2} i(c+d x)} \cos [c+d x]^2 \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i(c+d x)}\right]-\right.$$

$$i(8 A+7 C) e^{\frac{3}{2} i(c+d x)} \cos [c+d x]^2 \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i(c+d x)}\right]+$$

$$\left.3(2 C+7 C \cos [c+d x]+8 A \cos [c+d x]^2) \sin \left[\frac{1}{2}(c+d x)\right]\right)$$

**Problem 1141: Result unnecessarily involves higher level functions.**

$$\int \frac{(a+a \operatorname{Sec}[c+d x])^{3/2} (A+C \operatorname{Sec}[c+d x]^2)}{\sqrt{\cos [c+d x]}} dx$$

Optimal (type 3, 191 leaves, 6 steps):

$$\frac{a^{3/2} (24 A+11 C) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right] \sqrt{\cos [c+d x]} \sqrt{\operatorname{Sec}[c+d x]}}{8 d} +$$

$$\frac{a^2 (24 A+19 C) \sin [c+d x]}{24 d \cos [c+d x]^{3/2} \sqrt{a+a \operatorname{Sec}[c+d x]}} +$$

$$\frac{a C \sqrt{a+a \operatorname{Sec}[c+d x]} \sin [c+d x]}{4 d \cos [c+d x]^{3/2}} + \frac{C(a+a \operatorname{Sec}[c+d x])^{3/2} \sin [c+d x]}{3 d \cos [c+d x]^{3/2}}$$

Result (type 5, 229 leaves):

$$\frac{1}{24 d \cos [c+d x]^{5/2} (A+2 C+A \cos [2(c+d x)])}$$

$$a(1+\cos [c+d x])(C+A \cos [c+d x]^2) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^3 \sqrt{a(1+\operatorname{Sec}[c+d x])}$$

$$\left(-3 i(24 A+11 C) e^{\frac{1}{2} i(c+d x)} \cos [c+d x]^3 \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i(c+d x)}\right]-\right.$$

$$i(24 A+11 C) e^{\frac{3}{2} i(c+d x)} \cos [c+d x]^3 \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i(c+d x)}\right]+$$

$$\left.(8 C+22 C \cos [c+d x]+3(8 A+11 C) \cos [c+d x]^2) \sin \left[\frac{1}{2}(c+d x)\right]\right)$$

**Problem 1142: Result unnecessarily involves higher level functions.**

$$\int \frac{(a+a \operatorname{Sec}[c+d x])^{3/2} (A+C \operatorname{Sec}[c+d x]^2)}{\cos [c+d x]^{3/2}} dx$$

Optimal (type 3, 238 leaves, 7 steps):

$$\frac{1}{64 d} a^{3/2} (112 A + 75 C) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c + d x]}{\sqrt{a + a \operatorname{Sec}[c + d x]}}\right] \sqrt{\operatorname{Cos}[c + d x]} \sqrt{\operatorname{Sec}[c + d x]} +$$

$$\frac{a^2 (16 A + 13 C) \operatorname{Sin}[c + d x]}{32 d \operatorname{Cos}[c + d x]^{5/2} \sqrt{a + a \operatorname{Sec}[c + d x]}} + \frac{a^2 (112 A + 75 C) \operatorname{Sin}[c + d x]}{64 d \operatorname{Cos}[c + d x]^{3/2} \sqrt{a + a \operatorname{Sec}[c + d x]}} +$$

$$\frac{a C \sqrt{a + a \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{8 d \operatorname{Cos}[c + d x]^{5/2}} + \frac{C (a + a \operatorname{Sec}[c + d x])^{3/2} \operatorname{Sin}[c + d x]}{4 d \operatorname{Cos}[c + d x]^{5/2}}$$

Result (type 5, 261 leaves):

$$\frac{1}{768 d \operatorname{Cos}[c + d x]^{7/2} (A + 2 C + A \operatorname{Cos}[2 (c + d x)])}$$

$$a (1 + \operatorname{Cos}[c + d x]) (C + A \operatorname{Cos}[c + d x]^2) \operatorname{Sec}\left[\frac{1}{2} (c + d x)\right]^3 \sqrt{a (1 + \operatorname{Sec}[c + d x])}$$

$$\left(-12 i (112 A + 75 C) e^{\frac{1}{2} i (c + d x)} \operatorname{Cos}[c + d x]^4 \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i (c + d x)}\right] -\right.$$

$$4 i (112 A + 75 C) e^{\frac{3}{2} i (c + d x)} \operatorname{Cos}[c + d x]^4 \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i (c + d x)}\right] +$$

$$3 (64 A + 164 C + 7 (48 A + 55 C) \operatorname{Cos}[c + d x] + 4 (16 A + 25 C) \operatorname{Cos}[2 (c + d x)] +$$

$$\left.112 A \operatorname{Cos}[3 (c + d x)] + 75 C \operatorname{Cos}[3 (c + d x)]\right) \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]$$

**Problem 1143: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + a \operatorname{Sec}[c + d x])^{3/2} (A + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Cos}[c + d x]^{5/2}} dx$$

Optimal (type 3, 285 leaves, 8 steps):

$$\frac{1}{128 d} a^{3/2} (176 A + 133 C) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c + d x]}{\sqrt{a + a \operatorname{Sec}[c + d x]}}\right] \sqrt{\operatorname{Cos}[c + d x]} \sqrt{\operatorname{Sec}[c + d x]} +$$

$$\frac{a^2 (80 A + 67 C) \operatorname{Sin}[c + d x]}{240 d \operatorname{Cos}[c + d x]^{7/2} \sqrt{a + a \operatorname{Sec}[c + d x]}} +$$

$$\frac{a^2 (176 A + 133 C) \operatorname{Sin}[c + d x]}{192 d \operatorname{Cos}[c + d x]^{5/2} \sqrt{a + a \operatorname{Sec}[c + d x]}} + \frac{a^2 (176 A + 133 C) \operatorname{Sin}[c + d x]}{128 d \operatorname{Cos}[c + d x]^{3/2} \sqrt{a + a \operatorname{Sec}[c + d x]}} +$$

$$\frac{3 a C \sqrt{a + a \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{40 d \operatorname{Cos}[c + d x]^{7/2}} + \frac{C (a + a \operatorname{Sec}[c + d x])^{3/2} \operatorname{Sin}[c + d x]}{5 d \operatorname{Cos}[c + d x]^{7/2}}$$

Result (type 5, 263 leaves):

$$\frac{1}{1920 d \cos [c+d x]^{9/2} (A+2 C+A \cos [2(c+d x)])} \\
 a (1+\cos [c+d x]) (C+A \cos [c+d x]^2) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^3 \sqrt{a(1+\operatorname{Sec}[c+d x])} \\
 \left(-15 i (176 A+133 C) e^{\frac{1}{2} i(c+d x)} \cos [c+d x]^5 \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i(c+d x)}\right] - \right. \\
 \left. 5 i (176 A+133 C) e^{\frac{3}{2} i(c+d x)} \cos [c+d x]^5 \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i(c+d x)}\right] + \right. \\
 \left. (384 C+912 C \cos [c+d x]+8(80 A+133 C) \cos [c+d x]^2 + \right. \\
 \left. 10(176 A+133 C) \cos [c+d x]^3 + 15(176 A+133 C) \cos [c+d x]^4) \sin \left[\frac{1}{2}(c+d x)\right]\right)$$

**Problem 1147: Result unnecessarily involves higher level functions.**

$$\int \cos [c+d x]^{7/2} (a+a \operatorname{Sec}[c+d x])^{5/2} (A+C \operatorname{Sec}[c+d x]^2) dx$$

Optimal (type 3, 230 leaves, 7 steps):

$$\frac{2 a^{5/2} C \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right] \sqrt{\cos [c+d x]} \sqrt{\operatorname{Sec}[c+d x]}}{d} + \\
 \frac{2 a^3 (32 A+49 C) \sin [c+d x]}{21 d \sqrt{\cos [c+d x]} \sqrt{a+a \operatorname{Sec}[c+d x]}} + \\
 \frac{2 a^2 (8 A+7 C) \sqrt{\cos [c+d x]} \sqrt{a+a \operatorname{Sec}[c+d x]} \sin [c+d x]}{21 d} + \\
 \frac{2 a A \cos [c+d x]^{3/2} (a+a \operatorname{Sec}[c+d x])^{3/2} \sin [c+d x]}{7 d} + \\
 \frac{2 A \cos [c+d x]^{5/2} (a+a \operatorname{Sec}[c+d x])^{5/2} \sin [c+d x]}{7 d}$$

Result (type 5, 297 leaves):

$$\left(C \cos [c+d x]^{9/2} \left(-2 i e^{\frac{1}{2} i(c+d x)} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i(c+d x)}\right] - \right. \right. \\
 \left. \left. \frac{2}{3} i e^{\frac{3}{2} i(c+d x)} \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i(c+d x)}\right]\right) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^5 \right. \\
 \left. (a(1+\operatorname{Sec}[c+d x]))^{5/2} (A+C \operatorname{Sec}[c+d x]^2)\right) / (2 d (A+2 C+A \cos [2 c+2 d x])) + \\
 \left(\cos [c+d x]^{9/2} \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^5 (a(1+\operatorname{Sec}[c+d x]))^{5/2} (A+C \operatorname{Sec}[c+d x]^2) \right. \\
 \left. \left(\frac{5}{8}(3 A+4 C) \sin \left[\frac{1}{2}(c+d x)\right] + \frac{1}{24}(11 A+4 C) \sin \left[\frac{3}{2}(c+d x)\right] + \right. \right. \\
 \left. \left. \frac{1}{8} A \sin \left[\frac{5}{2}(c+d x)\right] + \frac{1}{56} A \sin \left[\frac{7}{2}(c+d x)\right]\right)\right) / (d (A+2 C+A \cos [2 c+2 d x]))$$

**Problem 1148: Result unnecessarily involves higher level functions.**

$$\int \cos [c+d x]^{5 / 2}(a+a \sec [c+d x])^{5 / 2}(A+C \sec [c+d x])^2 d x$$

Optimal (type 3, 230 leaves, 7 steps):

$$\frac{5 a^{5 / 2} C \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan [c+d x]}{\sqrt{a+a \sec [c+d x]}}\right] \sqrt{\cos [c+d x]} \sqrt{\sec [c+d x]}}{d} +$$

$$\frac{a^3(64 A+15 C) \sin [c+d x]}{15 d \sqrt{\cos [c+d x]} \sqrt{a+a \sec [c+d x]}} - \frac{a^2(16 A-15 C) \sqrt{a+a \sec [c+d x]} \sin [c+d x]}{15 d \sqrt{\cos [c+d x]}} +$$

$$\frac{2 a A \sqrt{\cos [c+d x]}(a+a \sec [c+d x])^{3 / 2} \sin [c+d x]}{3 d} +$$

$$\frac{2 A \cos [c+d x]^{3 / 2}(a+a \sec [c+d x])^{5 / 2} \sin [c+d x]}{5 d}$$

Result (type 5, 230 leaves):

$$\frac{1}{60 d \sqrt{\cos [c+d x]}(A+2 C+A \cos [2(c+d x)])}$$

$$a^2(1+\cos [c+d x])^2(C+A \cos [c+d x])^2 \sec \left[\frac{1}{2}(c+d x)\right]^5 \sqrt{a(1+\sec [c+d x])}$$

$$\left(-150 i C e^{\frac{1}{2} i(c+d x)} \cos [c+d x] \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i(c+d x)}\right] -\right.$$

$$\left.50 i C e^{\frac{3}{2} i(c+d x)} \cos [c+d x] \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i(c+d x)}\right] + (28 A+30 C +\right.$$

$$\left.(181 A+60 C) \cos [c+d x]+28 A \cos [2(c+d x)]+3 A \cos [3(c+d x)]\right) \sin \left[\frac{1}{2}(c+d x)\right]$$

**Problem 1149: Result unnecessarily involves higher level functions.**

$$\int \cos [c+d x]^{3 / 2}(a+a \sec [c+d x])^{5 / 2}(A+C \sec [c+d x])^2 d x$$

Optimal (type 3, 244 leaves, 7 steps):

$$\frac{a^{5 / 2}(8 A+19 C) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan [c+d x]}{\sqrt{a+a \sec [c+d x]}}\right] \sqrt{\cos [c+d x]} \sqrt{\sec [c+d x]}}{4 d} +$$

$$\frac{a^3(56 A-27 C) \sin [c+d x]}{12 d \sqrt{\cos [c+d x]} \sqrt{a+a \sec [c+d x]}} - \frac{a^2(8 A-21 C) \sqrt{a+a \sec [c+d x]} \sin [c+d x]}{12 d \sqrt{\cos [c+d x]}} -$$

$$\frac{a(4 A-3 C)(a+a \sec [c+d x])^{3 / 2} \sin [c+d x]}{6 d \sqrt{\cos [c+d x]}} +$$

$$\frac{2 A \sqrt{\cos [c+d x]}(a+a \sec [c+d x])^{5 / 2} \sin [c+d x]}{3 d}$$

Result (type 5, 246 leaves):

$$\frac{1}{24 d \cos [c+d x]^{3/2} (A+2 C+A \cos [2(c+d x)])} \\ a^2 (1+\cos [c+d x])^2 (C+A \cos [c+d x])^2 \sec \left[ \frac{1}{2}(c+d x) \right]^5 \sqrt{a(1+\sec [c+d x])} \\ \left( -3 i (8 A+19 C) e^{\frac{1}{2} i(c+d x)} \cos [c+d x]^2 \operatorname{Hypergeometric2F1} \left[ \frac{1}{4}, 1, \frac{5}{4}, -e^{2 i(c+d x)} \right] - \right. \\ \left. i (8 A+19 C) e^{\frac{3}{2} i(c+d x)} \cos [c+d x]^2 \operatorname{Hypergeometric2F1} \left[ \frac{3}{4}, 1, \frac{7}{4}, -e^{2 i(c+d x)} \right] + (32 A+6 C + \right. \\ \left. (6 A+33 C) \cos [c+d x] + 32 A \cos [2(c+d x)] + 2 A \cos [3(c+d x)]) \sin \left[ \frac{1}{2}(c+d x) \right] \right)$$

**Problem 1150: Result unnecessarily involves higher level functions.**

$$\int \frac{\sqrt{\cos [c+d x]} (a+a \sec [c+d x])^{5/2} (A+C \sec [c+d x])^2}{dx}$$

Optimal (type 3, 238 leaves, 7 steps):

$$\frac{5 a^{5/2} (8 A+5 C) \operatorname{ArcSinh} \left[ \frac{-\sqrt{a} \tan [c+d x]}{\sqrt{a+a \sec [c+d x]}} \right] \sqrt{\cos [c+d x]} \sqrt{\sec [c+d x]}}{8 d} + \\ \frac{a^3 (24 A-49 C) \sin [c+d x]}{24 d \sqrt{\cos [c+d x]} \sqrt{a+a \sec [c+d x]}} + \frac{a^2 (24 A+31 C) \sqrt{a+a \sec [c+d x]} \sin [c+d x]}{24 d \sqrt{\cos [c+d x]}} + \\ \frac{5 a C (a+a \sec [c+d x])^{3/2} \sin [c+d x]}{12 d \sqrt{\cos [c+d x]}} + \frac{C (a+a \sec [c+d x])^{5/2} \sin [c+d x]}{3 d \sqrt{\cos [c+d x]}}$$

Result (type 5, 244 leaves):

$$\frac{1}{48 d \cos [c+d x]^{5/2} (A+2 C+A \cos [2(c+d x)])} \\ a^2 (1+\cos [c+d x])^2 (C+A \cos [c+d x])^2 \sec \left[ \frac{1}{2}(c+d x) \right]^5 \sqrt{a(1+\sec [c+d x])} \\ \left( -15 i (8 A+5 C) e^{\frac{1}{2} i(c+d x)} \cos [c+d x]^3 \operatorname{Hypergeometric2F1} \left[ \frac{1}{4}, 1, \frac{5}{4}, -e^{2 i(c+d x)} \right] - \right. \\ \left. 5 i (8 A+5 C) e^{\frac{3}{2} i(c+d x)} \cos [c+d x]^3 \operatorname{Hypergeometric2F1} \left[ \frac{3}{4}, 1, \frac{7}{4}, -e^{2 i(c+d x)} \right] + \right. \\ \left. (8 C+34 C \cos [c+d x] + 3 (8 A+25 C) \cos [c+d x]^2 + 48 A \cos [c+d x]^3) \sin \left[ \frac{1}{2}(c+d x) \right] \right)$$

**Problem 1151: Result unnecessarily involves higher level functions.**

$$\int \frac{(a+a \sec [c+d x])^{5/2} (A+C \sec [c+d x])^2}{\sqrt{\cos [c+d x]}} dx$$

Optimal (type 3, 238 leaves, 7 steps):

$$\frac{1}{64 d} a^{5/2} (304 A + 163 C) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c + d x]}{\sqrt{a + a \operatorname{Sec}[c + d x]}}\right] \sqrt{\operatorname{Cos}[c + d x]} \sqrt{\operatorname{Sec}[c + d x]} +$$

$$\frac{a^3 (432 A + 299 C) \operatorname{Sin}[c + d x]}{192 d \operatorname{Cos}[c + d x]^{3/2} \sqrt{a + a \operatorname{Sec}[c + d x]}} + \frac{a^2 (16 A + 17 C) \sqrt{a + a \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{32 d \operatorname{Cos}[c + d x]^{3/2}} +$$

$$\frac{5 a C (a + a \operatorname{Sec}[c + d x])^{3/2} \operatorname{Sin}[c + d x]}{24 d \operatorname{Cos}[c + d x]^{3/2}} + \frac{C (a + a \operatorname{Sec}[c + d x])^{5/2} \operatorname{Sin}[c + d x]}{4 d \operatorname{Cos}[c + d x]^{3/2}}$$

Result (type 5, 248 leaves):

$$\frac{1}{384 d \operatorname{Cos}[c + d x]^{7/2} (A + 2 C + A \operatorname{Cos}[2 (c + d x)])}$$

$$a^2 (1 + \operatorname{Cos}[c + d x])^2 (C + A \operatorname{Cos}[c + d x]^2) \operatorname{Sec}\left[\frac{1}{2} (c + d x)\right]^5 \sqrt{a (1 + \operatorname{Sec}[c + d x])}$$

$$\left(-3 i (304 A + 163 C) e^{\frac{1}{2} i (c + d x)} \operatorname{Cos}[c + d x]^4 \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i (c + d x)}\right] -\right.$$

$$i (304 A + 163 C) e^{\frac{3}{2} i (c + d x)} \operatorname{Cos}[c + d x]^4 \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i (c + d x)}\right] +$$

$$(48 C + 184 C \operatorname{Cos}[c + d x] + (96 A + 326 C) \operatorname{Cos}[c + d x]^2 + (528 A + 489 C) \operatorname{Cos}[c + d x]^3)$$

$$\left.\operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]\right)$$

Problem 1152: Result unnecessarily involves higher level functions.

$$\int \frac{(a + a \operatorname{Sec}[c + d x])^{5/2} (A + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Cos}[c + d x]^{3/2}} dx$$

Optimal (type 3, 285 leaves, 8 steps):

$$\frac{1}{128 d} a^{5/2} (400 A + 283 C) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c + d x]}{\sqrt{a + a \operatorname{Sec}[c + d x]}}\right] \sqrt{\operatorname{Cos}[c + d x]} \sqrt{\operatorname{Sec}[c + d x]} +$$

$$\frac{a^3 (1040 A + 787 C) \operatorname{Sin}[c + d x]}{960 d \operatorname{Cos}[c + d x]^{5/2} \sqrt{a + a \operatorname{Sec}[c + d x]}} + \frac{a^3 (400 A + 283 C) \operatorname{Sin}[c + d x]}{128 d \operatorname{Cos}[c + d x]^{3/2} \sqrt{a + a \operatorname{Sec}[c + d x]}} +$$

$$\frac{a^2 (80 A + 79 C) \sqrt{a + a \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{240 d \operatorname{Cos}[c + d x]^{5/2}} +$$

$$\frac{a C (a + a \operatorname{Sec}[c + d x])^{3/2} \operatorname{Sin}[c + d x]}{8 d \operatorname{Cos}[c + d x]^{5/2}} + \frac{C (a + a \operatorname{Sec}[c + d x])^{5/2} \operatorname{Sin}[c + d x]}{5 d \operatorname{Cos}[c + d x]^{5/2}}$$

Result (type 5, 267 leaves):

$$\frac{1}{3840 d \cos [c+d x]^{9/2} (A+2 C+A \cos [2(c+d x)])}$$

$$a^2 (1+\cos [c+d x])^2 (C+A \cos [c+d x]^2) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^5 \sqrt{a(1+\operatorname{Sec}[c+d x])}$$

$$\left(-15 i(400 A+283 C) e^{\frac{1}{2} i(c+d x)} \cos [c+d x]^5 \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i(c+d x)}\right] -\right.$$

$$5 i(400 A+283 C) e^{\frac{3}{2} i(c+d x)} \cos [c+d x]^5 \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i(c+d x)}\right] +$$

$$(384 C+1392 C \cos [c+d x]+8(80 A+283 C) \cos [c+d x]^2 +$$

$$\left.10(272 A+283 C) \cos [c+d x]^3+15(400 A+283 C) \cos [c+d x]^4\right) \sin\left[\frac{1}{2}(c+d x)\right]$$

**Problem 1153: Result unnecessarily involves higher level functions.**

$$\int \frac{(a+a \operatorname{Sec}[c+d x])^{5/2} (A+C \operatorname{Sec}[c+d x]^2)}{\cos [c+d x]^{5/2}} dx$$

Optimal (type 3, 332 leaves, 9 steps):

$$\frac{1}{512 d} a^{5/2} (1304 A+1015 C) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan [c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right] \sqrt{\cos [c+d x]} \sqrt{\operatorname{Sec}[c+d x]} +$$

$$\frac{a^3 (136 A+109 C) \sin [c+d x]}{192 d \cos [c+d x]^{7/2} \sqrt{a+a \operatorname{Sec}[c+d x]}} + \frac{a^3 (1304 A+1015 C) \sin [c+d x]}{768 d \cos [c+d x]^{5/2} \sqrt{a+a \operatorname{Sec}[c+d x]}} +$$

$$\frac{a^3 (1304 A+1015 C) \sin [c+d x]}{512 d \cos [c+d x]^{3/2} \sqrt{a+a \operatorname{Sec}[c+d x]}} + \frac{a^2 (24 A+23 C) \sqrt{a+a \operatorname{Sec}[c+d x]} \sin [c+d x]}{96 d \cos [c+d x]^{7/2}} +$$

$$\frac{a C (a+a \operatorname{Sec}[c+d x])^{3/2} \sin [c+d x]}{12 d \cos [c+d x]^{7/2}} + \frac{C (a+a \operatorname{Sec}[c+d x])^{5/2} \sin [c+d x]}{6 d \cos [c+d x]^{7/2}}$$

Result (type 5, 282 leaves):

$$\frac{1}{3072 d \cos [c+d x]^{11/2} (A+2 C+A \cos [2(c+d x)])}$$

$$a^2 (1+\cos [c+d x])^2 (C+A \cos [c+d x]^2) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^5 \sqrt{a(1+\operatorname{Sec}[c+d x])}$$

$$\left(-3 i(1304 A+1015 C) e^{\frac{1}{2} i(c+d x)} \cos [c+d x]^6 \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i(c+d x)}\right] -\right.$$

$$i(1304 A+1015 C) e^{\frac{3}{2} i(c+d x)} \cos [c+d x]^6 \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i(c+d x)}\right] +$$

$$(256 C+896 C \cos [c+d x]+48(8 A+29 C) \cos [c+d x]^2+8(184 A+203 C) \cos [c+d x]^3 +$$

$$\left.(2608 A+2030 C) \cos [c+d x]^4+(3912 A+3045 C) \cos [c+d x]^5\right) \sin\left[\frac{1}{2}(c+d x)\right]$$

**Problem 1164: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + C \operatorname{Sec}[c + dx]^2}{\sqrt{\operatorname{Cos}[c + dx]} (a + a \operatorname{Sec}[c + dx])^{3/2}} dx$$

Optimal (type 3, 185 leaves, 7 steps):

$$\frac{2 C \operatorname{ArcSinh}\left[\frac{-\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right] \sqrt{\operatorname{Cos}[c+dx]} \sqrt{\operatorname{Sec}[c+dx]}}{a^{3/2} d} + \frac{1}{2 \sqrt{2} a^{3/2} d}$$

$$\frac{(3 A - 5 C) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{\sqrt{2} \sqrt{a+a \operatorname{Sec}[c+dx]}}\right] \sqrt{\operatorname{Cos}[c+dx]} \sqrt{\operatorname{Sec}[c+dx]} - (A + C) \operatorname{Sin}[c+dx]}{2 d \operatorname{Cos}[c+dx]^{3/2} (a + a \operatorname{Sec}[c+dx])^{3/2}}$$

Result (type 3, 386 leaves):

$$-\left(\left(2 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] (C + A \operatorname{Cos}[c+dx]^2) \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{1+\operatorname{Cos}[c+dx]} \left(\sqrt{2}(3A-C) \operatorname{Log}[1+\operatorname{Cos}[c+dx]] + 8 C \operatorname{Log}\left[\sqrt{\operatorname{Cos}[c+dx]} (1+\operatorname{Cos}[c+dx])\right] - 2 \sqrt{2} C \operatorname{Log}\left[(1+\operatorname{Cos}[c+dx])^2\right] - 3 \sqrt{2} A \operatorname{Log}\left[2 \sqrt{1+\operatorname{Cos}[c+dx]} + \sqrt{2-2 \operatorname{Cos}[c+dx]^2}\right] + \sqrt{2} C \operatorname{Log}\left[2 \sqrt{1+\operatorname{Cos}[c+dx]} + \sqrt{2-2 \operatorname{Cos}[c+dx]^2}\right] - 8 C \operatorname{Log}\left[1+\operatorname{Cos}[c+dx] + \sqrt{1+\operatorname{Cos}[c+dx]} \sqrt{\operatorname{Sin}[c+dx]^2}\right] + 2 \sqrt{2} C \operatorname{Log}\left[3+2 \operatorname{Cos}[c+dx] - \operatorname{Cos}[c+dx]^2 + 2 \sqrt{2} \sqrt{1+\operatorname{Cos}[c+dx]} \sqrt{\operatorname{Sin}[c+dx]^2}\right]\right) + (A+C) \sqrt{\operatorname{Sin}[c+dx]^2}\right) / \left(a d \sqrt{\operatorname{Cos}[c+dx]} (1+\operatorname{Cos}[c+dx]) \sqrt{\operatorname{Sin}[c+dx]^2}\right) + (A+2 C+A \operatorname{Cos}[2(c+dx)]) \sqrt{a(1+\operatorname{Sec}[c+dx])} \sqrt{\operatorname{Sin}[c+dx]^2}\right)$$

**Problem 1165: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + C \operatorname{Sec}[c + dx]^2}{\operatorname{Cos}[c + dx]^{3/2} (a + a \operatorname{Sec}[c + dx])^{3/2}} dx$$

Optimal (type 3, 228 leaves, 8 steps):



$$\begin{aligned}
 & - \frac{3 C \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right] \sqrt{\operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]}}{a^{3/2} d} + \frac{1}{2 \sqrt{2} a^{3/2} d} \\
 & \frac{(A+9 C) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{\sqrt{2} \sqrt{a+a \operatorname{Sec}[c+d x]}}\right] \sqrt{\operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]} -}{\frac{(A+C) \operatorname{Sin}[c+d x]}{2 d \operatorname{Cos}[c+d x]^{5/2} (a+a \operatorname{Sec}[c+d x])^{3/2}} + \frac{(A+3 C) \operatorname{Sin}[c+d x]}{2 a d \operatorname{Cos}[c+d x]^{3/2} \sqrt{a+a \operatorname{Sec}[c+d x]}}}
 \end{aligned}$$

Result (type 3, 540 leaves):

$$\begin{aligned}
 & \left( \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^3 \sqrt{\operatorname{Cos}[c+d x]} (A+C \operatorname{Sec}[c+d x]^2) \left( 8 C \operatorname{Sec}[c+d x] \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] + \right. \right. \\
 & \quad \left. \left. 2 \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \left( A \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] + C \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right) \right) \right) / \\
 & \left( d (A+2 C+A \operatorname{Cos}[2 c+2 d x]) (a(1+\operatorname{Sec}[c+d x]))^{3/2} - \right. \\
 & \left. \left( \sqrt{2} (A+3 C) \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2 \sqrt{\operatorname{Cos}[c+d x]} \sqrt{1+\operatorname{Cos}[c+d x]} \right. \right. \\
 & \quad \left. \left( \operatorname{Log}[1+\operatorname{Cos}[c+d x]] - \operatorname{Log}\left[2 \sqrt{1+\operatorname{Cos}[c+d x]} + \sqrt{2-2 \operatorname{Cos}[c+d x]^2}\right] \right) \right. \\
 & \quad \left. (A+C \operatorname{Sec}[c+d x]^2) \operatorname{Sin}[c+d x] \right) / \\
 & \left( d \sqrt{1-\operatorname{Cos}[c+d x]^2} (A+2 C+A \operatorname{Cos}[2 c+2 d x]) (a(1+\operatorname{Sec}[c+d x]))^{3/2} \right) + \\
 & \left( 3 C \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2 \sqrt{\operatorname{Cos}[c+d x]} \sqrt{1+\operatorname{Cos}[c+d x]} \right. \\
 & \quad \left( -\sqrt{2} \operatorname{Log}\left[(1+\operatorname{Cos}[c+d x])^2\right] + 4 \operatorname{Log}\left[\sqrt{\operatorname{Cos}[c+d x]} + \operatorname{Cos}[c+d x]^{3/2}\right] - \right. \\
 & \quad \left. 4 \operatorname{Log}\left[1+\operatorname{Cos}[c+d x] + \sqrt{1+\operatorname{Cos}[c+d x]} \sqrt{1-\operatorname{Cos}[c+d x]^2}\right] + \right. \\
 & \quad \left. \left. \sqrt{2} \operatorname{Log}\left[3+2 \operatorname{Cos}[c+d x] - \operatorname{Cos}[c+d x]^2 + 2 \sqrt{2} \sqrt{1+\operatorname{Cos}[c+d x]} \sqrt{1-\operatorname{Cos}[c+d x]^2}\right] \right) \right. \\
 & \quad \left. (A+C \operatorname{Sec}[c+d x]^2) \operatorname{Sin}[c+d x] \right) / \\
 & \left( d \sqrt{1-\operatorname{Cos}[c+d x]^2} (A+2 C+A \operatorname{Cos}[2 c+2 d x]) (a(1+\operatorname{Sec}[c+d x]))^{3/2} \right)
 \end{aligned}$$

**Problem 1171: Result more than twice size of optimal antiderivative.**

$$\int \frac{A+C \operatorname{Sec}[c+d x]^2}{\operatorname{Cos}[c+d x]^{3/2} (a+a \operatorname{Sec}[c+d x])^{5/2}} dx$$

Optimal (type 3, 232 leaves, 8 steps):

$$\frac{2 C \operatorname{ArcSinh}\left[\frac{-\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right] \sqrt{\operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]}}{a^{5/2} d} + \frac{1}{16 \sqrt{2} a^{5/2} d}$$

$$\frac{(5 A-43 C) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{\sqrt{2} \sqrt{a+a \operatorname{Sec}[c+d x]}}\right] \sqrt{\operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]} - (A+C) \operatorname{Sin}[c+d x]}{4 d \operatorname{Cos}[c+d x]^{5/2} (a+a \operatorname{Sec}[c+d x])^{5/2}} + \frac{(5 A-11 C) \operatorname{Sin}[c+d x]}{16 a d \operatorname{Cos}[c+d x]^{3/2} (a+a \operatorname{Sec}[c+d x])^{3/2}}$$

Result (type 3, 563 leaves):

$$\left( \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^5 (A+C \operatorname{Sec}[c+d x]^2) \right. \\ \left. \left( \frac{1}{2} \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \left( 5 A \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] - 11 C \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right) + \right. \right. \\ \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^4 \left( -A \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] - C \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right) \right) \right) / \\ \left( d \sqrt{\operatorname{Cos}[c+d x]} (A+2 C+A \operatorname{Cos}[2 c+2 d x]) (a(1+\operatorname{Sec}[c+d x]))^{5/2} + \right. \\ \left. 1 \right) \\ 4 d (A+2 C+A \operatorname{Cos}[2 c+2 d x]) (a(1+\operatorname{Sec}[c+d x]))^{5/2} \\ \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^5 \sqrt{\operatorname{Sec}[c+d x]} (A+C \operatorname{Sec}[c+d x]^2) \\ \left( - \left( \left( \sqrt{2} (5 A-11 C) \sqrt{\operatorname{Cos}[c+d x]} \sqrt{1+\operatorname{Cos}[c+d x]} \right. \right. \right. \\ \left. \left. \left( \operatorname{Log}[1+\operatorname{Cos}[c+d x]] - \operatorname{Log}\left[2 \sqrt{1+\operatorname{Cos}[c+d x]} + \sqrt{2-2 \operatorname{Cos}[c+d x]^2}\right] \right) \right. \right. \\ \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right] \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x] \right) / \left( \sqrt{1-\operatorname{Cos}[c+d x]^2} \right) \right) - \\ \frac{1}{\sqrt{1-\operatorname{Cos}[c+d x]^2}} 16 C \sqrt{\operatorname{Cos}[c+d x]} \sqrt{1+\operatorname{Cos}[c+d x]} \\ \left( -\sqrt{2} \operatorname{Log}\left[\left(1+\operatorname{Cos}[c+d x]\right)^2\right] + 4 \operatorname{Log}\left[\sqrt{\operatorname{Cos}[c+d x]} + \operatorname{Cos}[c+d x]^{3/2}\right] - \right. \\ \left. 4 \operatorname{Log}\left[1+\operatorname{Cos}[c+d x] + \sqrt{1+\operatorname{Cos}[c+d x]} \sqrt{1-\operatorname{Cos}[c+d x]^2}\right] + \right. \\ \left. \sqrt{2} \operatorname{Log}\left[3+2 \operatorname{Cos}[c+d x] - \operatorname{Cos}[c+d x]^2 + 2 \sqrt{2} \sqrt{1+\operatorname{Cos}[c+d x]} \sqrt{1-\operatorname{Cos}[c+d x]^2}\right] \right) \\ \left. \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right] \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x] \right)$$

**Problem 1172: Result more than twice size of optimal antiderivative.**

$$\int \frac{A+C \operatorname{Sec}[c+d x]^2}{\operatorname{Cos}[c+d x]^{5/2} (a+a \operatorname{Sec}[c+d x])^{5/2}} dx$$

Optimal (type 3, 277 leaves, 9 steps):

$$\begin{aligned}
 & - \frac{5 C \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right] \sqrt{\operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]}}{a^{5/2} d} + \frac{1}{16 \sqrt{2} a^{5/2} d} \\
 & \frac{(3 A+115 C) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{\sqrt{2} \sqrt{a+a \operatorname{Sec}[c+d x]}}\right] \sqrt{\operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]} -}{\frac{(A+C) \operatorname{Sin}[c+d x]}{4 d \operatorname{Cos}[c+d x]^{7/2} (a+a \operatorname{Sec}[c+d x])^{5/2}} +} \\
 & \frac{(A-15 C) \operatorname{Sin}[c+d x]}{16 a d \operatorname{Cos}[c+d x]^{5/2} (a+a \operatorname{Sec}[c+d x])^{3/2}} + \frac{(3 A+35 C) \operatorname{Sin}[c+d x]}{16 a^2 d \operatorname{Cos}[c+d x]^{3/2} \sqrt{a+a \operatorname{Sec}[c+d x]}}
 \end{aligned}$$

Result (type 3, 580 leaves):

$$\begin{aligned}
 & \left( \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^5 (A+C \operatorname{Sec}[c+d x]^2) \left( 16 C \operatorname{Sec}[c+d x] \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] + \right. \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^4 \left( A \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] + C \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right) + \right. \\
 & \quad \left. \left. \frac{1}{2} \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \left( 3 A \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] + 19 C \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right) \right) \right) / \\
 & \frac{\left( d \sqrt{\operatorname{Cos}[c+d x]} (A+2 C+A \operatorname{Cos}[2 c+2 d x]) (a(1+\operatorname{Sec}[c+d x]))^{5/2} + 1}{4 d (A+2 C+A \operatorname{Cos}[2 c+2 d x]) (a(1+\operatorname{Sec}[c+d x]))^{5/2}} \right. \\
 & \left. \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^5 \sqrt{\operatorname{Sec}[c+d x]} (A+C \operatorname{Sec}[c+d x]^2) \right. \\
 & \left. \left( - \left( \left( \sqrt{2} (3 A+35 C) \sqrt{\operatorname{Cos}[c+d x]} \sqrt{1+\operatorname{Cos}[c+d x]} \right. \right. \right. \right. \\
 & \quad \left. \left. \left( \operatorname{Log}[1+\operatorname{Cos}[c+d x]] - \operatorname{Log}\left[2 \sqrt{1+\operatorname{Cos}[c+d x]} + \sqrt{2-2 \operatorname{Cos}[c+d x]^2}\right] \right) \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right] \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x] \right) / \left( \sqrt{1-\operatorname{Cos}[c+d x]^2} \right) \right) \right. \right. \\
 & \quad \left. \frac{1}{\sqrt{1-\operatorname{Cos}[c+d x]^2}} 40 C \sqrt{\operatorname{Cos}[c+d x]} \sqrt{1+\operatorname{Cos}[c+d x]} \right. \\
 & \quad \left( -\sqrt{2} \operatorname{Log}\left[\left(1+\operatorname{Cos}[c+d x]\right)^2\right] + 4 \operatorname{Log}\left[\sqrt{\operatorname{Cos}[c+d x]} + \operatorname{Cos}[c+d x]^{3/2}\right] - \right. \\
 & \quad \left. 4 \operatorname{Log}\left[1+\operatorname{Cos}[c+d x] + \sqrt{1+\operatorname{Cos}[c+d x]} \sqrt{1-\operatorname{Cos}[c+d x]^2}\right] + \right. \\
 & \quad \left. \left. \sqrt{2} \operatorname{Log}\left[3+2 \operatorname{Cos}[c+d x] - \operatorname{Cos}[c+d x]^2 + 2 \sqrt{2} \sqrt{1+\operatorname{Cos}[c+d x]} \sqrt{1-\operatorname{Cos}[c+d x]^2}\right] \right) \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right] \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x] \right) \right)
 \end{aligned}$$

**Problem 1182: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c+d x]^{3 / 2} (A+B \sec [c+d x]+C \sec [c+d x]^2) d x$$

Optimal (type 4, 65 leaves, 5 steps):

$$\frac{2 B \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{d} + \frac{2(A+3 C) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{3 d} + \frac{2 A \sqrt{\cos [c+d x]} \sin [c+d x]}{3 d}$$

Result (type 5, 682 leaves):

$$\left( \cos [c+d x]^{5 / 2} (A+B \sec [c+d x]+C \sec [c+d x]^2) \left( -\frac{4 B \cot [c]}{d} + \frac{4 A \cos [d x] \sin [c]}{3 d} + \frac{4 A \cos [c] \sin [d x]}{3 d} \right) \right) /$$

$$(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) -$$

$$\left( 4 A \cos [c+d x]^2 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right] \right.$$

$$\left. (A+B \sec [c+d x]+C \sec [c+d x]^2) \sec [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]]} \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \right) /$$

$$(3 d(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\cot [c]^2}) -$$

$$\left( 4 C \cos [c+d x]^2 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right] \right.$$

$$\left. (A+B \sec [c+d x]+C \sec [c+d x]^2) \sec [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]]} \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \right) /$$

$$(d(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\cot [c]^2}) -$$

$$\left( 2 B \cos [c+d x]^2 \operatorname{Csc}[c] \left( A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2 \right) \right.$$

$$\left. \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\},\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]\right]^2\right) \right.$$

$$\left. \left. \operatorname{Sin}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]\right) / \left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right. \right.$$

$$\left. \left. \sqrt{1+\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1+\operatorname{Tan}[c]^2} \right. \right.$$

$$\left. \left. \left. \left. \sqrt{1+\operatorname{Tan}[c]^2} \right) - \frac{\frac{\operatorname{Sin}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1+\operatorname{Tan}[c]^2}} + \frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1+\operatorname{Tan}[c]^2}}{\cos [c]^2+\operatorname{Sin}[c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1+\operatorname{Tan}[c]^2}} \right) \right) / \right.$$

$$\left. \left. \left( d \left( A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x] \right) \right) \right)$$

**Problem 1183: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sqrt{\cos [c+d x]} \left( A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2 \right) dx$$

Optimal (type 4, 61 leaves, 5 steps):

$$\frac{2(A-C) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{d} + \frac{2 B \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{d} + \frac{2 C \operatorname{Sin}[c+d x]}{d \sqrt{\cos [c+d x]}}$$

Result (type 5, 759 leaves):

$$\left( \cos [c+d x]^{5/2} \left( A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2 \right) \right.$$

$$\left. \left( -\frac{2(A-2 C+A \cos [2 c]) \operatorname{Csc}[c] \operatorname{Sec}[c]}{d} + \frac{4 C \operatorname{Sec}[c] \operatorname{Sec}[c+d x] \operatorname{Sin}[d x]}{d} \right) \right) /$$

$$\left( A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x] \right) -$$

$$\left( 4 B \cos [c+d x]^2 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2 \right)$$

$$\left( A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2 \right) \operatorname{Sec}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]$$

$$\begin{aligned}
 & \left. \begin{aligned}
 & \sqrt{1 - \sin [d x - \text{ArcTan}[\text{Cot}[c]]]} \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \sin [c] \sin [d x - \text{ArcTan}[\text{Cot}[c]]]} \\
 & \sqrt{1 + \sin [d x - \text{ArcTan}[\text{Cot}[c]]]} \Bigg) / \\
 & \left( d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \text{Cot}[c]^2} \right) - \\
 & \left( 2 A \cos [c + d x]^2 \text{Csc}[c] (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) \right. \\
 & \left. \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos [d x + \text{ArcTan}[\text{Tan}[c]]\right]^2\right] \right. \right. \\
 & \left. \left. \sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] \right) / \left( \sqrt{1 - \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \right. \right. \\
 & \left. \left. \sqrt{1 + \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \text{Tan}[c]^2} \right. \right. \\
 & \left. \left. \sqrt{1 + \text{Tan}[c]^2} \right) - \frac{\frac{\sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \text{Tan}[c]^2}} \right) / \\
 & \left( d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right) + \\
 & \left( 2 C \cos [c + d x]^2 \text{Csc}[c] (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) \right. \\
 & \left. \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos [d x + \text{ArcTan}[\text{Tan}[c]]\right]^2\right] \right. \right. \\
 & \left. \left. \sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] \right) / \left( \sqrt{1 - \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \right. \right. \\
 & \left. \left. \sqrt{1 + \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \text{Tan}[c]^2} \right. \right. \\
 & \left. \left. \sqrt{1 + \text{Tan}[c]^2} \right) - \frac{\frac{\sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \text{Tan}[c]^2}} \right) /
 \end{aligned}
 \end{aligned}$$

$$\left( \sqrt{1 + \tan[c]^2} \right) - \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \Bigg) /$$

$$(d (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]))$$

**Problem 1187: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c + d x]^{9/2} (a + a \sec[c + d x]) (A + B \sec[c + d x] + C \sec[c + d x]^2) dx$$

Optimal (type 4, 175 leaves, 8 steps):

$$\frac{2 a (7 A + 9 (B + C)) \text{EllipticE}\left[\frac{1}{2} (c + d x), 2\right]}{15 d} + \frac{2 a (5 (A + B) + 7 C) \text{EllipticF}\left[\frac{1}{2} (c + d x), 2\right]}{21 d} +$$

$$\frac{2 a (5 (A + B) + 7 C) \sqrt{\cos[c + d x]} \sin[c + d x]}{21 d} + \frac{2 a (7 A + 9 (B + C)) \cos[c + d x]^{3/2} \sin[c + d x]}{45 d} +$$

$$\frac{2 a (A + B) \cos[c + d x]^{5/2} \sin[c + d x]}{7 d} + \frac{2 a A \cos[c + d x]^{7/2} \sin[c + d x]}{9 d}$$

Result (type 5, 1292 leaves):

$$a \left( \sqrt{\cos[c + d x]} (1 + \cos[c + d x]) \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \right.$$

$$\left( - \frac{(7 A + 9 B + 9 C) \cot[c]}{15 d} + \frac{(23 A + 23 B + 28 C) \cos[d x] \sin[c]}{84 d} + \right.$$

$$\frac{(19 A + 18 B + 18 C) \cos[2 d x] \sin[2 c]}{180 d} + \frac{(A + B) \cos[3 d x] \sin[3 c]}{28 d} + \frac{A \cos[4 d x] \sin[4 c]}{72 d} +$$

$$\frac{(23 A + 23 B + 28 C) \cos[c] \sin[d x]}{84 d} + \frac{(19 A + 18 B + 18 C) \cos[2 c] \sin[2 d x]}{180 d} +$$

$$\left. \frac{(A + B) \cos[3 c] \sin[3 d x]}{28 d} + \frac{A \cos[4 c] \sin[4 d x]}{72 d} \right) -$$

$$\left( 5 A (1 + \cos[c + d x]) \csc[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[d x - \text{ArcTan}[\cot[c]]]^2\right] \right.$$

$$\left. \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \sec[d x - \text{ArcTan}[\cot[c]]] \sqrt{1 - \sin[d x - \text{ArcTan}[\cot[c]]]} \right.$$

$$\left. \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[d x - \text{ArcTan}[\cot[c]]]} \right)$$

$$\begin{aligned}
 & \left. \sqrt{1 + \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \right) / \left( 21 d \sqrt{1 + \text{Cot} [c]^2} \right) - \\
 & \left( 5 B (1 + \cos [c + d x]) \text{Csc} [c] \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \text{ArcTan} [\text{Cot} [c]]]^2 \right] \right. \\
 & \quad \text{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \text{Sec} [d x - \text{ArcTan} [\text{Cot} [c]]] \sqrt{1 - \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \\
 & \quad \sqrt{-\sqrt{1 + \text{Cot} [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \\
 & \quad \left. \left. \sqrt{1 + \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \right) / \left( 21 d \sqrt{1 + \text{Cot} [c]^2} \right) - \right. \\
 & \left( C (1 + \cos [c + d x]) \text{Csc} [c] \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \text{ArcTan} [\text{Cot} [c]]]^2 \right] \right. \\
 & \quad \text{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \text{Sec} [d x - \text{ArcTan} [\text{Cot} [c]]] \sqrt{1 - \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \\
 & \quad \left. \left. \sqrt{-\sqrt{1 + \text{Cot} [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \sqrt{1 + \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \right) / \right. \\
 & \left( 3 d \sqrt{1 + \text{Cot} [c]^2} \right) - \frac{1}{30 d} 7 A (1 + \cos [c + d x]) \text{Csc} [c] \text{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \\
 & \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \text{ArcTan} [\text{Tan} [c]]]^2 \right] \right. \\
 & \quad \left. \left. \sin [d x + \text{ArcTan} [\text{Tan} [c]]] \tan [c] \right) / \right. \\
 & \left( \sqrt{1 - \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \right. \\
 & \quad \left. \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2} \sqrt{1 + \tan [c]^2} \right) - \\
 & \left. \frac{\frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2}} \right) - \frac{1}{10 d}
 \end{aligned}$$



$$\begin{aligned}
 & 3 B (1 + \cos [c + d x]) \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \right. \right. \\
 & \quad \left. \left. \left\{\frac{3}{4}\right\}, \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]^2\right] \operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] \right) / \\
 & \left( \sqrt{1 - \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right. \\
 & \quad \left. \sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \operatorname{Tan}[c]^2} \sqrt{1 + \operatorname{Tan}[c]^2} \right) - \\
 & \left. \frac{\frac{\operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1 + \operatorname{Tan}[c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \operatorname{Tan}[c]^2}} \right) - \\
 & \frac{1}{10 d} 3 C (1 + \cos [c + d x]) \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \\
 & \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]^2\right] \right. \\
 & \quad \left. \operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] \right) / \\
 & \left( \sqrt{1 - \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right. \\
 & \quad \left. \sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \operatorname{Tan}[c]^2} \sqrt{1 + \operatorname{Tan}[c]^2} \right) - \\
 & \left. \frac{\frac{\operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1 + \operatorname{Tan}[c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \operatorname{Tan}[c]^2}} \right)
 \end{aligned}$$

**Problem 1188: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c + d x]^{7/2} (a + a \operatorname{Sec}[c + d x]) (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 4, 142 leaves, 7 steps):

$$\frac{2 a (3 (A+B) + 5 C) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 d} + \frac{2 a (5 A+7 (B+C)) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{21 d} + \frac{2 a (5 A+7 (B+C)) \sqrt{\cos [c+d x]} \sin [c+d x]}{21 d} + \frac{2 a (A+B) \cos [c+d x]^{3 / 2} \sin [c+d x]}{5 d} + \frac{2 a A \cos [c+d x]^{5 / 2} \sin [c+d x]}{7 d}$$

Result (type 5, 1240 leaves):

$$a \left( \sqrt{\cos [c+d x]} (1+\cos [c+d x]) \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \left( -\frac{(3 A+3 B+5 C) \cot [c]}{5 d} + \frac{(23 A+28 B+28 C) \cos [d x] \sin [c]}{84 d} + \frac{(A+B) \cos [2 d x] \sin [2 c]}{10 d} + \frac{A \cos [3 d x] \sin [3 c]}{28 d} + \frac{(23 A+28 B+28 C) \cos [c] \sin [d x]}{84 d} + \frac{(A+B) \cos [2 c] \sin [2 d x]}{10 d} + \frac{A \cos [3 c] \sin [3 d x]}{28 d} \right) - \left( 5 A (1+\cos [c+d x]) \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]\right]^2 \right) \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \operatorname{Sec}[d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]]} \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \right) / \left( 21 d \sqrt{1+\cot [c]^2} \right) - \left( B (1+\cos [c+d x]) \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]\right]^2 \right) \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \operatorname{Sec}[d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]]} \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \right) / \left( 3 d \sqrt{1+\cot [c]^2} \right) - \left( C (1+\cos [c+d x]) \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]\right]^2 \right) \right.$$

$$\begin{aligned}
 & \left. \begin{aligned}
 & \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \\
 & \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 + \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} } \Bigg) / \\
 & \left( 3d \sqrt{1 + \text{Cot}[c]^2} \right) - \frac{1}{10d} 3A (1 + \text{Cos}[c + dx]) \text{Csc}[c] \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \\
 & \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]]^2\right] \right) \\
 & \left. \begin{aligned}
 & \text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] \right) / \\
 & \left( \sqrt{1 - \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]]} \right. \\
 & \left. \sqrt{\text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \sqrt{1 + \text{Tan}[c]^2}} \right) - \\
 & \left. \frac{\frac{\text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \frac{2 \text{Cos}[c]^2 \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}}{\text{Cos}[c]^2 + \text{Sin}[c]^2}}{\sqrt{\text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}}} \right) - \frac{1}{10d} \\
 & 3B (1 + \text{Cos}[c + dx]) \text{Csc}[c] \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \right. \right. \\
 & \left. \left. \left\{\frac{3}{4}\right\}, \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]]^2\right] \text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] \right) / \\
 & \left( \sqrt{1 - \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]]} \right. \\
 & \left. \sqrt{\text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \sqrt{1 + \text{Tan}[c]^2}} \right) - \\
 & \left. \frac{\frac{\text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \frac{2 \text{Cos}[c]^2 \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}}{\text{Cos}[c]^2 + \text{Sin}[c]^2}}{\sqrt{\text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}}} \right) - \frac{1}{2d}
 \end{aligned}
 \end{aligned}$$

$$C (1 + \cos [c + d x]) \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \right.\right.$$

$$\left. \left. \frac{\cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]^2 \sin [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]] \operatorname{Tan}[c]}{\sqrt{1 - \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right.} \right.$$

$$\left. \left. \frac{\sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \operatorname{Tan}[c]^2} \sqrt{1 + \operatorname{Tan}[c]^2}}{\frac{\sin [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]] \operatorname{Tan}[c]}{\sqrt{1 + \operatorname{Tan}[c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]] \sqrt{1 + \operatorname{Tan}[c]^2}}{\cos [c]^2 + \sin [c]^2}} \right.} \right.$$

$$\left. \left. \frac{\sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \operatorname{Tan}[c]^2}}{\sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \operatorname{Tan}[c]^2}} \right) -$$

**Problem 1189: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c + d x]^{5/2} (a + a \operatorname{Sec}[c + d x]) (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 4, 106 leaves, 6 steps):

$$\frac{2 a (3 A + 5 (B + C)) \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), 2\right]}{5 d} + \frac{2 a (A + B + 3 C) \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), 2\right]}{3 d} +$$

$$\frac{2 a (A + B) \sqrt{\cos [c + d x]} \sin [c + d x]}{3 d} + \frac{2 a A \cos [c + d x]^{3/2} \sin [c + d x]}{5 d}$$

Result (type 5, 1186 leaves):

$$a \left( \sqrt{\cos [c + d x]} (1 + \cos [c + d x]) \right.$$

$$\operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \left( -\frac{(3 A + 5 B + 5 C) \operatorname{Cot}[c]}{5 d} + \frac{(A + B) \cos [d x] \sin [c]}{3 d} + \right.$$

$$\left. \frac{A \cos [2 d x] \sin [2 c]}{10 d} + \frac{(A + B) \cos [c] \sin [d x]}{3 d} + \frac{A \cos [2 c] \sin [2 d x]}{10 d} \right) -$$

$$\left( A (1 + \cos [c + d x]) \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2 \right] \right)$$

$$\begin{aligned}
 & \left( \frac{\sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sec[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \sin[dx - \text{ArcTan}[\text{Cot}[c]]]}}{\sqrt{-\sqrt{1 + \text{Cot}[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\text{Cot}[c]]]}} \right. \\
 & \left. \frac{\sqrt{1 + \sin[dx - \text{ArcTan}[\text{Cot}[c]]]}}{\left(3d\sqrt{1 + \text{Cot}[c]^2}\right)} - \right. \\
 & \left( B(1 + \cos[c + dx]) \text{Csc}[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\text{Cot}[c]]]^2\right] \right. \\
 & \left. \frac{\sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sec[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \sin[dx - \text{ArcTan}[\text{Cot}[c]]]}}{\sqrt{-\sqrt{1 + \text{Cot}[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 + \sin[dx - \text{ArcTan}[\text{Cot}[c]]]}} \right) / \\
 & \left(3d\sqrt{1 + \text{Cot}[c]^2}\right) - \frac{1}{d\sqrt{1 + \text{Cot}[c]^2}} C(1 + \cos[c + dx]) \text{Csc}[c] \\
 & \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\text{Cot}[c]]]^2\right] \\
 & \frac{\sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sec[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \sin[dx - \text{ArcTan}[\text{Cot}[c]]]}}{\sqrt{-\sqrt{1 + \text{Cot}[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 + \sin[dx - \text{ArcTan}[\text{Cot}[c]]]}} - \\
 & \frac{1}{10d} 3A(1 + \cos[c + dx]) \text{Csc}[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \\
 & \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos[dx + \text{ArcTan}[\text{Tan}[c]]]^2\right] \right. \\
 & \left. \frac{\sin[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 - \cos[dx + \text{ArcTan}[\text{Tan}[c]]]}} \right) / \left( \sqrt{1 + \cos[dx + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{\cos[c] \cos[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \tan[c]^2}} \right. \\
 & \left. \frac{\sqrt{1 + \tan[c]^2}}{\sqrt{1 + \tan[c]^2}} - \frac{\frac{\sin[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \tan[c]^2}}} \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{2d} B (1 + \cos [c + dx]) \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \right. \right. \\
 & \quad \left. \left. \left\{\frac{3}{4}\right\}, \cos [dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]]^2\right] \operatorname{Sin}[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] \right) / \\
 & \left( \sqrt{1 - \cos [dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \cos [dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right. \\
 & \quad \left. \sqrt{\cos [c] \cos [dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \operatorname{Tan}[c]^2} \sqrt{1 + \operatorname{Tan}[c]^2} \right) - \\
 & \left. \frac{\frac{\operatorname{Sin}[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1 + \operatorname{Tan}[c]^2}} + \frac{2 \cos [c]^2 \cos [dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}}{\cos [c]^2 + \operatorname{Sin}[c]^2}}{\sqrt{\cos [c] \cos [dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \operatorname{Tan}[c]^2}} \right) - \frac{1}{2d} \\
 & C (1 + \cos [c + dx]) \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \right. \right. \\
 & \quad \left. \left. \cos [dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]]^2\right] \operatorname{Sin}[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] \right) / \\
 & \left( \sqrt{1 - \cos [dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \cos [dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right. \\
 & \quad \left. \sqrt{\cos [c] \cos [dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \operatorname{Tan}[c]^2} \sqrt{1 + \operatorname{Tan}[c]^2} \right) - \\
 & \left. \frac{\frac{\operatorname{Sin}[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1 + \operatorname{Tan}[c]^2}} + \frac{2 \cos [c]^2 \cos [dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}}{\cos [c]^2 + \operatorname{Sin}[c]^2}}{\sqrt{\cos [c] \cos [dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \operatorname{Tan}[c]^2}} \right)
 \end{aligned}$$

**Problem 1190: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c + dx]^{3/2} (a + a \operatorname{Sec}[c + dx]) (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) dx$$

Optimal (type 4, 98 leaves, 6 steps):

$$\frac{2 a (A+B-C) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{d} + \frac{2 a (A+3(B+C)) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{3 d} +$$

$$\frac{2 a C \sin [c+d x]}{d \sqrt{\cos [c+d x]}} + \frac{2 a A \sqrt{\cos [c+d x]} \sin [c+d x]}{3 d}$$

Result (type 5, 1173 leaves):

$$a \left( \sqrt{\cos [c+d x]} (1+\cos [c+d x]) \right.$$

$$\left. \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \left( -\frac{(A+B-2 C+A \cos [2 c]+B \cos [2 c]) \operatorname{Csc}[c] \operatorname{Sec}[c]}{2 d} + \right. \right.$$

$$\left. \left. \frac{A \cos [d x] \sin [c]}{3 d} + \frac{A \cos [c] \sin [d x]}{3 d} + \frac{C \operatorname{Sec}[c] \operatorname{Sec}[c+d x] \sin [d x]}{d} \right) - \right.$$

$$\left( A(1+\cos [c+d x]) \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2 \right.$$

$$\left. \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \operatorname{Sec}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right.$$

$$\left. \sqrt{-\sqrt{1+\operatorname{Cot}[c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1+\sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) /$$

$$\left( 3 d \sqrt{1+\operatorname{Cot}[c]^2} \right) - \frac{1}{d \sqrt{1+\operatorname{Cot}[c]^2}} B(1+\cos [c+d x]) \operatorname{Csc}[c]$$

$$\operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2$$

$$\operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \operatorname{Sec}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right.$$

$$\left. \sqrt{-\sqrt{1+\operatorname{Cot}[c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right.$$

$$\left. \sqrt{1+\sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} - \frac{1}{d \sqrt{1+\operatorname{Cot}[c]^2}} \right.$$

$$C(1+\cos [c+d x]) \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2$$

$$\operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \operatorname{Sec}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right.$$

$$\left. \sqrt{-\sqrt{1+\operatorname{Cot}[c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1+\sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} - \right.$$

$$\left. \frac{1}{2 d} A(1+\cos [c+d x]) \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \right)$$

$$\left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right]^2\right] \right.$$

$$\left. \frac{\sin\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right] \text{Tan}[c]}{\sqrt{1 - \cos\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right]}} \right)$$

$$\sqrt{1 + \cos\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right]} \sqrt{\cos[c] \cos\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right]} \sqrt{1 + \text{Tan}[c]^2}$$

$$\left. \frac{\sqrt{1 + \text{Tan}[c]^2} \left( \frac{\sin\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \frac{2 \cos[c]^2 \cos\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right] \sqrt{1 + \text{Tan}[c]^2}}{\cos[c]^2 + \sin[c]^2} \right)}{\sqrt{\cos[c] \cos\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right]} \sqrt{1 + \text{Tan}[c]^2}} \right) -$$

$$\frac{1}{2d} B \left(1 + \cos[c + d x]\right) \text{Csc}[c] \text{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \right. \right.$$

$$\left. \left. \left\{\frac{3}{4}\right\}, \cos\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right]^2\right] \frac{\sin\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right] \text{Tan}[c]}{\sqrt{1 - \cos\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right]}} \right)$$

$$\left( \frac{\sqrt{1 - \cos\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right]} \sqrt{1 + \cos\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right]}}{\sqrt{\cos[c] \cos\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right]} \sqrt{1 + \text{Tan}[c]^2}} \sqrt{1 + \text{Tan}[c]^2} \right) -$$

$$\left. \frac{\frac{\sin\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \frac{2 \cos[c]^2 \cos\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right] \sqrt{1 + \text{Tan}[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right]} \sqrt{1 + \text{Tan}[c]^2}} \right) + \frac{1}{2d}$$

$$C \left(1 + \cos[c + d x]\right) \text{Csc}[c] \text{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \right. \right.$$

$$\left. \left. \cos\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right]^2\right] \frac{\sin\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right] \text{Tan}[c]}{\sqrt{1 - \cos\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right]}} \right)$$

$$\left( \frac{\sqrt{1 - \cos\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right]} \sqrt{1 + \cos\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right]}}{\sqrt{\cos[c] \cos\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right]} \sqrt{1 + \text{Tan}[c]^2}} \right)$$



$$\left( \sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]]} \sqrt{1 + \tan[c]^2} \sqrt{1 + \tan[c]^2} \right) - \left( \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]]} \sqrt{1 + \tan[c]^2}} \right)$$

**Problem 1191: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sqrt{\cos[c + d x]} (a + a \sec[c + d x]) (A + B \sec[c + d x] + C \sec[c + d x]^2) dx$$

Optimal (type 4, 103 leaves, 6 steps):

$$\frac{2 a (A - B - C) \text{EllipticE}\left[\frac{1}{2} (c + d x), 2\right]}{d} + \frac{2 a (3 A + 3 B + C) \text{EllipticF}\left[\frac{1}{2} (c + d x), 2\right]}{3 d} + \frac{2 a C \sin[c + d x]}{3 d \cos[c + d x]^{3/2}} + \frac{2 a (B + C) \sin[c + d x]}{d \sqrt{\cos[c + d x]}}$$

Result (type 5, 1180 leaves):

$$a \left( \sqrt{\cos[c + d x]} \left( 1 + \cos[c + d x] \right) \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \right. \\ \left( - \frac{(A - 2 B - 2 C + A \cos[2 c]) \csc[c] \sec[c]}{2 d} + \frac{C \sec[c] \sec[c + d x]^2 \sin[d x]}{3 d} + \frac{\sec[c] \sec[c + d x] (C \sin[c] + 3 B \sin[d x] + 3 C \sin[d x])}{3 d} \right) - \frac{1}{d \sqrt{1 + \cot[c]^2}} \\ A (1 + \cos[c + d x]) \csc[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[d x - \text{ArcTan}[\cot[c]]]\right]^2 \\ \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \sec[d x - \text{ArcTan}[\cot[c]]] \sqrt{1 - \sin[d x - \text{ArcTan}[\cot[c]]]} \\ \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[d x - \text{ArcTan}[\cot[c]]]} \\ \sqrt{1 + \sin[d x - \text{ArcTan}[\cot[c]]]} - \frac{1}{d \sqrt{1 + \cot[c]^2}} \\ B (1 + \cos[c + d x]) \csc[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[d x - \text{ArcTan}[\cot[c]]]\right]^2 \\ \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \sec[d x - \text{ArcTan}[\cot[c]]] \sqrt{1 - \sin[d x - \text{ArcTan}[\cot[c]]]} \right)$$

$$\begin{aligned}
 & \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]]} \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} - \\
 & \left( C(1+\cos [c+d x]) \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \operatorname{Sec}[d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \right. \\
 & \quad \left. \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]]} \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \right) / \\
 & \left( 3 d \sqrt{1+\cot [c]^2} \right) - \frac{1}{2 d} A(1+\cos [c+d x]) \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \\
 & \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\tan [c]]]^2\right] \right. \\
 & \quad \left. \sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c] \right) / \left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \right. \\
 & \quad \left. \sqrt{1+\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2} \right. \\
 & \quad \left. \sqrt{1+\tan [c]^2} \right) - \frac{\frac{\sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}{\cos [c]^2+\sin [c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2}} \Bigg) + \\
 & \frac{1}{2 d} B(1+\cos [c+d x]) \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\}, \right. \right. \\
 & \quad \left. \left. \left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\tan [c]]]^2\right] \sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c] \right) / \\
 & \left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \right. \\
 & \quad \left. \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2} \sqrt{1+\tan [c]^2} \right) -
 \end{aligned}$$

$$\left. \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}}} + \frac{1}{2 d} \right)$$

$$C (1 + \cos[c + d x]) \csc[c] \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \right. \right.$$

$$\left. \left. \frac{\cos[d x + \text{ArcTan}[\tan[c]]]^2 \sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 - \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \cos[d x + \text{ArcTan}[\tan[c]]]}} \right. \right.$$

$$\left. \left. \frac{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}} \sqrt{1 + \tan[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \right) - \right.$$

$$\left. \left. \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \right) \right)$$

**Problem 1192: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \sec[c + d x]) (A + B \sec[c + d x] + C \sec[c + d x]^2)}{\sqrt{\cos[c + d x]}} dx$$

Optimal (type 4, 141 leaves, 7 steps):

$$-\frac{2 a (5 A + 5 B + 3 C) \text{EllipticE}\left[\frac{1}{2} (c + d x), 2\right]}{5 d} + \frac{2 a (3 A + B + C) \text{EllipticF}\left[\frac{1}{2} (c + d x), 2\right]}{3 d} +$$

$$\frac{2 a C \sin[c + d x]}{5 d \cos[c + d x]^{5/2}} + \frac{2 a (B + C) \sin[c + d x]}{3 d \cos[c + d x]^{3/2}} + \frac{2 a (5 A + 5 B + 3 C) \sin[c + d x]}{5 d \sqrt{\cos[c + d x]}}$$

Result (type 5, 1228 leaves):

$$a \left( \sqrt{\cos[c + d x]} (1 + \cos[c + d x]) \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \right.$$

$$\left. \left( \frac{(5 A + 5 B + 3 C) \csc[c] \sec[c]}{5 d} + \frac{C \sec[c] \sec[c + d x]^3 \sin[d x]}{5 d} \right) \right.$$

$$\begin{aligned}
 & \frac{\text{Sec}[c] \text{Sec}[c+dx]^2 (3C \text{Sin}[c] + 5B \text{Sin}[dx] + 5C \text{Sin}[dx])}{15d} + \frac{1}{15d} \text{Sec}[c] \text{Sec}[c+dx] \\
 & \left. \left( 5B \text{Sin}[c] + 5C \text{Sin}[c] + 15A \text{Sin}[dx] + 15B \text{Sin}[dx] + 9C \text{Sin}[dx] \right) \right) - \frac{1}{d \sqrt{1+\text{Cot}[c]^2}} \\
 & A (1+\text{Cos}[c+dx]) \text{Csc}[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]\right]^2 \\
 & \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \\
 & \sqrt{-\sqrt{1+\text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1+\text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]}} - \\
 & \left( B (1+\text{Cos}[c+dx]) \text{Csc}[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]\right]^2 \right. \\
 & \left. \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right. \\
 & \left. \sqrt{-\sqrt{1+\text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right. \\
 & \left. \sqrt{1+\text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right) / \left( 3d \sqrt{1+\text{Cot}[c]^2} \right) - \\
 & \left( C (1+\text{Cos}[c+dx]) \text{Csc}[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]\right]^2 \right. \\
 & \left. \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right. \\
 & \left. \sqrt{-\sqrt{1+\text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1+\text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]}} \right) / \\
 & \left( 3d \sqrt{1+\text{Cot}[c]^2} \right) + \frac{1}{2d} A (1+\text{Cos}[c+dx]) \text{Csc}[c] \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \\
 & \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]]\right]^2 \right. \\
 & \left. \text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] \right) / \\
 & \left( \sqrt{1 - \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]]} \right. \\
 & \left. \sqrt{\text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \sqrt{1 + \text{Tan}[c]^2}} \right) -
 \end{aligned}$$

$$\left. \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}}} \right) + \frac{1}{2 d}$$

$$B (1 + \cos[c + d x]) \csc[c] \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \right. \right.$$

$$\left. \left. \frac{\cos[d x + \text{ArcTan}[\tan[c]]]^2 \sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 - \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \cos[d x + \text{ArcTan}[\tan[c]]]}} \right. \right.$$

$$\left. \left. \frac{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}} \sqrt{1 + \tan[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \right) -$$

$$\left. \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \right) + \frac{1}{10 d}$$

$$3 C (1 + \cos[c + d x]) \csc[c] \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \right. \right.$$

$$\left. \left. \left\{\frac{3}{4}\right\}, \frac{\cos[d x + \text{ArcTan}[\tan[c]]]^2 \sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 - \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \cos[d x + \text{ArcTan}[\tan[c]]]}} \right. \right.$$

$$\left. \left. \frac{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}} \sqrt{1 + \tan[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \right) -$$

$$\left. \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \right)$$

Problem 1193: Result unnecessarily involves higher level functions and more

than twice size of optimal antiderivative.

$$\int \frac{(a + a \operatorname{Sec}[c + d x]) (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Cos}[c + d x]^{3/2}} dx$$

Optimal (type 4, 177 leaves, 8 steps):

$$\begin{aligned} & - \frac{2 a (5 A + 3 (B + C)) \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{5 d} + \\ & \frac{2 a (7 A + 7 B + 5 C) \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{21 d} + \frac{2 a C \operatorname{Sin}[c + d x]}{7 d \operatorname{Cos}[c + d x]^{7/2}} + \\ & \frac{2 a (B + C) \operatorname{Sin}[c + d x]}{5 d \operatorname{Cos}[c + d x]^{5/2}} + \frac{2 a (7 A + 7 B + 5 C) \operatorname{Sin}[c + d x]}{21 d \operatorname{Cos}[c + d x]^{3/2}} + \frac{2 a (5 A + 3 (B + C)) \operatorname{Sin}[c + d x]}{5 d \sqrt{\operatorname{Cos}[c + d x]}} \end{aligned}$$

Result (type 5, 1284 leaves):

$$\begin{aligned} & a \left( \sqrt{\operatorname{Cos}[c + d x]} (1 + \operatorname{Cos}[c + d x]) \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \right. \\ & \left( \frac{(5 A + 3 B + 3 C) \operatorname{Csc}[c] \operatorname{Sec}[c]}{5 d} + \frac{C \operatorname{Sec}[c] \operatorname{Sec}[c + d x]^4 \operatorname{Sin}[d x]}{7 d} + \right. \\ & \left. \frac{\operatorname{Sec}[c] \operatorname{Sec}[c + d x]^3 (5 C \operatorname{Sin}[c] + 7 B \operatorname{Sin}[d x] + 7 C \operatorname{Sin}[d x])}{35 d} + \frac{1}{105 d} \right. \\ & \left. \operatorname{Sec}[c] \operatorname{Sec}[c + d x]^2 (21 B \operatorname{Sin}[c] + 21 C \operatorname{Sin}[c] + 35 A \operatorname{Sin}[d x] + \right. \\ & \left. 35 B \operatorname{Sin}[d x] + 25 C \operatorname{Sin}[d x]) + \frac{1}{105 d} \operatorname{Sec}[c] \operatorname{Sec}[c + d x] \right. \\ & \left. \left. (35 A \operatorname{Sin}[c] + 35 B \operatorname{Sin}[c] + 25 C \operatorname{Sin}[c] + 105 A \operatorname{Sin}[d x] + 63 B \operatorname{Sin}[d x] + 63 C \operatorname{Sin}[d x]) \right) \right) - \\ & \left( A (1 + \operatorname{Cos}[c + d x]) \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2 \right. \\ & \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right. \\ & \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right. \\ & \left. \left. \sqrt{1 + \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) \right) / \left( 3 d \sqrt{1 + \operatorname{Cot}[c]^2} \right) - \\ & \left( B (1 + \operatorname{Cos}[c + d x]) \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2 \right. \\ & \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{\sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]} \sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]}}{3d \sqrt{1+\cot[c]^2}} - \right. \\
 & \left. \left( 5C(1+\cos[c+dx]) \text{Csc}[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\cot[c]]]^2\right]\right) \right. \\
 & \left. \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \text{Sec}[dx - \text{ArcTan}[\cot[c]]] \sqrt{1-\sin[dx - \text{ArcTan}[\cot[c]]]} \right. \\
 & \left. \sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]} \sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]} \right) / \\
 & \left( 21d \sqrt{1+\cot[c]^2} + \frac{1}{2d} A(1+\cos[c+dx]) \text{Csc}[c] \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \right. \\
 & \left. \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos[dx + \text{ArcTan}[\tan[c]]]^2\right]\right) \right. \\
 & \left. \left. \sin[dx + \text{ArcTan}[\tan[c]]] \tan[c] \right) / \right. \\
 & \left( \sqrt{1-\cos[dx + \text{ArcTan}[\tan[c]]]} \sqrt{1+\cos[dx + \text{ArcTan}[\tan[c]]]} \right. \\
 & \left. \sqrt{\cos[c] \cos[dx + \text{ArcTan}[\tan[c]]]} \sqrt{1+\tan[c]^2} \sqrt{1+\tan[c]^2} \right) - \\
 & \left. \frac{\frac{\sin[dx + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1+\tan[c]^2}} + \frac{2\cos[c]^2 \cos[dx + \text{ArcTan}[\tan[c]]] \sqrt{1+\tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[dx + \text{ArcTan}[\tan[c]]]} \sqrt{1+\tan[c]^2}} \right) + \frac{1}{10d} \\
 & 3B(1+\cos[c+dx]) \text{Csc}[c] \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \right. \right. \\
 & \left. \left. \left\{\frac{3}{4}\right\}, \cos[dx + \text{ArcTan}[\tan[c]]]^2\right]\right) \sin[dx + \text{ArcTan}[\tan[c]]] \tan[c] \right) / \\
 & \left( \sqrt{1-\cos[dx + \text{ArcTan}[\tan[c]]]} \sqrt{1+\cos[dx + \text{ArcTan}[\tan[c]]]} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]]} \sqrt{1 + \tan[c]^2} \sqrt{1 + \tan[c]^2} \right) - \\
 & \left( \frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2} \right) + \\
 & \left( \sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]]} \sqrt{1 + \tan[c]^2} \right) \\
 & \frac{1}{10 d} 3 C (1 + \cos[c + d x]) \text{Csc}[c] \text{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \\
 & \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos[d x + \text{ArcTan}[\tan[c]]]^2\right] \right) \\
 & \left( \frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 - \cos[d x + \text{ArcTan}[\tan[c]]]} \sqrt{1 + \cos[d x + \text{ArcTan}[\tan[c]]]} \right) \\
 & \left( \sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]]} \sqrt{1 + \tan[c]^2} \sqrt{1 + \tan[c]^2} \right) - \\
 & \left( \frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2} \right)
 \end{aligned}$$

**Problem 1194: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c + d x]^{11/2} (a + a \text{Sec}[c + d x])^2 (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) dx$$

Optimal (type 4, 251 leaves, 10 steps):



$$\begin{aligned}
 & \frac{4 a^2 (7 A+8 B+9 C) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{15 d} + \frac{4 a^2 (50 A+55 B+66 C) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{231 d} + \\
 & \frac{4 a^2 (50 A+55 B+66 C) \sqrt{\cos [c+d x]} \sin [c+d x]}{231 d} + \\
 & \frac{4 a^2 (7 A+8 B+9 C) \cos [c+d x]^{3 / 2} \sin [c+d x]}{45 d} + \\
 & \frac{2 a^2 (89 A+121 B+99 C) \cos [c+d x]^{5 / 2} \sin [c+d x]}{693 d} + \\
 & \frac{2 A \cos [c+d x]^{5 / 2} (a+a \cos [c+d x])^2 \sin [c+d x]}{11 d} + \\
 & \frac{2 (4 A+11 B) \cos [c+d x]^{5 / 2} (a^2+a^2 \cos [c+d x]) \sin [c+d x]}{99 d}
 \end{aligned}$$

Result (type 5, 1364 leaves):

$$\begin{aligned}
 & a^2 \left( \sqrt{\cos [c+d x]} (1+\cos [c+d x])^2 \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 \right. \\
 & \left( -\frac{(7 A+8 B+9 C) \cot [c]}{15 d} + \frac{(941 A+1012 B+1122 C) \cos [d x] \sin [c]}{3696 d} + \right. \\
 & \frac{(38 A+37 B+36 C) \cos [2 d x] \sin [2 c]}{360 d} + \frac{(101 A+88 B+44 C) \cos [3 d x] \sin [3 c]}{2464 d} + \\
 & \frac{(2 A+B) \cos [4 d x] \sin [4 c]}{144 d} + \frac{A \cos [5 d x] \sin [5 c]}{352 d} + \\
 & \frac{(941 A+1012 B+1122 C) \cos [c] \sin [d x]}{3696 d} + \frac{(38 A+37 B+36 C) \cos [2 c] \sin [2 d x]}{360 d} + \\
 & \frac{(101 A+88 B+44 C) \cos [3 c] \sin [3 d x]}{2464 d} + \\
 & \left. \left. \frac{(2 A+B) \cos [4 c] \sin [4 d x]}{144 d} + \frac{A \cos [5 c] \sin [5 d x]}{352 d} \right) - \right. \\
 & \left. \left( 50 A (1+\cos [c+d x])^2 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]\right]^2\right] \right. \right. \\
 & \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 \operatorname{Sec}[d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \\
 & \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]]} \\
 & \left. \left. \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]}\right) / \left( 231 d \sqrt{1+\cot [c]^2} \right) - \right.
 \end{aligned}$$

$$\left( 5 B (1 + \cos [c + d x])^2 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2 \right. \\ \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^4 \operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right. \\ \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right. \\ \left. \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) / \left( 21 d \sqrt{1 + \operatorname{Cot}[c]^2} \right) -$$

$$\left( 2 C (1 + \cos [c + d x])^2 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2 \right. \\ \left. \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^4 \operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right. \\ \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) /$$

$$\left( 7 d \sqrt{1 + \operatorname{Cot}[c]^2} \right) - \frac{1}{30 d} 7 A (1 + \cos [c + d x])^2 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^4$$

$$\left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]\right]^2 \right.$$

$$\left. \sin [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] \right) /$$

$$\left( \sqrt{1 - \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right.$$

$$\left. \sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \operatorname{Tan}[c]^2} \sqrt{1 + \operatorname{Tan}[c]^2} \right) -$$

$$\left( \frac{\frac{\sin [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1 + \operatorname{Tan}[c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \operatorname{Tan}[c]^2}} \right) - \frac{1}{15 d}$$

$$4 B (1 + \cos [c + d x])^2 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^4 \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \right.$$

$$\left\{ \frac{3}{4}, \cos [d x + \text{ArcTan} [\text{Tan} [c]]]^2 \sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c] \right\} /$$

$$\left( \sqrt{1 - \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \right.$$

$$\left. \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \text{Tan} [c]^2} \sqrt{1 + \text{Tan} [c]^2} \right) -$$

$$\frac{\frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 + \text{Tan} [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \sqrt{1 + \text{Tan} [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \text{Tan} [c]^2}} \right) -$$

$$\frac{1}{10 d} 3 C (1 + \cos [c + d x])^2 \text{Csc} [c] \text{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^4$$

$$\left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \text{ArcTan} [\text{Tan} [c]]]^2 \right] \right.$$

$$\left. \sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c] \right) /$$

$$\left( \sqrt{1 - \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \right.$$

$$\left. \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \text{Tan} [c]^2} \sqrt{1 + \text{Tan} [c]^2} \right) -$$

$$\frac{\frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 + \text{Tan} [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \sqrt{1 + \text{Tan} [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \text{Tan} [c]^2}} \right)$$

**Problem 1195: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c + d x]^{9/2} (a + a \sec [c + d x])^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 4, 215 leaves, 9 steps):

$$\frac{4 a^2 (8 A+9 B+12 C) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{15 d} +$$

$$\frac{4 a^2 (5 A+6 B+7 C) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{21 d} + \frac{4 a^2 (5 A+6 B+7 C) \sqrt{\cos [c+d x]} \sin [c+d x]}{21 d} +$$

$$\frac{2 a^2 (19 A+27 B+21 C) \cos [c+d x]^{3 / 2} \sin [c+d x]}{105 d} +$$

$$\frac{2 A \cos [c+d x]^{3 / 2}(a+a \cos [c+d x])^2 \sin [c+d x]}{9 d} +$$

$$\frac{2(4 A+9 B) \cos [c+d x]^{3 / 2}\left(a^2+a^2 \cos [c+d x]\right) \sin [c+d x]}{63 d}$$

Result (type 5, 1699 leaves):

$$\frac{1}{A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]}$$

$$\cos [c+d x]^{9 / 2} \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4(a+a \sec [c+d x])^2(A+B \sec [c+d x]+C \sec [c+d x]^2)$$

$$\left(-\frac{2(8 A+9 B+12 C) \cot [c]}{15 d}+\frac{(46 A+51 B+56 C) \cos [d x] \sin [c]}{84 d}+\right.$$

$$\frac{(37 A+36 B+18 C) \cos [2 d x] \sin [2 c]}{180 d}+\frac{(2 A+B) \cos [3 d x] \sin [3 c]}{28 d}+$$

$$\frac{A \cos [4 d x] \sin [4 c]}{72 d}+\frac{(46 A+51 B+56 C) \cos [c] \sin [d x]}{84 d}+$$

$$\left.\frac{(37 A+36 B+18 C) \cos [2 c] \sin [2 d x]}{180 d}+\frac{(2 A+B) \cos [3 c] \sin [3 d x]}{28 d}+\frac{A \cos [4 c] \sin [4 d x]}{72 d}\right)-$$

$$\frac{1}{21 d(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\cot [c]^2}}$$

$$10 A \cos [c+d x]^4 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right]$$

$$\sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4(a+a \sec [c+d x])^2(A+B \sec [c+d x]+C \sec [c+d x]^2)$$

$$\sec [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]}$$

$$\sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]}-}$$

$$\frac{1}{7 d(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\cot [c]^2}}$$

$$4 B \cos [c+d x]^4 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right]$$

$$\sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4(a+a \sec [c+d x])^2(A+B \sec [c+d x]+C \sec [c+d x]^2)$$

$$\sec [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]}$$

$$\begin{aligned}
 & \frac{\sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]} \sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]} - 1}{3d(A+2C+2B\cos[c+dx]+A\cos[2c+2dx])\sqrt{1+\cot[c]^2}} \\
 & 2C\cos[c+dx]^4 \text{Csc}[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\cot[c]]]^2\right] \\
 & \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a\sec[c+dx])^2 (A+B\sec[c+dx]+C\sec[c+dx]^2) \\
 & \text{Sec}[dx - \text{ArcTan}[\cot[c]]] \sqrt{1-\sin[dx - \text{ArcTan}[\cot[c]]]} \\
 & \frac{\sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]} \sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]} - 1}{8A\cos[c+dx]^4 \text{Csc}[c] \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a\sec[c+dx])^2 (A+B\sec[c+dx]+C\sec[c+dx]^2)} \\
 & \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos[dx + \text{ArcTan}[\tan[c]]]^2\right] \right) \\
 & \left( \frac{\sin[dx + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1-\cos[dx + \text{ArcTan}[\tan[c]]]}} \right) \\
 & \left( \frac{\sqrt{1+\cos[dx + \text{ArcTan}[\tan[c]]]} \sqrt{\cos[c] \cos[dx + \text{ArcTan}[\tan[c]]]} \sqrt{1+\tan[c]^2}}{\sqrt{1+\tan[c]^2}} - \frac{\frac{\sin[dx + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1+\tan[c]^2}} + \frac{2\cos[c]^2 \cos[dx + \text{ArcTan}[\tan[c]]] \sqrt{1+\tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[dx + \text{ArcTan}[\tan[c]]]} \sqrt{1+\tan[c]^2}} \right) \\
 & (15d(A+2C+2B\cos[c+dx]+A\cos[2c+2dx])) - \\
 & \left( 3B\cos[c+dx]^4 \text{Csc}[c] \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a\sec[c+dx])^2 (A+B\sec[c+dx]+C\sec[c+dx]^2) \right) \\
 & \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos[dx + \text{ArcTan}[\tan[c]]]^2\right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{\sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 - \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \tan [c]^2}} \right) / \left( \frac{\sqrt{1 + \tan [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \tan [c]^2}} \right) \\
 & - \left( \frac{\frac{\sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \tan [c]^2}} \right) / \\
 & (5 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) - \\
 & \left( 4 C \cos [c + d x]^4 \text{Csc}[c] \text{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^4 (a + a \text{Sec}[c + d x])^2 (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) \right. \\
 & \left. \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos [d x + \text{ArcTan}[\text{Tan}[c]]\right]^2 \right) \right) \\
 & \left( \frac{\sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 - \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \tan [c]^2}} \right) / \left( \frac{\sqrt{1 + \tan [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \tan [c]^2}} \right) \\
 & - \left( \frac{\frac{\sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \tan [c]^2}} \right) / \\
 & (5 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]))
 \end{aligned}$$

**Problem 1196: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c + d x]^{7/2} (a + a \text{Sec}[c + d x])^2 (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) dx$$

Optimal (type 4, 179 leaves, 8 steps):

$$\frac{4 a^2 (3 A+4 B+5 C) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 d} + \frac{4 a^2 (6 A+7 B+14 C) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{21 d} +$$

$$\frac{2 a^2 (33 A+49 B+35 C) \sqrt{\cos [c+d x]} \sin [c+d x]}{105 d} +$$

$$\frac{2 A \sqrt{\cos [c+d x]} (a+a \cos [c+d x])^2 \sin [c+d x]}{7 d} +$$

$$\frac{2 (4 A+7 B) \sqrt{\cos [c+d x]} (a^2+a^2 \cos [c+d x]) \sin [c+d x]}{35 d}$$

Result(type 5, 2001 leaves):

$$\frac{1}{10 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])}$$

$$3 i A \cos [c+d x]^4 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 (A+B \sec [c+d x]+C \sec [c+d x]^2)$$

$$\left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c]+i \sin [c])^2\right] \right. \right.$$

$$\left. \frac{\sqrt{e^{-i d x} (2 (1+e^{2 i d x}) \cos [c]+2 i (-1+e^{2 i d x}) \sin [c])}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}} \right) /$$

$$(3 i d (1+e^{2 i d x}) \cos [c]-3 d (-1+e^{2 i d x}) \sin [c]) -$$

$$\left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c]+i \sin [c])^2\right] \right.$$

$$\left. \frac{\sqrt{e^{-i d x} (2 (1+e^{2 i d x}) \cos [c]+2 i (-1+e^{2 i d x}) \sin [c])}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}} \right) /$$

$$\left. (-i d (1+e^{2 i d x}) \cos [c]+d (-1+e^{2 i d x}) \sin [c]) \right) +$$

$$\frac{1}{5 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])}$$

$$2$$

$$i B \cos [c+d x]^4$$

$$\operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4$$

$$(a+a \sec [c+d x])^2$$

$$(A+B \sec [c+d x]+C \sec [c+d x]^2)$$

$$\left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c]+i \sin [c])^2\right] \right. \right.$$

$$\left. \frac{\sqrt{e^{-i d x} (2 (1+e^{2 i d x}) \cos [c]+2 i (-1+e^{2 i d x}) \sin [c])}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}} \right) /$$

$$(3 i d (1+e^{2 i d x}) \cos [c]-3 d (-1+e^{2 i d x}) \sin [c]) -$$

$$\left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c]+i \sin [c])^2\right] \right.$$

$$\left. \frac{\sqrt{e^{-i d x} (2 (1+e^{2 i d x}) \cos [c]+2 i (-1+e^{2 i d x}) \sin [c])}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}} \right)$$

$$\begin{aligned}
 & \left( \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \\
 & \left( -i d \left( 1 + e^{2 i d x} \right) \cos [c] + d \left( -1 + e^{2 i d x} \right) \sin [c] \right) + \\
 & \frac{1}{2 \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right)} \\
 & i C \\
 & \cos [c + d x]^4 \\
 & \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^4 \\
 & \left( a + a \operatorname{Sec}[c + d x] \right)^2 \\
 & \left( A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2 \right) \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2\right] \right. \right. \\
 & \left. \left. \sqrt{e^{-i d x} \left( 2 \left( 1 + e^{2 i d x} \right) \cos [c] + 2 i \left( -1 + e^{2 i d x} \right) \sin [c] \right)} \right. \right. \\
 & \left. \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \right. \\
 & \left. \left( 3 i d \left( 1 + e^{2 i d x} \right) \cos [c] - 3 d \left( -1 + e^{2 i d x} \right) \sin [c] \right) - \right. \\
 & \left. \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2\right] \right. \right. \\
 & \left. \left. \sqrt{e^{-i d x} \left( 2 \left( 1 + e^{2 i d x} \right) \cos [c] + 2 i \left( -1 + e^{2 i d x} \right) \sin [c] \right)} \right. \right. \\
 & \left. \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \right. \\
 & \left. \left( -i d \left( 1 + e^{2 i d x} \right) \cos [c] + d \left( -1 + e^{2 i d x} \right) \sin [c] \right) \right) + \\
 & \left( \cos [c + d x]^{9/2} \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^4 \left( a + a \operatorname{Sec}[c + d x] \right)^2 \left( A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2 \right) \right. \\
 & \left( -\frac{2 (3 A + 4 B + 5 C) \cot [c]}{5 d} + \frac{(51 A + 56 B + 28 C) \cos [d x] \sin [c]}{84 d} + \right. \\
 & \frac{(2 A + B) \cos [2 d x] \sin [2 c]}{10 d} + \frac{A \cos [3 d x] \sin [3 c]}{28 d} + \frac{(51 A + 56 B + 28 C) \cos [c] \sin [d x]}{84 d} + \\
 & \left. \left. \frac{(2 A + B) \cos [2 c] \sin [2 d x]}{10 d} + \frac{A \cos [3 c] \sin [3 d x]}{28 d} \right) \right) / \\
 & \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) - \\
 & \frac{1}{7 d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \sqrt{1 + \cot [c]^2}} \\
 & 4 A \cos [c + d x]^4 \operatorname{Csc}[c] \\
 & \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\cot [c]]]^2\right] \\
 & \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^4 \left( a + a \operatorname{Sec}[c + d x] \right)^2 \\
 & \left( A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2 \right) \\
 & \operatorname{Sec}[d x - \operatorname{ArcTan}[\cot [c]]] \\
 & \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\cot [c]]]}
 \end{aligned}$$



$$\frac{\sqrt{-\sqrt{1+\cot^2[c]} \sin[c] \sin[d x - \text{ArcTan}[\cot[c]]]}}{\sqrt{1+\sin[d x - \text{ArcTan}[\cot[c]]]} - 1}$$


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$$\frac{3 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\cot [c]^2} 2 B \cos [c+d x]^4 \csc [c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x - \text{ArcTan}[\cot [c]]]^2\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 (A+B \sec [c+d x]+C \sec [c+d x]^2) \sec [d x - \text{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x - \text{ArcTan}[\cot [c]]]}}{\sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x - \text{ArcTan}[\cot [c]]]}}$$


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$$\frac{3 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\cot [c]^2} 4 C \cos [c+d x]^4 \csc [c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x - \text{ArcTan}[\cot [c]]]^2\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 (A+B \sec [c+d x]+C \sec [c+d x]^2) \sec [d x - \text{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x - \text{ArcTan}[\cot [c]]]}}{\sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x - \text{ArcTan}[\cot [c]]]}}$$

**Problem 1197: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c+d x]^{5 / 2} (a+a \sec [c+d x])^2 (A+B \sec [c+d x]+C \sec [c+d x]^2) d x$$

Optimal (type 4, 170 leaves, 8 steps):

$$\frac{4 a^2 (4 A+5 B) \text{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 d} + \frac{4 a^2 (A+2 B+3 C) \text{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{3 d} + \frac{2 a^2 (7 A+5 B-15 C) \sqrt{\cos [c+d x]} \sin [c+d x]}{15 d} + \frac{2 C (a+a \cos [c+d x])^2 \sin [c+d x]}{d \sqrt{\cos [c+d x]}} + \frac{2 (A-5 C) \sqrt{\cos [c+d x]} (a^2+a^2 \cos [c+d x]) \sin [c+d x]}{5 d}$$

Result (type 5, 1356 leaves):

$$\left( \cos [c+d x]^{9/2} \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a+a \sec [c+d x])^2 (A+B \sec [c+d x]+C \sec [c+d x]^2) \right. \\ \left. \left( -\frac{1}{10 d} (8 A+10 B-5 C+8 A \cos [2 c]+10 B \cos [2 c]+5 C \cos [2 c]) \csc [c] \sec [c] + \right. \right. \\ \left. \frac{(2 A+B) \cos [d x] \sin [c]}{3 d} + \frac{A \cos [2 d x] \sin [2 c]}{10 d} + \frac{(2 A+B) \cos [c] \sin [d x]}{3 d} + \right. \\ \left. \left. \frac{C \sec [c] \sec [c+d x] \sin [d x]}{d} + \frac{A \cos [2 c] \sin [2 d x]}{10 d} \right) \right) / \\ (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) - \\ \frac{1}{3 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\cot [c]^2} \\ 2 A \cos [c+d x]^4 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]\right]^2} \\ \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a+a \sec [c+d x])^2 (A+B \sec [c+d x]+C \sec [c+d x]^2) \\ \sec [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \\ \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} - \\ \frac{1}{3 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\cot [c]^2} \\ 4 B \cos [c+d x]^4 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]\right]^2} \\ \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a+a \sec [c+d x])^2 (A+B \sec [c+d x]+C \sec [c+d x]^2) \\ \sec [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \\ \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} - \\ \frac{1}{d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\cot [c]^2} \\ 2 C \cos [c+d x]^4 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]\right]^2} \\ \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a+a \sec [c+d x])^2 (A+B \sec [c+d x]+C \sec [c+d x]^2) \\ \sec [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \\ \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} -$$

$$\left( 4 A \cos [c+d x]^4 \csc [c] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a+a \sec [c+d x])^2 (A+B \sec [c+d x]+C \sec [c+d x]^2) \right.$$

$$\left( \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x+\text{ArcTan}[\tan [c]]] \right]^2 \right) \right.$$

$$\left. \sin [d x+\text{ArcTan}[\tan [c]]] \tan [c] \right) / \left( \sqrt{1-\cos [d x+\text{ArcTan}[\tan [c]]]} \right)$$

$$\sqrt{1+\cos [d x+\text{ArcTan}[\tan [c]]]} \sqrt{\cos [c] \cos [d x+\text{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2}$$

$$\left. \left. \left. \sqrt{1+\tan [c]^2} \right) - \frac{\frac{\sin [d x+\text{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x+\text{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}{\cos [c]^2+\sin [c]^2}}{\sqrt{\cos [c] \cos [d x+\text{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2}} \right) \right) /$$

$$(5 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])) -$$

$$\left( B \cos [c+d x]^4 \csc [c] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a+a \sec [c+d x])^2 (A+B \sec [c+d x]+C \sec [c+d x]^2) \right.$$

$$\left( \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x+\text{ArcTan}[\tan [c]]] \right]^2 \right) \right.$$

$$\left. \sin [d x+\text{ArcTan}[\tan [c]]] \tan [c] \right) / \left( \sqrt{1-\cos [d x+\text{ArcTan}[\tan [c]]]} \right)$$

$$\sqrt{1+\cos [d x+\text{ArcTan}[\tan [c]]]} \sqrt{\cos [c] \cos [d x+\text{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2}$$

$$\left. \left. \left. \sqrt{1+\tan [c]^2} \right) - \frac{\frac{\sin [d x+\text{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x+\text{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}{\cos [c]^2+\sin [c]^2}}{\sqrt{\cos [c] \cos [d x+\text{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2}} \right) \right) /$$

$$(d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]))$$

**Problem 1198: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \text{Cos}[c + d x]^{3/2} (a + a \text{Sec}[c + d x])^2 (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) dx$$

Optimal (type 4, 170 leaves, 8 steps):

$$\frac{4 a^2 (A - C) \text{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{d} + \frac{4 a^2 (2 A + 3 B + 2 C) \text{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{3 d} + \frac{2 a^2 (A - 3 B - 5 C) \sqrt{\text{Cos}[c + d x]} \text{Sin}[c + d x]}{3 d} + \frac{2 C (a + a \text{Cos}[c + d x])^2 \text{Sin}[c + d x]}{3 d \text{Cos}[c + d x]^{3/2}} + \frac{2 (3 B + 4 C) (a^2 + a^2 \text{Cos}[c + d x]) \text{Sin}[c + d x]}{3 d \sqrt{\text{Cos}[c + d x]}}$$

Result (type 5, 1583 leaves):

$$\frac{1}{2 (A + 2 C + 2 B \text{Cos}[c + d x] + A \text{Cos}[2 c + 2 d x])} \left( i A \text{Cos}[c + d x]^4 \text{Csc}[c] \text{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^4 (a + a \text{Sec}[c + d x])^2 (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) \left( \left( 2 e^{2 i d x} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\text{Cos}[c] + i \text{Sin}[c])^2\right] \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \text{Cos}[c] + 2 i (-1 + e^{2 i d x}) \text{Sin}[c])} \sqrt{1 + e^{2 i d x} \text{Cos}[2 c] + i e^{2 i d x} \text{Sin}[2 c]}\right) / \left( 3 i d (1 + e^{2 i d x}) \text{Cos}[c] - 3 d (-1 + e^{2 i d x}) \text{Sin}[c] \right) - \left( 2 \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\text{Cos}[c] + i \text{Sin}[c])^2\right] \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \text{Cos}[c] + 2 i (-1 + e^{2 i d x}) \text{Sin}[c])} \sqrt{1 + e^{2 i d x} \text{Cos}[2 c] + i e^{2 i d x} \text{Sin}[2 c]}\right) / \left( -i d (1 + e^{2 i d x}) \text{Cos}[c] + d (-1 + e^{2 i d x}) \text{Sin}[c] \right) \right) - \frac{1}{2 (A + 2 C + 2 B \text{Cos}[c + d x] + A \text{Cos}[2 c + 2 d x])} \left( i C \text{Cos}[c + d x]^4 \text{Csc}[c] \text{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^4 (a + a \text{Sec}[c + d x])^2 (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) \left( \left( 2 e^{2 i d x} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\text{Cos}[c] + i \text{Sin}[c])^2\right] \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \text{Cos}[c] + 2 i (-1 + e^{2 i d x}) \text{Sin}[c])} \right) \right)$$

$$\begin{aligned}
 & \left( \sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]} \right) / \\
 & \left( 3 i d (1 + e^{2 i d x}) \cos[c] - 3 d (-1 + e^{2 i d x}) \sin[c] \right) - \\
 & \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right. \\
 & \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])} \right. \\
 & \left. \sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]} \right) / \\
 & \left( -i d (1 + e^{2 i d x}) \cos[c] + d (-1 + e^{2 i d x}) \sin[c] \right) + \\
 & \left( \cos[c + d x]^{9/2} \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^4 (a + a \sec[c + d x])^2 (A + B \sec[c + d x] + C \sec[c + d x]^2) \right. \\
 & \left( -\frac{(2 A - B - 4 C + 2 A \cos[2 c] + B \cos[2 c]) \csc[c] \sec[c]}{2 d} + \right. \\
 & \frac{A \cos[d x] \sin[c]}{3 d} + \frac{A \cos[c] \sin[d x]}{3 d} + \frac{C \sec[c] \sec[c + d x]^2 \sin[d x]}{3 d} + \\
 & \left. \left. \frac{\sec[c] \sec[c + d x] (C \sin[c] + 3 B \sin[d x] + 6 C \sin[d x])}{3 d} \right) \right) / \\
 & \frac{(A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) - 1}{1} \\
 & \frac{3 d (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) \sqrt{1 + \cot[c]^2} + 4 A \cos[c + d x]^4 \csc[c]}{1} \\
 & \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[d x - \operatorname{ArcTan}[\cot[c]]]^2\right] \\
 & \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^4 (a + a \sec[c + d x])^2 \\
 & (A + B \sec[c + d x] + C \sec[c + d x]^2) \\
 & \sec[d x - \operatorname{ArcTan}[\cot[c]]] \\
 & \sqrt{1 - \sin[d x - \operatorname{ArcTan}[\cot[c]]]} \\
 & \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[d x - \operatorname{ArcTan}[\cot[c]]]} \\
 & \frac{\sqrt{1 + \sin[d x - \operatorname{ArcTan}[\cot[c]]]} - 1}{1} \\
 & \frac{d (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) \sqrt{1 + \cot[c]^2} + 2 B \cos[c + d x]^4 \csc[c]}{1} \\
 & \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[d x - \operatorname{ArcTan}[\cot[c]]]^2\right] \\
 & \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^4 (a + a \sec[c + d x])^2 \\
 & (A + B \sec[c + d x] + C \sec[c + d x]^2) \\
 & \sec[d x - \operatorname{ArcTan}[\cot[c]]] \sqrt{1 - \sin[d x - \operatorname{ArcTan}[\cot[c]]]} \\
 & \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[d x - \operatorname{ArcTan}[\cot[c]]]}
 \end{aligned}$$

$$\frac{\sqrt{1 + \sin[d x - \text{ArcTan}[\text{Cot}[c]]]} - 1}{3 d (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) \sqrt{1 + \text{Cot}[c]^2} + 4 C \cos[c + d x]^4 \text{Csc}[c]}$$

$$\text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[d x - \text{ArcTan}[\text{Cot}[c]]]^2\right]$$

$$\text{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^4 (a + a \text{Sec}[c + d x])^2 (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2)$$

$$\text{Sec}[d x - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \sin[d x - \text{ArcTan}[\text{Cot}[c]]]}$$

$$\frac{\sqrt{-\sqrt{1 + \text{Cot}[c]^2} \sin[c] \sin[d x - \text{ArcTan}[\text{Cot}[c]]]}}{\sqrt{1 + \sin[d x - \text{ArcTan}[\text{Cot}[c]]]}$$

**Problem 1199: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sqrt{\cos[c + d x]} (a + a \text{Sec}[c + d x])^2 (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) dx$$

Optimal (type 4, 174 leaves, 8 steps):

$$\frac{4 a^2 (5 B + 4 C) \text{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{5 d} + \frac{4 a^2 (3 A + 2 B + C) \text{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{3 d} + \frac{2 a^2 (15 A + 25 B + 17 C) \sin[c + d x]}{15 d \sqrt{\cos[c + d x]}}$$

$$\frac{2 C (a + a \cos[c + d x])^2 \sin[c + d x]}{5 d \cos[c + d x]^{5/2}} + \frac{2 (5 B + 4 C) (a^2 + a^2 \cos[c + d x]) \sin[c + d x]}{15 d \cos[c + d x]^{3/2}}$$

Result (type 5, 1599 leaves):

$$\frac{1}{2 (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x])}$$

$$i B \cos[c + d x]^4 \text{Csc}[c] \text{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^4 (a + a \text{Sec}[c + d x])^2 (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2)$$

$$\left( \left( 2 e^{2 i d x} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right. \right.$$

$$\left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])}}{\sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]}} \right) /$$

$$(3 i d (1 + e^{2 i d x}) \cos[c] - 3 d (-1 + e^{2 i d x}) \sin[c]) -$$

$$\left( 2 \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right.$$

$$\left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])}}{\sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]}} \right) /$$

$$\begin{aligned}
 & \left( -i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c] \right) - \\
 & \frac{1}{5 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])} \\
 & \frac{2}{i} \\
 & C \\
 & \cos [c + d x]^4 \\
 & \csc [c] \\
 & \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \\
 & (a + a \sec [c + d x])^2 \\
 & (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \right. \\
 & \quad \left. \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) \right) / \\
 & \quad (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) - \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) \right) / \\
 & \quad \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) + \\
 & \left( \cos [c + d x]^{9/2} \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a + a \sec [c + d x])^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left( -\frac{(-5 A - 20 B - 16 C + 5 A \cos [2 c]) \csc [c] \sec [c]}{10 d} + \frac{C \sec [c] \sec [c + d x]^3 \sin [d x]}{5 d} + \right. \\
 & \quad \left. \frac{\sec [c] \sec [c + d x]^2 (3 C \sin [c] + 5 B \sin [d x] + 10 C \sin [d x])}{15 d} + \frac{1}{15 d} \sec [c] \sec [c + d x] \right. \\
 & \quad \left. \left. \left. (5 B \sin [c] + 10 C \sin [c] + 15 A \sin [d x] + 30 B \sin [d x] + 24 C \sin [d x]) \right) \right) \right) / \\
 & \left. (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) - \right. \\
 & \frac{1}{d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2}} \\
 & 2 A \\
 & \cos [c + d x]^4 \csc [c] \\
 & \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\cot [c]]]^2 \right] \\
 & \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \\
 & (a + a \sec [c + d x])^2 \\
 & (A + B \sec [c + d x] + C \sec [c + d x]^2)
 \end{aligned}$$

$$\frac{\frac{\text{Sec}[d x - \text{ArcTan}[\text{Cot}[c]]]}{\sqrt{1 - \text{Sin}[d x - \text{ArcTan}[\text{Cot}[c]]]}} \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[d x - \text{ArcTan}[\text{Cot}[c]]]} \sqrt{1 + \text{Sin}[d x - \text{ArcTan}[\text{Cot}[c]]]} - 1}{3 d (A + 2 C + 2 B \text{Cos}[c + d x] + A \text{Cos}[2 c + 2 d x]) \sqrt{1 + \text{Cot}[c]^2} 4 B \text{Cos}[c + d x]^4 \text{Csc}[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \text{Sin}[d x - \text{ArcTan}[\text{Cot}[c]]]^2\right]} \frac{\text{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^4 (a + a \text{Sec}[c + d x])^2 (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) \text{Sec}[d x - \text{ArcTan}[\text{Cot}[c]]]}{\sqrt{1 - \text{Sin}[d x - \text{ArcTan}[\text{Cot}[c]]]}} \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[d x - \text{ArcTan}[\text{Cot}[c]]]} \sqrt{1 + \text{Sin}[d x - \text{ArcTan}[\text{Cot}[c]]]} - 1}{3 d (A + 2 C + 2 B \text{Cos}[c + d x] + A \text{Cos}[2 c + 2 d x]) \sqrt{1 + \text{Cot}[c]^2} 2 C \text{Cos}[c + d x]^4 \text{Csc}[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \text{Sin}[d x - \text{ArcTan}[\text{Cot}[c]]]^2\right]} \frac{\text{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^4 (a + a \text{Sec}[c + d x])^2 (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) \text{Sec}[d x - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \text{Sin}[d x - \text{ArcTan}[\text{Cot}[c]]]}}{\sqrt{-\sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[d x - \text{ArcTan}[\text{Cot}[c]]]} \sqrt{1 + \text{Sin}[d x - \text{ArcTan}[\text{Cot}[c]]]}}$$

**Problem 1200: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \text{Sec}[c + d x])^2 (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2)}{\sqrt{\text{Cos}[c + d x]}} dx$$

Optimal (type 4, 215 leaves, 9 steps):



$$\begin{aligned}
 & - \frac{4 a^2 (5 A+4 B+3 C) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 d} + \frac{4 a^2 (14 A+7 B+6 C) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{21 d} + \\
 & \frac{2 a^2 (35 A+49 B+33 C) \operatorname{Sin}[c+d x]}{105 d \operatorname{Cos}[c+d x]^{3/2}} + \frac{4 a^2 (5 A+4 B+3 C) \operatorname{Sin}[c+d x]}{5 d \sqrt{\operatorname{Cos}[c+d x]}} + \\
 & \frac{2 C (a+a \operatorname{Cos}[c+d x])^2 \operatorname{Sin}[c+d x]}{7 d \operatorname{Cos}[c+d x]^{7/2}} + \frac{2 (7 B+4 C) (a^2+a^2 \operatorname{Cos}[c+d x]) \operatorname{Sin}[c+d x]}{35 d \operatorname{Cos}[c+d x]^{5/2}}
 \end{aligned}$$

Result (type 5, 2041 leaves):

$$\begin{aligned}
 & \frac{1}{2 (A+2 C+2 B \operatorname{Cos}[c+d x]+A \operatorname{Cos}[2 c+2 d x])} \\
 & \quad i A \operatorname{Cos}[c+d x]^4 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \\
 & \quad \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\operatorname{Cos}[c]+i \operatorname{Sin}[c])\right]^2 \right. \right. \\
 & \quad \left. \left. \frac{\sqrt{e^{-i d x} (2 (1+e^{2 i d x}) \operatorname{Cos}[c]+2 i (-1+e^{2 i d x}) \operatorname{Sin}[c])}}{\sqrt{1+e^{2 i d x} \operatorname{Cos}[2 c]+i e^{2 i d x} \operatorname{Sin}[2 c]}} \right) / \right. \\
 & \quad \left. (3 i d (1+e^{2 i d x}) \operatorname{Cos}[c]-3 d (-1+e^{2 i d x}) \operatorname{Sin}[c]) - \right. \\
 & \quad \left. \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\operatorname{Cos}[c]+i \operatorname{Sin}[c])\right]^2 \right) \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1+e^{2 i d x}) \operatorname{Cos}[c]+2 i (-1+e^{2 i d x}) \operatorname{Sin}[c])}}{\sqrt{1+e^{2 i d x} \operatorname{Cos}[2 c]+i e^{2 i d x} \operatorname{Sin}[2 c]}} \right) / \right. \\
 & \quad \left. (-i d (1+e^{2 i d x}) \operatorname{Cos}[c]+d (-1+e^{2 i d x}) \operatorname{Sin}[c]) \right) - \\
 & \quad \frac{1}{5 (A+2 C+2 B \operatorname{Cos}[c+d x]+A \operatorname{Cos}[2 c+2 d x])} \\
 & \quad 2 \\
 & \quad i \\
 & \quad B \\
 & \quad \operatorname{Cos}[c+d x]^4 \\
 & \quad \operatorname{Csc}[c] \\
 & \quad \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 \\
 & \quad (a+a \operatorname{Sec}[c+d x])^2 \\
 & \quad (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \\
 & \quad \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\operatorname{Cos}[c]+i \operatorname{Sin}[c])\right]^2 \right. \right. \\
 & \quad \left. \left. \frac{\sqrt{e^{-i d x} (2 (1+e^{2 i d x}) \operatorname{Cos}[c]+2 i (-1+e^{2 i d x}) \operatorname{Sin}[c])}}{\sqrt{1+e^{2 i d x} \operatorname{Cos}[2 c]+i e^{2 i d x} \operatorname{Sin}[2 c]}} \right) / \right. \\
 & \quad \left. (3 i d (1+e^{2 i d x}) \operatorname{Cos}[c]-3 d (-1+e^{2 i d x}) \operatorname{Sin}[c]) - \right. \\
 & \quad \left. \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\operatorname{Cos}[c]+i \operatorname{Sin}[c])\right]^2 \right) \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \cos [c] + 2 i (-1 + e^{2 i dx}) \sin [c])}}{\sqrt{1 + e^{2 i dx} \cos [2 c] + i e^{2 i dx} \sin [2 c]}} \Big/ \\
 & \left( -i d (1 + e^{2 i dx}) \cos [c] + d (-1 + e^{2 i dx}) \sin [c] \right) - \\
 & \frac{1}{10 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])} \\
 & 3 \\
 & i \\
 & C \\
 & \cos [c + d x]^4 \\
 & \operatorname{Csc}[c] \\
 & \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^4 \\
 & (a + a \operatorname{Sec}[c + d x])^2 \\
 & (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\
 & \left( \left( 2 e^{2 i dx} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i dx} (\cos [c] + i \sin [c])^2\right] \right. \right. \\
 & \left. \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \cos [c] + 2 i (-1 + e^{2 i dx}) \sin [c])}}{\sqrt{1 + e^{2 i dx} \cos [2 c] + i e^{2 i dx} \sin [2 c]}} \Big/ \right. \\
 & \left. (3 i d (1 + e^{2 i dx}) \cos [c] - 3 d (-1 + e^{2 i dx}) \sin [c]) - \right. \\
 & \left. \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i dx} (\cos [c] + i \sin [c])^2\right] \right) \right. \\
 & \left. \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \cos [c] + 2 i (-1 + e^{2 i dx}) \sin [c])}}{\sqrt{1 + e^{2 i dx} \cos [2 c] + i e^{2 i dx} \sin [2 c]}} \Big/ \right. \\
 & \left. (-i d (1 + e^{2 i dx}) \cos [c] + d (-1 + e^{2 i dx}) \sin [c]) \right) + \\
 & \frac{1}{A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]} \\
 & \cos [c + d x]^{9/2} \\
 & \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^4 \\
 & (a + a \operatorname{Sec}[c + d x])^2 \\
 & (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\
 & \left( \frac{2 (5 A + 4 B + 3 C) \operatorname{Csc}[c] \operatorname{Sec}[c]}{5 d} + \frac{C \operatorname{Sec}[c] \operatorname{Sec}[c + d x]^4 \sin [d x]}{7 d} + \right. \\
 & \left. \frac{\operatorname{Sec}[c] \operatorname{Sec}[c + d x]^3 (5 C \sin [c] + 7 B \sin [d x] + 14 C \sin [d x])}{35 d} + \frac{1}{105 d} \right. \\
 & \left. \operatorname{Sec}[c] \operatorname{Sec}[c + d x]^2 (21 B \sin [c] + 42 C \sin [c] + 35 A \sin [d x] + 70 B \sin [d x] + 60 C \sin [d x]) + \right. \\
 & \left. \frac{1}{105 d} \operatorname{Sec}[c] \operatorname{Sec}[c + d x] \right. \\
 & \left. (35 A \sin [c] + 70 B \sin [c] + 60 C \sin [c] + 210 A \sin [d x] + 168 B \sin [d x] + 126 C \sin [d x]) \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{3 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\cot [c]^2}} \\
 & 4 A \cos [c+d x]^4 \csc [c] \\
 & \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right] \\
 & \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 \\
 & (A+B \sec [c+d x]+C \sec [c+d x]^2) \\
 & \sec [d x-\operatorname{ArcTan}[\cot [c]]] \\
 & \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \\
 & \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]]} \\
 & \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} - \\
 & \frac{1}{1}
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{3 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\cot [c]^2}} \\
 & 2 B \cos [c+d x]^4 \csc [c] \\
 & \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right] \\
 & \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 \\
 & (A+B \sec [c+d x]+C \sec [c+d x]^2) \\
 & \sec [d x-\operatorname{ArcTan}[\cot [c]]] \\
 & \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \\
 & \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]]} \\
 & \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} - \\
 & \frac{1}{1}
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{7 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\cot [c]^2}} \\
 & 4 C \cos [c+d x]^4 \csc [c] \\
 & \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right] \\
 & \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 \\
 & (A+B \sec [c+d x]+C \sec [c+d x]^2) \\
 & \sec [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \\
 & \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]]} \\
 & \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]}
 \end{aligned}$$

**Problem 1201: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \operatorname{Sec}[c + d x])^2 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Cos}[c + d x]^{3/2}} dx$$

Optimal (type 4, 251 leaves, 10 steps):

$$\begin{aligned} & - \frac{4 a^2 (12 A + 9 B + 8 C) \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{15 d} + \\ & \frac{4 a^2 (7 A + 6 B + 5 C) \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{21 d} + \frac{2 a^2 (21 A + 27 B + 19 C) \operatorname{Sin}[c + d x]}{105 d \operatorname{Cos}[c + d x]^{5/2}} + \\ & \frac{4 a^2 (7 A + 6 B + 5 C) \operatorname{Sin}[c + d x]}{21 d \operatorname{Cos}[c + d x]^{3/2}} + \frac{4 a^2 (12 A + 9 B + 8 C) \operatorname{Sin}[c + d x]}{15 d \sqrt{\operatorname{Cos}[c + d x]}} + \\ & \frac{2 C (a + a \operatorname{Cos}[c + d x])^2 \operatorname{Sin}[c + d x]}{9 d \operatorname{Cos}[c + d x]^{9/2}} + \frac{2 (9 B + 4 C) (a^2 + a^2 \operatorname{Cos}[c + d x]) \operatorname{Sin}[c + d x]}{63 d \operatorname{Cos}[c + d x]^{7/2}} \end{aligned}$$

Result (type 5, 1741 leaves):

$$\begin{aligned} & \frac{1}{A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]} \\ & \operatorname{Cos}[c + d x]^{9/2} \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^4 (a + a \operatorname{Sec}[c + d x])^2 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\ & \left( \frac{2 (12 A + 9 B + 8 C) \operatorname{Csc}[c] \operatorname{Sec}[c]}{15 d} + \frac{C \operatorname{Sec}[c] \operatorname{Sec}[c + d x]^5 \operatorname{Sin}[d x]}{9 d} + \right. \\ & \frac{\operatorname{Sec}[c] \operatorname{Sec}[c + d x]^4 (7 C \operatorname{Sin}[c] + 9 B \operatorname{Sin}[d x] + 18 C \operatorname{Sin}[d x])}{63 d} + \frac{1}{105 d} 2 \operatorname{Sec}[c] \operatorname{Sec}[c + d x] \\ & (35 A \operatorname{Sin}[c] + 30 B \operatorname{Sin}[c] + 25 C \operatorname{Sin}[c] + 84 A \operatorname{Sin}[d x] + 63 B \operatorname{Sin}[d x] + 56 C \operatorname{Sin}[d x]) + \\ & \frac{1}{315 d} \operatorname{Sec}[c] \operatorname{Sec}[c + d x]^3 (45 B \operatorname{Sin}[c] + 90 C \operatorname{Sin}[c] + 63 A \operatorname{Sin}[d x] + 126 B \operatorname{Sin}[d x] + \\ & 112 C \operatorname{Sin}[d x]) + \frac{1}{315 d} \operatorname{Sec}[c] \operatorname{Sec}[c + d x]^2 (63 A \operatorname{Sin}[c] + 126 B \operatorname{Sin}[c] + \\ & 112 C \operatorname{Sin}[c] + 210 A \operatorname{Sin}[d x] + 180 B \operatorname{Sin}[d x] + 150 C \operatorname{Sin}[d x]) \left. \right) - \\ & \frac{1}{3 d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2}} \\ & 2 A \operatorname{Cos}[c + d x]^4 \operatorname{Csc}[c] \\ & \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \\ & \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^4 (a + a \operatorname{Sec}[c + d x])^2 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\ & \operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\ & \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1 + \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} - \\ & \frac{1}{7 d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2}} \end{aligned}$$

$$4 B \cos [c+d x]^4 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \operatorname{Sec}[d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]]} \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} - 1$$

$$21 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\cot [c]^2} 10 C \cos [c+d x]^4 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \operatorname{Sec}[d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]]} \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} +$$

$$\left(4 A \cos [c+d x]^4 \csc [c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2)\right)$$

$$\left(\operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\tan [c]]]^2\right]\right)$$

$$\operatorname{Sin}[d x+\operatorname{ArcTan}[\tan [c]]] \tan [c] \left/ \left(\sqrt{1-\cos [d x+\operatorname{ArcTan}[\tan [c]]]}\right)\right.$$

$$\sqrt{1+\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2}$$

$$\left. \left. \left. \left. \sqrt{1+\tan [c]^2} \right) - \frac{\frac{\operatorname{Sin}[d x+\operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}{\cos [c]^2+\sin [c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2}} \right) \right) \right/$$

$$(5 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])) +$$

$$\left(3 B \cos [c+d x]^4 \csc [c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2)\right)$$

$$\left( \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \text{ArcTan} [\text{Tan} [c]]]^2 \right] \right. \right.$$

$$\left. \left. \frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 - \cos [d x + \text{ArcTan} [\text{Tan} [c]]]}}, \right. \right.$$

$$\left. \left. \frac{\sqrt{1 + \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2}}{\sqrt{1 + \tan [c]^2}} - \frac{\frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2}} \right) \right) /$$

$$(5 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) +$$

$$\left( 8 C \cos [c + d x]^4 \csc [c] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a + a \sec [c + d x])^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right)$$

$$\left( \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \text{ArcTan} [\text{Tan} [c]]]^2 \right] \right. \right.$$

$$\left. \left. \frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 - \cos [d x + \text{ArcTan} [\text{Tan} [c]]]}}, \right. \right.$$

$$\left. \left. \frac{\sqrt{1 + \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2}}{\sqrt{1 + \tan [c]^2}} - \frac{\frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2}} \right) \right) /$$

$$(15 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]))$$

**Problem 1202: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c + d x]^{11/2} (a + a \sec [c + d x])^3 (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 4, 267 leaves, 10 steps):

$$\begin{aligned}
 & \frac{4 a^3 (15 A + 17 B + 21 C) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{15 d} + \\
 & \frac{4 a^3 (105 A + 121 B + 143 C) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{231 d} + \\
 & \frac{4 a^3 (105 A + 121 B + 143 C) \sqrt{\cos [c+d x]} \sin [c+d x]}{231 d} + \\
 & \frac{4 a^3 (210 A + 253 B + 264 C) \cos [c+d x]^{3/2} \sin [c+d x]}{1155 d} + \\
 & \frac{2 A \cos [c+d x]^{3/2} (a+a \cos [c+d x])^3 \sin [c+d x]}{11 d} + \\
 & \frac{2 (6 A + 11 B) \cos [c+d x]^{3/2} (a^2+a^2 \cos [c+d x])^2 \sin [c+d x]}{99 a d} + \frac{1}{693 d} \\
 & 2 (105 A + 143 B + 99 C) \cos [c+d x]^{3/2} (a^3+a^3 \cos [c+d x]) \sin [c+d x]
 \end{aligned}$$

Result (type 5, 1364 leaves):

$$\begin{aligned}
 & a^3 \left( \sqrt{\cos [c+d x]} (1+\cos [c+d x])^3 \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 \right. \\
 & \left( -\frac{(15 A+17 B+21 C) \cot [c]}{30 d} + \frac{(1953 A+2134 B+2354 C) \cos [d x] \sin [c]}{7392 d} + \right. \\
 & \frac{(75 A+73 B+54 C) \cos [2 d x] \sin [2 c]}{720 d} + \frac{(189 A+132 B+44 C) \cos [3 d x] \sin [3 c]}{4928 d} + \\
 & \frac{(3 A+B) \cos [4 d x] \sin [4 c]}{288 d} + \frac{A \cos [5 d x] \sin [5 c]}{704 d} + \\
 & \frac{(1953 A+2134 B+2354 C) \cos [c] \sin [d x]}{7392 d} + \frac{(75 A+73 B+54 C) \cos [2 c] \sin [2 d x]}{720 d} + \\
 & \frac{(189 A+132 B+44 C) \cos [3 c] \sin [3 d x]}{4928 d} + \\
 & \left. \left. \frac{(3 A+B) \cos [4 c] \sin [4 d x]}{288 d} + \frac{A \cos [5 c] \sin [5 d x]}{704 d} \right) - \right. \\
 & \left( 5 A (1+\cos [c+d x])^3 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]\right]^2 \right) \\
 & \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 \operatorname{Sec}[d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \\
 & \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]]}
 \end{aligned}$$

$$\begin{aligned}
 & \left. \sqrt{1 + \sin [d x - \text{ArcTan}[\text{Cot}[c]]]} \right) / \left( 22 d \sqrt{1 + \text{Cot}[c]^2} \right) - \\
 & \left( 11 B (1 + \cos [c + d x])^3 \text{Csc}[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \text{ArcTan}[\text{Cot}[c]]]^2\right] \right. \\
 & \quad \text{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 \text{Sec}[d x - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \sin [d x - \text{ArcTan}[\text{Cot}[c]]]} \\
 & \quad \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \sin [c] \sin [d x - \text{ArcTan}[\text{Cot}[c]]]} \\
 & \quad \left. \left. \sqrt{1 + \sin [d x - \text{ArcTan}[\text{Cot}[c]]]} \right) / \left( 42 d \sqrt{1 + \text{Cot}[c]^2} \right) - \right. \\
 & \left( 13 C (1 + \cos [c + d x])^3 \text{Csc}[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \text{ArcTan}[\text{Cot}[c]]]^2\right] \right. \\
 & \quad \text{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 \text{Sec}[d x - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \sin [d x - \text{ArcTan}[\text{Cot}[c]]]} \\
 & \quad \left. \left. \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \sin [c] \sin [d x - \text{ArcTan}[\text{Cot}[c]]]} \sqrt{1 + \sin [d x - \text{ArcTan}[\text{Cot}[c]]]} \right) / \right. \\
 & \left( 42 d \sqrt{1 + \text{Cot}[c]^2} \right) - \frac{1}{4 d} A (1 + \cos [c + d x])^3 \text{Csc}[c] \text{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 \\
 & \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos [d x + \text{ArcTan}[\text{Tan}[c]]]^2\right] \right. \\
 & \quad \left. \sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] \right) / \\
 & \left( \sqrt{1 - \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \right. \\
 & \quad \left. \sqrt{\cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \text{Tan}[c]^2} \sqrt{1 + \text{Tan}[c]^2} \right) - \\
 & \left. \frac{\frac{\sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \text{Tan}[c]^2}} \right) - \\
 & \frac{1}{60 d} 17 B (1 + \cos [c + d x])^3 \text{Csc}[c] \text{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6
 \end{aligned}$$



$$\left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right]^2\right] \right. \\ \left. \frac{\sin\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right] \text{Tan}[c]}{\sqrt{1 - \cos\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right]} \sqrt{1 + \cos\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right]} \right. \\ \left. \frac{\sqrt{\cos[c] \cos\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right]} \sqrt{1 + \text{Tan}[c]^2} \sqrt{1 + \text{Tan}[c]^2}}{\frac{\sin\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \frac{2 \cos[c]^2 \cos\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right] \sqrt{1 + \text{Tan}[c]^2}}{\cos[c]^2 + \sin[c]^2}} \right. \\ \left. \frac{1}{20 d} \cos\left[c + d x\right]^3 \csc[c] \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^6 \right) - \\ \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right]^2\right] \right. \\ \left. \frac{\sin\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right] \text{Tan}[c]}{\sqrt{1 - \cos\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right]} \sqrt{1 + \cos\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right]} \right. \\ \left. \frac{\sqrt{\cos[c] \cos\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right]} \sqrt{1 + \text{Tan}[c]^2} \sqrt{1 + \text{Tan}[c]^2}}{\frac{\sin\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \frac{2 \cos[c]^2 \cos\left[d x + \text{ArcTan}\left[\text{Tan}[c]\right]\right] \sqrt{1 + \text{Tan}[c]^2}}{\cos[c]^2 + \sin[c]^2}} \right) -$$

**Problem 1203: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c + d x]^{9/2} (a + a \sec[c + d x])^3 (A + B \sec[c + d x] + C \sec[c + d x]^2) dx$$

Optimal (type 4, 231 leaves, 9 steps):

$$\frac{4 a^3 (17 A + 21 B + 27 C) \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{15 d} +$$

$$\frac{4 a^3 (11 A + 13 B + 21 C) \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{21 d} +$$

$$\frac{4 a^3 (32 A + 41 B + 42 C) \sqrt{\cos [c + d x]} \sin [c + d x]}{105 d} +$$

$$\frac{2 A \sqrt{\cos [c + d x]} (a + a \cos [c + d x])^3 \sin [c + d x]}{9 d} +$$

$$\frac{2 (2 A + 3 B) \sqrt{\cos [c + d x]} (a^2 + a^2 \cos [c + d x])^2 \sin [c + d x]}{21 a d} +$$

$$\frac{2 (73 A + 99 B + 63 C) \sqrt{\cos [c + d x]} (a^3 + a^3 \cos [c + d x]) \sin [c + d x]}{315 d}$$

Result (type 5, 1697 leaves):

$$\frac{1}{A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]}$$

$$\cos [c + d x]^{11/2} \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)$$

$$\left( - \frac{(17 A + 21 B + 27 C) \cot [c]}{15 d} + \frac{(97 A + 107 B + 84 C) \cos [d x] \sin [c]}{168 d} + \right.$$

$$\frac{(73 A + 54 B + 18 C) \cos [2 d x] \sin [2 c]}{360 d} + \frac{(3 A + B) \cos [3 d x] \sin [3 c]}{56 d} +$$

$$\frac{A \cos [4 d x] \sin [4 c]}{144 d} + \frac{(97 A + 107 B + 84 C) \cos [c] \sin [d x]}{168 d} +$$

$$\frac{(73 A + 54 B + 18 C) \cos [2 c] \sin [2 d x]}{360 d} +$$

$$\left. \frac{(3 A + B) \cos [3 c] \sin [3 d x]}{56 d} + \frac{A \cos [4 c] \sin [4 d x]}{144 d} \right) -$$

$$\frac{1}{21 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2}}$$

$$11 A \cos [c + d x]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\cot [c]]]^2\right]$$

$$\operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)$$

$$\operatorname{Sec}[d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\cot [c]]]}$$

$$\sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\cot [c]]]} -$$

$$\frac{1}{21 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2}}$$

$$13 B \cos [c+d x]^5 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right]$$

$$\sec \left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 (A+B \sec [c+d x]+C \sec [c+d x]^2)$$

$$\sec [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]}$$

$$\sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} - 1}$$

$$d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\cot [c]^2}$$

$$C \cos [c+d x]^5 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right]$$

$$\sec \left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 (A+B \sec [c+d x]+C \sec [c+d x]^2)$$

$$\sec [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]}$$

$$\sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} - 1}$$

$$\left( 17 A \cos [c+d x]^5 \csc [c] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 (A+B \sec [c+d x]+C \sec [c+d x]^2) \right)$$

$$\left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\tan [c]]]^2\right] \right)$$

$$\sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c] \left/ \left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \right) \right.$$

$$\sqrt{1+\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2}$$

$$\left. \left. \sqrt{1+\tan [c]^2} \right) - \frac{\frac{\sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}{\cos [c]^2+\sin [c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2}} \right) \left/ \right.$$

$$(30 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])) -$$

$$\left( 7 B \cos [c+d x]^5 \csc [c] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 (A+B \sec [c+d x]+C \sec [c+d x]^2) \right)$$

$$\left( \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \right]^2 \right) \right.$$

$$\left. \frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 - \cos [d x + \text{ArcTan} [\text{Tan} [c]]]}}, \right.$$

$$\left. \frac{\sqrt{1 + \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2}}{\sqrt{1 + \tan [c]^2}} - \frac{\frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2}} \right) \left. \right) /$$

$$(10 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) -$$

$$\left( 9 C \cos [c + d x]^5 \csc [c] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 (a + a \sec [c + d x])^3 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right)$$

$$\left( \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \right]^2 \right) \right.$$

$$\left. \frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 - \cos [d x + \text{ArcTan} [\text{Tan} [c]]]}}, \right.$$

$$\left. \frac{\sqrt{1 + \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2}}{\sqrt{1 + \tan [c]^2}} - \frac{\frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2}} \right) \left. \right) /$$

$$(10 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]))$$

**Problem 1204: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c + d x]^{7/2} (a + a \sec [c + d x])^3 (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 4, 227 leaves, 9 steps):

$$\frac{4 a^3 (7 A+9 B+5 C) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 d} + \frac{4 a^3 (13 A+21 B+35 C) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{21 d} +$$

$$\frac{4 a^3 (41 A+42 B-35 C) \sqrt{\cos [c+d x]} \sin [c+d x]}{105 d} + \frac{2 C (a+a \cos [c+d x])^3 \sin [c+d x]}{d \sqrt{\cos [c+d x]}} +$$

$$\frac{2 (A-7 C) \sqrt{\cos [c+d x]} (a^2+a^2 \cos [c+d x])^2 \sin [c+d x]}{7 a d} +$$

$$\frac{2 (11 A+7 B-35 C) \sqrt{\cos [c+d x]} (a^3+a^3 \cos [c+d x]) \sin [c+d x]}{35 d}$$

Result (type 5, 1688 leaves):

$$\frac{1}{A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]}$$

$$\cos [c+d x]^{11/2} \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 (A+B \sec [c+d x]+C \sec [c+d x]^2)$$

$$\left(-\frac{1}{20 d}(14 A+18 B+5 C+14 A \cos [2 c]+18 B \cos [2 c]+15 C \cos [2 c]) \csc [c] \sec [c]+$$

$$\frac{(107 A+84 B+28 C) \cos [d x] \sin [c]}{168 d}+\frac{(3 A+B) \cos [2 d x] \sin [2 c]}{20 d}+\right.$$

$$\frac{A \cos [3 d x] \sin [3 c]}{56 d}+\frac{(107 A+84 B+28 C) \cos [c] \sin [d x]}{168 d}+$$

$$\left.\frac{C \sec [c] \sec [c+d x] \sin [d x]}{2 d}+\frac{(3 A+B) \cos [2 c] \sin [2 d x]}{20 d}+\frac{A \cos [3 c] \sin [3 d x]}{56 d}\right)-$$

$$\frac{1}{21 d(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\cot [c]^2}}$$

$$13 A \cos [c+d x]^5 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]\right]^2$$

$$\sec \left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 (A+B \sec [c+d x]+C \sec [c+d x]^2)$$

$$\sec [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]}$$

$$\sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]}-}$$

$$\frac{1}{d(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\cot [c]^2}}$$

$$B \cos [c+d x]^5 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]\right]^2$$

$$\sec \left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 (A+B \sec [c+d x]+C \sec [c+d x]^2)$$

$$\sec [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]}$$

$$\sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]}-}$$

$$\begin{aligned}
 & \frac{1}{3 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2}} \\
 & 5 C \cos [c + d x]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\cot [c]]]^2\right] \\
 & \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\
 & \operatorname{Sec}[d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\cot [c]]]} \\
 & \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\cot [c]]]} -} \\
 & \left( 7 A \cos [c + d x]^5 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \left. \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos [d x + \operatorname{ArcTan}[\tan [c]]]^2\right] \right. \right. \\
 & \left. \left. \sin [d x + \operatorname{ArcTan}[\tan [c]]] \tan [c] \right) / \left( \sqrt{1 - \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \right. \right. \\
 & \left. \left. \sqrt{1 + \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}} \right. \right. \\
 & \left. \left. \sqrt{1 + \tan [c]^2} \right) - \frac{\frac{\sin [d x + \operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}}} \right) / \\
 & (10 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) - \\
 & \left( 9 B \cos [c + d x]^5 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \left. \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos [d x + \operatorname{ArcTan}[\tan [c]]]^2\right] \right. \right. \\
 & \left. \left. \sin [d x + \operatorname{ArcTan}[\tan [c]]] \tan [c] \right) / \left( \sqrt{1 - \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \right. \right.
 \end{aligned}$$

$$\left( \frac{\sqrt{1 + \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2}}{\sqrt{1 + \tan [c]^2}} - \frac{\frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2}} \right) /$$

$$(10 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) -$$

$$\left( C \cos [c + d x]^5 \csc [c] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 (a + a \sec [c + d x])^3 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right.$$

$$\left. \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \text{ArcTan} [\text{Tan} [c]] \right]^2 \right] \right)$$

$$\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \tan [c] \Big/ \left( \sqrt{1 - \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \right.$$

$$\left. \frac{\sqrt{1 + \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2}}{\sqrt{1 + \tan [c]^2}} - \frac{\frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2}} \right) /$$

$$(2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]))$$

**Problem 1205: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c + d x]^{5/2} (a + a \sec [c + d x])^3 (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 4, 226 leaves, 9 steps):

$$\frac{4 a^3 (9 A+5 B-5 C) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 d} +$$

$$\frac{4 a^3 (3 A+5(B+C)) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{3 d} + \frac{4 a^3 (6 A-5 B-20 C) \sqrt{\cos [c+d x]} \sin [c+d x]}{15 d} +$$

$$\frac{2 C(a+a \cos [c+d x])^3 \sin [c+d x]}{3 d \cos [c+d x]^{3 / 2}} + \frac{2(B+2 C)\left(a^2+a^2 \cos [c+d x]\right)^2 \sin [c+d x]}{a d \sqrt{\cos [c+d x]}} +$$

$$\frac{2(3 A-15 B-35 C) \sqrt{\cos [c+d x]}\left(a^3+a^3 \cos [c+d x]\right) \sin [c+d x]}{15 d}$$

Result (type 5, 1672 leaves):

$$\left(\cos [c+d x]^{11 / 2} \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^6(a+a \sec [c+d x])^3(A+B \sec [c+d x]+C \sec [c+d x]^2)\right.$$

$$\left(-\frac{1}{20 d}(18 A+5 B-25 C+18 A \cos [2 c]+15 B \cos [2 c]+5 C \cos [2 c]) \operatorname{Csc}[c] \operatorname{Sec}[c]+$$

$$\frac{(3 A+B) \cos [d x] \sin [c]}{6 d}+\frac{A \cos [2 d x] \sin [2 c]}{20 d}+\right.$$

$$\frac{(3 A+B) \cos [c] \sin [d x]}{6 d}+\frac{C \sec [c] \sec [c+d x]^2 \sin [d x]}{6 d}+$$

$$\left.\left.\frac{\sec [c] \sec [c+d x](C \sin [c]+3 B \sin [d x]+9 C \sin [d x])}{6 d}+\frac{A \cos [2 c] \sin [2 d x]}{20 d}\right)\right) /$$

$$\frac{(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])}{1}-$$

$$d(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\cot [c]^2}$$

$$A \cos [c+d x]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right]$$

$$\sec \left[\frac{c}{2}+\frac{d x}{2}\right]^6(a+a \sec [c+d x])^3(A+B \sec [c+d x]+C \sec [c+d x]^2)$$

$$\sec [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]}$$

$$\sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]}-}$$

$$\frac{1}{1}}$$

$$\frac{3 d(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\cot [c]^2}}{1}$$

$$5 B \cos [c+d x]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right]$$

$$\sec \left[\frac{c}{2}+\frac{d x}{2}\right]^6(a+a \sec [c+d x])^3(A+B \sec [c+d x]+C \sec [c+d x]^2)$$

$$\sec [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]}$$

$$\sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]}-}$$

$$\frac{1}{1}}$$

$$\frac{3 d(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\cot [c]^2}}{1}$$



$$\begin{aligned}
 & 5 C \cos [c+d x]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \\
 & \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^3 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \\
 & \operatorname{Sec}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \sqrt{-\sqrt{1+\operatorname{Cot}[c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} -} \\
 & \left(9 A \cos [c+d x]^5 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^3 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2)\right. \\
 & \left.\left(\operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]^2\right]\right.\right. \\
 & \left.\left.\operatorname{Sin}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]\right) / \left(\sqrt{1-\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]}\right.\right. \\
 & \left.\left.\sqrt{1+\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]}\right) \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1+\operatorname{Tan}[c]^2}}\right. \\
 & \left.\left.\sqrt{1+\operatorname{Tan}[c]^2}\right) - \frac{\frac{\operatorname{Sin}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1+\operatorname{Tan}[c]^2}} + \frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1+\operatorname{Tan}[c]^2}}{\cos [c]^2+\sin [c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1+\operatorname{Tan}[c]^2}}}\right) / \\
 & (10 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])) - \\
 & \left(B \cos [c+d x]^5 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^3 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2)\right. \\
 & \left.\left(\operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]^2\right]\right.\right. \\
 & \left.\left.\operatorname{Sin}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]\right) / \left(\sqrt{1-\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]}\right.\right. \\
 & \left.\left.\sqrt{1+\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]}\right) \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1+\operatorname{Tan}[c]^2}}\right)
 \end{aligned}$$

$$\left( \sqrt{1 + \tan[c]^2} \right) - \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c] + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{1 + \tan[c]^2}}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \Bigg) /$$

$$(2 d (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x])) +$$

$$\left( C \cos[c + d x]^5 \csc[c] \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \sec[c + d x])^3 (A + B \sec[c + d x] + C \sec[c + d x]^2) \right.$$

$$\left. \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos[d x + \text{ArcTan}[\tan[c]]]^2\right] \right) \right)$$

$$\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c] \Bigg) / \left( \sqrt{1 - \cos[d x + \text{ArcTan}[\tan[c]]]} \right)$$

$$\sqrt{1 + \cos[d x + \text{ArcTan}[\tan[c]]]} \sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}$$

$$\left( \sqrt{1 + \tan[c]^2} \right) - \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c] + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{1 + \tan[c]^2}}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \Bigg) /$$

$$(2 d (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]))$$

**Problem 1206: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c + d x]^{3/2} (a + a \sec[c + d x])^3 (A + B \sec[c + d x] + C \sec[c + d x]^2) dx$$

Optimal (type 4, 231 leaves, 9 steps):

$$\frac{4 a^3 (5 A-5 B-9 C) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 d} +$$

$$\frac{4 a^3 (5 A+5 B+3 C) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{3 d} - \frac{4 a^3 (5 A+20 B+21 C) \sqrt{\cos [c+d x]} \sin [c+d x]}{15 d} +$$

$$\frac{2 C (a+a \cos [c+d x])^3 \sin [c+d x]}{5 d \cos [c+d x]^{5/2}} + \frac{2 (5 B+6 C) (a^2+a^2 \cos [c+d x])^2 \sin [c+d x]}{15 a d \cos [c+d x]^{3/2}} +$$

$$\frac{2 (15 A+35 B+33 C) (a^3+a^3 \cos [c+d x]) \sin [c+d x]}{15 d \sqrt{\cos [c+d x]}}$$

Result (type 5, 1673 leaves):

$$\frac{1}{A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]}$$

$$\cos [c+d x]^{11/2} \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 (A+B \sec [c+d x]+C \sec [c+d x]^2)$$

$$\left(-\frac{(5 A-25 B-36 C+15 A \cos [2 c]+5 B \cos [2 c]) \csc [c] \sec [c]}{20 d}+\right.$$

$$\frac{A \cos [d x] \sin [c]}{6 d}+\frac{A \cos [c] \sin [d x]}{6 d}+\frac{C \sec [c] \sec [c+d x]^3 \sin [d x]}{10 d}+\left.$$

$$\frac{\sec [c] \sec [c+d x]^2 (3 C \sin [c]+5 B \sin [d x]+15 C \sin [d x])}{30 d}+\frac{1}{30 d}\right.$$

$$\left.\sec [c] \sec [c+d x] (5 B \sin [c]+15 C \sin [c]+15 A \sin [d x]+45 B \sin [d x]+54 C \sin [d x])\right)-$$

$$\frac{1}{3 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\cot [c]^2}}$$

$$5 A \cos [c+d x]^5 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right]$$

$$\sec \left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 (A+B \sec [c+d x]+C \sec [c+d x]^2)$$

$$\sec [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]}$$

$$\sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]}-}$$

$$\frac{1}{3 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\cot [c]^2}}$$

$$5 B \cos [c+d x]^5 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right]$$

$$\sec \left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 (A+B \sec [c+d x]+C \sec [c+d x]^2)$$

$$\sec [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]}$$

$$\sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]}-}$$

$$\begin{aligned}
 & \frac{1}{d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2}} \\
 & C \cos [c + d x]^5 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\cot [c]]]^2\right] \\
 & \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\
 & \operatorname{Sec}[d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\cot [c]]]} \\
 & \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\cot [c]]]} -} \\
 & \left( A \cos [c + d x]^5 \csc [c] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \left. \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos [d x + \operatorname{ArcTan}[\tan [c]]]^2\right] \right. \right. \\
 & \left. \left. \sin [d x + \operatorname{ArcTan}[\tan [c]]] \tan [c] \right) / \left( \sqrt{1 - \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \right. \right. \\
 & \left. \left. \sqrt{1 + \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}} \right. \right. \\
 & \left. \left. \sqrt{1 + \tan [c]^2} \right) - \frac{\frac{\sin [d x + \operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}}} \right) / \\
 & (2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) + \\
 & \left( B \cos [c + d x]^5 \csc [c] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \left. \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos [d x + \operatorname{ArcTan}[\tan [c]]]^2\right] \right. \right. \\
 & \left. \left. \sin [d x + \operatorname{ArcTan}[\tan [c]]] \tan [c] \right) / \left( \sqrt{1 - \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left( \frac{\sqrt{1 + \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2}}{\sqrt{1 + \tan [c]^2}} - \frac{\frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2}} \right) \right) / \\
 & (2 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) + \\
 & \left( 9 C \cos [c + d x]^5 \csc [c] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 (a + a \sec [c + d x])^3 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \left. \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \text{ArcTan} [\text{Tan} [c]] \right]^2 \right] \right) \right. \\
 & \left. \sin [d x + \text{ArcTan} [\text{Tan} [c]]] \tan [c] \right) / \left( \sqrt{1 - \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \right) \\
 & \left. \left( \frac{\sqrt{1 + \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2}}{\sqrt{1 + \tan [c]^2}} - \frac{\frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2}} \right) \right) / \\
 & (10 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]))
 \end{aligned}$$

**Problem 1207: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sqrt{\cos [c + d x]} (a + a \sec [c + d x])^3 (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 4, 231 leaves, 9 steps):

$$\begin{aligned}
 & - \frac{4 a^3 (5 A+9 B+7 C) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 d} + \frac{4 a^3 (35 A+21 B+13 C) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{21 d} + \\
 & \frac{4 a^3 (140 A+147 B+106 C) \operatorname{Sin}[c+d x]}{105 d \sqrt{\operatorname{Cos}[c+d x]}} + \frac{2 C (a+a \operatorname{Cos}[c+d x])^3 \operatorname{Sin}[c+d x]}{7 d \operatorname{Cos}[c+d x]^{7 / 2}} + \\
 & \frac{2 (7 B+6 C) (a^2+a^2 \operatorname{Cos}[c+d x])^2 \operatorname{Sin}[c+d x]}{35 a d \operatorname{Cos}[c+d x]^{5 / 2}} + \frac{2 (5 A+9 B+7 C) (a^3+a^3 \operatorname{Cos}[c+d x]) \operatorname{Sin}[c+d x]}{15 d \operatorname{Cos}[c+d x]^{3 / 2}}
 \end{aligned}$$

Result (type 5, 1692 leaves):

$$\begin{aligned}
 & \frac{1}{A+2 C+2 B \operatorname{Cos}[c+d x]+A \operatorname{Cos}[2 c+2 d x]} \\
 & \operatorname{Cos}[c+d x]^{11 / 2} \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^3 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \\
 & \left( - \frac{(-25 A-36 B-28 C+5 A \operatorname{Cos}[2 c]) \operatorname{Csc}[c] \operatorname{Sec}[c]}{20 d} + \frac{C \operatorname{Sec}[c] \operatorname{Sec}[c+d x]^4 \operatorname{Sin}[d x]}{14 d} + \right. \\
 & \frac{\operatorname{Sec}[c] \operatorname{Sec}[c+d x]^3 (5 C \operatorname{Sin}[c]+7 B \operatorname{Sin}[d x]+21 C \operatorname{Sin}[d x])}{70 d} + \frac{1}{210 d} \operatorname{Sec}[c] \\
 & \operatorname{Sec}[c+d x]^2 (21 B \operatorname{Sin}[c]+63 C \operatorname{Sin}[c]+35 A \operatorname{Sin}[d x]+105 B \operatorname{Sin}[d x]+130 C \operatorname{Sin}[d x]) + \\
 & \left. \frac{1}{210 d} \operatorname{Sec}[c] \operatorname{Sec}[c+d x] (35 A \operatorname{Sin}[c]+105 B \operatorname{Sin}[c]+130 C \operatorname{Sin}[c]+ \right. \\
 & \left. 315 A \operatorname{Sin}[d x]+378 B \operatorname{Sin}[d x]+294 C \operatorname{Sin}[d x]) \right) - \\
 & \frac{1}{3 d (A+2 C+2 B \operatorname{Cos}[c+d x]+A \operatorname{Cos}[2 c+2 d x]) \sqrt{1+\operatorname{Cot}[c]^2}} \\
 & 5 A \operatorname{Cos}[c+d x]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \\
 & \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^3 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \\
 & \operatorname{Sec}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1-\operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \sqrt{-\sqrt{1+\operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1+\operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} - \\
 & \frac{1}{d (A+2 C+2 B \operatorname{Cos}[c+d x]+A \operatorname{Cos}[2 c+2 d x]) \sqrt{1+\operatorname{Cot}[c]^2}} \\
 & B \operatorname{Cos}[c+d x]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \\
 & \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^3 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \\
 & \operatorname{Sec}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1-\operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \sqrt{-\sqrt{1+\operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1+\operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} - \\
 & \frac{1}{21 d (A+2 C+2 B \operatorname{Cos}[c+d x]+A \operatorname{Cos}[2 c+2 d x]) \sqrt{1+\operatorname{Cot}[c]^2}}
 \end{aligned}$$

$$13 C \cos [c+d x]^5 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right]$$

$$\sec \left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 (A+B \sec [c+d x]+C \sec [c+d x]^2)$$

$$\sec [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]}$$

$$\sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} +$$

$$\left( A \cos [c+d x]^5 \csc [c] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 (A+B \sec [c+d x]+C \sec [c+d x]^2) \right.$$

$$\left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\tan [c]]]^2\right] \right.$$

$$\left. \sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c] \right) / \left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \right.$$

$$\left. \sqrt{1+\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2} \right.$$

$$\left. \left. \sqrt{1+\tan [c]^2} \right) - \frac{\frac{\sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}{\cos [c]^2+\sin [c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2}} \right) /$$

$$(2 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])) +$$

$$\left( 9 B \cos [c+d x]^5 \csc [c] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 (A+B \sec [c+d x]+C \sec [c+d x]^2) \right.$$

$$\left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\tan [c]]]^2\right] \right.$$

$$\left. \sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c] \right) / \left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \right.$$

$$\left. \sqrt{1+\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2} \right.$$

$$\left( \sqrt{1 + \tan[c]^2} \right) - \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c] + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{1 + \tan[c]^2}}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \Bigg) /$$

$$(10 d (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x])) +$$

$$\left( 7 C \cos[c + d x]^5 \csc[c] \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \sec[c + d x])^3 (A + B \sec[c + d x] + C \sec[c + d x]^2) \right.$$

$$\left. \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos[d x + \text{ArcTan}[\tan[c]]]^2\right] \right) \right)$$

$$\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c] \Bigg) / \left( \sqrt{1 - \cos[d x + \text{ArcTan}[\tan[c]]]} \right)$$

$$\sqrt{1 + \cos[d x + \text{ArcTan}[\tan[c]]]} \sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}$$

$$\left( \sqrt{1 + \tan[c]^2} \right) - \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c] + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{1 + \tan[c]^2}}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \Bigg) /$$

$$(10 d (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]))$$

**Problem 1208: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \sec[c + d x])^3 (A + B \sec[c + d x] + C \sec[c + d x]^2)}{\sqrt{\cos[c + d x]}} dx$$

Optimal (type 4, 267 leaves, 10 steps):



$$\begin{aligned}
 & - \frac{4 a^3 (27 A + 21 B + 17 C) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{15 d} + \\
 & \frac{4 a^3 (21 A + 13 B + 11 C) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{21 d} + \\
 & \frac{4 a^3 (42 A + 41 B + 32 C) \operatorname{Sin}[c+d x]}{105 d \operatorname{Cos}[c+d x]^{3/2}} + \frac{4 a^3 (27 A + 21 B + 17 C) \operatorname{Sin}[c+d x]}{15 d \sqrt{\operatorname{Cos}[c+d x]}} + \\
 & \frac{2 C (a + a \operatorname{Cos}[c+d x])^3 \operatorname{Sin}[c+d x]}{9 d \operatorname{Cos}[c+d x]^{9/2}} + \frac{2 (3 B + 2 C) (a^2 + a^2 \operatorname{Cos}[c+d x])^2 \operatorname{Sin}[c+d x]}{21 a d \operatorname{Cos}[c+d x]^{7/2}} + \\
 & \frac{2 (63 A + 99 B + 73 C) (a^3 + a^3 \operatorname{Cos}[c+d x]) \operatorname{Sin}[c+d x]}{315 d \operatorname{Cos}[c+d x]^{5/2}}
 \end{aligned}$$

Result (type 5, 1739 leaves):

$$\begin{aligned}
 & \frac{1}{A + 2 C + 2 B \operatorname{Cos}[c+d x] + A \operatorname{Cos}[2 c + 2 d x]} \\
 & \operatorname{Cos}[c+d x]^{11/2} \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \operatorname{Sec}[c+d x])^3 (A + B \operatorname{Sec}[c+d x] + C \operatorname{Sec}[c+d x]^2) \\
 & \left( \frac{(27 A + 21 B + 17 C) \operatorname{Csc}[c] \operatorname{Sec}[c]}{15 d} + \frac{C \operatorname{Sec}[c] \operatorname{Sec}[c+d x]^5 \operatorname{Sin}[d x]}{18 d} + \right. \\
 & \left. \frac{\operatorname{Sec}[c] \operatorname{Sec}[c+d x]^4 (7 C \operatorname{Sin}[c] + 9 B \operatorname{Sin}[d x] + 27 C \operatorname{Sin}[d x])}{126 d} + \frac{1}{630 d} \operatorname{Sec}[c] \operatorname{Sec}[c+d x]^3 \right. \\
 & \left. (45 B \operatorname{Sin}[c] + 135 C \operatorname{Sin}[c] + 63 A \operatorname{Sin}[d x] + 189 B \operatorname{Sin}[d x] + 238 C \operatorname{Sin}[d x]) + \frac{1}{210 d} \right. \\
 & \left. \operatorname{Sec}[c] \operatorname{Sec}[c+d x] (105 A \operatorname{Sin}[c] + 130 B \operatorname{Sin}[c] + 110 C \operatorname{Sin}[c] + 378 A \operatorname{Sin}[d x] + \right. \\
 & \left. 294 B \operatorname{Sin}[d x] + 238 C \operatorname{Sin}[d x]) + \frac{1}{630 d} \operatorname{Sec}[c] \operatorname{Sec}[c+d x]^2 (63 A \operatorname{Sin}[c] + \right. \\
 & \left. 189 B \operatorname{Sin}[c] + 238 C \operatorname{Sin}[c] + 315 A \operatorname{Sin}[d x] + 390 B \operatorname{Sin}[d x] + 330 C \operatorname{Sin}[d x]) \right) - \\
 & \frac{1}{d (A + 2 C + 2 B \operatorname{Cos}[c+d x] + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2}} \\
 & A \operatorname{Cos}[c+d x]^5 \operatorname{Csc}[c] \\
 & \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \\
 & \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \operatorname{Sec}[c+d x])^3 (A + B \operatorname{Sec}[c+d x] + C \operatorname{Sec}[c+d x]^2) \\
 & \operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1 + \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} - \\
 & \frac{1}{21 d (A + 2 C + 2 B \operatorname{Cos}[c+d x] + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2}} \\
 & 13 B \operatorname{Cos}[c+d x]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right]
 \end{aligned}$$

$$\begin{aligned}
 & \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \text{Sec}[c + dx])^3 (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \\
 & \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \\
 & \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 + \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} -} \\
 & \frac{1}{21 d (A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2 c + 2 dx]) \sqrt{1 + \text{Cot}[c]^2}} \\
 & 11 C \text{Cos}[c + dx]^5 \text{Csc}[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]^2\right] \\
 & \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \text{Sec}[c + dx])^3 (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \\
 & \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \\
 & \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 + \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} +} \\
 & \left( 9 A \text{Cos}[c + dx]^5 \text{Csc}[c] \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \text{Sec}[c + dx])^3 (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \right. \\
 & \left. \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]]^2\right] \right. \right. \\
 & \left. \left. \text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] \right) / \left( \sqrt{1 - \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]]} \right. \right. \\
 & \left. \left. \sqrt{1 + \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{\text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right. \right. \\
 & \left. \left. \sqrt{1 + \text{Tan}[c]^2} \right) - \frac{\frac{\text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \frac{2 \text{Cos}[c]^2 \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}}{\text{Cos}[c]^2 + \text{Sin}[c]^2}}{\sqrt{\text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}}} \right) / \\
 & (10 d (A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2 c + 2 dx])) + \\
 & \left( 7 B \text{Cos}[c + dx]^5 \text{Csc}[c] \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \text{Sec}[c + dx])^3 (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \right.
 \end{aligned}$$

$$\left( \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \text{ArcTan} [\text{Tan} [c]]]^2 \right] \right. \right.$$

$$\left. \left. \frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 - \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \right) \right) / \left( \sqrt{1 + \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2} \right.$$

$$\left. \left. \left. \left. \sqrt{1 + \tan [c]^2} \right) - \frac{\frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2}} \right) \right) \right) /$$

$$(10 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) +$$

$$\left( 17 C \cos [c + d x]^5 \csc [c] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 (a + a \sec [c + d x])^3 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right)$$

$$\left( \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \text{ArcTan} [\text{Tan} [c]]]^2 \right] \right. \right.$$

$$\left. \left. \frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 - \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \right) \right) / \left( \sqrt{1 + \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2} \right.$$

$$\left. \left. \left. \left. \sqrt{1 + \tan [c]^2} \right) - \frac{\frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2}} \right) \right) \right) /$$

$$(30 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]))$$

**Problem 1209: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c + d x]^{13/2} (a + a \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 4, 310 leaves, 11 steps):

$$\begin{aligned} & \frac{8 a^4 (185 A + 208 B + 247 C) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{195 d} + \\ & \frac{8 a^4 (100 A + 113 B + 132 C) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{231 d} + \\ & \frac{8 a^4 (100 A + 113 B + 132 C) \sqrt{\cos [c+d x]} \sin [c+d x]}{231 d} + \\ & \frac{4 a^4 (5255 A + 6019 B + 6721 C) \cos [c+d x]^{3/2} \sin [c+d x]}{15015 d} + \\ & \frac{2 a (8 A + 13 B) \cos [c+d x]^{3/2} (a+a \cos [c+d x])^3 \sin [c+d x]}{143 d} + \\ & \frac{2 A \cos [c+d x]^{3/2} (a+a \cos [c+d x])^4 \sin [c+d x]}{13 d} + \frac{1}{99 d} \\ & 2 (13 A + 17 B + 11 C) \cos [c+d x]^{3/2} (a^2+a^2 \cos [c+d x])^2 \sin [c+d x] + \frac{1}{9009 d} \\ & 4 (1355 A + 1612 B + 1573 C) \cos [c+d x]^{3/2} (a^4+a^4 \cos [c+d x]) \sin [c+d x] \end{aligned}$$

Result (type 5, 1416 leaves):

$$\begin{aligned} & a^4 \left( \sqrt{\cos [c+d x]} (1+\cos [c+d x])^4 \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^8 \right. \\ & \left( -\frac{(185 A+208 B+247 C) \cot [c]}{390 d} + \frac{(3764 A+4087 B+4488 C) \cos [d x] \sin [c]}{14784 d} + \right. \\ & \frac{(15625 A+15392 B+13208 C) \cos [2 d x] \sin [2 c]}{149760 d} + \\ & \frac{(404 A+321 B+176 C) \cos [3 d x] \sin [3 c]}{9856 d} + \\ & \frac{(98 A+52 B+13 C) \cos [4 d x] \sin [4 c]}{7488 d} + \frac{(4 A+B) \cos [5 d x] \sin [5 c]}{1408 d} + \\ & \frac{A \cos [6 d x] \sin [6 c]}{3328 d} + \frac{(3764 A+4087 B+4488 C) \cos [c] \sin [d x]}{14784 d} + \\ & \frac{(15625 A+15392 B+13208 C) \cos [2 c] \sin [2 d x]}{149760 d} + \\ & \frac{(404 A+321 B+176 C) \cos [3 c] \sin [3 d x]}{9856 d} + \frac{(98 A+52 B+13 C) \cos [4 c] \sin [4 d x]}{7488 d} + \\ & \left. \frac{(4 A+B) \cos [5 c] \sin [5 d x]}{1408 d} + \frac{A \cos [6 c] \sin [6 d x]}{3328 d} \right) - \\ & \left( 50 A (1+\cos [c+d x])^4 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]\right]^2 \right) \end{aligned}$$

$$\begin{aligned}
 & \left. \begin{aligned}
 & \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^8 \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \\
 & \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 + \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}
 \end{aligned} \right) / \\
 & \left( 231 d \sqrt{1 + \text{Cot}[c]^2} \right) - \left( 113 B (1 + \text{Cos}[c + dx])^4 \text{Csc}[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \right. \right. \\
 & \left. \left. \left\{\frac{5}{4}\right\}, \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]^2\right] \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^8 \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \right. \\
 & \left. \sqrt{1 - \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right. \\
 & \left. \sqrt{1 + \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right) / \left( 462 d \sqrt{1 + \text{Cot}[c]^2} \right) - \\
 & \left( 2 C (1 + \text{Cos}[c + dx])^4 \text{Csc}[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]^2\right] \right. \\
 & \left. \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^8 \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right. \\
 & \left. \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 + \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right) / \\
 & \left( 7 d \sqrt{1 + \text{Cot}[c]^2} \right) - \frac{1}{156 d} 37 A (1 + \text{Cos}[c + dx])^4 \text{Csc}[c] \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^8 \\
 & \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]]^2\right] \right. \\
 & \left. \text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] \right) / \\
 & \left( \sqrt{1 - \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]]} \right. \\
 & \left. \sqrt{\text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \sqrt{1 + \text{Tan}[c]^2}} \right) - \\
 & \left. \frac{\frac{\text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \frac{2 \text{Cos}[c]^2 \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}}{\text{Cos}[c]^2 + \text{Sin}[c]^2}}{\sqrt{\text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}}} \right) - \frac{1}{15 d}
 \end{aligned}$$

$$\begin{aligned}
 & 4 B (1 + \cos [c + d x])^4 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^8 \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \right. \right. \\
 & \quad \left. \left. \left\{\frac{3}{4}\right\}, \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]^2\right] \operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]\right) / \\
 & \left( \sqrt{1 - \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right. \\
 & \quad \left. \sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \operatorname{Tan}[c]^2} \sqrt{1 + \operatorname{Tan}[c]^2} \right) - \\
 & \left. \frac{\operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] + \frac{2 \cos [c]^2 \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}}{\cos [c]^2 + \operatorname{Sin}[c]^2}}{\sqrt{1 + \operatorname{Tan}[c]^2}} \right) - \\
 & \quad \left. \sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \operatorname{Tan}[c]^2} \right) - \\
 & \frac{1}{60 d} 19 C (1 + \cos [c + d x])^4 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^8 \\
 & \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]^2\right] \right. \\
 & \quad \left. \operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]\right) / \\
 & \left( \sqrt{1 - \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right. \\
 & \quad \left. \sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \operatorname{Tan}[c]^2} \sqrt{1 + \operatorname{Tan}[c]^2} \right) - \\
 & \left. \frac{\operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] + \frac{2 \cos [c]^2 \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}}{\cos [c]^2 + \operatorname{Sin}[c]^2}}{\sqrt{1 + \operatorname{Tan}[c]^2}} \right) \left. \right)
 \end{aligned}$$

**Problem 1210: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c + d x]^{11/2} (a + a \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 4, 274 leaves, 10 steps):

$$\begin{aligned} & \frac{8 a^4 (16 A+19 B+24 C) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{15 d} + \\ & \frac{8 a^4 (113 A+132 B+187 C) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{231 d} + \\ & \frac{4 a^4 (667 A+803 B+913 C) \sqrt{\cos [c+d x]} \sin [c+d x]}{1155 d} + \\ & \frac{2 a (8 A+11 B) \sqrt{\cos [c+d x]} (a+a \cos [c+d x])^3 \sin [c+d x]}{99 d} + \\ & \frac{2 A \sqrt{\cos [c+d x]} (a+a \cos [c+d x])^4 \sin [c+d x]}{11 d} + \frac{1}{231 d} \\ & 2 (43 A+55 B+33 C) \sqrt{\cos [c+d x]} (a^2+a^2 \cos [c+d x])^2 \sin [c+d x] + \frac{1}{3465 d} \\ & 4 (769 A+946 B+891 C) \sqrt{\cos [c+d x]} (a^4+a^4 \cos [c+d x]) \sin [c+d x] \end{aligned}$$

Result (type 5, 1751 leaves):

$$\begin{aligned} & \frac{1}{A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]} \\ & \cos [c+d x]^{13 / 2} \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \sec [c+d x])^4 (A+B \sec [c+d x]+C \sec [c+d x]^2) \\ & \left( -\frac{(16 A+19 B+24 C) \cot [c]}{15 d} + \frac{(4087 A+4488 B+4202 C) \cos [d x] \sin [c]}{7392 d} + \right. \\ & \quad \frac{(148 A+127 B+72 C) \cos [2 d x] \sin [2 c]}{720 d} + \\ & \quad \frac{(321 A+176 B+44 C) \cos [3 d x] \sin [3 c]}{4928 d} + \frac{(4 A+B) \cos [4 d x] \sin [4 c]}{288 d} + \\ & \quad \frac{A \cos [5 d x] \sin [5 c]}{704 d} + \frac{(4087 A+4488 B+4202 C) \cos [c] \sin [d x]}{7392 d} + \\ & \quad \frac{(148 A+127 B+72 C) \cos [2 c] \sin [2 d x]}{720 d} + \frac{(321 A+176 B+44 C) \cos [3 c] \sin [3 d x]}{4928 d} \\ & \quad \left. \frac{(4 A+B) \cos [4 c] \sin [4 d x]}{288 d} + \frac{A \cos [5 c] \sin [5 d x]}{704 d} \right) - \\ & \frac{1}{231 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\cot [c]^2}} \\ & 113 A \cos [c+d x]^6 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right] \\ & \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \sec [c+d x])^4 (A+B \sec [c+d x]+C \sec [c+d x]^2) \\ & \operatorname{Sec}[d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \\ & \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} -} \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{7 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2}} \\
 & 4 B \cos [c + d x]^6 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\cot [c]]]^2\right] \\
 & \sec \left[\frac{c}{2} + \frac{d x}{2}\right]^8 (a + a \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \sec [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\cot [c]]]} \\
 & \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\cot [c]]]} -} \\
 & \frac{1}{21 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2}} \\
 & 17 C \cos [c + d x]^6 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\cot [c]]]^2\right] \\
 & \sec \left[\frac{c}{2} + \frac{d x}{2}\right]^8 (a + a \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \sec [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\cot [c]]]} \\
 & \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\cot [c]]]} -} \\
 & \left( 8 A \cos [c + d x]^6 \csc [c] \sec \left[\frac{c}{2} + \frac{d x}{2}\right]^8 (a + a \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \left. \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos [d x + \operatorname{ArcTan}[\tan [c]]]^2\right] \right) \right. \\
 & \left. \left. \frac{\sin [d x + \operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1 - \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \right)} \right. \\
 & \left. \frac{\sqrt{1 + \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}}}{\sqrt{1 + \tan [c]^2}} \right) - \frac{\frac{\sin [d x + \operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}}} \left. \right) / \\
 & (15 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) -
 \end{aligned}$$



$$\left( 19 B \cos [c+d x]^6 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \operatorname{Sec}[c+d x])^4 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \right)$$

$$\left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\},\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]^2\right]\right)$$

$$\sin [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] \Big/ \left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right)$$

$$\sqrt{1+\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1+\operatorname{Tan}[c]^2}$$

$$\left. \left( \sqrt{1+\operatorname{Tan}[c]^2} \right) - \frac{\frac{\sin [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1+\operatorname{Tan}[c]^2}} + \frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1+\operatorname{Tan}[c]^2}}{\cos [c]^2+\sin [c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1+\operatorname{Tan}[c]^2}} \right) \Big/$$

$$(30 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])) -$$

$$\left( 4 C \cos [c+d x]^6 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \operatorname{Sec}[c+d x])^4 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \right)$$

$$\left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\},\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]^2\right]\right)$$

$$\sin [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] \Big/ \left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right)$$

$$\sqrt{1+\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1+\operatorname{Tan}[c]^2}$$

$$\left. \left( \sqrt{1+\operatorname{Tan}[c]^2} \right) - \frac{\frac{\sin [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1+\operatorname{Tan}[c]^2}} + \frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1+\operatorname{Tan}[c]^2}}{\cos [c]^2+\sin [c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1+\operatorname{Tan}[c]^2}} \right) \Big/$$

$$(5 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]))$$

**Problem 1211: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c+d x]^{9 / 2}\left(a+a \sec [c+d x]\right)^4\left(A+B \sec [c+d x]+C \sec [c+d x]^2\right) d x$$

Optimal (type 4, 270 leaves, 10 steps):

$$\begin{aligned} & \frac{8 a^4\left(19 A+24 B+21 C\right) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{15 d}+ \\ & \frac{8 a^4\left(12 A+17 B+28 C\right) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{21 d}+ \\ & \frac{4 a^4\left(73 A+83 B+7 C\right) \sqrt{\cos [c+d x]} \sin [c+d x]}{105 d}+ \\ & \frac{2 a(A-9 C) \sqrt{\cos [c+d x]}\left(a+a \cos [c+d x]\right)^3 \sin [c+d x]}{9 d}+ \\ & \frac{2 C\left(a+a \cos [c+d x]\right)^4 \sin [c+d x]}{d \sqrt{\cos [c+d x]}}+ \\ & \frac{2\left(5 A+3 B-21 C\right) \sqrt{\cos [c+d x]}\left(a^2+a^2 \cos [c+d x]\right)^2 \sin [c+d x]}{21 d}+\frac{1}{315 d} \\ & 4\left(86 A+81 B-126 C\right) \sqrt{\cos [c+d x]}\left(a^4+a^4 \cos [c+d x]\right) \sin [c+d x] \end{aligned}$$

Result (type 5, 1742 leaves):

$$\begin{aligned} & \frac{1}{A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]} \\ & \cos [c+d x]^{13 / 2} \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^8\left(a+a \sec [c+d x]\right)^4\left(A+B \sec [c+d x]+C \sec [c+d x]^2\right) \\ & \left(-\frac{1}{120 d}\left(76 A+96 B+69 C+76 A \cos [2 c]+96 B \cos [2 c]+99 C \cos [2 c]\right) \operatorname{Csc}[c] \operatorname{Sec}[c]+ \right. \\ & \quad \frac{\left(204 A+191 B+112 C\right) \cos [d x] \sin [c]}{336 d}+ \\ & \quad \frac{\left(127 A+72 B+18 C\right) \cos [2 d x] \sin [2 c]}{720 d}+\frac{\left(4 A+B\right) \cos [3 d x] \sin [3 c]}{112 d}+ \\ & \quad \frac{A \cos [4 d x] \sin [4 c]}{288 d}+\frac{\left(204 A+191 B+112 C\right) \cos [c] \sin [d x]}{336 d}+ \\ & \quad \frac{C \operatorname{Sec}[c] \operatorname{Sec}[c+d x] \sin [d x]}{4 d}+\frac{\left(127 A+72 B+18 C\right) \cos [2 c] \sin [2 d x]}{720 d}+ \\ & \quad \left.\frac{\left(4 A+B\right) \cos [3 c] \sin [3 d x]}{112 d}+\frac{A \cos [4 c] \sin [4 d x]}{288 d}\right) \frac{1}{7 d\left(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]\right) \sqrt{1+\operatorname{Cot}[c]^2}} \end{aligned}$$

$$4 A \cos [c+d x]^6 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right]$$

$$\sec \left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \sec [c+d x])^4 (A+B \sec [c+d x]+C \sec [c+d x]^2)$$

$$\sec [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]}$$

$$\sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} -$$

$$1$$

$$21 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\cot [c]^2}$$

$$17 B \cos [c+d x]^6 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right]$$

$$\sec \left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \sec [c+d x])^4 (A+B \sec [c+d x]+C \sec [c+d x]^2)$$

$$\sec [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]}$$

$$\sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} -$$

$$1$$

$$3 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\cot [c]^2}$$

$$4 C \cos [c+d x]^6 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right]$$

$$\sec \left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \sec [c+d x])^4 (A+B \sec [c+d x]+C \sec [c+d x]^2)$$

$$\sec [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]}$$

$$\sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} -$$

$$\left( 19 A \cos [c+d x]^6 \csc [c] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \sec [c+d x])^4 (A+B \sec [c+d x]+C \sec [c+d x]^2) \right)$$

$$\left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\tan [c]]]^2\right] \right)$$

$$\sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c] \Big/ \left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \right)$$

$$\sqrt{1+\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2}$$

$$\left. \left. \left. \sqrt{1 + \tan [c]^2} \right) - \frac{\frac{\sin [d x + \text{ArcTan} [\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2}}} \right) \right) /$$

$$(30 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) -$$

$$\left( 4 B \cos [c + d x]^6 \csc [c] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 (a + a \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right)$$

$$\left( \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \text{ArcTan} [\tan [c]]]^2 \right] \right) \right)$$

$$\sin [d x + \text{ArcTan} [\tan [c]]] \tan [c] \left/ \left( \sqrt{1 - \cos [d x + \text{ArcTan} [\tan [c]]]} \right) \right.$$

$$\sqrt{1 + \cos [d x + \text{ArcTan} [\tan [c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2}}$$

$$\left. \left. \left. \sqrt{1 + \tan [c]^2} \right) - \frac{\frac{\sin [d x + \text{ArcTan} [\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2}}} \right) \right) /$$

$$(5 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) -$$

$$\left( 7 C \cos [c + d x]^6 \csc [c] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 (a + a \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right)$$

$$\left( \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \text{ArcTan} [\tan [c]]]^2 \right] \right) \right)$$

$$\sin [d x + \text{ArcTan} [\tan [c]]] \tan [c] \left/ \left( \sqrt{1 - \cos [d x + \text{ArcTan} [\tan [c]]]} \right) \right.$$

$$\sqrt{1 + \cos [d x + \text{ArcTan} [\tan [c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2}}$$

$$\left. \left. \left. \sqrt{1 + \tan [c]^2} \right) - \frac{\frac{\sin [d x + \text{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}}} \right) \right) /$$

$$(10 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]))$$

**Problem 1212: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c + d x]^{7/2} (a + a \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 4, 269 leaves, 10 steps):

$$\frac{8 a^4 (8 A + 7 B) \text{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{5 d} + \frac{8 a^4 (17 A + 28 B + 35 C) \text{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{21 d} +$$

$$\frac{4 a^4 (83 A + 7 B - 175 C) \sqrt{\cos [c + d x]} \sin [c + d x]}{105 d} +$$

$$\frac{2 a (3 B + 8 C) (a + a \cos [c + d x])^3 \sin [c + d x]}{3 d \sqrt{\cos [c + d x]}} + \frac{2 C (a + a \cos [c + d x])^4 \sin [c + d x]}{3 d \cos [c + d x]^{3/2}} +$$

$$\frac{2 (A - 7 B - 21 C) \sqrt{\cos [c + d x]} (a^2 + a^2 \cos [c + d x])^2 \sin [c + d x]}{7 d} + \frac{1}{105 d}$$

$$4 (27 A - 42 B - 175 C) \sqrt{\cos [c + d x]} (a^4 + a^4 \cos [c + d x]) \sin [c + d x]$$

Result (type 5, 1451 leaves):

$$\frac{1}{A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]}$$

$$\cos [c + d x]^{13/2} \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 (a + a \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2)$$

$$\left( -\frac{1}{40 d} (32 A + 23 B - 20 C + 32 A \cos [2 c] + 33 B \cos [2 c] + 20 C \cos [2 c]) \csc [c] \sec [c] + \right.$$

$$\frac{(191 A + 112 B + 28 C) \cos [d x] \sin [c]}{336 d} + \frac{(4 A + B) \cos [2 d x] \sin [2 c]}{40 d} + \frac{A \cos [3 d x] \sin [3 c]}{112 d} +$$

$$\frac{(191 A + 112 B + 28 C) \cos [c] \sin [d x]}{336 d} + \frac{C \sec [c] \sec [c + d x]^2 \sin [d x]}{12 d} +$$

$$\frac{\sec [c] \sec [c + d x] (C \sin [c] + 3 B \sin [d x] + 12 C \sin [d x])}{12 d} +$$

$$\left. \frac{(4 A + B) \cos [2 c] \sin [2 d x]}{40 d} + \frac{A \cos [3 c] \sin [3 d x]}{112 d} \right) -$$

$$\frac{1}{21 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2}}$$

$$17 A \cos [c + d x]^6 \csc [c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \text{ArcTan}[\cot [c]]]^2\right]$$

$$\begin{aligned}
 & \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \text{Sec}[c + dx])^4 (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \\
 & \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \\
 & \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 + \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} -} \\
 & \frac{1}{3d(A + 2C + 2B \text{Cos}[c + dx] + A \text{Cos}[2c + 2dx]) \sqrt{1 + \text{Cot}[c]^2}} \\
 & 4B \text{Cos}[c + dx]^6 \text{Csc}[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]^2\right] \\
 & \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \text{Sec}[c + dx])^4 (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \\
 & \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \\
 & \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 + \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} -} \\
 & \frac{1}{3d(A + 2C + 2B \text{Cos}[c + dx] + A \text{Cos}[2c + 2dx]) \sqrt{1 + \text{Cot}[c]^2}} \\
 & 5C \text{Cos}[c + dx]^6 \text{Csc}[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]^2\right] \\
 & \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \text{Sec}[c + dx])^4 (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \\
 & \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \\
 & \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 + \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} -} \\
 & \left( 4A \text{Cos}[c + dx]^6 \text{Csc}[c] \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \text{Sec}[c + dx])^4 (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \right. \\
 & \left. \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]]^2\right] \right. \right. \\
 & \left. \left. \text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] \right) / \left( \sqrt{1 - \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]]} \right) \right. \\
 & \left. \sqrt{1 + \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{\text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \text{Tan}[c]^2} \right)
 \end{aligned}$$

$$\left. \left( \sqrt{1 + \tan[c]^2} \right) - \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \right) /$$

$$(5 d (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x])) -$$

$$\left( 7 B \cos[c + d x]^6 \csc[c] \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^8 (a + a \sec[c + d x])^4 (A + B \sec[c + d x] + C \sec[c + d x]^2) \right.$$

$$\left. \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos[d x + \text{ArcTan}[\tan[c]]]^2\right] \right) \right.$$

$$\left. \frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 - \cos[d x + \text{ArcTan}[\tan[c]]]}} \right) /$$

$$\sqrt{1 + \cos[d x + \text{ArcTan}[\tan[c]]]} \sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}$$

$$\left. \left( \sqrt{1 + \tan[c]^2} \right) - \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \right) /$$

$$(10 d (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]))$$

**Problem 1213: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c + d x]^{5/2} (a + a \sec[c + d x])^4 (A + B \sec[c + d x] + C \sec[c + d x]^2) dx$$

Optimal (type 4, 267 leaves, 10 steps):

$$\frac{56 a^4 (A-C) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 d} + \frac{8 a^4 (4 A+5 B+4 C) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{3 d} +$$

$$\frac{4 a^4 (A-25 B-41 C) \sqrt{\cos [c+d x]} \sin [c+d x]}{15 d} + \frac{2 a (5 B+8 C) (a+a \cos [c+d x])^3 \sin [c+d x]}{15 d \cos [c+d x]^{3 / 2}} +$$

$$\frac{2 C (a+a \cos [c+d x])^4 \sin [c+d x]}{5 d \cos [c+d x]^{5 / 2}} + \frac{2 (5 A+15 B+19 C) (a^2+a^2 \cos [c+d x])^2 \sin [c+d x]}{5 d \sqrt{\cos [c+d x]}} -$$

$$\frac{4 (6 A+25 B+34 C) \sqrt{\cos [c+d x]} (a^4+a^4 \cos [c+d x]) \sin [c+d x]}{15 d}$$

Result (type 5, 1449 leaves):

$$\frac{1}{A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]}$$

$$\cos [c+d x]^{13 / 2} \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \operatorname{Sec}[c+d x])^4 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2)$$

$$\left(-\frac{1}{40 d}(23 A-20 B-61 C+33 A \cos [2 c]+20 B \cos [2 c]+5 C \cos [2 c]) \operatorname{Csc}[c] \operatorname{Sec}[c]+$$

$$\frac{(4 A+B) \cos [d x] \sin [c]}{12 d}+\frac{A \cos [2 d x] \sin [2 c]}{40 d}+\right.$$

$$\frac{(4 A+B) \cos [c] \sin [d x]}{12 d}+\frac{C \operatorname{Sec}[c] \operatorname{Sec}[c+d x]^3 \sin [d x]}{20 d}+$$

$$\frac{\operatorname{Sec}[c] \operatorname{Sec}[c+d x]^2(3 C \sin [c]+5 B \sin [d x]+20 C \sin [d x])}{60 d}+\frac{1}{60 d}$$

$$\left.\operatorname{Sec}[c] \operatorname{Sec}[c+d x](5 B \sin [c]+20 C \sin [c]+15 A \sin [d x]+60 B \sin [d x]+99 C \sin [d x])+\right.$$

$$\left.\frac{A \cos [2 c] \sin [2 d x]}{40 d}\right)-$$

$$\frac{1}{3 d(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\operatorname{Cot}[c]^2}}$$

$$4 A \cos [c+d x]^6 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right]$$

$$\operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \operatorname{Sec}[c+d x])^4 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2)$$

$$\operatorname{Sec}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]}$$

$$\sqrt{-\sqrt{1+\operatorname{Cot}[c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]}-}$$

$$\frac{1}{3 d(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\operatorname{Cot}[c]^2}}$$

$$5 B \cos [c+d x]^6 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right]$$

$$\operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \operatorname{Sec}[c+d x])^4 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2)$$

$$\operatorname{Sec}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]}$$



$$\begin{aligned}
 & \frac{\sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]} \sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]} - 1}{3d(A+2C+2B\cos[c+dx]+A\cos[2c+2dx])\sqrt{1+\cot[c]^2}} \\
 & 4C\cos[c+dx]^6 \csc[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\cot[c]]]^2\right] \\
 & \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a+a\sec[c+dx])^4 (A+B\sec[c+dx]+C\sec[c+dx]^2) \\
 & \sec[dx - \text{ArcTan}[\cot[c]]] \sqrt{1-\sin[dx - \text{ArcTan}[\cot[c]]]} \\
 & \sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]} \sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]} - \\
 & \left( 7A\cos[c+dx]^6 \csc[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a+a\sec[c+dx])^4 (A+B\sec[c+dx]+C\sec[c+dx]^2) \right. \\
 & \left. \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos[dx + \text{ArcTan}[\tan[c]]]^2\right] \right) \right. \\
 & \left. \frac{\sin[dx + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1-\cos[dx + \text{ArcTan}[\tan[c]]]}} \right) \\
 & \frac{\sqrt{1+\cos[dx + \text{ArcTan}[\tan[c]]]} \sqrt{\cos[c] \cos[dx + \text{ArcTan}[\tan[c]]]} \sqrt{1+\tan[c]^2}}{\sqrt{1+\tan[c]^2}} - \frac{\frac{\sin[dx + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1+\tan[c]^2}} + \frac{2\cos[c]^2 \cos[dx + \text{ArcTan}[\tan[c]]] \sqrt{1+\tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[dx + \text{ArcTan}[\tan[c]]]} \sqrt{1+\tan[c]^2}}} \left. \right) / \\
 & (10d(A+2C+2B\cos[c+dx]+A\cos[2c+2dx])) + \\
 & \left( 7C\cos[c+dx]^6 \csc[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a+a\sec[c+dx])^4 (A+B\sec[c+dx]+C\sec[c+dx]^2) \right. \\
 & \left. \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos[dx + \text{ArcTan}[\tan[c]]]^2\right] \right) \right)
 \end{aligned}$$

$$\left( \frac{\sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 - \cos [d x + \text{ArcTan}[\text{Tan}[c]]]}} \right) / \left( \sqrt{1 + \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \tan [c]^2} \right) - \left( \frac{\frac{\sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \tan [c]^2}} \right) / (10 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]))$$

**Problem 1214: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c + d x]^{3/2} (a + a \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 4, 271 leaves, 10 steps):

$$\begin{aligned} & - \frac{8 a^4 (7 B + 8 C) \text{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{5 d} + \frac{8 a^4 (35 A + 28 B + 17 C) \text{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{21 d} \\ & + \frac{4 a^4 (175 A + 287 B + 253 C) \sqrt{\cos [c + d x]} \sin [c + d x]}{105 d} \\ & + \frac{2 a (7 B + 8 C) (a + a \cos [c + d x])^3 \sin [c + d x]}{35 d \cos [c + d x]^{5/2}} + \frac{2 C (a + a \cos [c + d x])^4 \sin [c + d x]}{7 d \cos [c + d x]^{7/2}} \\ & + \frac{2 (35 A + 77 B + 73 C) (a^2 + a^2 \cos [c + d x])^2 \sin [c + d x]}{105 d \cos [c + d x]^{3/2}} \\ & + \frac{4 (175 A + 238 B + 197 C) (a^4 + a^4 \cos [c + d x]) \sin [c + d x]}{105 d \sqrt{\cos [c + d x]}} \end{aligned}$$

Result (type 5, 1454 leaves):

$$\begin{aligned} & \frac{1}{A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]} \\ & \cos [c + d x]^{13/2} \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 (a + a \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2) \\ & \left( - \frac{1}{40 d} (-20 A - 61 B - 64 C + 20 A \cos [2 c] + 5 B \cos [2 c]) \csc [c] \sec [c] + \right. \\ & \frac{A \cos [d x] \sin [c]}{12 d} + \frac{A \cos [c] \sin [d x]}{12 d} + \frac{C \sec [c] \sec [c + d x]^4 \sin [d x]}{28 d} + \\ & \left. \frac{\sec [c] \sec [c + d x]^3 (5 C \sin [c] + 7 B \sin [d x] + 28 C \sin [d x])}{140 d} + \frac{1}{420 d} \sec [c] \right. \\ & \left. \sec [c + d x]^2 (21 B \sin [c] + 84 C \sin [c] + 35 A \sin [d x] + 140 B \sin [d x] + 235 C \sin [d x]) + \right. \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{420 d} \operatorname{Sec}[c] \operatorname{Sec}[c+d x] \left( 35 A \operatorname{Sin}[c] + 140 B \operatorname{Sin}[c] + 235 C \operatorname{Sin}[c] + \right. \\
 & \quad \left. 420 A \operatorname{Sin}[d x] + 693 B \operatorname{Sin}[d x] + 672 C \operatorname{Sin}[d x] \right) - \\
 & \frac{1}{3 d (A+2 C+2 B \operatorname{Cos}[c+d x]+A \operatorname{Cos}[2 c+2 d x]) \sqrt{1+\operatorname{Cot}[c]^2}} \\
 & 5 A \operatorname{Cos}[c+d x]^6 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \\
 & \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \operatorname{Sec}[c+d x])^4 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \\
 & \operatorname{Sec}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1-\operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \sqrt{-\sqrt{1+\operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1+\operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} - \\
 & \frac{1}{3 d (A+2 C+2 B \operatorname{Cos}[c+d x]+A \operatorname{Cos}[2 c+2 d x]) \sqrt{1+\operatorname{Cot}[c]^2}} \\
 & 4 B \operatorname{Cos}[c+d x]^6 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \\
 & \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \operatorname{Sec}[c+d x])^4 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \\
 & \operatorname{Sec}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1-\operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \sqrt{-\sqrt{1+\operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1+\operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} - \\
 & \frac{1}{21 d (A+2 C+2 B \operatorname{Cos}[c+d x]+A \operatorname{Cos}[2 c+2 d x]) \sqrt{1+\operatorname{Cot}[c]^2}} \\
 & 17 C \operatorname{Cos}[c+d x]^6 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \\
 & \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \operatorname{Sec}[c+d x])^4 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \\
 & \operatorname{Sec}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1-\operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \sqrt{-\sqrt{1+\operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1+\operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} + \\
 & \left( 7 B \operatorname{Cos}[c+d x]^6 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \operatorname{Sec}[c+d x])^4 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \right. \\
 & \left. \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \operatorname{Cos}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]^2\right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{\sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 - \cos [d x + \text{ArcTan}[\text{Tan}[c]]]}} \right) / \left( \sqrt{1 + \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \tan [c]^2} \right. \\
 & \left. \sqrt{1 + \tan [c]^2} \right) - \frac{\frac{\sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \tan [c]^2}} \Bigg) / \\
 & (10 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) + \\
 & \left( 4 C \cos [c + d x]^6 \csc [c] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 (a + a \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \left. \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \text{ArcTan}[\text{Tan}[c]]]^2 \right] \right) \right) \\
 & \left( \frac{\sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 - \cos [d x + \text{ArcTan}[\text{Tan}[c]]]}} \right) / \left( \sqrt{1 + \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \tan [c]^2} \right. \\
 & \left. \sqrt{1 + \tan [c]^2} \right) - \frac{\frac{\sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \tan [c]^2}} \Bigg) / \\
 & (5 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]))
 \end{aligned}$$

**Problem 1215: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sqrt{\cos [c + d x]} (a + a \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 4, 274 leaves, 10 steps):

$$\begin{aligned}
 & - \frac{8 a^4 (21 A + 24 B + 19 C) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{15 d} + \\
 & \frac{8 a^4 (28 A + 17 B + 12 C) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{21 d} + \frac{4 a^4 (287 A + 253 B + 193 C) \operatorname{Sin}[c+d x]}{105 d \sqrt{\operatorname{Cos}[c+d x]}} + \\
 & \frac{2 a (9 B + 8 C) (a+a \operatorname{Cos}[c+d x])^3 \operatorname{Sin}[c+d x]}{63 d \operatorname{Cos}[c+d x]^{7/2}} + \frac{2 C (a+a \operatorname{Cos}[c+d x])^4 \operatorname{Sin}[c+d x]}{9 d \operatorname{Cos}[c+d x]^{9/2}} + \\
 & \frac{2 (63 A + 117 B + 97 C) (a^2+a^2 \operatorname{Cos}[c+d x])^2 \operatorname{Sin}[c+d x]}{315 d \operatorname{Cos}[c+d x]^{5/2}} + \\
 & \frac{4 (21 A + 24 B + 19 C) (a^4+a^4 \operatorname{Cos}[c+d x]) \operatorname{Sin}[c+d x]}{45 d \operatorname{Cos}[c+d x]^{3/2}}
 \end{aligned}$$

Result (type 5, 1748 leaves):

$$\begin{aligned}
 & \frac{1}{A+2 C+2 B \operatorname{Cos}[c+d x]+A \operatorname{Cos}[2 c+2 d x]} \\
 & \operatorname{Cos}[c+d x]^{13/2} \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \operatorname{Sec}[c+d x])^4 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \\
 & \left( - \frac{(-183 A-192 B-152 C+15 A \operatorname{Cos}[2 c]) \operatorname{Csc}[c] \operatorname{Sec}[c]}{120 d} + \frac{C \operatorname{Sec}[c] \operatorname{Sec}[c+d x]^5 \operatorname{Sin}[d x]}{36 d} + \right. \\
 & \frac{\operatorname{Sec}[c] \operatorname{Sec}[c+d x]^4 (7 C \operatorname{Sin}[c]+9 B \operatorname{Sin}[d x]+36 C \operatorname{Sin}[d x])}{252 d} + \frac{1}{1260 d} \operatorname{Sec}[c] \operatorname{Sec}[c+d x]^3 \\
 & (45 B \operatorname{Sin}[c]+180 C \operatorname{Sin}[c]+63 A \operatorname{Sin}[d x]+252 B \operatorname{Sin}[d x]+427 C \operatorname{Sin}[d x]) + \frac{1}{420 d} \\
 & \operatorname{Sec}[c] \operatorname{Sec}[c+d x] (140 A \operatorname{Sin}[c]+235 B \operatorname{Sin}[c]+240 C \operatorname{Sin}[c]+693 A \operatorname{Sin}[d x]+ \\
 & 672 B \operatorname{Sin}[d x]+532 C \operatorname{Sin}[d x]) + \frac{1}{1260 d} \operatorname{Sec}[c] \operatorname{Sec}[c+d x]^2 (63 A \operatorname{Sin}[c]+ \\
 & \left. 252 B \operatorname{Sin}[c]+427 C \operatorname{Sin}[c]+420 A \operatorname{Sin}[d x]+705 B \operatorname{Sin}[d x]+720 C \operatorname{Sin}[d x]) \right) - \\
 & \frac{1}{3 d (A+2 C+2 B \operatorname{Cos}[c+d x]+A \operatorname{Cos}[2 c+2 d x]) \sqrt{1+\operatorname{Cot}[c]^2}} \\
 & 4 A \operatorname{Cos}[c+d x]^6 \operatorname{Csc}[c] \\
 & \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \\
 & \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \operatorname{Sec}[c+d x])^4 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \\
 & \operatorname{Sec}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1-\operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \sqrt{-\sqrt{1+\operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1+\operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} - \\
 & \frac{1}{21 d (A+2 C+2 B \operatorname{Cos}[c+d x]+A \operatorname{Cos}[2 c+2 d x]) \sqrt{1+\operatorname{Cot}[c]^2}} \\
 & 17 B \operatorname{Cos}[c+d x]^6 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right]
 \end{aligned}$$

$$\begin{aligned}
 & \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \text{Sec}[c + dx])^4 (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \\
 & \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \\
 & \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 + \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} -} \\
 & \frac{1}{\text{-----}} \\
 & 7d (A + 2C + 2B \text{Cos}[c + dx] + A \text{Cos}[2c + 2dx]) \sqrt{1 + \text{Cot}[c]^2} \\
 & 4C \text{Cos}[c + dx]^6 \text{Csc}[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]^2\right] \\
 & \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \text{Sec}[c + dx])^4 (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \\
 & \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \\
 & \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 + \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} +} \\
 & \left( 7A \text{Cos}[c + dx]^6 \text{Csc}[c] \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \text{Sec}[c + dx])^4 (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \right. \\
 & \left. \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]]^2\right] \right) \right. \\
 & \left. \text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] \right) / \left( \sqrt{1 - \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]]} \right. \\
 & \left. \sqrt{1 + \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{\text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}} \right. \\
 & \left. \left. \left. \sqrt{1 + \text{Tan}[c]^2} \right) - \frac{\frac{\text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \frac{2 \text{Cos}[c]^2 \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}}{\text{Cos}[c]^2 + \text{Sin}[c]^2}}{\sqrt{\text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}}} \right) \right) / \\
 & (10d (A + 2C + 2B \text{Cos}[c + dx] + A \text{Cos}[2c + 2dx])) + \\
 & \left( 4B \text{Cos}[c + dx]^6 \text{Csc}[c] \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \text{Sec}[c + dx])^4 (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \right.
 \end{aligned}$$

$$\left( \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \text{ArcTan} [\text{Tan} [c]]]^2 \right] \right. \right.$$

$$\left. \left. \frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 - \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \right) \right) / \left( \sqrt{1 + \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2} \right.$$

$$\left. \left. \left. \left. \sqrt{1 + \tan [c]^2} \right) - \frac{\frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2}} \right) \right) \right) /$$

$$(5 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) +$$

$$\left( 19 C \cos [c + d x]^6 \csc [c] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 (a + a \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right)$$

$$\left( \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \text{ArcTan} [\text{Tan} [c]]]^2 \right] \right. \right.$$

$$\left. \left. \frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 - \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \right) \right) / \left( \sqrt{1 + \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2} \right.$$

$$\left. \left. \left. \left. \sqrt{1 + \tan [c]^2} \right) - \frac{\frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2}} \right) \right) \right) /$$

$$(30 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]))$$

**Problem 1216:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(a + a \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\sqrt{\operatorname{Cos}[c + d x]}} dx$$

Optimal (type 4, 310 leaves, 11 steps):

$$\begin{aligned} & \frac{8 a^4 (24 A + 19 B + 16 C) \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{15 d} + \\ & \frac{8 a^4 (187 A + 132 B + 113 C) \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{231 d} + \frac{4 a^4 (913 A + 803 B + 667 C) \operatorname{Sin}[c + d x]}{1155 d \operatorname{Cos}[c + d x]^{3/2}} + \\ & \frac{8 a^4 (24 A + 19 B + 16 C) \operatorname{Sin}[c + d x]}{15 d \sqrt{\operatorname{Cos}[c + d x]}} + \frac{2 a (11 B + 8 C) (a + a \operatorname{Cos}[c + d x])^3 \operatorname{Sin}[c + d x]}{99 d \operatorname{Cos}[c + d x]^{9/2}} + \\ & \frac{2 C (a + a \operatorname{Cos}[c + d x])^4 \operatorname{Sin}[c + d x]}{11 d \operatorname{Cos}[c + d x]^{11/2}} + \frac{2 (33 A + 55 B + 43 C) (a^2 + a^2 \operatorname{Cos}[c + d x])^2 \operatorname{Sin}[c + d x]}{231 d \operatorname{Cos}[c + d x]^{7/2}} + \\ & \frac{4 (891 A + 946 B + 769 C) (a^4 + a^4 \operatorname{Cos}[c + d x]) \operatorname{Sin}[c + d x]}{3465 d \operatorname{Cos}[c + d x]^{5/2}} \end{aligned}$$

Result (type 5, 1795 leaves):

$$\begin{aligned} & \frac{1}{A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]} \\ & \operatorname{Cos}[c + d x]^{13/2} \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^8 (a + a \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\ & \left( \frac{(24 A + 19 B + 16 C) \operatorname{Csc}[c] \operatorname{Sec}[c]}{15 d} + \frac{C \operatorname{Sec}[c] \operatorname{Sec}[c + d x]^6 \operatorname{Sin}[d x]}{44 d} + \right. \\ & \frac{\operatorname{Sec}[c] \operatorname{Sec}[c + d x]^5 (9 C \operatorname{Sin}[c] + 11 B \operatorname{Sin}[d x] + 44 C \operatorname{Sin}[d x])}{396 d} + \frac{1}{2772 d} \operatorname{Sec}[c] \\ & \operatorname{Sec}[c + d x]^4 (77 B \operatorname{Sin}[c] + 308 C \operatorname{Sin}[c] + 99 A \operatorname{Sin}[d x] + 396 B \operatorname{Sin}[d x] + 675 C \operatorname{Sin}[d x]) + \\ & \frac{1}{13860 d} \operatorname{Sec}[c] \operatorname{Sec}[c + d x]^3 (495 A \operatorname{Sin}[c] + 1980 B \operatorname{Sin}[c] + 3375 C \operatorname{Sin}[c] + \\ & 2772 A \operatorname{Sin}[d x] + 4697 B \operatorname{Sin}[d x] + 4928 C \operatorname{Sin}[d x]) + \frac{1}{4620 d} \\ & \operatorname{Sec}[c] \operatorname{Sec}[c + d x] (2585 A \operatorname{Sin}[c] + 2640 B \operatorname{Sin}[c] + 2260 C \operatorname{Sin}[c] + 7392 A \operatorname{Sin}[d x] + \\ & 5852 B \operatorname{Sin}[d x] + 4928 C \operatorname{Sin}[d x]) + \frac{1}{13860 d} \operatorname{Sec}[c] \operatorname{Sec}[c + d x]^2 (2772 A \operatorname{Sin}[c] + \\ & 4697 B \operatorname{Sin}[c] + 4928 C \operatorname{Sin}[c] + 7755 A \operatorname{Sin}[d x] + 7920 B \operatorname{Sin}[d x] + 6780 C \operatorname{Sin}[d x]) \left. \right) - \\ & \frac{1}{21 d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2}} \\ & 17 A \operatorname{Cos}[c + d x]^6 \operatorname{Csc}[c] \\ & \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \\ & \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^8 (a + a \operatorname{Sec}[c + d x])^4 \\ & (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\ & \operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \end{aligned}$$



$$\begin{aligned}
 & \frac{\sqrt{-\sqrt{1+\cot^2[c]} \sin[c] \sin[d x - \text{ArcTan}[\cot[c]]]}}{\sqrt{1+\sin[d x - \text{ArcTan}[\cot[c]]]} - 1} \\
 & \frac{7 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\cot^2[c]} + 4 B \cos [c+d x]^6 \csc [c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x - \text{ArcTan}[\cot [c]]]^2\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \sec [c+d x])^4 (A+B \sec [c+d x]+C \sec [c+d x]^2) \sec [d x - \text{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x - \text{ArcTan}[\cot [c]]]}}{1} \\
 & \frac{\sqrt{-\sqrt{1+\cot^2[c]} \sin [c] \sin [d x - \text{ArcTan}[\cot [c]]]} \sqrt{1+\sin [d x - \text{ArcTan}[\cot [c]]]} - 231 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\cot^2[c]} + 113 C \cos [c+d x]^6 \csc [c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x - \text{ArcTan}[\cot [c]]]^2\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \sec [c+d x])^4 (A+B \sec [c+d x]+C \sec [c+d x]^2) \sec [d x - \text{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x - \text{ArcTan}[\cot [c]]]}}{1} \\
 & \left( \sqrt{-\sqrt{1+\cot^2[c]} \sin [c] \sin [d x - \text{ArcTan}[\cot [c]]]} \sqrt{1+\sin [d x - \text{ArcTan}[\cot [c]]]} + 4 A \cos [c+d x]^6 \csc [c] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \sec [c+d x])^4 (A+B \sec [c+d x]+C \sec [c+d x]^2) \right. \\
 & \left. \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x + \text{ArcTan}[\tan [c]]]^2\right] \sin [d x + \text{ArcTan}[\tan [c]]] \tan [c] \right) / \left( \sqrt{1-\cos [d x + \text{ArcTan}[\tan [c]]]} \sqrt{1+\cos [d x + \text{ArcTan}[\tan [c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2} \right. \right. \\
 & \left. \left. \sqrt{1+\tan [c]^2} \right) - \frac{\frac{\sin [d x + \text{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2}} \right) / \\
 & (5 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])) +
 \end{aligned}$$

$$\left( 19 B \cos [c+d x]^6 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \operatorname{Sec}[c+d x])^4 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \right.$$

$$\left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\},\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]^2\right] \right.$$

$$\left. \frac{\sin [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1-\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]}} \right)$$

$$\sqrt{1+\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1+\operatorname{Tan}[c]^2}$$

$$\left. \left. \left. \sqrt{1+\operatorname{Tan}[c]^2} \right) - \frac{\frac{\sin [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1+\operatorname{Tan}[c]^2}} + \frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1+\operatorname{Tan}[c]^2}}{\cos [c]^2+\sin [c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1+\operatorname{Tan}[c]^2}} \right) \right) /$$

$$(30 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])) +$$

$$\left( 8 C \cos [c+d x]^6 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \operatorname{Sec}[c+d x])^4 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \right.$$

$$\left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\},\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]^2\right] \right.$$

$$\left. \frac{\sin [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1-\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]}} \right)$$

$$\sqrt{1+\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1+\operatorname{Tan}[c]^2}$$

$$\left. \left. \left. \sqrt{1+\operatorname{Tan}[c]^2} \right) - \frac{\frac{\sin [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1+\operatorname{Tan}[c]^2}} + \frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1+\operatorname{Tan}[c]^2}}{\cos [c]^2+\sin [c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1+\operatorname{Tan}[c]^2}} \right) \right) /$$

$$(15 d (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]))$$

Problem 1217: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^{7 / 2} (A+B \sec [c+d x]+C \sec [c+d x]^2)}{a+a \sec [c+d x]} d x$$

Optimal (type 4, 210 leaves, 8 steps):

$$\begin{aligned} & -\frac{3(7 A-7 B+5 C) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 a d}+\frac{5(9 A-7 B+7 C) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{21 a d}+ \\ & \frac{5(9 A-7 B+7 C) \sqrt{\cos [c+d x]} \sin [c+d x]}{21 a d}-\frac{(7 A-7 B+5 C) \cos [c+d x]^{3 / 2} \sin [c+d x]}{5 a d}+ \\ & \frac{(9 A-7 B+7 C) \cos [c+d x]^{5 / 2} \sin [c+d x]}{7 a d}-\frac{(A-B+C) \cos [c+d x]^{7 / 2} \sin [c+d x]}{d(a+a \cos [c+d x])} \end{aligned}$$

Result (type 5, 2117 leaves):

$$\begin{aligned} & \frac{1}{10(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])(a+a \sec [c+d x])} \\ & 21 i A \cos \left[\frac{c}{2}+\frac{d x}{2}\right]^2 \cos [c+d x] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] (A+B \sec [c+d x]+C \sec [c+d x]^2) \\ & \left(\left(2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4},-e^{2 i d x}(\cos [c]+i \sin [c])^2\right]\right.\right. \\ & \quad \left.\left.\frac{\sqrt{e^{-i d x}(2(1+e^{2 i d x}) \cos [c]+2 i(-1+e^{2 i d x}) \sin [c])}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}}\right) / \right. \\ & \quad \left.(3 i d(1+e^{2 i d x}) \cos [c]-3 d(-1+e^{2 i d x}) \sin [c])-\right. \\ & \quad \left.\left(2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4},-e^{2 i d x}(\cos [c]+i \sin [c])^2\right]\right.\right. \\ & \quad \left.\left.\frac{\sqrt{e^{-i d x}(2(1+e^{2 i d x}) \cos [c]+2 i(-1+e^{2 i d x}) \sin [c])}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}}\right) / \right. \\ & \quad \left.\left.(-i d(1+e^{2 i d x}) \cos [c]+d(-1+e^{2 i d x}) \sin [c])\right)\right)+ \\ & \frac{1}{10(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])(a+a \sec [c+d x])} \\ & 21 \\ & i \\ & B \\ & \cos \left[\frac{c}{2}+\frac{d x}{2}\right]^2 \\ & \cos [c+d x] \\ & \operatorname{Csc}\left[\frac{c}{2}\right] \\ & \operatorname{Sec}\left[\frac{c}{2}\right] \end{aligned}$$

$$\begin{aligned}
 & (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])\right]^2 \right) \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]}} \right) / \\
 & \quad (3 i d (1 + e^{2 i d x}) \operatorname{Cos}[c] - 3 d (-1 + e^{2 i d x}) \operatorname{Sin}[c]) - \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])\right]^2 \right) \\
 & \quad \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2 i d x}) \operatorname{Cos}[c] + d (-1 + e^{2 i d x}) \operatorname{Sin}[c]) \right) - \\
 & \quad \frac{1}{2 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) (a + a \operatorname{Sec}[c + d x])} \\
 & \quad \frac{3}{i} \\
 & \quad C \\
 & \quad \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \\
 & \quad \operatorname{Cos}[c + d x] \\
 & \quad \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \\
 & \quad (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\
 & \quad \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])\right]^2 \right) \right. \\
 & \quad \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]}} \right) / \\
 & \quad \quad (3 i d (1 + e^{2 i d x}) \operatorname{Cos}[c] - 3 d (-1 + e^{2 i d x}) \operatorname{Sin}[c]) - \\
 & \quad \quad \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])\right]^2 \right) \\
 & \quad \quad \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]}} \right) / \\
 & \quad \quad \left. (-i d (1 + e^{2 i d x}) \operatorname{Cos}[c] + d (-1 + e^{2 i d x}) \operatorname{Sin}[c]) \right) + \\
 & \quad \quad \frac{1}{(A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) (a + a \operatorname{Sec}[c + d x])} \\
 & \quad \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \\
 & \quad \operatorname{Cos}[c + d x]^{3/2} \\
 & \quad (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{4 (5A - 5B + 5C + 16A \cos[c] - 16B \cos[c] + 10C \cos[c]) \operatorname{Csc}[c]}{5d} + \right. \\
 & \frac{2 (51A - 28B + 28C) \cos[dx] \sin[c]}{21d} - \frac{4 (A - B) \cos[2dx] \sin[2c]}{5d} + \\
 & \frac{2A \cos[3dx] \sin[3c]}{7d} + \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] \left(A \sin\left[\frac{dx}{2}\right] - B \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right]\right)}{d} + \\
 & \frac{2 (51A - 28B + 28C) \cos[c] \sin[dx]}{21d} - \\
 & \left. \frac{4 (A - B) \cos[2c] \sin[2dx]}{5d} + \frac{2A \cos[3c] \sin[3dx]}{7d} \right) - \\
 & \left( 30A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c + dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \right. \right. \\
 & \left. \left. \frac{\sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2 \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2)}{\operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right. \right. \\
 & \left. \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right. \right. \\
 & \left. \left. \sqrt{1 + \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) / \right) \\
 & \left( 7d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{1 + \operatorname{Cot}[c]^2} (a + a \operatorname{Sec}[c + dx]) \right) + \\
 & \left( 10B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c + dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \left. \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2 \right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right. \\
 & \left. \operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right. \\
 & \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1 + \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) / \\
 & \left( 3d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{1 + \operatorname{Cot}[c]^2} (a + a \operatorname{Sec}[c + dx]) \right) - \\
 & \left( 10C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c + dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \left. \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2 \right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right)
 \end{aligned}$$

$$\frac{\left( \frac{\text{Sec}[d x - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \text{Sin}[d x - \text{ArcTan}[\text{Cot}[c]]]}}{\sqrt{-\sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[d x - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 + \text{Sin}[d x - \text{ArcTan}[\text{Cot}[c]]]}} \right)}{\left( 3 d (A + 2 C + 2 B \text{Cos}[c + d x] + A \text{Cos}[2 c + 2 d x]) \sqrt{1 + \text{Cot}[c]^2} (a + a \text{Sec}[c + d x]) \right)}$$

**Problem 1218: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\text{Cos}[c + d x]^{5/2} (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2)}{a + a \text{Sec}[c + d x]} dx$$

Optimal (type 4, 174 leaves, 7 steps):

$$\frac{3 (7 A - 5 B + 5 C) \text{EllipticE}\left[\frac{1}{2} (c + d x), 2\right]}{5 a d} - \frac{(5 A - 5 B + 3 C) \text{EllipticF}\left[\frac{1}{2} (c + d x), 2\right]}{3 a d} - \frac{(5 A - 5 B + 3 C) \sqrt{\text{Cos}[c + d x]} \text{Sin}[c + d x]}{3 a d} + \frac{(7 A - 5 B + 5 C) \text{Cos}[c + d x]^{3/2} \text{Sin}[c + d x]}{5 a d} - \frac{(A - B + C) \text{Cos}[c + d x]^{5/2} \text{Sin}[c + d x]}{d (a + a \text{Cos}[c + d x])}$$

Result (type 5, 2063 leaves):

$$\frac{1}{10 (A + 2 C + 2 B \text{Cos}[c + d x] + A \text{Cos}[2 c + 2 d x]) (a + a \text{Sec}[c + d x])} + \frac{21 i A \text{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \text{Cos}[c + d x] \text{Csc}\left[\frac{c}{2}\right] \text{Sec}\left[\frac{c}{2}\right] (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2)}{\left( \left( 2 e^{2 i d x} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\text{Cos}[c] + i \text{Sin}[c])^2\right] \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \text{Cos}[c] + 2 i (-1 + e^{2 i d x}) \text{Sin}[c])} \sqrt{1 + e^{2 i d x} \text{Cos}[2 c] + i e^{2 i d x} \text{Sin}[2 c]} \right) \right)}{\left( 3 i d (1 + e^{2 i d x}) \text{Cos}[c] - 3 d (-1 + e^{2 i d x}) \text{Sin}[c] \right) - \left( 2 \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\text{Cos}[c] + i \text{Sin}[c])^2\right] \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \text{Cos}[c] + 2 i (-1 + e^{2 i d x}) \text{Sin}[c])} \sqrt{1 + e^{2 i d x} \text{Cos}[2 c] + i e^{2 i d x} \text{Sin}[2 c]} \right) \right)}{\left( -i d (1 + e^{2 i d x}) \text{Cos}[c] + d (-1 + e^{2 i d x}) \text{Sin}[c] \right)}$$

$$\frac{1}{2 (A + 2 C + 2 B \text{Cos}[c + d x] + A \text{Cos}[2 c + 2 d x]) (a + a \text{Sec}[c + d x])} + \frac{3 i B \text{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \text{Cos}[c + d x]}{3 i B}$$

$$\begin{aligned}
 & \text{Csc}\left[\frac{c}{2}\right] \text{Sec}\left[\frac{c}{2}\right] \\
 & (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \\
 & \left( \left( 2 e^{2 i dx} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i dx} (\text{Cos}[c] + i \text{Sin}[c])\right]^2 \right) \right. \\
 & \quad \left. \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \text{Cos}[c] + 2 i (-1 + e^{2 i dx}) \text{Sin}[c])}}{\sqrt{1 + e^{2 i dx} \text{Cos}[2 c] + i e^{2 i dx} \text{Sin}[2 c]}} \right) / \\
 & \quad (3 i d (1 + e^{2 i dx}) \text{Cos}[c] - 3 d (-1 + e^{2 i dx}) \text{Sin}[c]) - \\
 & \quad \left( 2 \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i dx} (\text{Cos}[c] + i \text{Sin}[c])\right]^2 \right) \\
 & \quad \left. \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \text{Cos}[c] + 2 i (-1 + e^{2 i dx}) \text{Sin}[c])}}{\sqrt{1 + e^{2 i dx} \text{Cos}[2 c] + i e^{2 i dx} \text{Sin}[2 c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2 i dx}) \text{Cos}[c] + d (-1 + e^{2 i dx}) \text{Sin}[c]) \right) + \\
 & \quad \frac{1}{2 (A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2 c + 2 dx]) (a + a \text{Sec}[c + dx])} \\
 & \quad 3 i C \\
 & \quad \text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \text{Cos}[c + dx] \\
 & \quad \text{Csc}\left[\frac{c}{2}\right] \text{Sec}\left[\frac{c}{2}\right] \\
 & \quad (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \\
 & \quad \left( \left( 2 e^{2 i dx} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i dx} (\text{Cos}[c] + i \text{Sin}[c])\right]^2 \right) \right. \\
 & \quad \quad \left. \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \text{Cos}[c] + 2 i (-1 + e^{2 i dx}) \text{Sin}[c])}}{\sqrt{1 + e^{2 i dx} \text{Cos}[2 c] + i e^{2 i dx} \text{Sin}[2 c]}} \right) / \\
 & \quad \quad (3 i d (1 + e^{2 i dx}) \text{Cos}[c] - 3 d (-1 + e^{2 i dx}) \text{Sin}[c]) - \\
 & \quad \quad \left( 2 \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i dx} (\text{Cos}[c] + i \text{Sin}[c])\right]^2 \right) \\
 & \quad \quad \left. \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \text{Cos}[c] + 2 i (-1 + e^{2 i dx}) \text{Sin}[c])}}{\sqrt{1 + e^{2 i dx} \text{Cos}[2 c] + i e^{2 i dx} \text{Sin}[2 c]}} \right) / \\
 & \quad \quad \left. (-i d (1 + e^{2 i dx}) \text{Cos}[c] + d (-1 + e^{2 i dx}) \text{Sin}[c]) \right) + \\
 & \quad \left( \text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \text{Cos}[c + dx]^{3/2} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \right. \\
 & \quad \left. \left( -\frac{1}{5 d} 4 (5 A - 5 B + 5 C + 16 A \text{Cos}[c] - 10 B \text{Cos}[c] + 10 C \text{Cos}[c]) \text{Csc}[c] - \right. \right. \\
 & \quad \quad \left. \left. \frac{8 (A - B) \text{Cos}[dx] \text{Sin}[c]}{3 d} + \frac{4 A \text{Cos}[2 dx] \text{Sin}[2 c]}{5 d} \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] \left(A \operatorname{Sin}\left[\frac{dx}{2}\right] - B \operatorname{Sin}\left[\frac{dx}{2}\right] + C \operatorname{Sin}\left[\frac{dx}{2}\right]\right)}{d} - \\
 & \left. \left. \frac{8(A-B) \operatorname{Cos}[c] \operatorname{Sin}[dx]}{3d} + \frac{4A \operatorname{Cos}[2c] \operatorname{Sin}[2dx]}{5d} \right) \right) / \\
 & \left( (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) (a + a \operatorname{Sec}[c + dx]) \right) + \\
 & \left( 10A \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Cos}[c + dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2 \right. \\
 & \quad \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \\
 & \quad \operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \quad \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \quad \left. \left. \sqrt{1 + \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) \right) / \\
 & \left( 3d (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) \sqrt{1 + \operatorname{Cot}[c]^2} (a + a \operatorname{Sec}[c + dx]) \right) - \\
 & \left( 10B \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Cos}[c + dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2 \right. \\
 & \quad \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \\
 & \quad \operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \quad \left. \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1 + \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) \right) / \\
 & \left( 3d (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) \sqrt{1 + \operatorname{Cot}[c]^2} (a + a \operatorname{Sec}[c + dx]) \right) + \\
 & \left( 2C \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Cos}[c + dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2 \right. \\
 & \quad \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \\
 & \quad \operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \quad \left. \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1 + \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) \right) /
 \end{aligned}$$



$$\left( d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} (a + a \sec [c + d x]) \right)$$

**Problem 1219: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\cos [c + d x]^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2)}{a + a \sec [c + d x]} dx$$

Optimal (type 4, 134 leaves, 6 steps):

$$\begin{aligned} & - \frac{(3 A - 3 B + C) \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{a d} + \frac{(5 A - 3 B + 3 C) \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{3 a d} + \\ & \frac{(5 A - 3 B + 3 C) \sqrt{\cos [c + d x]} \sin [c + d x]}{3 a d} - \frac{(A - B + C) \cos [c + d x]^{3/2} \sin [c + d x]}{d (a + a \cos [c + d x])} \end{aligned}$$

Result (type 5, 2008 leaves):

$$\begin{aligned} & - \frac{1}{2 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])} \\ & 3 i A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \cos [c + d x] \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} \right] (A + B \sec [c + d x] + C \sec [c + d x]^2) \\ & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \right. \\ & \quad \left. \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \right. \\ & \quad \left. (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) - \right. \\ & \quad \left. \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \right. \\ & \quad \left. \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \right. \\ & \quad \left. \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) \right) + \\ & \frac{1}{2 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])} \\ & 3 \\ & i \\ & B \\ & \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \\ & \cos [c + d x] \\ & \operatorname{Csc} \left[ \frac{c}{2} \right] \\ & \operatorname{Sec} \left[ \frac{c}{2} \right] \end{aligned}$$

$$\begin{aligned}
 & (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])\right]^2 \right) \right. \\
 & \quad \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]}} \Bigg) / \\
 & \quad (3 i d (1 + e^{2 i d x}) \operatorname{Cos}[c] - 3 d (-1 + e^{2 i d x}) \operatorname{Sin}[c]) - \\
 & \quad \left. \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])\right]^2 \right) \right. \\
 & \quad \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]}} \Bigg) / \\
 & \quad \left. (-i d (1 + e^{2 i d x}) \operatorname{Cos}[c] + d (-1 + e^{2 i d x}) \operatorname{Sin}[c]) \right) - \\
 & \quad \frac{1}{2 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) (a + a \operatorname{Sec}[c + d x])} \\
 & \quad i \\
 & \quad C \\
 & \quad \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \\
 & \quad \operatorname{Cos}[c + d x] \\
 & \quad \operatorname{Csc}\left[\frac{c}{2}\right] \\
 & \quad \operatorname{Sec}\left[\frac{c}{2}\right] \\
 & \quad (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\
 & \quad \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])\right]^2 \right) \right. \\
 & \quad \quad \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]}} \Bigg) / \\
 & \quad \quad (3 i d (1 + e^{2 i d x}) \operatorname{Cos}[c] - 3 d (-1 + e^{2 i d x}) \operatorname{Sin}[c]) - \\
 & \quad \quad \left. \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])\right]^2 \right) \right. \\
 & \quad \quad \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]}} \Bigg) / \\
 & \quad \quad \left. (-i d (1 + e^{2 i d x}) \operatorname{Cos}[c] + d (-1 + e^{2 i d x}) \operatorname{Sin}[c]) \right) + \\
 & \quad \left( \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \operatorname{Cos}[c + d x]^{3/2} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \quad \left. \left( \frac{4 (A - B + C + 2 A \operatorname{Cos}[c] - 2 B \operatorname{Cos}[c]) \operatorname{Csc}[c]}{d} + \frac{8 A \operatorname{Cos}[d x] \operatorname{Sin}[c]}{3 d} \right) + \right.
 \end{aligned}$$

$$\left. \left( \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] \left( A \operatorname{Sin}\left[\frac{dx}{2}\right] - B \operatorname{Sin}\left[\frac{dx}{2}\right] + C \operatorname{Sin}\left[\frac{dx}{2}\right] \right)}{d} + \frac{8 A \operatorname{Cos}[c] \operatorname{Sin}[dx]}{3 d} \right) \right) /$$

$$\left( (A + 2 C + 2 B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2 c + 2 dx]) (a + a \operatorname{Sec}[c + dx]) \right) -$$

$$\left( 10 A \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Cos}[c + dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right.$$

$$\operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right]$$

$$\operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2)$$

$$\operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}$$

$$\sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}$$

$$\left. \sqrt{1 + \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) /$$

$$\left( 3 d (A + 2 C + 2 B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2 c + 2 dx]) \sqrt{1 + \operatorname{Cot}[c]^2} (a + a \operatorname{Sec}[c + dx]) \right) +$$

$$\left( 2 B \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Cos}[c + dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right.$$

$$\operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right]$$

$$\operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2)$$

$$\operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}$$

$$\sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1 + \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) /$$

$$\left( d (A + 2 C + 2 B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2 c + 2 dx]) \sqrt{1 + \operatorname{Cot}[c]^2} (a + a \operatorname{Sec}[c + dx]) \right) -$$

$$\left( 2 C \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Cos}[c + dx] \operatorname{Csc}\left[\frac{c}{2}\right] \right.$$

$$\operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right]$$

$$\operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2)$$

$$\operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}$$

$$\sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1 + \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) /$$

$$\left( d (A + 2 C + 2 B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2 c + 2 dx]) \sqrt{1 + \operatorname{Cot}[c]^2} (a + a \operatorname{Sec}[c + dx]) \right)$$

**Problem 1220: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\cos [c+d x]} (A+B \sec [c+d x]+C \sec [c+d x]^2)}{a+a \sec [c+d x]} d x$$

Optimal (type 4, 93 leaves, 5 steps):

$$\frac{(3 A-B+C) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{a d}-\frac{(A-B-C) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{a d}-\frac{(A-B+C) \sqrt{\cos [c+d x]} \sin [c+d x]}{d(a+a \cos [c+d x])}$$

Result (type 5, 1973 leaves):

$$\frac{1}{2(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])(a+a \sec [c+d x])} + \frac{3 i A \cos \left[\frac{c}{2}+\frac{d x}{2}\right]^2 \cos [c+d x] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] (A+B \sec [c+d x]+C \sec [c+d x]^2)}{\left(\left(2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4},-e^{2 i d x}(\cos [c]+i \sin [c])^2\right]\right.\right. \\ \left.\left.\frac{\sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}}\right)}{\left(3 i d\left(1+e^{2 i d x}\right) \cos [c]-3 d\left(-1+e^{2 i d x}\right) \sin [c]\right)-\right.} \\ \left.\left(2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4},-e^{2 i d x}(\cos [c]+i \sin [c])^2\right]\right)\right. \\ \left.\frac{\sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}}\right)}{\left(-i d\left(1+e^{2 i d x}\right) \cos [c]+d\left(-1+e^{2 i d x}\right) \sin [c]\right)}\right) - \\ \frac{1}{2(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])(a+a \sec [c+d x])} + \frac{i B \cos \left[\frac{c}{2}+\frac{d x}{2}\right]^2 \cos [c+d x] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] (A+B \sec [c+d x]+C \sec [c+d x]^2)}{\left(\left(2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4},-e^{2 i d x}(\cos [c]+i \sin [c])^2\right]\right.\right. \\ \left.\left.\frac{\sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}}\right)}{\left(3 i d\left(1+e^{2 i d x}\right) \cos [c]-3 d\left(-1+e^{2 i d x}\right) \sin [c]\right)-\right.}$$

$$\begin{aligned}
 & \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) + \\
 & \quad \frac{1}{2 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])} \\
 & \quad i C \\
 & \quad \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \\
 & \quad \cos [c + d x] \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} \right] \\
 & \quad (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \quad \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right) \right. \\
 & \quad \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \quad \quad (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) - \\
 & \quad \quad \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right) \\
 & \quad \quad \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \quad \quad \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) + \\
 & \quad \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \cos [c + d x]^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left( -\frac{4 (A - B + C + 2 A \cos [c]) \operatorname{Csc} [c]}{d} - \right. \\
 & \quad \left. \left. \frac{4 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right] (A \sin \left[ \frac{d x}{2} \right] - B \sin \left[ \frac{d x}{2} \right] + C \sin \left[ \frac{d x}{2} \right])}{d} \right) \right) / \\
 & \quad \left( (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x]) \right) + \\
 & \quad \left( 2 A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \cos [c + d x] \operatorname{Csc} \left[ \frac{c}{2} \right] \right. \\
 & \quad \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \right]^2 \\
 & \quad \operatorname{Sec} \left[ \frac{c}{2} \right] (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \quad \left. \operatorname{Sec} [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \right)
 \end{aligned}$$

$$\left( \sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]} \sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]} \right) /$$

$$\left( d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{1+\cot[c]^2} (a + a \sec[c + dx]) \right) -$$

$$\left( 2B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c + dx] \csc\left[\frac{c}{2}\right] \right.$$

$$\text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\cot[c]]]^2\right]$$

$$\sec\left[\frac{c}{2}\right] (A + B \sec[c + dx] + C \sec[c + dx]^2)$$

$$\sec[dx - \text{ArcTan}[\cot[c]]] \sqrt{1 - \sin[dx - \text{ArcTan}[\cot[c]]]}$$

$$\left. \sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]} \sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]} \right) /$$

$$\left( d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{1+\cot[c]^2} (a + a \sec[c + dx]) \right) -$$

$$\left( 2C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c + dx] \csc\left[\frac{c}{2}\right] \right.$$

$$\text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\cot[c]]]^2\right]$$

$$\sec\left[\frac{c}{2}\right] (A + B \sec[c + dx] + C \sec[c + dx]^2)$$

$$\sec[dx - \text{ArcTan}[\cot[c]]] \sqrt{1 - \sin[dx - \text{ArcTan}[\cot[c]]]}$$

$$\left. \sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]} \sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]} \right) /$$

$$\left( d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{1+\cot[c]^2} (a + a \sec[c + dx]) \right)$$

**Problem 1221: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec[c + dx] + C \sec[c + dx]^2}{\sqrt{\cos[c + dx]} (a + a \sec[c + dx])} dx$$

Optimal (type 4, 122 leaves, 6 steps):

$$-\frac{(A - B + 3C) \text{EllipticE}\left[\frac{1}{2}(c + dx), 2\right]}{ad} + \frac{(A + B - C) \text{EllipticF}\left[\frac{1}{2}(c + dx), 2\right]}{ad} +$$

$$\frac{(A - B + 3C) \sin[c + dx]}{ad \sqrt{\cos[c + dx]}} - \frac{(A - B + C) \sin[c + dx]}{d \sqrt{\cos[c + dx]} (a + a \cos[c + dx])}$$

Result (type 5, 2009 leaves):

$$\begin{aligned}
 & \frac{1}{2(A+2C+2B \cos[c+dx]) (a+a \sec[c+dx])} \\
 & + \frac{i A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c+dx] \csc\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right] (A+B \sec[c+dx] + C \sec[c+dx]^2)}{\left( \left( 2 e^{2 i d x} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right. \right. \\
 & \quad \left. \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])} \right. \right. \\
 & \quad \left. \left. \sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]} \right) \right) / \\
 & \quad (3 i d (1 + e^{2 i d x}) \cos[c] - 3 d (-1 + e^{2 i d x}) \sin[c]) - \\
 & \quad \left( 2 \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right. \\
 & \quad \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])} \right. \\
 & \quad \left. \sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]} \right) / \\
 & \quad \left. (-i d (1 + e^{2 i d x}) \cos[c] + d (-1 + e^{2 i d x}) \sin[c]) \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{2(A+2C+2B \cos[c+dx]) (a+a \sec[c+dx])} \\
 & + \frac{i B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c+dx] \csc\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right] (A+B \sec[c+dx] + C \sec[c+dx]^2)}{\left( \left( 2 e^{2 i d x} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right. \right. \\
 & \quad \left. \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])} \right. \right. \\
 & \quad \left. \left. \sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]} \right) \right) / \\
 & \quad (3 i d (1 + e^{2 i d x}) \cos[c] - 3 d (-1 + e^{2 i d x}) \sin[c]) - \\
 & \quad \left( 2 \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right. \\
 & \quad \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])} \right. \\
 & \quad \left. \sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]} \right) / \\
 & \quad \left. (-i d (1 + e^{2 i d x}) \cos[c] + d (-1 + e^{2 i d x}) \sin[c]) \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{2(A+2C+2B \cos[c+dx]) (a+a \sec[c+dx])} \\
 & + \frac{3}{i}
 \end{aligned}$$

$$\begin{aligned}
 & C \\
 & \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \\
 & \cos[c + dx] \\
 & \csc\left[\frac{c}{2}\right] \\
 & \sec\left[\frac{c}{2}\right] \\
 & (A + B \sec[c + dx] + C \sec[c + dx]^2) \\
 & \left( \left( 2 e^{2i dx} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2i dx} (\cos[c] + i \sin[c])^2\right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i dx} (2 (1 + e^{2i dx}) \cos[c] + 2 i (-1 + e^{2i dx}) \sin[c])}}{\sqrt{1 + e^{2i dx} \cos[2c] + i e^{2i dx} \sin[2c]}} \right) / \\
 & \quad (3 i d (1 + e^{2i dx}) \cos[c] - 3 d (-1 + e^{2i dx}) \sin[c]) - \\
 & \quad \left( 2 \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i dx} (\cos[c] + i \sin[c])^2\right] \right. \\
 & \quad \left. \frac{\sqrt{e^{-i dx} (2 (1 + e^{2i dx}) \cos[c] + 2 i (-1 + e^{2i dx}) \sin[c])}}{\sqrt{1 + e^{2i dx} \cos[2c] + i e^{2i dx} \sin[2c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2i dx}) \cos[c] + d (-1 + e^{2i dx}) \sin[c]) \right) + \\
 & \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c + dx]^{3/2} (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\
 & \quad \left( \frac{2 (2 C + A \cos[c] - B \cos[c] + C \cos[c]) \csc\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right] \sec[c]}{d} + \right. \\
 & \quad \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right] (A \sin\left[\frac{dx}{2}\right] - B \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{d} + \\
 & \quad \left. \left. \frac{8 C \sec[c] \sec[c + dx] \sin[dx]}{d} \right) \right) / \\
 & \left( (A + 2 C + 2 B \cos[c + dx] + A \cos[2c + 2dx]) (a + a \sec[c + dx]) \right) - \\
 & \left( 2 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \cos[c + dx] \csc\left[\frac{c}{2}\right] \right. \\
 & \quad \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\text{Cot}[c]]]^2\right] \\
 & \quad \sec\left[\frac{c}{2}\right] (A + B \sec[c + dx] + C \sec[c + dx]^2) \\
 & \quad \sec[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \sin[dx - \text{ArcTan}[\text{Cot}[c]]]} \\
 & \quad \left. \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\text{Cot}[c]]]} \right)
 \end{aligned}$$



$$\begin{aligned}
 & \left. \sqrt{1 + \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \right) / \\
 & \left( d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \text{Cot} [c]^2} (a + a \sec [c + d x]) \right) - \\
 & \left( 2 B \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \cos [c + d x] \csc \left[ \frac{c}{2} \right] \right. \\
 & \quad \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \text{ArcTan} [\text{Cot} [c]]]^2 \right] \\
 & \quad \sec \left[ \frac{c}{2} \right] (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \quad \sec [d x - \text{ArcTan} [\text{Cot} [c]]] \sqrt{1 - \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \\
 & \quad \left. \sqrt{-\sqrt{1 + \text{Cot} [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\text{Cot} [c]]] \sqrt{1 + \sin [d x - \text{ArcTan} [\text{Cot} [c]]}} \right) / \\
 & \left( d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \text{Cot} [c]^2} (a + a \sec [c + d x]) \right) + \\
 & \left( 2 C \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \cos [c + d x] \csc \left[ \frac{c}{2} \right] \right. \\
 & \quad \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \text{ArcTan} [\text{Cot} [c]]]^2 \right] \\
 & \quad \sec \left[ \frac{c}{2} \right] (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \quad \sec [d x - \text{ArcTan} [\text{Cot} [c]]] \sqrt{1 - \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \\
 & \quad \left. \sqrt{-\sqrt{1 + \text{Cot} [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\text{Cot} [c]]] \sqrt{1 + \sin [d x - \text{ArcTan} [\text{Cot} [c]]}} \right) / \\
 & \left( d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \text{Cot} [c]^2} (a + a \sec [c + d x]) \right)
 \end{aligned}$$

**Problem 1222: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec [c + d x] + C \sec [c + d x]^2}{\cos [c + d x]^{3/2} (a + a \sec [c + d x])} dx$$

Optimal (type 4, 165 leaves, 7 steps):

$$\begin{aligned}
 & \frac{(A - 3 B + 3 C) \text{EllipticE} \left[ \frac{1}{2} (c + d x), 2 \right]}{a d} + \frac{(3 A - 3 B + 5 C) \text{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right]}{3 a d} + \\
 & \frac{(3 A - 3 B + 5 C) \sin [c + d x]}{3 a d \cos [c + d x]^{3/2}} - \frac{(A - 3 B + 3 C) \sin [c + d x]}{a d \sqrt{\cos [c + d x]}} - \frac{(A - B + C) \sin [c + d x]}{d \cos [c + d x]^{3/2} (a + a \cos [c + d x])}
 \end{aligned}$$

Result (type 5, 2052 leaves):

$$\frac{1}{2 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])} \\ + A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \cos [c + d x] \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} \right] (A + B \sec [c + d x] + C \sec [c + d x]^2) \\ \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c]) \right]^2 \right) \right. \\ \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\ (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) - \\ \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c]) \right]^2 \right) \\ \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\ \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) -$$

$$\frac{1}{2 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])} \\ + 3 i B \\ \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \cos [c + d x] \\ \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} \right] \\ (A + B \sec [c + d x] + C \sec [c + d x]^2) \\ \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c]) \right]^2 \right) \right. \\ \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\ (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) - \\ \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c]) \right]^2 \right) \\ \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\ \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) +$$

$$\frac{1}{2 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])} \\ + 3 i C \\ \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \cos [c + d x] \\ \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} \right] \\ (A + B \sec [c + d x] + C \sec [c + d x]^2)$$

$$\begin{aligned}
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c]) \right]^2 \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \quad (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) - \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c]) \right]^2 \right) \\
 & \quad \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) + \\
 & \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \cos [c + d x]^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left( -\frac{1}{d} 2 (-2 B + 2 C + A \cos [c] - B \cos [c] + C \cos [c]) \operatorname{Csc} \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} \right] \sec [c] - \right. \\
 & \quad \frac{4 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right] (A \sin \left[ \frac{d x}{2} \right] - B \sin \left[ \frac{d x}{2} \right] + C \sin \left[ \frac{d x}{2} \right])}{d} + \\
 & \quad \frac{8 C \sec [c] \sec [c + d x]^2 \sin [d x]}{3 d} + \\
 & \quad \left. \left. \frac{8 \sec [c] \sec [c + d x] (C \sin [c] + 3 B \sin [d x] - 3 C \sin [d x])}{3 d} \right) \right) / \\
 & \quad \left( (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x]) \right) - \\
 & \quad \left( 2 A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \cos [c + d x] \operatorname{Csc} \left[ \frac{c}{2} \right] \right. \\
 & \quad \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right]^2 \\
 & \quad \sec \left[ \frac{c}{2} \right] (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \quad \sec [d x - \operatorname{ArcTan} [\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan} [\cot [c]]]} \\
 & \quad \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]]} \\
 & \quad \left. \left. \sqrt{1 + \sin [d x - \operatorname{ArcTan} [\cot [c]]]} \right) \right) / \\
 & \quad \left( d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} (a + a \sec [c + d x]) \right) + \\
 & \quad \left( 2 B \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \cos [c + d x] \operatorname{Csc} \left[ \frac{c}{2} \right] \right.
 \end{aligned}$$

$$\begin{aligned} & \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin\left[d x - \text{ArcTan}[\text{Cot}[c]]\right]^2\right] \\ & \text{Sec}\left[\frac{c}{2}\right] (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) \\ & \text{Sec}\left[d x - \text{ArcTan}[\text{Cot}[c]]\right] \sqrt{1 - \sin\left[d x - \text{ArcTan}[\text{Cot}[c]]\right]} \\ & \left. \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \sin[c] \sin\left[d x - \text{ArcTan}[\text{Cot}[c]]\right]} \sqrt{1 + \sin\left[d x - \text{ArcTan}[\text{Cot}[c]]\right]}\right) / \\ & \left( d (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) \sqrt{1 + \text{Cot}[c]^2} (a + a \text{Sec}[c + d x]) \right) - \\ & \left( 10 C \cos\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \cos[c + d x] \text{Csc}\left[\frac{c}{2}\right] \right. \\ & \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin\left[d x - \text{ArcTan}[\text{Cot}[c]]\right]^2\right] \\ & \text{Sec}\left[\frac{c}{2}\right] (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) \\ & \text{Sec}\left[d x - \text{ArcTan}[\text{Cot}[c]]\right] \sqrt{1 - \sin\left[d x - \text{ArcTan}[\text{Cot}[c]]\right]} \\ & \left. \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \sin[c] \sin\left[d x - \text{ArcTan}[\text{Cot}[c]]\right]} \sqrt{1 + \sin\left[d x - \text{ArcTan}[\text{Cot}[c]]\right]}\right) / \\ & \left( 3 d (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) \sqrt{1 + \text{Cot}[c]^2} (a + a \text{Sec}[c + d x]) \right) \end{aligned}$$

**Problem 1223: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2}{\cos[c + d x]^{5/2} (a + a \text{Sec}[c + d x])} dx$$

Optimal (type 4, 210 leaves, 8 steps):

$$\begin{aligned} & \frac{3 (5 A - 5 B + 7 C) \text{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] - (3 A - 5 B + 5 C) \text{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{5 a d} + \\ & \frac{(5 A - 5 B + 7 C) \sin[c + d x]}{5 a d \cos[c + d x]^{5/2}} - \frac{(3 A - 5 B + 5 C) \sin[c + d x]}{3 a d \cos[c + d x]^{3/2}} + \\ & \frac{3 (5 A - 5 B + 7 C) \sin[c + d x]}{5 a d \sqrt{\cos[c + d x]}} - \frac{(A - B + C) \sin[c + d x]}{d \cos[c + d x]^{5/2} (a + a \cos[c + d x])} \end{aligned}$$

Result (type 5, 2111 leaves):

$$\begin{aligned} & \frac{1}{2 (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) (a + a \text{Sec}[c + d x])} \\ & 3 i A \cos\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \cos[c + d x] \text{Csc}\left[\frac{c}{2}\right] \text{Sec}\left[\frac{c}{2}\right] (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) \\ & \left( \left( 2 e^{2 i d x} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right) \right) \end{aligned}$$

$$\begin{aligned}
 & \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \Big/ \\
 & \left( 3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c] \right) - \\
 & \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right) \\
 & \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \Big/ \\
 & \left( -i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c] \right) \Big) + \\
 & \frac{1}{2 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])} \\
 & 3 \\
 & i \\
 & B \\
 & \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \\
 & \cos [c + d x] \\
 & \operatorname{Csc} \left[ \frac{c}{2} \right] \\
 & \operatorname{Sec} \left[ \frac{c}{2} \right] \\
 & (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right) \right. \\
 & \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \Big/ \\
 & \left. (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) \right) - \\
 & \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right) \\
 & \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \Big/ \\
 & \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) \Big) - \\
 & \frac{1}{10 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])} \\
 & 21 \\
 & i \\
 & C \\
 & \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \\
 & \cos [c + d x]
 \end{aligned}$$

$$\begin{aligned}
 & \text{Csc}\left[\frac{c}{2}\right] \text{Sec}\left[\frac{c}{2}\right] \\
 & (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \\
 & \left( \left( 2 e^{2 i dx} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i dx} (\text{Cos}[c] + i \text{Sin}[c])\right]^2 \right) \right. \\
 & \quad \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \text{Cos}[c] + 2 i (-1 + e^{2 i dx}) \text{Sin}[c])}}{\sqrt{1 + e^{2 i dx} \text{Cos}[2 c] + i e^{2 i dx} \text{Sin}[2 c]}} \Bigg) / \\
 & \quad (3 i d (1 + e^{2 i dx}) \text{Cos}[c] - 3 d (-1 + e^{2 i dx}) \text{Sin}[c]) - \\
 & \quad \left( 2 \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i dx} (\text{Cos}[c] + i \text{Sin}[c])\right]^2 \right) \\
 & \quad \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \text{Cos}[c] + 2 i (-1 + e^{2 i dx}) \text{Sin}[c])}}{\sqrt{1 + e^{2 i dx} \text{Cos}[2 c] + i e^{2 i dx} \text{Sin}[2 c]}} \Bigg) / \\
 & \quad \left. (-i d (1 + e^{2 i dx}) \text{Cos}[c] + d (-1 + e^{2 i dx}) \text{Sin}[c]) \right) + \\
 & \quad \frac{1}{(A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2 c + 2 dx]) (a + a \text{Sec}[c + dx])} \\
 & \text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \\
 & \text{Cos}[c + dx]^{3/2} \\
 & (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \\
 & \left( \frac{1}{5 d} 2 (10 A - 10 B + 16 C + 5 A \text{Cos}[c] - 5 B \text{Cos}[c] + 5 C \text{Cos}[c]) \text{Csc}\left[\frac{c}{2}\right] \text{Sec}\left[\frac{c}{2}\right] \text{Sec}[c] + \right. \\
 & \quad \frac{4 \text{Sec}\left[\frac{c}{2}\right] \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] (A \text{Sin}\left[\frac{dx}{2}\right] - B \text{Sin}\left[\frac{dx}{2}\right] + C \text{Sin}\left[\frac{dx}{2}\right])}{d} + \\
 & \quad \frac{8 C \text{Sec}[c] \text{Sec}[c + dx]^3 \text{Sin}[dx]}{5 d} - \frac{1}{15 d} \\
 & \quad 8 \text{Sec}[c] \text{Sec}[c + dx] (-5 B \text{Sin}[c] + 5 C \text{Sin}[c] - 15 A \text{Sin}[dx] + 15 B \text{Sin}[dx] - 24 C \text{Sin}[dx]) + \\
 & \quad \left. \frac{8 \text{Sec}[c] \text{Sec}[c + dx]^2 (3 C \text{Sin}[c] + 5 B \text{Sin}[dx] - 5 C \text{Sin}[dx])}{15 d} \right) + \\
 & \left( 2 A \text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \text{Cos}[c + dx] \text{Csc}\left[\frac{c}{2}\right] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \right. \right. \\
 & \quad \left. \left. \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]^2 \right] \text{Sec}\left[\frac{c}{2}\right] (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \right. \\
 & \quad \left. \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right. \\
 & \quad \left. \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right. \\
 & \quad \left. \sqrt{1 + \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sqrt{1 + \cot [c]^2} (a + a \sec [c + dx]) \right) - \\
 & \left( 10 B \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \cos [c + dx] \operatorname{Csc} \left[ \frac{c}{2} \right] \right. \\
 & \quad \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [dx - \operatorname{ArcTan} [\cot [c]]]^2 \right] \\
 & \quad \sec \left[ \frac{c}{2} \right] (A + B \sec [c + dx] + C \sec [c + dx]^2) \\
 & \quad \sec [dx - \operatorname{ArcTan} [\cot [c]]] \sqrt{1 - \sin [dx - \operatorname{ArcTan} [\cot [c]]]} \\
 & \quad \left. \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [dx - \operatorname{ArcTan} [\cot [c]]] \sqrt{1 + \sin [dx - \operatorname{ArcTan} [\cot [c]]]} \right) / \\
 & \left( 3 d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sqrt{1 + \cot [c]^2} (a + a \sec [c + dx]) \right) + \\
 & \left( 10 C \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \cos [c + dx] \operatorname{Csc} \left[ \frac{c}{2} \right] \right. \\
 & \quad \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [dx - \operatorname{ArcTan} [\cot [c]]]^2 \right] \\
 & \quad \sec \left[ \frac{c}{2} \right] (A + B \sec [c + dx] + C \sec [c + dx]^2) \\
 & \quad \sec [dx - \operatorname{ArcTan} [\cot [c]]] \sqrt{1 - \sin [dx - \operatorname{ArcTan} [\cot [c]]]} \\
 & \quad \left. \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [dx - \operatorname{ArcTan} [\cot [c]]] \sqrt{1 + \sin [dx - \operatorname{ArcTan} [\cot [c]]]} \right) / \\
 & \left( 3 d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sqrt{1 + \cot [c]^2} (a + a \sec [c + dx]) \right)
 \end{aligned}$$

**Problem 1224: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\cos [c + dx]^{7/2} (A + B \sec [c + dx] + C \sec [c + dx]^2)}{(a + a \sec [c + dx])^2} dx$$

Optimal (type 4, 258 leaves, 9 steps):

$$\begin{aligned}
 & - \frac{7 (11A - 8B + 5C) \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right]}{5a^2d} + \\
 & \frac{5 (30A - 21B + 14C) \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right]}{21a^2d} + \frac{5 (30A - 21B + 14C) \sqrt{\cos[c + dx]} \sin[c + dx]}{21a^2d} - \\
 & \frac{7 (11A - 8B + 5C) \cos[c + dx]^{3/2} \sin[c + dx]}{15a^2d} + \frac{(30A - 21B + 14C) \cos[c + dx]^{5/2} \sin[c + dx]}{7a^2d} - \\
 & \frac{(11A - 8B + 5C) \cos[c + dx]^{7/2} \sin[c + dx]}{3a^2d(1 + \cos[c + dx])} - \frac{(A - B + C) \cos[c + dx]^{9/2} \sin[c + dx]}{3d(a + a \cos[c + dx])^2}
 \end{aligned}$$

Result (type 5, 2174 leaves):

$$\begin{aligned}
 & - \frac{1}{5(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) (a + a \sec[c + dx])^2} \\
 & 77iA \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \sec[c + dx] + C \sec[c + dx])^2 \\
 & \left( \left( 2e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix}(\cos[c] + i \sin[c])^2\right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-ix}(2(1 + e^{2ix})\cos[c] + 2i(-1 + e^{2ix})\sin[c])}}{\sqrt{1 + e^{2ix}\cos[2c] + ie^{2ix}\sin[2c]}} \right) / \\
 & \quad (3id(1 + e^{2ix})\cos[c] - 3d(-1 + e^{2ix})\sin[c]) - \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix}(\cos[c] + i \sin[c])^2\right] \right. \\
 & \quad \left. \frac{\sqrt{e^{-ix}(2(1 + e^{2ix})\cos[c] + 2i(-1 + e^{2ix})\sin[c])}}{\sqrt{1 + e^{2ix}\cos[2c] + ie^{2ix}\sin[2c]}} \right) / \\
 & \quad \left. (-id(1 + e^{2ix})\cos[c] + d(-1 + e^{2ix})\sin[c]) \right) + \\
 & \frac{1}{5(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) (a + a \sec[c + dx])^2} \\
 & 56 \\
 & i \\
 & B \\
 & \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \\
 & \operatorname{Csc}\left[\frac{c}{2}\right] \\
 & \operatorname{Sec}\left[\frac{c}{2}\right] \\
 & (A + B \sec[c + dx] + C \sec[c + dx])^2 \\
 & \left( \left( 2e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix}(\cos[c] + i \sin[c])^2\right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-ix}(2(1 + e^{2ix})\cos[c] + 2i(-1 + e^{2ix})\sin[c])}}{\sqrt{1 + e^{2ix}\cos[2c] + ie^{2ix}\sin[2c]}} \right) /
 \end{aligned}$$





$$\left( 20 B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \csc\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin\left[dx - \operatorname{ArcTan}[\cot[c]]\right]\right]^2 \right. \\ \left. \sec\left[\frac{c}{2}\right] (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\ \left. \sec\left[dx - \operatorname{ArcTan}[\cot[c]]\right] \sqrt{1 - \sin\left[dx - \operatorname{ArcTan}[\cot[c]]\right]} \right. \\ \left. \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin\left[dx - \operatorname{ArcTan}[\cot[c]]\right]} \right. \\ \left. \sqrt{1 + \sin\left[dx - \operatorname{ArcTan}[\cot[c]]\right]} \right) / \\ \left( d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{1 + \cot[c]^2} (a + a \sec[c + dx])^2 \right) - \\ \left( 40 C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \csc\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin\left[dx - \operatorname{ArcTan}[\cot[c]]\right]\right]^2 \right. \\ \left. \sec\left[\frac{c}{2}\right] (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\ \left. \sec\left[dx - \operatorname{ArcTan}[\cot[c]]\right] \sqrt{1 - \sin\left[dx - \operatorname{ArcTan}[\cot[c]]\right]} \right. \\ \left. \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin\left[dx - \operatorname{ArcTan}[\cot[c]]\right]} \sqrt{1 + \sin\left[dx - \operatorname{ArcTan}[\cot[c]]\right]} \right) / \\ \left( 3 d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{1 + \cot[c]^2} (a + a \sec[c + dx])^2 \right) + \\ \frac{1}{(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) (a + a \sec[c + dx])^2} \\ \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c + dx]} \\ (A + B \sec[c + dx] + C \sec[c + dx]^2) \\ \left( \frac{1}{5d} 8 (25A - 20B + 15C + 52A \cos[c] - 36B \cos[c] + 20C \cos[c]) \csc[c] + \right. \\ \frac{4 (107A - 56B + 28C) \cos[dx] \sin[c]}{21d} - \frac{8 (2A - B) \cos[2dx] \sin[2c]}{5d} + \\ \frac{4A \cos[3dx] \sin[3c]}{7d} - \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (A \sin\left[\frac{dx}{2}\right] - B \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{3d} + \\ \frac{8 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right] (5A \sin\left[\frac{dx}{2}\right] - 4B \sin\left[\frac{dx}{2}\right] + 3C \sin\left[\frac{dx}{2}\right])}{d} + \\ \frac{4 (107A - 56B + 28C) \cos[c] \sin[dx]}{21d} - \frac{8 (2A - B) \cos[2c] \sin[2dx]}{5d} + \\ \left. \frac{4A \cos[3c] \sin[3dx]}{7d} - \frac{4 (A - B + C) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{3d} \right)$$

Problem 1225: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^{5 / 2} (A+B \sec [c+d x]+C \sec [c+d x]^2)}{(a+a \sec [c+d x])^2} d x$$

Optimal (type 4, 214 leaves, 8 steps):

$$\frac{(56 A-35 B+20 C) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 a^2 d}-\frac{5(3 A-2 B+C) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{3 a^2 d}-\frac{5(3 A-2 B+C) \sqrt{\cos [c+d x]} \sin [c+d x]}{3 a^2 d}+\frac{(56 A-35 B+20 C) \cos [c+d x]^{3 / 2} \sin [c+d x]}{15 a^2 d}-\frac{(3 A-2 B+C) \cos [c+d x]^{5 / 2} \sin [c+d x]}{a^2 d(1+\cos [c+d x])}-\frac{(A-B+C) \cos [c+d x]^{7 / 2} \sin [c+d x]}{3 d(a+a \cos [c+d x])^2}$$

Result (type 5, 2120 leaves):

$$\frac{1}{5(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])(a+a \sec [c+d x])^2} \\ 56 i A \cos \left[\frac{c}{2}+\frac{d x}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \sec \left[\frac{c}{2}\right] (A+B \sec [c+d x]+C \sec [c+d x]^2) \\ \left(\left(2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4},-e^{2 i d x}(\cos [c]+i \sin [c])\right]^2\right) \sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)} \sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}\right) / \\ (3 i d\left(1+e^{2 i d x}\right) \cos [c]-3 d\left(-1+e^{2 i d x}\right) \sin [c])- \\ \left(2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4},-e^{2 i d x}(\cos [c]+i \sin [c])\right]^2\right) \sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)} \sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}\right) / \\ (-i d\left(1+e^{2 i d x}\right) \cos [c]+d\left(-1+e^{2 i d x}\right) \sin [c])\right) - \\ \frac{1}{(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])(a+a \sec [c+d x])^2} \\ 7 i B \\ \cos \left[\frac{c}{2}+\frac{d x}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \sec \left[\frac{c}{2}\right] \\ (A+B \sec [c+d x]+C \sec [c+d x]^2) \\ \left(\left(2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4},-e^{2 i d x}(\cos [c]+i \sin [c])\right]^2\right) \sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)} \sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}\right) /$$

$$\begin{aligned}
& \left( 3 i d (1 + e^{2 i d x}) \operatorname{Cos}[c] - 3 d (-1 + e^{2 i d x}) \operatorname{Sin}[c] \right) - \\
& \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right. \\
& \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]}} \right) / \\
& \left. (-i d (1 + e^{2 i d x}) \operatorname{Cos}[c] + d (-1 + e^{2 i d x}) \operatorname{Sin}[c]) \right) + \\
& \quad \frac{1}{(A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) (a + a \operatorname{Sec}[c + d x])^2} \\
& 4 i C \\
& \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^4 \\
& \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \\
& (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\
& \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right. \right. \\
& \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]}} \right) / \\
& \left. (3 i d (1 + e^{2 i d x}) \operatorname{Cos}[c] - 3 d (-1 + e^{2 i d x}) \operatorname{Sin}[c]) - \right. \\
& \left. \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right. \right. \\
& \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]}} \right) / \\
& \left. (-i d (1 + e^{2 i d x}) \operatorname{Cos}[c] + d (-1 + e^{2 i d x}) \operatorname{Sin}[c]) \right) + \\
& \left( 20 A \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2 \right) \\
& \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\
& \operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
& \frac{\sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}}{\sqrt{1 + \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \Bigg) / \\
& \left( d (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2} (a + a \operatorname{Sec}[c + d x])^2 \right) - \\
& \left( 40 B \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2 \right)
\end{aligned}$$

$$\begin{aligned}
 & \sec\left[\frac{c}{2}\right] (A + B \sec[c + dx] + C \sec[c + dx]^2) \\
 & \sec[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \sin[dx - \text{ArcTan}[\text{Cot}[c]]]} \\
 & \left. \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 + \sin[dx - \text{ArcTan}[\text{Cot}[c]]}} \right) / \\
 & \left( 3d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{1 + \text{Cot}[c]^2} (a + a \sec[c + dx])^2 \right) + \\
 & \left( 20C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \text{Csc}\left[\frac{c}{2}\right] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\text{Cot}[c]]]^2\right] \right. \\
 & \left. \sec\left[\frac{c}{2}\right] (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\
 & \left. \sec[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \sin[dx - \text{ArcTan}[\text{Cot}[c]]]} \right. \\
 & \left. \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 + \sin[dx - \text{ArcTan}[\text{Cot}[c]]}} \right) / \\
 & \left( 3d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{1 + \text{Cot}[c]^2} (a + a \sec[c + dx])^2 \right) + \\
 & \frac{1}{(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) (a + a \sec[c + dx])^2} \\
 & \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c + dx]} \\
 & (A + B \sec[c + dx] + C \sec[c + dx]^2) \\
 & \left( -\frac{1}{5d} 8 (20A - 15B + 10C + 36A \cos[c] - 20B \cos[c] + 10C \cos[c]) \text{Csc}[c] - \right. \\
 & \frac{16(2A - B) \cos[dx] \sin[c]}{3d} + \frac{8A \cos[2dx] \sin[2c]}{5d} + \\
 & \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (A \sin\left[\frac{dx}{2}\right] - B \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{3d} - \\
 & \left. \frac{8 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right] (4A \sin\left[\frac{dx}{2}\right] - 3B \sin\left[\frac{dx}{2}\right] + 2C \sin\left[\frac{dx}{2}\right])}{d} - \right. \\
 & \left. \frac{16(2A - B) \cos[c] \sin[dx]}{3d} + \frac{8A \cos[2c] \sin[2dx]}{5d} + \frac{4(A - B + C) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{3d} \right)
 \end{aligned}$$

**Problem 1226: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c + dx]^{3/2} (A + B \sec[c + dx] + C \sec[c + dx]^2)}{(a + a \sec[c + dx])^2} dx$$

Optimal (type 4, 180 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{(7A - 4B + C) \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right]}{a^2 d} + \\
 & \frac{(10A - 5B + 2C) \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right]}{3a^2 d} + \frac{(10A - 5B + 2C) \sqrt{\cos[c + dx]} \sin[c + dx]}{3a^2 d} - \\
 & \frac{(7A - 4B + C) \cos[c + dx]^{3/2} \sin[c + dx]}{3a^2 d (1 + \cos[c + dx])} - \frac{(A - B + C) \cos[c + dx]^{5/2} \sin[c + dx]}{3d (a + a \cos[c + dx])^2}
 \end{aligned}$$

Result (type 5, 2064 leaves):

$$\begin{aligned}
 & - \frac{1}{(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) (a + a \sec[c + dx])^2} \\
 & 7i A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \sec[c + dx] + C \sec[c + dx]^2) \\
 & \left( \left( 2 e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix} (\cos[c] + i \sin[c])^2\right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-ix} (2(1 + e^{2ix}) \cos[c] + 2i(-1 + e^{2ix}) \sin[c])}}{\sqrt{1 + e^{2ix} \cos[2c] + i e^{2ix} \sin[2c]}} \right) / \\
 & \quad (3i d (1 + e^{2ix}) \cos[c] - 3d(-1 + e^{2ix}) \sin[c]) - \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix} (\cos[c] + i \sin[c])^2\right] \right. \\
 & \quad \left. \frac{\sqrt{e^{-ix} (2(1 + e^{2ix}) \cos[c] + 2i(-1 + e^{2ix}) \sin[c])}}{\sqrt{1 + e^{2ix} \cos[2c] + i e^{2ix} \sin[2c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2ix}) \cos[c] + d(-1 + e^{2ix}) \sin[c]) \right) + \\
 & \frac{1}{(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) (a + a \sec[c + dx])^2} \\
 & 4 \\
 & i \\
 & B \\
 & \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \\
 & \operatorname{Csc}\left[\frac{c}{2}\right] \\
 & \operatorname{Sec}\left[\frac{c}{2}\right] \\
 & (A + B \sec[c + dx] + C \sec[c + dx]^2) \\
 & \left( \left( 2 e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix} (\cos[c] + i \sin[c])^2\right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-ix} (2(1 + e^{2ix}) \cos[c] + 2i(-1 + e^{2ix}) \sin[c])}}{\sqrt{1 + e^{2ix} \cos[2c] + i e^{2ix} \sin[2c]}} \right) / \\
 & \quad (3i d (1 + e^{2ix}) \cos[c] - 3d(-1 + e^{2ix}) \sin[c]) - \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix} (\cos[c] + i \sin[c])^2\right] \right. \\
 & \quad \left. \frac{\sqrt{e^{-ix} (2(1 + e^{2ix}) \cos[c] + 2i(-1 + e^{2ix}) \sin[c])}}{\sqrt{1 + e^{2ix} \cos[2c] + i e^{2ix} \sin[2c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2ix}) \cos[c] + d(-1 + e^{2ix}) \sin[c]) \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \cos [c] + 2 i (-1 + e^{2 i dx}) \sin [c])}}{\sqrt{1 + e^{2 i dx} \cos [2 c] + i e^{2 i dx} \sin [2 c]}} \Big/ \\
 & \left( -i d (1 + e^{2 i dx}) \cos [c] + d (-1 + e^{2 i dx}) \sin [c] \right) - \\
 & \frac{1}{(A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^2} \\
 & i \\
 & C \\
 & \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \\
 & \operatorname{Csc} \left[ \frac{c}{2} \right] \\
 & \operatorname{Sec} \left[ \frac{c}{2} \right] \\
 & (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \left( \left( 2 e^{2 i dx} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i dx} (\cos [c] + i \sin [c])^2 \right] \right. \right. \\
 & \left. \left. \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \cos [c] + 2 i (-1 + e^{2 i dx}) \sin [c])}}{\sqrt{1 + e^{2 i dx} \cos [2 c] + i e^{2 i dx} \sin [2 c]}} \right) \Big/ \right. \\
 & \left. (3 i d (1 + e^{2 i dx}) \cos [c] - 3 d (-1 + e^{2 i dx}) \sin [c]) - \right. \\
 & \left. \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i dx} (\cos [c] + i \sin [c])^2 \right] \right) \right. \\
 & \left. \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \cos [c] + 2 i (-1 + e^{2 i dx}) \sin [c])}}{\sqrt{1 + e^{2 i dx} \cos [2 c] + i e^{2 i dx} \sin [2 c]}} \right) \Big/ \\
 & \left. (-i d (1 + e^{2 i dx}) \cos [c] + d (-1 + e^{2 i dx}) \sin [c]) \right) - \\
 & \left( 40 A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \right]^2 \right) \\
 & \operatorname{Sec} \left[ \frac{c}{2} \right] (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \operatorname{Sec} [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \\
 & \sqrt{-\sqrt{1 + \operatorname{Cot} [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \\
 & \left. \sqrt{1 + \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \right) \Big/ \\
 & \left( 3 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \operatorname{Cot} [c]^2} (a + a \sec [c + d x])^2 \right) + \\
 & \left( 20 B \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \right]^2 \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \begin{aligned}
 & \text{Sec}\left[\frac{c}{2}\right] (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \\
 & \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \\
 & \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \\
 & \sqrt{1 + \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \Big) / \\
 & \left( 3d (A + 2C + 2B \text{Cos}[c + dx] + A \text{Cos}[2c + 2dx]) \sqrt{1 + \text{Cot}[c]^2} (a + a \text{Sec}[c + dx])^2 \right) - \\
 & \left( 8C \text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \text{Csc}\left[\frac{c}{2}\right] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]^2\right] \right. \\
 & \left. \text{Sec}\left[\frac{c}{2}\right] (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \right. \\
 & \left. \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right. \\
 & \left. \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \sqrt{1 + \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \right) / \\
 & \left( 3d (A + 2C + 2B \text{Cos}[c + dx] + A \text{Cos}[2c + 2dx]) \sqrt{1 + \text{Cot}[c]^2} (a + a \text{Sec}[c + dx])^2 \right) + \\
 & \left( \text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\text{Cos}[c + dx]} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \right. \\
 & \left( \frac{8(3A - 2B + C + 4A \text{Cos}[c] - 2B \text{Cos}[c]) \text{Csc}[c]}{d} + \frac{16A \text{Cos}[dx] \text{Sin}[c]}{3d} + \right. \\
 & \frac{8 \text{Sec}\left[\frac{c}{2}\right] \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] (3A \text{Sin}\left[\frac{dx}{2}\right] - 2B \text{Sin}\left[\frac{dx}{2}\right] + C \text{Sin}\left[\frac{dx}{2}\right])}{d} - \\
 & \frac{4 \text{Sec}\left[\frac{c}{2}\right] \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (A \text{Sin}\left[\frac{dx}{2}\right] - B \text{Sin}\left[\frac{dx}{2}\right] + C \text{Sin}\left[\frac{dx}{2}\right])}{3d} + \\
 & \left. \left. \frac{16A \text{Cos}[c] \text{Sin}[dx]}{3d} - \frac{4(A - B + C) \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \text{Tan}\left[\frac{c}{2}\right]}{3d} \right) \right) / \\
 & \left( (A + 2C + 2B \text{Cos}[c + dx] + A \text{Cos}[2c + 2dx]) (a + a \text{Sec}[c + dx])^2 \right)
 \end{aligned}
 \end{aligned}$$

**Problem 1227: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\text{Cos}[c + dx]} (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2)}{(a + a \text{Sec}[c + dx])^2} dx$$

Optimal (type 4, 144 leaves, 6 steps):



$$\frac{(4A - B) \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right]}{a^2 d} - \frac{(5A - 2B - C) \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right]}{3 a^2 d} - \frac{(5A - 2B - C) \sqrt{\cos[c + dx]} \operatorname{Sin}[c + dx]}{3 a^2 d (1 + \cos[c + dx])} - \frac{(A - B + C) \cos[c + dx]^{3/2} \operatorname{Sin}[c + dx]}{3 d (a + a \cos[c + dx])^2}$$

Result (type 5, 1628 leaves):

$$\frac{1}{(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) (a + a \sec[c + dx])^2} \left( 4i A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\ \left. \left( \left( 2 e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix} (\cos[c] + i \sin[c])^2\right] \right. \right. \right. \\ \left. \left. \sqrt{e^{-ix} (2(1 + e^{2ix}) \cos[c] + 2i(-1 + e^{2ix}) \sin[c])} \right. \right. \\ \left. \left. \sqrt{1 + e^{2ix} \cos[2c] + i e^{2ix} \sin[2c]} \right) / \right. \\ \left. (3id(1 + e^{2ix}) \cos[c] - 3d(-1 + e^{2ix}) \sin[c]) - \right. \\ \left. \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix} (\cos[c] + i \sin[c])^2\right] \right. \right. \\ \left. \left. \sqrt{e^{-ix} (2(1 + e^{2ix}) \cos[c] + 2i(-1 + e^{2ix}) \sin[c])} \right. \right. \\ \left. \left. \sqrt{1 + e^{2ix} \cos[2c] + i e^{2ix} \sin[2c]} \right) / \right. \\ \left. (-id(1 + e^{2ix}) \cos[c] + d(-1 + e^{2ix}) \sin[c]) \right) - \\ \frac{1}{(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) (a + a \sec[c + dx])^2} \\ i B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \\ \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \\ (A + B \sec[c + dx] + C \sec[c + dx]^2) \\ \left( \left( 2 e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix} (\cos[c] + i \sin[c])^2\right] \right. \right. \\ \left. \left. \sqrt{e^{-ix} (2(1 + e^{2ix}) \cos[c] + 2i(-1 + e^{2ix}) \sin[c])} \right. \right. \\ \left. \left. \sqrt{1 + e^{2ix} \cos[2c] + i e^{2ix} \sin[2c]} \right) / \right. \\ \left. (3id(1 + e^{2ix}) \cos[c] - 3d(-1 + e^{2ix}) \sin[c]) - \right. \\ \left. \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix} (\cos[c] + i \sin[c])^2\right] \right. \right. \\ \left. \left. \sqrt{e^{-ix} (2(1 + e^{2ix}) \cos[c] + 2i(-1 + e^{2ix}) \sin[c])} \right. \right. \\ \left. \left. \sqrt{1 + e^{2ix} \cos[2c] + i e^{2ix} \sin[2c]} \right) / \right. \\ \left. (-id(1 + e^{2ix}) \cos[c] + d(-1 + e^{2ix}) \sin[c]) \right) +$$

$$\left( 20 A \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 \csc \left[ \frac{c}{2} \right] \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [dx - \text{ArcTan} [\text{Cot} [c]]] \right]^2 \right. \\
 \left. \sec \left[ \frac{c}{2} \right] (A + B \sec [c + dx] + C \sec [c + dx]^2) \right. \\
 \left. \sec [dx - \text{ArcTan} [\text{Cot} [c]]] \sqrt{1 - \sin [dx - \text{ArcTan} [\text{Cot} [c]]]} \right. \\
 \left. \sqrt{-\sqrt{1 + \text{Cot} [c]^2} \sin [c] \sin [dx - \text{ArcTan} [\text{Cot} [c]]]} \right. \\
 \left. \sqrt{1 + \sin [dx - \text{ArcTan} [\text{Cot} [c]]]} \right) / \\
 \left( 3d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sqrt{1 + \text{Cot} [c]^2} (a + a \sec [c + dx])^2 \right) - \\
 \left( 8B \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 \csc \left[ \frac{c}{2} \right] \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [dx - \text{ArcTan} [\text{Cot} [c]]] \right]^2 \right. \\
 \left. \sec \left[ \frac{c}{2} \right] (A + B \sec [c + dx] + C \sec [c + dx]^2) \right. \\
 \left. \sec [dx - \text{ArcTan} [\text{Cot} [c]]] \sqrt{1 - \sin [dx - \text{ArcTan} [\text{Cot} [c]]]} \right. \\
 \left. \sqrt{-\sqrt{1 + \text{Cot} [c]^2} \sin [c] \sin [dx - \text{ArcTan} [\text{Cot} [c]]]} \sqrt{1 + \sin [dx - \text{ArcTan} [\text{Cot} [c]]]} \right) / \\
 \left( 3d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sqrt{1 + \text{Cot} [c]^2} (a + a \sec [c + dx])^2 \right) - \\
 \left( 4C \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 \csc \left[ \frac{c}{2} \right] \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [dx - \text{ArcTan} [\text{Cot} [c]]] \right]^2 \right. \\
 \left. \sec \left[ \frac{c}{2} \right] (A + B \sec [c + dx] + C \sec [c + dx]^2) \right. \\
 \left. \sec [dx - \text{ArcTan} [\text{Cot} [c]]] \sqrt{1 - \sin [dx - \text{ArcTan} [\text{Cot} [c]]]} \right. \\
 \left. \sqrt{-\sqrt{1 + \text{Cot} [c]^2} \sin [c] \sin [dx - \text{ArcTan} [\text{Cot} [c]]]} \sqrt{1 + \sin [dx - \text{ArcTan} [\text{Cot} [c]]]} \right) / \\
 \left( 3d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sqrt{1 + \text{Cot} [c]^2} (a + a \sec [c + dx])^2 \right) + \\
 \left( \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 \sqrt{\cos [c + dx]} (A + B \sec [c + dx] + C \sec [c + dx]^2) \right. \\
 \left. \left( -\frac{8(2A - B + 2A \cos [c]) \csc [c]}{d} - \frac{8 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{dx}{2} \right] (2A \sin \left[ \frac{dx}{2} \right] - B \sin \left[ \frac{dx}{2} \right])}{d} \right) + \right. \\
 \left. \frac{4 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^3 (A \sin \left[ \frac{dx}{2} \right] - B \sin \left[ \frac{dx}{2} \right] + C \sin \left[ \frac{dx}{2} \right])}{3d} \right) +$$

$$\left. \frac{4 (A - B + C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Tan}\left[\frac{c}{2}\right]}{3d} \right) /$$

$$\left( (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2 \right)$$

**Problem 1228: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2}{\sqrt{\cos[c + dx]} (a + a \operatorname{Sec}[c + dx])^2} dx$$

Optimal (type 4, 133 leaves, 6 steps):

$$-\frac{(A - C) \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right]}{a^2 d} + \frac{(2A + B + 2C) \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right]}{3a^2 d}$$

$$-\frac{(A - C) \sqrt{\cos[c + dx]} \operatorname{Sin}[c + dx]}{a^2 d (1 + \cos[c + dx])} - \frac{(A - B + C) \sqrt{\cos[c + dx]} \operatorname{Sin}[c + dx]}{3d (a + a \cos[c + dx])^2}$$

Result (type 5, 1620 leaves):

$$-\frac{1}{(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2}$$

$$+ \frac{i A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2)}{\left( \left( 2 e^{2i dx} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2i dx} (\cos[c] + i \operatorname{Sin}[c])^2\right] \right. \right.$$

$$\left. \frac{\sqrt{e^{-i dx} (2 (1 + e^{2i dx}) \cos[c] + 2i (-1 + e^{2i dx}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2i dx} \cos[2c] + i e^{2i dx} \operatorname{Sin}[2c]}} \right) /$$

$$\left( 3i d (1 + e^{2i dx}) \cos[c] - 3d (-1 + e^{2i dx}) \operatorname{Sin}[c] \right) -$$

$$\left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i dx} (\cos[c] + i \operatorname{Sin}[c])^2\right] \right.$$

$$\left. \frac{\sqrt{e^{-i dx} (2 (1 + e^{2i dx}) \cos[c] + 2i (-1 + e^{2i dx}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2i dx} \cos[2c] + i e^{2i dx} \operatorname{Sin}[2c]}} \right) /$$

$$\left. \left. (-i d (1 + e^{2i dx}) \cos[c] + d (-1 + e^{2i dx}) \operatorname{Sin}[c]) \right) \right) +$$

$$\frac{1}{(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2}$$

$$+ \frac{i C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right]}{1}$$

$$\begin{aligned}
 & \text{Sec}\left[\frac{c}{2}\right] \\
 & (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) \\
 & \left( \left( 2 e^{2 i d x} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\text{Cos}[c] + i \text{Sin}[c])^2\right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \text{Cos}[c] + 2 i (-1 + e^{2 i d x}) \text{Sin}[c])}}{\sqrt{1 + e^{2 i d x} \text{Cos}[2 c] + i e^{2 i d x} \text{Sin}[2 c]}} \right) / \\
 & \quad (3 i d (1 + e^{2 i d x}) \text{Cos}[c] - 3 d (-1 + e^{2 i d x}) \text{Sin}[c]) - \\
 & \quad \left( 2 \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\text{Cos}[c] + i \text{Sin}[c])^2\right] \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \text{Cos}[c] + 2 i (-1 + e^{2 i d x}) \text{Sin}[c])}}{\sqrt{1 + e^{2 i d x} \text{Cos}[2 c] + i e^{2 i d x} \text{Sin}[2 c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2 i d x}) \text{Cos}[c] + d (-1 + e^{2 i d x}) \text{Sin}[c]) \right) - \\
 & \left( 8 A \text{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^4 \text{Csc}\left[\frac{c}{2}\right] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \text{Sin}[d x - \text{ArcTan}[\text{Cot}[c]]]\right]^2 \right) \\
 & \text{Sec}\left[\frac{c}{2}\right] (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) \\
 & \text{Sec}[d x - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \text{Sin}[d x - \text{ArcTan}[\text{Cot}[c]]]} \\
 & \frac{\sqrt{-\sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[d x - \text{ArcTan}[\text{Cot}[c]]]}}{\sqrt{1 + \text{Sin}[d x - \text{ArcTan}[\text{Cot}[c]]]} \Bigg) / \\
 & \left( 3 d (A + 2 C + 2 B \text{Cos}[c + d x] + A \text{Cos}[2 c + 2 d x]) \sqrt{1 + \text{Cot}[c]^2} (a + a \text{Sec}[c + d x])^2 \right) - \\
 & \left( 4 B \text{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^4 \text{Csc}\left[\frac{c}{2}\right] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \text{Sin}[d x - \text{ArcTan}[\text{Cot}[c]]]\right]^2 \right) \\
 & \text{Sec}\left[\frac{c}{2}\right] (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) \\
 & \text{Sec}[d x - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \text{Sin}[d x - \text{ArcTan}[\text{Cot}[c]]]} \\
 & \frac{\sqrt{-\sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[d x - \text{ArcTan}[\text{Cot}[c]]]}}{\sqrt{1 + \text{Sin}[d x - \text{ArcTan}[\text{Cot}[c]]]} \Bigg) / \\
 & \left( 3 d (A + 2 C + 2 B \text{Cos}[c + d x] + A \text{Cos}[2 c + 2 d x]) \sqrt{1 + \text{Cot}[c]^2} (a + a \text{Sec}[c + d x])^2 \right) - \\
 & \left( 8 C \text{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^4 \text{Csc}\left[\frac{c}{2}\right] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \text{Sin}[d x - \text{ArcTan}[\text{Cot}[c]]]\right]^2 \right)
 \end{aligned}$$

$$\begin{aligned}
 & \sec\left[\frac{c}{2}\right] (A+B \sec[c+dx] + C \sec[c+dx]^2) \\
 & \sec[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \sin[dx - \text{ArcTan}[\text{Cot}[c]]]} \\
 & \left. \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 + \sin[dx - \text{ArcTan}[\text{Cot}[c]]]} \right) / \\
 & \left( 3d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \sqrt{1 + \text{Cot}[c]^2} (a + a \sec[c+dx])^2 \right) + \\
 & \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c+dx]} (A+B \sec[c+dx] + C \sec[c+dx]^2) \right. \\
 & \left. \left( \frac{8(A-C) \text{Csc}[c]}{d} + \frac{8 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right] (A \sin\left[\frac{dx}{2}\right] - C \sin\left[\frac{dx}{2}\right])}{d} - \right. \right. \\
 & \left. \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (A \sin\left[\frac{dx}{2}\right] - B \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{3d} - \right. \\
 & \left. \left. \frac{4(A-B+C) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{3d} \right) \right) / \\
 & \left( (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) (a + a \sec[c+dx])^2 \right)
 \end{aligned}$$

**Problem 1229: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A+B \sec[c+dx] + C \sec[c+dx]^2}{\cos[c+dx]^{3/2} (a + a \sec[c+dx])^2} dx$$

Optimal (type 4, 167 leaves, 7 steps):

$$\begin{aligned}
 & \frac{(B-4C) \text{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{a^2 d} + \\
 & \frac{(A+2B-5C) \text{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{3a^2 d} - \frac{(B-4C) \sin[c+dx]}{a^2 d \sqrt{\cos[c+dx]}} + \\
 & \frac{(A+2B-5C) \sin[c+dx]}{3a^2 d \sqrt{\cos[c+dx]} (1 + \cos[c+dx])} - \frac{(A-B+C) \sin[c+dx]}{3d \sqrt{\cos[c+dx]} (a + a \cos[c+dx])^2}
 \end{aligned}$$

Result (type 5, 1660 leaves):

$$\begin{aligned}
 & \frac{1}{(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) (a + a \sec[c+dx])^2} \\
 & + B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \text{Csc}\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right] (A+B \sec[c+dx] + C \sec[c+dx]^2) \\
 & \left( \left( 2e^{2ix} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix} (\cos[c] + i \sin[c])\right]^2 \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \cos [c] + 2 i (-1 + e^{2 i dx}) \sin [c])}}{\sqrt{1 + e^{2 i dx} \cos [2 c] + i e^{2 i dx} \sin [2 c]}} \Big/ \\
 & \left( 3 i d (1 + e^{2 i dx}) \cos [c] - 3 d (-1 + e^{2 i dx}) \sin [c] \right) - \\
 & \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i dx} (\cos [c] + i \sin [c])^2 \right] \right) \\
 & \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \cos [c] + 2 i (-1 + e^{2 i dx}) \sin [c])}}{\sqrt{1 + e^{2 i dx} \cos [2 c] + i e^{2 i dx} \sin [2 c]}} \Big/ \\
 & \left( -i d (1 + e^{2 i dx}) \cos [c] + d (-1 + e^{2 i dx}) \sin [c] \right) - \\
 & \frac{1}{(A + 2 C + 2 B \cos [c + dx] + A \cos [2 c + 2 dx]) (a + a \sec [c + dx])^2} \\
 & 4 i C \\
 & \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} \right] \\
 & (A + B \sec [c + dx] + C \sec [c + dx]^2) \\
 & \left( \left( 2 e^{2 i dx} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i dx} (\cos [c] + i \sin [c])^2 \right] \right) \right. \\
 & \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \cos [c] + 2 i (-1 + e^{2 i dx}) \sin [c])}}{\sqrt{1 + e^{2 i dx} \cos [2 c] + i e^{2 i dx} \sin [2 c]}} \Big/ \\
 & \left. (3 i d (1 + e^{2 i dx}) \cos [c] - 3 d (-1 + e^{2 i dx}) \sin [c]) - \right. \\
 & \left. \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i dx} (\cos [c] + i \sin [c])^2 \right] \right) \right) \\
 & \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \cos [c] + 2 i (-1 + e^{2 i dx}) \sin [c])}}{\sqrt{1 + e^{2 i dx} \cos [2 c] + i e^{2 i dx} \sin [2 c]}} \Big/ \\
 & \left. (-i d (1 + e^{2 i dx}) \cos [c] + d (-1 + e^{2 i dx}) \sin [c]) \right) - \\
 & \left( 4 A \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [dx - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \right]^2 \right) \\
 & \operatorname{Sec} \left[ \frac{c}{2} \right] (A + B \sec [c + dx] + C \sec [c + dx]^2) \\
 & \operatorname{Sec} [dx - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \sqrt{1 - \sin [dx - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \\
 & \sqrt{-\sqrt{1 + \operatorname{Cot} [c]^2} \sin [c] \sin [dx - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \\
 & \left. \sqrt{1 + \sin [dx - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \right) \Big/ \\
 & \left( 3 d (A + 2 C + 2 B \cos [c + dx] + A \cos [2 c + 2 dx]) \sqrt{1 + \operatorname{Cot} [c]^2} (a + a \sec [c + dx])^2 \right) -
 \end{aligned}$$

$$\left( 8 B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin\left[dx - \operatorname{ArcTan}\left[\operatorname{Cot}[c]\right]\right]^2\right] \right. \\
 \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right. \\
 \left. \operatorname{Sec}\left[dx - \operatorname{ArcTan}\left[\operatorname{Cot}[c]\right]\right] \sqrt{1 - \sin\left[dx - \operatorname{ArcTan}\left[\operatorname{Cot}[c]\right]\right]} \right. \\
 \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin[c] \sin\left[dx - \operatorname{ArcTan}\left[\operatorname{Cot}[c]\right]\right] \sqrt{1 + \sin\left[dx - \operatorname{ArcTan}\left[\operatorname{Cot}[c]\right]\right]}} \right) / \\
 \left( 3 d (A + 2 C + 2 B \cos[c + dx] + A \cos[2c + 2 dx]) \sqrt{1 + \operatorname{Cot}[c]^2} (a + a \operatorname{Sec}[c + dx])^2 \right) + \\
 \left( 20 C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin\left[dx - \operatorname{ArcTan}\left[\operatorname{Cot}[c]\right]\right]^2\right] \right. \\
 \left. \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right. \\
 \left. \operatorname{Sec}\left[dx - \operatorname{ArcTan}\left[\operatorname{Cot}[c]\right]\right] \sqrt{1 - \sin\left[dx - \operatorname{ArcTan}\left[\operatorname{Cot}[c]\right]\right]} \right. \\
 \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin[c] \sin\left[dx - \operatorname{ArcTan}\left[\operatorname{Cot}[c]\right]\right] \sqrt{1 + \sin\left[dx - \operatorname{ArcTan}\left[\operatorname{Cot}[c]\right]\right]}} \right) / \\
 \left( 3 d (A + 2 C + 2 B \cos[c + dx] + A \cos[2c + 2 dx]) \sqrt{1 + \operatorname{Cot}[c]^2} (a + a \operatorname{Sec}[c + dx])^2 \right) + \\
 \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c + dx]} (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right. \\
 \left( \frac{4 (2 C - B \cos[c] + 2 C \cos[c]) \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c]}{d} + \right. \\
 \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (A \sin\left[\frac{dx}{2}\right] - B \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{3 d} + \\
 \frac{8 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] (-B \sin\left[\frac{dx}{2}\right] + 2 C \sin\left[\frac{dx}{2}\right])}{d} + \\
 \left. \left. \frac{16 C \operatorname{Sec}[c] \operatorname{Sec}[c + dx] \sin[dx]}{d} + \frac{4 (A - B + C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Tan}\left[\frac{c}{2}\right]}{3 d} \right) \right) / \\
 \left( (A + 2 C + 2 B \cos[c + dx] + A \cos[2c + 2 dx]) (a + a \operatorname{Sec}[c + dx])^2 \right)$$

**Problem 1230: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2}{\cos[c + dx]^{5/2} (a + a \operatorname{Sec}[c + dx])^2} dx$$

Optimal (type 4, 211 leaves, 8 steps):

$$\frac{(A-4B+7C) \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] + (2A-5B+10C) \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{a^2 d} + \frac{(2A-5B+10C) \operatorname{Sin}[c+dx] - (A-4B+7C) \operatorname{Sin}[c+dx]}{3 a^2 d \operatorname{Cos}[c+dx]^{3/2}} - \frac{(A-4B+7C) \operatorname{Sin}[c+dx]}{a^2 d \sqrt{\operatorname{Cos}[c+dx]}} - \frac{(A-B+C) \operatorname{Sin}[c+dx]}{3 d \operatorname{Cos}[c+dx]^{3/2} (a+a \operatorname{Cos}[c+dx])^2}$$

Result (type 5, 2107 leaves):

$$\frac{1}{(A+2C+2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) (a+a \operatorname{Sec}[c+dx])^2} + \frac{i A \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2)}{\left(\left(2 e^{2 i dx} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i dx} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right]\right) \sqrt{e^{-i dx} (2 (1+e^{2 i dx}) \operatorname{Cos}[c] + 2 i (-1+e^{2 i dx}) \operatorname{Sin}[c])} \sqrt{1+e^{2 i dx} \operatorname{Cos}[2c] + i e^{2 i dx} \operatorname{Sin}[2c]}\right) / (3 i d (1+e^{2 i dx}) \operatorname{Cos}[c] - 3 d (-1+e^{2 i dx}) \operatorname{Sin}[c]) - \left(2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i dx} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right]\right) \sqrt{e^{-i dx} (2 (1+e^{2 i dx}) \operatorname{Cos}[c] + 2 i (-1+e^{2 i dx}) \operatorname{Sin}[c])} \sqrt{1+e^{2 i dx} \operatorname{Cos}[2c] + i e^{2 i dx} \operatorname{Sin}[2c]}\right) / (-i d (1+e^{2 i dx}) \operatorname{Cos}[c] + d (-1+e^{2 i dx}) \operatorname{Sin}[c])\right) - \frac{1}{(A+2C+2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) (a+a \operatorname{Sec}[c+dx])^2} + \frac{4 i B \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2)}{\left(\left(2 e^{2 i dx} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i dx} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right]\right) \sqrt{e^{-i dx} (2 (1+e^{2 i dx}) \operatorname{Cos}[c] + 2 i (-1+e^{2 i dx}) \operatorname{Sin}[c])} \sqrt{1+e^{2 i dx} \operatorname{Cos}[2c] + i e^{2 i dx} \operatorname{Sin}[2c]}\right) / (3 i d (1+e^{2 i dx}) \operatorname{Cos}[c] - 3 d (-1+e^{2 i dx}) \operatorname{Sin}[c]) - \left(2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i dx} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right]\right) \sqrt{e^{-i dx} (2 (1+e^{2 i dx}) \operatorname{Cos}[c] + 2 i (-1+e^{2 i dx}) \operatorname{Sin}[c])} \sqrt{1+e^{2 i dx} \operatorname{Cos}[2c] + i e^{2 i dx} \operatorname{Sin}[2c]}\right) / (-i d (1+e^{2 i dx}) \operatorname{Cos}[c] + d (-1+e^{2 i dx}) \operatorname{Sin}[c])\right) +$$



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$$\begin{aligned}
 & \frac{(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) (a + a \sec[c + dx])^2}{7iC} \\
 & \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \\
 & \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \\
 & (A + B \sec[c + dx] + C \sec[c + dx]^2) \\
 & \left( \left( 2 e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix} (\cos[c] + i \sin[c])\right]^2 \right) \right. \\
 & \quad \left. \frac{\sqrt{e^{-ix} (2(1 + e^{2ix}) \cos[c] + 2i(-1 + e^{2ix}) \sin[c])}}{\sqrt{1 + e^{2ix} \cos[2c] + i e^{2ix} \sin[2c]}} \right) / \\
 & \quad (3id(1 + e^{2ix}) \cos[c] - 3d(-1 + e^{2ix}) \sin[c]) - \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix} (\cos[c] + i \sin[c])\right]^2 \right) \\
 & \quad \frac{\sqrt{e^{-ix} (2(1 + e^{2ix}) \cos[c] + 2i(-1 + e^{2ix}) \sin[c])}}{\sqrt{1 + e^{2ix} \cos[2c] + i e^{2ix} \sin[2c]}} \right) / \\
 & \quad \left. (-id(1 + e^{2ix}) \cos[c] + d(-1 + e^{2ix}) \sin[c]) \right) - \\
 & \left( 8A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2 \right) \\
 & \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \sec[c + dx] + C \sec[c + dx]^2) \\
 & \operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \frac{\sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}}{\sqrt{1 + \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \Big/ \\
 & \left( 3d(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{1 + \operatorname{Cot}[c]^2} (a + a \sec[c + dx])^2 \right) + \\
 & \left( 20B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2 \right) \\
 & \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \sec[c + dx] + C \sec[c + dx]^2) \\
 & \operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \frac{\sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}}}{\Big/} \\
 & \left( 3d(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{1 + \operatorname{Cot}[c]^2} (a + a \sec[c + dx])^2 \right) -
 \end{aligned}$$

$$\left( 40 C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \csc\left[\frac{c}{2}\right] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin\left[dx - \text{ArcTan}[\cot[c]]\right]\right]^2 \right. \\ \left. \sec\left[\frac{c}{2}\right] (A + B \sec[c + dx] + C \sec[c + dx]^2) \right. \\ \left. \sec\left[dx - \text{ArcTan}[\cot[c]]\right] \sqrt{1 - \sin\left[dx - \text{ArcTan}[\cot[c]]\right]} \right. \\ \left. \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin\left[dx - \text{ArcTan}[\cot[c]]\right]} \sqrt{1 + \sin\left[dx - \text{ArcTan}[\cot[c]]\right]} \right) / \\ \left( 3d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{1 + \cot[c]^2} (a + a \sec[c + dx])^2 \right) + \\ \frac{1}{(A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) (a + a \sec[c + dx])^2} \\ \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c + dx]} \\ (A + B \sec[c + dx] + C \sec[c + dx]^2) \\ \left( -\frac{1}{d} 4 (-2B + 4C + A \cos[c] - 2B \cos[c] + 3C \cos[c]) \csc\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right] \sec[c] - \right. \\ \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (A \sin\left[\frac{dx}{2}\right] - B \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{3d} - \\ \frac{8 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right] (A \sin\left[\frac{dx}{2}\right] - 2B \sin\left[\frac{dx}{2}\right] + 3C \sin\left[\frac{dx}{2}\right])}{d} + \\ \frac{16 C \sec[c] \sec[c + dx]^2 \sin[dx]}{3d} + \\ \left. \frac{16 \sec[c] \sec[c + dx] (C \sin[c] + 3B \sin[dx] - 6C \sin[dx])}{3d} - \right. \\ \left. \frac{4 (A - B + C) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{3d} \right)$$

**Problem 1231: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec[c + dx] + C \sec[c + dx]^2}{\cos[c + dx]^{7/2} (a + a \sec[c + dx])^2} dx$$

Optimal (type 4, 250 leaves, 9 steps):

$$\begin{aligned}
 & - \frac{(20A - 35B + 56C) \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right] - 5(A - 2B + 3C) \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right]}{5a^2d} + \\
 & \frac{(20A - 35B + 56C) \operatorname{Sin}[c + dx]}{15a^2d \operatorname{Cos}[c + dx]^{5/2}} - \frac{5(A - 2B + 3C) \operatorname{Sin}[c + dx]}{3a^2d \operatorname{Cos}[c + dx]^{3/2}} + \frac{(20A - 35B + 56C) \operatorname{Sin}[c + dx]}{5a^2d \sqrt{\operatorname{Cos}[c + dx]}} \\
 & \frac{(A - 2B + 3C) \operatorname{Sin}[c + dx]}{a^2d \operatorname{Cos}[c + dx]^{5/2} (1 + \operatorname{Cos}[c + dx])} - \frac{(A - B + C) \operatorname{Sin}[c + dx]}{3d \operatorname{Cos}[c + dx]^{5/2} (a + a \operatorname{Cos}[c + dx])^2}
 \end{aligned}$$

Result (type 5, 2164 leaves):

$$\begin{aligned}
 & - \frac{1}{(A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2} \\
 & 4iA \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \\
 & \left( \left( 2e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])\right]^2 \right. \right. \\
 & \quad \left. \left. \frac{\sqrt{e^{-ix} (2(1 + e^{2ix}) \operatorname{Cos}[c] + 2i(-1 + e^{2ix}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2ix} \operatorname{Cos}[2c] + i e^{2ix} \operatorname{Sin}[2c]}} \right) \right) / \\
 & \quad (3i d (1 + e^{2ix}) \operatorname{Cos}[c] - 3d(-1 + e^{2ix}) \operatorname{Sin}[c]) - \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])\right]^2 \right) \\
 & \quad \left. \frac{\sqrt{e^{-ix} (2(1 + e^{2ix}) \operatorname{Cos}[c] + 2i(-1 + e^{2ix}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2ix} \operatorname{Cos}[2c] + i e^{2ix} \operatorname{Sin}[2c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2ix}) \operatorname{Cos}[c] + d(-1 + e^{2ix}) \operatorname{Sin}[c]) \right) + \\
 & \frac{1}{(A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^2} \\
 & 7 \\
 & i \\
 & B \\
 & \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \\
 & \operatorname{Csc}\left[\frac{c}{2}\right] \\
 & \operatorname{Sec}\left[\frac{c}{2}\right] \\
 & (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \\
 & \left( \left( 2e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])\right]^2 \right) \right. \\
 & \quad \left. \frac{\sqrt{e^{-ix} (2(1 + e^{2ix}) \operatorname{Cos}[c] + 2i(-1 + e^{2ix}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2ix} \operatorname{Cos}[2c] + i e^{2ix} \operatorname{Sin}[2c]}} \right) / \\
 & \quad (3i d (1 + e^{2ix}) \operatorname{Cos}[c] - 3d(-1 + e^{2ix}) \operatorname{Sin}[c]) - \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])\right]^2 \right)
 \end{aligned}$$

$$\begin{aligned}
 & \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \cos [c] + 2 i (-1 + e^{2 i dx}) \sin [c])}}{\sqrt{1 + e^{2 i dx} \cos [2 c] + i e^{2 i dx} \sin [2 c]}} \Bigg/ \\
 & \left( -i d (1 + e^{2 i dx}) \cos [c] + d (-1 + e^{2 i dx}) \sin [c] \right) - \\
 & \frac{1}{5 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^2} \\
 & 56 \\
 & i \\
 & C \\
 & \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \\
 & \csc \left[ \frac{c}{2} \right] \\
 & \sec \left[ \frac{c}{2} \right] \\
 & (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \left( \left( 2 e^{2 i dx} \text{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i dx} (\cos [c] + i \sin [c])^2 \right] \right) \right. \\
 & \quad \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \cos [c] + 2 i (-1 + e^{2 i dx}) \sin [c])}}{\sqrt{1 + e^{2 i dx} \cos [2 c] + i e^{2 i dx} \sin [2 c]}} \Bigg/ \\
 & \quad \left( 3 i d (1 + e^{2 i dx}) \cos [c] - 3 d (-1 + e^{2 i dx}) \sin [c] \right) - \\
 & \quad \left( 2 \text{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i dx} (\cos [c] + i \sin [c])^2 \right] \right) \\
 & \quad \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \cos [c] + 2 i (-1 + e^{2 i dx}) \sin [c])}}{\sqrt{1 + e^{2 i dx} \cos [2 c] + i e^{2 i dx} \sin [2 c]}} \Bigg/ \\
 & \quad \left. \left( -i d (1 + e^{2 i dx}) \cos [c] + d (-1 + e^{2 i dx}) \sin [c] \right) \right) + \\
 & \left( 20 A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \csc \left[ \frac{c}{2} \right] \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \text{ArcTan} [\text{Cot} [c]]] \right]^2 \right) \\
 & \sec \left[ \frac{c}{2} \right] (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \sec [d x - \text{ArcTan} [\text{Cot} [c]]] \sqrt{1 - \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \\
 & \sqrt{-\sqrt{1 + \text{Cot} [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \\
 & \left. \sqrt{1 + \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \right) \Bigg/ \\
 & \left( 3 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \text{Cot} [c]^2} (a + a \sec [c + d x])^2 \right) -
 \end{aligned}$$

$$\left( 40 B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \csc\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin\left[dx - \operatorname{ArcTan}[\cot[c]]\right]\right]^2 \right.$$

$$\left. \sec\left[\frac{c}{2}\right] (A + B \sec[c + dx] + C \sec[c + dx]^2) \right.$$

$$\left. \sec\left[dx - \operatorname{ArcTan}[\cot[c]]\right] \sqrt{1 - \sin\left[dx - \operatorname{ArcTan}[\cot[c]]\right]} \right.$$

$$\left. \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin\left[dx - \operatorname{ArcTan}[\cot[c]]\right]} \right.$$

$$\left. \sqrt{1 + \sin\left[dx - \operatorname{ArcTan}[\cot[c]]\right]} \right) /$$

$$\left( 3 d (A + 2 C + 2 B \cos[c + dx] + A \cos[2c + 2 dx]) \sqrt{1 + \cot[c]^2} (a + a \sec[c + dx])^2 \right) +$$

$$\left( 20 C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \csc\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin\left[dx - \operatorname{ArcTan}[\cot[c]]\right]\right]^2 \right.$$

$$\left. \sec\left[\frac{c}{2}\right] (A + B \sec[c + dx] + C \sec[c + dx]^2) \right.$$

$$\left. \sec\left[dx - \operatorname{ArcTan}[\cot[c]]\right] \sqrt{1 - \sin\left[dx - \operatorname{ArcTan}[\cot[c]]\right]} \right.$$

$$\left. \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin\left[dx - \operatorname{ArcTan}[\cot[c]]\right]} \sqrt{1 + \sin\left[dx - \operatorname{ArcTan}[\cot[c]]\right]} \right) /$$

$$\left( d (A + 2 C + 2 B \cos[c + dx] + A \cos[2c + 2 dx]) \sqrt{1 + \cot[c]^2} (a + a \sec[c + dx])^2 \right) +$$

$$\frac{1}{(A + 2 C + 2 B \cos[c + dx] + A \cos[2c + 2 dx]) (a + a \sec[c + dx])^2}$$

$$\cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c + dx]}$$

$$(A + B \sec[c + dx] + C \sec[c + dx]^2)$$

$$\left( \frac{1}{5 d} 4 (10 A - 20 B + 36 C + 10 A \cos[c] - 15 B \cos[c] + 20 C \cos[c]) \csc\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right] \sec[c] + \right.$$

$$\frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (A \sin\left[\frac{dx}{2}\right] - B \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{3 d} +$$

$$\frac{8 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right] (2 A \sin\left[\frac{dx}{2}\right] - 3 B \sin\left[\frac{dx}{2}\right] + 4 C \sin\left[\frac{dx}{2}\right])}{d} +$$

$$\frac{16 C \sec[c] \sec[c + dx]^3 \sin[dx]}{5 d} - \frac{1}{15 d} 16 \sec[c] \sec[c + dx]$$

$$(-5 B \sin[c] + 10 C \sin[c] - 15 A \sin[dx] + 30 B \sin[dx] - 54 C \sin[dx]) + \frac{1}{15 d} 16 \sec[c]$$

$$\left. \sec[c + dx]^2 (3 C \sin[c] + 5 B \sin[dx] - 10 C \sin[dx]) + \frac{4 (A - B + C) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{3 d} \right)$$

**Problem 1232: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\cos [c+d x]^{5 / 2} (A+B \sec [c+d x]+C \sec [c+d x]^2)}{(a+a \sec [c+d x])^3} d x$$

Optimal (type 4, 273 leaves, 9 steps):

$$\begin{aligned} & \frac{7(33 A-17 B+7 C) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{10 a^3 d} - \\ & \frac{(63 A-33 B+13 C) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{6 a^3 d} - \frac{(63 A-33 B+13 C) \sqrt{\cos [c+d x]} \sin [c+d x]}{6 a^3 d} + \\ & \frac{7(33 A-17 B+7 C) \cos [c+d x]^{3 / 2} \sin [c+d x]}{30 a^3 d} - \frac{(A-B+C) \cos [c+d x]^{9 / 2} \sin [c+d x]}{5 d(a+a \cos [c+d x])^3} - \\ & \frac{(12 A-7 B+2 C) \cos [c+d x]^{7 / 2} \sin [c+d x]}{15 a d(a+a \cos [c+d x])^2} - \frac{(63 A-33 B+13 C) \cos [c+d x]^{5 / 2} \sin [c+d x]}{10 d\left(a^3+a^3 \cos [c+d x]\right)} \end{aligned}$$

Result (type 5, 2257 leaves):

$$\begin{aligned} & \frac{1}{5(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) (a+a \sec [c+d x])^3} \\ & \frac{231 i A \cos \left[\frac{c}{2}+\frac{d x}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+d x] (A+B \sec [c+d x]+C \sec [c+d x]^2)}{\left(\left(2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x}(\cos [c]+i \sin [c])^2\right]\right.\right. \\ & \quad \left.\left.\sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)}\right.\right. \\ & \quad \left.\left.\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}\right)\right) / \\ & \quad (3 i d\left(1+e^{2 i d x}\right) \cos [c]-3 d\left(-1+e^{2 i d x}\right) \sin [c]) - \\ & \quad \left(2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x}(\cos [c]+i \sin [c])^2\right]\right. \\ & \quad \left.\sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)}\right.\right. \\ & \quad \left.\left.\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}\right)\right) / \\ & \quad \left.(-i d\left(1+e^{2 i d x}\right) \cos [c]+d\left(-1+e^{2 i d x}\right) \sin [c])\right) - \\ & \frac{1}{5(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) (a+a \sec [c+d x])^3} \\ & \frac{119 i B}{\cos \left[\frac{c}{2}+\frac{d x}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right]} \\ & \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+d x] \\ & (A+B \sec [c+d x]+C \sec [c+d x]^2) \end{aligned}$$

$$\begin{aligned}
 & \left( \left( 2 e^{2 i d x} \text{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c]) \right]^2 \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \quad (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) - \\
 & \quad \left( 2 \text{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c]) \right]^2 \right) \\
 & \quad \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \quad \left. \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) + \right. \\
 & \quad \left. \frac{1}{5 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^3} \right. \\
 & \quad 49 i C \\
 & \quad \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \csc \left[ \frac{c}{2} \right] \\
 & \quad \sec \left[ \frac{c}{2} \right] \sec [c + d x] \\
 & \quad (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \quad \left( \left( 2 e^{2 i d x} \text{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c]) \right]^2 \right. \right. \\
 & \quad \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \quad (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) - \\
 & \quad \left( 2 \text{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c]) \right]^2 \right) \\
 & \quad \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \quad \left. \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) + \right. \\
 & \quad \left. \left( 84 A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \csc \left[ \frac{c}{2} \right] \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \text{ArcTan} [\cot [c]]] \right]^2 \right) \right. \\
 & \quad \sec \left[ \frac{c}{2} \right] \sec [c + d x] (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \quad \sec [d x - \text{ArcTan} [\cot [c]]] \sqrt{1 - \sin [d x - \text{ArcTan} [\cot [c]]]} \\
 & \quad \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]]} \\
 & \quad \left. \left. \sqrt{1 + \sin [d x - \text{ArcTan} [\cot [c]]]} \right) / \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sqrt{1 + \cot [c]^2} (a + a \sec [c + dx])^3 \right) - \\
 & \left( 44 B \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^6 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [dx - \operatorname{ArcTan} [\cot [c]]]^2 \right] \right. \\
 & \quad \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} [c + dx] (A + B \sec [c + dx] + C \sec [c + dx]^2) \\
 & \quad \operatorname{Sec} [dx - \operatorname{ArcTan} [\cot [c]]] \sqrt{1 - \sin [dx - \operatorname{ArcTan} [\cot [c]]]} \\
 & \quad \left. \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [dx - \operatorname{ArcTan} [\cot [c]]] \sqrt{1 + \sin [dx - \operatorname{ArcTan} [\cot [c]]]} \right) / \\
 & \left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sqrt{1 + \cot [c]^2} (a + a \sec [c + dx])^3 \right) + \\
 & \left( 52 C \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^6 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [dx - \operatorname{ArcTan} [\cot [c]]]^2 \right] \right. \\
 & \quad \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} [c + dx] (A + B \sec [c + dx] + C \sec [c + dx]^2) \\
 & \quad \operatorname{Sec} [dx - \operatorname{ArcTan} [\cot [c]]] \sqrt{1 - \sin [dx - \operatorname{ArcTan} [\cot [c]]]} \\
 & \quad \left. \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [dx - \operatorname{ArcTan} [\cot [c]]] \sqrt{1 + \sin [dx - \operatorname{ArcTan} [\cot [c]]]} \right) / \\
 & \left( 3d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sqrt{1 + \cot [c]^2} (a + a \sec [c + dx])^3 \right) + \\
 & \left( \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^6 (A + B \sec [c + dx] + C \sec [c + dx]^2) \right. \\
 & \quad \left( -\frac{1}{5d} (99A - 59B + 29C + 132A \cos [c] - 60B \cos [c] + 20C \cos [c]) \operatorname{Csc} [c] - \right. \\
 & \quad \frac{32(3A - B) \cos [dx] \sin [c]}{3d} + \frac{16A \cos [2dx] \sin [2c]}{5d} - \\
 & \quad \frac{4 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right]^5 \left( A \sin \left[ \frac{dx}{2} \right] - B \sin \left[ \frac{dx}{2} \right] + C \sin \left[ \frac{dx}{2} \right] \right)}{5d} + \frac{1}{15d} \\
 & \quad 8 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right]^3 \left( 24A \sin \left[ \frac{dx}{2} \right] - 19B \sin \left[ \frac{dx}{2} \right] + 14C \sin \left[ \frac{dx}{2} \right] \right) - \\
 & \quad \frac{1}{5d} 8 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right] \left( 99A \sin \left[ \frac{dx}{2} \right] - 59B \sin \left[ \frac{dx}{2} \right] + 29C \sin \left[ \frac{dx}{2} \right] \right) - \\
 & \quad \frac{32(3A - B) \cos [c] \sin [dx]}{3d} + \frac{16A \cos [2c] \sin [2dx]}{5d} + \\
 & \quad \left. \left. \frac{8(24A - 19B + 14C) \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \operatorname{Tan} \left[ \frac{c}{2} \right]}{15d} - \frac{4(A - B + C) \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 \operatorname{Tan} \left[ \frac{c}{2} \right]}{5d} \right) \right) / \\
 & \left( \sqrt{\cos [c + dx]} (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) (a + a \sec [c + dx])^3 \right)
 \end{aligned}$$



**Problem 1233: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\cos [c+d x]^{3 / 2} (A+B \sec [c+d x]+C \sec [c+d x]^2)}{(a+a \sec [c+d x])^3} d x$$

Optimal (type 4, 234 leaves, 8 steps):

$$\begin{aligned} & -\frac{(119 A-49 B+9 C) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{10 a^3 d} + \frac{(33 A-13 B+3 C) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{6 a^3 d} + \\ & \frac{(33 A-13 B+3 C) \sqrt{\cos [c+d x]} \sin [c+d x]}{6 a^3 d} - \frac{(A-B+C) \cos [c+d x]^{7 / 2} \sin [c+d x]}{5 d(a+a \cos [c+d x])^3} - \\ & \frac{(2 A-B) \cos [c+d x]^{5 / 2} \sin [c+d x]}{3 a d(a+a \cos [c+d x])^2} - \frac{(119 A-49 B+9 C) \cos [c+d x]^{3 / 2} \sin [c+d x]}{30 d\left(a^3+a^3 \cos [c+d x]\right)} \end{aligned}$$

Result (type 5, 2206 leaves):

$$\begin{aligned} & \frac{1}{5(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])(a+a \sec [c+d x])^3} \\ & 119 i A \cos \left[\frac{c}{2}+\frac{d x}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+d x](A+B \sec [c+d x]+C \sec [c+d x]^2) \\ & \left(\left(2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4},-e^{2 i d x}(\cos [c]+i \sin [c])^2\right]\right.\right. \\ & \quad \left.\left.\frac{\sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}}\right)\right) / \\ & \quad \left(3 i d\left(1+e^{2 i d x}\right) \cos [c]-3 d\left(-1+e^{2 i d x}\right) \sin [c]\right)- \\ & \quad \left(2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4},-e^{2 i d x}(\cos [c]+i \sin [c])^2\right]\right) \\ & \quad \left.\frac{\sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}}\right) / \\ & \quad \left.(-i d\left(1+e^{2 i d x}\right) \cos [c]+d\left(-1+e^{2 i d x}\right) \sin [c]\right)\right) + \\ & \frac{1}{5(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])(a+a \sec [c+d x])^3} \\ & 49 \\ & i \\ & B \\ & \cos \left[\frac{c}{2}+\frac{d x}{2}\right]^6 \\ & \operatorname{Csc}\left[\frac{c}{2}\right] \\ & \operatorname{Sec}\left[\frac{c}{2}\right] \end{aligned}$$

$$\begin{aligned}
 & \text{Sec}[c + d x] \\
 & (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) \\
 & \left( \left( 2 e^{2 i d x} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\text{Cos}[c] + i \text{Sin}[c])\right]^2 \right) \right. \\
 & \quad \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \text{Cos}[c] + 2 i (-1 + e^{2 i d x}) \text{Sin}[c])} \\
 & \quad \left. \sqrt{1 + e^{2 i d x} \text{Cos}[2 c] + i e^{2 i d x} \text{Sin}[2 c]} \right) / \\
 & (3 i d (1 + e^{2 i d x}) \text{Cos}[c] - 3 d (-1 + e^{2 i d x}) \text{Sin}[c]) - \\
 & \left( 2 \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\text{Cos}[c] + i \text{Sin}[c])\right]^2 \right) \\
 & \quad \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \text{Cos}[c] + 2 i (-1 + e^{2 i d x}) \text{Sin}[c])} \\
 & \quad \left. \sqrt{1 + e^{2 i d x} \text{Cos}[2 c] + i e^{2 i d x} \text{Sin}[2 c]} \right) / \\
 & (-i d (1 + e^{2 i d x}) \text{Cos}[c] + d (-1 + e^{2 i d x}) \text{Sin}[c]) \Big) - \\
 & \qquad \qquad \qquad 1 \\
 & \hline
 & 5 (A + 2 C + 2 B \text{Cos}[c + d x] + A \text{Cos}[2 c + 2 d x]) (a + a \text{Sec}[c + d x])^3 \\
 & 9 \\
 & i \\
 & C \\
 & \text{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 \\
 & \text{Csc}\left[\frac{c}{2}\right] \\
 & \text{Sec}\left[\frac{c}{2}\right] \\
 & \text{Sec}[c + d x] \\
 & (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) \\
 & \left( \left( 2 e^{2 i d x} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\text{Cos}[c] + i \text{Sin}[c])\right]^2 \right) \right. \\
 & \quad \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \text{Cos}[c] + 2 i (-1 + e^{2 i d x}) \text{Sin}[c])} \\
 & \quad \left. \sqrt{1 + e^{2 i d x} \text{Cos}[2 c] + i e^{2 i d x} \text{Sin}[2 c]} \right) / \\
 & (3 i d (1 + e^{2 i d x}) \text{Cos}[c] - 3 d (-1 + e^{2 i d x}) \text{Sin}[c]) - \\
 & \left( 2 \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\text{Cos}[c] + i \text{Sin}[c])\right]^2 \right) \\
 & \quad \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \text{Cos}[c] + 2 i (-1 + e^{2 i d x}) \text{Sin}[c])} \\
 & \quad \left. \sqrt{1 + e^{2 i d x} \text{Cos}[2 c] + i e^{2 i d x} \text{Sin}[2 c]} \right) / \\
 & (-i d (1 + e^{2 i d x}) \text{Cos}[c] + d (-1 + e^{2 i d x}) \text{Sin}[c]) \Big) - \\
 & \left( 44 A \text{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 \text{Csc}\left[\frac{c}{2}\right] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \text{Sin}[d x - \text{ArcTan}[\text{Cot}[c]]\right]^2 \right) \right. \\
 & \quad \left. \text{Sec}\left[\frac{c}{2}\right] \text{Sec}[c + d x] (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \begin{aligned}
 & \frac{\sec [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\cot [c]]]}}{\sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\cot [c]]]}} \\
 & \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\cot [c]]]}}
 \end{aligned} \right) / \\
 & \left( d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} (a + a \sec [c + d x])^3 \right) + \\
 & \left( 52 B \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan}[\cot [c]]]^2 \right] \right) \\
 & \frac{\sec \left[ \frac{c}{2} \right] \sec [c + d x] (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sec [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\cot [c]]]}} \\
 & \frac{\sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\cot [c]]]}}{\sqrt{1 + \sin [d x - \operatorname{ArcTan}[\cot [c]]]}} \left. \right) / \\
 & \left( 3 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} (a + a \sec [c + d x])^3 \right) - \\
 & \left( 4 C \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan}[\cot [c]]]^2 \right] \right) \\
 & \frac{\sec \left[ \frac{c}{2} \right] \sec [c + d x] (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sec [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\cot [c]]]}} \\
 & \frac{\sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\cot [c]]]}}{\sqrt{1 + \sin [d x - \operatorname{ArcTan}[\cot [c]]]}} \left. \right) / \\
 & \left( d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} (a + a \sec [c + d x])^3 \right) + \\
 & \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right) \\
 & \left( \frac{8 (59 A - 29 B + 9 C + 60 A \cos [c] - 20 B \cos [c]) \operatorname{Csc} [c]}{5 d} + \frac{32 A \cos [d x] \sin [c]}{3 d} + \right. \\
 & \left. \frac{4 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^5 (A \sin \left[ \frac{d x}{2} \right] - B \sin \left[ \frac{d x}{2} \right] + C \sin \left[ \frac{d x}{2} \right])}{5 d} + \frac{1}{5 d} \right) \\
 & 8 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right] \left( 59 A \sin \left[ \frac{d x}{2} \right] - 29 B \sin \left[ \frac{d x}{2} \right] + 9 C \sin \left[ \frac{d x}{2} \right] \right) - \frac{1}{15 d} 8 \sec \left[ \frac{c}{2} \right] \\
 & \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^3 \left( 19 A \sin \left[ \frac{d x}{2} \right] - 14 B \sin \left[ \frac{d x}{2} \right] + 9 C \sin \left[ \frac{d x}{2} \right] \right) + \frac{32 A \cos [c] \sin [d x]}{3 d} -
 \end{aligned}$$

$$\left. \left( \frac{8 (19 A - 14 B + 9 C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Tan}\left[\frac{c}{2}\right]}{15 d} + \frac{4 (A - B + C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Tan}\left[\frac{c}{2}\right]}{5 d} \right) \right) /$$

$$\left( \sqrt{\operatorname{Cos}[c + dx]} (A + 2 C + 2 B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2 c + 2 dx]) (a + a \operatorname{Sec}[c + dx])^3 \right)$$

**Problem 1234: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\operatorname{Cos}[c + dx]} (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2)}{(a + a \operatorname{Sec}[c + dx])^3} dx$$

Optimal (type 4, 201 leaves, 7 steps):

$$\frac{(49 A - 9 B - C) \operatorname{EllipticE}\left[\frac{1}{2} (c + dx), 2\right]}{10 a^3 d} -$$

$$\frac{(13 A - 3 B - C) \operatorname{EllipticF}\left[\frac{1}{2} (c + dx), 2\right]}{6 a^3 d} - \frac{(A - B + C) \operatorname{Cos}[c + dx]^{5/2} \operatorname{Sin}[c + dx]}{5 d (a + a \operatorname{Cos}[c + dx])^3} -$$

$$\frac{(8 A - 3 B - 2 C) \operatorname{Cos}[c + dx]^{3/2} \operatorname{Sin}[c + dx]}{15 a d (a + a \operatorname{Cos}[c + dx])^2} - \frac{(13 A - 3 B - C) \sqrt{\operatorname{Cos}[c + dx]} \operatorname{Sin}[c + dx]}{6 d (a^3 + a^3 \operatorname{Cos}[c + dx])}$$

Result (type 5, 2175 leaves):

$$\frac{1}{5 (A + 2 C + 2 B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2 c + 2 dx]) (a + a \operatorname{Sec}[c + dx])^3}$$

$$49 i A \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c + dx] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2)$$

$$\left( \left( 2 e^{2 i dx} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i dx} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right. \right.$$

$$\left. \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i dx}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i dx} \operatorname{Cos}[2 c] + i e^{2 i dx} \operatorname{Sin}[2 c]}} \right) /$$

$$(3 i d (1 + e^{2 i dx}) \operatorname{Cos}[c] - 3 d (-1 + e^{2 i dx}) \operatorname{Sin}[c]) -$$

$$\left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i dx} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right.$$

$$\left. \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i dx}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i dx} \operatorname{Cos}[2 c] + i e^{2 i dx} \operatorname{Sin}[2 c]}} \right) /$$

$$\left. (-i d (1 + e^{2 i dx}) \operatorname{Cos}[c] + d (-1 + e^{2 i dx}) \operatorname{Sin}[c]) \right) -$$

$$\frac{1}{5 (A + 2 C + 2 B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2 c + 2 dx]) (a + a \operatorname{Sec}[c + dx])^3}$$

$$9 i B$$

$$\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right]$$

$$\begin{aligned}
 & \sec\left[\frac{c}{2}\right] \sec[c+dx] \\
 & (A+B \sec[c+dx] + C \sec[c+dx]^2) \\
 & \left( \left( 2 e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix} (\cos[c] + i \sin[c])\right]^2 \right) \right. \\
 & \quad \left. \frac{\sqrt{e^{-ix} (2 (1 + e^{2ix}) \cos[c] + 2 i (-1 + e^{2ix}) \sin[c])}}{\sqrt{1 + e^{2ix} \cos[2c] + i e^{2ix} \sin[2c]}} \right) / \\
 & \quad (3 i d (1 + e^{2ix}) \cos[c] - 3 d (-1 + e^{2ix}) \sin[c]) - \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix} (\cos[c] + i \sin[c])\right]^2 \right) \\
 & \quad \frac{\sqrt{e^{-ix} (2 (1 + e^{2ix}) \cos[c] + 2 i (-1 + e^{2ix}) \sin[c])}}{\sqrt{1 + e^{2ix} \cos[2c] + i e^{2ix} \sin[2c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2ix}) \cos[c] + d (-1 + e^{2ix}) \sin[c]) \right) - \\
 & \quad \quad \quad 1 \\
 & 5 (A + 2C + 2B \cos[c+dx] + A \cos[2c+2dx]) (a + a \sec[c+dx])^3 \\
 & i C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \\
 & \csc\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right] \sec[c+dx] \\
 & (A+B \sec[c+dx] + C \sec[c+dx]^2) \\
 & \left( \left( 2 e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix} (\cos[c] + i \sin[c])\right]^2 \right) \right. \\
 & \quad \left. \frac{\sqrt{e^{-ix} (2 (1 + e^{2ix}) \cos[c] + 2 i (-1 + e^{2ix}) \sin[c])}}{\sqrt{1 + e^{2ix} \cos[2c] + i e^{2ix} \sin[2c]}} \right) / \\
 & \quad (3 i d (1 + e^{2ix}) \cos[c] - 3 d (-1 + e^{2ix}) \sin[c]) - \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix} (\cos[c] + i \sin[c])\right]^2 \right) \\
 & \quad \frac{\sqrt{e^{-ix} (2 (1 + e^{2ix}) \cos[c] + 2 i (-1 + e^{2ix}) \sin[c])}}{\sqrt{1 + e^{2ix} \cos[2c] + i e^{2ix} \sin[2c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2ix}) \cos[c] + d (-1 + e^{2ix}) \sin[c]) \right) + \\
 & \left( 52 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \csc\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\cot[c]]]\right]^2 \right) \\
 & \sec\left[\frac{c}{2}\right] \sec[c+dx] (A+B \sec[c+dx] + C \sec[c+dx]^2) \\
 & \sec[dx - \operatorname{ArcTan}[\cot[c]]] \sqrt{1 - \sin[dx - \operatorname{ArcTan}[\cot[c]]]} \\
 & \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]]]}
 \end{aligned}$$

$$\begin{aligned}
 & \left. \sqrt{1 + \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \right) / \\
 & \left( 3 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \text{Cot} [c]^2} (a + a \sec [c + d x])^3 \right) - \\
 & \left( 4 B \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \text{Csc} \left[ \frac{c}{2} \right] \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \text{ArcTan} [\text{Cot} [c]]]^2 \right] \right. \\
 & \quad \text{Sec} \left[ \frac{c}{2} \right] \text{Sec} [c + d x] (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \quad \left. \text{Sec} [d x - \text{ArcTan} [\text{Cot} [c]]] \sqrt{1 - \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \right. \\
 & \quad \left. \sqrt{-\sqrt{1 + \text{Cot} [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \sqrt{1 + \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \right) / \\
 & \left( d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \text{Cot} [c]^2} (a + a \sec [c + d x])^3 \right) - \\
 & \left( 4 C \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \text{Csc} \left[ \frac{c}{2} \right] \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \text{ArcTan} [\text{Cot} [c]]]^2 \right] \right. \\
 & \quad \text{Sec} \left[ \frac{c}{2} \right] \text{Sec} [c + d x] (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \quad \left. \text{Sec} [d x - \text{ArcTan} [\text{Cot} [c]]] \sqrt{1 - \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \right. \\
 & \quad \left. \sqrt{-\sqrt{1 + \text{Cot} [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \sqrt{1 + \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \right) / \\
 & \left( 3 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \text{Cot} [c]^2} (a + a \sec [c + d x])^3 \right) + \\
 & \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 (A + B \sec [c + d x] + C \sec [c + d x]^2) \left( -\frac{8 (29 A - 9 B - C + 20 A \cos [c]) \text{Csc} [c]}{5 d} - \right. \right. \\
 & \quad \frac{1}{5 d} 8 \text{Sec} \left[ \frac{c}{2} \right] \text{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right] \left( 29 A \sin \left[ \frac{d x}{2} \right] - 9 B \sin \left[ \frac{d x}{2} \right] - C \sin \left[ \frac{d x}{2} \right] \right) - \\
 & \quad \frac{4 \text{Sec} \left[ \frac{c}{2} \right] \text{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^5 \left( A \sin \left[ \frac{d x}{2} \right] - B \sin \left[ \frac{d x}{2} \right] + C \sin \left[ \frac{d x}{2} \right] \right)}{5 d} + \frac{1}{15 d} \\
 & \quad 8 \text{Sec} \left[ \frac{c}{2} \right] \text{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^3 \left( 14 A \sin \left[ \frac{d x}{2} \right] - 9 B \sin \left[ \frac{d x}{2} \right] + 4 C \sin \left[ \frac{d x}{2} \right] \right) + \\
 & \quad \left. \left. \frac{8 (14 A - 9 B + 4 C) \text{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \text{Tan} \left[ \frac{c}{2} \right]}{15 d} - \frac{4 (A - B + C) \text{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \text{Tan} \left[ \frac{c}{2} \right]}{5 d} \right) \right) / \\
 & \left( \sqrt{\cos [c + d x]} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^3 \right)
 \end{aligned}$$

Problem 1235: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2}{\sqrt{\operatorname{Cos}[c + d x]} (a + a \operatorname{Sec}[c + d x])^3} dx$$

Optimal (type 4, 193 leaves, 7 steps):

$$\begin{aligned} & - \frac{(9A + B - C) \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right]}{10a^3d} + \\ & \frac{(3A + B + C) \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right]}{6a^3d} - \frac{(A - B + C) \operatorname{Cos}[c + dx]^{3/2} \operatorname{Sin}[c + dx]}{5d(a + a \operatorname{Cos}[c + dx])^3} - \\ & \frac{(6A - B - 4C) \sqrt{\operatorname{Cos}[c + dx]} \operatorname{Sin}[c + dx]}{15ad(a + a \operatorname{Cos}[c + dx])^2} + \frac{(9A + B - C) \sqrt{\operatorname{Cos}[c + dx]} \operatorname{Sin}[c + dx]}{10d(a^3 + a^3 \operatorname{Cos}[c + dx])} \end{aligned}$$

Result (type 5, 2167 leaves):

$$\begin{aligned} & - \frac{1}{5(A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^3} \\ & 9iA \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c + dx] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \\ & \left( \left( 2e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right. \right. \\ & \quad \left. \left. \frac{\sqrt{e^{-ix} (2(1 + e^{2ix}) \operatorname{Cos}[c] + 2i(-1 + e^{2ix}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2ix} \operatorname{Cos}[2c] + ie^{2ix} \operatorname{Sin}[2c]}} \right) \right) / \\ & \quad (3id(1 + e^{2ix}) \operatorname{Cos}[c] - 3d(-1 + e^{2ix}) \operatorname{Sin}[c]) - \\ & \quad \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right. \\ & \quad \left. \frac{\sqrt{e^{-ix} (2(1 + e^{2ix}) \operatorname{Cos}[c] + 2i(-1 + e^{2ix}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2ix} \operatorname{Cos}[2c] + ie^{2ix} \operatorname{Sin}[2c]}} \right) \right) / \\ & \quad \left. (-id(1 + e^{2ix}) \operatorname{Cos}[c] + d(-1 + e^{2ix}) \operatorname{Sin}[c]) \right) - \\ & \frac{1}{5(A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^3} \\ & i \\ & B \\ & \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \\ & \operatorname{Csc}\left[\frac{c}{2}\right] \\ & \operatorname{Sec}\left[\frac{c}{2}\right] \\ & \operatorname{Sec}[c + dx] \\ & (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \\ & \left( \left( 2e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right. \right. \\ & \quad \left. \left. \frac{\sqrt{e^{-ix} (2(1 + e^{2ix}) \operatorname{Cos}[c] + 2i(-1 + e^{2ix}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2ix} \operatorname{Cos}[2c] + ie^{2ix} \operatorname{Sin}[2c]}} \right) \right) \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \\
 & \left( 3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c] \right) - \\
 & \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \\
 & \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \right. \\
 & \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \\
 & \left( -i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c] \right) + \\
 & \frac{1}{5 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^3} \\
 & i \\
 & C \\
 & \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \\
 & \operatorname{Csc} \left[ \frac{c}{2} \right] \\
 & \operatorname{Sec} \left[ \frac{c}{2} \right] \\
 & \operatorname{Sec} [c + d x] \\
 & (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \right. \\
 & \left. \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \right. \right. \\
 & \left. \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \right. \\
 & \left. \left( 3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c] \right) - \right. \\
 & \left. \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \right. \\
 & \left. \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \right. \right. \\
 & \left. \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \right. \\
 & \left. \left( -i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c] \right) \right) - \\
 & \left( 4 A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]^2 \right] \right. \\
 & \left. \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} [c + d x] (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) \right. \\
 & \left. \operatorname{Sec} [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \right. \\
 & \left. \sqrt{-\sqrt{1 + \operatorname{Cot} [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \right. \\
 & \left. \sqrt{1 + \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \right) /
 \end{aligned}$$



$$\begin{aligned}
 & \left( d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sqrt{1 + \cot [c]^2} (a + a \sec [c + dx])^3 \right) - \\
 & \left( 4B \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^6 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [dx - \operatorname{ArcTan} [\cot [c]]] \right]^2 \right. \\
 & \quad \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} [c + dx] (A + B \operatorname{Sec} [c + dx] + C \operatorname{Sec} [c + dx]^2) \\
 & \quad \operatorname{Sec} [dx - \operatorname{ArcTan} [\cot [c]]] \sqrt{1 - \sin [dx - \operatorname{ArcTan} [\cot [c]]]} \\
 & \quad \left. \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [dx - \operatorname{ArcTan} [\cot [c]]]} \right. \\
 & \quad \left. \sqrt{1 + \sin [dx - \operatorname{ArcTan} [\cot [c]]]} \right) / \\
 & \left( 3d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sqrt{1 + \cot [c]^2} (a + a \sec [c + dx])^3 \right) - \\
 & \left( 4C \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^6 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [dx - \operatorname{ArcTan} [\cot [c]]] \right]^2 \right. \\
 & \quad \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} [c + dx] (A + B \operatorname{Sec} [c + dx] + C \operatorname{Sec} [c + dx]^2) \\
 & \quad \operatorname{Sec} [dx - \operatorname{ArcTan} [\cot [c]]] \sqrt{1 - \sin [dx - \operatorname{ArcTan} [\cot [c]]]} \\
 & \quad \left. \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [dx - \operatorname{ArcTan} [\cot [c]]]} \sqrt{1 + \sin [dx - \operatorname{ArcTan} [\cot [c]]]} \right) / \\
 & \left( 3d (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) \sqrt{1 + \cot [c]^2} (a + a \sec [c + dx])^3 \right) + \\
 & \left( \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^6 (A + B \operatorname{Sec} [c + dx] + C \operatorname{Sec} [c + dx]^2) \left( \frac{8(9A + B - C) \operatorname{Csc} [c]}{5d} - \right. \right. \\
 & \quad \frac{1}{15d} 8 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right]^3 \left( 9A \sin \left[ \frac{dx}{2} \right] - 4B \sin \left[ \frac{dx}{2} \right] - C \sin \left[ \frac{dx}{2} \right] \right) + \\
 & \quad \frac{8 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right] \left( 9A \sin \left[ \frac{dx}{2} \right] + B \sin \left[ \frac{dx}{2} \right] - C \sin \left[ \frac{dx}{2} \right] \right)}{5d} + \\
 & \quad \frac{4 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right]^5 \left( A \sin \left[ \frac{dx}{2} \right] - B \sin \left[ \frac{dx}{2} \right] + C \sin \left[ \frac{dx}{2} \right] \right)}{5d} - \\
 & \quad \left. \left. \frac{8(9A - 4B - C) \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \operatorname{Tan} \left[ \frac{c}{2} \right]}{15d} + \frac{4(A - B + C) \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 \operatorname{Tan} \left[ \frac{c}{2} \right]}{5d} \right) \right) / \\
 & \left( \sqrt{\cos [c + dx]} (A + 2C + 2B \cos [c + dx] + A \cos [2c + 2dx]) (a + a \sec [c + dx])^3 \right)
 \end{aligned}$$

**Problem 1236:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2}{\operatorname{Cos}[c + d x]^{3/2} (a + a \operatorname{Sec}[c + d x])^3} dx$$

Optimal (type 4, 191 leaves, 7 steps):

$$\begin{aligned} & - \frac{(A - B - 9 C) \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{10 a^3 d} + \\ & \frac{(A + B + 3 C) \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{6 a^3 d} - \frac{(A - B + C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{Sin}[c + d x]}{5 d (a + a \operatorname{Cos}[c + d x])^3} + \\ & \frac{(4 A + B - 6 C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{Sin}[c + d x]}{15 a d (a + a \operatorname{Cos}[c + d x])^2} + \frac{(A - B - 9 C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{Sin}[c + d x]}{10 d (a^3 + a^3 \operatorname{Cos}[c + d x])} \end{aligned}$$

Result (type 5, 2164 leaves):

$$\begin{aligned} & - \frac{1}{5 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) (a + a \operatorname{Sec}[c + d x])^3} \\ & \quad i A \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c + d x] (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\ & \quad \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right. \right. \\ & \quad \left. \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]}} \right) \right) / \\ & \quad (3 i d (1 + e^{2 i d x}) \operatorname{Cos}[c] - 3 d (-1 + e^{2 i d x}) \operatorname{Sin}[c]) - \\ & \quad \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right. \\ & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]}} \right) / \\ & \quad \left. (-i d (1 + e^{2 i d x}) \operatorname{Cos}[c] + d (-1 + e^{2 i d x}) \operatorname{Sin}[c]) \right) + \\ & \quad \frac{1}{5 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) (a + a \operatorname{Sec}[c + d x])^3} \\ & \quad i \\ & \quad B \\ & \quad \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 \\ & \quad \operatorname{Csc}\left[\frac{c}{2}\right] \\ & \quad \operatorname{Sec}\left[\frac{c}{2}\right] \\ & \quad \operatorname{Sec}[c + d x] \\ & \quad (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\ & \quad \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right. \right. \\ & \quad \left. \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]}} \right) \right) \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]} \right) / \\
 & \left( 3 i d (1 + e^{2 i d x}) \cos[c] - 3 d (-1 + e^{2 i d x}) \sin[c] \right) - \\
 & \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2 \right] \right. \\
 & \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])} \right. \\
 & \left. \sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]} \right) / \\
 & \left( -i d (1 + e^{2 i d x}) \cos[c] + d (-1 + e^{2 i d x}) \sin[c] \right) + \\
 & \frac{1}{5 (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) (a + a \sec[c + d x])^3} \\
 & 9 \\
 & i \\
 & C \\
 & \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \\
 & \operatorname{Csc} \left[ \frac{c}{2} \right] \\
 & \operatorname{Sec} \left[ \frac{c}{2} \right] \\
 & \operatorname{Sec}[c + d x] \\
 & (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2 \right] \right. \right. \\
 & \left. \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])} \right. \right. \\
 & \left. \left. \sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]} \right) / \right. \\
 & \left. \left( 3 i d (1 + e^{2 i d x}) \cos[c] - 3 d (-1 + e^{2 i d x}) \sin[c] \right) - \right. \\
 & \left. \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2 \right] \right. \right. \\
 & \left. \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])} \right. \right. \\
 & \left. \left. \sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]} \right) / \right. \\
 & \left. \left( -i d (1 + e^{2 i d x}) \cos[c] + d (-1 + e^{2 i d x}) \sin[c] \right) \right) - \\
 & \left( 4 A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \right]^2 \right) \\
 & \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec}[c + d x] (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\
 & \operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \sin[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin[c] \sin[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}
 \end{aligned}$$

$$\begin{aligned}
 & \left. \sqrt{1 + \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \right) / \\
 & \left( 3 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \text{Cot} [c]^2} (a + a \sec [c + d x])^3 \right) - \\
 & \left( 4 B \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \text{Csc} \left[ \frac{c}{2} \right] \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \text{ArcTan} [\text{Cot} [c]]]^2 \right] \right. \\
 & \quad \text{Sec} \left[ \frac{c}{2} \right] \text{Sec} [c + d x] (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \quad \left. \text{Sec} [d x - \text{ArcTan} [\text{Cot} [c]]] \sqrt{1 - \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \right. \\
 & \quad \left. \sqrt{-\sqrt{1 + \text{Cot} [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \right. \\
 & \quad \left. \sqrt{1 + \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \right) / \\
 & \left( 3 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \text{Cot} [c]^2} (a + a \sec [c + d x])^3 \right) - \\
 & \left( 4 C \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \text{Csc} \left[ \frac{c}{2} \right] \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \text{ArcTan} [\text{Cot} [c]]]^2 \right] \right. \\
 & \quad \text{Sec} \left[ \frac{c}{2} \right] \text{Sec} [c + d x] (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \quad \left. \text{Sec} [d x - \text{ArcTan} [\text{Cot} [c]]] \sqrt{1 - \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \right. \\
 & \quad \left. \sqrt{-\sqrt{1 + \text{Cot} [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \sqrt{1 + \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \right) / \\
 & \left( d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \text{Cot} [c]^2} (a + a \sec [c + d x])^3 \right) + \\
 & \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left( \frac{8 (A - B - 9 C) \text{Csc} [c]}{5 d} + \frac{8 \text{Sec} \left[ \frac{c}{2} \right] \text{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right] (A \sin \left[ \frac{d x}{2} \right] - B \sin \left[ \frac{d x}{2} \right] - 9 C \sin \left[ \frac{d x}{2} \right])}{5 d} + \right. \\
 & \quad \frac{1}{15 d} 8 \text{Sec} \left[ \frac{c}{2} \right] \text{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^3 (4 A \sin \left[ \frac{d x}{2} \right] + B \sin \left[ \frac{d x}{2} \right] - 6 C \sin \left[ \frac{d x}{2} \right]) - \\
 & \quad \frac{4 \text{Sec} \left[ \frac{c}{2} \right] \text{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^5 (A \sin \left[ \frac{d x}{2} \right] - B \sin \left[ \frac{d x}{2} \right] + C \sin \left[ \frac{d x}{2} \right])}{5 d} + \\
 & \quad \left. \left. \frac{8 (4 A + B - 6 C) \text{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \text{Tan} \left[ \frac{c}{2} \right]}{15 d} - \frac{4 (A - B + C) \text{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \text{Tan} \left[ \frac{c}{2} \right]}{5 d} \right) \right) / \\
 & \left( \sqrt{\cos [c + d x]} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^3 \right)
 \end{aligned}$$

Problem 1237: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{A + B \sec [c + d x] + C \sec [c + d x]^2}{\cos [c + d x]^{5/2} (a + a \sec [c + d x])^3} dx$$

Optimal (type 4, 229 leaves, 8 steps):

$$\frac{(A + 9 B - 49 C) \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{10 a^3 d} + \frac{(A + 3 B - 13 C) \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{6 a^3 d} - \frac{(A + 9 B - 49 C) \sin [c + d x]}{10 a^3 d \sqrt{\cos [c + d x]}} - \frac{(A - B + C) \sin [c + d x]}{5 d \sqrt{\cos [c + d x]} (a + a \cos [c + d x])^3} + \frac{(2 A + 3 B - 8 C) \sin [c + d x]}{15 a d \sqrt{\cos [c + d x]} (a + a \cos [c + d x])^2} + \frac{(A + 3 B - 13 C) \sin [c + d x]}{6 d \sqrt{\cos [c + d x]} (a^3 + a^3 \cos [c + d x])}$$

Result (type 5, 2205 leaves):

$$\frac{1}{5 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^3} + \frac{i A \cos \left[\frac{c}{2} + \frac{d x}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c + d x] (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2\right] \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \right. \\ \left. (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) - \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2\right] \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \right. \\ \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) + \frac{1}{5 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^3} + \frac{9 i B \cos \left[\frac{c}{2} + \frac{d x}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c + d x] (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2\right] \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \right)}$$

$$\begin{aligned}
 & \left( \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \\
 & \left( 3 i d \left( 1 + e^{2 i d x} \right) \cos [c] - 3 d \left( -1 + e^{2 i d x} \right) \sin [c] \right) - \\
 & \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} \left( \cos [c] + i \sin [c] \right)^2 \right] \right. \\
 & \left. \sqrt{e^{-i d x} \left( 2 \left( 1 + e^{2 i d x} \right) \cos [c] + 2 i \left( -1 + e^{2 i d x} \right) \sin [c] \right)} \right. \\
 & \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \\
 & \left( -i d \left( 1 + e^{2 i d x} \right) \cos [c] + d \left( -1 + e^{2 i d x} \right) \sin [c] \right) - \\
 & \frac{1}{5 \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \left( a + a \sec [c + d x] \right)^3} \\
 & 49 i C \\
 & \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \operatorname{Csc} \left[ \frac{c}{2} \right] \\
 & \sec \left[ \frac{c}{2} \right] \sec [c + d x] \\
 & \left( A + B \sec [c + d x] + C \sec [c + d x]^2 \right) \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} \left( \cos [c] + i \sin [c] \right)^2 \right] \right. \right. \\
 & \left. \left. \sqrt{e^{-i d x} \left( 2 \left( 1 + e^{2 i d x} \right) \cos [c] + 2 i \left( -1 + e^{2 i d x} \right) \sin [c] \right)} \right. \right. \\
 & \left. \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \right. \\
 & \left. \left( 3 i d \left( 1 + e^{2 i d x} \right) \cos [c] - 3 d \left( -1 + e^{2 i d x} \right) \sin [c] \right) - \right. \\
 & \left. \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} \left( \cos [c] + i \sin [c] \right)^2 \right] \right. \right. \\
 & \left. \left. \sqrt{e^{-i d x} \left( 2 \left( 1 + e^{2 i d x} \right) \cos [c] + 2 i \left( -1 + e^{2 i d x} \right) \sin [c] \right)} \right. \right. \\
 & \left. \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \right. \\
 & \left. \left( -i d \left( 1 + e^{2 i d x} \right) \cos [c] + d \left( -1 + e^{2 i d x} \right) \sin [c] \right) \right) - \\
 & \left( 4 A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \right]^2 \right) \\
 & \sec \left[ \frac{c}{2} \right] \sec [c + d x] \left( A + B \sec [c + d x] + C \sec [c + d x]^2 \right) \\
 & \sec [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \\
 & \sqrt{-\sqrt{1 + \operatorname{Cot} [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \\
 & \left. \sqrt{1 + \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \right) / \\
 & \left( 3 d \left( A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x] \right) \sqrt{1 + \operatorname{Cot} [c]^2} \left( a + a \sec [c + d x] \right)^3 \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \left( 4 B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin\left[dx - \operatorname{ArcTan}\left[\operatorname{Cot}[c]\right]\right]^2\right] \right. \\
 & \quad \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c + dx] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \\
 & \quad \operatorname{Sec}\left[dx - \operatorname{ArcTan}\left[\operatorname{Cot}[c]\right]\right] \sqrt{1 - \sin\left[dx - \operatorname{ArcTan}\left[\operatorname{Cot}[c]\right]\right]} \\
 & \quad \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin[c] \sin\left[dx - \operatorname{ArcTan}\left[\operatorname{Cot}[c]\right]\right]} \sqrt{1 + \sin\left[dx - \operatorname{ArcTan}\left[\operatorname{Cot}[c]\right]\right]} \right) / \\
 & \left( d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{1 + \operatorname{Cot}[c]^2} (a + a \operatorname{Sec}[c + dx])^3 \right) + \\
 & \left( 52 C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin\left[dx - \operatorname{ArcTan}\left[\operatorname{Cot}[c]\right]\right]^2\right] \right. \\
 & \quad \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c + dx] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \\
 & \quad \operatorname{Sec}\left[dx - \operatorname{ArcTan}\left[\operatorname{Cot}[c]\right]\right] \sqrt{1 - \sin\left[dx - \operatorname{ArcTan}\left[\operatorname{Cot}[c]\right]\right]} \\
 & \quad \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin[c] \sin\left[dx - \operatorname{ArcTan}\left[\operatorname{Cot}[c]\right]\right]} \sqrt{1 + \sin\left[dx - \operatorname{ArcTan}\left[\operatorname{Cot}[c]\right]\right]} \right) / \\
 & \left( 3 d (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{1 + \operatorname{Cot}[c]^2} (a + a \operatorname{Sec}[c + dx])^3 \right) + \\
 & \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right. \\
 & \quad \left( \frac{1}{5d} 4 (20C - A \cos[c] - 9B \cos[c] + 29C \cos[c]) \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c] - \right. \\
 & \quad \frac{1}{5d} 8 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] \left( A \sin\left[\frac{dx}{2}\right] + 9B \sin\left[\frac{dx}{2}\right] - 29C \sin\left[\frac{dx}{2}\right] \right) + \\
 & \quad \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^5 \left( A \sin\left[\frac{dx}{2}\right] - B \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right] \right)}{5d} + \frac{1}{15d} 8 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 \\
 & \quad \left( A \sin\left[\frac{dx}{2}\right] - 6B \sin\left[\frac{dx}{2}\right] + 11C \sin\left[\frac{dx}{2}\right] \right) + \frac{32C \operatorname{Sec}[c] \operatorname{Sec}[c + dx] \sin[dx]}{d} + \\
 & \quad \left. \frac{8(A - 6B + 11C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Tan}\left[\frac{c}{2}\right]}{15d} + \frac{4(A - B + C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Tan}\left[\frac{c}{2}\right]}{5d} \right) \left. \right) / \\
 & \left( \sqrt{\cos[c + dx]} (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^3 \right)
 \end{aligned}$$

**Problem 1238:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2}{\cos[c + dx]^{7/2} (a + a \operatorname{Sec}[c + dx])^3} dx$$

Optimal (type 4, 268 leaves, 9 steps):

$$\frac{(9A - 49B + 119C) \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right]}{10a^3d} + \frac{(3A - 13B + 33C) \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right]}{6a^3d} + \frac{(3A - 13B + 33C) \operatorname{Sin}[c + dx]}{6a^3d \operatorname{Cos}[c + dx]^{3/2}} - \frac{(9A - 49B + 119C) \operatorname{Sin}[c + dx]}{10a^3d \sqrt{\operatorname{Cos}[c + dx]}} - \frac{(A - B + C) \operatorname{Sin}[c + dx]}{5d \operatorname{Cos}[c + dx]^{3/2} (a + a \operatorname{Cos}[c + dx])^3} + \frac{(B - 2C) \operatorname{Sin}[c + dx]}{3ad \operatorname{Cos}[c + dx]^{3/2} (a + a \operatorname{Cos}[c + dx])^2} - \frac{(9A - 49B + 119C) \operatorname{Sin}[c + dx]}{30d \operatorname{Cos}[c + dx]^{3/2} (a^3 + a^3 \operatorname{Cos}[c + dx])}$$

Result (type 5, 2248 leaves):

$$\frac{1}{5(A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^3} - \frac{9iA \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c + dx] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx])^2}{\left(\left(2e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \sqrt{e^{-ix} (2(1 + e^{2ix}) \operatorname{Cos}[c] + 2i(-1 + e^{2ix}) \operatorname{Sin}[c])} \sqrt{1 + e^{2ix} \operatorname{Cos}[2c] + i e^{2ix} \operatorname{Sin}[2c]}\right)}{(3id(1 + e^{2ix}) \operatorname{Cos}[c] - 3d(-1 + e^{2ix}) \operatorname{Sin}[c]) - \left(2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \sqrt{e^{-ix} (2(1 + e^{2ix}) \operatorname{Cos}[c] + 2i(-1 + e^{2ix}) \operatorname{Sin}[c])} \sqrt{1 + e^{2ix} \operatorname{Cos}[2c] + i e^{2ix} \operatorname{Sin}[2c]}\right)}{(-id(1 + e^{2ix}) \operatorname{Cos}[c] + d(-1 + e^{2ix}) \operatorname{Sin}[c])}\right)} - \frac{1}{5(A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) (a + a \operatorname{Sec}[c + dx])^3} - \frac{49iB \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c + dx] (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx])^2}{\left(\left(2e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \sqrt{e^{-ix} (2(1 + e^{2ix}) \operatorname{Cos}[c] + 2i(-1 + e^{2ix}) \operatorname{Sin}[c])} \sqrt{1 + e^{2ix} \operatorname{Cos}[2c] + i e^{2ix} \operatorname{Sin}[2c]}\right)}{(3id(1 + e^{2ix}) \operatorname{Cos}[c] - 3d(-1 + e^{2ix}) \operatorname{Sin}[c]) - \right)}$$



$$\begin{aligned}
 & \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) + \\
 & \quad \frac{1}{5 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^3} \\
 & \quad 119 i C \\
 & \quad \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \operatorname{Csc} \left[ \frac{c}{2} \right] \\
 & \quad \sec \left[ \frac{c}{2} \right] \sec [c + d x] \\
 & \quad (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \quad \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \quad \left. (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) - \right. \\
 & \quad \left. \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) - \\
 & \quad \left( 4 A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right]^2 \right) \\
 & \quad \sec \left[ \frac{c}{2} \right] \sec [c + d x] (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \quad \sec [d x - \operatorname{ArcTan} [\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan} [\cot [c]]]} \\
 & \quad \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]]} \\
 & \quad \left. \sqrt{1 + \sin [d x - \operatorname{ArcTan} [\cot [c]]]} \right) / \\
 & \quad \left( d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} (a + a \sec [c + d x])^3 \right) + \\
 & \quad \left( 52 B \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right]^2 \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{\sec\left[\frac{c}{2}\right] \sec[c+dx] (A+B \sec[c+dx] + C \sec[c+dx]^2)}{\sec[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \sin[dx - \text{ArcTan}[\text{Cot}[c]]]}} \right. \\
 & \left. \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 + \sin[dx - \text{ArcTan}[\text{Cot}[c]]]}} \right) / \\
 & \left( 3d (A + 2C + 2B \cos[c+dx] + A \cos[2c + 2dx]) \sqrt{1 + \text{Cot}[c]^2} (a + a \sec[c+dx])^3 \right) - \\
 & \left( 44C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \text{Csc}\left[\frac{c}{2}\right] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\text{Cot}[c]]]^2\right] \right. \\
 & \left. \frac{\sec\left[\frac{c}{2}\right] \sec[c+dx] (A+B \sec[c+dx] + C \sec[c+dx]^2)}{\sec[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \sin[dx - \text{ArcTan}[\text{Cot}[c]]]}} \right. \\
 & \left. \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 + \sin[dx - \text{ArcTan}[\text{Cot}[c]]]}} \right) / \\
 & \left( d (A + 2C + 2B \cos[c+dx] + A \cos[2c + 2dx]) \sqrt{1 + \text{Cot}[c]^2} (a + a \sec[c+dx])^3 \right) + \\
 & \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (A + B \sec[c+dx] + C \sec[c+dx]^2) \right. \\
 & \left( -\frac{1}{5d} 4 (-20B + 60C + 9A \cos[c] - 29B \cos[c] + 59C \cos[c]) \text{Csc}\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right] \sec[c] - \right. \\
 & \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^5 (A \sin\left[\frac{dx}{2}\right] - B \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{5d} - \frac{1}{15d} 8 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^3 \\
 & \left( 6A \sin\left[\frac{dx}{2}\right] - 11B \sin\left[\frac{dx}{2}\right] + 16C \sin\left[\frac{dx}{2}\right] \right) - \frac{1}{5d} 8 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right] \\
 & \left( 9A \sin\left[\frac{dx}{2}\right] - 29B \sin\left[\frac{dx}{2}\right] + 59C \sin\left[\frac{dx}{2}\right] \right) + \frac{32C \sec[c] \sec[c+dx]^2 \sin[dx]}{3d} + \\
 & \frac{32 \sec[c] \sec[c+dx] (C \sin[c] + 3B \sin[dx] - 9C \sin[dx])}{3d} - \\
 & \left. \left. \frac{8 (6A - 11B + 16C) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{15d} - \frac{4 (A - B + C) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \tan\left[\frac{c}{2}\right]}{5d} \right) \right) / \\
 & \left( \sqrt{\cos[c+dx]} (A + 2C + 2B \cos[c+dx] + A \cos[2c + 2dx]) (a + a \sec[c+dx])^3 \right)
 \end{aligned}$$

**Problem 1239: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c+dx]^{3/2} (A + B \sec[c+dx] + C \sec[c+dx]^2)}{(a + a \sec[c+dx])^4} dx$$

Optimal (type 4, 278 leaves, 9 steps):

$$\begin{aligned}
 & - \frac{(176 A - 57 B + 8 C) \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{10 a^4 d} + \\
 & \frac{(339 A - 108 B + 17 C) \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{42 a^4 d} + \frac{(339 A - 108 B + 17 C) \sqrt{\cos [c + d x]} \sin [c + d x]}{42 a^4 d} - \\
 & \frac{(43 A - 15 B + C) \cos [c + d x]^{5/2} \sin [c + d x]}{42 a^4 d (1 + \cos [c + d x])^2} - \frac{(176 A - 57 B + 8 C) \cos [c + d x]^{3/2} \sin [c + d x]}{30 a^4 d (1 + \cos [c + d x])} - \\
 & \frac{(A - B + C) \cos [c + d x]^{9/2} \sin [c + d x]}{7 d (a + a \cos [c + d x])^4} - \frac{(13 A - 6 B - C) \cos [c + d x]^{7/2} \sin [c + d x]}{35 a d (a + a \cos [c + d x])^3}
 \end{aligned}$$

Result (type 5, 2319 leaves):

$$\begin{aligned}
 & - \frac{1}{5 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^4} \\
 & 352 i A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} [c + d x]^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \quad (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) - \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) + \\
 & \frac{1}{5 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^4} \\
 & 114 \\
 & i \\
 & B \\
 & \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 \\
 & \operatorname{Csc} \left[ \frac{c}{2} \right] \\
 & \operatorname{Sec} \left[ \frac{c}{2} \right] \\
 & \operatorname{Sec} [c + d x]^2 \\
 & (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \\
 & \left( 3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c] \right) - \\
 & \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \\
 & \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \right. \\
 & \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \\
 & \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) - \\
 & \qquad \qquad \qquad 1 \\
 & \frac{5 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^4}{16} \\
 & \frac{i}{C} \\
 & \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 \\
 & \operatorname{Csc} \left[ \frac{c}{2} \right] \\
 & \operatorname{Sec} \left[ \frac{c}{2} \right] \\
 & \operatorname{Sec} [c + d x]^2 \\
 & (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \right. \\
 & \left. \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \right. \right. \\
 & \left. \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \right. \\
 & \left. \left( 3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c] \right) - \right. \\
 & \left. \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \right. \\
 & \left. \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \right. \right. \\
 & \left. \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \right. \\
 & \left. \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) \right) - \\
 & \left( 904 A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \right]^2 \right) \\
 & \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} [c + d x]^2 (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) \\
 & \operatorname{Sec} [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \\
 & \sqrt{-\sqrt{1 + \operatorname{Cot} [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]}
 \end{aligned}$$

$$\begin{aligned}
 & \left. \sqrt{1 + \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \right) / \\
 & \left( 7 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \text{Cot} [c]^2} (a + a \sec [c + d x])^4 \right) + \\
 & \left( 288 B \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 \text{Csc} \left[ \frac{c}{2} \right] \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \text{ArcTan} [\text{Cot} [c]]] \right]^2 \right) \\
 & \quad \sec \left[ \frac{c}{2} \right] \sec [c + d x]^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \quad \sec [d x - \text{ArcTan} [\text{Cot} [c]]] \sqrt{1 - \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \\
 & \quad \sqrt{-\sqrt{1 + \text{Cot} [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \\
 & \left. \sqrt{1 + \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \right) / \\
 & \left( 7 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \text{Cot} [c]^2} (a + a \sec [c + d x])^4 \right) - \\
 & \left( 136 C \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 \text{Csc} \left[ \frac{c}{2} \right] \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \text{ArcTan} [\text{Cot} [c]]] \right]^2 \right) \\
 & \quad \sec \left[ \frac{c}{2} \right] \sec [c + d x]^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \quad \sec [d x - \text{ArcTan} [\text{Cot} [c]]] \sqrt{1 - \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \\
 & \quad \sqrt{-\sqrt{1 + \text{Cot} [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \sqrt{1 + \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \right) / \\
 & \left( 21 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \text{Cot} [c]^2} (a + a \sec [c + d x])^4 \right) + \\
 & \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left( \frac{16 (96 A - 37 B + 8 C + 8 \theta A \cos [c] - 2 \theta B \cos [c]) \text{Csc} [c]}{5 d} + \frac{64 A \cos [d x] \sin [c]}{3 d} - \right. \\
 & \quad \left. \frac{4 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^7 (A \sin \left[ \frac{d x}{2} \right] - B \sin \left[ \frac{d x}{2} \right] + C \sin \left[ \frac{d x}{2} \right])}{7 d} + \frac{1}{5 d} \right. \\
 & \quad \left. 16 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right] \left( 96 A \sin \left[ \frac{d x}{2} \right] - 37 B \sin \left[ \frac{d x}{2} \right] + 8 C \sin \left[ \frac{d x}{2} \right] \right) + \frac{1}{35 d} \right. \\
 & \quad \left. 8 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^5 \left( 33 A \sin \left[ \frac{d x}{2} \right] - 26 B \sin \left[ \frac{d x}{2} \right] + 19 C \sin \left[ \frac{d x}{2} \right] \right) - \frac{1}{105 d} \right. \\
 & \quad \left. 8 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^3 \left( 629 A \sin \left[ \frac{d x}{2} \right] - 363 B \sin \left[ \frac{d x}{2} \right] + 167 C \sin \left[ \frac{d x}{2} \right] \right) \right) +
 \end{aligned}$$

$$\left( \frac{64 A \cos [c] \sin [d x]}{3 d} - \frac{8 (629 A - 363 B + 167 C) \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \tan \left[ \frac{c}{2} \right]}{105 d} + \frac{8 (33 A - 26 B + 19 C) \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \tan \left[ \frac{c}{2} \right]}{35 d} - \frac{4 (A - B + C) \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \tan \left[ \frac{c}{2} \right]}{7 d} \right) / \left( \cos [c + d x]^{3/2} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^4 \right)$$

**Problem 1240: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\cos [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2)}{(a + a \sec [c + d x])^4} dx$$

Optimal (type 4, 244 leaves, 8 steps):

$$\frac{(57 A - 8 B - C) \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{10 a^4 d} - \frac{(108 A - 17 B - 4 C) \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{42 a^4 d} - \frac{(141 A - 29 B - 13 C) \cos [c + d x]^{3/2} \sin [c + d x]}{210 a^4 d (1 + \cos [c + d x])^2} - \frac{(108 A - 17 B - 4 C) \sqrt{\cos [c + d x]} \sin [c + d x]}{42 a^4 d (1 + \cos [c + d x])} - \frac{(A - B + C) \cos [c + d x]^{7/2} \sin [c + d x]}{7 d (a + a \cos [c + d x])^4} - \frac{(11 A - 4 B - 3 C) \cos [c + d x]^{5/2} \sin [c + d x]}{35 a d (a + a \cos [c + d x])^3}$$

Result (type 5, 2286 leaves):

$$\frac{1}{5 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^4} - \frac{114 i A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 \operatorname{Csc} \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} \right] \sec [c + d x]^2 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \left( 3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c] \right) - \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \left( -i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c] \right) \right) - \frac{1}{16 i B} 5 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^4$$

$$\begin{aligned}
 & \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^8 \operatorname{Csc}\left[\frac{c}{2}\right] \\
 & \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^2 \\
 & (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \\
 & \left( \left( 2 e^{2i dx} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2i dx} (\cos[c] + i \sin[c])^2\right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i dx} (2(1+e^{2i dx}) \cos[c] + 2i(-1+e^{2i dx}) \sin[c])}}{\sqrt{1+e^{2i dx} \cos[2c] + i e^{2i dx} \sin[2c]}} \right) / \\
 & \quad (3i d (1+e^{2i dx}) \cos[c] - 3d(-1+e^{2i dx}) \sin[c]) - \\
 & \quad \left. \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i dx} (\cos[c] + i \sin[c])^2\right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i dx} (2(1+e^{2i dx}) \cos[c] + 2i(-1+e^{2i dx}) \sin[c])}}{\sqrt{1+e^{2i dx} \cos[2c] + i e^{2i dx} \sin[2c]}} \right) / \\
 & \quad \left. (-i d (1+e^{2i dx}) \cos[c] + d(-1+e^{2i dx}) \sin[c]) \right) - \\
 & \quad \left. \frac{1}{5(A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) (a+a \operatorname{Sec}[c+dx])^4} \right. \\
 & \quad \left. 2i C \right. \\
 & \quad \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^8 \operatorname{Csc}\left[\frac{c}{2}\right] \\
 & \quad \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^2 \\
 & \quad (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \\
 & \quad \left( \left( 2 e^{2i dx} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2i dx} (\cos[c] + i \sin[c])^2\right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i dx} (2(1+e^{2i dx}) \cos[c] + 2i(-1+e^{2i dx}) \sin[c])}}{\sqrt{1+e^{2i dx} \cos[2c] + i e^{2i dx} \sin[2c]}} \right) / \\
 & \quad (3i d (1+e^{2i dx}) \cos[c] - 3d(-1+e^{2i dx}) \sin[c]) - \\
 & \quad \left. \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i dx} (\cos[c] + i \sin[c])^2\right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i dx} (2(1+e^{2i dx}) \cos[c] + 2i(-1+e^{2i dx}) \sin[c])}}{\sqrt{1+e^{2i dx} \cos[2c] + i e^{2i dx} \sin[2c]}} \right) / \\
 & \quad \left. (-i d (1+e^{2i dx}) \cos[c] + d(-1+e^{2i dx}) \sin[c]) \right) + \\
 & \quad \left( 288 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^8 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2 \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^2 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right. \\
 & \quad \left. \operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{\sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]}}{\sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]}} \right) / \\
 & \left( 7d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \sqrt{1+\cot[c]^2} (a+a \sec[c+dx])^4 \right) - \\
 & \left( 136B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^8 \csc\left[\frac{c}{2}\right] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\cot[c]]]\right]^2 \right. \\
 & \quad \sec\left[\frac{c}{2}\right] \sec[c+dx]^2 (A+B \sec[c+dx] + C \sec[c+dx]^2) \\
 & \quad \left. \sec[dx - \text{ArcTan}[\cot[c]]] \sqrt{1-\sin[dx - \text{ArcTan}[\cot[c]]]} \right. \\
 & \quad \left. \frac{\sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]} \sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]} \right) / \\
 & \left( 21d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \sqrt{1+\cot[c]^2} (a+a \sec[c+dx])^4 \right) - \\
 & \left( 32C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^8 \csc\left[\frac{c}{2}\right] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\cot[c]]]\right]^2 \right. \\
 & \quad \sec\left[\frac{c}{2}\right] \sec[c+dx]^2 (A+B \sec[c+dx] + C \sec[c+dx]^2) \\
 & \quad \left. \sec[dx - \text{ArcTan}[\cot[c]]] \sqrt{1-\sin[dx - \text{ArcTan}[\cot[c]]]} \right. \\
 & \quad \left. \frac{\sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]} \sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]} \right) / \\
 & \left( 21d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \sqrt{1+\cot[c]^2} (a+a \sec[c+dx])^4 \right) + \\
 & \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (A+B \sec[c+dx] + C \sec[c+dx]^2) \left( -\frac{16(37A-8B-C+20A \cos[c]) \csc[c]}{5d} - \right. \right. \\
 & \quad \frac{1}{5d} 16 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right] \left( 37A \sin\left[\frac{dx}{2}\right] - 8B \sin\left[\frac{dx}{2}\right] - C \sin\left[\frac{dx}{2}\right] \right) + \\
 & \quad \left. \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^7 (A \sin\left[\frac{dx}{2}\right] - B \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{7d} - \frac{1}{35d} \right. \\
 & \quad \left. 8 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^5 \left( 26A \sin\left[\frac{dx}{2}\right] - 19B \sin\left[\frac{dx}{2}\right] + 12C \sin\left[\frac{dx}{2}\right] \right) + \frac{1}{105d} \right. \\
 & \quad \left. 8 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^3 \left( 363A \sin\left[\frac{dx}{2}\right] - 167B \sin\left[\frac{dx}{2}\right] + 41C \sin\left[\frac{dx}{2}\right] \right) + \right. \\
 & \quad \left. \frac{8(363A-167B+41C) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{105d} \right) -
 \end{aligned}$$



$$\left. \frac{8 (26 A - 19 B + 12 C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Tan}\left[\frac{c}{2}\right] + 4 (A - B + C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Tan}\left[\frac{c}{2}\right]}{35 d} + \frac{4 (A - B + C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Tan}\left[\frac{c}{2}\right]}{7 d} \right) \Bigg/$$

$$\left( \operatorname{Cos}[c + dx]^{3/2} (A + 2 C + 2 B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2 c + 2 d x]) (a + a \operatorname{Sec}[c + dx])^4 \right)$$

**Problem 1241: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2}{\sqrt{\operatorname{Cos}[c + dx]} (a + a \operatorname{Sec}[c + dx])^4} dx$$

Optimal (type 4, 232 leaves, 8 steps):

$$-\frac{(8 A + B) \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right]}{10 a^4 d} + \frac{(17 A + 4 B + 3 C) \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right]}{42 a^4 d} -$$

$$\frac{(83 A + B - 15 C) \sqrt{\operatorname{Cos}[c + dx]} \operatorname{Sin}[c + dx]}{210 a^4 d (1 + \operatorname{Cos}[c + dx])^2} + \frac{(8 A + B) \sqrt{\operatorname{Cos}[c + dx]} \operatorname{Sin}[c + dx]}{10 a^4 d (1 + \operatorname{Cos}[c + dx])} -$$

$$\frac{(A - B + C) \operatorname{Cos}[c + dx]^{5/2} \operatorname{Sin}[c + dx]}{7 d (a + a \operatorname{Cos}[c + dx])^4} - \frac{(9 A - 2 B - 5 C) \operatorname{Cos}[c + dx]^{3/2} \operatorname{Sin}[c + dx]}{35 a d (a + a \operatorname{Cos}[c + dx])^3}$$

Result (type 5, 1862 leaves):

$$-\frac{1}{5 (A + 2 C + 2 B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2 c + 2 d x]) (a + a \operatorname{Sec}[c + dx])^4}$$

$$16 i A \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^8 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c + dx]^2 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2)$$

$$\left( \left( 2 e^{2 i dx} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i dx} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right. \right.$$

$$\frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i dx}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i dx} \operatorname{Cos}[2 c] + i e^{2 i dx} \operatorname{Sin}[2 c]}} \Bigg) /$$

$$(3 i d (1 + e^{2 i dx}) \operatorname{Cos}[c] - 3 d (-1 + e^{2 i dx}) \operatorname{Sin}[c]) -$$

$$\left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i dx} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right. \right.$$

$$\frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i dx}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i dx} \operatorname{Cos}[2 c] + i e^{2 i dx} \operatorname{Sin}[2 c]}} \Bigg) /$$

$$\left. \left. (-i d (1 + e^{2 i dx}) \operatorname{Cos}[c] + d (-1 + e^{2 i dx}) \operatorname{Sin}[c]) \right) -$$

$$\frac{1}{5 (A + 2 C + 2 B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2 c + 2 d x]) (a + a \operatorname{Sec}[c + dx])^4}$$

$$2$$

$$i$$

$$B$$

$$\begin{aligned}
 & \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^8 \\
 & \csc\left[\frac{c}{2}\right] \\
 & \sec\left[\frac{c}{2}\right] \\
 & \sec[c+dx]^2 \\
 & (A+B \sec[c+dx] + C \sec[c+dx]^2) \\
 & \left( \left( 2 e^{2 i d x} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])}}{\sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]}} \right) / \\
 & \quad (3 i d (1 + e^{2 i d x}) \cos[c] - 3 d (-1 + e^{2 i d x}) \sin[c]) - \\
 & \quad \left( 2 \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])}}{\sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2 i d x}) \cos[c] + d (-1 + e^{2 i d x}) \sin[c]) \right) - \\
 & \left( 136 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^8 \csc\left[\frac{c}{2}\right] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\text{Cot}[c]]]\right]^2 \right) \\
 & \quad \sec\left[\frac{c}{2}\right] \sec[c+dx]^2 (A+B \sec[c+dx] + C \sec[c+dx]^2) \\
 & \quad \sec[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \sin[dx - \text{ArcTan}[\text{Cot}[c]]]} \\
 & \quad \left. \frac{\sqrt{-\sqrt{1 + \text{Cot}[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\text{Cot}[c]]]}}{\sqrt{1 + \sin[dx - \text{ArcTan}[\text{Cot}[c]]]}} \right) / \\
 & \left( 21 d (A + 2 C + 2 B \cos[c+dx] + A \cos[2c + 2dx]) \sqrt{1 + \text{Cot}[c]^2} (a + a \sec[c+dx])^4 \right) - \\
 & \left( 32 B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^8 \csc\left[\frac{c}{2}\right] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\text{Cot}[c]]]\right]^2 \right) \\
 & \quad \sec\left[\frac{c}{2}\right] \sec[c+dx]^2 (A+B \sec[c+dx] + C \sec[c+dx]^2) \\
 & \quad \sec[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \sin[dx - \text{ArcTan}[\text{Cot}[c]]]} \\
 & \quad \left. \frac{\sqrt{-\sqrt{1 + \text{Cot}[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\text{Cot}[c]]]}}{\sqrt{1 + \sin[dx - \text{ArcTan}[\text{Cot}[c]]]}} \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( 21 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} (a + a \sec [c + d x])^4 \right) - \\
 & \left( 8 C \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right]^2 \right. \\
 & \quad \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} [c + d x]^2 (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) \\
 & \quad \left. \operatorname{Sec} [d x - \operatorname{ArcTan} [\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan} [\cot [c]]]} \right. \\
 & \quad \left. \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]]} \sqrt{1 + \sin [d x - \operatorname{ArcTan} [\cot [c]]]} \right) / \\
 & \left( 7 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} (a + a \sec [c + d x])^4 \right) + \\
 & \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) \right. \\
 & \quad \left( \frac{16 (8 A + B) \operatorname{Csc} [c]}{5 d} + \frac{16 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right] (8 A \sin \left[ \frac{d x}{2} \right] + B \sin \left[ \frac{d x}{2} \right])}{5 d} - \frac{1}{105 d} \right. \\
 & \quad 8 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^3 (167 A \sin \left[ \frac{d x}{2} \right] - 41 B \sin \left[ \frac{d x}{2} \right] - 15 C \sin \left[ \frac{d x}{2} \right]) - \\
 & \quad \left. \frac{4 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^7 (A \sin \left[ \frac{d x}{2} \right] - B \sin \left[ \frac{d x}{2} \right] + C \sin \left[ \frac{d x}{2} \right])}{7 d} + \frac{1}{35 d} \right. \\
 & \quad 8 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^5 (19 A \sin \left[ \frac{d x}{2} \right] - 12 B \sin \left[ \frac{d x}{2} \right] + 5 C \sin \left[ \frac{d x}{2} \right]) - \\
 & \quad \left. \frac{8 (167 A - 41 B - 15 C) \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \operatorname{Tan} \left[ \frac{c}{2} \right]}{105 d} + \right. \\
 & \quad \left. \left. \frac{8 (19 A - 12 B + 5 C) \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \operatorname{Tan} \left[ \frac{c}{2} \right]}{35 d} - \frac{4 (A - B + C) \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \operatorname{Tan} \left[ \frac{c}{2} \right]}{7 d} \right) / \right) \\
 & \left( \cos [c + d x]^{3/2} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^4 \right)
 \end{aligned}$$

**Problem 1242: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2}{\cos [c + d x]^{3/2} (a + a \sec [c + d x])^4} dx$$

Optimal (type 4, 229 leaves, 8 steps):

$$\begin{aligned}
 & - \frac{(A-C) \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{10 a^4 d} + \frac{(4A+3B+4C) \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{42 a^4 d} + \\
 & \frac{(41A+15B-C) \sqrt{\cos[c+dx]} \sin[c+dx]}{210 a^4 d (1+\cos[c+dx])^2} + \frac{(A-C) \sqrt{\cos[c+dx]} \sin[c+dx]}{10 a^4 d (1+\cos[c+dx])} - \\
 & \frac{(A-B+C) \cos[c+dx]^{3/2} \sin[c+dx]}{7 d (a+a \cos[c+dx])^4} - \frac{(A-C) \sqrt{\cos[c+dx]} \sin[c+dx]}{5 a d (a+a \cos[c+dx])^3}
 \end{aligned}$$

Result (type 5, 1862 leaves):

$$\begin{aligned}
 & - \frac{1}{5 (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) (a+a \sec[c+dx])^4} \\
 & 2 i A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^8 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^2 (A+B \sec[c+dx] + C \sec[c+dx]^2) \\
 & \left( \left( 2 e^{2 i dx} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i dx} (\cos[c] + i \sin[c])^2\right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i dx} (2 (1+e^{2 i dx}) \cos[c] + 2 i (-1+e^{2 i dx}) \sin[c])}}{\sqrt{1+e^{2 i dx} \cos[2c] + i e^{2 i dx} \sin[2c]}} \right) / \\
 & \quad \left( 3 i d (1+e^{2 i dx}) \cos[c] - 3 d (-1+e^{2 i dx}) \sin[c] \right) - \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i dx} (\cos[c] + i \sin[c])^2\right] \right. \\
 & \quad \left. \frac{\sqrt{e^{-i dx} (2 (1+e^{2 i dx}) \cos[c] + 2 i (-1+e^{2 i dx}) \sin[c])}}{\sqrt{1+e^{2 i dx} \cos[2c] + i e^{2 i dx} \sin[2c]}} \right) / \\
 & \quad \left. \left. (-i d (1+e^{2 i dx}) \cos[c] + d (-1+e^{2 i dx}) \sin[c]) \right) \right) + \\
 & \frac{1}{5 (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) (a+a \sec[c+dx])^4} \\
 & 2 \\
 & i \\
 & C \\
 & \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^8 \\
 & \operatorname{Csc}\left[\frac{c}{2}\right] \\
 & \operatorname{Sec}\left[\frac{c}{2}\right] \\
 & \operatorname{Sec}[c+dx]^2 \\
 & (A+B \sec[c+dx] + C \sec[c+dx]^2) \\
 & \left( \left( 2 e^{2 i dx} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i dx} (\cos[c] + i \sin[c])^2\right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i dx} (2 (1+e^{2 i dx}) \cos[c] + 2 i (-1+e^{2 i dx}) \sin[c])}}{\sqrt{1+e^{2 i dx} \cos[2c] + i e^{2 i dx} \sin[2c]}} \right) / \\
 & \quad \left. \left( 3 i d (1+e^{2 i dx}) \cos[c] - 3 d (-1+e^{2 i dx}) \sin[c] \right) - \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i dx} (\cos[c] + i \sin[c])^2 \right] \right. \\
 & \quad \frac{\sqrt{e^{-i dx} (2(1+e^{2i dx}) \cos[c] + 2i(-1+e^{2i dx}) \sin[c])}}{\sqrt{1+e^{2i dx} \cos[2c] + i e^{2i dx} \sin[2c]}} \Bigg) / \\
 & \quad \left. (-i d (1+e^{2i dx}) \cos[c] + d (-1+e^{2i dx}) \sin[c]) \right) - \\
 & \left( 32 A \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^8 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin[dx - \operatorname{ArcTan}[\cot[c]]] \right]^2 \right) \\
 & \quad \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec}[c+dx]^2 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \\
 & \quad \operatorname{Sec}[dx - \operatorname{ArcTan}[\cot[c]]] \sqrt{1 - \sin[dx - \operatorname{ArcTan}[\cot[c]]]} \\
 & \quad \frac{\sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]]]}}{\sqrt{1 + \sin[dx - \operatorname{ArcTan}[\cot[c]]]}} \Bigg) / \\
 & \quad \left( 21 d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \sqrt{1+\cot[c]^2} (a+a \operatorname{Sec}[c+dx])^4 \right) - \\
 & \left( 8 B \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^8 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin[dx - \operatorname{ArcTan}[\cot[c]]] \right]^2 \right) \\
 & \quad \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec}[c+dx]^2 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \\
 & \quad \operatorname{Sec}[dx - \operatorname{ArcTan}[\cot[c]]] \sqrt{1 - \sin[dx - \operatorname{ArcTan}[\cot[c]]]} \\
 & \quad \frac{\sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]]]}}{\sqrt{1 + \sin[dx - \operatorname{ArcTan}[\cot[c]]]}} \Bigg) / \\
 & \quad \left( 7 d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \sqrt{1+\cot[c]^2} (a+a \operatorname{Sec}[c+dx])^4 \right) - \\
 & \left( 32 C \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^8 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin[dx - \operatorname{ArcTan}[\cot[c]]] \right]^2 \right) \\
 & \quad \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec}[c+dx]^2 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \\
 & \quad \operatorname{Sec}[dx - \operatorname{ArcTan}[\cot[c]]] \sqrt{1 - \sin[dx - \operatorname{ArcTan}[\cot[c]]]} \\
 & \quad \frac{\sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]]]}}{\sqrt{1 + \sin[dx - \operatorname{ArcTan}[\cot[c]]]}} \Bigg) / \\
 & \quad \left( 21 d (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \sqrt{1+\cot[c]^2} (a+a \operatorname{Sec}[c+dx])^4 \right) +
 \end{aligned}$$

$$\left( \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^8 (A + B \sec [c + dx] + C \sec [c + dx]^2) \left( \frac{16 (A - C) \operatorname{Csc} [c]}{5 d} - \frac{1}{35 d} \right. \right. \\
8 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right]^5 \left( 12 A \operatorname{Sin} \left[ \frac{dx}{2} \right] - 5 B \operatorname{Sin} \left[ \frac{dx}{2} \right] - 2 C \operatorname{Sin} \left[ \frac{dx}{2} \right] \right) + \\
\left. \frac{16 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right] \left( A \operatorname{Sin} \left[ \frac{dx}{2} \right] - C \operatorname{Sin} \left[ \frac{dx}{2} \right] \right)}{5 d} + \frac{1}{105 d} \right. \\
8 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right]^3 \left( 41 A \operatorname{Sin} \left[ \frac{dx}{2} \right] + 15 B \operatorname{Sin} \left[ \frac{dx}{2} \right] - C \operatorname{Sin} \left[ \frac{dx}{2} \right] \right) + \\
\left. \frac{4 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right]^7 \left( A \operatorname{Sin} \left[ \frac{dx}{2} \right] - B \operatorname{Sin} \left[ \frac{dx}{2} \right] + C \operatorname{Sin} \left[ \frac{dx}{2} \right] \right)}{7 d} + \right. \\
\left. \frac{8 (41 A + 15 B - C) \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \operatorname{Tan} \left[ \frac{c}{2} \right]}{105 d} - \right. \\
\left. \frac{8 (12 A - 5 B - 2 C) \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 \operatorname{Tan} \left[ \frac{c}{2} \right]}{35 d} + \frac{4 (A - B + C) \operatorname{Sec} \left[ \frac{c}{2} + \frac{dx}{2} \right]^6 \operatorname{Tan} \left[ \frac{c}{2} \right]}{7 d} \right) \Bigg/ \\
\left( \cos [c + dx]^{3/2} (A + 2 C + 2 B \cos [c + dx] + A \cos [2 c + 2 dx]) (a + a \sec [c + dx])^4 \right)$$

**Problem 1243: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec [c + dx] + C \sec [c + dx]^2}{\cos [c + dx]^{5/2} (a + a \sec [c + dx])^4} dx$$

Optimal (type 4, 234 leaves, 8 steps):

$$\frac{(B + 8 C) \operatorname{EllipticE} \left[ \frac{1}{2} (c + dx), 2 \right]}{10 a^4 d} + \frac{(3 A + 4 B + 17 C) \operatorname{EllipticF} \left[ \frac{1}{2} (c + dx), 2 \right]}{42 a^4 d} + \\
\frac{(15 A - B - 83 C) \sqrt{\cos [c + dx]} \operatorname{Sin} [c + dx]}{210 a^4 d (1 + \cos [c + dx])^2} - \frac{(B + 8 C) \sqrt{\cos [c + dx]} \operatorname{Sin} [c + dx]}{10 a^4 d (1 + \cos [c + dx])} - \\
\frac{(A - B + C) \sqrt{\cos [c + dx]} \operatorname{Sin} [c + dx]}{7 d (a + a \cos [c + dx])^4} + \frac{(5 A + 2 B - 9 C) \sqrt{\cos [c + dx]} \operatorname{Sin} [c + dx]}{35 a d (a + a \cos [c + dx])^3}$$

Result (type 5, 1862 leaves):

$$\frac{1}{5 (A + 2 C + 2 B \cos [c + dx] + A \cos [2 c + 2 dx]) (a + a \sec [c + dx])^4} \\
2 i B \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^8 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} [c + dx]^2 (A + B \sec [c + dx] + C \sec [c + dx]^2) \\
\left( \left( 2 e^{2 i dx} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i dx} (\cos [c] + i \operatorname{Sin} [c])^2 \right] \right. \right. \\
\left. \left. \sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \cos [c] + 2 i (-1 + e^{2 i dx}) \operatorname{Sin} [c])} \right) \right)$$

$$\begin{aligned}
 & \left( \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \\
 & \left( 3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c] \right) - \\
 & \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \\
 & \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \right. \\
 & \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \\
 & \left( -i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c] \right) + \\
 & \frac{1}{5 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^4} \\
 & 16 i C \\
 & \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 \operatorname{Csc} \left[ \frac{c}{2} \right] \\
 & \sec \left[ \frac{c}{2} \right] \sec [c + d x]^2 \\
 & (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \right. \\
 & \left. \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \right. \right. \\
 & \left. \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \right. \\
 & \left. \left( 3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c] \right) - \right. \\
 & \left. \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \right. \\
 & \left. \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \right. \right. \\
 & \left. \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \right. \\
 & \left. \left( -i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c] \right) \right) - \\
 & \left( 8 A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \right]^2 \right) \\
 & \sec \left[ \frac{c}{2} \right] \sec [c + d x]^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \sec [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \\
 & \sqrt{-\sqrt{1 + \operatorname{Cot} [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \\
 & \left. \sqrt{1 + \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \right) / \\
 & \left( 7 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \operatorname{Cot} [c]^2} (a + a \sec [c + d x])^4 \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \left( 32 B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^8 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin\left[dx - \operatorname{ArcTan}\left[\operatorname{Cot}[c]\right]\right]^2\right] \right. \\
 & \quad \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c + dx]^2 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \\
 & \quad \operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \quad \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1 + \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) / \\
 & (21 d (A + 2 C + 2 B \cos[c + dx] + A \cos[2c + 2 dx]) \sqrt{1 + \operatorname{Cot}[c]^2} (a + a \operatorname{Sec}[c + dx])^4) - \\
 & \left( 136 C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^8 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin\left[dx - \operatorname{ArcTan}\left[\operatorname{Cot}[c]\right]\right]^2\right] \right. \\
 & \quad \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c + dx]^2 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \\
 & \quad \operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \quad \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1 + \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) / \\
 & (21 d (A + 2 C + 2 B \cos[c + dx] + A \cos[2c + 2 dx]) \sqrt{1 + \operatorname{Cot}[c]^2} (a + a \operatorname{Sec}[c + dx])^4) + \\
 & \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \left( -\frac{16 (B + 8 C) \operatorname{Csc}[c]}{5 d} + \frac{1}{105 d} \right. \right. \\
 & \quad 8 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 \left( 15 A \sin\left[\frac{dx}{2}\right] - B \sin\left[\frac{dx}{2}\right] - 83 C \sin\left[\frac{dx}{2}\right] \right) + \\
 & \quad \frac{1}{35 d} 8 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^5 \left( 5 A \sin\left[\frac{dx}{2}\right] + 2 B \sin\left[\frac{dx}{2}\right] - 9 C \sin\left[\frac{dx}{2}\right] \right) - \\
 & \quad \left. \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^7 (A \sin\left[\frac{dx}{2}\right] - B \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right])}{7 d} \right. \\
 & \quad \left. \frac{16 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] (B \sin\left[\frac{dx}{2}\right] + 8 C \sin\left[\frac{dx}{2}\right])}{5 d} + \frac{8 (15 A - B - 83 C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Tan}\left[\frac{c}{2}\right]}{105 d} \right. \\
 & \quad \left. \left. \frac{8 (5 A + 2 B - 9 C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Tan}\left[\frac{c}{2}\right]}{35 d} - \frac{4 (A - B + C) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Tan}\left[\frac{c}{2}\right]}{7 d} \right) \right) / \\
 & (\cos[c + dx]^{3/2} (A + 2 C + 2 B \cos[c + dx] + A \cos[2c + 2 dx]) (a + a \operatorname{Sec}[c + dx])^4)
 \end{aligned}$$

**Problem 1244: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2}{\cos[c + dx]^{7/2} (a + a \operatorname{Sec}[c + dx])^4} dx$$



Optimal (type 4, 276 leaves, 9 steps):

$$\frac{(A+8B-57C) \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{10a^4d} + \frac{(4A+17B-108C) \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{42a^4d} - \frac{(A+8B-57C) \operatorname{Sin}[c+dx]}{10a^4d\sqrt{\operatorname{Cos}[c+dx]}} + \frac{(13A+29B-141C) \operatorname{Sin}[c+dx]}{210a^4d\sqrt{\operatorname{Cos}[c+dx]}(1+\operatorname{Cos}[c+dx])^2} + \frac{(4A+17B-108C) \operatorname{Sin}[c+dx]}{42a^4d\sqrt{\operatorname{Cos}[c+dx]}(1+\operatorname{Cos}[c+dx])} - \frac{(A-B+C) \operatorname{Sin}[c+dx]}{7d\sqrt{\operatorname{Cos}[c+dx]}(a+a\operatorname{Cos}[c+dx])^4} + \frac{(3A+4B-11C) \operatorname{Sin}[c+dx]}{35ad\sqrt{\operatorname{Cos}[c+dx]}(a+a\operatorname{Cos}[c+dx])^3}$$

Result (type 5, 2316 leaves):

$$\frac{1}{5(A+2C+2B\operatorname{Cos}[c+dx]+A\operatorname{Cos}[2c+2dx])(a+a\operatorname{Sec}[c+dx])^4} + \frac{2iA\operatorname{Cos}\left[\frac{c}{2}+\frac{dx}{2}\right]^8 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^2 (A+B\operatorname{Sec}[c+dx]+C\operatorname{Sec}[c+dx]^2)}{\left(\left(2e^{2ix}\operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix}(\operatorname{Cos}[c]+i\operatorname{Sin}[c])^2\right]\right.\right. \\ \left.\left.\sqrt{e^{-ix}(2(1+e^{2ix})\operatorname{Cos}[c]+2i(-1+e^{2ix})\operatorname{Sin}[c])}\right.}\right. \\ \left.\left.\sqrt{1+e^{2ix}\operatorname{Cos}[2c]+ie^{2ix}\operatorname{Sin}[2c]}\right)\right) / \\ (3id(1+e^{2ix})\operatorname{Cos}[c]-3d(-1+e^{2ix})\operatorname{Sin}[c]) - \\ \left(2\operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix}(\operatorname{Cos}[c]+i\operatorname{Sin}[c])^2\right]\right. \\ \left.\sqrt{e^{-ix}(2(1+e^{2ix})\operatorname{Cos}[c]+2i(-1+e^{2ix})\operatorname{Sin}[c])}\right.}\right. \\ \left.\left.\sqrt{1+e^{2ix}\operatorname{Cos}[2c]+ie^{2ix}\operatorname{Sin}[2c]}\right)\right) / \\ \left.(-id(1+e^{2ix})\operatorname{Cos}[c]+d(-1+e^{2ix})\operatorname{Sin}[c])\right) + \frac{1}{5(A+2C+2B\operatorname{Cos}[c+dx]+A\operatorname{Cos}[2c+2dx])(a+a\operatorname{Sec}[c+dx])^4} + \frac{16iB\operatorname{Cos}\left[\frac{c}{2}+\frac{dx}{2}\right]^8 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^2 (A+B\operatorname{Sec}[c+dx]+C\operatorname{Sec}[c+dx]^2)}{\left(\left(2e^{2ix}\operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix}(\operatorname{Cos}[c]+i\operatorname{Sin}[c])^2\right]\right.\right. \\ \left.\left.\sqrt{e^{-ix}(2(1+e^{2ix})\operatorname{Cos}[c]+2i(-1+e^{2ix})\operatorname{Sin}[c])}\right.}\right. \\ \left.\left.\sqrt{1+e^{2ix}\operatorname{Cos}[2c]+ie^{2ix}\operatorname{Sin}[2c]}\right)\right) / \\ (3id(1+e^{2ix})\operatorname{Cos}[c]-3d(-1+e^{2ix})\operatorname{Sin}[c]) -$$

$$\begin{aligned}
 & \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) - \\
 & \quad \frac{1}{5 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a + a \sec [c + d x])^4} \\
 & \quad 114 i C \\
 & \quad \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 \operatorname{Csc} \left[ \frac{c}{2} \right] \\
 & \quad \sec \left[ \frac{c}{2} \right] \sec [c + d x]^2 \\
 & \quad (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \quad \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \quad \left. (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) - \right. \\
 & \quad \left. \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) - \\
 & \quad \left( 32 A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \right]^2 \right) \\
 & \quad \sec \left[ \frac{c}{2} \right] \sec [c + d x]^2 (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \quad \sec [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \\
 & \quad \sqrt{-\sqrt{1 + \operatorname{Cot} [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \\
 & \quad \left. \sqrt{1 + \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]} \right) / \\
 & \quad \left( 21 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \operatorname{Cot} [c]^2} (a + a \sec [c + d x])^4 \right) - \\
 & \quad \left( 136 B \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \right]^2 \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sec\left[\frac{c}{2}\right] \sec[c+dx]^2 (A+B \sec[c+dx] + C \sec[c+dx]^2) \right. \\
 & \left. \sec[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \sin[dx - \text{ArcTan}[\text{Cot}[c]]]} \right. \\
 & \left. \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 + \sin[dx - \text{ArcTan}[\text{Cot}[c]]]} \right) / \\
 & \left( 21 d (A + 2 C + 2 B \cos[c+dx] + A \cos[2c+2dx]) \sqrt{1 + \text{Cot}[c]^2} (a + a \sec[c+dx])^4 \right) + \\
 & \left( 288 C \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^8 \text{Csc}\left[\frac{c}{2}\right] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\text{Cot}[c]]]^2\right] \right. \\
 & \left. \sec\left[\frac{c}{2}\right] \sec[c+dx]^2 (A+B \sec[c+dx] + C \sec[c+dx]^2) \right. \\
 & \left. \sec[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \sin[dx - \text{ArcTan}[\text{Cot}[c]]]} \right. \\
 & \left. \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 + \sin[dx - \text{ArcTan}[\text{Cot}[c]]]} \right) / \\
 & \left( 7 d (A + 2 C + 2 B \cos[c+dx] + A \cos[2c+2dx]) \sqrt{1 + \text{Cot}[c]^2} (a + a \sec[c+dx])^4 \right) + \\
 & \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (A+B \sec[c+dx] + C \sec[c+dx]^2) \right. \\
 & \left( \frac{1}{5d} 8 (20C - A \cos[c] - 8B \cos[c] + 37C \cos[c]) \text{Csc}\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right] \sec[c] - \right. \\
 & \frac{1}{105d} 8 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^3 \left( A \sin\left[\frac{dx}{2}\right] + 83B \sin\left[\frac{dx}{2}\right] - 237C \sin\left[\frac{dx}{2}\right] \right) - \\
 & \frac{1}{5d} 16 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right] \left( A \sin\left[\frac{dx}{2}\right] + 8B \sin\left[\frac{dx}{2}\right] - 37C \sin\left[\frac{dx}{2}\right] \right) + \\
 & \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^7 \left( A \sin\left[\frac{dx}{2}\right] - B \sin\left[\frac{dx}{2}\right] + C \sin\left[\frac{dx}{2}\right] \right)}{7d} + \frac{1}{35d} \\
 & 8 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^5 \left( 2A \sin\left[\frac{dx}{2}\right] - 9B \sin\left[\frac{dx}{2}\right] + 16C \sin\left[\frac{dx}{2}\right] \right) + \\
 & \frac{64C \sec[c] \sec[c+dx] \sin[dx]}{d} - \frac{8(A + 83B - 237C) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{105d} + \\
 & \left. \left. \frac{8(2A - 9B + 16C) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \tan\left[\frac{c}{2}\right]}{35d} + \frac{4(A - B + C) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \tan\left[\frac{c}{2}\right]}{7d} \right) \right) / \\
 & \left( \cos[c+dx]^{3/2} (A + 2 C + 2 B \cos[c+dx] + A \cos[2c+2dx]) (a + a \sec[c+dx])^4 \right)
 \end{aligned}$$

**Problem 1248: Result unnecessarily involves higher level functions.**

$$\int \cos[c+dx]^{3/2} \sqrt{a + a \sec[c+dx]} (A+B \sec[c+dx] + C \sec[c+dx]^2) dx$$

Optimal (type 3, 140 leaves, 5 steps):

$$\frac{2 \sqrt{a} C \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right] \sqrt{\operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]}}{d} + \frac{2 a (A+3 B) \operatorname{Sin}[c+d x]}{3 d \sqrt{\operatorname{Cos}[c+d x]} \sqrt{a+a \operatorname{Sec}[c+d x]}} + \frac{2 A \sqrt{\operatorname{Cos}[c+d x]} \sqrt{a+a \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{3 d}$$

Result (type 5, 192 leaves):

$$\left(4 \sqrt{\operatorname{Cos}[c+d x]} (C+B \operatorname{Cos}[c+d x]+A \operatorname{Cos}[c+d x]^2) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right] \sqrt{a(1+\operatorname{Sec}[c+d x])} \left(-3 i C e^{\frac{1}{2} i(c+d x)} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i(c+d x)}\right] - i C e^{\frac{3}{2} i(c+d x)} \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i(c+d x)}\right] + (2 A+3 B+A \operatorname{Cos}[c+d x]) \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)\right) / (3 d (A+2 C+2 B \operatorname{Cos}[c+d x]+A \operatorname{Cos}[2(c+d x)]))$$

**Problem 1249: Result unnecessarily involves higher level functions.**

$$\int \sqrt{\operatorname{Cos}[c+d x]} \sqrt{a+a \operatorname{Sec}[c+d x]} (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) dx$$

Optimal (type 3, 139 leaves, 5 steps):

$$\frac{\sqrt{a} (2 B+C) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right] \sqrt{\operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]}}{d} + \frac{a (2 A-C) \operatorname{Sin}[c+d x]}{d \sqrt{\operatorname{Cos}[c+d x]} \sqrt{a+a \operatorname{Sec}[c+d x]}} + \frac{C \sqrt{a+a \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{d \sqrt{\operatorname{Cos}[c+d x]}}$$

Result (type 5, 209 leaves):

$$\left(2 (C+B \operatorname{Cos}[c+d x]+A \operatorname{Cos}[c+d x]^2) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right] \sqrt{a(1+\operatorname{Sec}[c+d x])} \left(-3 i (2 B+C) e^{\frac{1}{2} i(c+d x)} \operatorname{Cos}[c+d x] \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i(c+d x)}\right] - i (2 B+C) e^{\frac{3}{2} i(c+d x)} \operatorname{Cos}[c+d x] \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i(c+d x)}\right] + 3 (C+2 A \operatorname{Cos}[c+d x]) \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)\right) / (3 d \sqrt{\operatorname{Cos}[c+d x]} (A+2 C+2 B \operatorname{Cos}[c+d x]+A \operatorname{Cos}[2(c+d x)]))$$

**Problem 1250: Result unnecessarily involves higher level functions.**

$$\int \frac{\sqrt{a+a \operatorname{Sec}[c+d x]} (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2)}{\sqrt{\operatorname{Cos}[c+d x]}} dx$$

Optimal (type 3, 151 leaves, 5 steps):

$$\frac{1}{4d} \sqrt{a} (8A+4B+3C) \operatorname{ArcSinh} \left[ \frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}} \right] \sqrt{\operatorname{Cos}[c+dx]} \sqrt{\operatorname{Sec}[c+dx]} +$$

$$\frac{a(4B+C) \operatorname{Sin}[c+dx]}{4d \operatorname{Cos}[c+dx]^{3/2} \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{C \sqrt{a+a \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{2d \operatorname{Cos}[c+dx]^{3/2}}$$

Result (type 5, 172 leaves):

$$\frac{1}{12d} \sqrt{\operatorname{Cos}[c+dx]} \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right] \sqrt{a(1+\operatorname{Sec}[c+dx])}$$

$$\left( -3i(8A+4B+3C) e^{\frac{1}{2}i(c+dx)} \operatorname{Hypergeometric2F1} \left[ \frac{1}{4}, 1, \frac{5}{4}, -e^{2i(c+dx)} \right] - \right.$$

$$i(8A+4B+3C) e^{\frac{3}{2}i(c+dx)} \operatorname{Hypergeometric2F1} \left[ \frac{3}{4}, 1, \frac{7}{4}, -e^{2i(c+dx)} \right] +$$

$$\left. 3 \operatorname{Sec}[c+dx] (4B+3C+2C \operatorname{Sec}[c+dx]) \operatorname{Sin} \left[ \frac{1}{2} (c+dx) \right] \right)$$

**Problem 1251: Result unnecessarily involves higher level functions.**

$$\int \frac{\sqrt{a+a \operatorname{Sec}[c+dx]} (A+B \operatorname{Sec}[c+dx]+C \operatorname{Sec}[c+dx]^2)}{\operatorname{Cos}[c+dx]^{3/2}} dx$$

Optimal (type 3, 199 leaves, 6 steps):

$$\frac{1}{8d} \sqrt{a} (8A+6B+5C) \operatorname{ArcSinh} \left[ \frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}} \right] \sqrt{\operatorname{Cos}[c+dx]} \sqrt{\operatorname{Sec}[c+dx]} +$$

$$\frac{a(6B+C) \operatorname{Sin}[c+dx]}{12d \operatorname{Cos}[c+dx]^{5/2} \sqrt{a+a \operatorname{Sec}[c+dx]}} +$$

$$\frac{a(8A+6B+5C) \operatorname{Sin}[c+dx]}{8d \operatorname{Cos}[c+dx]^{3/2} \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{C \sqrt{a+a \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{3d \operatorname{Cos}[c+dx]^{5/2}}$$

Result (type 5, 194 leaves):

$$\frac{1}{24d} \sqrt{\operatorname{Cos}[c+dx]} \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right] \sqrt{a(1+\operatorname{Sec}[c+dx])}$$

$$\left( -3i(8A+6B+5C) e^{\frac{1}{2}i(c+dx)} \operatorname{Hypergeometric2F1} \left[ \frac{1}{4}, 1, \frac{5}{4}, -e^{2i(c+dx)} \right] - \right.$$

$$i(8A+6B+5C) e^{\frac{3}{2}i(c+dx)} \operatorname{Hypergeometric2F1} \left[ \frac{3}{4}, 1, \frac{7}{4}, -e^{2i(c+dx)} \right] +$$

$$\left. \operatorname{Sec}[c+dx] (3(8A+6B+5C) + 2(6B+5C) \operatorname{Sec}[c+dx] + 8C \operatorname{Sec}[c+dx]^2) \operatorname{Sin} \left[ \frac{1}{2} (c+dx) \right] \right)$$

**Problem 1252: Result unnecessarily involves higher level functions.**

$$\int \frac{\sqrt{a+a \operatorname{Sec}[c+dx]} (A+B \operatorname{Sec}[c+dx]+C \operatorname{Sec}[c+dx]^2)}{\operatorname{Cos}[c+dx]^{5/2}} dx$$

Optimal (type 3, 247 leaves, 7 steps):

$$\frac{1}{64 d} \sqrt{a} (48 A + 40 B + 35 C) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c + d x]}{\sqrt{a + a \operatorname{Sec}[c + d x]}}\right] \sqrt{\operatorname{Cos}[c + d x]} \sqrt{\operatorname{Sec}[c + d x]} +$$

$$\frac{a (8 B + C) \operatorname{Sin}[c + d x]}{24 d \operatorname{Cos}[c + d x]^{7/2} \sqrt{a + a \operatorname{Sec}[c + d x]}} + \frac{a (48 A + 40 B + 35 C) \operatorname{Sin}[c + d x]}{96 d \operatorname{Cos}[c + d x]^{5/2} \sqrt{a + a \operatorname{Sec}[c + d x]}} +$$

$$\frac{a (48 A + 40 B + 35 C) \operatorname{Sin}[c + d x]}{64 d \operatorname{Cos}[c + d x]^{3/2} \sqrt{a + a \operatorname{Sec}[c + d x]}} + \frac{C \sqrt{a + a \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{4 d \operatorname{Cos}[c + d x]^{7/2}}$$

Result (type 5, 334 leaves):

$$\frac{1}{128 d} (48 A + 40 B + 35 C) \sqrt{\operatorname{Cos}[c + d x]}$$

$$\left( -2 i e^{\frac{1}{2} i (c + d x)} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i (c + d x)}\right] - \frac{2}{3} i e^{\frac{3}{2} i (c + d x)} \right.$$

$$\left. \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i (c + d x)}\right] \right) \operatorname{Sec}\left[\frac{1}{2} (c + d x)\right] \sqrt{a (1 + \operatorname{Sec}[c + d x])} +$$

$$\frac{1}{d} \sqrt{\operatorname{Cos}[c + d x]} \operatorname{Sec}\left[\frac{1}{2} (c + d x)\right] \sqrt{a (1 + \operatorname{Sec}[c + d x])} \left( \frac{1}{4} C \operatorname{Sec}[c + d x]^4 \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right] \right) +$$

$$\frac{1}{24} \operatorname{Sec}[c + d x]^3 \left( 8 B \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right] + 7 C \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right] \right) +$$

$$\frac{1}{64} \operatorname{Sec}[c + d x] \left( 48 A \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right] + 40 B \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right] + 35 C \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right] \right) +$$

$$\frac{1}{96} \operatorname{Sec}[c + d x]^2 \left( 48 A \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right] + 40 B \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right] + 35 C \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right] \right)$$

### Problem 1256: Result unnecessarily involves higher level functions.

$$\int \operatorname{Cos}[c + d x]^{5/2} (a + a \operatorname{Sec}[c + d x])^{3/2} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 3, 192 leaves, 6 steps):

$$\frac{2 a^{3/2} C \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c + d x]}{\sqrt{a + a \operatorname{Sec}[c + d x]}}\right] \sqrt{\operatorname{Cos}[c + d x]} \sqrt{\operatorname{Sec}[c + d x]}}{d} +$$

$$\frac{2 a^2 (12 A + 20 B + 15 C) \operatorname{Sin}[c + d x]}{15 d \sqrt{\operatorname{Cos}[c + d x]} \sqrt{a + a \operatorname{Sec}[c + d x]}} +$$

$$\frac{2 a (3 A + 5 B) \sqrt{\operatorname{Cos}[c + d x]} \sqrt{a + a \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{15 d} +$$

$$\frac{2 A \operatorname{Cos}[c + d x]^{3/2} (a + a \operatorname{Sec}[c + d x])^{3/2} \operatorname{Sin}[c + d x]}{5 d}$$

Result (type 5, 224 leaves):

$$\frac{1}{15 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 (c + d x)])}$$

$$a \sqrt{\cos [c + d x]} (1 + \cos [c + d x]) (C + B \cos [c + d x] + A \cos [c + d x]^2) \sec \left[ \frac{1}{2} (c + d x) \right]^3$$

$$\sqrt{a (1 + \sec [c + d x])} \left( -30 i C e^{\frac{1}{2} i (c + d x)} \operatorname{Hypergeometric2F1} \left[ \frac{1}{4}, 1, \frac{5}{4}, -e^{2 i (c + d x)} \right] - \right.$$

$$10 i C e^{\frac{3}{2} i (c + d x)} \operatorname{Hypergeometric2F1} \left[ \frac{3}{4}, 1, \frac{7}{4}, -e^{2 i (c + d x)} \right] +$$

$$\left. (39 A + 50 B + 30 C + 2 (9 A + 5 B) \cos [c + d x] + 3 A \cos [2 (c + d x)]) \sin \left[ \frac{1}{2} (c + d x) \right] \right)$$

**Problem 1257: Result unnecessarily involves higher level functions.**

$$\int \cos [c + d x]^{3/2} (a + a \sec [c + d x])^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 3, 197 leaves, 6 steps):

$$\frac{a^{3/2} (2 B + 3 C) \operatorname{ArcSinh} \left[ \frac{\sqrt{a} \tan [c + d x]}{\sqrt{a + a \sec [c + d x]}} \right] \sqrt{\cos [c + d x]} \sqrt{\sec [c + d x]}}{d} +$$

$$\frac{a^2 (8 A + 6 B - 3 C) \sin [c + d x]}{3 d \sqrt{\cos [c + d x]} \sqrt{a + a \sec [c + d x]}} - \frac{a (2 A - 3 C) \sqrt{a + a \sec [c + d x]} \sin [c + d x]}{3 d \sqrt{\cos [c + d x]}} +$$

$$\frac{2 A \sqrt{\cos [c + d x]} (a + a \sec [c + d x])^{3/2} \sin [c + d x]}{3 d}$$

Result (type 5, 242 leaves):

$$\frac{1}{3 d \sqrt{\cos [c + d x]} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 (c + d x)])}$$

$$a (1 + \cos [c + d x]) (C + B \cos [c + d x] + A \cos [c + d x]^2) \sec \left[ \frac{1}{2} (c + d x) \right]^3 \sqrt{a (1 + \sec [c + d x])}$$

$$\left( -3 i (2 B + 3 C) e^{\frac{1}{2} i (c + d x)} \cos [c + d x] \operatorname{Hypergeometric2F1} \left[ \frac{1}{4}, 1, \frac{5}{4}, -e^{2 i (c + d x)} \right] - \right.$$

$$i (2 B + 3 C) e^{\frac{3}{2} i (c + d x)} \cos [c + d x] \operatorname{Hypergeometric2F1} \left[ \frac{3}{4}, 1, \frac{7}{4}, -e^{2 i (c + d x)} \right] +$$

$$\left. (A + 3 C + 2 (5 A + 3 B) \cos [c + d x] + A \cos [2 (c + d x)]) \sin \left[ \frac{1}{2} (c + d x) \right] \right)$$

**Problem 1258: Result unnecessarily involves higher level functions.**

$$\int \sqrt{\cos [c + d x]} (a + a \sec [c + d x])^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 3, 203 leaves, 6 steps):

$$\frac{1}{4d} a^{3/2} (8A + 12B + 7C) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c + dx]}{\sqrt{a + a \operatorname{Sec}[c + dx]}}\right] \sqrt{\operatorname{Cos}[c + dx]} \sqrt{\operatorname{Sec}[c + dx]} +$$

$$\frac{a^2 (8A - 4B - 5C) \operatorname{Sin}[c + dx]}{4d \sqrt{\operatorname{Cos}[c + dx]} \sqrt{a + a \operatorname{Sec}[c + dx]}} +$$

$$\frac{a (4B + 3C) \sqrt{a + a \operatorname{Sec}[c + dx]} \operatorname{Sin}[c + dx]}{4d \sqrt{\operatorname{Cos}[c + dx]}} + \frac{C (a + a \operatorname{Sec}[c + dx])^{3/2} \operatorname{Sin}[c + dx]}{2d \sqrt{\operatorname{Cos}[c + dx]}}$$

Result (type 5, 256 leaves):

$$\frac{1}{12d \operatorname{Cos}[c + dx]^{3/2} (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2(c + dx)])}$$

$$a (1 + \operatorname{Cos}[c + dx]) (C + B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[c + dx]^2) \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^3 \sqrt{a (1 + \operatorname{Sec}[c + dx])}$$

$$\left(-3i (8A + 12B + 7C) e^{\frac{1}{2}i(c+dx)} \operatorname{Cos}[c + dx]^2 \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2i(c+dx)}\right] -\right.$$

$$i (8A + 12B + 7C) e^{\frac{3}{2}i(c+dx)} \operatorname{Cos}[c + dx]^2 \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2i(c+dx)}\right] +$$

$$\left.3 ((4B + 7C) \operatorname{Cos}[c + dx] + 2(2A + C + 2A \operatorname{Cos}[2(c + dx)])) \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right)$$

**Problem 1259: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + a \operatorname{Sec}[c + dx])^{3/2} (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2)}{\sqrt{\operatorname{Cos}[c + dx]}} dx$$

Optimal (type 3, 201 leaves, 6 steps):

$$\frac{1}{8d} a^{3/2} (24A + 14B + 11C) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c + dx]}{\sqrt{a + a \operatorname{Sec}[c + dx]}}\right] \sqrt{\operatorname{Cos}[c + dx]} \sqrt{\operatorname{Sec}[c + dx]} +$$

$$\frac{a^2 (24A + 30B + 19C) \operatorname{Sin}[c + dx]}{24d \operatorname{Cos}[c + dx]^{3/2} \sqrt{a + a \operatorname{Sec}[c + dx]}} +$$

$$\frac{a (2B + C) \sqrt{a + a \operatorname{Sec}[c + dx]} \operatorname{Sin}[c + dx]}{4d \operatorname{Cos}[c + dx]^{3/2}} + \frac{C (a + a \operatorname{Sec}[c + dx])^{3/2} \operatorname{Sin}[c + dx]}{3d \operatorname{Cos}[c + dx]^{3/2}}$$

Result (type 5, 261 leaves):

$$\frac{1}{24d \operatorname{Cos}[c + dx]^{5/2} (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2(c + dx)])}$$

$$a (1 + \operatorname{Cos}[c + dx]) (C + B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[c + dx]^2) \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^3 \sqrt{a (1 + \operatorname{Sec}[c + dx])}$$

$$\left(-3i (24A + 14B + 11C) e^{\frac{1}{2}i(c+dx)} \operatorname{Cos}[c + dx]^3 \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2i(c+dx)}\right] -\right.$$

$$i (24A + 14B + 11C) e^{\frac{3}{2}i(c+dx)} \operatorname{Cos}[c + dx]^3 \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2i(c+dx)}\right] +$$

$$\left. (8C + 2(6B + 11C) \operatorname{Cos}[c + dx] + 3(8A + 14B + 11C) \operatorname{Cos}[c + dx]^2) \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right)$$



### Problem 1260: Result unnecessarily involves higher level functions.

$$\int \frac{(a + a \sec [c + d x])^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\cos [c + d x]^{3/2}} dx$$

Optimal (type 3, 253 leaves, 7 steps):

$$\begin{aligned} & \frac{1}{64 d} a^{3/2} (112 A + 88 B + 75 C) \operatorname{ArcSinh} \left[ \frac{\sqrt{a} \tan [c + d x]}{\sqrt{a + a \sec [c + d x]}} \right] \sqrt{\cos [c + d x]} \sqrt{\sec [c + d x]} + \\ & \frac{a^2 (48 A + 56 B + 39 C) \sin [c + d x]}{96 d \cos [c + d x]^{5/2} \sqrt{a + a \sec [c + d x]}} + \frac{a^2 (112 A + 88 B + 75 C) \sin [c + d x]}{64 d \cos [c + d x]^{3/2} \sqrt{a + a \sec [c + d x]}} + \\ & \frac{a (8 B + 3 C) \sqrt{a + a \sec [c + d x]} \sin [c + d x]}{24 d \cos [c + d x]^{5/2}} + \frac{C (a + a \sec [c + d x])^{3/2} \sin [c + d x]}{4 d \cos [c + d x]^{5/2}} \end{aligned}$$

Result (type 5, 281 leaves):

$$\begin{aligned} & \frac{1}{192 d \cos [c + d x]^{7/2} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 (c + d x)])} \\ & a (1 + \cos [c + d x]) (C + B \cos [c + d x] + A \cos [c + d x]^2) \sec \left[ \frac{1}{2} (c + d x) \right]^3 \sqrt{a (1 + \sec [c + d x])} \\ & \left( -3 i (112 A + 88 B + 75 C) e^{\frac{1}{2} i (c + d x)} \cos [c + d x]^4 \operatorname{Hypergeometric2F1} \left[ \frac{1}{4}, 1, \frac{5}{4}, -e^{2 i (c + d x)} \right] - \right. \\ & \quad \left. i (112 A + 88 B + 75 C) e^{\frac{3}{2} i (c + d x)} \cos [c + d x]^4 \operatorname{Hypergeometric2F1} \left[ \frac{3}{4}, 1, \frac{7}{4}, -e^{2 i (c + d x)} \right] + \right. \\ & \quad \left. (48 C + 8 (8 B + 15 C) \cos [c + d x] + 2 (48 A + 88 B + 75 C) \cos [c + d x]^2 + \right. \\ & \quad \left. 3 (112 A + 88 B + 75 C) \cos [c + d x]^3) \sin \left[ \frac{1}{2} (c + d x) \right] \right) \end{aligned}$$

### Problem 1261: Result unnecessarily involves higher level functions.

$$\int \frac{(a + a \sec [c + d x])^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\cos [c + d x]^{5/2}} dx$$

Optimal (type 3, 303 leaves, 8 steps):

$$\begin{aligned} & \frac{1}{128 d} a^{3/2} (176 A + 150 B + 133 C) \operatorname{ArcSinh} \left[ \frac{\sqrt{a} \tan [c + d x]}{\sqrt{a + a \sec [c + d x]}} \right] \sqrt{\cos [c + d x]} \sqrt{\sec [c + d x]} + \\ & \frac{a^2 (80 A + 90 B + 67 C) \sin [c + d x]}{240 d \cos [c + d x]^{7/2} \sqrt{a + a \sec [c + d x]}} + \\ & \frac{a^2 (176 A + 150 B + 133 C) \sin [c + d x]}{192 d \cos [c + d x]^{5/2} \sqrt{a + a \sec [c + d x]}} + \frac{a^2 (176 A + 150 B + 133 C) \sin [c + d x]}{128 d \cos [c + d x]^{3/2} \sqrt{a + a \sec [c + d x]}} + \\ & \frac{a (10 B + 3 C) \sqrt{a + a \sec [c + d x]} \sin [c + d x]}{40 d \cos [c + d x]^{7/2}} + \frac{C (a + a \sec [c + d x])^{3/2} \sin [c + d x]}{5 d \cos [c + d x]^{7/2}} \end{aligned}$$

Result (type 5, 301 leaves):

1

$$\begin{aligned}
 & 1920 d \operatorname{Cos}[c+d x]^{9/2} \left( A+2 C+2 B \operatorname{Cos}[c+d x]+A \operatorname{Cos}\left[2(c+d x)\right]\right) \\
 & a\left(1+\operatorname{Cos}[c+d x]\right)\left(C+B \operatorname{Cos}[c+d x]+A \operatorname{Cos}\left[c+d x\right]^2\right) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^3 \sqrt{a\left(1+\operatorname{Sec}[c+d x]\right)} \\
 & \left(-15 i\left(176 A+150 B+133 C\right) e^{\frac{1}{2} i(c+d x)} \operatorname{Cos}[c+d x]^5 \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4},-e^{2 i(c+d x)}\right]-\right. \\
 & \left.5 i\left(176 A+150 B+133 C\right) e^{\frac{3}{2} i(c+d x)} \operatorname{Cos}[c+d x]^5 \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4},-e^{2 i(c+d x)}\right]+ \right. \\
 & \left.(384 C+48(10 B+19 C) \operatorname{Cos}[c+d x]+8(80 A+150 B+133 C) \operatorname{Cos}[c+d x]^2+10(176 A+150 B+ \right. \\
 & \left.133 C) \operatorname{Cos}[c+d x]^3+15(176 A+150 B+133 C) \operatorname{Cos}[c+d x]^4\right) \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\left.\right)
 \end{aligned}$$

**Problem 1265: Result unnecessarily involves higher level functions.**

$$\int \operatorname{Cos}[c+d x]^{7/2}\left(a+a \operatorname{Sec}[c+d x]\right)^{5/2}\left(A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2\right) d x$$

Optimal (type 3, 242 leaves, 7 steps):

$$\begin{aligned}
 & \frac{2 a^{5/2} C \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right] \sqrt{\operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]}}{d} + \\
 & \frac{2 a^3(160 A+224 B+245 C) \operatorname{Sin}[c+d x]}{105 d \sqrt{\operatorname{Cos}[c+d x]} \sqrt{a+a \operatorname{Sec}[c+d x]}} + \frac{1}{105 d} \\
 & \frac{2 a^2(40 A+56 B+35 C) \sqrt{\operatorname{Cos}[c+d x]} \sqrt{a+a \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]+}{35 d} \\
 & \frac{2 a(5 A+7 B) \operatorname{Cos}[c+d x]^{3/2}\left(a+a \operatorname{Sec}[c+d x]\right)^{3/2} \operatorname{Sin}[c+d x]}{7 d} + \\
 & \frac{2 A \operatorname{Cos}[c+d x]^{5/2}\left(a+a \operatorname{Sec}[c+d x]\right)^{5/2} \operatorname{Sin}[c+d x]}{7 d}
 \end{aligned}$$

Result (type 5, 343 leaves):

$$\begin{aligned}
 & \left(C \operatorname{Cos}[c+d x]^{9/2}\left(-2 i e^{\frac{1}{2} i(c+d x)} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4},-e^{2 i(c+d x)}\right]-\right.\right. \\
 & \left.\left.\frac{2}{3} i e^{\frac{3}{2} i(c+d x)} \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4},-e^{2 i(c+d x)}\right]\right)\right. \\
 & \left.\operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^5\left(a\left(1+\operatorname{Sec}[c+d x]\right)\right)^{5/2}\left(A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2\right)\right) / \\
 & \left(2 d\left(A+2 C+2 B \operatorname{Cos}[c+d x]+A \operatorname{Cos}\left[2 c+2 d x\right]\right)+\right. \\
 & \left(\operatorname{Cos}[c+d x]^{9/2} \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^5\left(a\left(1+\operatorname{Sec}[c+d x]\right)\right)^{5/2}\left(A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2\right)\right. \\
 & \left.\left(\frac{5}{8}(3 A+4 B+4 C) \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]+\frac{1}{24}(11 A+10 B+4 C) \operatorname{Sin}\left[\frac{3}{2}(c+d x)\right]+\right.\right. \\
 & \left.\left.\frac{1}{40}(5 A+2 B) \operatorname{Sin}\left[\frac{5}{2}(c+d x)\right]+\frac{1}{56} A \operatorname{Sin}\left[\frac{7}{2}(c+d x)\right]\right)\right) / \\
 & \left(d\left(A+2 C+2 B \operatorname{Cos}[c+d x]+A \operatorname{Cos}\left[2 c+2 d x\right]\right)\right)
 \end{aligned}$$

**Problem 1266: Result unnecessarily involves higher level functions.**

$$\int \cos [c+d x]^{5/2} (a+a \sec [c+d x])^{5/2} (A+B \sec [c+d x]+C \sec [c+d x]^2) dx$$

Optimal (type 3, 243 leaves, 7 steps):

$$\frac{a^{5/2} (2 B+5 C) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \sec [c+d x]}}\right] \sqrt{\cos [c+d x]} \sqrt{\sec [c+d x]}}{d} +$$

$$\frac{a^3 (64 A+70 B+15 C) \sin [c+d x]}{15 d \sqrt{\cos [c+d x]} \sqrt{a+a \sec [c+d x]}} - \frac{a^2 (16 A+10 B-15 C) \sqrt{a+a \sec [c+d x]} \sin [c+d x]}{15 d \sqrt{\cos [c+d x]}} +$$

$$\frac{2 a (A+B) \sqrt{\cos [c+d x]} (a+a \sec [c+d x])^{3/2} \sin [c+d x]}{3 d} +$$

$$\frac{2 A \cos [c+d x]^{3/2} (a+a \sec [c+d x])^{5/2} \sin [c+d x]}{5 d}$$

Result (type 5, 271 leaves):

$$\frac{1}{60 d \sqrt{\cos [c+d x]} (A+2 C+2 B \cos [c+d x]+A \cos [2(c+d x)])}$$

$$a^2 (1+\cos [c+d x])^2 (C+B \cos [c+d x]+A \cos [c+d x]^2) \sec \left[\frac{1}{2}(c+d x)\right]^5 \sqrt{a(1+\sec [c+d x])}$$

$$\left(-30 i(2 B+5 C) e^{\frac{1}{2} i(c+d x)} \cos [c+d x] \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i(c+d x)}\right] -\right.$$

$$\left.10 i(2 B+5 C) e^{\frac{3}{2} i(c+d x)} \cos [c+d x] \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i(c+d x)}\right] +\right.$$

$$(28 A+10 B+30 C+(181 A+160 B+60 C) \cos [c+d x]+$$

$$\left.2(14 A+5 B) \cos [2(c+d x)]+3 A \cos [3(c+d x)]\right) \sin \left[\frac{1}{2}(c+d x)\right]$$

**Problem 1267: Result unnecessarily involves higher level functions.**

$$\int \cos [c+d x]^{3/2} (a+a \sec [c+d x])^{5/2} (A+B \sec [c+d x]+C \sec [c+d x]^2) dx$$

Optimal (type 3, 253 leaves, 7 steps):

$$\frac{1}{4 d} a^{5/2} (8 A+20 B+19 C) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \sec [c+d x]}}\right] \sqrt{\cos [c+d x]} \sqrt{\sec [c+d x]} +$$

$$\frac{a^3 (56 A+12 B-27 C) \sin [c+d x]}{12 d \sqrt{\cos [c+d x]} \sqrt{a+a \sec [c+d x]}} - \frac{a^2 (8 A-12 B-21 C) \sqrt{a+a \sec [c+d x]} \sin [c+d x]}{12 d \sqrt{\cos [c+d x]}}$$

$$\frac{a(4 A-3 C)(a+a \sec [c+d x])^{3/2} \sin [c+d x]}{6 d \sqrt{\cos [c+d x]}} +$$

$$\frac{2 A \sqrt{\cos [c+d x]} (a+a \sec [c+d x])^{5/2} \sin [c+d x]}{3 d}$$

Result (type 5, 282 leaves):

$$\frac{1}{24 d \cos [c+d x]^{3/2} (A+2 C+2 B \cos [c+d x]+A \cos [2(c+d x)])} a^2 (1+\cos [c+d x])^2 (C+B \cos [c+d x]+A \cos [c+d x]^2) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^5 \sqrt{a(1+\operatorname{Sec}[c+d x])} \\ \left(-3 i(8 A+20 B+19 C) e^{\frac{1}{2} i(c+d x)} \cos [c+d x]^2 \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i(c+d x)}\right]-\right. \\ \left. i(8 A+20 B+19 C) e^{\frac{3}{2} i(c+d x)} \cos [c+d x]^2 \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i(c+d x)}\right]+(32 A+12 B+6 C+3(2 A+4 B+11 C) \cos [c+d x]+4(8 A+3 B) \cos [2(c+d x)]+2 A \cos [3(c+d x)]) \sin \left[\frac{1}{2}(c+d x)\right]\right)$$

Problem 1268: Result unnecessarily involves higher level functions.

$$\int \sqrt{\cos [c+d x]} (a+a \operatorname{Sec}[c+d x])^{5/2} (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) dx$$

Optimal (type 3, 253 leaves, 7 steps):

$$\frac{1}{8 d} a^{5/2} (40 A+38 B+25 C) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan [c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right] \sqrt{\cos [c+d x]} \sqrt{\operatorname{Sec}[c+d x]}+ \\ \frac{a^3(24 A-54 B-49 C) \sin [c+d x]}{24 d \sqrt{\cos [c+d x]} \sqrt{a+a \operatorname{Sec}[c+d x]}}+\frac{a^2(24 A+42 B+31 C) \sqrt{a+a \operatorname{Sec}[c+d x]} \sin [c+d x]}{24 d \sqrt{\cos [c+d x]}}+ \\ \frac{a(6 B+5 C)(a+a \operatorname{Sec}[c+d x])^{3/2} \sin [c+d x]}{12 d \sqrt{\cos [c+d x]}}+\frac{C(a+a \operatorname{Sec}[c+d x])^{5/2} \sin [c+d x]}{3 d \sqrt{\cos [c+d x]}}$$

Result (type 5, 276 leaves):

$$\frac{1}{48 d \cos [c+d x]^{5/2} (A+2 C+2 B \cos [c+d x]+A \cos [2(c+d x)])} a^2 (1+\cos [c+d x])^2 (C+B \cos [c+d x]+A \cos [c+d x]^2) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^5 \sqrt{a(1+\operatorname{Sec}[c+d x])} \\ \left(-3 i(40 A+38 B+25 C) e^{\frac{1}{2} i(c+d x)} \cos [c+d x]^3 \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i(c+d x)}\right]-\right. \\ \left. i(40 A+38 B+25 C) e^{\frac{3}{2} i(c+d x)} \cos [c+d x]^3 \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i(c+d x)}\right]+(8 C+2(6 B+17 C) \cos [c+d x]+3(8 A+22 B+25 C) \cos [c+d x]^2+48 A \cos [c+d x]^3) \sin \left[\frac{1}{2}(c+d x)\right]\right)$$

Problem 1269: Result unnecessarily involves higher level functions.

$$\int \frac{(a+a \operatorname{Sec}[c+d x])^{5/2} (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2)}{\sqrt{\cos [c+d x]}} dx$$

Optimal (type 3, 253 leaves, 7 steps):

$$\frac{1}{64 d} a^{5/2} (304 A + 200 B + 163 C) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c + d x]}{\sqrt{a + a \operatorname{Sec}[c + d x]}}\right] \sqrt{\operatorname{Cos}[c + d x]} \sqrt{\operatorname{Sec}[c + d x]} +$$

$$\frac{a^3 (432 A + 392 B + 299 C) \operatorname{Sin}[c + d x]}{192 d \operatorname{Cos}[c + d x]^{3/2} \sqrt{a + a \operatorname{Sec}[c + d x]}} + \frac{a^2 (16 A + 24 B + 17 C) \sqrt{a + a \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{32 d \operatorname{Cos}[c + d x]^{3/2}} +$$

$$\frac{a (8 B + 5 C) (a + a \operatorname{Sec}[c + d x])^{3/2} \operatorname{Sin}[c + d x]}{24 d \operatorname{Cos}[c + d x]^{3/2}} + \frac{C (a + a \operatorname{Sec}[c + d x])^{5/2} \operatorname{Sin}[c + d x]}{4 d \operatorname{Cos}[c + d x]^{3/2}}$$

Result (type 5, 283 leaves):

$$\frac{1}{384 d \operatorname{Cos}[c + d x]^{7/2} (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2(c + d x)])}$$

$$a^2 (1 + \operatorname{Cos}[c + d x])^2 (C + B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[c + d x]^2) \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^5 \sqrt{a (1 + \operatorname{Sec}[c + d x])}$$

$$\left(-3 i (304 A + 200 B + 163 C) e^{\frac{1}{2} i (c + d x)} \operatorname{Cos}[c + d x]^4 \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i (c + d x)}\right] -\right.$$

$$i (304 A + 200 B + 163 C) e^{\frac{3}{2} i (c + d x)} \operatorname{Cos}[c + d x]^4 \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i (c + d x)}\right] +$$

$$(48 C + 8 (8 B + 23 C) \operatorname{Cos}[c + d x] + (96 A + 272 B + 326 C) \operatorname{Cos}[c + d x]^2 +$$

$$\left.(528 A + 600 B + 489 C) \operatorname{Cos}[c + d x]^3\right) \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]$$

**Problem 1270: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + a \operatorname{Sec}[c + d x])^{5/2} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Cos}[c + d x]^{3/2}} dx$$

Optimal (type 3, 301 leaves, 8 steps):

$$\frac{1}{128 d} a^{5/2} (400 A + 326 B + 283 C) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c + d x]}{\sqrt{a + a \operatorname{Sec}[c + d x]}}\right] \sqrt{\operatorname{Cos}[c + d x]} \sqrt{\operatorname{Sec}[c + d x]} +$$

$$\frac{a^3 (1040 A + 950 B + 787 C) \operatorname{Sin}[c + d x]}{960 d \operatorname{Cos}[c + d x]^{5/2} \sqrt{a + a \operatorname{Sec}[c + d x]}} + \frac{a^3 (400 A + 326 B + 283 C) \operatorname{Sin}[c + d x]}{128 d \operatorname{Cos}[c + d x]^{3/2} \sqrt{a + a \operatorname{Sec}[c + d x]}} +$$

$$\frac{a^2 (80 A + 110 B + 79 C) \sqrt{a + a \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{240 d \operatorname{Cos}[c + d x]^{5/2}} +$$

$$\frac{a (2 B + C) (a + a \operatorname{Sec}[c + d x])^{3/2} \operatorname{Sin}[c + d x]}{8 d \operatorname{Cos}[c + d x]^{5/2}} + \frac{C (a + a \operatorname{Sec}[c + d x])^{5/2} \operatorname{Sin}[c + d x]}{5 d \operatorname{Cos}[c + d x]^{5/2}}$$

Result (type 5, 305 leaves):

1

$$\begin{aligned}
 & 3840 d \cos [c+d x]^{9/2} (A+2 C+2 B \cos [c+d x]+A \cos [2(c+d x)]) \\
 & a^2 (1+\cos [c+d x])^2 (C+B \cos [c+d x]+A \cos [c+d x]^2) \sec \left[\frac{1}{2}(c+d x)\right]^5 \sqrt{a(1+\sec [c+d x])} \\
 & \left(-15 i(400 A+326 B+283 C) e^{\frac{1}{2} i(c+d x)} \cos [c+d x]^5 \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i(c+d x)}\right]-\right. \\
 & \left.5 i(400 A+326 B+283 C) e^{\frac{3}{2} i(c+d x)} \cos [c+d x]^5 \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i(c+d x)}\right]+ \right. \\
 & \left.(384 C+48(10 B+29 C) \cos [c+d x]+8(80 A+230 B+283 C) \cos [c+d x]^2+10(272 A+326 B+ \right. \\
 & \left.283 C) \cos [c+d x]^3+15(400 A+326 B+283 C) \cos [c+d x]^4) \sin \left[\frac{1}{2}(c+d x)\right]\right)
 \end{aligned}$$

**Problem 1271: Result unnecessarily involves higher level functions.**

$$\int \frac{(a+a \sec [c+d x])^{5/2} (A+B \sec [c+d x]+C \sec [c+d x]^2)}{\cos [c+d x]^{5/2}} dx$$

Optimal (type 3, 353 leaves, 9 steps):

$$\begin{aligned}
 & \frac{1}{512 d} a^{5/2} (1304 A+1132 B+1015 C) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan [c+d x]}{\sqrt{a+a \sec [c+d x]}}\right] \sqrt{\cos [c+d x]} \sqrt{\sec [c+d x]}+ \\
 & \frac{a^3(680 A+628 B+545 C) \sin [c+d x]}{960 d \cos [c+d x]^{7/2} \sqrt{a+a \sec [c+d x]}}+\frac{a^3(1304 A+1132 B+1015 C) \sin [c+d x]}{768 d \cos [c+d x]^{5/2} \sqrt{a+a \sec [c+d x]}}+ \\
 & \frac{a^3(1304 A+1132 B+1015 C) \sin [c+d x]}{512 d \cos [c+d x]^{3/2} \sqrt{a+a \sec [c+d x]}}+ \\
 & \frac{a^2(120 A+156 B+115 C) \sqrt{a+a \sec [c+d x]} \sin [c+d x]}{480 d \cos [c+d x]^{7/2}}+ \\
 & \frac{a(12 B+5 C)(a+a \sec [c+d x])^{3/2} \sin [c+d x]}{60 d \cos [c+d x]^{7/2}}+\frac{C(a+a \sec [c+d x])^{5/2} \sin [c+d x]}{6 d \cos [c+d x]^{7/2}}
 \end{aligned}$$

Result (type 5, 536 leaves):

$$\begin{aligned}
 & \left( (1304 A + 1132 B + 1015 C) \cos [c + d x]^{9/2} \right. \\
 & \quad \left( -2 i e^{\frac{1}{2} i (c+d x)} \operatorname{Hypergeometric2F1} \left[ \frac{1}{4}, 1, \frac{5}{4}, -e^{2 i (c+d x)} \right] - \right. \\
 & \quad \left. \frac{2}{3} i e^{\frac{3}{2} i (c+d x)} \operatorname{Hypergeometric2F1} \left[ \frac{3}{4}, 1, \frac{7}{4}, -e^{2 i (c+d x)} \right] \right) \\
 & \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^5 (a (1 + \operatorname{Sec} [c + d x]))^{5/2} (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) \right) / \\
 & (2048 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) + \\
 & \frac{1}{d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])} \\
 & \cos [c + d x]^{9/2} \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^5 (a (1 + \operatorname{Sec} [c + d x]))^{5/2} \\
 & (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) \left( \frac{1}{12} C \operatorname{Sec} [c + d x]^6 \sin \left[ \frac{1}{2} (c + d x) \right] + \right. \\
 & \quad \frac{1}{120} \operatorname{Sec} [c + d x]^5 \left( 12 B \sin \left[ \frac{1}{2} (c + d x) \right] + 35 C \sin \left[ \frac{1}{2} (c + d x) \right] \right) + \frac{1}{320} \operatorname{Sec} [c + d x]^4 \\
 & \quad \left( 40 A \sin \left[ \frac{1}{2} (c + d x) \right] + 116 B \sin \left[ \frac{1}{2} (c + d x) \right] + 145 C \sin \left[ \frac{1}{2} (c + d x) \right] \right) + \frac{1}{1920} \operatorname{Sec} [c + d x]^3 \\
 & \quad \left( 920 A \sin \left[ \frac{1}{2} (c + d x) \right] + 1132 B \sin \left[ \frac{1}{2} (c + d x) \right] + 1015 C \sin \left[ \frac{1}{2} (c + d x) \right] \right) + \frac{1}{1024} \operatorname{Sec} [ \\
 & \quad c + d x] \left( 1304 A \sin \left[ \frac{1}{2} (c + d x) \right] + 1132 B \sin \left[ \frac{1}{2} (c + d x) \right] + 1015 C \sin \left[ \frac{1}{2} (c + d x) \right] \right) + \frac{1}{1536} \\
 & \quad \left. \operatorname{Sec} [c + d x]^2 \left( 1304 A \sin \left[ \frac{1}{2} (c + d x) \right] + 1132 B \sin \left[ \frac{1}{2} (c + d x) \right] + 1015 C \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right)
 \end{aligned}$$

**Problem 1275: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\cos [c + d x]} (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2)}{\sqrt{a + a \operatorname{Sec} [c + d x]}} dx$$

Optimal (type 3, 178 leaves, 7 steps):

$$\begin{aligned}
 & \frac{2 C \operatorname{ArcSinh} \left[ \frac{\sqrt{a} \operatorname{Tan} [c + d x]}{\sqrt{a + a \operatorname{Sec} [c + d x]}} \right] \sqrt{\cos [c + d x]} \sqrt{\operatorname{Sec} [c + d x]}}{\sqrt{a} d} - \frac{1}{\sqrt{a} d} \\
 & \frac{\sqrt{2} (A - B + C) \operatorname{ArcTanh} \left[ \frac{\sqrt{a} \sqrt{\operatorname{Sec} [c + d x]} \sin [c + d x]}{\sqrt{2} \sqrt{a + a \operatorname{Sec} [c + d x]}} \right] \sqrt{\cos [c + d x]} \sqrt{\operatorname{Sec} [c + d x]} +}{d \sqrt{\cos [c + d x]} \sqrt{a + a \operatorname{Sec} [c + d x]}} \\
 & \frac{2 A \sin [c + d x]}{d \sqrt{\cos [c + d x]} \sqrt{a + a \operatorname{Sec} [c + d x]}}
 \end{aligned}$$

Result (type 3, 388 leaves):

$$\frac{1}{2 d \sqrt{\cos [c+d x]} \sqrt{a(1+\sec [c+d x])} \sqrt{\sin [c+d x]^2}}$$

$$\sin [c+d x] \left( 2 \sqrt{2} (A-B) \sqrt{1+\cos [c+d x]} \log [1+\cos [c+d x]] - 4 C \sqrt{1+\cos [c+d x]} \right.$$

$$\log [\sqrt{\cos [c+d x]} (1+\cos [c+d x])] + \sqrt{2} C \sqrt{1+\cos [c+d x]} \log [(1+\cos [c+d x])^2] -$$

$$2 \sqrt{2} A \sqrt{1+\cos [c+d x]} \log [2 \sqrt{1+\cos [c+d x]} + \sqrt{2-2 \cos [c+d x]^2}] +$$

$$2 \sqrt{2} B \sqrt{1+\cos [c+d x]} \log [2 \sqrt{1+\cos [c+d x]} + \sqrt{2-2 \cos [c+d x]^2}] +$$

$$4 C \sqrt{1+\cos [c+d x]} \log [1+\cos [c+d x] + \sqrt{1+\cos [c+d x]} \sqrt{\sin [c+d x]^2}] -$$

$$\sqrt{2} C \sqrt{1+\cos [c+d x]} \log [3+2 \cos [c+d x] - \cos [c+d x]^2] +$$

$$\left. 2 \sqrt{2} \sqrt{1+\cos [c+d x]} \sqrt{\sin [c+d x]^2} + 4 A \sqrt{\sin [c+d x]^2} \right)$$

**Problem 1283: Result more than twice size of optimal antiderivative.**

$$\int \frac{A+B \sec [c+d x]+C \sec [c+d x]^2}{\sqrt{\cos [c+d x]}(a+a \sec [c+d x])^{3/2}} dx$$

Optimal (type 3, 189 leaves, 7 steps):

$$\frac{2 C \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan [c+d x]}{\sqrt{a+a \sec [c+d x]}}\right] \sqrt{\cos [c+d x]} \sqrt{\sec [c+d x]}}{a^{3/2} d} + \frac{1}{2 \sqrt{2} a^{3/2} d}$$

$$\frac{(3 A+B-5 C) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\sec [c+d x]} \sin [c+d x]}{\sqrt{2} \sqrt{a+a \sec [c+d x]}}\right] \sqrt{\cos [c+d x]} \sqrt{\sec [c+d x]} - (A-B+C) \sin [c+d x]}{2 d \cos [c+d x]^{3/2} (a+a \sec [c+d x])^{3/2}}$$

Result (type 3, 572 leaves):



$$\begin{aligned}
 & - \left( \left( 2 \cos \left[ \frac{1}{2} (c + d x) \right] \sqrt{\cos [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \right. \\
 & \quad \left. \left. \left( A \sin \left[ \frac{1}{2} (c + d x) \right] - B \sin \left[ \frac{1}{2} (c + d x) \right] + C \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) / \right. \\
 & \quad \left. \left( d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a (1 + \sec [c + d x]))^{3/2} \right) \right) - \\
 & \left( \sqrt{2} (3 A + B - C) \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\cos [c + d x]} \sqrt{1 + \cos [c + d x]} \right. \\
 & \quad \left. \left( \log [1 + \cos [c + d x]] - \log [2 \sqrt{1 + \cos [c + d x]} + \sqrt{2 - 2 \cos [c + d x]^2}] \right) \right. \\
 & \quad \left. (A + B \sec [c + d x] + C \sec [c + d x]^2) \sin [c + d x] \right) / \\
 & \left( d \sqrt{1 - \cos [c + d x]^2} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a (1 + \sec [c + d x]))^{3/2} \right) - \\
 & \left( 2 C \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\cos [c + d x]} \sqrt{1 + \cos [c + d x]} \right. \\
 & \quad \left( -\sqrt{2} \log [(1 + \cos [c + d x])^2] + 4 \log [\sqrt{\cos [c + d x]} + \cos [c + d x]^{3/2}] - \right. \\
 & \quad 4 \log [1 + \cos [c + d x] + \sqrt{1 + \cos [c + d x]} \sqrt{1 - \cos [c + d x]^2}] + \\
 & \quad \left. \left. \sqrt{2} \log [3 + 2 \cos [c + d x] - \cos [c + d x]^2 + 2 \sqrt{2} \sqrt{1 + \cos [c + d x]} \sqrt{1 - \cos [c + d x]^2}] \right) \right. \\
 & \quad \left. (A + B \sec [c + d x] + C \sec [c + d x]^2) \sin [c + d x] \right) / \\
 & \left( d \sqrt{1 - \cos [c + d x]^2} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a (1 + \sec [c + d x]))^{3/2} \right)
 \end{aligned}$$

### Problem 1289: Result more than twice size of optimal antiderivative.

$$\int \frac{A + B \sec [c + d x] + C \sec [c + d x]^2}{\sqrt{\cos [c + d x]} (a + a \sec [c + d x])^{5/2}} dx$$

Optimal (type 3, 183 leaves, 5 steps):

$$\frac{1}{16 \sqrt{2} a^{5/2} d}$$

$$\frac{(19 A + 5 B + 3 C) \operatorname{ArcTanh} \left[ \frac{\sqrt{a} \sqrt{\sec [c + d x]} \sin [c + d x]}{\sqrt{2} \sqrt{a + a \sec [c + d x]}} \right] \sqrt{\cos [c + d x]} \sqrt{\sec [c + d x]} - (A - B + C) \sin [c + d x]}{4 d \cos [c + d x]^{3/2} (a + a \sec [c + d x])^{5/2}} - \frac{(9 A - B - 7 C) \sin [c + d x]}{16 a d \cos [c + d x]^{3/2} (a + a \sec [c + d x])^{3/2}}$$

Result (type 3, 379 leaves):

$$\begin{aligned} & \left( \cos \left[ \frac{1}{2} (c + d x) \right] \right)^5 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\ & \left( \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right] \right)^4 \left( A \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] - B \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] + C \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] \right) + \\ & \left. \frac{1}{2} \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \left( -13 A \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] + 5 B \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] + 3 C \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] \right) \right) \Bigg) \Bigg) \Bigg) / \\ & \left( d \sqrt{\cos[c + d x]} (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) (a (1 + \operatorname{Sec}[c + d x]))^{5/2} \right) - \\ & \left( (19 A + 5 B + 3 C) \cos \left[ \frac{1}{2} (c + d x) \right]^4 \sqrt{1 + \cos[c + d x]} \right. \\ & \left. \left( \log[1 + \cos[c + d x]] - \log[2 \sqrt{1 + \cos[c + d x]} + \sqrt{2 - 2 \cos[c + d x]^2}] \right) \right) \\ & (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \operatorname{Sin}[c + d x] \Bigg) / \left( 2 \sqrt{2} d \sqrt{\cos[c + d x]} \right. \\ & \left. \sqrt{1 - \cos[c + d x]^2} (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) (a (1 + \operatorname{Sec}[c + d x]))^{5/2} \right) \end{aligned}$$

**Problem 1290: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2}{\cos[c + d x]^{3/2} (a + a \operatorname{Sec}[c + d x])^{5/2}} dx$$

Optimal (type 3, 241 leaves, 8 steps):

$$\begin{aligned} & \frac{2 C \operatorname{ArcSinh} \left[ \frac{\sqrt{a} \operatorname{Tan}[c + d x]}{\sqrt{a + a \operatorname{Sec}[c + d x]}} \right] \sqrt{\cos[c + d x]} \sqrt{\operatorname{Sec}[c + d x]}}{a^{5/2} d} + \frac{1}{16 \sqrt{2} a^{5/2} d} \\ & (5 A + 3 B - 43 C) \operatorname{ArcTanh} \left[ \frac{\sqrt{a} \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{\sqrt{2} \sqrt{a + a \operatorname{Sec}[c + d x]}} \right] \sqrt{\cos[c + d x]} \sqrt{\operatorname{Sec}[c + d x]} - \\ & \frac{(A - B + C) \operatorname{Sin}[c + d x]}{4 d \cos[c + d x]^{5/2} (a + a \operatorname{Sec}[c + d x])^{5/2}} + \frac{(5 A + 3 B - 11 C) \operatorname{Sin}[c + d x]}{16 a d \cos[c + d x]^{3/2} (a + a \operatorname{Sec}[c + d x])^{3/2}} \end{aligned}$$

Result (type 3, 625 leaves):

$$\begin{aligned}
 & \left( \cos \left[ \frac{1}{2} (c + d x) \right] \right)^5 (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \left( \frac{1}{2} \sec \left[ \frac{1}{2} (c + d x) \right] \right)^2 \left( 5 A \sin \left[ \frac{1}{2} (c + d x) \right] + 3 B \sin \left[ \frac{1}{2} (c + d x) \right] - 11 C \sin \left[ \frac{1}{2} (c + d x) \right] \right) + \\
 & \left. \sec \left[ \frac{1}{2} (c + d x) \right] \right)^4 \left( -A \sin \left[ \frac{1}{2} (c + d x) \right] + B \sin \left[ \frac{1}{2} (c + d x) \right] - C \sin \left[ \frac{1}{2} (c + d x) \right] \right) \Bigg) / \\
 & \left( d \sqrt{\cos [c + d x]} (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a (1 + \sec [c + d x]))^{5/2} \right) + \\
 & \left( \cos \left[ \frac{1}{2} (c + d x) \right] \right)^5 \sqrt{\sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \left( - \left( \left( \sqrt{2} (5 A + 3 B - 11 C) \sqrt{\cos [c + d x]} \sqrt{1 + \cos [c + d x]} \right. \right. \right. \\
 & \left. \left. \left( \log [1 + \cos [c + d x]] - \log [2 \sqrt{1 + \cos [c + d x]} + \sqrt{2 - 2 \cos [c + d x]^2}] \right) \right. \right. \\
 & \left. \left. \sec \left[ \frac{1}{2} (c + d x) \right] \sqrt{\sec [c + d x]} \sin [c + d x] \right) / \left( \sqrt{1 - \cos [c + d x]^2} \right) \right) - \\
 & \frac{1}{\sqrt{1 - \cos [c + d x]^2}} 16 C \sqrt{\cos [c + d x]} \sqrt{1 + \cos [c + d x]} \\
 & \left( -\sqrt{2} \log [(1 + \cos [c + d x])^2] + 4 \log [\sqrt{\cos [c + d x]} + \cos [c + d x]^{3/2}] - \right. \\
 & \left. 4 \log [1 + \cos [c + d x] + \sqrt{1 + \cos [c + d x]} \sqrt{1 - \cos [c + d x]^2}] + \right. \\
 & \left. \sqrt{2} \log [3 + 2 \cos [c + d x] - \cos [c + d x]^2 + 2 \sqrt{2} \sqrt{1 + \cos [c + d x]} \sqrt{1 - \cos [c + d x]^2}] \right) \\
 & \left. \sec \left[ \frac{1}{2} (c + d x) \right] \sqrt{\sec [c + d x]} \sin [c + d x] \right) \Bigg) / \\
 & \left( 4 d (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) (a (1 + \sec [c + d x]))^{5/2} \right)
 \end{aligned}$$

**Problem 1291: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec [c + d x] + C \sec [c + d x]^2}{\cos [c + d x]^{5/2} (a + a \sec [c + d x])^{5/2}} dx$$

Optimal (type 3, 294 leaves, 9 steps):

$$\frac{(2B - 5C) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right] \sqrt{\operatorname{Cos}[c+dx]} \sqrt{\operatorname{Sec}[c+dx]}}{a^{5/2} d} + \frac{1}{16 \sqrt{2} a^{5/2} d}$$

$$\frac{(3A - 43B + 115C) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{\sqrt{2} \sqrt{a+a \operatorname{Sec}[c+dx]}}\right] \sqrt{\operatorname{Cos}[c+dx]} \sqrt{\operatorname{Sec}[c+dx]} - \frac{(A - B + C) \operatorname{Sin}[c+dx]}{4 d \operatorname{Cos}[c+dx]^{7/2} (a+a \operatorname{Sec}[c+dx])^{5/2}} + \frac{(A + 7B - 15C) \operatorname{Sin}[c+dx]}{16 a d \operatorname{Cos}[c+dx]^{5/2} (a+a \operatorname{Sec}[c+dx])^{3/2}} + \frac{(3A - 11B + 35C) \operatorname{Sin}[c+dx]}{16 a^2 d \operatorname{Cos}[c+dx]^{3/2} \sqrt{a+a \operatorname{Sec}[c+dx]}}$$

Result (type 3, 651 leaves):

$$\left( \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^5 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \left( 16 C \operatorname{Sec}[c+dx] \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4 \left( A \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] - B \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + C \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) + \frac{1}{2} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left( 3 A \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] - 11 B \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + 19 C \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) /$$

$$\left( d \sqrt{\operatorname{Cos}[c+dx]} (A + 2C + 2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c + 2dx]) (a (1 + \operatorname{Sec}[c+dx]))^{5/2} + \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^5 \sqrt{\operatorname{Sec}[c+dx]} (A + B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right.$$

$$\left. - \left( \left( \sqrt{2} (3A - 11B + 35C) \sqrt{\operatorname{Cos}[c+dx]} \sqrt{1 + \operatorname{Cos}[c+dx]} \left( \operatorname{Log}[1 + \operatorname{Cos}[c+dx]] - \operatorname{Log}\left[2 \sqrt{1 + \operatorname{Cos}[c+dx]} + \sqrt{2 - 2 \operatorname{Cos}[c+dx]^2}\right] \right) \right. \right.$$

$$\left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx] \right) / \left( \sqrt{1 - \operatorname{Cos}[c+dx]^2} \right) - \frac{1}{2 \sqrt{1 - \operatorname{Cos}[c+dx]^2}} (32B - 80C) \sqrt{\operatorname{Cos}[c+dx]} \sqrt{1 + \operatorname{Cos}[c+dx]} \left( -\sqrt{2} \operatorname{Log}\left[(1 + \operatorname{Cos}[c+dx])^2\right] + 4 \operatorname{Log}\left[\sqrt{\operatorname{Cos}[c+dx]} + \operatorname{Cos}[c+dx]^{3/2}\right] - 4 \operatorname{Log}\left[1 + \operatorname{Cos}[c+dx] + \sqrt{1 + \operatorname{Cos}[c+dx]} \sqrt{1 - \operatorname{Cos}[c+dx]^2}\right] + \sqrt{2} \operatorname{Log}\left[3 + 2 \operatorname{Cos}[c+dx] - \operatorname{Cos}[c+dx]^2 + 2 \sqrt{2} \sqrt{1 + \operatorname{Cos}[c+dx]} \sqrt{1 - \operatorname{Cos}[c+dx]^2}\right] \right) \right) /$$

$$\left( 4 d (A + 2C + 2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c + 2dx]) (a (1 + \operatorname{Sec}[c+dx]))^{5/2} \right)$$

**Problem 1294: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c+d x]^{5 / 2} (a+b \sec [c+d x]) (A+B \sec [c+d x]+C \sec [c+d x]^2) d x$$

Optimal (type 4, 116 leaves, 6 steps):

$$\frac{2(3 a A+5 b B+5 a C) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 d}+\frac{2(A b+a B+3 b C) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{3 d}+\frac{2(A b+a B) \sqrt{\cos [c+d x]} \sin [c+d x]}{3 d}+\frac{2 a A \cos [c+d x]^{3 / 2} \sin [c+d x]}{5 d}$$

Result (type 5, 1569 leaves):

$$\left(\cos [c+d x]^{7 / 2}(a+b \sec [c+d x])(A+B \sec [c+d x]+C \sec [c+d x]^2)\right. \\ \left(-\frac{4(3 a A+5 b B+5 a C) \cot [c]}{5 d}+\frac{4(A b+a B) \cos [d x] \sin [c]}{3 d}+\frac{2 a A \cos [2 d x] \sin [2 c]}{5 d}+\frac{4(A b+a B) \cos [c] \sin [d x]}{3 d}+\frac{2 a A \cos [2 c] \sin [2 d x]}{5 d}\right) / \\ \left((b+a \cos [c+d x])(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])\right)- \\ \left(4 a b \cos [c+d x]^3 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]\right]^2\right. \\ \left.\frac{(a+b \sec [c+d x])(A+B \sec [c+d x]+C \sec [c+d x]^2)}{\sec [d x-\operatorname{ArcTan}[\cot [c]]} \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]}\right. \\ \left.\sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]} \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]}}\right) / \\ \left(3 d(b+a \cos [c+d x])(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\cot [c]^2}\right)- \\ \left(4 a b \cos [c+d x]^3 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]\right]^2\right. \\ \left.\frac{(a+b \sec [c+d x])(A+B \sec [c+d x]+C \sec [c+d x]^2)}{\sec [d x-\operatorname{ArcTan}[\cot [c]]} \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]}\right. \\ \left.\sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]} \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]}}\right) / \\ \left(3 d(b+a \cos [c+d x])(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\cot [c]^2}\right)- \\ \left(4 b c \cos [c+d x]^3 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]\right]^2\right. \\ \left.\frac{(a+b \sec [c+d x])(A+B \sec [c+d x]+C \sec [c+d x]^2)}{\sec [d x-\operatorname{ArcTan}[\cot [c]]} \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]}\right)$$

$$\left( \frac{\sec [d x - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \sin [d x - \text{ArcTan}[\text{Cot}[c]]]} \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \sin [c] \sin [d x - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 + \sin [d x - \text{ArcTan}[\text{Cot}[c]]]}}}{\left( d (b + a \cos [c + d x]) (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \text{Cot}[c]^2} \right) - \left( 6 a A \cos [c + d x]^3 \text{Csc}[c] (a + b \sec [c + d x]) (A + B \sec [c + d x] + C \sec [c + d x]^2) \right.} \right) /$$

$$\left( \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos [d x + \text{ArcTan}[\text{Tan}[c]]\right]^2\right] \right. \right.$$

$$\left. \left. \sin [d x + \text{ArcTan}[\text{Tan}[c]]] \tan [c] \right) / \left( \sqrt{1 - \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \tan [c]^2} \right. \right.$$

$$\left. \left. \sqrt{1 + \tan [c]^2} \right) - \frac{\frac{\sin [d x + \text{ArcTan}[\text{Tan}[c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \tan [c]^2}} \right) /$$

$$\left( 5 d (b + a \cos [c + d x]) (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right) - \left( 2 b B \cos [c + d x]^3 \text{Csc}[c] (a + b \sec [c + d x]) (A + B \sec [c + d x] + C \sec [c + d x]^2) \right.$$

$$\left( \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos [d x + \text{ArcTan}[\text{Tan}[c]]\right]^2\right] \right. \right.$$

$$\left. \left. \sin [d x + \text{ArcTan}[\text{Tan}[c]]] \tan [c] \right) / \left( \sqrt{1 - \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \tan [c]^2} \right. \right.$$

$$\left. \left( \sqrt{1 + \tan[c]^2} \right) - \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \right) /$$

$$(d (b + a \cos[c + d x]) (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x])) -$$

$$\left( 2 a C \cos[c + d x]^3 \text{Csc}[c] (a + b \text{Sec}[c + d x]) (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) \right.$$

$$\left. \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos[d x + \text{ArcTan}[\tan[c]]]^2\right] \right) \right.$$

$$\left. \left. \frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 - \cos[d x + \text{ArcTan}[\tan[c]]]}} \right) / \left( \sqrt{1 + \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}} \right) \right.$$

$$\left. \left( \sqrt{1 + \tan[c]^2} \right) - \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \right) /$$

$$(d (b + a \cos[c + d x]) (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]))$$

**Problem 1295: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c + d x]^{3/2} (a + b \sec[c + d x]) (A + B \sec[c + d x] + C \sec[c + d x]^2) dx$$

Optimal (type 4, 106 leaves, 6 steps):

$$\frac{2 (A b + a B - b C) \text{EllipticE}\left[\frac{1}{2} (c + d x), 2\right]}{d} + \frac{2 (3 b B + a (A + 3 C)) \text{EllipticF}\left[\frac{1}{2} (c + d x), 2\right]}{3 d} +$$

$$\frac{2 b C \sin[c + d x]}{d \sqrt{\cos[c + d x]}} + \frac{2 a A \sqrt{\cos[c + d x]} \sin[c + d x]}{3 d}$$

Result (type 5, 1904 leaves):

$$\frac{1}{(b + a \cos[c + d x]) (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x])}$$

$$\begin{aligned}
 & i A b \cos [c+d x]^3 \operatorname{Csc}[c] (a+b \operatorname{Sec}[c+d x]) (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c]+i \sin [c])^2\right] \right. \right. \\
 & \quad \left. \left. \frac{\sqrt{e^{-i d x} (2 (1+e^{2 i d x}) \cos [c]+2 i (-1+e^{2 i d x}) \sin [c])}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}} \right) \right) / \\
 & \quad (3 i d (1+e^{2 i d x}) \cos [c]-3 d (-1+e^{2 i d x}) \sin [c]) - \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c]+i \sin [c])^2\right] \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1+e^{2 i d x}) \cos [c]+2 i (-1+e^{2 i d x}) \sin [c])}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \quad \left. (-i d (1+e^{2 i d x}) \cos [c]+d (-1+e^{2 i d x}) \sin [c]) \right) +
 \end{aligned}$$

1

$$(b+a \cos [c+d x]) (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])$$

$$\begin{aligned}
 & i a b \cos [c+d x]^3 \\
 & \operatorname{Csc}[c] (a+b \operatorname{Sec}[c+d x]) \\
 & (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c]+i \sin [c])^2\right] \right. \right. \\
 & \quad \left. \left. \frac{\sqrt{e^{-i d x} (2 (1+e^{2 i d x}) \cos [c]+2 i (-1+e^{2 i d x}) \sin [c])}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}} \right) \right) / \\
 & \quad (3 i d (1+e^{2 i d x}) \cos [c]-3 d (-1+e^{2 i d x}) \sin [c]) - \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c]+i \sin [c])^2\right] \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1+e^{2 i d x}) \cos [c]+2 i (-1+e^{2 i d x}) \sin [c])}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \quad \left. (-i d (1+e^{2 i d x}) \cos [c]+d (-1+e^{2 i d x}) \sin [c]) \right) -
 \end{aligned}$$

1

$$(b+a \cos [c+d x]) (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])$$

$$\begin{aligned}
 & i b C \\
 & \cos [c+d x]^3 \operatorname{Csc}[c] \\
 & (a+b \operatorname{Sec}[c+d x]) \\
 & (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c]+i \sin [c])^2\right] \right. \right. \\
 & \quad \left. \left. \frac{\sqrt{e^{-i d x} (2 (1+e^{2 i d x}) \cos [c]+2 i (-1+e^{2 i d x}) \sin [c])}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}} \right) \right) / \\
 & \quad (3 i d (1+e^{2 i d x}) \cos [c]-3 d (-1+e^{2 i d x}) \sin [c]) -
 \end{aligned}$$



$$\begin{aligned}
 & \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) + \\
 & \left( \cos [c + d x]^{7/2} (a + b \sec [c + d x]) (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left( -\frac{2 (A b + a B - 2 b C + A b \cos [2 c] + a B \cos [2 c]) \operatorname{Csc}[c] \operatorname{Sec}[c]}{d} + \right. \\
 & \quad \left. \frac{4 a A \cos [d x] \sin [c]}{3 d} + \frac{4 a A \cos [c] \sin [d x]}{3 d} + \frac{4 b C \sec [c] \sec [c + d x] \sin [d x]}{d} \right) / \\
 & \quad \left. ((b + a \cos [c + d x]) (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) - \right. \\
 & \quad \left. \left( 4 a A \cos [c + d x]^3 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \right]^2 \right) \right. \\
 & \quad \left. \frac{(a + b \sec [c + d x]) (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right. \\
 & \quad \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) / \\
 & \quad \left. (3 d (b + a \cos [c + d x]) (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2}) - \right. \\
 & \quad \left. \left( 4 b B \cos [c + d x]^3 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \right]^2 \right) \right. \\
 & \quad \left. \frac{(a + b \sec [c + d x]) (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right. \\
 & \quad \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) / \\
 & \quad \left. (d (b + a \cos [c + d x]) (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2}) - \right. \\
 & \quad \left. \left( 4 a C \cos [c + d x]^3 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \right]^2 \right) \right. \\
 & \quad \left. \frac{(a + b \sec [c + d x]) (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right. \\
 & \quad \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) / \\
 & \quad \left. (d (b + a \cos [c + d x]) (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2}) \right)
 \end{aligned}$$

**Problem 1296: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sqrt{\cos [c+d x]} (a+b \operatorname{Sec}[c+d x]) (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) d x$$

Optimal (type 4, 112 leaves, 6 steps):

$$-\frac{2(b B-a(A-C)) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{d} + \frac{2(3 A b+3 a B+b C) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{3 d} + \frac{2 b C \sin [c+d x]}{3 d \cos [c+d x]^{3 / 2}} + \frac{2(b B+a C) \sin [c+d x]}{d \sqrt{\cos [c+d x]}}$$

Result (type 5, 1909 leaves):

$$\frac{1}{(b+a \cos [c+d x]) (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])} \frac{i a A \cos [c+d x]^3 \operatorname{Csc}[c] (a+b \operatorname{Sec}[c+d x]) (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2)}{\left(\left(2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x}(\cos [c]+i \sin [c])^2\right]\right) \frac{\sqrt{e^{-i d x}(2(1+e^{2 i d x}) \cos [c]+2 i(-1+e^{2 i d x}) \sin [c])}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}}\right) / \left(3 i d(1+e^{2 i d x}) \cos [c]-3 d(-1+e^{2 i d x}) \sin [c]\right)-\left(2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x}(\cos [c]+i \sin [c])^2\right]\right) \frac{\sqrt{e^{-i d x}(2(1+e^{2 i d x}) \cos [c]+2 i(-1+e^{2 i d x}) \sin [c])}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}}\right) / \left(-i d(1+e^{2 i d x}) \cos [c]+d(-1+e^{2 i d x}) \sin [c]\right)\right)}{1} \frac{1}{(b+a \cos [c+d x]) (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])} \frac{i b B \cos [c+d x]^3 \operatorname{Csc}[c] (a+b \operatorname{Sec}[c+d x]) (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2)}{\left(\left(2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x}(\cos [c]+i \sin [c])^2\right]\right) \frac{\sqrt{e^{-i d x}(2(1+e^{2 i d x}) \cos [c]+2 i(-1+e^{2 i d x}) \sin [c])}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}}\right) / \left(3 i d(1+e^{2 i d x}) \cos [c]-3 d(-1+e^{2 i d x}) \sin [c]\right)-\left(2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x}(\cos [c]+i \sin [c])^2\right]\right) \frac{\sqrt{e^{-i d x}(2(1+e^{2 i d x}) \cos [c]+2 i(-1+e^{2 i d x}) \sin [c])}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}}\right) / \left(-i d(1+e^{2 i d x}) \cos [c]+d(-1+e^{2 i d x}) \sin [c]\right)\right)}$$

$$\begin{aligned}
 & \left. \frac{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}}{(-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c])} - \right. \\
 & \frac{1}{(b + a \cos [c + d x]) (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])} \\
 & i a C \\
 & \cos [c + d x]^3 \operatorname{Csc}[c] \\
 & (a + b \operatorname{Sec}[c + d x]) \\
 & (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2\right] \right. \right. \\
 & \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
 & (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) - \\
 & \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2\right] \right. \\
 & \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) + \\
 & \left( \cos [c + d x]^{7/2} (a + b \operatorname{Sec}[c + d x]) (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \left( -\frac{2 (a A - 2 b B - 2 a C + a A \cos [2 c]) \operatorname{Csc}[c] \operatorname{Sec}[c]}{d} + \frac{4 b C \operatorname{Sec}[c] \operatorname{Sec}[c + d x]^2 \sin [d x]}{3 d} \right. \\
 & \left. \left. \frac{1}{3 d} 4 \operatorname{Sec}[c] \operatorname{Sec}[c + d x] (b C \sin [c] + 3 b B \sin [d x] + 3 a C \sin [d x]) \right) \right) / \\
 & ((b + a \cos [c + d x]) (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) - \\
 & \left( 4 A b \cos [c + d x]^3 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2 \right. \\
 & \frac{(a + b \operatorname{Sec}[c + d x]) (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} } \\
 & \left. \frac{\sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}}{\right) / \\
 & \left( d (b + a \cos [c + d x]) (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2} \right) - \\
 & \left( 4 a B \cos [c + d x]^3 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2 \right. \\
 & \frac{(a + b \operatorname{Sec}[c + d x]) (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} } \\
 & \left. \right)
 \end{aligned}$$

$$\left( \sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[d x - \text{ArcTan}[\cot[c]]]} \sqrt{1+\sin[d x - \text{ArcTan}[\cot[c]]]} \right) /$$

$$\left( d (b+a \cos[c+d x]) (A+2 C+2 B \cos[c+d x]+A \cos[2 c+2 d x]) \sqrt{1+\cot[c]^2} \right) -$$

$$\left( 4 b C \cos[c+d x]^3 \csc[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[d x - \text{ArcTan}[\cot[c]]]\right]^2 \right)$$

$$\frac{(a+b \sec[c+d x]) (A+B \sec[c+d x]+C \sec[c+d x]^2)}{\sec[d x - \text{ArcTan}[\cot[c]]] \sqrt{1-\sin[d x - \text{ArcTan}[\cot[c]]]}}$$

$$\left( \sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[d x - \text{ArcTan}[\cot[c]]]} \sqrt{1+\sin[d x - \text{ArcTan}[\cot[c]]]} \right) /$$

$$\left( 3 d (b+a \cos[c+d x]) (A+2 C+2 B \cos[c+d x]+A \cos[2 c+2 d x]) \sqrt{1+\cot[c]^2} \right)$$

**Problem 1300: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c+d x]^{7/2} (a+b \sec[c+d x])^2 (A+B \sec[c+d x]+C \sec[c+d x]^2) dx$$

Optimal (type 4, 202 leaves, 7 steps):

$$\frac{2 (6 a A b + 3 a^2 B + 5 b^2 B + 10 a b C) \text{EllipticE}\left[\frac{1}{2} (c+d x), 2\right]}{5 d} +$$

$$\frac{2 (14 a b B + 7 b^2 (A+3 C) + a^2 (5 A+7 C)) \text{EllipticF}\left[\frac{1}{2} (c+d x), 2\right]}{21 d} +$$

$$\frac{2 (4 A b^2 + 14 a b B + a^2 (5 A+7 C)) \sqrt{\cos[c+d x]} \sin[c+d x]}{21 d} +$$

$$\frac{2 a (4 A b + 7 a B) \cos[c+d x]^{3/2} \sin[c+d x]}{35 d} + \frac{2 A \sqrt{\cos[c+d x]} (b+a \cos[c+d x])^2 \sin[c+d x]}{7 d}$$

Result (type 5, 2361 leaves):

$$\left( \cos[c+d x]^{9/2} (a+b \sec[c+d x])^2 \right.$$

$$(A+B \sec[c+d x]+C \sec[c+d x]^2) \left( -\frac{4 (6 a A b + 3 a^2 B + 5 b^2 B + 10 a b C) \cot[c]}{5 d} + \right.$$

$$\frac{(23 a^2 A + 28 A b^2 + 56 a b B + 28 a^2 C) \cos[d x] \sin[c]}{21 d} + \frac{2 a (2 A b + a B) \cos[2 d x] \sin[2 c]}{5 d} +$$

$$\frac{a^2 A \cos[3 d x] \sin[3 c]}{7 d} + \frac{(23 a^2 A + 28 A b^2 + 56 a b B + 28 a^2 C) \cos[c] \sin[d x]}{21 d} +$$

$$\left. \left. \frac{2 a (2 A b + a B) \cos[2 c] \sin[2 d x]}{5 d} + \frac{a^2 A \cos[3 c] \sin[3 d x]}{7 d} \right) \right) /$$

$$\begin{aligned}
 & \left( (b + a \cos[c + dx])^2 (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \right) - \\
 & \left( 20 a^2 A \cos[c + dx]^4 \csc[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\cot[c]]]\right]^2 \right) \\
 & \frac{(a + b \sec[c + dx])^2 (A + B \sec[c + dx] + C \sec[c + dx]^2)}{\sec[dx - \operatorname{ArcTan}[\cot[c]]] \sqrt{1 - \sin[dx - \operatorname{ArcTan}[\cot[c]]]}} \\
 & \left. \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]]] \sqrt{1 + \sin[dx - \operatorname{ArcTan}[\cot[c]]]}} \right) / \\
 & \left( 21 d (b + a \cos[c + dx])^2 (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{1 + \cot[c]^2} \right) - \\
 & \left( 4 A b^2 \cos[c + dx]^4 \csc[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\cot[c]]]\right]^2 \right) \\
 & \frac{(a + b \sec[c + dx])^2 (A + B \sec[c + dx] + C \sec[c + dx]^2)}{\sec[dx - \operatorname{ArcTan}[\cot[c]]] \sqrt{1 - \sin[dx - \operatorname{ArcTan}[\cot[c]]]}} \\
 & \left. \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]]] \sqrt{1 + \sin[dx - \operatorname{ArcTan}[\cot[c]]]}} \right) / \\
 & \left( 3 d (b + a \cos[c + dx])^2 (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{1 + \cot[c]^2} \right) - \\
 & \left( 8 a b B \cos[c + dx]^4 \csc[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\cot[c]]]\right]^2 \right) \\
 & \frac{(a + b \sec[c + dx])^2 (A + B \sec[c + dx] + C \sec[c + dx]^2)}{\sec[dx - \operatorname{ArcTan}[\cot[c]]] \sqrt{1 - \sin[dx - \operatorname{ArcTan}[\cot[c]]]}} \\
 & \left. \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]]] \sqrt{1 + \sin[dx - \operatorname{ArcTan}[\cot[c]]]}} \right) / \\
 & \left( 3 d (b + a \cos[c + dx])^2 (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{1 + \cot[c]^2} \right) - \\
 & \left( 4 a^2 C \cos[c + dx]^4 \csc[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\cot[c]]]\right]^2 \right) \\
 & \frac{(a + b \sec[c + dx])^2 (A + B \sec[c + dx] + C \sec[c + dx]^2)}{\sec[dx - \operatorname{ArcTan}[\cot[c]]] \sqrt{1 - \sin[dx - \operatorname{ArcTan}[\cot[c]]]}} \\
 & \left. \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]]] \sqrt{1 + \sin[dx - \operatorname{ArcTan}[\cot[c]]]}} \right) / \\
 & \left( 3 d (b + a \cos[c + dx])^2 (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{1 + \cot[c]^2} \right) - \\
 & \left( 4 b^2 C \cos[c + dx]^4 \csc[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\cot[c]]]\right]^2 \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( (a + b \operatorname{Sec}[c + d x])^2 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \left. \operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right. \\
 & \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) / \\
 & \left( d (b + a \operatorname{Cos}[c + d x])^2 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2} \right) - \\
 & \left( 12 a A b \operatorname{Cos}[c + d x]^4 \operatorname{Csc}[c] (a + b \operatorname{Sec}[c + d x])^2 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \left. \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]^2\right] \right) \right. \\
 & \left. \operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] \right) / \left( \sqrt{1 - \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right. \\
 & \left. \sqrt{1 + \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{\operatorname{Cos}[c] \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \operatorname{Tan}[c]^2} \right. \\
 & \left. \sqrt{1 + \operatorname{Tan}[c]^2} \right) - \frac{\frac{\operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1 + \operatorname{Tan}[c]^2}} + \frac{2 \operatorname{Cos}[c]^2 \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}}{\operatorname{Cos}[c]^2 + \operatorname{Sin}[c]^2}}{\sqrt{\operatorname{Cos}[c] \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \operatorname{Tan}[c]^2}} \right) / \\
 & \left( 5 d (b + a \operatorname{Cos}[c + d x])^2 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \right) - \\
 & \left( 6 a^2 B \operatorname{Cos}[c + d x]^4 \operatorname{Csc}[c] (a + b \operatorname{Sec}[c + d x])^2 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \left. \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]^2\right] \right) \right. \\
 & \left. \operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] \right) / \left( \sqrt{1 - \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right. \\
 & \left. \sqrt{1 + \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{\operatorname{Cos}[c] \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \operatorname{Tan}[c]^2} \right)
 \end{aligned}$$

$$\left. \left. \left. \left. \sqrt{1 + \tan[c]^2} \right) - \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \right) \right) \right) /$$

$$\left( 5 d (b + a \cos[c + d x])^2 (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) \right) -$$

$$\left( 2 b^2 B \cos[c + d x]^4 \csc[c] (a + b \sec[c + d x])^2 (A + B \sec[c + d x] + C \sec[c + d x]^2) \right)$$

$$\left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos[d x + \text{ArcTan}[\tan[c]]]^2\right] \right)$$

$$\left. \left. \left. \left. \frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 - \cos[d x + \text{ArcTan}[\tan[c]]]}} \right) \right) \right) /$$

$$\sqrt{1 + \cos[d x + \text{ArcTan}[\tan[c]]]} \sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}$$

$$\left. \left. \left. \left. \sqrt{1 + \tan[c]^2} \right) - \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \right) \right) \right) /$$

$$\left( d (b + a \cos[c + d x])^2 (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) \right) -$$

$$\left( 4 a b C \cos[c + d x]^4 \csc[c] (a + b \sec[c + d x])^2 (A + B \sec[c + d x] + C \sec[c + d x]^2) \right)$$

$$\left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos[d x + \text{ArcTan}[\tan[c]]]^2\right] \right)$$

$$\left. \left. \left. \left. \frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 - \cos[d x + \text{ArcTan}[\tan[c]]]}} \right) \right) \right) /$$

$$\sqrt{1 + \cos[d x + \text{ArcTan}[\tan[c]]]} \sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}$$

$$\left( \sqrt{1 + \tan[c]^2} \right) - \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \Bigg) /$$

$$\left( d (b + a \cos[c + d x])^2 (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) \right)$$

**Problem 1301: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c + d x]^{5/2} (a + b \sec[c + d x])^2 (A + B \sec[c + d x] + C \sec[c + d x]^2) dx$$

Optimal (type 4, 186 leaves, 7 steps):

$$\frac{2 (10 a b B + 5 b^2 (A - C) + a^2 (3 A + 5 C)) \text{EllipticE}\left[\frac{1}{2} (c + d x), 2\right]}{5 d} +$$

$$\frac{2 (a^2 B + 3 b^2 B + 2 a b (A + 3 C)) \text{EllipticF}\left[\frac{1}{2} (c + d x), 2\right]}{3 d} +$$

$$\frac{2 a (2 A b + a B - 6 b C) \sqrt{\cos[c + d x]} \sin[c + d x]}{3 d} +$$

$$\frac{2 a^2 (A - 5 C) \cos[c + d x]^{3/2} \sin[c + d x]}{5 d} + \frac{2 C (b + a \cos[c + d x])^2 \sin[c + d x]}{d \sqrt{\cos[c + d x]}}$$

Result (type 5, 3011 leaves):

$$\frac{1}{5 (b + a \cos[c + d x])^2 (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x])}$$

$$3 i a^2 A \cos[c + d x]^4 \text{Csc}[c] (a + b \sec[c + d x])^2 (A + B \sec[c + d x] + C \sec[c + d x]^2)$$

$$\left( \left( 2 e^{2 i d x} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right. \right.$$

$$\frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])}}{\sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]}} \Bigg) /$$

$$(3 i d (1 + e^{2 i d x}) \cos[c] - 3 d (-1 + e^{2 i d x}) \sin[c]) -$$

$$\left( 2 \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right.$$

$$\frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])}}{\sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]}} \Bigg) /$$

$$\left. (-i d (1 + e^{2 i d x}) \cos[c] + d (-1 + e^{2 i d x}) \sin[c]) \right) +$$

$$\frac{1}{(b + a \cos[c + d x])^2 (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x])}$$

$$i A b^2$$



$$\begin{aligned}
 & \cos [c+d x]^4 \operatorname{Csc}[c] \\
 & (a+b \operatorname{Sec}[c+d x])^2 \\
 & (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x}(\cos [c]+i \sin [c])^2\right] \right. \right. \\
 & \quad \left. \left. \frac{\sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}} \right) \right) / \\
 & \quad \left( 3 i d\left(1+e^{2 i d x}\right) \cos [c]-3 d\left(-1+e^{2 i d x}\right) \sin [c]\right)- \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x}(\cos [c]+i \sin [c])^2\right] \right) \\
 & \quad \frac{\sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \quad \left. \left. \left(-i d\left(1+e^{2 i d x}\right) \cos [c]+d\left(-1+e^{2 i d x}\right) \sin [c]\right)\right) \right) + \\
 & \qquad \qquad \qquad 1
 \end{aligned}$$

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$$(b+a \cos [c+d x])^2 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])$$

$$2 i a b B$$

$$\begin{aligned}
 & \cos [c+d x]^4 \operatorname{Csc}[c] \\
 & (a+b \operatorname{Sec}[c+d x])^2 \\
 & (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x}(\cos [c]+i \sin [c])^2\right] \right) \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \quad \left( 3 i d\left(1+e^{2 i d x}\right) \cos [c]-3 d\left(-1+e^{2 i d x}\right) \sin [c]\right)- \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x}(\cos [c]+i \sin [c])^2\right] \right) \\
 & \quad \frac{\sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \quad \left. \left. \left(-i d\left(1+e^{2 i d x}\right) \cos [c]+d\left(-1+e^{2 i d x}\right) \sin [c]\right)\right) \right) + \\
 & \qquad \qquad \qquad 1
 \end{aligned}$$

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$$(b+a \cos [c+d x])^2 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])$$

$$i a^2 C \cos [c+d x]^4$$

$$\begin{aligned}
 & \operatorname{Csc}[c] (a+b \operatorname{Sec}[c+d x])^2 \\
 & (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x}(\cos [c]+i \sin [c])^2\right] \right) \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}} \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( 3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c] \right) - \\
 & \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) - \\
 & \quad \quad \quad 1 \\
 & \frac{(b + a \cos [c + d x])^2 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])}{i b^2 C \cos [c + d x]^4} \\
 & \operatorname{Csc}[c] (a + b \operatorname{Sec}[c + d x])^2 \\
 & (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \left. (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) - \right. \\
 & \left. \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) + \\
 & \left( \cos [c + d x]^{9/2} (a + b \operatorname{Sec}[c + d x])^2 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \quad \left( -\frac{1}{5 d} (3 a^2 A + 5 A b^2 + 10 a b B + 5 a^2 C - 10 b^2 C + 3 a^2 A \cos [2 c] + 5 A b^2 \cos [2 c] + \right. \\
 & \quad \quad 10 a b B \cos [2 c] + 5 a^2 C \cos [2 c]) \operatorname{Csc}[c] \operatorname{Sec}[c] + \frac{4 a (2 A b + a B) \cos [d x] \sin [c]}{3 d} + \\
 & \quad \frac{2 a^2 A \cos [2 d x] \sin [2 c]}{5 d} + \frac{4 a (2 A b + a B) \cos [c] \sin [d x]}{3 d} + \\
 & \quad \left. \left. \frac{4 b^2 C \operatorname{Sec}[c] \operatorname{Sec}[c + d x] \sin [d x]}{d} + \frac{2 a^2 A \cos [2 c] \sin [2 d x]}{5 d} \right) \right) / \\
 & \left( (b + a \cos [c + d x])^2 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right) - \\
 & \left( 8 a A b \cos [c + d x]^4 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2 \right] \right. \\
 & \quad \left. (a + b \operatorname{Sec}[c + d x])^2 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \quad \left. \operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{\sqrt{-\sqrt{1+\cot^2[c]} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]}}{\sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]}} \right) / \\
 & \left( 3d (b+a \cos[c+dx])^2 (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \sqrt{1+\cot^2[c]} - \right. \\
 & \left. \left( 4a^2 B \cos[c+dx]^4 \csc[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\cot[c]]]^2\right] \right)^2 \right. \\
 & \left. \frac{(a+b \sec[c+dx])^2 (A+B \sec[c+dx] + C \sec[c+dx]^2)}{\sec[dx - \text{ArcTan}[\cot[c]]] \sqrt{1-\sin[dx - \text{ArcTan}[\cot[c]]]}} \right. \\
 & \left. \frac{\sqrt{-\sqrt{1+\cot^2[c]} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]}}{\sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]}} \right) / \\
 & \left( 3d (b+a \cos[c+dx])^2 (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \sqrt{1+\cot^2[c]} - \right. \\
 & \left. \left( 4b^2 B \cos[c+dx]^4 \csc[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\cot[c]]]^2\right] \right)^2 \right. \\
 & \left. \frac{(a+b \sec[c+dx])^2 (A+B \sec[c+dx] + C \sec[c+dx]^2)}{\sec[dx - \text{ArcTan}[\cot[c]]] \sqrt{1-\sin[dx - \text{ArcTan}[\cot[c]]]}} \right. \\
 & \left. \frac{\sqrt{-\sqrt{1+\cot^2[c]} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]} \sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]}}{\sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]}} \right) / \\
 & \left( d (b+a \cos[c+dx])^2 (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \sqrt{1+\cot^2[c]} - \right. \\
 & \left. \left( 8abC \cos[c+dx]^4 \csc[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\cot[c]]]^2\right] \right)^2 \right. \\
 & \left. \frac{(a+b \sec[c+dx])^2 (A+B \sec[c+dx] + C \sec[c+dx]^2)}{\sec[dx - \text{ArcTan}[\cot[c]]] \sqrt{1-\sin[dx - \text{ArcTan}[\cot[c]]]}} \right. \\
 & \left. \frac{\sqrt{-\sqrt{1+\cot^2[c]} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]} \sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]}}{\sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]}} \right) / \\
 & \left( d (b+a \cos[c+dx])^2 (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \sqrt{1+\cot^2[c]} \right)
 \end{aligned}$$

**Problem 1302: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c+d x]^{3 / 2}(a+b \sec [c+d x])^2(A+B \sec [c+d x]+C \sec [c+d x]^2) d x$$

Optimal (type 4, 180 leaves, 7 steps):

$$\frac{2\left(a^2 B-b^2 B+2 a b(A-C)\right) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{d} +$$

$$\frac{2\left(6 a b B+b^2(3 A+C)+a^2(A+3 C)\right) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{3 d} + \frac{2 b(3 b B+4 a C) \sin [c+d x]}{3 d \sqrt{\cos [c+d x]}} +$$

$$\frac{2 a^2(A-C) \sqrt{\cos [c+d x]} \sin [c+d x]}{3 d} + \frac{2 C(b+a \cos [c+d x])^2 \sin [c+d x]}{3 d \cos [c+d x]^{3 / 2}}$$

Result (type 5, 2779 leaves):

$$\frac{1}{(b+a \cos [c+d x])^2(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])}$$

$$2 i a A b \cos [c+d x]^4 \operatorname{Csc}[c](a+b \sec [c+d x])^2(A+B \sec [c+d x]+C \sec [c+d x]^2)$$

$$\left(\left(2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4},-e^{2 i d x}(\cos [c]+i \sin [c])^2\right]\right.\right.$$

$$\left.\frac{\sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}}\right) /$$

$$\left(3 i d\left(1+e^{2 i d x}\right) \cos [c]-3 d\left(-1+e^{2 i d x}\right) \sin [c]\right)-$$

$$\left(2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4},-e^{2 i d x}(\cos [c]+i \sin [c])^2\right]\right)$$

$$\left.\frac{\sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}}\right) /$$

$$\left(-i d\left(1+e^{2 i d x}\right) \cos [c]+d\left(-1+e^{2 i d x}\right) \sin [c]\right)\right) +$$

$$\frac{1}{(b+a \cos [c+d x])^2(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])}$$

$$i a^2 B$$

$$\cos [c+d x]^4 \operatorname{Csc}[c]$$

$$(a+b \sec [c+d x])^2$$

$$(A+B \sec [c+d x]+C \sec [c+d x]^2)$$

$$\left(\left(2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4},-e^{2 i d x}(\cos [c]+i \sin [c])^2\right]\right.\right.$$

$$\left.\frac{\sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}}\right) /$$

$$\left(3 i d\left(1+e^{2 i d x}\right) \cos [c]-3 d\left(-1+e^{2 i d x}\right) \sin [c]\right)-$$

$$\left(2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4},-e^{2 i d x}(\cos [c]+i \sin [c])^2\right]\right)$$

$$\left.\frac{\sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}}\right)$$

$$\begin{aligned}
 & \frac{\sqrt{1 + e^{2ix} \cos[2c] + ie^{2ix} \sin[2c]}}{(-id(1 + e^{2ix}) \cos[c] + d(-1 + e^{2ix}) \sin[c]) - 1} \\
 & \frac{(b + a \cos[c + dx])^2 (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])}{ib^2 B} \\
 & \cos[c + dx]^4 \operatorname{Csc}[c] \\
 & (a + b \operatorname{Sec}[c + dx])^2 \\
 & (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \\
 & \left( \left( 2e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix} (\cos[c] + i \sin[c])^2\right] \right) \right. \\
 & \quad \frac{\sqrt{e^{-ix} (2(1 + e^{2ix}) \cos[c] + 2i(-1 + e^{2ix}) \sin[c])}}{\sqrt{1 + e^{2ix} \cos[2c] + ie^{2ix} \sin[2c]}} \Bigg) / \\
 & \quad (3id(1 + e^{2ix}) \cos[c] - 3d(-1 + e^{2ix}) \sin[c]) - \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix} (\cos[c] + i \sin[c])^2\right] \right) \\
 & \quad \frac{\sqrt{e^{-ix} (2(1 + e^{2ix}) \cos[c] + 2i(-1 + e^{2ix}) \sin[c])}}{\sqrt{1 + e^{2ix} \cos[2c] + ie^{2ix} \sin[2c]}} \Bigg) / \\
 & \quad \left. (-id(1 + e^{2ix}) \cos[c] + d(-1 + e^{2ix}) \sin[c]) \right) - 1 \\
 & \frac{(b + a \cos[c + dx])^2 (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])}{2iabC} \\
 & \cos[c + dx]^4 \operatorname{Csc}[c] \\
 & (a + b \operatorname{Sec}[c + dx])^2 \\
 & (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \\
 & \left( \left( 2e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix} (\cos[c] + i \sin[c])^2\right] \right) \right. \\
 & \quad \frac{\sqrt{e^{-ix} (2(1 + e^{2ix}) \cos[c] + 2i(-1 + e^{2ix}) \sin[c])}}{\sqrt{1 + e^{2ix} \cos[2c] + ie^{2ix} \sin[2c]}} \Bigg) / \\
 & \quad (3id(1 + e^{2ix}) \cos[c] - 3d(-1 + e^{2ix}) \sin[c]) - \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix} (\cos[c] + i \sin[c])^2\right] \right) \\
 & \quad \frac{\sqrt{e^{-ix} (2(1 + e^{2ix}) \cos[c] + 2i(-1 + e^{2ix}) \sin[c])}}{\sqrt{1 + e^{2ix} \cos[2c] + ie^{2ix} \sin[2c]}} \Bigg) / \\
 & \quad \left. (-id(1 + e^{2ix}) \cos[c] + d(-1 + e^{2ix}) \sin[c]) \right) + \\
 & (\cos[c + dx])^{9/2} (a + b \operatorname{Sec}[c + dx])^2 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2)
 \end{aligned}$$

$$\begin{aligned}
 & \left( -\frac{1}{d} (2 a A b + a^2 B - 2 b^2 B - 4 a b C + 2 a A b \cos [2 c] + a^2 B \cos [2 c]) \operatorname{Csc}[c] \operatorname{Sec}[c] + \right. \\
 & \quad \frac{4 a^2 A \cos [d x] \sin [c]}{3 d} + \frac{4 a^2 A \cos [c] \sin [d x]}{3 d} + \frac{4 b^2 C \operatorname{Sec}[c] \operatorname{Sec}[c+d x]^2 \sin [d x]}{3 d} + \\
 & \quad \left. \frac{1}{3 d} 4 \operatorname{Sec}[c] \operatorname{Sec}[c+d x] (b^2 C \sin [c] + 3 b^2 B \sin [d x] + 6 a b C \sin [d x]) \right) / \\
 & \left( (b+a \cos [c+d x])^2 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right) - \\
 & \left( 4 a^2 A \cos [c+d x]^4 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right. \\
 & \quad \frac{(a+b \operatorname{Sec}[c+d x])^2 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2)}{\operatorname{Sec}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \quad \sqrt{-\sqrt{1+\operatorname{Cot}[c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \quad \left. \sqrt{1+\sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) / \\
 & \left( 3 d (b+a \cos [c+d x])^2 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\operatorname{Cot}[c]^2} \right) - \\
 & \left( 4 A b^2 \cos [c+d x]^4 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right. \\
 & \quad \frac{(a+b \operatorname{Sec}[c+d x])^2 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2)}{\operatorname{Sec}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \quad \left. \sqrt{-\sqrt{1+\operatorname{Cot}[c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1+\sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) / \\
 & \left( d (b+a \cos [c+d x])^2 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\operatorname{Cot}[c]^2} \right) - \\
 & \left( 8 a b B \cos [c+d x]^4 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right. \\
 & \quad \frac{(a+b \operatorname{Sec}[c+d x])^2 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2)}{\operatorname{Sec}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \quad \left. \sqrt{-\sqrt{1+\operatorname{Cot}[c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1+\sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) / \\
 & \left( d (b+a \cos [c+d x])^2 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\operatorname{Cot}[c]^2} \right) - \\
 & \left( 4 a^2 C \cos [c+d x]^4 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right. \\
 & \quad \frac{(a+b \operatorname{Sec}[c+d x])^2 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2)}{\operatorname{Sec}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]}
 \end{aligned}$$

$$\left( \sqrt{-\sqrt{1+\cot^2[c]} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]} \sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]} \right) /$$

$$\left( d (b + a \cos[c + dx])^2 (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{1 + \cot^2[c]} \right) -$$

$$\left( 4 b^2 C \cos[c + dx]^4 \csc[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\cot[c]]]^2\right] \right.$$

$$\frac{(a + b \sec[c + dx])^2 (A + B \sec[c + dx] + C \sec[c + dx]^2)}{\sec[dx - \text{ArcTan}[\cot[c]]] \sqrt{1 - \sin[dx - \text{ArcTan}[\cot[c]]]}}$$

$$\left. \sqrt{-\sqrt{1+\cot^2[c]} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]} \sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]} \right) /$$

$$\left( 3 d (b + a \cos[c + dx])^2 (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{1 + \cot^2[c]} \right)$$

**Problem 1303: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sqrt{\cos[c + dx]} (a + b \sec[c + dx])^2 (A + B \sec[c + dx] + C \sec[c + dx]^2) dx$$

Optimal (type 4, 201 leaves, 7 steps):

$$\frac{2 (10 a b B - 5 a^2 (A - C) + b^2 (5 A + 3 C)) \text{EllipticE}\left[\frac{1}{2} (c + dx), 2\right]}{5 d} +$$

$$\frac{2 (3 a^2 B + b^2 B + 2 a b (3 A + C)) \text{EllipticF}\left[\frac{1}{2} (c + dx), 2\right]}{3 d} + \frac{2 b (5 b B + 4 a C) \sin[c + dx]}{15 d \cos[c + dx]^{3/2}} +$$

$$\frac{2 (5 A b^2 + 10 a b B + 4 a^2 C + 3 b^2 C) \sin[c + dx]}{5 d \sqrt{\cos[c + dx]}} + \frac{2 C (b + a \cos[c + dx])^2 \sin[c + dx]}{5 d \cos[c + dx]^{5/2}}$$

Result (type 5, 3017 leaves):

$$\frac{1}{(b + a \cos[c + dx])^2 (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])}$$

$$i a^2 A \cos[c + dx]^4 \csc[c] (a + b \sec[c + dx])^2 (A + B \sec[c + dx] + C \sec[c + dx]^2)$$

$$\left( \left( 2 e^{2 i dx} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i dx} (\cos[c] + i \sin[c])^2\right] \right. \right.$$

$$\frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \cos[c] + 2 i (-1 + e^{2 i dx}) \sin[c])}}{\sqrt{1 + e^{2 i dx} \cos[2c] + i e^{2 i dx} \sin[2c]}} \left. \right) /$$

$$(3 i d (1 + e^{2 i dx}) \cos[c] - 3 d (-1 + e^{2 i dx}) \sin[c]) -$$

$$\left( 2 \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i dx} (\cos[c] + i \sin[c])^2\right] \right.$$

$$\left. \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \cos[c] + 2 i (-1 + e^{2 i dx}) \sin[c])}}{\sqrt{1 + e^{2 i dx} \cos[2c] + i e^{2 i dx} \sin[2c]}} \right)$$

$$\begin{aligned}
 & \left( \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \\
 & \left( -i d \left( 1 + e^{2 i d x} \right) \cos [c] + d \left( -1 + e^{2 i d x} \right) \sin [c] \right) - \\
 & \qquad \qquad \qquad 1 \\
 & \hline
 & (b + a \cos [c + d x])^2 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \\
 & i A b^2 \\
 & \cos [c + d x]^4 \operatorname{Csc}[c] \\
 & (a + b \operatorname{Sec}[c + d x])^2 \\
 & (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \right. \\
 & \quad \left. \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \right. \right. \\
 & \quad \left. \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) \right) / \\
 & (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) - \\
 & \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \\
 & \quad \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \right. \\
 & \quad \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \\
 & \left. \left( -i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c] \right) \right) - \\
 & \qquad \qquad \qquad 1 \\
 & \hline
 & (b + a \cos [c + d x])^2 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \\
 & 2 i a b B \\
 & \cos [c + d x]^4 \operatorname{Csc}[c] \\
 & (a + b \operatorname{Sec}[c + d x])^2 \\
 & (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \right. \\
 & \quad \left. \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \right. \right. \\
 & \quad \left. \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) \right) / \\
 & (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) - \\
 & \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \\
 & \quad \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \right. \\
 & \quad \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \\
 & \left. \left( -i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c] \right) \right) - \\
 & \qquad \qquad \qquad 1 \\
 & \hline
 & (b + a \cos [c + d x])^2 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \\
 & i a^2 C \cos [c + d x]^4
 \end{aligned}$$





$$\begin{aligned}
 & \frac{1}{15d} 4 \operatorname{Sec}[c] \operatorname{Sec}[c+dx] \left( 5b^2 B \operatorname{Sin}[c] + 10abC \operatorname{Sin}[c] + \right. \\
 & \quad \left. 15A b^2 \operatorname{Sin}[dx] + 30abB \operatorname{Sin}[dx] + 15a^2 C \operatorname{Sin}[dx] + 9b^2 C \operatorname{Sin}[dx] \right) - \\
 & \left( 8aAb \operatorname{Cos}[c+dx]^4 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right. \\
 & \quad \frac{(a+b \operatorname{Sec}[c+dx])^2 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2)}{\operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \quad \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \quad \left. \sqrt{1 + \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) / \\
 & \left( d(b+a \operatorname{Cos}[c+dx])^2 (A+2C+2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) \sqrt{1 + \operatorname{Cot}[c]^2} \right) - \\
 & \left( 4a^2 B \operatorname{Cos}[c+dx]^4 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right. \\
 & \quad \frac{(a+b \operatorname{Sec}[c+dx])^2 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2)}{\operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \quad \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1 + \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) / \\
 & \left( d(b+a \operatorname{Cos}[c+dx])^2 (A+2C+2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) \sqrt{1 + \operatorname{Cot}[c]^2} \right) - \\
 & \left( 4b^2 B \operatorname{Cos}[c+dx]^4 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right. \\
 & \quad \frac{(a+b \operatorname{Sec}[c+dx])^2 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2)}{\operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \quad \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1 + \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) / \\
 & \left( 3d(b+a \operatorname{Cos}[c+dx])^2 (A+2C+2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) \sqrt{1 + \operatorname{Cot}[c]^2} \right) - \\
 & \left( 8aAbC \operatorname{Cos}[c+dx]^4 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right. \\
 & \quad \frac{(a+b \operatorname{Sec}[c+dx])^2 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2)}{\operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \quad \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1 + \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) /
 \end{aligned}$$

$$\left( 3 d (b + a \cos [c + d x])^2 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} \right)$$

**Problem 1306: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c + d x]^{9/2} (a + b \sec [c + d x])^3 (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 4, 296 leaves, 8 steps):

$$\begin{aligned} & \frac{1}{15 d} 2 (27 a^2 b B + 15 b^3 B + 9 a b^2 (3 A + 5 C) + a^3 (7 A + 9 C)) \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] + \\ & \frac{1}{21 d} 2 (5 a^3 B + 21 a b^2 B + 7 b^3 (A + 3 C) + 3 a^2 b (5 A + 7 C)) \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] + \\ & \frac{1}{63 d} 2 (8 A b^3 + 15 a^3 B + 54 a b^2 B + 9 a^2 b (5 A + 7 C)) \sqrt{\cos [c + d x]} \sin [c + d x] + \\ & \frac{2 a (24 A b^2 + 99 a b B + 7 a^2 (7 A + 9 C)) \cos [c + d x]^{3/2} \sin [c + d x]}{315 d} + \\ & \frac{2 (2 A b + 3 a B) \sqrt{\cos [c + d x]} (b + a \cos [c + d x])^2 \sin [c + d x]}{21 d} + \\ & \frac{2 A \sqrt{\cos [c + d x]} (b + a \cos [c + d x])^3 \sin [c + d x]}{9 d} \end{aligned}$$

Result (type 5, 3237 leaves):

$$\begin{aligned} & \frac{1}{(b + a \cos [c + d x])^3 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])} \\ & \cos [c + d x]^{11/2} (a + b \sec [c + d x])^3 (A + B \sec [c + d x] + C \sec [c + d x]^2) \\ & \left( -\frac{1}{15 d} 4 (7 a^3 A + 27 a A b^2 + 27 a^2 b B + 15 b^3 B + 9 a^3 C + 45 a b^2 C) \cot [c] + \right. \\ & \frac{1}{21 d} (69 a^2 A b + 28 A b^3 + 23 a^3 B + 84 a b^2 B + 84 a^2 b C) \cos [d x] \sin [c] + \\ & \frac{a (19 a^2 A + 54 A b^2 + 54 a b B + 18 a^2 C) \cos [2 d x] \sin [2 c]}{45 d} + \\ & \frac{a^2 (3 A b + a B) \cos [3 d x] \sin [3 c]}{7 d} + \frac{a^3 A \cos [4 d x] \sin [4 c]}{18 d} + \frac{1}{21 d} \\ & (69 a^2 A b + 28 A b^3 + 23 a^3 B + 84 a b^2 B + 84 a^2 b C) \cos [c] \sin [d x] + \\ & \frac{a (19 a^2 A + 54 A b^2 + 54 a b B + 18 a^2 C) \cos [2 c] \sin [2 d x]}{45 d} + \\ & \left. \frac{a^2 (3 A b + a B) \cos [3 c] \sin [3 d x]}{7 d} + \frac{a^3 A \cos [4 c] \sin [4 d x]}{18 d} \right) - \\ & \left( 20 a^2 A b \cos [c + d x]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\cot [c]]]^2\right] \right) \\ & (a + b \sec [c + d x])^3 (A + B \sec [c + d x] + C \sec [c + d x]^2) \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{\sec [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}}{\sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}}} \right) / \\
 & \left( 7 d (b + a \cos [c + d x])^3 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2} \right) - \\
 & \left( 4 A b^3 \cos [c + d x]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right. \\
 & \left. \frac{(a + b \sec [c + d x])^3 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sec [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right. \\
 & \left. \frac{\sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}}}{\sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}}} \right) / \\
 & \left( 3 d (b + a \cos [c + d x])^3 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2} \right) - \\
 & \left( 20 a^3 B \cos [c + d x]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right. \\
 & \left. \frac{(a + b \sec [c + d x])^3 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sec [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right. \\
 & \left. \frac{\sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}}}{\sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}}} \right) / \\
 & \left( 21 d (b + a \cos [c + d x])^3 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2} \right) - \\
 & \left( 4 a b^2 B \cos [c + d x]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right. \\
 & \left. \frac{(a + b \sec [c + d x])^3 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sec [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right. \\
 & \left. \frac{\sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}}}{\sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}}} \right) / \\
 & \left( d (b + a \cos [c + d x])^3 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2} \right) - \\
 & \left( 4 a^2 b C \cos [c + d x]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right. \\
 & \left. \frac{(a + b \sec [c + d x])^3 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sec [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right. \\
 & \left. \frac{\sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}}}{\sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}}} \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( d (b + a \cos [c + d x])^3 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} \right) - \\
 & \left( 4 b^3 C \cos [c + d x]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\cot [c]]]^2\right] \right. \\
 & \quad \left. \frac{(a + b \sec [c + d x])^3 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sec [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\cot [c]]]} \right. \\
 & \quad \left. \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\cot [c]]]} \right) / \\
 & \left( d (b + a \cos [c + d x])^3 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} \right) - \\
 & \left( 14 a^3 A \cos [c + d x]^5 \operatorname{Csc}[c] (a + b \sec [c + d x])^3 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left. \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos [d x + \operatorname{ArcTan}[\tan [c]]]^2\right] \right) \right. \\
 & \quad \left. \frac{\sin [d x + \operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1 - \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \right) / \\
 & \quad \left. \frac{\sqrt{1 + \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}}}{\sqrt{1 + \tan [c]^2}} - \frac{\frac{\sin [d x + \operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}}} \right) / \\
 & \left( 15 d (b + a \cos [c + d x])^3 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right) - \\
 & \left( 18 a A b^2 \cos [c + d x]^5 \operatorname{Csc}[c] (a + b \sec [c + d x])^3 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \quad \left. \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos [d x + \operatorname{ArcTan}[\tan [c]]]^2\right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{\sin [d x + \operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1 - \cos [d x + \operatorname{ArcTan}[\tan [c]]]}} \right) / \left( \sqrt{1 + \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \sqrt{1 + \tan [c]^2} \right. \\
 & \left. - \frac{\frac{\sin [d x + \operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \sqrt{1 + \tan [c]^2}} \right) / \\
 & \left( 5 d (b + a \cos [c + d x])^3 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right) - \\
 & \left( 18 a^2 b B \cos [c + d x]^5 \operatorname{Csc}[c] (a + b \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \left. \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos [d x + \operatorname{ArcTan}[\tan [c]]]^2\right] \right) \right) \\
 & \left( \frac{\sin [d x + \operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1 - \cos [d x + \operatorname{ArcTan}[\tan [c]]]}} \right) / \left( \sqrt{1 + \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \sqrt{1 + \tan [c]^2} \right. \\
 & \left. - \frac{\frac{\sin [d x + \operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \sqrt{1 + \tan [c]^2}} \right) / \\
 & \left( 5 d (b + a \cos [c + d x])^3 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right) - \\
 & \left( 2 b^3 B \cos [c + d x]^5 \operatorname{Csc}[c] (a + b \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \left. \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos [d x + \operatorname{ArcTan}[\tan [c]]]^2\right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{\sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 - \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \tan [c]^2}} \right) / \left( \frac{\sqrt{1 + \tan [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \tan [c]^2}} \right) - \left( \frac{\frac{\sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \tan [c]^2}} \right) / \\
 & \left( d (b + a \cos [c + d x])^3 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right) - \\
 & \left( 6 a^3 C \cos [c + d x]^5 \text{Csc}[c] (a + b \sec [c + d x])^3 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \left. \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \text{ArcTan}[\text{Tan}[c]] \right]^2 \right] \right) \right) \\
 & \left( \frac{\sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 - \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \tan [c]^2}} \right) / \left( \frac{\sqrt{1 + \tan [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \tan [c]^2}} \right) - \left( \frac{\frac{\sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \tan [c]^2}} \right) / \\
 & \left( 5 d (b + a \cos [c + d x])^3 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right) - \\
 & \left( 6 a b^2 C \cos [c + d x]^5 \text{Csc}[c] (a + b \sec [c + d x])^3 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\
 & \left. \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \text{ArcTan}[\text{Tan}[c]] \right]^2 \right] \right) \right)
 \end{aligned}$$

$$\left( \frac{\sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 - \cos [d x + \text{ArcTan}[\text{Tan}[c]]]}} \right) / \left( \frac{\sqrt{1 + \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \text{Tan}[c]^2}}{\sqrt{1 + \text{Tan}[c]^2}} - \frac{\frac{\sin [d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{1 + \text{Tan}[c]^2}} \right) / \left( d (b + a \cos [c + d x])^3 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right)$$

**Problem 1307: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c + d x]^{7/2} (a + b \sec [c + d x])^3 (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 4, 277 leaves, 8 steps):

$$\begin{aligned} & \frac{1}{5 d} 2 (3 a^3 B + 15 a b^2 B + 5 b^3 (A - C) + 3 a^2 b (3 A + 5 C)) \text{EllipticE}\left[\frac{1}{2} (c + d x), 2\right] + \\ & \frac{1}{21 d} 2 (21 a^2 b B + 21 b^3 B + 21 a b^2 (A + 3 C) + a^3 (5 A + 7 C)) \text{EllipticF}\left[\frac{1}{2} (c + d x), 2\right] + \\ & \frac{1}{21 d} 2 a (21 a b B + 6 b^2 (3 A - 7 C) + a^2 (5 A + 7 C)) \sqrt{\cos [c + d x]} \sin [c + d x] + \\ & \frac{2 a^2 (11 A b + 7 a B - 35 b C) \cos [c + d x]^{3/2} \sin [c + d x]}{35 d} + \\ & \frac{2 a (A - 7 C) \sqrt{\cos [c + d x]} (b + a \cos [c + d x])^2 \sin [c + d x]}{7 d} + \frac{2 C (b + a \cos [c + d x])^3 \sin [c + d x]}{d \sqrt{\cos [c + d x]}} \end{aligned}$$

Result (type 5, 3915 leaves):

$$\begin{aligned} & \frac{1}{5 (b + a \cos [c + d x])^3 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])} \\ & 9 i a^2 A b \cos [c + d x]^5 \text{Csc}[c] (a + b \sec [c + d x])^3 (A + B \sec [c + d x] + C \sec [c + d x]^2) \\ & \left( \left( 2 e^{2 i d x} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2\right] \right. \right. \\ & \quad \left. \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) \right) / \\ & \quad (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) - \\ & \quad \left( 2 \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2\right] \right. \\ & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) \end{aligned}$$



$$\frac{\sqrt{1+e^{2ix} \cos[2c] + ie^{2ix} \sin[2c]}}{(-id(1+e^{2ix}) \cos[c] + d(-1+e^{2ix}) \sin[c]) + 1} \frac{(b+a \cos[c+dx])^3 (A+2C+2B \cos[c+dx] + A \cos[2c+2dx])}{iAb^3 \cos[c+dx]^5 \csc[c] (a+b \sec[c+dx])^3 (A+B \sec[c+dx] + C \sec[c+dx]^2) \left( \left( 2e^{2ix} \text{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix} (\cos[c] + i \sin[c])^2 \right] \sqrt{e^{-ix} (2(1+e^{2ix}) \cos[c] + 2i(-1+e^{2ix}) \sin[c])} \sqrt{1+e^{2ix} \cos[2c] + ie^{2ix} \sin[2c]} \right) / (3id(1+e^{2ix}) \cos[c] - 3d(-1+e^{2ix}) \sin[c]) - \left( 2 \text{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix} (\cos[c] + i \sin[c])^2 \right] \sqrt{e^{-ix} (2(1+e^{2ix}) \cos[c] + 2i(-1+e^{2ix}) \sin[c])} \sqrt{1+e^{2ix} \cos[2c] + ie^{2ix} \sin[2c]} \right) / (-id(1+e^{2ix}) \cos[c] + d(-1+e^{2ix}) \sin[c]) \right) + 1$$

$$\frac{5(b+a \cos[c+dx])^3 (A+2C+2B \cos[c+dx] + A \cos[2c+2dx])}{3ia^3 B \cos[c+dx]^5 \csc[c] (a+b \sec[c+dx])^3 (A+B \sec[c+dx] + C \sec[c+dx]^2) \left( \left( 2e^{2ix} \text{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix} (\cos[c] + i \sin[c])^2 \right] \sqrt{e^{-ix} (2(1+e^{2ix}) \cos[c] + 2i(-1+e^{2ix}) \sin[c])} \sqrt{1+e^{2ix} \cos[2c] + ie^{2ix} \sin[2c]} \right) / (3id(1+e^{2ix}) \cos[c] - 3d(-1+e^{2ix}) \sin[c]) - \left( 2 \text{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix} (\cos[c] + i \sin[c])^2 \right] \sqrt{e^{-ix} (2(1+e^{2ix}) \cos[c] + 2i(-1+e^{2ix}) \sin[c])} \sqrt{1+e^{2ix} \cos[2c] + ie^{2ix} \sin[2c]} \right) / (-id(1+e^{2ix}) \cos[c] + d(-1+e^{2ix}) \sin[c]) \right) + 1$$

$$\frac{(b+a \cos[c+dx])^3 (A+2C+2B \cos[c+dx] + A \cos[2c+2dx])}{3iab^2 B}$$

$$\frac{\begin{aligned} & \cos [c+d x]^5 \operatorname{Csc}[c] \\ & (a+b \operatorname{Sec}[c+d x])^3 \\ & (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \\ & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x}(\cos [c]+i \sin [c])^2\right] \right. \right. \\ & \quad \left. \left. \sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)} \right. \right. \\ & \quad \left. \left. \sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]} \right) / \right. \\ & \quad \left. \left( 3 i d\left(1+e^{2 i d x}\right) \cos [c]-3 d\left(-1+e^{2 i d x}\right) \sin [c]\right)- \right. \\ & \quad \left. \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x}(\cos [c]+i \sin [c])^2\right] \right. \right. \\ & \quad \left. \left. \sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)} \right. \right. \\ & \quad \left. \left. \sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]} \right) / \right. \\ & \quad \left. \left. \left. (-i d\left(1+e^{2 i d x}\right) \cos [c]+d\left(-1+e^{2 i d x}\right) \sin [c]\right) \right) \right) + \end{aligned}}{1}$$

$$\frac{\begin{aligned} & (b+a \cos [c+d x])^3 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \\ & 3 i a^2 b C \\ & \cos [c+d x]^5 \operatorname{Csc}[c] \\ & (a+b \operatorname{Sec}[c+d x])^3 \\ & (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \\ & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x}(\cos [c]+i \sin [c])^2\right] \right. \right. \\ & \quad \left. \left. \sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)} \right. \right. \\ & \quad \left. \left. \sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]} \right) / \right. \\ & \quad \left. \left( 3 i d\left(1+e^{2 i d x}\right) \cos [c]-3 d\left(-1+e^{2 i d x}\right) \sin [c]\right)- \right. \\ & \quad \left. \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x}(\cos [c]+i \sin [c])^2\right] \right. \right. \\ & \quad \left. \left. \sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)} \right. \right. \\ & \quad \left. \left. \sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]} \right) / \right. \\ & \quad \left. \left. \left. (-i d\left(1+e^{2 i d x}\right) \cos [c]+d\left(-1+e^{2 i d x}\right) \sin [c]\right) \right) \right) - \end{aligned}}{1}$$

$$\frac{\begin{aligned} & (b+a \cos [c+d x])^3 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \\ & i b^3 C \\ & \cos [c+d x]^5 \operatorname{Csc}[c] \\ & (a+b \operatorname{Sec}[c+d x])^3 \\ & (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \\ & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x}(\cos [c]+i \sin [c])^2\right] \right. \right. \\ & \quad \left. \left. \sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)} \right. \right. \end{aligned}}$$

$$\begin{aligned}
 & \left( \frac{\sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]}}{(3 i d (1 + e^{2 i d x}) \cos[c] - 3 d (-1 + e^{2 i d x}) \sin[c]) -} \right. \\
 & \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right. \\
 & \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])}}{\sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]}} \right) \left. \right) / \\
 & \left( -i d (1 + e^{2 i d x}) \cos[c] + d (-1 + e^{2 i d x}) \sin[c] \right) + \\
 & \frac{1}{(b + a \cos[c + d x])^3 (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x])} \\
 & \cos[c + d x]^{11/2} \\
 & (a + b \sec[c + d x])^3 \\
 & (A + B \sec[c + d x] + C \sec[c + d x]^2) \\
 & \left( -\frac{1}{5 d} 2 (9 a^2 A b + 5 A b^3 + 3 a^3 B + 15 a b^2 B + 15 a^2 b C - 10 b^3 C + 9 a^2 A b \cos[2 c] + 5 A b^3 \cos[2 c] + \right. \\
 & \quad \left. 3 a^3 B \cos[2 c] + 15 a b^2 B \cos[2 c] + 15 a^2 b C \cos[2 c]) \operatorname{Csc}[c] \operatorname{Sec}[c] + \right. \\
 & \quad \left. \frac{a (23 a^2 A + 84 A b^2 + 84 a b B + 28 a^2 C) \cos[d x] \sin[c]}{21 d} + \frac{2 a^2 (3 A b + a B) \cos[2 d x] \sin[2 c]}{5 d} + \right. \\
 & \quad \left. \frac{a^3 A \cos[3 d x] \sin[3 c]}{7 d} + \frac{a (23 a^2 A + 84 A b^2 + 84 a b B + 28 a^2 C) \cos[c] \sin[d x]}{21 d} + \right. \\
 & \quad \left. \frac{4 b^3 C \sec[c] \sec[c + d x] \sin[d x]}{d} + \right. \\
 & \quad \left. \frac{2 a^2 (3 A b + a B) \cos[2 c] \sin[2 d x]}{5 d} + \frac{a^3 A \cos[3 c] \sin[3 d x]}{7 d} \right) - \\
 & \left( 20 a^3 A \cos[c + d x]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right. \\
 & \quad (a + b \sec[c + d x])^3 (A + B \sec[c + d x] + C \sec[c + d x]^2) \\
 & \quad \operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \sin[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \quad \left. \frac{\sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin[c] \sin[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}}{\sqrt{1 + \sin[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) / \\
 & \left( 21 d (b + a \cos[c + d x])^3 (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2} \right) - \\
 & \left( 4 a A b^2 \cos[c + d x]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right. \\
 & \quad (a + b \sec[c + d x])^3 (A + B \sec[c + d x] + C \sec[c + d x]^2) \\
 & \quad \left. \operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \sin[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right)
 \end{aligned}$$

$$\left( \frac{\sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[d x - \text{ArcTan}[\cot[c]]]}}{\sqrt{1+\sin[d x - \text{ArcTan}[\cot[c]]]}} \right) /$$

$$\left( d (b+a \cos[c+d x])^3 (A+2 C+2 B \cos[c+d x]+A \cos[2 c+2 d x]) \sqrt{1+\cot[c]^2} \right) -$$

$$\left( 4 a^2 b B \cos[c+d x]^5 \csc[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[d x - \text{ArcTan}[\cot[c]]]^2\right] \right)^2$$

$$\frac{(a+b \sec[c+d x])^3 (A+B \sec[c+d x]+C \sec[c+d x]^2)}{\sec[d x - \text{ArcTan}[\cot[c]]] \sqrt{1-\sin[d x - \text{ArcTan}[\cot[c]]]}}$$

$$\left( \frac{\sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[d x - \text{ArcTan}[\cot[c]]]} \sqrt{1+\sin[d x - \text{ArcTan}[\cot[c]]]}}{\sqrt{1+\sin[d x - \text{ArcTan}[\cot[c]]]}} \right) /$$

$$\left( d (b+a \cos[c+d x])^3 (A+2 C+2 B \cos[c+d x]+A \cos[2 c+2 d x]) \sqrt{1+\cot[c]^2} \right) -$$

$$\left( 4 b^3 B \cos[c+d x]^5 \csc[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[d x - \text{ArcTan}[\cot[c]]]^2\right] \right)^2$$

$$\frac{(a+b \sec[c+d x])^3 (A+B \sec[c+d x]+C \sec[c+d x]^2)}{\sec[d x - \text{ArcTan}[\cot[c]]] \sqrt{1-\sin[d x - \text{ArcTan}[\cot[c]]]}}$$

$$\left( \frac{\sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[d x - \text{ArcTan}[\cot[c]]]} \sqrt{1+\sin[d x - \text{ArcTan}[\cot[c]]]}}{\sqrt{1+\sin[d x - \text{ArcTan}[\cot[c]]]}} \right) /$$

$$\left( d (b+a \cos[c+d x])^3 (A+2 C+2 B \cos[c+d x]+A \cos[2 c+2 d x]) \sqrt{1+\cot[c]^2} \right) -$$

$$\left( 4 a^3 C \cos[c+d x]^5 \csc[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[d x - \text{ArcTan}[\cot[c]]]^2\right] \right)^2$$

$$\frac{(a+b \sec[c+d x])^3 (A+B \sec[c+d x]+C \sec[c+d x]^2)}{\sec[d x - \text{ArcTan}[\cot[c]]] \sqrt{1-\sin[d x - \text{ArcTan}[\cot[c]]]}}$$

$$\left( \frac{\sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[d x - \text{ArcTan}[\cot[c]]]} \sqrt{1+\sin[d x - \text{ArcTan}[\cot[c]]]}}{\sqrt{1+\sin[d x - \text{ArcTan}[\cot[c]]]}} \right) /$$

$$\left( 3 d (b+a \cos[c+d x])^3 (A+2 C+2 B \cos[c+d x]+A \cos[2 c+2 d x]) \sqrt{1+\cot[c]^2} \right) -$$

$$\left( 12 a b^2 C \cos[c+d x]^5 \csc[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[d x - \text{ArcTan}[\cot[c]]]^2\right] \right)^2$$

$$\frac{(a+b \sec[c+d x])^3 (A+B \sec[c+d x]+C \sec[c+d x]^2)}{\sec[d x - \text{ArcTan}[\cot[c]]] \sqrt{1-\sin[d x - \text{ArcTan}[\cot[c]]]}}$$

$$\left. \sqrt{-\sqrt{1+\cot^2[c]} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]} \sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]}\right) /$$

$$\left( d (b + a \cos[c + dx])^3 (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{1 + \cot^2[c]^2} \right)$$

**Problem 1308: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c + dx]^{5/2} (a + b \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2) dx$$

Optimal (type 4, 267 leaves, 8 steps):

$$\frac{1}{5d} 2 (15 a^2 b B - 5 b^3 B + 15 a b^2 (A - C) + a^3 (3A + 5C)) \text{EllipticE}\left[\frac{1}{2}(c + dx), 2\right] +$$

$$\frac{1}{3d} 2 (a^3 B + 9 a b^2 B + b^3 (3A + C) + 3 a^2 b (A + 3C)) \text{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] +$$

$$\frac{2 a (a^2 B - 6 b^2 B + 3 a b (A - 5C)) \sqrt{\cos[c + dx]} \sin[c + dx]}{3 d} +$$

$$\frac{2 a^2 (3 a A - 15 b B - 35 a C) \cos[c + dx]^{3/2} \sin[c + dx]}{15 d} +$$

$$\frac{2 (b B + 2 a C) (b + a \cos[c + dx])^2 \sin[c + dx]}{d \sqrt{\cos[c + dx]}} + \frac{2 C (b + a \cos[c + dx])^3 \sin[c + dx]}{3 d \cos[c + dx]^{3/2}}$$

Result (type 5, 3868 leaves):

$$\frac{1}{5 (b + a \cos[c + dx])^3 (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])}$$

$$3 i a^3 A \cos[c + dx]^5 \csc[c] (a + b \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2)$$

$$\left( \left( 2 e^{2 i dx} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i dx} (\cos[c] + i \sin[c])^2\right] \right. \right.$$

$$\left. \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \cos[c] + 2 i (-1 + e^{2 i dx}) \sin[c])}}{\sqrt{1 + e^{2 i dx} \cos[2c] + i e^{2 i dx} \sin[2c]}} \right) /$$

$$(3 i d (1 + e^{2 i dx}) \cos[c] - 3 d (-1 + e^{2 i dx}) \sin[c]) -$$

$$\left( 2 \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i dx} (\cos[c] + i \sin[c])^2\right] \right.$$

$$\left. \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \cos[c] + 2 i (-1 + e^{2 i dx}) \sin[c])}}{\sqrt{1 + e^{2 i dx} \cos[2c] + i e^{2 i dx} \sin[2c]}} \right) /$$

$$\left. (-i d (1 + e^{2 i dx}) \cos[c] + d (-1 + e^{2 i dx}) \sin[c]) \right) +$$

$$\frac{1}{(b + a \cos[c + dx])^3 (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])}$$

$$3 i a A b^2$$

$$\cos[c + dx]^5 \csc[c]$$

$$\begin{aligned}
 & (a + b \operatorname{Sec}[c + d x])^3 \\
 & (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right. \right. \\
 & \quad \left. \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]}} \right) \right) / \\
 & \quad (3 i d (1 + e^{2 i d x}) \operatorname{Cos}[c] - 3 d (-1 + e^{2 i d x}) \operatorname{Sin}[c]) - \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right) \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2 i d x}) \operatorname{Cos}[c] + d (-1 + e^{2 i d x}) \operatorname{Sin}[c]) \right) + \\
 & \qquad \qquad \qquad 1
 \end{aligned}$$

$$\begin{aligned}
 & (b + a \operatorname{Cos}[c + d x])^3 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \\
 & 3 i a^2 b B \\
 & \operatorname{Cos}[c + d x]^5 \operatorname{Csc}[c] \\
 & (a + b \operatorname{Sec}[c + d x])^3 \\
 & (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right) \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]}} \right) / \\
 & \quad (3 i d (1 + e^{2 i d x}) \operatorname{Cos}[c] - 3 d (-1 + e^{2 i d x}) \operatorname{Sin}[c]) - \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right) \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2 i d x}) \operatorname{Cos}[c] + d (-1 + e^{2 i d x}) \operatorname{Sin}[c]) \right) - \\
 & \qquad \qquad \qquad 1
 \end{aligned}$$

$$\begin{aligned}
 & (b + a \operatorname{Cos}[c + d x])^3 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \\
 & i b^3 B \operatorname{Cos}[c + d x]^5 \\
 & \operatorname{Csc}[c] (a + b \operatorname{Sec}[c + d x])^3 \\
 & (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right) \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]}} \right) / \\
 & \quad (3 i d (1 + e^{2 i d x}) \operatorname{Cos}[c] - 3 d (-1 + e^{2 i d x}) \operatorname{Sin}[c]) -
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \\
 & \quad \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \\
 & \quad \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \\
 & \quad \left( -i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c] \right) + \\
 & \quad \frac{1}{(b + a \cos [c + d x])^3 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])} \\
 & \quad i a^3 C \cos [c + d x]^5 \\
 & \quad \operatorname{Csc}[c] (a + b \operatorname{Sec}[c + d x])^3 \\
 & \quad (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\
 & \quad \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right) \right. \\
 & \quad \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \\
 & \quad \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \\
 & \quad (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) - \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \\
 & \quad \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \\
 & \quad \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \\
 & \quad \left. \left( -i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c] \right) \right) - \\
 & \quad \frac{1}{(b + a \cos [c + d x])^3 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])} \\
 & \quad 3 i a b^2 C \\
 & \quad \cos [c + d x]^5 \operatorname{Csc}[c] \\
 & \quad (a + b \operatorname{Sec}[c + d x])^3 \\
 & \quad (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\
 & \quad \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right) \right. \\
 & \quad \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \\
 & \quad \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \\
 & \quad (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) - \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \\
 & \quad \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \\
 & \quad \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \\
 & \quad \left. \left( -i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c] \right) \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{(b + a \cos [c + d x])^3 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])} \\
 & \cos [c + d x]^{11/2} \\
 & (a + b \sec [c + d x])^3 \\
 & (A + B \sec [c + d x] + C \sec [c + d x]^2) \\
 & \left( -\frac{1}{5 d} 2 (3 a^3 A + 15 a A b^2 + 15 a^2 b B - 10 b^3 B + 5 a^3 C - 30 a b^2 C + 3 a^3 A \cos [2 c] + \right. \\
 & \quad \left. 15 a A b^2 \cos [2 c] + 15 a^2 b B \cos [2 c] + 5 a^3 C \cos [2 c]) \csc [c] \sec [c] + \right. \\
 & \quad \frac{4 a^2 (3 A b + a B) \cos [d x] \sin [c]}{3 d} + \frac{2 a^3 A \cos [2 d x] \sin [2 c]}{5 d} + \\
 & \quad \frac{4 a^2 (3 A b + a B) \cos [c] \sin [d x]}{3 d} + \frac{4 b^3 C \sec [c] \sec [c + d x]^2 \sin [d x]}{3 d} + \\
 & \quad \left. \frac{1}{3 d} 4 \sec [c] \sec [c + d x] (b^3 C \sin [c] + 3 b^3 B \sin [d x] + 9 a b^2 C \sin [d x]) + \right. \\
 & \quad \left. \frac{2 a^3 A \cos [2 c] \sin [2 d x]}{5 d} \right) - \\
 & \left( 4 a^2 A b \cos [c + d x]^5 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\cot [c]]]\right]^2 \right) \\
 & \frac{(a + b \sec [c + d x])^3 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sec [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\cot [c]]]}} \\
 & \frac{\sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\cot [c]]]}}{\sqrt{1 + \sin [d x - \operatorname{ArcTan}[\cot [c]]]}} \Bigg) / \\
 & \left( d (b + a \cos [c + d x])^3 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} \right) - \\
 & \left( 4 A b^3 \cos [c + d x]^5 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\cot [c]]]\right]^2 \right) \\
 & \frac{(a + b \sec [c + d x])^3 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sec [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\cot [c]]]}} \\
 & \frac{\sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\cot [c]]]}}{\sqrt{1 + \sin [d x - \operatorname{ArcTan}[\cot [c]]]}} \Bigg) / \\
 & \left( d (b + a \cos [c + d x])^3 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} \right) - \\
 & \left( 4 a^3 B \cos [c + d x]^5 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\cot [c]]]\right]^2 \right)
 \end{aligned}$$



$$\begin{aligned}
 & \left( \frac{(a + b \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right. \\
 & \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right) / \\
 & \left( 3 d (b + a \operatorname{Cos}[c + d x])^3 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2} \right) - \\
 & \left( 12 a b^2 B \operatorname{Cos}[c + d x]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right) \\
 & \left( \frac{(a + b \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right. \\
 & \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right) / \\
 & \left( d (b + a \operatorname{Cos}[c + d x])^3 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2} \right) - \\
 & \left( 12 a^2 b C \operatorname{Cos}[c + d x]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right) \\
 & \left( \frac{(a + b \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right. \\
 & \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right) / \\
 & \left( d (b + a \operatorname{Cos}[c + d x])^3 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2} \right) - \\
 & \left( 4 b^3 C \operatorname{Cos}[c + d x]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right) \\
 & \left( \frac{(a + b \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right. \\
 & \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right) / \\
 & \left( 3 d (b + a \operatorname{Cos}[c + d x])^3 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2} \right)
 \end{aligned}$$

**Problem 1309: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \operatorname{Cos}[c + d x]^{3/2} (a + b \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 4, 274 leaves, 8 steps):

$$\begin{aligned} & \frac{1}{5d} 2 (5 a^3 B - 15 a b^2 B + 15 a^2 b (A - C) - b^3 (5 A + 3 C)) \text{EllipticE}\left[\frac{1}{2} (c + d x), 2\right] + \\ & \frac{1}{3d} 2 (9 a^2 b B + b^3 B + 3 a b^2 (3 A + C) + a^3 (A + 3 C)) \text{EllipticF}\left[\frac{1}{2} (c + d x), 2\right] + \\ & \frac{2 b (15 A b^2 + 35 a b B + 24 a^2 C + 9 b^2 C) \text{Sin}[c + d x]}{15 d \sqrt{\text{Cos}[c + d x]}} + \\ & \frac{2 a^2 (5 a A - 5 b B - 9 a C) \sqrt{\text{Cos}[c + d x]} \text{Sin}[c + d x]}{15 d} + \\ & \frac{2 (5 b B + 6 a C) (b + a \text{Cos}[c + d x])^2 \text{Sin}[c + d x]}{15 d \text{Cos}[c + d x]^{3/2}} + \frac{2 C (b + a \text{Cos}[c + d x])^3 \text{Sin}[c + d x]}{5 d \text{Cos}[c + d x]^{5/2}} \end{aligned}$$

Result (type 5, 3871 leaves):

$$\begin{aligned} & \frac{1}{(b + a \text{Cos}[c + d x])^3 (A + 2 C + 2 B \text{Cos}[c + d x] + A \text{Cos}[2 c + 2 d x])} \\ & 3 i a^2 A b \text{Cos}[c + d x]^5 \text{Csc}[c] (a + b \text{Sec}[c + d x])^3 (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) \\ & \left( \left( 2 e^{2 i d x} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\text{Cos}[c] + i \text{Sin}[c])^2\right] \right. \right. \\ & \quad \left. \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \text{Cos}[c] + 2 i (-1 + e^{2 i d x}) \text{Sin}[c])}}{\sqrt{1 + e^{2 i d x} \text{Cos}[2 c] + i e^{2 i d x} \text{Sin}[2 c]}} \right) \right) / \\ & \quad (3 i d (1 + e^{2 i d x}) \text{Cos}[c] - 3 d (-1 + e^{2 i d x}) \text{Sin}[c]) - \\ & \quad \left( 2 \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\text{Cos}[c] + i \text{Sin}[c])^2\right] \right. \\ & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \text{Cos}[c] + 2 i (-1 + e^{2 i d x}) \text{Sin}[c])}}{\sqrt{1 + e^{2 i d x} \text{Cos}[2 c] + i e^{2 i d x} \text{Sin}[2 c]}} \right) \right) / \\ & \quad \left. (-i d (1 + e^{2 i d x}) \text{Cos}[c] + d (-1 + e^{2 i d x}) \text{Sin}[c]) \right) - \\ & \frac{1}{(b + a \text{Cos}[c + d x])^3 (A + 2 C + 2 B \text{Cos}[c + d x] + A \text{Cos}[2 c + 2 d x])} \\ & i A b^3 \\ & \text{Cos}[c + d x]^5 \text{Csc}[c] \\ & (a + b \text{Sec}[c + d x])^3 \\ & (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) \\ & \left( \left( 2 e^{2 i d x} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\text{Cos}[c] + i \text{Sin}[c])^2\right] \right. \right. \\ & \quad \left. \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \text{Cos}[c] + 2 i (-1 + e^{2 i d x}) \text{Sin}[c])}}{\sqrt{1 + e^{2 i d x} \text{Cos}[2 c] + i e^{2 i d x} \text{Sin}[2 c]}} \right) \right) / \\ & \quad (3 i d (1 + e^{2 i d x}) \text{Cos}[c] - 3 d (-1 + e^{2 i d x}) \text{Sin}[c]) - \\ & \quad \left( 2 \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\text{Cos}[c] + i \text{Sin}[c])^2\right] \right. \\ & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \text{Cos}[c] + 2 i (-1 + e^{2 i d x}) \text{Sin}[c])}}{\sqrt{1 + e^{2 i d x} \text{Cos}[2 c] + i e^{2 i d x} \text{Sin}[2 c]}} \right) \right) \end{aligned}$$

$$\frac{\sqrt{1+e^{2ix} \cos[2c] + ie^{2ix} \sin[2c]}}{(-id(1+e^{2ix}) \cos[c] + d(-1+e^{2ix}) \sin[c]) + 1}$$


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$$\frac{(b+a \cos[c+dx])^3 (A+2C+2B \cos[c+dx] + A \cos[2c+2dx])}{ia^3 B \cos[c+dx]^5 \csc[c] (a+b \sec[c+dx])^3 (A+B \sec[c+dx] + C \sec[c+dx]^2) \left( \left( 2e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix}(\cos[c] + i \sin[c])^2\right] \right) \frac{\sqrt{e^{-ix}(2(1+e^{2ix}) \cos[c] + 2i(-1+e^{2ix}) \sin[c])}}{\sqrt{1+e^{2ix} \cos[2c] + ie^{2ix} \sin[2c]}} \right) / \left( 3id(1+e^{2ix}) \cos[c] - 3d(-1+e^{2ix}) \sin[c] \right) - \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix}(\cos[c] + i \sin[c])^2\right] \right) \frac{\sqrt{e^{-ix}(2(1+e^{2ix}) \cos[c] + 2i(-1+e^{2ix}) \sin[c])}}{\sqrt{1+e^{2ix} \cos[2c] + ie^{2ix} \sin[2c]}} \right) / \left( -id(1+e^{2ix}) \cos[c] + d(-1+e^{2ix}) \sin[c] \right) - 1}$$

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$$\frac{(b+a \cos[c+dx])^3 (A+2C+2B \cos[c+dx] + A \cos[2c+2dx])}{3iab^2 B \cos[c+dx]^5 \csc[c] (a+b \sec[c+dx])^3 (A+B \sec[c+dx] + C \sec[c+dx]^2) \left( \left( 2e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix}(\cos[c] + i \sin[c])^2\right] \right) \frac{\sqrt{e^{-ix}(2(1+e^{2ix}) \cos[c] + 2i(-1+e^{2ix}) \sin[c])}}{\sqrt{1+e^{2ix} \cos[2c] + ie^{2ix} \sin[2c]}} \right) / \left( 3id(1+e^{2ix}) \cos[c] - 3d(-1+e^{2ix}) \sin[c] \right) - \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix}(\cos[c] + i \sin[c])^2\right] \right) \frac{\sqrt{e^{-ix}(2(1+e^{2ix}) \cos[c] + 2i(-1+e^{2ix}) \sin[c])}}{\sqrt{1+e^{2ix} \cos[2c] + ie^{2ix} \sin[2c]}} \right) / \left( -id(1+e^{2ix}) \cos[c] + d(-1+e^{2ix}) \sin[c] \right) - 1}$$

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$$\frac{(b+a \cos[c+dx])^3 (A+2C+2B \cos[c+dx] + A \cos[2c+2dx])}{3ia^2 b C}$$

$$\begin{aligned}
 & \frac{\cos [c+d x]^5 \operatorname{Csc}[c]}{(a+b \operatorname{Sec}[c+d x])^3} \\
 & (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x}(\cos [c]+i \sin [c])^2\right] \right. \right. \\
 & \quad \left. \left. \frac{\sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}} \right) \right) / \\
 & \quad \left( 3 i d\left(1+e^{2 i d x}\right) \cos [c]-3 d\left(-1+e^{2 i d x}\right) \sin [c]\right)- \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x}(\cos [c]+i \sin [c])^2\right] \right) \\
 & \quad \frac{\sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \quad \left. \left. \left(-i d\left(1+e^{2 i d x}\right) \cos [c]+d\left(-1+e^{2 i d x}\right) \sin [c]\right)\right) \right) - \\
 & \quad 1 \\
 & \frac{5(b+a \cos [c+d x])^3(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])}{3 i b^3 C} \\
 & \frac{\cos [c+d x]^5 \operatorname{Csc}[c]}{(a+b \operatorname{Sec}[c+d x])^3} \\
 & (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x}(\cos [c]+i \sin [c])^2\right] \right) \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \quad \left( 3 i d\left(1+e^{2 i d x}\right) \cos [c]-3 d\left(-1+e^{2 i d x}\right) \sin [c]\right)- \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x}(\cos [c]+i \sin [c])^2\right] \right) \\
 & \quad \frac{\sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)}}{\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \quad \left. \left. \left(-i d\left(1+e^{2 i d x}\right) \cos [c]+d\left(-1+e^{2 i d x}\right) \sin [c]\right)\right) \right) + \\
 & \quad 1 \\
 & \frac{(b+a \cos [c+d x])^3(A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])}{\cos [c+d x]^{11 / 2}} \\
 & (a+b \operatorname{Sec}[c+d x])^3 \\
 & (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \\
 & \left( -\frac{1}{5 d} 2\left(15 a^2 A b-10 A b^3+5 a^3 B-30 a b^2 B-30 a^2 b C-\right. \right. \\
 & \quad \left. \left. 6 b^3 C+15 a^2 A b \cos [2 c]+5 a^3 B \cos [2 c]\right) \operatorname{Csc}[c] \operatorname{Sec}[c]+ \right. \\
 & \quad \left. \frac{4 a^3 A \cos [d x] \sin [c]}{3 d}+\frac{4 a^3 A \cos [c] \sin [d x]}{3 d}+\frac{4 b^3 C \operatorname{Sec}[c] \operatorname{Sec}[c+d x]^3 \sin [d x]}{5 d} \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{15d} 4 \operatorname{Sec}[c] \operatorname{Sec}[c+dx]^2 (3b^3 C \sin[c] + 5b^3 B \sin[dx] + 15a^2 C \sin[dx]) + \\
 & \frac{1}{15d} 4 \operatorname{Sec}[c] \operatorname{Sec}[c+dx] (5b^3 B \sin[c] + 15a^2 C \sin[c] + \\
 & \quad 15Ab^3 \sin[dx] + 45a^2 B \sin[dx] + 45a^2 b C \sin[dx] + 9b^3 C \sin[dx]) \Big) - \\
 & \left( 4a^3 A \operatorname{Cos}[c+dx]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right. \\
 & \quad \frac{(a+b \operatorname{Sec}[c+dx])^3 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2)}{\operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \quad \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \quad \left. \sqrt{1 + \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) / \\
 & \left( 3d (b+a \operatorname{Cos}[c+dx])^3 (A+2C+2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) \sqrt{1 + \operatorname{Cot}[c]^2} \right) - \\
 & \left( 12aAb^2 \operatorname{Cos}[c+dx]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right. \\
 & \quad \frac{(a+b \operatorname{Sec}[c+dx])^3 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2)}{\operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \quad \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \quad \left. \sqrt{1 + \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) / \\
 & \left( d (b+a \operatorname{Cos}[c+dx])^3 (A+2C+2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) \sqrt{1 + \operatorname{Cot}[c]^2} \right) - \\
 & \left( 12a^2 b B \operatorname{Cos}[c+dx]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right. \\
 & \quad \frac{(a+b \operatorname{Sec}[c+dx])^3 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2)}{\operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \quad \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \sqrt{1 + \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) / \\
 & \left( d (b+a \operatorname{Cos}[c+dx])^3 (A+2C+2B \operatorname{Cos}[c+dx] + A \operatorname{Cos}[2c+2dx]) \sqrt{1 + \operatorname{Cot}[c]^2} \right) - \\
 & \left( 4b^3 B \operatorname{Cos}[c+dx]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right. \\
 & \quad \left. (a+b \operatorname{Sec}[c+dx])^3 (A+B \operatorname{Sec}[c+dx] + C \operatorname{Sec}[c+dx]^2) \right)
 \end{aligned}$$

$$\left( \frac{\sec [d x - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \sin [d x - \text{ArcTan}[\text{Cot}[c]]]}}{\sqrt{-\sqrt{1 + \text{Cot}[c]^2} \sin [c] \sin [d x - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 + \sin [d x - \text{ArcTan}[\text{Cot}[c]]]}}} \right) /$$

$$\left( 3 d (b + a \cos [c + d x])^3 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \text{Cot}[c]^2} - \right.$$

$$\left. 4 a^3 C \cos [c + d x]^5 \text{Csc}[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \text{ArcTan}[\text{Cot}[c]]]^2\right] \right.$$

$$\left. \frac{(a + b \sec [c + d x])^3 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sec [d x - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \sin [d x - \text{ArcTan}[\text{Cot}[c]]]}} \right.$$

$$\left. \frac{\sqrt{-\sqrt{1 + \text{Cot}[c]^2} \sin [c] \sin [d x - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 + \sin [d x - \text{ArcTan}[\text{Cot}[c]]]}}}{\sqrt{-\sqrt{1 + \text{Cot}[c]^2} \sin [c] \sin [d x - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 + \sin [d x - \text{ArcTan}[\text{Cot}[c]]]}}} \right) /$$

$$\left( d (b + a \cos [c + d x])^3 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \text{Cot}[c]^2} - \right.$$

$$\left. 4 a b^2 C \cos [c + d x]^5 \text{Csc}[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \text{ArcTan}[\text{Cot}[c]]]^2\right] \right.$$

$$\left. \frac{(a + b \sec [c + d x])^3 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sec [d x - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \sin [d x - \text{ArcTan}[\text{Cot}[c]]]}} \right.$$

$$\left. \frac{\sqrt{-\sqrt{1 + \text{Cot}[c]^2} \sin [c] \sin [d x - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 + \sin [d x - \text{ArcTan}[\text{Cot}[c]]]}}}{\sqrt{-\sqrt{1 + \text{Cot}[c]^2} \sin [c] \sin [d x - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 + \sin [d x - \text{ArcTan}[\text{Cot}[c]]]}}} \right) /$$

$$\left( d (b + a \cos [c + d x])^3 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \text{Cot}[c]^2} \right)$$

**Problem 1310: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sqrt{\cos [c + d x]} (a + b \sec [c + d x])^3 (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 4, 294 leaves, 8 steps):

$$-\frac{1}{5d} 2 (15 a^2 b B + 3 b^3 B - 5 a^3 (A - C) + 3 a b^2 (5 A + 3 C)) \text{EllipticE}\left[\frac{1}{2} (c + d x), 2\right] +$$

$$\frac{1}{21d} 2 (21 a^3 B + 21 a b^2 B + 21 a^2 b (3 A + C) + b^3 (7 A + 5 C)) \text{EllipticF}\left[\frac{1}{2} (c + d x), 2\right] +$$

$$\frac{2 b (35 A b^2 + 63 a b B + 24 a^2 C + 25 b^2 C) \sin [c + d x]}{105 d \cos [c + d x]^{3/2}} +$$

$$\frac{2 (98 a^2 b B + 21 b^3 B + 24 a^3 C + 21 a b^2 (5 A + 3 C)) \sin [c + d x]}{35 d \sqrt{\cos [c + d x]}} +$$

$$\frac{2 (7 b B + 6 a C) (b + a \cos [c + d x])^2 \sin [c + d x]}{35 d \cos [c + d x]^{5/2}} + \frac{2 C (b + a \cos [c + d x])^3 \sin [c + d x]}{7 d \cos [c + d x]^{7/2}}$$

Result (type 5, 3933 leaves):

$$\frac{1}{(b + a \cos [c + d x])^3 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])} \\ \frac{i a^3 A \cos [c + d x]^5 \operatorname{Csc}[c] (a + b \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])\right]^2 \right. \right. \\ \left. \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \right. \right. \\ \left. \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) \right) / \\ (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) - \\ \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])\right]^2 \right) \\ \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \right. \\ \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \\ \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) -$$

1

$$\frac{1}{(b + a \cos [c + d x])^3 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])} \\ \frac{3 i a A b^2 \cos [c + d x]^5 \operatorname{Csc}[c] (a + b \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])\right]^2 \right. \right. \\ \left. \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \right. \right. \\ \left. \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) \right) / \\ (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) - \\ \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])\right]^2 \right) \\ \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \right. \\ \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \\ \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) -$$

1

$$\frac{1}{(b + a \cos [c + d x])^3 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])} \\ \frac{3 i a^2 b B \cos [c + d x]^5 \operatorname{Csc}[c] (a + b \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])\right]^2 \right. \right. \\ \left. \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \right. \right. \\ \left. \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) \right) / \\ (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) - \\ \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])\right]^2 \right) \\ \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \right. \\ \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \\ \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) -$$

$$\begin{aligned}
 & \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \cos [c] + 2 i (-1 + e^{2 i dx}) \sin [c])}}{\sqrt{1 + e^{2 i dx} \cos [2 c] + i e^{2 i dx} \sin [2 c]}} \Big/ \\
 & \left( 3 i d (1 + e^{2 i dx}) \cos [c] - 3 d (-1 + e^{2 i dx}) \sin [c] \right) - \\
 & \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i dx} (\cos [c] + i \sin [c])^2 \right] \right) \\
 & \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \cos [c] + 2 i (-1 + e^{2 i dx}) \sin [c])}}{\sqrt{1 + e^{2 i dx} \cos [2 c] + i e^{2 i dx} \sin [2 c]}} \Big/ \\
 & \left( -i d (1 + e^{2 i dx}) \cos [c] + d (-1 + e^{2 i dx}) \sin [c] \right) - \\
 & \frac{1}{5 (b + a \cos [c + d x])^3 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])} \\
 & 3 i b^3 B \cos [c + d x]^5 \\
 & \operatorname{Csc}[c] (a + b \operatorname{Sec}[c + d x])^3 \\
 & (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\
 & \left( \left( 2 e^{2 i dx} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i dx} (\cos [c] + i \sin [c])^2 \right] \right) \right. \\
 & \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \cos [c] + 2 i (-1 + e^{2 i dx}) \sin [c])}}{\sqrt{1 + e^{2 i dx} \cos [2 c] + i e^{2 i dx} \sin [2 c]}} \Big/ \\
 & \left. \left( 3 i d (1 + e^{2 i dx}) \cos [c] - 3 d (-1 + e^{2 i dx}) \sin [c] \right) - \right. \\
 & \left. \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i dx} (\cos [c] + i \sin [c])^2 \right] \right) \right) \\
 & \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \cos [c] + 2 i (-1 + e^{2 i dx}) \sin [c])}}{\sqrt{1 + e^{2 i dx} \cos [2 c] + i e^{2 i dx} \sin [2 c]}} \Big/ \\
 & \left. \left( -i d (1 + e^{2 i dx}) \cos [c] + d (-1 + e^{2 i dx}) \sin [c] \right) \right) - \\
 & \frac{1}{(b + a \cos [c + d x])^3 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])} \\
 & i a^3 C \cos [c + d x]^5 \\
 & \operatorname{Csc}[c] (a + b \operatorname{Sec}[c + d x])^3 \\
 & (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\
 & \left( \left( 2 e^{2 i dx} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i dx} (\cos [c] + i \sin [c])^2 \right] \right) \right. \\
 & \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \cos [c] + 2 i (-1 + e^{2 i dx}) \sin [c])}}{\sqrt{1 + e^{2 i dx} \cos [2 c] + i e^{2 i dx} \sin [2 c]}} \Big/ \\
 & \left. \left( 3 i d (1 + e^{2 i dx}) \cos [c] - 3 d (-1 + e^{2 i dx}) \sin [c] \right) - \right. \\
 & \left. \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i dx} (\cos [c] + i \sin [c])^2 \right] \right) \right) \\
 & \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \cos [c] + 2 i (-1 + e^{2 i dx}) \sin [c])}}{\sqrt{1 + e^{2 i dx} \cos [2 c] + i e^{2 i dx} \sin [2 c]}} \Big/
 \end{aligned}$$



$$\begin{aligned}
 & \left( \frac{\sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]}}{(-i d (1 + e^{2 i d x}) \cos[c] + d (-1 + e^{2 i d x}) \sin[c])} - \right. \\
 & \quad \left. \frac{1}{5 (b + a \cos[c + d x])^3 (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x])} \right. \\
 & \quad 9 i a b^2 C \\
 & \quad \cos[c + d x]^5 \operatorname{Csc}[c] \\
 & \quad (a + b \operatorname{Sec}[c + d x])^3 \\
 & \quad (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\
 & \quad \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])}}{\sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]}} \right) / \\
 & \quad \left. (3 i d (1 + e^{2 i d x}) \cos[c] - 3 d (-1 + e^{2 i d x}) \sin[c]) - \right. \\
 & \quad \left. \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])}}{\sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2 i d x}) \cos[c] + d (-1 + e^{2 i d x}) \sin[c]) \right) + \\
 & \quad \left. \frac{1}{(b + a \cos[c + d x])^3 (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x])} \right. \\
 & \quad \cos[c + d x]^{11/2} \\
 & \quad (a + b \operatorname{Sec}[c + d x])^3 \\
 & \quad (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\
 & \quad \left( -\frac{1}{5 d} (5 a^3 A - 30 a A b^2 - 30 a^2 b B - 6 b^3 B - 10 a^3 C - 18 a b^2 C + 5 a^3 A \cos[2 c]) \operatorname{Csc}[c] \operatorname{Sec}[c] + \right. \\
 & \quad \frac{4 b^3 C \operatorname{Sec}[c] \operatorname{Sec}[c + d x]^4 \sin[d x]}{7 d} + \frac{1}{35 d} 4 \operatorname{Sec}[c] \operatorname{Sec}[c + d x]^3 \\
 & \quad (5 b^3 C \sin[c] + 7 b^3 B \sin[d x] + 21 a b^2 C \sin[d x]) + \frac{1}{105 d} 4 \operatorname{Sec}[c] \operatorname{Sec}[c + d x] \\
 & \quad (35 A b^3 \sin[c] + 105 a b^2 B \sin[c] + 105 a^2 b C \sin[c] + 25 b^3 C \sin[c] + 315 a A b^2 \sin[d x] + \\
 & \quad 315 a^2 b B \sin[d x] + 63 b^3 B \sin[d x] + 105 a^3 C \sin[d x] + 189 a b^2 C \sin[d x]) + \\
 & \quad \frac{1}{105 d} 4 \operatorname{Sec}[c] \operatorname{Sec}[c + d x]^2 (21 b^3 B \sin[c] + 63 a b^2 C \sin[c] + 35 A b^3 \sin[d x] + \\
 & \quad \left. 105 a b^2 B \sin[d x] + 105 a^2 b C \sin[d x] + 25 b^3 C \sin[d x]) \right) - \\
 & \quad \left( 12 a^2 A b \cos[c + d x]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right. \\
 & \quad \left. (a + b \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \quad \left. \operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \sin[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{\sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]}}{\sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]}} \right) / \\
 & \left( d (b + a \cos[c + dx])^3 (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{1 + \cot[c]^2} \right) - \\
 & \left( 4 A b^3 \cos[c + dx]^5 \csc[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\cot[c]]]^2\right] \right) \\
 & \frac{(a + b \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2)}{\sec[dx - \text{ArcTan}[\cot[c]]] \sqrt{1 - \sin[dx - \text{ArcTan}[\cot[c]]]}} \\
 & \left. \frac{\sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]}}{\sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]}} \right) / \\
 & \left( 3 d (b + a \cos[c + dx])^3 (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{1 + \cot[c]^2} \right) - \\
 & \left( 4 a^3 B \cos[c + dx]^5 \csc[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\cot[c]]]^2\right] \right) \\
 & \frac{(a + b \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2)}{\sec[dx - \text{ArcTan}[\cot[c]]] \sqrt{1 - \sin[dx - \text{ArcTan}[\cot[c]]]}} \\
 & \left. \frac{\sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]] \sqrt{1 + \sin[dx - \text{ArcTan}[\cot[c]]]}}}{\sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]}} \right) / \\
 & \left( d (b + a \cos[c + dx])^3 (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{1 + \cot[c]^2} \right) - \\
 & \left( 4 a b^2 B \cos[c + dx]^5 \csc[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\cot[c]]]^2\right] \right) \\
 & \frac{(a + b \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2)}{\sec[dx - \text{ArcTan}[\cot[c]]] \sqrt{1 - \sin[dx - \text{ArcTan}[\cot[c]]]}} \\
 & \left. \frac{\sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]] \sqrt{1 + \sin[dx - \text{ArcTan}[\cot[c]]]}}}{\sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]}} \right) / \\
 & \left( d (b + a \cos[c + dx])^3 (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx]) \sqrt{1 + \cot[c]^2} \right) - \\
 & \left( 4 a^2 b C \cos[c + dx]^5 \csc[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\cot[c]]]^2\right] \right) \\
 & \frac{(a + b \sec[c + dx])^3 (A + B \sec[c + dx] + C \sec[c + dx]^2)}{\sec[dx - \text{ArcTan}[\cot[c]]] \sqrt{1 - \sin[dx - \text{ArcTan}[\cot[c]]]}}
 \end{aligned}$$

$$\left. \sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[d x - \text{ArcTan}[\cot[c]]]} \sqrt{1+\sin[d x - \text{ArcTan}[\cot[c]]]}\right) /$$

$$\left( d (b+a \cos[c+d x])^3 (A+2 C+2 B \cos[c+d x]+A \cos[2 c+2 d x]) \sqrt{1+\cot[c]^2} \right) -$$

$$\left( 20 b^3 C \cos[c+d x]^5 \csc[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[d x - \text{ArcTan}[\cot[c]]]^2\right] \right)$$

$$\frac{(a+b \sec[c+d x])^3 (A+B \sec[c+d x]+C \sec[c+d x]^2)}{\sec[d x - \text{ArcTan}[\cot[c]]] \sqrt{1-\sin[d x - \text{ArcTan}[\cot[c]]]}}$$

$$\left. \sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[d x - \text{ArcTan}[\cot[c]]]} \sqrt{1+\sin[d x - \text{ArcTan}[\cot[c]]]}\right) /$$

$$\left( 21 d (b+a \cos[c+d x])^3 (A+2 C+2 B \cos[c+d x]+A \cos[2 c+2 d x]) \sqrt{1+\cot[c]^2} \right)$$

**Problem 1311: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a+b \sec[c+d x])^3 (A+B \sec[c+d x]+C \sec[c+d x]^2)}{\sqrt{\cos[c+d x]}} dx$$

Optimal (type 4, 357 leaves, 9 steps):

$$-\frac{1}{15 d} 2 (15 a^3 B+27 a b^2 B+9 a^2 b (5 A+3 C)+b^3 (9 A+7 C)) \text{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]+$$

$$\frac{1}{21 d} 2 (21 a^2 b B+5 b^3 B+7 a^3 (3 A+C)+3 a b^2 (7 A+5 C)) \text{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]+$$

$$\frac{2 b (63 A b^2+99 a b B+24 a^2 C+49 b^2 C) \sin[c+d x]}{315 d \cos[c+d x]^{5/2}}+$$

$$\frac{2 (54 a^2 b B+15 b^3 B+8 a^3 C+9 a b^2 (7 A+5 C)) \sin[c+d x]}{63 d \cos[c+d x]^{3/2}}+$$

$$\frac{2 (15 a^3 B+27 a b^2 B+9 a^2 b (5 A+3 C)+b^3 (9 A+7 C)) \sin[c+d x]}{15 d \sqrt{\cos[c+d x]}}+$$

$$\frac{2 (3 b B+2 a C) (b+a \cos[c+d x])^2 \sin[c+d x]}{21 d \cos[c+d x]^{7/2}}+\frac{2 C (b+a \cos[c+d x])^3 \sin[c+d x]}{9 d \cos[c+d x]^{9/2}}$$

Result (type 5, 3345 leaves):

$$\frac{1}{(b+a \cos[c+d x])^3 (A+2 C+2 B \cos[c+d x]+A \cos[2 c+2 d x])}$$

$$\cos[c+d x]^{11/2} (a+b \sec[c+d x])^3 (A+B \sec[c+d x]+C \sec[c+d x]^2)$$

$$\left( \frac{1}{15 d} 4 (45 a^2 A b+9 A b^3+15 a^3 B+27 a b^2 B+27 a^2 b C+7 b^3 C) \csc[c] \sec[c]+$$

$$\frac{4 b^3 C \sec[c] \sec[c+d x]^5 \sin[d x]}{9 d}+\frac{1}{63 d} 4 \sec[c] \sec[c+d x]^4 \right)$$

$$\begin{aligned}
 & \left( 7 b^3 C \sin [c] + 9 b^3 B \sin [d x] + 27 a b^2 C \sin [d x] \right) + \frac{1}{315 d} 4 \operatorname{Sec}[c] \operatorname{Sec}[c+d x]^2 \\
 & \left( 63 A b^3 \sin [c] + 189 a b^2 B \sin [c] + 189 a^2 b C \sin [c] + 49 b^3 C \sin [c] + 315 a A b^2 \sin [d x] + \right. \\
 & \quad \left. 315 a^2 b B \sin [d x] + 75 b^3 B \sin [d x] + 105 a^3 C \sin [d x] + 225 a b^2 C \sin [d x] \right) + \\
 & \frac{1}{315 d} 4 \operatorname{Sec}[c] \operatorname{Sec}[c+d x]^3 \left( 45 b^3 B \sin [c] + 135 a b^2 C \sin [c] + 63 A b^3 \sin [d x] + \right. \\
 & \quad \left. 189 a b^2 B \sin [d x] + 189 a^2 b C \sin [d x] + 49 b^3 C \sin [d x] \right) + \frac{1}{105 d} \\
 & 4 \operatorname{Sec}[c] \operatorname{Sec}[c+d x] \left( 105 a A b^2 \sin [c] + 105 a^2 b B \sin [c] + 25 b^3 B \sin [c] + \right. \\
 & \quad \left. 35 a^3 C \sin [c] + 75 a b^2 C \sin [c] + 315 a^2 A b \sin [d x] + 63 A b^3 \sin [d x] + \right. \\
 & \quad \left. 105 a^3 B \sin [d x] + 189 a b^2 B \sin [d x] + 189 a^2 b C \sin [d x] + 49 b^3 C \sin [d x] \right) \Big) - \\
 & \left( 4 a^3 A \cos [c+d x]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2 \right] \right. \\
 & \quad \left. \frac{(a+b \operatorname{Sec}[c+d x])^3 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2)}{\operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1-\sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right. \\
 & \quad \left. \sqrt{-\sqrt{1+\operatorname{Cot}[c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1+\sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) / \\
 & \left( d (b+a \cos [c+d x])^3 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\operatorname{Cot}[c]^2} \right) - \\
 & \left( 4 a A b^2 \cos [c+d x]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2 \right] \right. \\
 & \quad \left. \frac{(a+b \operatorname{Sec}[c+d x])^3 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2)}{\operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1-\sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right. \\
 & \quad \left. \sqrt{-\sqrt{1+\operatorname{Cot}[c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1+\sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) / \\
 & \left( d (b+a \cos [c+d x])^3 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\operatorname{Cot}[c]^2} \right) - \\
 & \left( 4 a^2 b B \cos [c+d x]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2 \right] \right. \\
 & \quad \left. \frac{(a+b \operatorname{Sec}[c+d x])^3 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2)}{\operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1-\sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right. \\
 & \quad \left. \sqrt{-\sqrt{1+\operatorname{Cot}[c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1+\sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) / \\
 & \left( d (b+a \cos [c+d x])^3 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\operatorname{Cot}[c]^2} \right) - \\
 & \left( 20 b^3 B \cos [c+d x]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2 \right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{(a + b \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right. \\
 & \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right) / \\
 & \left( 21 d (b + a \operatorname{Cos}[c + d x])^3 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2} \right) - \\
 & \left( 4 a^3 C \operatorname{Cos}[c + d x]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right) \\
 & \left( \frac{(a + b \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right. \\
 & \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right) / \\
 & \left( 3 d (b + a \operatorname{Cos}[c + d x])^3 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2} \right) - \\
 & \left( 20 a b^2 C \operatorname{Cos}[c + d x]^5 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right) \\
 & \left( \frac{(a + b \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right. \\
 & \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right) / \\
 & \left( 7 d (b + a \operatorname{Cos}[c + d x])^3 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2} \right) + \\
 & \left( 6 a^2 A b \operatorname{Cos}[c + d x]^5 \operatorname{Csc}[c] (a + b \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right. \\
 & \left. \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]^2\right] \right) \right. \\
 & \left. \operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] \right) / \left( \sqrt{1 - \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right) \\
 & \sqrt{1 + \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{\operatorname{Cos}[c] \operatorname{Cos}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \operatorname{Tan}[c]^2}
 \end{aligned}$$

$$\left. \left( \sqrt{1 + \tan[c]^2} \right) - \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \right) /$$

$$\left( d (b + a \cos[c + d x])^3 (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) \right) +$$

$$\left( 6 A b^3 \cos[c + d x]^5 \csc[c] (a + b \sec[c + d x])^3 (A + B \sec[c + d x] + C \sec[c + d x]^2) \right.$$

$$\left. \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos[d x + \text{ArcTan}[\tan[c]]]^2\right] \right) \right.$$

$$\left. \left. \frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 - \cos[d x + \text{ArcTan}[\tan[c]]]}} \right) / \left( \sqrt{1 + \cos[d x + \text{ArcTan}[\tan[c]]]} \sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}} \right) \right.$$

$$\left. \left. \left( \sqrt{1 + \tan[c]^2} \right) - \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \right) / \right.$$

$$\left( 5 d (b + a \cos[c + d x])^3 (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) \right) +$$

$$\left( 2 a^3 B \cos[c + d x]^5 \csc[c] (a + b \sec[c + d x])^3 (A + B \sec[c + d x] + C \sec[c + d x]^2) \right.$$

$$\left. \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos[d x + \text{ArcTan}[\tan[c]]]^2\right] \right) \right.$$

$$\left. \left. \frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 - \cos[d x + \text{ArcTan}[\tan[c]]]}} \right) / \left( \sqrt{1 + \cos[d x + \text{ArcTan}[\tan[c]]]} \sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}} \right) \right.$$

$$\left. \left( \sqrt{1 + \tan[c]^2} \right) - \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \right) /$$

$$\left( d (b + a \cos[c + d x])^3 (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) \right) +$$

$$\left( 18 a b^2 B \cos[c + d x]^5 \csc[c] (a + b \sec[c + d x])^3 (A + B \sec[c + d x] + C \sec[c + d x]^2) \right.$$

$$\left. \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos[d x + \text{ArcTan}[\tan[c]]]^2\right] \right) \right.$$

$$\left. \left. \frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 - \cos[d x + \text{ArcTan}[\tan[c]]]}} \right) / \left( \sqrt{1 + \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}} \right) \right.$$

$$\left. \left. \left( \sqrt{1 + \tan[c]^2} \right) - \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \right) / \right.$$

$$\left( 5 d (b + a \cos[c + d x])^3 (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) \right) +$$

$$\left( 18 a^2 b C \cos[c + d x]^5 \csc[c] (a + b \sec[c + d x])^3 (A + B \sec[c + d x] + C \sec[c + d x]^2) \right.$$

$$\left. \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos[d x + \text{ArcTan}[\tan[c]]]^2\right] \right) \right.$$

$$\left. \left. \frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 - \cos[d x + \text{ArcTan}[\tan[c]]]}} \right) / \left( \sqrt{1 + \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}} \right) \right.$$

$$\left( \sqrt{1 + \tan[c]^2} \right) - \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \Bigg) /$$

$$\left( 5 d (b + a \cos[c + d x])^3 (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) \right) +$$

$$\left( 14 b^3 C \cos[c + d x]^5 \csc[c] (a + b \sec[c + d x])^3 (A + B \sec[c + d x] + C \sec[c + d x]^2) \right.$$

$$\left. \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos[d x + \text{ArcTan}[\tan[c]]]^2\right] \right) \right.$$

$$\left. \frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 - \cos[d x + \text{ArcTan}[\tan[c]]]}} \right) /$$

$$\sqrt{1 + \cos[d x + \text{ArcTan}[\tan[c]]]} \sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}$$

$$\left( \sqrt{1 + \tan[c]^2} \right) - \frac{\frac{\sin[d x + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \Bigg) /$$

$$\left( 15 d (b + a \cos[c + d x])^3 (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) \right)$$

Problem 1313: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \cos[c + d x]^{9/2} (a + b \sec[c + d x])^4 (A + B \sec[c + d x] + C \sec[c + d x]^2) dx$$

Optimal (type 4, 377 leaves, 9 steps):



$$\frac{1}{15 d}$$

$$2 (36 a^3 b B + 60 a b^3 B + 15 b^4 (A - C) + 18 a^2 b^2 (3 A + 5 C) + a^4 (7 A + 9 C)) \text{EllipticE}\left[\frac{1}{2} (c + d x), 2\right] +$$

$$\frac{1}{21 d} 2 (5 a^4 B + 42 a^2 b^2 B + 21 b^4 B + 28 a b^3 (A + 3 C) + 4 a^3 b (5 A + 7 C)) \text{EllipticF}\left[\frac{1}{2} (c + d x), 2\right] +$$

$$\frac{1}{63 d} 2 a (15 a^3 B + 117 a b^2 B + 2 b^3 (31 A - 63 C) + 12 a^2 b (5 A + 7 C)) \sqrt{\text{Cos}[c + d x]} \text{Sin}[c + d x] +$$

$$\frac{1}{315 d} 2 a^2 (162 a b B + 3 b^2 (41 A - 105 C) + 7 a^2 (7 A + 9 C)) \text{Cos}[c + d x]^{3/2} \text{Sin}[c + d x] +$$

$$\frac{1}{21 d} 2 a (5 A b + 3 a B - 21 b C) \sqrt{\text{Cos}[c + d x]} (b + a \text{Cos}[c + d x])^2 \text{Sin}[c + d x] +$$

$$\frac{2 a (A - 9 C) \sqrt{\text{Cos}[c + d x]} (b + a \text{Cos}[c + d x])^3 \text{Sin}[c + d x]}{9 d} + \frac{2 C (b + a \text{Cos}[c + d x])^4 \text{Sin}[c + d x]}{d \sqrt{\text{Cos}[c + d x]}}$$

Result (type 5, 4114 leaves):

$$\frac{1}{(b + a \text{Cos}[c + d x])^4 (A + 2 C + 2 B \text{Cos}[c + d x] + A \text{Cos}[2 c + 2 d x]) \text{Cos}[c + d x]^{13/2} (a + b \text{Sec}[c + d x])^4 (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2)}$$

$$\left( -\frac{1}{15 d} 2 (7 a^4 A + 54 a^2 A b^2 + 15 A b^4 + 36 a^3 b B + 60 a b^3 B + 9 a^4 C + 90 a^2 b^2 C - 30 b^4 C + 7 a^4 A \text{Cos}[2 c] + 54 a^2 A b^2 \text{Cos}[2 c] + 15 A b^4 \text{Cos}[2 c] + 36 a^3 b B \text{Cos}[2 c] + 60 a b^3 B \text{Cos}[2 c] + 9 a^4 C \text{Cos}[2 c] + 90 a^2 b^2 C \text{Cos}[2 c]) \text{Csc}[c] \text{Sec}[c] + \frac{1}{21 d} a (92 a^2 A b + 112 A b^3 + 23 a^3 B + 168 a b^2 B + 112 a^2 b C) \text{Cos}[d x] \text{Sin}[c] + a^2 (19 a^2 A + 108 A b^2 + 72 a b B + 18 a^2 C) \text{Cos}[2 d x] \text{Sin}[2 c] \right) +$$

$$\frac{45 d}{a^3 (4 A b + a B) \text{Cos}[3 d x] \text{Sin}[3 c]} + \frac{a^4 A \text{Cos}[4 d x] \text{Sin}[4 c]}{18 d} + \frac{1}{21 d} a (92 a^2 A b + 112 A b^3 + 23 a^3 B + 168 a b^2 B + 112 a^2 b C) \text{Cos}[c] \text{Sin}[d x] + \frac{4 b^4 C \text{Sec}[c] \text{Sec}[c + d x] \text{Sin}[d x]}{d} + \frac{a^2 (19 a^2 A + 108 A b^2 + 72 a b B + 18 a^2 C) \text{Cos}[2 c] \text{Sin}[2 d x]}{45 d} + \frac{a^3 (4 A b + a B) \text{Cos}[3 c] \text{Sin}[3 d x]}{7 d} + \frac{a^4 A \text{Cos}[4 c] \text{Sin}[4 d x]}{18 d} \Big) -$$

$$\left( 80 a^3 A b \text{Cos}[c + d x]^6 \text{Csc}[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \text{Sin}[d x - \text{ArcTan}[\text{Cot}[c]]]^2\right] \right. \\ \left. (a + b \text{Sec}[c + d x])^4 (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2) \text{Sec}[d x - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \text{Sin}[d x - \text{ArcTan}[\text{Cot}[c]]]} \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[d x - \text{ArcTan}[\text{Cot}[c]]]} \sqrt{1 + \text{Sin}[d x - \text{ArcTan}[\text{Cot}[c]]]} \right) /$$

$$\begin{aligned}
 & \left( 21 d (b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} \right) - \\
 & \left( 16 a A b^3 \cos [c + d x]^6 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\cot [c]]]\right]^2 \right) \\
 & \frac{(a + b \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sec [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\cot [c]]]}} \\
 & \left. \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\cot [c]]]}} \right) / \\
 & \left( 3 d (b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} \right) - \\
 & \left( 20 a^4 B \cos [c + d x]^6 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\cot [c]]]\right]^2 \right) \\
 & \frac{(a + b \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sec [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\cot [c]]]}} \\
 & \left. \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\cot [c]]]}} \right) / \\
 & \left( 21 d (b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} \right) - \\
 & \left( 8 a^2 b^2 B \cos [c + d x]^6 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\cot [c]]]\right]^2 \right) \\
 & \frac{(a + b \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sec [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\cot [c]]]}} \\
 & \left. \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\cot [c]]]}} \right) / \\
 & \left( d (b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} \right) - \\
 & \left( 4 b^4 B \cos [c + d x]^6 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\cot [c]]]\right]^2 \right) \\
 & \frac{(a + b \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sec [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\cot [c]]]}} \\
 & \left. \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\cot [c]]]}} \right) / \\
 & \left( d (b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} \right) - \\
 & \left( 16 a^3 b C \cos [c + d x]^6 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\cot [c]]]\right]^2 \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{(a + b \operatorname{Sec}[c + dx])^4 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2)}{\operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right. \\
 & \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right) / \\
 & \left( 3d (b + a \operatorname{Cos}[c + dx])^4 (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) \sqrt{1 + \operatorname{Cot}[c]^2} \right) - \\
 & \left( 16 a b^3 C \operatorname{Cos}[c + dx]^6 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right. \\
 & \left. \frac{(a + b \operatorname{Sec}[c + dx])^4 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2)}{\operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right. \\
 & \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right) / \\
 & \left( d (b + a \operatorname{Cos}[c + dx])^4 (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) \sqrt{1 + \operatorname{Cot}[c]^2} \right) - \\
 & \left( 14 a^4 A \operatorname{Cos}[c + dx]^6 \operatorname{Csc}[c] (a + b \operatorname{Sec}[c + dx])^4 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right. \\
 & \left. \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \operatorname{Cos}[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]]^2\right] \right. \right. \\
 & \left. \left. \operatorname{Sin}[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] \right) / \left( \sqrt{1 - \operatorname{Cos}[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]]}} \right. \right. \\
 & \left. \left. \sqrt{1 + \operatorname{Cos}[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]]}} \sqrt{\operatorname{Cos}[c] \operatorname{Cos}[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}} \right. \right. \\
 & \left. \left. \sqrt{1 + \operatorname{Tan}[c]^2} \right) - \frac{\frac{\operatorname{Sin}[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1 + \operatorname{Tan}[c]^2}} + \frac{2 \operatorname{Cos}[c]^2 \operatorname{Cos}[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}}{\operatorname{Cos}[c]^2 + \operatorname{Sin}[c]^2}}{\sqrt{\operatorname{Cos}[c] \operatorname{Cos}[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}}} \right) / \\
 & \left( 15d (b + a \operatorname{Cos}[c + dx])^4 (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) \right) - \\
 & \left( 36 a^2 A b^2 \operatorname{Cos}[c + dx]^6 \operatorname{Csc}[c] (a + b \operatorname{Sec}[c + dx])^4 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \right)
 \end{aligned}$$

$$\left( \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \right]^2 \right) \right.$$

$$\left. \frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 - \cos [d x + \text{ArcTan} [\text{Tan} [c]]]}}, \right.$$

$$\left. \frac{\sqrt{1 + \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \text{Tan} [c]^2}}{\sqrt{1 + \text{Tan} [c]^2}} - \frac{\frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 + \text{Tan} [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \sqrt{1 + \text{Tan} [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \text{Tan} [c]^2}} \right) \left. \right) /$$

$$\left( 5 d (b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right) -$$

$$\left( 2 A b^4 \cos [c + d x]^6 \text{Csc} [c] (a + b \text{Sec} [c + d x])^4 (A + B \text{Sec} [c + d x] + C \text{Sec} [c + d x]^2) \right)$$

$$\left( \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \right]^2 \right) \right.$$

$$\left. \frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 - \cos [d x + \text{ArcTan} [\text{Tan} [c]]]}}, \right.$$

$$\left. \frac{\sqrt{1 + \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \text{Tan} [c]^2}}{\sqrt{1 + \text{Tan} [c]^2}} - \frac{\frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 + \text{Tan} [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \sqrt{1 + \text{Tan} [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \text{Tan} [c]^2}} \right) \left. \right) /$$

$$\left( d (b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right) -$$

$$\left( 24 a^3 b B \cos [c + d x]^6 \text{Csc} [c] (a + b \text{Sec} [c + d x])^4 (A + B \text{Sec} [c + d x] + C \text{Sec} [c + d x]^2) \right)$$

$$\left( \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \right]^2 \right) \right.$$

$$\left. \frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 - \cos [d x + \text{ArcTan} [\text{Tan} [c]]]}}, \right.$$

$$\left. \frac{\sqrt{1 + \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2}}{\sqrt{1 + \tan [c]^2}} - \frac{\frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2}} \right) \left. \right) /$$

$$\left( 5 d (b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right) -$$

$$\left( 8 a b^3 B \cos [c + d x]^6 \text{Csc} [c] (a + b \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right)$$

$$\left( \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \right]^2 \right) \right.$$

$$\left. \frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 - \cos [d x + \text{ArcTan} [\text{Tan} [c]]]}}, \right.$$

$$\left. \frac{\sqrt{1 + \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2}}{\sqrt{1 + \tan [c]^2}} - \frac{\frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2}} \right) \left. \right) /$$

$$\left( d (b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right) -$$

$$\left( 6 a^4 C \cos [c + d x]^6 \text{Csc} [c] (a + b \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right)$$

$$\left( \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \text{ArcTan} [\text{Tan} [c]]]^2 \right] \right. \right.$$

$$\left. \left. \frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 - \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \right) \right) / \left( \sqrt{1 + \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2} \right.$$

$$\left. \left. \left. \left. \sqrt{1 + \tan [c]^2} \right) - \frac{\frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2}} \right) \right) \right) /$$

$$\left( 5 d (b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right) -$$

$$\left( 12 a^2 b^2 C \cos [c + d x]^6 \csc [c] (a + b \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right)$$

$$\left( \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \text{ArcTan} [\text{Tan} [c]]]^2 \right] \right. \right.$$

$$\left. \left. \frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 - \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \right) \right) / \left( \sqrt{1 + \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2} \right.$$

$$\left. \left. \left. \left. \sqrt{1 + \tan [c]^2} \right) - \frac{\frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2}} \right) \right) \right) /$$

$$\left( d (b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right) +$$

$$\left( 2 b^4 C \cos [c + d x]^6 \csc [c] (a + b \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2) \right)$$

$$\left( \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \right]^2 \right. \right. \\ \left. \left. \sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c] \right) / \left( \sqrt{1 - \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \right. \right. \\ \left. \left. \sqrt{1 + \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2} \right. \right. \\ \left. \left. \sqrt{1 + \tan [c]^2} \right) - \frac{\frac{\sin [d x + \text{ArcTan} [\text{Tan} [c]]] \text{Tan} [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\text{Tan} [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\text{Tan} [c]]]} \sqrt{1 + \tan [c]^2}} \right) / \right. \\ \left. (d (b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])) \right)$$

**Problem 1314: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c + d x]^{7/2} (a + b \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 4, 371 leaves, 9 steps):

$$\frac{1}{5 d} 2 (3 a^4 B + 30 a^2 b^2 B - 5 b^4 B + 20 a b^3 (A - C) + 4 a^3 b (3 A + 5 C)) \text{EllipticE} \left[ \frac{1}{2} (c + d x), 2 \right] + \frac{1}{21 d} \\ 2 (28 a^3 b B + 84 a b^3 B + 7 b^4 (3 A + C) + 42 a^2 b^2 (A + 3 C) + a^4 (5 A + 7 C)) \text{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right] + \\ \frac{1}{21 d} 2 a (28 a^2 b B - 42 b^3 B + 3 a b^2 (13 A - 49 C) + a^3 (5 A + 7 C)) \sqrt{\cos [c + d x]} \sin [c + d x] + \\ \frac{1}{105 d} 2 a^2 (54 a A b + 21 a^2 B - 105 b^2 B - 350 a b C) \cos [c + d x]^{3/2} \sin [c + d x] + \\ \frac{1}{7 d} 2 a (a A - 7 b B - 21 a C) \sqrt{\cos [c + d x]} (b + a \cos [c + d x])^2 \sin [c + d x] + \\ \frac{2 (3 b B + 8 a C) (b + a \cos [c + d x])^3 \sin [c + d x]}{3 d \sqrt{\cos [c + d x]}} + \frac{2 C (b + a \cos [c + d x])^4 \sin [c + d x]}{3 d \cos [c + d x]^{3/2}}$$

Result (type 5, 4776 leaves):

$$\frac{1}{5 (b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])} \\ 12 i a^3 A b \cos [c + d x]^6 \text{Csc} [c] (a + b \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2) \\ \left( \left( 2 e^{2 i d x} \text{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c]) \right]^2 \right. \right. \\ \left. \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \right. \right.$$

$$\frac{\begin{aligned} & \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \Big/ \\ & \left( 3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c] \right) - \\ & \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \\ & \quad \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \right. \\ & \quad \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) \Big/ \\ & \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) + \\ & \qquad \qquad \qquad 1 \end{aligned}}{(b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])}$$

$$\frac{\begin{aligned} & 4 i a A b^3 \\ & \cos [c + d x]^6 \operatorname{Csc} [c] \\ & (a + b \operatorname{Sec} [c + d x])^4 \\ & (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) \\ & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right) \right. \\ & \quad \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \right. \\ & \quad \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) \Big/ \\ & \left( 3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c] \right) - \\ & \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \\ & \quad \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \right. \\ & \quad \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) \Big/ \\ & \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) + \\ & \qquad \qquad \qquad 1 \end{aligned}}{5 (b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])}$$

$$\frac{\begin{aligned} & 3 i a^4 B \\ & \cos [c + d x]^6 \operatorname{Csc} [c] \\ & (a + b \operatorname{Sec} [c + d x])^4 \\ & (A + B \operatorname{Sec} [c + d x] + C \operatorname{Sec} [c + d x]^2) \\ & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right) \right. \\ & \quad \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \right. \\ & \quad \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) \Big/ \\ & \left( 3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c] \right) - \\ & \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \\ & \quad \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \right. \\ & \quad \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) \Big/ \\ & \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) + \\ & \qquad \qquad \qquad 1 \end{aligned}}{3 i a^4 B}$$



$$\begin{aligned}
 & \left. \frac{\sqrt{1 + e^{2ix} \cos[2c] + i e^{2ix} \sin[2c]}}{(-i d (1 + e^{2ix}) \cos[c] + d (-1 + e^{2ix}) \sin[c])} \right) + \\
 & \frac{1}{(b + a \cos[c + dx])^4 (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])} \\
 & 6 i a^2 b^2 B \\
 & \cos[c + dx]^6 \operatorname{Csc}[c] \\
 & (a + b \operatorname{Sec}[c + dx])^4 \\
 & (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \\
 & \left( \left( 2 e^{2ix} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix} (\cos[c] + i \sin[c])^2 \right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-ix} (2 (1 + e^{2ix}) \cos[c] + 2 i (-1 + e^{2ix}) \sin[c])}}{\sqrt{1 + e^{2ix} \cos[2c] + i e^{2ix} \sin[2c]}} \right) / \\
 & \quad (3 i d (1 + e^{2ix}) \cos[c] - 3 d (-1 + e^{2ix}) \sin[c]) - \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix} (\cos[c] + i \sin[c])^2 \right] \right) \\
 & \quad \left. \frac{\sqrt{e^{-ix} (2 (1 + e^{2ix}) \cos[c] + 2 i (-1 + e^{2ix}) \sin[c])}}{\sqrt{1 + e^{2ix} \cos[2c] + i e^{2ix} \sin[2c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2ix}) \cos[c] + d (-1 + e^{2ix}) \sin[c]) \right) - \\
 & \frac{1}{(b + a \cos[c + dx])^4 (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])} \\
 & i b^4 B \cos[c + dx]^6 \\
 & \operatorname{Csc}[c] (a + b \operatorname{Sec}[c + dx])^4 \\
 & (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) \\
 & \left( \left( 2 e^{2ix} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix} (\cos[c] + i \sin[c])^2 \right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-ix} (2 (1 + e^{2ix}) \cos[c] + 2 i (-1 + e^{2ix}) \sin[c])}}{\sqrt{1 + e^{2ix} \cos[2c] + i e^{2ix} \sin[2c]}} \right) / \\
 & \quad (3 i d (1 + e^{2ix}) \cos[c] - 3 d (-1 + e^{2ix}) \sin[c]) - \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix} (\cos[c] + i \sin[c])^2 \right] \right) \\
 & \quad \left. \frac{\sqrt{e^{-ix} (2 (1 + e^{2ix}) \cos[c] + 2 i (-1 + e^{2ix}) \sin[c])}}{\sqrt{1 + e^{2ix} \cos[2c] + i e^{2ix} \sin[2c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2ix}) \cos[c] + d (-1 + e^{2ix}) \sin[c]) \right) + \\
 & \frac{1}{(b + a \cos[c + dx])^4 (A + 2C + 2B \cos[c + dx] + A \cos[2c + 2dx])} \\
 & 4 i a^3 b C \\
 & \cos[c + dx]^6 \operatorname{Csc}[c]
 \end{aligned}$$

$$\begin{aligned}
 & \frac{(a + b \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])\right]^2 \right) \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])} \sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]} \right) / \left( 3 i d (1 + e^{2 i d x}) \operatorname{Cos}[c] - 3 d (-1 + e^{2 i d x}) \operatorname{Sin}[c] \right) - \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])\right]^2 \right) \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])} \sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]} \right) / \left( -i d (1 + e^{2 i d x}) \operatorname{Cos}[c] + d (-1 + e^{2 i d x}) \operatorname{Sin}[c] \right) \right) - 1}{(b + a \operatorname{Cos}[c + d x])^4 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x])} \\
 & \frac{4 i a b^3 C \operatorname{Cos}[c + d x]^6 \operatorname{Csc}[c] (a + b \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])\right]^2 \right) \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])} \sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]} \right) / \left( 3 i d (1 + e^{2 i d x}) \operatorname{Cos}[c] - 3 d (-1 + e^{2 i d x}) \operatorname{Sin}[c] \right) - \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])\right]^2 \right) \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])} \sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]} \right) / \left( -i d (1 + e^{2 i d x}) \operatorname{Cos}[c] + d (-1 + e^{2 i d x}) \operatorname{Sin}[c] \right) \right) + 1}{(b + a \operatorname{Cos}[c + d x])^4 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x])} \\
 & \frac{\operatorname{Cos}[c + d x]^{13/2} (a + b \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \left( -\frac{1}{5 d} 2 (12 a^3 A b + 20 a A b^3 + 3 a^4 B + 30 a^2 b^2 B - 10 b^4 B + 20 a^3 b C - 40 a b^3 C + 12 a^3 A b \operatorname{Cos}[2 c] + 20 a A b^3 \operatorname{Cos}[2 c] + 3 a^4 B \operatorname{Cos}[2 c] + 30 a^2 b^2 B \operatorname{Cos}[2 c] + 20 a^3 b C \operatorname{Cos}[2 c]) \operatorname{Csc}[c] \operatorname{Sec}[c] + \frac{a^2 (23 a^2 A + 168 A b^2 + 112 a b B + 28 a^2 C) \operatorname{Cos}[d x] \operatorname{Sin}[c]}{21 d} \right)}{21 d}
 \end{aligned}$$

$$\begin{aligned}
 & \frac{2 a^3 (4 A b + a B) \cos [2 d x] \sin [2 c]}{5 d} + \frac{a^4 A \cos [3 d x] \sin [3 c]}{7 d} + \\
 & \frac{a^2 (23 a^2 A + 168 A b^2 + 112 a b B + 28 a^2 C) \cos [c] \sin [d x]}{21 d} + \\
 & \frac{4 b^4 C \sec [c] \sec [c + d x]^2 \sin [d x]}{3 d} + \frac{1}{3 d} \\
 & \left. \begin{aligned}
 & 4 \sec [c] \sec [c + d x] (b^4 C \sin [c] + 3 b^4 B \sin [d x] + 12 a b^3 C \sin [d x]) + \\
 & \frac{2 a^3 (4 A b + a B) \cos [2 c] \sin [2 d x]}{5 d} + \frac{a^4 A \cos [3 c] \sin [3 d x]}{7 d} \right) - \\
 & \left( 20 a^4 A \cos [c + d x]^6 \csc [c] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right]^2 \right. \\
 & \frac{(a + b \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sec [d x - \operatorname{ArcTan} [\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan} [\cot [c]]]} \\
 & \frac{\sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]]}{\sqrt{1 + \sin [d x - \operatorname{ArcTan} [\cot [c]]}} \left. \right) / \\
 & \left( 21 d (b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} \right) - \\
 & \left( 8 a^2 A b^2 \cos [c + d x]^6 \csc [c] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right]^2 \right. \\
 & \frac{(a + b \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sec [d x - \operatorname{ArcTan} [\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan} [\cot [c]]]} \\
 & \frac{\sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]]}{\sqrt{1 + \sin [d x - \operatorname{ArcTan} [\cot [c]]}} \left. \right) / \\
 & \left( d (b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} \right) - \\
 & \left( 4 A b^4 \cos [c + d x]^6 \csc [c] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right]^2 \right. \\
 & \frac{(a + b \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sec [d x - \operatorname{ArcTan} [\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan} [\cot [c]]]} \\
 & \frac{\sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]]}{\sqrt{1 + \sin [d x - \operatorname{ArcTan} [\cot [c]]}} \left. \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( d (b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} \right) - \\
 & \left( 16 a^3 b B \cos [c + d x]^6 \csc [c] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right]^2 \right. \\
 & \quad \frac{(a + b \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sec [d x - \operatorname{ArcTan} [\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan} [\cot [c]]]}} \\
 & \quad \left. \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]] \sqrt{1 + \sin [d x - \operatorname{ArcTan} [\cot [c]]]}} \right) / \\
 & \left( 3 d (b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} \right) - \\
 & \left( 16 a b^3 B \cos [c + d x]^6 \csc [c] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right]^2 \right. \\
 & \quad \frac{(a + b \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sec [d x - \operatorname{ArcTan} [\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan} [\cot [c]]]}} \\
 & \quad \left. \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]] \sqrt{1 + \sin [d x - \operatorname{ArcTan} [\cot [c]]]}} \right) / \\
 & \left( d (b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} \right) - \\
 & \left( 4 a^4 C \cos [c + d x]^6 \csc [c] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right]^2 \right. \\
 & \quad \frac{(a + b \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sec [d x - \operatorname{ArcTan} [\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan} [\cot [c]]]}} \\
 & \quad \left. \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]] \sqrt{1 + \sin [d x - \operatorname{ArcTan} [\cot [c]]]}} \right) / \\
 & \left( 3 d (b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} \right) - \\
 & \left( 24 a^2 b^2 C \cos [c + d x]^6 \csc [c] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right]^2 \right. \\
 & \quad \frac{(a + b \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sec [d x - \operatorname{ArcTan} [\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan} [\cot [c]]]}} \\
 & \quad \left. \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]] \sqrt{1 + \sin [d x - \operatorname{ArcTan} [\cot [c]]]}} \right) / \\
 & \left( d (b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} \right) - \\
 & \left( 4 b^4 C \cos [c + d x]^6 \csc [c] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right]^2 \right)
 \end{aligned}$$

$$\frac{(a + b \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}}{\sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}}}} \Bigg/$$

$$\left( 3 d (b + a \operatorname{Cos}[c + d x])^4 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2} \right)$$

**Problem 1315: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \operatorname{Cos}[c + d x]^{5/2} (a + b \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 4, 388 leaves, 9 steps):

$$\frac{1}{5 d} 2 (20 a^3 b B - 20 a b^3 B + 30 a^2 b^2 (A - C) - b^4 (5 A + 3 C) + a^4 (3 A + 5 C)) \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), 2\right] +$$

$$\frac{1}{3 d} 2 (a^4 B + 18 a^2 b^2 B + b^4 B + 4 a b^3 (3 A + C) + 4 a^3 b (A + 3 C)) \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), 2\right] +$$

$$\frac{1}{15 d} 2 a (5 a^3 B - 105 a b^2 B + 4 a^2 b (5 A - 33 C) - 6 b^3 (5 A + 3 C)) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{Sin}[c + d x] -$$

$$\frac{1}{15 d} 2 a^2 (50 a b B - a^2 (3 A - 59 C) + 3 b^2 (5 A + 3 C)) \operatorname{Cos}[c + d x]^{3/2} \operatorname{Sin}[c + d x] +$$

$$\frac{2 (5 A b^2 + 15 a b B + 16 a^2 C + 3 b^2 C) (b + a \operatorname{Cos}[c + d x])^2 \operatorname{Sin}[c + d x]}{5 d \sqrt{\operatorname{Cos}[c + d x]}} +$$

$$\frac{2 (5 b B + 8 a C) (b + a \operatorname{Cos}[c + d x])^3 \operatorname{Sin}[c + d x]}{15 d \operatorname{Cos}[c + d x]^{3/2}} + \frac{2 C (b + a \operatorname{Cos}[c + d x])^4 \operatorname{Sin}[c + d x]}{5 d \operatorname{Cos}[c + d x]^{5/2}}$$

Result (type 5, 4960 leaves):

$$\frac{1}{5 (b + a \operatorname{Cos}[c + d x])^4 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x])}$$

$$3 i a^4 A \operatorname{Cos}[c + d x]^6 \operatorname{Csc}[c] (a + b \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)$$

$$\left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])\right]^2 \right. \right.$$

$$\left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]}} \right) \Bigg/$$

$$(3 i d (1 + e^{2 i d x}) \operatorname{Cos}[c] - 3 d (-1 + e^{2 i d x}) \operatorname{Sin}[c]) -$$

$$\left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])\right]^2 \right.$$

$$\left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]}} \right) \Bigg/$$

$$\left. (-i d (1 + e^{2 i d x}) \operatorname{Cos}[c] + d (-1 + e^{2 i d x}) \operatorname{Sin}[c]) \right) +$$

1

$$\frac{(b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])}{6 i a^2 A b^2 \cos [c + d x]^6 \operatorname{Csc}[c] (a + b \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c]) \right]^2 \right) \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) - \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c]) \right]^2 \right) \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) -$$

1

$$\frac{(b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])}{i A b^4 \cos [c + d x]^6 \operatorname{Csc}[c] (a + b \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c]) \right]^2 \right) \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) - \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c]) \right]^2 \right) \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) +$$

1

$$\frac{(b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])}{4 i a^3 b B \cos [c + d x]^6 \operatorname{Csc}[c] (a + b \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}$$

$$\left( \left( 2 e^{2 i d x} \text{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c]) \right]^2 \right. \right. \\ \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\ \left. (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) - \right. \\ \left. \left( 2 \text{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c]) \right]^2 \right) \right. \\ \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\ \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) - \\ \frac{1}{1}$$

$$\left( (b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\ \left. 4 i a b^3 B \right. \\ \left. \cos [c + d x]^6 \csc [c] \right. \\ \left. (a + b \sec [c + d x])^4 \right. \\ \left. (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\ \left( \left( 2 e^{2 i d x} \text{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c]) \right]^2 \right) \right. \\ \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\ \left. (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) - \right. \\ \left. \left( 2 \text{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c]) \right]^2 \right) \right. \\ \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\ \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) + \\ \frac{1}{1}$$

$$\left( (b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right. \\ \left. i a^4 C \right. \\ \left. \cos [c + d x]^6 \csc [c] \right. \\ \left. (a + b \sec [c + d x])^4 \right. \\ \left. (A + B \sec [c + d x] + C \sec [c + d x]^2) \right. \\ \left( \left( 2 e^{2 i d x} \text{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c]) \right]^2 \right) \right. \\ \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\ \left. (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) - \right.$$

$$\frac{\left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2\right] \sqrt{e^{-i d x} \left(2 \left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)} \sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}\right) / \left(-i d\left(1+e^{2 i d x}\right) \cos [c]+d\left(-1+e^{2 i d x}\right) \sin [c]\right)-1}{(b+a \cos [c+d x])^4 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) 6 i a^2 b^2 C \cos [c+d x]^6 \operatorname{Csc}[c] (a+b \sec [c+d x])^4 (A+B \sec [c+d x]+C \sec [c+d x]^2) \left(\left(2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2\right] \sqrt{e^{-i d x} \left(2 \left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)} \sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}\right) / \left(3 i d\left(1+e^{2 i d x}\right) \cos [c]-3 d\left(-1+e^{2 i d x}\right) \sin [c]\right)-\left(2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2\right] \sqrt{e^{-i d x} \left(2 \left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)} \sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}\right) / \left(-i d\left(1+e^{2 i d x}\right) \cos [c]+d\left(-1+e^{2 i d x}\right) \sin [c]\right)-1$$

$$\frac{5 (b+a \cos [c+d x])^4 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) 3 i b^4 C \cos [c+d x]^6 \operatorname{Csc}[c] (a+b \sec [c+d x])^4 (A+B \sec [c+d x]+C \sec [c+d x]^2) \left(\left(2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2\right] \sqrt{e^{-i d x} \left(2 \left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)} \sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}\right) / \left(3 i d\left(1+e^{2 i d x}\right) \cos [c]-3 d\left(-1+e^{2 i d x}\right) \sin [c]\right)-\left(2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2\right] \sqrt{e^{-i d x} \left(2 \left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)} \sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}\right) / \left(-i d\left(1+e^{2 i d x}\right) \cos [c]+d\left(-1+e^{2 i d x}\right) \sin [c]\right)+1$$



1

$$\begin{aligned}
 & \frac{(b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x])}{\cos [c + d x]^{13/2}} \\
 & \frac{(a + b \sec [c + d x])^4}{(A + B \sec [c + d x] + C \sec [c + d x]^2)} \\
 & \left( -\frac{1}{5 d} 2 (3 a^4 A + 30 a^2 A b^2 - 10 A b^4 + 20 a^3 b B - 40 a b^3 B + 5 a^4 C - 60 a^2 b^2 C - 6 b^4 C + \right. \\
 & \quad 3 a^4 A \cos [2 c] + 30 a^2 A b^2 \cos [2 c] + 20 a^3 b B \cos [2 c] + 5 a^4 C \cos [2 c]) \csc [c] \sec [c] + \\
 & \quad \frac{4 a^3 (4 A b + a B) \cos [d x] \sin [c]}{3 d} + \frac{2 a^4 A \cos [2 d x] \sin [2 c]}{5 d} + \\
 & \quad \frac{4 a^3 (4 A b + a B) \cos [c] \sin [d x]}{3 d} + \frac{4 b^4 C \sec [c] \sec [c + d x]^3 \sin [d x]}{5 d} + \frac{1}{15 d} \\
 & \quad 4 \sec [c] \sec [c + d x]^2 (3 b^4 C \sin [c] + 5 b^4 B \sin [d x] + 20 a b^3 C \sin [d x]) + \\
 & \quad \frac{1}{15 d} 4 \sec [c] \sec [c + d x] (5 b^4 B \sin [c] + 20 a b^3 C \sin [c] + 15 A b^4 \sin [d x] + \\
 & \quad \left. 60 a b^3 B \sin [d x] + 90 a^2 b^2 C \sin [d x] + 9 b^4 C \sin [d x]) + \frac{2 a^4 A \cos [2 c] \sin [2 d x]}{5 d} \right) - \\
 & \left( 16 a^3 A b \cos [c + d x]^6 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\cot [c]]]^2\right] \right. \\
 & \quad \frac{(a + b \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sec [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\cot [c]]]} \\
 & \quad \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\cot [c]]]} \\
 & \quad \left. \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\cot [c]]]} \right) / \\
 & \left( 3 d (b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} \right) - \\
 & \left( 16 a A b^3 \cos [c + d x]^6 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\cot [c]]]^2\right] \right. \\
 & \quad \frac{(a + b \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sec [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\cot [c]]]} \\
 & \quad \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\cot [c]]]} \\
 & \quad \left. \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\cot [c]]]} \right) / \\
 & \left( d (b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \cot [c]^2} \right) - \\
 & \left( 4 a^4 B \cos [c + d x]^6 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\cot [c]]]^2\right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{(a + b \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right. \\
 & \left. \frac{\sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}}{\sqrt{1 + \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right) / \\
 & \left( 3 d (b + a \operatorname{Cos}[c + d x])^4 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2} \right) - \\
 & \left( 24 a^2 b^2 B \operatorname{Cos}[c + d x]^6 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right) \\
 & \left( \frac{(a + b \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right. \\
 & \left. \frac{\sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}}}{\sqrt{1 + \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right) / \\
 & \left( d (b + a \operatorname{Cos}[c + d x])^4 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2} \right) - \\
 & \left( 4 b^4 B \operatorname{Cos}[c + d x]^6 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right) \\
 & \left( \frac{(a + b \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right. \\
 & \left. \frac{\sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}}}{\sqrt{1 + \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right) / \\
 & \left( 3 d (b + a \operatorname{Cos}[c + d x])^4 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2} \right) - \\
 & \left( 16 a^3 b C \operatorname{Cos}[c + d x]^6 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right) \\
 & \left( \frac{(a + b \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right. \\
 & \left. \frac{\sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}}}{\sqrt{1 + \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right) / \\
 & \left( d (b + a \operatorname{Cos}[c + d x])^4 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x]) \sqrt{1 + \operatorname{Cot}[c]^2} \right) - \\
 & \left( 16 a b^3 C \operatorname{Cos}[c + d x]^6 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right) \\
 & \left( \frac{(a + b \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right)
 \end{aligned}$$

$$\left. \sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]} \sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]}\right) /$$

$$(3d(b+a \cos[c+dx])^4 (A+2C+2B \cos[c+dx]+A \cos[2c+2dx]) \sqrt{1+\cot[c]^2})$$

**Problem 1316: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c+dx]^{3/2} (a+b \sec[c+dx])^4 (A+B \sec[c+dx]+C \sec[c+dx]^2) dx$$

Optimal (type 4, 384 leaves, 9 steps):

$$\frac{1}{5d} 2 (5a^4 B - 30a^2 b^2 B - 3b^4 B + 20a^3 b (A-C) - 4ab^3 (5A+3C)) \text{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] + \frac{1}{21d}$$

$$2 (84a^3 b B + 28ab^3 B + 42a^2 b^2 (3A+C) + 7a^4 (A+3C) + b^4 (7A+5C)) \text{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] +$$

$$\frac{2b(413a^2 b B + 63b^3 B + 192a^3 C + 2ab^2 (175A+101C)) \sin[c+dx]}{105d \sqrt{\cos[c+dx]}} - \frac{1}{105d}$$

$$2a^2 (98ab B - a^2 (35A-87C) + 5b^2 (7A+5C)) \sqrt{\cos[c+dx]} \sin[c+dx] +$$

$$\left(2(35A b^2 + 77ab B + 48a^2 C + 25b^2 C) (b+a \cos[c+dx])^2 \sin[c+dx]\right) / (105d \cos[c+dx]^{3/2}) +$$

$$\frac{2(7b B + 8a C) (b+a \cos[c+dx])^3 \sin[c+dx]}{35d \cos[c+dx]^{5/2}} + \frac{2C (b+a \cos[c+dx])^4 \sin[c+dx]}{7d \cos[c+dx]^{7/2}}$$

Result (type 5, 4791 leaves):

$$\frac{1}{(b+a \cos[c+dx])^4 (A+2C+2B \cos[c+dx]+A \cos[2c+2dx])}$$

$$4i a^3 A b \cos[c+dx]^6 \csc[c] (a+b \sec[c+dx])^4 (A+B \sec[c+dx]+C \sec[c+dx]^2)$$

$$\left( \left( 2e^{2i dx} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2i dx} (\cos[c] + i \sin[c])^2\right] \right. \right.$$

$$\frac{\sqrt{e^{-i dx} (2(1+e^{2i dx}) \cos[c] + 2i(-1+e^{2i dx}) \sin[c])}}{\sqrt{1+e^{2i dx} \cos[2c] + i e^{2i dx} \sin[2c]}} \Bigg) /$$

$$(3i d (1+e^{2i dx}) \cos[c] - 3d (-1+e^{2i dx}) \sin[c]) -$$

$$\left( 2 \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i dx} (\cos[c] + i \sin[c])^2\right] \right.$$

$$\frac{\sqrt{e^{-i dx} (2(1+e^{2i dx}) \cos[c] + 2i(-1+e^{2i dx}) \sin[c])}}{\sqrt{1+e^{2i dx} \cos[2c] + i e^{2i dx} \sin[2c]}} \Bigg) /$$

$$\left. \left. (-i d (1+e^{2i dx}) \cos[c] + d (-1+e^{2i dx}) \sin[c]) \right) \right) -$$

$$\frac{1}{(b+a \cos[c+dx])^4 (A+2C+2B \cos[c+dx]+A \cos[2c+2dx])}$$

$$4i a A b^3$$

$$\frac{\begin{aligned} & \cos [c+d x]^6 \operatorname{Csc}[c] \\ & (a+b \operatorname{Sec}[c+d x])^4 \\ & (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \\ & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x}(\cos [c]+i \sin [c])^2\right] \right. \right. \\ & \quad \left. \left. \sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)} \right. \right. \\ & \quad \left. \left. \sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]} \right) / \right. \\ & \quad \left. \left( 3 i d\left(1+e^{2 i d x}\right) \cos [c]-3 d\left(-1+e^{2 i d x}\right) \sin [c]\right)- \right. \\ & \quad \left. \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x}(\cos [c]+i \sin [c])^2\right] \right) \right. \\ & \quad \left. \sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)} \right. \right. \\ & \quad \left. \left. \sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]} \right) / \right. \\ & \quad \left. \left. \left. (-i d\left(1+e^{2 i d x}\right) \cos [c]+d\left(-1+e^{2 i d x}\right) \sin [c]\right) \right) \right) + \end{aligned}}$$

1

$$\frac{(b+a \cos [c+d x])^4 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])}{i a^4 B}$$

$$\frac{\begin{aligned} & \cos [c+d x]^6 \operatorname{Csc}[c] \\ & (a+b \operatorname{Sec}[c+d x])^4 \\ & (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \\ & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x}(\cos [c]+i \sin [c])^2\right] \right) \right. \\ & \quad \left. \sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)} \right. \\ & \quad \left. \sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]} \right) / \right. \\ & \quad \left. \left( 3 i d\left(1+e^{2 i d x}\right) \cos [c]-3 d\left(-1+e^{2 i d x}\right) \sin [c]\right)- \right. \\ & \quad \left. \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x}(\cos [c]+i \sin [c])^2\right] \right) \right. \\ & \quad \left. \sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)} \right. \right. \\ & \quad \left. \left. \sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]} \right) / \right. \\ & \quad \left. \left. \left. (-i d\left(1+e^{2 i d x}\right) \cos [c]+d\left(-1+e^{2 i d x}\right) \sin [c]\right) \right) \right) - \end{aligned}}$$

1

$$\frac{(b+a \cos [c+d x])^4 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x])}{6 i a^2 b^2 B}$$

$$\frac{\begin{aligned} & \cos [c+d x]^6 \operatorname{Csc}[c] \\ & (a+b \operatorname{Sec}[c+d x])^4 \\ & (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \\ & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x}(\cos [c]+i \sin [c])^2\right] \right) \right. \\ & \quad \left. \sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)} \right. \end{aligned}}$$

$$\begin{aligned}
 & \left( \sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]} \right) / \\
 & \left( 3 i d (1 + e^{2 i d x}) \cos[c] - 3 d (-1 + e^{2 i d x}) \sin[c] \right) - \\
 & \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2 \right] \right. \\
 & \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])}}{\sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]}} \right) / \\
 & \left. (-i d (1 + e^{2 i d x}) \cos[c] + d (-1 + e^{2 i d x}) \sin[c]) \right) - \\
 & \qquad \qquad \qquad 1 \\
 \hline
 & 5 (b + a \cos[c + d x])^4 (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) \\
 & 3 i b^4 B \cos[c + d x]^6 \\
 & \operatorname{Csc}[c] (a + b \operatorname{Sec}[c + d x])^4 \\
 & (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2 \right] \right) \right. \\
 & \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])}}{\sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]}} \right) / \\
 & \left( 3 i d (1 + e^{2 i d x}) \cos[c] - 3 d (-1 + e^{2 i d x}) \sin[c] \right) - \\
 & \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2 \right] \right. \\
 & \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])}}{\sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]}} \right) / \\
 & \left. (-i d (1 + e^{2 i d x}) \cos[c] + d (-1 + e^{2 i d x}) \sin[c]) \right) - \\
 & \qquad \qquad \qquad 1 \\
 \hline
 & (b + a \cos[c + d x])^4 (A + 2 C + 2 B \cos[c + d x] + A \cos[2 c + 2 d x]) \\
 & 4 i a^3 b C \\
 & \cos[c + d x]^6 \operatorname{Csc}[c] \\
 & (a + b \operatorname{Sec}[c + d x])^4 \\
 & (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2 \right] \right) \right. \\
 & \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])}}{\sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]}} \right) / \\
 & \left( 3 i d (1 + e^{2 i d x}) \cos[c] - 3 d (-1 + e^{2 i d x}) \sin[c] \right) - \\
 & \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2 \right] \right. \\
 & \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])}}{\sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]}} \right) /
 \end{aligned}$$

$$\left( -i d (1 + e^{2 i d x}) \operatorname{Cos}[c] + d (-1 + e^{2 i d x}) \operatorname{Sin}[c] \right) -$$


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$$5 (b + a \operatorname{Cos}[c + d x])^4 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x])$$

$$12 i a b^3 C$$

$$\operatorname{Cos}[c + d x]^6 \operatorname{Csc}[c]$$

$$(a + b \operatorname{Sec}[c + d x])^4$$

$$(A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)$$

$$\left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right. \right.$$

$$\left. \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])} \right. \right.$$

$$\left. \left. \sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]} \right) \right) /$$

$$(3 i d (1 + e^{2 i d x}) \operatorname{Cos}[c] - 3 d (-1 + e^{2 i d x}) \operatorname{Sin}[c]) -$$

$$\left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right.$$

$$\left. \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])} \right. \right.$$

$$\left. \left. \sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]} \right) \right) /$$

$$\left( -i d (1 + e^{2 i d x}) \operatorname{Cos}[c] + d (-1 + e^{2 i d x}) \operatorname{Sin}[c] \right) +$$


---


$$1$$


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$$(b + a \operatorname{Cos}[c + d x])^4 (A + 2 C + 2 B \operatorname{Cos}[c + d x] + A \operatorname{Cos}[2 c + 2 d x])$$

$$\operatorname{Cos}[c + d x]^{13/2}$$

$$(a + b \operatorname{Sec}[c + d x])^4$$

$$(A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)$$

$$\left( -\frac{1}{5 d} 2 (20 a^3 A b - 40 a A b^3 + 5 a^4 B - 60 a^2 b^2 B - 6 b^4 B - 40 a^3 b C - 24 a b^3 C + \right.$$

$$20 a^3 A b \operatorname{Cos}[2 c] + 5 a^4 B \operatorname{Cos}[2 c]) \operatorname{Csc}[c] \operatorname{Sec}[c] + \frac{4 a^4 A \operatorname{Cos}[d x] \operatorname{Sin}[c]}{3 d} +$$

$$\frac{4 a^4 A \operatorname{Cos}[c] \operatorname{Sin}[d x]}{3 d} + \frac{4 b^4 C \operatorname{Sec}[c] \operatorname{Sec}[c + d x]^4 \operatorname{Sin}[d x]}{7 d} + \frac{1}{35 d} 4 \operatorname{Sec}[c]$$

$$\operatorname{Sec}[c + d x]^3 (5 b^4 C \operatorname{Sin}[c] + 7 b^4 B \operatorname{Sin}[d x] + 28 a b^3 C \operatorname{Sin}[d x]) + \frac{1}{105 d} 4 \operatorname{Sec}[c] \operatorname{Sec}[c + d x]$$

$$(35 A b^4 \operatorname{Sin}[c] + 140 a b^3 B \operatorname{Sin}[c] + 210 a^2 b^2 C \operatorname{Sin}[c] + 25 b^4 C \operatorname{Sin}[c] + 420 a A b^3 \operatorname{Sin}[d x] +$$

$$630 a^2 b^2 B \operatorname{Sin}[d x] + 63 b^4 B \operatorname{Sin}[d x] + 420 a^3 b C \operatorname{Sin}[d x] + 252 a b^3 C \operatorname{Sin}[d x]) +$$

$$\frac{1}{105 d} 4 \operatorname{Sec}[c] \operatorname{Sec}[c + d x]^2 (21 b^4 B \operatorname{Sin}[c] + 84 a b^3 C \operatorname{Sin}[c] + 35 A b^4 \operatorname{Sin}[d x] +$$

$$140 a b^3 B \operatorname{Sin}[d x] + 210 a^2 b^2 C \operatorname{Sin}[d x] + 25 b^4 C \operatorname{Sin}[d x]) \left. \right) -$$

$$\left( 4 a^4 A \operatorname{Cos}[c + d x]^6 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right.$$

$$(a + b \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)$$

$$\operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \left. \right)$$

$$\left. \frac{\sqrt{-\sqrt{1+\cot^2[c]} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]}}{\sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]}} \right) /$$

$$\left( 3d (b+a \cos[c+dx])^4 (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \sqrt{1+\cot^2[c]} \right) -$$

$$\left( 24a^2 A b^2 \cos[c+dx]^6 \csc[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\cot[c]]]^2\right] \right)$$

$$\frac{(a+b \sec[c+dx])^4 (A+B \sec[c+dx] + C \sec[c+dx]^2)}{\sec[dx - \text{ArcTan}[\cot[c]]] \sqrt{1-\sin[dx - \text{ArcTan}[\cot[c]]]}}$$

$$\left. \frac{\sqrt{-\sqrt{1+\cot^2[c]} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]}}{\sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]}} \right) /$$

$$\left( d (b+a \cos[c+dx])^4 (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \sqrt{1+\cot^2[c]} \right) -$$

$$\left( 4A b^4 \cos[c+dx]^6 \csc[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\cot[c]]]^2\right] \right)$$

$$\frac{(a+b \sec[c+dx])^4 (A+B \sec[c+dx] + C \sec[c+dx]^2)}{\sec[dx - \text{ArcTan}[\cot[c]]] \sqrt{1-\sin[dx - \text{ArcTan}[\cot[c]]]}}$$

$$\left. \frac{\sqrt{-\sqrt{1+\cot^2[c]} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]}}{\sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]}} \right) /$$

$$\left( 3d (b+a \cos[c+dx])^4 (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \sqrt{1+\cot^2[c]} \right) -$$

$$\left( 16a^3 b B \cos[c+dx]^6 \csc[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\cot[c]]]^2\right] \right)$$

$$\frac{(a+b \sec[c+dx])^4 (A+B \sec[c+dx] + C \sec[c+dx]^2)}{\sec[dx - \text{ArcTan}[\cot[c]]] \sqrt{1-\sin[dx - \text{ArcTan}[\cot[c]]]}}$$

$$\left. \frac{\sqrt{-\sqrt{1+\cot^2[c]} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]} \sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]}}{\sqrt{1+\sin[dx - \text{ArcTan}[\cot[c]]]}} \right) /$$

$$\left( d (b+a \cos[c+dx])^4 (A+2C+2B \cos[c+dx] + A \cos[2c+2dx]) \sqrt{1+\cot^2[c]} \right) -$$

$$\left( 16a b^3 B \cos[c+dx]^6 \csc[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\cot[c]]]^2\right] \right)$$

$$\begin{aligned}
 & \left( \frac{(a + b \operatorname{Sec}[c + dx])^4 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2)}{\operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right) / \\
 & \left( 3d (b + a \operatorname{Cos}[c + dx])^4 (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) \sqrt{1 + \operatorname{Cot}[c]^2} \right) - \\
 & \left( 4a^4 C \operatorname{Cos}[c + dx]^6 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right) \\
 & \left( \frac{(a + b \operatorname{Sec}[c + dx])^4 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2)}{\operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right) / \\
 & \left( d (b + a \operatorname{Cos}[c + dx])^4 (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) \sqrt{1 + \operatorname{Cot}[c]^2} \right) - \\
 & \left( 8a^2 b^2 C \operatorname{Cos}[c + dx]^6 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right) \\
 & \left( \frac{(a + b \operatorname{Sec}[c + dx])^4 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2)}{\operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right) / \\
 & \left( d (b + a \operatorname{Cos}[c + dx])^4 (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) \sqrt{1 + \operatorname{Cot}[c]^2} \right) - \\
 & \left( 20b^4 C \operatorname{Cos}[c + dx]^6 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right) \\
 & \left( \frac{(a + b \operatorname{Sec}[c + dx])^4 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2)}{\operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right) / \\
 & \left( 21d (b + a \operatorname{Cos}[c + dx])^4 (A + 2C + 2B \operatorname{Cos}[c + dx] + A \operatorname{Cos}[2c + 2dx]) \sqrt{1 + \operatorname{Cot}[c]^2} \right)
 \end{aligned}$$

**Problem 1317: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sqrt{\operatorname{Cos}[c + dx]} (a + b \operatorname{Sec}[c + dx])^4 (A + B \operatorname{Sec}[c + dx] + C \operatorname{Sec}[c + dx]^2) dx$$

Optimal (type 4, 401 leaves, 9 steps):



$$\begin{aligned}
 & -\frac{1}{15d} 2 (60 a^3 b B + 36 a b^3 B - 15 a^4 (A - C) + 18 a^2 b^2 (5 A + 3 C) + b^4 (9 A + 7 C)) \\
 & \quad \text{EllipticE}\left[\frac{1}{2}(c + dx), 2\right] + \frac{1}{21d} \\
 & \quad 2 (21 a^4 B + 42 a^2 b^2 B + 5 b^4 B + 28 a^3 b (3 A + C) + 4 a b^3 (7 A + 5 C)) \text{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] + \\
 & \quad \frac{2 b (261 a^2 b B + 75 b^3 B + 64 a^3 C + 2 a b^2 (147 A + 101 C)) \text{Sin}[c + dx]}{315 d \text{Cos}[c + dx]^{3/2}} + \\
 & \quad \frac{(2 (1098 a^3 b B + 756 a b^3 B + 192 a^4 C + 21 b^4 (9 A + 7 C) + 7 a^2 b^2 (261 A + 155 C)) \text{Sin}[c + dx])}{(315 d \sqrt{\text{Cos}[c + dx]})} + \\
 & \quad \frac{(2 (63 A b^2 + 117 a b B + 48 a^2 C + 49 b^2 C) (b + a \text{Cos}[c + dx])^2 \text{Sin}[c + dx])}{(315 d \text{Cos}[c + dx]^{5/2})} + \\
 & \quad \frac{2 (9 b B + 8 a C) (b + a \text{Cos}[c + dx])^3 \text{Sin}[c + dx]}{63 d \text{Cos}[c + dx]^{7/2}} + \frac{2 C (b + a \text{Cos}[c + dx])^4 \text{Sin}[c + dx]}{9 d \text{Cos}[c + dx]^{9/2}}
 \end{aligned}$$

Result (type 5, 4150 leaves):

$$\begin{aligned}
 & \frac{1}{(b + a \text{Cos}[c + dx])^4 (A + 2 C + 2 B \text{Cos}[c + dx] + A \text{Cos}[2c + 2dx])} \\
 & \quad \text{Cos}[c + dx]^{13/2} (a + b \text{Sec}[c + dx])^4 (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2) \\
 & \quad \left( -\frac{1}{15d} 2 (15 a^4 A - 180 a^2 A b^2 - 18 A b^4 - 120 a^3 b B - 72 a b^3 B - 30 a^4 C - 108 a^2 b^2 C - \right. \\
 & \quad \quad \left. 14 b^4 C + 15 a^4 A \text{Cos}[2c]) \text{Csc}[c] \text{Sec}[c] + \frac{4 b^4 C \text{Sec}[c] \text{Sec}[c + dx]^5 \text{Sin}[dx]}{9d} + \right. \\
 & \quad \quad \frac{1}{63d} 4 \text{Sec}[c] \text{Sec}[c + dx]^4 (7 b^4 C \text{Sin}[c] + 9 b^4 B \text{Sin}[dx] + 36 a b^3 C \text{Sin}[dx]) + \\
 & \quad \quad \frac{1}{315d} 4 \text{Sec}[c] \text{Sec}[c + dx]^2 \\
 & \quad \quad (63 A b^4 \text{Sin}[c] + 252 a b^3 B \text{Sin}[c] + 378 a^2 b^2 C \text{Sin}[c] + 49 b^4 C \text{Sin}[c] + 420 a A b^3 \text{Sin}[dx] + \\
 & \quad \quad \quad 630 a^2 b^2 B \text{Sin}[dx] + 75 b^4 B \text{Sin}[dx] + 420 a^3 b C \text{Sin}[dx] + 300 a b^3 C \text{Sin}[dx]) + \\
 & \quad \quad \frac{1}{315d} 4 \text{Sec}[c] \text{Sec}[c + dx]^3 (45 b^4 B \text{Sin}[c] + 180 a b^3 C \text{Sin}[c] + 63 A b^4 \text{Sin}[dx] + \\
 & \quad \quad \quad 252 a b^3 B \text{Sin}[dx] + 378 a^2 b^2 C \text{Sin}[dx] + 49 b^4 C \text{Sin}[dx]) + \frac{1}{105d} \\
 & \quad \quad \left. 4 \text{Sec}[c] \text{Sec}[c + dx] (140 a A b^3 \text{Sin}[c] + 210 a^2 b^2 B \text{Sin}[c] + 25 b^4 B \text{Sin}[c] + 140 a^3 b C \text{Sin}[c] + \right. \\
 & \quad \quad \quad 100 a b^3 C \text{Sin}[c] + 630 a^2 A b^2 \text{Sin}[dx] + 63 A b^4 \text{Sin}[dx] + 420 a^3 b B \text{Sin}[dx] + \\
 & \quad \quad \quad \left. 252 a b^3 B \text{Sin}[dx] + 105 a^4 C \text{Sin}[dx] + 378 a^2 b^2 C \text{Sin}[dx] + 49 b^4 C \text{Sin}[dx]) \right) - \\
 & \quad \left( 16 a^3 A b \text{Cos}[c + dx]^6 \text{Csc}[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]^2\right] \right) \\
 & \quad \frac{(a + b \text{Sec}[c + dx])^4 (A + B \text{Sec}[c + dx] + C \text{Sec}[c + dx]^2)}{\text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \\
 & \quad \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]}
 \end{aligned}$$

$$\begin{aligned}
& \left. \sqrt{1 + \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \right) / \\
& \left( d (b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \text{Cot} [c]^2} \right) - \\
& \left( 16 a A b^3 \cos [c + d x]^6 \text{Csc} [c] \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \text{ArcTan} [\text{Cot} [c]]]^2 \right] \right. \\
& \quad \frac{(a + b \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sec [d x - \text{ArcTan} [\text{Cot} [c]]] \sqrt{1 - \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \\
& \quad \left. \sqrt{-\sqrt{1 + \text{Cot} [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\text{Cot} [c]]] \sqrt{1 + \sin [d x - \text{ArcTan} [\text{Cot} [c]]}} \right) / \\
& \left( 3 d (b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \text{Cot} [c]^2} \right) - \\
& \left( 4 a^4 B \cos [c + d x]^6 \text{Csc} [c] \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \text{ArcTan} [\text{Cot} [c]]]^2 \right] \right. \\
& \quad \frac{(a + b \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sec [d x - \text{ArcTan} [\text{Cot} [c]]] \sqrt{1 - \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \\
& \quad \left. \sqrt{-\sqrt{1 + \text{Cot} [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\text{Cot} [c]]] \sqrt{1 + \sin [d x - \text{ArcTan} [\text{Cot} [c]]}} \right) / \\
& \left( d (b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \text{Cot} [c]^2} \right) - \\
& \left( 8 a^2 b^2 B \cos [c + d x]^6 \text{Csc} [c] \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \text{ArcTan} [\text{Cot} [c]]]^2 \right] \right. \\
& \quad \frac{(a + b \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sec [d x - \text{ArcTan} [\text{Cot} [c]]] \sqrt{1 - \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \\
& \quad \left. \sqrt{-\sqrt{1 + \text{Cot} [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\text{Cot} [c]]] \sqrt{1 + \sin [d x - \text{ArcTan} [\text{Cot} [c]]}} \right) / \\
& \left( d (b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \text{Cot} [c]^2} \right) - \\
& \left( 20 b^4 B \cos [c + d x]^6 \text{Csc} [c] \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \text{ArcTan} [\text{Cot} [c]]]^2 \right] \right. \\
& \quad \frac{(a + b \sec [c + d x])^4 (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sec [d x - \text{ArcTan} [\text{Cot} [c]]] \sqrt{1 - \sin [d x - \text{ArcTan} [\text{Cot} [c]]]} \\
& \quad \left. \sqrt{-\sqrt{1 + \text{Cot} [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\text{Cot} [c]]] \sqrt{1 + \sin [d x - \text{ArcTan} [\text{Cot} [c]]}} \right) / \\
& \left( 21 d (b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \sqrt{1 + \text{Cot} [c]^2} \right) -
\end{aligned}$$

$$\left( 16 a^3 b C \cos [c+d x]^6 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]\right]^2\right.$$

$$\frac{(a+b \sec [c+d x])^4 (A+B \sec [c+d x]+C \sec [c+d x]^2)}{\sec [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]}}$$

$$\left. \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]}} \right) /$$

$$\left( 3 d (b+a \cos [c+d x])^4 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\cot [c]^2} \right) -$$

$$\left( 80 a b^3 C \cos [c+d x]^6 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]\right]^2\right.$$

$$\frac{(a+b \sec [c+d x])^4 (A+B \sec [c+d x]+C \sec [c+d x]^2)}{\sec [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]}}$$

$$\left. \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]}} \right) /$$

$$\left( 21 d (b+a \cos [c+d x])^4 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \sqrt{1+\cot [c]^2} \right) -$$

$$\left( 2 a^4 A \cos [c+d x]^6 \csc [c] (a+b \sec [c+d x])^4 (A+B \sec [c+d x]+C \sec [c+d x]^2) \right.$$

$$\left. \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\tan [c]]]\right]^2\right) \right.$$

$$\left. \sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c] \right) / \left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \right)$$

$$\sqrt{1+\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2}$$

$$\left. \left. \sqrt{1+\tan [c]^2} \right) - \frac{\frac{\sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}{\cos [c]^2+\sin [c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2}} \right) /$$

$$\left( d (b+a \cos [c+d x])^4 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right) +$$



$$\left( 8 a^3 b B \cos [c+d x]^6 \operatorname{Csc}[c] (a+b \sec [c+d x])^4 (A+B \sec [c+d x]+C \sec [c+d x]^2) \right.$$

$$\left. \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\},\cos [d x+\operatorname{ArcTan}[\tan [c]]\right]^2\right] \right. \right.$$

$$\left. \left. \frac{\sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1-\cos [d x+\operatorname{ArcTan}[\tan [c]]]}} \right) \right) / \left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \right.$$

$$\left. \sqrt{1+\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2} \right.$$

$$\left. \left. \left. \left. \sqrt{1+\tan [c]^2} \right) - \frac{\frac{\sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}{\cos [c]^2+\sin [c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2}} \right) \right) \right) /$$

$$\left( d (b+a \cos [c+d x])^4 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right) +$$

$$\left( 24 a b^3 B \cos [c+d x]^6 \operatorname{Csc}[c] (a+b \sec [c+d x])^4 (A+B \sec [c+d x]+C \sec [c+d x]^2) \right.$$

$$\left. \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\},\cos [d x+\operatorname{ArcTan}[\tan [c]]\right]^2\right] \right. \right.$$

$$\left. \left. \frac{\sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1-\cos [d x+\operatorname{ArcTan}[\tan [c]]]}} \right) \right) / \left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \right.$$

$$\left. \sqrt{1+\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2} \right.$$

$$\left. \left. \left. \left. \sqrt{1+\tan [c]^2} \right) - \frac{\frac{\sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}{\cos [c]^2+\sin [c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2}} \right) \right) \right) /$$

$$\left( 5 d (b+a \cos [c+d x])^4 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right) +$$

$$\left( 2 a^4 C \cos [c+d x]^6 \operatorname{Csc}[c] (a+b \operatorname{Sec}[c+d x])^4 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \right.$$

$$\left. \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\},\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]\right]^2\right] \right. \right.$$

$$\left. \left. \operatorname{Sin}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]\right) / \left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right. \right.$$

$$\left. \left. \sqrt{1+\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1+\operatorname{Tan}[c]^2} \right. \right.$$

$$\left. \left. \sqrt{1+\operatorname{Tan}[c]^2} \right) - \frac{\frac{\operatorname{Sin}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1+\operatorname{Tan}[c]^2}} + \frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1+\operatorname{Tan}[c]^2}}{\cos [c]^2+\operatorname{Sin}[c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1+\operatorname{Tan}[c]^2}} \right) /$$

$$\left. \left( d (b+a \cos [c+d x])^4 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right) + \right.$$

$$\left( 36 a^2 b^2 C \cos [c+d x]^6 \operatorname{Csc}[c] (a+b \operatorname{Sec}[c+d x])^4 (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) \right.$$

$$\left. \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\},\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]\right]^2\right] \right. \right.$$

$$\left. \left. \operatorname{Sin}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]\right) / \left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right. \right.$$

$$\left. \left. \sqrt{1+\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1+\operatorname{Tan}[c]^2} \right. \right.$$

$$\left. \left. \sqrt{1+\operatorname{Tan}[c]^2} \right) - \frac{\frac{\operatorname{Sin}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1+\operatorname{Tan}[c]^2}} + \frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1+\operatorname{Tan}[c]^2}}{\cos [c]^2+\operatorname{Sin}[c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1+\operatorname{Tan}[c]^2}} \right) /$$

$$\left. \left( 5 d (b+a \cos [c+d x])^4 (A+2 C+2 B \cos [c+d x]+A \cos [2 c+2 d x]) \right) + \right.$$

$$\left( 14 b^4 C \cos [c + d x]^6 \operatorname{Csc}[c] (a + b \operatorname{Sec}[c + d x])^4 (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) \right.$$

$$\left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]\right]^2 \right.$$

$$\left. \left. \operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] \right) / \left( \sqrt{1 - \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right. \right.$$

$$\left. \left. \sqrt{1 + \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \operatorname{Tan}[c]^2} \right. \right.$$

$$\left. \left. \left. \left. \sqrt{1 + \operatorname{Tan}[c]^2} \right) - \frac{\frac{\operatorname{Sin}[d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1 + \operatorname{Tan}[c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}}{\cos [c]^2 + \operatorname{Sin}[c]^2}}{\sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \operatorname{Tan}[c]^2}} \right) \right) / \right.$$

$$\left. \left. (15 d (b + a \cos [c + d x])^4 (A + 2 C + 2 B \cos [c + d x] + A \cos [2 c + 2 d x]) \right) \right)$$

**Problem 1320: Attempted integration timed out after 120 seconds.**

$$\int \frac{\sqrt{\cos [c + d x]} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{a + b \operatorname{Sec}[c + d x]} dx$$

Optimal (type 4, 97 leaves, 6 steps):

$$\frac{2 A \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), 2\right]}{a d} - \frac{2 (A b - a B) \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), 2\right]}{a^2 d} +$$

$$\frac{2 (A b^2 - a (b B - a C)) \operatorname{EllipticPi}\left[\frac{2 a}{a + b}, \frac{1}{2} (c + d x), 2\right]}{a^2 (a + b) d}$$

Result (type 1, 1 leaves):

???

**Problem 1334: Unable to integrate problem.**

$$\int \cos [c + d x]^{9/2} \sqrt{a + b \operatorname{Sec}[c + d x]} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 4, 457 leaves, 12 steps):

$$\begin{aligned}
 & - \left( \left( 2 (a^2 - b^2) (16 A b^3 - 75 a^3 B - 24 a b^2 B + 6 a^2 b (6 A + 7 C)) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \right. \\
 & \quad \left. \left. \text{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right) / \left( 315 a^4 d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \right) \right) - \\
 & \left( 2 (16 A b^4 - 57 a^3 b B - 24 a b^3 B + 6 a^2 b^2 (4 A + 7 C) - 21 a^4 (7 A + 9 C)) \sqrt{\cos [c + d x]} \right. \\
 & \quad \left. \text{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \sec [c + d x]} \right) / \left( 315 a^4 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right) + \frac{1}{315 a^3 d} \\
 & 2 (8 A b^3 + 75 a^3 B - 12 a b^2 B + a^2 b (13 A + 21 C)) \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \sin [c + d x] - \\
 & \frac{1}{315 a^2 d} 2 (6 A b^2 - 9 a b B - 7 a^2 (7 A + 9 C)) \cos [c + d x]^{3/2} \sqrt{a + b \sec [c + d x]} \sin [c + d x] + \\
 & \frac{2 (A b + 9 a B) \cos [c + d x]^{5/2} \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{63 a d} + \\
 & \frac{2 A \cos [c + d x]^{7/2} \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{9 d}
 \end{aligned}$$

Result (type 8, 47 leaves):

$$\int \cos [c + d x]^{9/2} \sqrt{a + b \sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

### Problem 1335: Unable to integrate problem.

$$\int \cos [c + d x]^{7/2} \sqrt{a + b \sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 4, 360 leaves, 11 steps):

$$\begin{aligned}
 & \left( 2 (a^2 - b^2) (25 a^2 A + 8 A b^2 - 14 a b B + 35 a^2 C) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \text{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right) / \\
 & \left( 105 a^3 d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \right) + \\
 & \left( 2 (8 A b^3 + 63 a^3 B - 14 a b^2 B + a^2 b (19 A + 35 C)) \sqrt{\cos [c + d x]} \text{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right. \\
 & \quad \left. \sqrt{a + b \sec [c + d x]} \right) / \left( 105 a^3 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right) - \frac{1}{105 a^2 d} \\
 & 2 (4 A b^2 - 7 a b B - 5 a^2 (5 A + 7 C)) \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \sin [c + d x] + \\
 & \frac{2 (A b + 7 a B) \cos [c + d x]^{3/2} \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{35 a d} + \\
 & \frac{2 A \cos [c + d x]^{5/2} \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{7 d}
 \end{aligned}$$



Result (type 8, 47 leaves):

$$\int \cos [c + d x]^{7/2} \sqrt{a + b \operatorname{Sec}[c + d x]} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) dx$$

Problem 1336: Unable to integrate problem.

$$\int \cos [c + d x]^{5/2} \sqrt{a + b \operatorname{Sec}[c + d x]} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 4, 273 leaves, 10 steps):

$$\frac{2 (a^2 - b^2) (2 A b - 5 a B) \sqrt{\frac{b+a \operatorname{Cos}[c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a+b}\right]}{15 a^2 d \sqrt{\operatorname{Cos}[c + d x]} \sqrt{a + b \operatorname{Sec}[c + d x]}} - \frac{2 (2 A b^2 - 5 a b B - 3 a^2 (3 A + 5 C)) \sqrt{\operatorname{Cos}[c + d x]}}{15 a^2 d \sqrt{\frac{b+a \operatorname{Cos}[c+d x]}{a+b}}} + \frac{\operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a+b}\right] \sqrt{a + b \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{15 a d} + \frac{2 (A b + 5 a B) \sqrt{\operatorname{Cos}[c + d x]} \sqrt{a + b \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{15 a d} + \frac{2 A \operatorname{Cos}[c + d x]^{3/2} \sqrt{a + b \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{5 d}$$

Result (type 8, 47 leaves):

$$\int \cos [c + d x]^{5/2} \sqrt{a + b \operatorname{Sec}[c + d x]} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) dx$$

Problem 1337: Attempted integration timed out after 120 seconds.

$$\int \cos [c + d x]^{3/2} \sqrt{a + b \operatorname{Sec}[c + d x]} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 4, 277 leaves, 13 steps):

$$\begin{aligned}
 & - \frac{2 (A b^2 - a^2 (A + 3 C)) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{3 a d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\
 & \frac{2 b C \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\
 & \left(2 (A b + 3 a B) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}\right) / \\
 & \left(3 a d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}\right) + \frac{2 A \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{3 d}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

### Problem 1338: Unable to integrate problem.

$$\int \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]} (A+B \sec [c+d x]+C \sec [c+d x]^2) dx$$

Optimal (type 4, 258 leaves, 13 steps):

$$\begin{aligned}
 & \frac{(2 a B+b C) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\
 & \frac{(2 b B+a C) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \frac{1}{d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}} \\
 & (2 A-C) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]} + \\
 & \frac{C \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{d \sqrt{\cos [c+d x]}}
 \end{aligned}$$

Result (type 8, 47 leaves):

$$\int \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]} (A+B \sec [c+d x]+C \sec [c+d x]^2) dx$$

### Problem 1339: Unable to integrate problem.

$$\int \frac{\sqrt{a+b \sec [c+d x]} (A+B \sec [c+d x]+C \sec [c+d x]^2)}{\sqrt{\cos [c+d x]}} dx$$

Optimal (type 4, 346 leaves, 14 steps):

$$\begin{aligned}
 & \frac{(8 a A + 4 b B + 3 a C) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{4 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\
 & \left( \frac{(8 A b^2 + 4 a b B - a^2 C + 4 b^2 C) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{(4 b d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]})} - \right. \\
 & \left. \frac{(4 b B + a C) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}}{(4 b d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}) + \frac{C \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{2 d \cos [c+d x]^{3/2}}} + \right. \\
 & \left. \frac{(4 b B + a C) \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{4 b d \sqrt{\cos [c+d x]}} \right) /
 \end{aligned}$$

Result (type 8, 47 leaves):

$$\int \frac{\sqrt{a+b \sec [c+d x]} (A+B \sec [c+d x]+C \sec [c+d x]^2)}{\sqrt{\cos [c+d x]}} dx$$

**Problem 1340: Unable to integrate problem.**

$$\int \frac{\sqrt{a+b \sec [c+d x]} (A+B \sec [c+d x]+C \sec [c+d x]^2)}{\cos [c+d x]^{3/2}} dx$$

Optimal (type 4, 447 leaves, 15 steps):

$$\begin{aligned} & \left( (24 A b^2 + 18 a b B - a^2 C + 16 b^2 C) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right) / \\ & \left( 24 b d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \right) - \\ & \left( (2 a^2 b B - 8 b^3 B - a^3 C - 4 a b^2 (2 A + C)) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right) / \\ & \left( 8 b^2 d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \right) - \\ & \left( (24 A b^2 + 6 a b B - 3 a^2 C + 16 b^2 C) \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right. \\ & \left. \sqrt{a + b \sec [c + d x]} \right) / \left( 24 b^2 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right) + \\ & \frac{C \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{3 d \cos [c + d x]^{5/2}} + \frac{(6 b B + a C) \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{12 b d \cos [c + d x]^{3/2}} + \\ & \frac{(24 A b^2 + 6 a b B - 3 a^2 C + 16 b^2 C) \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{24 b^2 d \sqrt{\cos [c + d x]}} \end{aligned}$$

Result (type 8, 47 leaves):

$$\int \frac{\sqrt{a + b \sec [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\cos [c + d x]^{3/2}} dx$$

**Problem 1341: Attempted integration timed out after 120 seconds.**

$$\int \cos [c + d x]^{9/2} (a + b \sec [c + d x])^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 4, 455 leaves, 12 steps):

$$\begin{aligned}
 & \left( 2 (a^2 - b^2) (8 A b^3 + 75 a^3 B - 18 a b^2 B + a^2 (39 A b + 63 b C)) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \\
 & \quad \left. \text{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right) / \left( 315 a^3 d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \right) + \\
 & \left( 2 (8 A b^4 + 246 a^3 b B - 18 a b^3 B + 21 a^4 (7 A + 9 C) + 3 a^2 b^2 (11 A + 21 C)) \sqrt{\cos [c + d x]} \right. \\
 & \quad \left. \text{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b} \sqrt{a + b \sec [c + d x]}\right] \right) / \left( 315 a^3 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right) - \frac{1}{315 a^2 d} \\
 & \frac{2 (4 A b^3 - 75 a^3 B - 9 a b^2 B - 2 a^2 b (44 A + 63 C)) \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \sin [c + d x] +}{315 a d} \\
 & \frac{2 (3 A b^2 + 72 a b B + 7 a^2 (7 A + 9 C)) \cos [c + d x]^{3/2} \sqrt{a + b \sec [c + d x]} \sin [c + d x] +}{21 d} \\
 & \frac{2 (A b + 3 a B) \cos [c + d x]^{5/2} \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{9 d}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 1342: Attempted integration timed out after 120 seconds.**

$$\int \cos [c + d x]^{7/2} (a + b \sec [c + d x])^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 4, 359 leaves, 11 steps):

$$\begin{aligned}
 & \left( 2 (a^2 - b^2) (25 a^2 A - 6 A b^2 + 21 a b B + 35 a^2 C) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \text{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right) / \\
 & \quad \left( 105 a^2 d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \right) - \\
 & \left( 2 (6 A b^3 - 63 a^3 B - 21 a b^2 B - 2 a^2 b (41 A + 70 C)) \sqrt{\cos [c + d x]} \text{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b} \right. \right. \\
 & \quad \left. \left. \sqrt{a + b \sec [c + d x]}\right] \right) / \left( 105 a^2 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right) + \frac{1}{105 a d} \\
 & \frac{2 (3 A b^2 + 42 a b B + 5 a^2 (5 A + 7 C)) \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \sin [c + d x] +}{35 d} \\
 & \frac{2 (3 A b + 7 a B) \cos [c + d x]^{3/2} \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{7 d} \\
 & \frac{2 A \cos [c + d x]^{5/2} (a + b \sec [c + d x])^{3/2} \sin [c + d x]}{7 d}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 1343: Attempted integration timed out after 120 seconds.**

$$\int \cos [c+d x]^{5 / 2}(a+b \operatorname{Sec}[c+d x])^{3 / 2}(A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) d x$$

Optimal (type 4, 356 leaves, 14 steps):

$$\begin{aligned} & -\left(\left(2\left(3 A b^3-5 a^3 B+5 a b^2 B-3 a^2 b(A+5 C)\right) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]\right) / \right. \\ & \quad \left.\left(15 a d \sqrt{\cos [c+d x]} \sqrt{a+b \operatorname{Sec}[c+d x]}\right)\right)+ \\ & \quad \frac{2 b^2 C \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{d \sqrt{\cos [c+d x]} \sqrt{a+b \operatorname{Sec}[c+d x]}}+ \\ & \quad \frac{\left(2\left(3 A b^2+20 a b B+3 a^2(3 A+5 C)\right) \sqrt{\cos [c+d x]}\right)}{\operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \operatorname{Sec}[c+d x]}} / \left(15 a d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}\right)+ \\ & \quad \frac{2(3 A b+5 a B) \sqrt{\cos [c+d x]} \sqrt{a+b \operatorname{Sec}[c+d x]} \sin [c+d x]}{15 d}+ \\ & \quad \frac{2 A \cos [c+d x]^{3 / 2}(a+b \operatorname{Sec}[c+d x])^{3 / 2} \sin [c+d x]}{5 d} \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 1344: Attempted integration timed out after 120 seconds.**

$$\int \cos [c+d x]^{3 / 2}(a+b \operatorname{Sec}[c+d x])^{3 / 2}(A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2) d x$$

Optimal (type 4, 340 leaves, 14 steps):

$$\left( (6 a b B - b^2 (2 A - 3 C) + 2 a^2 (A + 3 C)) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right) /$$

$$\left( 3 d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \right) +$$

$$\frac{b (2 b B + 3 a C) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticPi}\left[2, \frac{1}{2} (c + d x), \frac{2 a}{a + b}\right]}{d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]}} + \frac{1}{3 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}}}$$

$$(8 A b + 6 a B - 3 b C) \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \sec [c + d x]} -$$

$$\frac{b (2 A - 3 C) \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{3 d \sqrt{\cos [c + d x]}} + \frac{2 A \sqrt{\cos [c + d x]} (a + b \sec [c + d x])^{3/2} \sin [c + d x]}{3 d}$$

Result(type 1, 1 leaves):

???

**Problem 1345: Attempted integration timed out after 120 seconds.**

$$\int \sqrt{\cos [c + d x]} (a + b \sec [c + d x])^{3/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 4, 353 leaves, 14 steps):

$$\left( (8 a^2 B + 4 b^2 B + a b (8 A + 7 C)) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right) /$$

$$\left( 4 d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \right) +$$

$$\left( (8 A b^2 + 12 a b B + 3 a^2 C + 4 b^2 C) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticPi}\left[2, \frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right) /$$

$$\left( 4 d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \right) + \frac{1}{4 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}}}$$

$$(8 a A - 4 b B - 5 a C) \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \sec [c + d x]} +$$

$$\frac{(4 b B + 3 a C) \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{4 d \sqrt{\cos [c + d x]}} + \frac{C (a + b \sec [c + d x])^{3/2} \sin [c + d x]}{2 d \sqrt{\cos [c + d x]}}$$

Result(type 1, 1 leaves):

???

**Problem 1346: Attempted integration timed out after 120 seconds.**

$$\int \frac{(a + b \operatorname{Sec}[c + d x])^{3/2} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\sqrt{\operatorname{Cos}[c + d x]}} dx$$

Optimal (type 4, 446 leaves, 15 steps):

$$\left( (42 a b B + 8 b^2 (3 A + 2 C) + a^2 (48 A + 17 C)) \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right) /$$

$$\left( 24 d \sqrt{\operatorname{Cos}[c + d x]} \sqrt{a + b \operatorname{Sec}[c + d x]} \right) +$$

$$\left( (6 a^2 b B + 8 b^3 B - a^3 C + 12 a b^2 (2 A + C)) \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \right.$$

$$\left. \operatorname{EllipticPi}\left[2, \frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right) / \left( 8 b d \sqrt{\operatorname{Cos}[c + d x]} \sqrt{a + b \operatorname{Sec}[c + d x]} \right) -$$

$$\left( (24 A b^2 + 30 a b B + 3 a^2 C + 16 b^2 C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right.$$

$$\left. \sqrt{a + b \operatorname{Sec}[c + d x]} \right) / \left( 24 b d \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \right) +$$

$$\frac{(2 b B + a C) \sqrt{a + b \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{4 d \operatorname{Cos}[c + d x]^{3/2}} +$$

$$\frac{(24 A b^2 + 30 a b B + 3 a^2 C + 16 b^2 C) \sqrt{a + b \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{24 b d \sqrt{\operatorname{Cos}[c + d x]}} +$$

$$\frac{C (a + b \operatorname{Sec}[c + d x])^{3/2} \operatorname{Sin}[c + d x]}{3 d \operatorname{Cos}[c + d x]^{3/2}}$$

Result (type 1, 1 leaves):

???

**Problem 1347: Attempted integration timed out after 120 seconds.**

$$\int \frac{(a + b \operatorname{Sec}[c + d x])^{3/2} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{\operatorname{Cos}[c + d x]^{3/2}} dx$$

Optimal (type 4, 551 leaves, 16 steps):



$$\begin{aligned}
 & \left( (136 a^2 b B + 128 b^3 B - 3 a^3 C + 12 a b^2 (28 A + 19 C)) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \\
 & \quad \left. \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right) / (192 b d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]}) - \\
 & \left( (8 a^3 b B - 96 a b^3 B - 3 a^4 C - 24 a^2 b^2 (2 A + C) - 16 b^4 (4 A + 3 C)) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \\
 & \quad \left. \operatorname{EllipticPi}\left[2, \frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right) / (64 b^2 d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]}) - \\
 & \left( (24 a^2 b B + 128 b^3 B - 9 a^3 C + 12 a b^2 (20 A + 13 C)) \sqrt{\cos [c + d x]} \right. \\
 & \quad \left. \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \sec [c + d x]} \right) / \\
 & \left( 192 b^2 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right) + \frac{(8 b B + 3 a C) \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{24 d \cos [c + d x]^{5/2}} + \\
 & \frac{(48 A b^2 + 56 a b B + 3 a^2 C + 36 b^2 C) \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{96 b d \cos [c + d x]^{3/2}} + \\
 & \left( (24 a^2 b B + 128 b^3 B - 9 a^3 C + 12 a b^2 (20 A + 13 C)) \sqrt{a + b \sec [c + d x]} \sin [c + d x] \right) / \\
 & \left( 192 b^2 d \sqrt{\cos [c + d x]} \right) + \frac{C (a + b \sec [c + d x])^{3/2} \sin [c + d x]}{4 d \cos [c + d x]^{5/2}}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 1348: Attempted integration timed out after 120 seconds.**

$$\int \cos [c + d x]^{11/2} (a + b \sec [c + d x])^{5/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 4, 565 leaves, 13 steps):

$$\begin{aligned}
 & \left( 2 (a^2 - b^2) (40 A b^4 + 1254 a^3 b B - 110 a b^3 B + 75 a^4 (9 A + 11 C) + 15 a^2 b^2 (19 A + 33 C)) \right. \\
 & \quad \left. \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right) / \\
 & \quad \left( 3465 a^3 d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \right) + \\
 & \quad \left( 2 (40 A b^5 + 1617 a^5 B + 3069 a^3 b^2 B - 110 a b^4 B + 15 a^2 b^3 (17 A + 33 C) + 15 a^4 b (247 A + 319 C)) \right. \\
 & \quad \left. \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \sec [c + d x]} \right) / \\
 & \quad \left( 3465 a^3 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} - \frac{1}{3465 a^2 d} \right) \\
 & \quad 2 (20 A b^4 - 1793 a^3 b B - 55 a b^3 B - 75 a^4 (9 A + 11 C) - 5 a^2 b^2 (205 A + 297 C)) \\
 & \quad \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \sin [c + d x] + \\
 & \quad \frac{1}{3465 a d} 2 (15 A b^3 + 539 a^3 B + 825 a b^2 B + 5 a^2 b (229 A + 297 C)) \\
 & \quad \cos [c + d x]^{3/2} \sqrt{a + b \sec [c + d x]} \sin [c + d x] + \frac{1}{231 d} \\
 & \quad 2 (5 A b^2 + 44 a b B + 3 a^2 (9 A + 11 C)) \cos [c + d x]^{5/2} \sqrt{a + b \sec [c + d x]} \sin [c + d x] + \\
 & \quad \frac{2 (5 A b + 11 a B) \cos [c + d x]^{7/2} (a + b \sec [c + d x])^{3/2} \sin [c + d x]}{99 d} + \\
 & \quad \frac{2 A \cos [c + d x]^{9/2} (a + b \sec [c + d x])^{5/2} \sin [c + d x]}{11 d}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 1349: Attempted integration timed out after 120 seconds.**

$$\int \cos [c + d x]^{9/2} (a + b \sec [c + d x])^{5/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 4, 452 leaves, 12 steps):

$$\begin{aligned}
 & - \left( \left( 2 (a^2 - b^2) (10 A b^3 - 75 a^3 B - 45 a b^2 B - 6 a^2 b (19 A + 28 C)) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \right. \\
 & \quad \left. \left. \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right) / \left( 315 a^2 d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \right) \right) - \\
 & \left( 2 (10 A b^4 - 435 a^3 b B - 45 a b^3 B - 21 a^4 (7 A + 9 C) - 3 a^2 b^2 (93 A + 161 C)) \sqrt{\cos [c + d x]} \right. \\
 & \quad \left. \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \sec [c + d x]} \right) / \left( 315 a^2 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right) + \\
 & \frac{1}{315 a d} 2 (5 A b^3 + 75 a^3 B + 135 a b^2 B + a^2 b (163 A + 231 C)) \sqrt{\cos [c + d x]} \\
 & \quad \sqrt{a + b \sec [c + d x]} \sin [c + d x] + \frac{1}{315 d} \\
 & 2 (15 A b^2 + 90 a b B + 7 a^2 (7 A + 9 C)) \cos [c + d x]^{3/2} \sqrt{a + b \sec [c + d x]} \sin [c + d x] + \\
 & \frac{2 (5 A b + 9 a B) \cos [c + d x]^{5/2} (a + b \sec [c + d x])^{3/2} \sin [c + d x]}{63 d} + \\
 & \frac{2 A \cos [c + d x]^{7/2} (a + b \sec [c + d x])^{5/2} \sin [c + d x]}{9 d}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 1350: Attempted integration timed out after 120 seconds.**

$$\int \cos [c + d x]^{7/2} (a + b \sec [c + d x])^{5/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 4, 441 leaves, 15 steps):

$$\begin{aligned}
 & - \left( \left( 2 (15 A b^4 - 56 a^3 b B + 56 a b^3 B + 10 a^2 b^2 (A - 7 C) - 5 a^4 (5 A + 7 C)) \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \right. \right. \\
 & \quad \left. \left. \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right) / \left( 105 a d \sqrt{\operatorname{Cos}[c + d x]} \sqrt{a + b \operatorname{Sec}[c + d x]} \right) \right) + \\
 & \quad \frac{2 b^3 C \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c + d x), \frac{2 a}{a + b}\right]}{d \sqrt{\operatorname{Cos}[c + d x]} \sqrt{a + b \operatorname{Sec}[c + d x]}} + \\
 & \quad \left( 2 (15 A b^3 + 63 a^3 B + 161 a b^2 B + 5 a^2 b (29 A + 49 C)) \sqrt{\operatorname{Cos}[c + d x]} \right. \\
 & \quad \left. \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \operatorname{Sec}[c + d x]} \right) / \left( 105 a d \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \right) + \\
 & \quad \frac{1}{105 d} 2 (15 A b^2 + 56 a b B + 5 a^2 (5 A + 7 C)) \sqrt{\operatorname{Cos}[c + d x]} \sqrt{a + b \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x] + \\
 & \quad \frac{2 (5 A b + 7 a B) \operatorname{Cos}[c + d x]^{3/2} (a + b \operatorname{Sec}[c + d x])^{3/2} \operatorname{Sin}[c + d x]}{35 d} + \\
 & \quad \frac{2 A \operatorname{Cos}[c + d x]^{5/2} (a + b \operatorname{Sec}[c + d x])^{5/2} \operatorname{Sin}[c + d x]}{7 d}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 1351: Attempted integration timed out after 120 seconds.**

$$\int \operatorname{Cos}[c + d x]^{5/2} (a + b \operatorname{Sec}[c + d x])^{5/2} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 4, 419 leaves, 15 steps):

$$\left( (10 a^3 B + 20 a b^2 B - b^3 (16 A - 15 C) + 4 a^2 b (4 A + 15 C)) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \\ \left. \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right) / \left( 15 d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \right) + \\ \frac{b^2 (2 b B + 5 a C) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c + d x), \frac{2 a}{a + b}\right]}{d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]}} + \\ \left( (70 a b B + b^2 (46 A - 15 C) + 6 a^2 (3 A + 5 C)) \sqrt{\cos [c + d x]} \right. \\ \left. \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \sec [c + d x]} \right) / \left( 15 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right) - \\ \frac{b (16 A b + 10 a B - 15 b C) \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{15 d \sqrt{\cos [c + d x]}} + \\ \frac{2 (A b + a B) \sqrt{\cos [c + d x]} (a + b \sec [c + d x])^{3/2} \sin [c + d x]}{3 d} + \\ \frac{2 A \cos [c + d x]^{3/2} (a + b \sec [c + d x])^{5/2} \sin [c + d x]}{5 d}$$

Result (type 1, 1 leaves):

???

**Problem 1352: Attempted integration timed out after 120 seconds.**

$$\int \cos [c + d x]^{3/2} (a + b \sec [c + d x])^{5/2} (A + B \sec [c + d x] + C \sec [c + d x]^2) dx$$

Optimal (type 4, 427 leaves, 15 steps):

$$\begin{aligned}
 & \left( (48 a^2 b B + 12 b^3 B + 8 a^3 (A + 3 C) + a b^2 (16 A + 33 C)) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \\
 & \quad \left. \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right) / \left( 12 d \sqrt{\cos [c + d x]} \sqrt{a + b \operatorname{Sec}[c + d x]} \right) + \\
 & \left( b (8 A b^2 + 20 a b B + 15 a^2 C + 4 b^2 C) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right) / \\
 & \left( 4 d \sqrt{\cos [c + d x]} \sqrt{a + b \operatorname{Sec}[c + d x]} \right) + \\
 & \left( (24 a^2 B - 12 b^2 B + a b (56 A - 27 C)) \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right. \\
 & \quad \left. \sqrt{a + b \operatorname{Sec}[c + d x]} \right) / \left( 12 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right) - \\
 & \frac{b (8 a A - 12 b B - 21 a C) \sqrt{a + b \operatorname{Sec}[c + d x]} \sin [c + d x]}{12 d \sqrt{\cos [c + d x]}} - \\
 & \frac{b (4 A - 3 C) (a + b \operatorname{Sec}[c + d x])^{3/2} \sin [c + d x]}{6 d \sqrt{\cos [c + d x]}} + \\
 & \frac{2 A \sqrt{\cos [c + d x]} (a + b \operatorname{Sec}[c + d x])^{5/2} \sin [c + d x]}{3 d}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 1353: Attempted integration timed out after 120 seconds.**

$$\int \sqrt{\cos [c + d x]} (a + b \operatorname{Sec}[c + d x])^{5/2} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2) dx$$

Optimal (type 4, 453 leaves, 15 steps):

$$\begin{aligned}
 & \left( (48 a^3 B + 66 a b^2 B + 8 b^3 (3 A + 2 C) + a^2 b (96 A + 59 C)) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \\
 & \quad \left. \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right) / \left( 24 d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \right) + \\
 & \left( (30 a^2 b B + 8 b^3 B + 5 a^3 C + 20 a b^2 (2 A + C)) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \\
 & \quad \left. \operatorname{EllipticPi}\left[2, \frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right) / \left( 8 d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \right) - \\
 & \left( (54 a b B - a^2 (48 A - 33 C) + 8 b^2 (3 A + 2 C)) \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right. \\
 & \quad \left. \sqrt{a + b \sec [c + d x]} \right) / \left( 24 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right) + \\
 & \frac{(24 A b^2 + 42 a b B + 15 a^2 C + 16 b^2 C) \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{24 d \sqrt{\cos [c + d x]}} + \\
 & \frac{(6 b B + 5 a C) (a + b \sec [c + d x])^{3/2} \sin [c + d x]}{12 d \sqrt{\cos [c + d x]}} + \\
 & \frac{C (a + b \sec [c + d x])^{5/2} \sin [c + d x]}{3 d \sqrt{\cos [c + d x]}}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 1354: Attempted integration timed out after 120 seconds.**

$$\int \frac{(a + b \sec [c + d x])^{5/2} (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sqrt{\cos [c + d x]}} dx$$

Optimal (type 4, 550 leaves, 16 steps):

$$\left( (472 a^2 b B + 128 b^3 B + 4 a b^2 (132 A + 89 C) + a^3 (384 A + 133 C)) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \\ \left. \text{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right) / \left( 192 d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \right) + \\ \left( (40 a^3 b B + 160 a b^3 B - 5 a^4 C + 120 a^2 b^2 (2 A + C) + 16 b^4 (4 A + 3 C)) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \\ \left. \text{EllipticPi}\left[2, \frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right) / \left( 64 b d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \right) - \\ \left( (264 a^2 b B + 128 b^3 B + 15 a^3 C + 4 a b^2 (108 A + 71 C)) \sqrt{\cos [c + d x]} \right. \\ \left. \text{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b} \sqrt{a + b \sec [c + d x]}\right] \right) / \left( 192 b d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right) + \\ \frac{(16 A b^2 + 24 a b B + 5 a^2 C + 12 b^2 C) \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{32 d \cos [c + d x]^{3/2}} + \\ \left( (264 a^2 b B + 128 b^3 B + 15 a^3 C + 4 a b^2 (108 A + 71 C)) \sqrt{a + b \sec [c + d x]} \sin [c + d x] \right) / \\ \left( 192 b d \sqrt{\cos [c + d x]} \right) + \\ \frac{(8 b B + 5 a C) (a + b \sec [c + d x])^{3/2} \sin [c + d x]}{24 d \cos [c + d x]^{3/2}} + \frac{C (a + b \sec [c + d x])^{5/2} \sin [c + d x]}{4 d \cos [c + d x]^{3/2}}$$

Result (type 1, 1 leaves):

???

**Problem 1355: Attempted integration timed out after 120 seconds.**

$$\int \frac{(a + b \sec [c + d x])^{5/2} (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\cos [c + d x]^{3/2}} dx$$

Optimal (type 4, 674 leaves, 17 steps):



$$\begin{aligned}
 & \left( (1330 a^3 b B + 3560 a b^3 B - 15 a^4 C + 256 b^4 (5 A + 4 C) + 4 a^2 b^2 (1180 A + 809 C)) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \\
 & \quad \left. \text{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right) / \left( 1920 b d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \right) - \\
 & \left( (10 a^4 b B - 240 a^2 b^3 B - 96 b^5 B - 3 a^5 C - 40 a^3 b^2 (2 A + C) - 80 a b^4 (4 A + 3 C)) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \\
 & \quad \left. \text{EllipticPi}\left[2, \frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right) / \left( 128 b^2 d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \right) - \\
 & \left( (150 a^3 b B + 2840 a b^3 B - 45 a^4 C + 256 b^4 (5 A + 4 C) + 12 a^2 b^2 (220 A + 141 C)) \sqrt{\cos [c + d x]} \right. \\
 & \quad \left. \text{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b} \sqrt{a + b \sec [c + d x]}\right] \right) / \left( 1920 b^2 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right) + \\
 & \frac{(80 A b^2 + 110 a b B + 15 a^2 C + 64 b^2 C) \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{240 d \cos [c + d x]^{5/2}} + \\
 & \left( (590 a^2 b B + 360 b^3 B + 15 a^3 C + 4 a b^2 (260 A + 193 C)) \sqrt{a + b \sec [c + d x]} \sin [c + d x] \right) / \\
 & (960 b d \cos [c + d x]^{3/2}) + \\
 & \left( (150 a^3 b B + 2840 a b^3 B - 45 a^4 C + 256 b^4 (5 A + 4 C) + 12 a^2 b^2 (220 A + 141 C)) \right. \\
 & \quad \left. \sqrt{a + b \sec [c + d x]} \sin [c + d x] \right) / \left( 1920 b^2 d \sqrt{\cos [c + d x]} \right) + \\
 & \frac{(2 b B + a C) (a + b \sec [c + d x])^{3/2} \sin [c + d x]}{8 d \cos [c + d x]^{5/2}} + \frac{C (a + b \sec [c + d x])^{5/2} \sin [c + d x]}{5 d \cos [c + d x]^{5/2}}
 \end{aligned}$$

Result(type 1, 1 leaves):

???

### Problem 1356: Unable to integrate problem.

$$\int \frac{\cos [c + d x]^{7/2} (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sqrt{a + b \sec [c + d x]}} dx$$

Optimal (type 4, 380 leaves, 11 steps):

$$\left( 2 (48 A b^4 - 49 a^3 b B - 56 a b^3 B + 5 a^4 (5 A + 7 C) + 2 a^2 b^2 (16 A + 35 C)) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \\ \left. \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right) / \left( 105 a^4 d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \right) - \\ \left( 2 (48 A b^3 - 63 a^3 B - 56 a b^2 B + a^2 (44 A b + 70 b C)) \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right. \\ \left. \sqrt{a + b \sec [c + d x]} \right) / \left( 105 a^4 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right) + \frac{1}{105 a^3 d} \\ 2 (24 A b^2 - 28 a b B + 5 a^2 (5 A + 7 C)) \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \sin [c + d x] - \\ \frac{2 (6 A b - 7 a B) \cos [c + d x]^{3/2} \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{35 a^2 d} + \\ \frac{2 A \cos [c + d x]^{5/2} \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{7 a d}$$

Result (type 8, 47 leaves):

$$\int \frac{\cos [c + d x]^{7/2} (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sqrt{a + b \sec [c + d x]}} dx$$

Problem 1357: Unable to integrate problem.

$$\int \frac{\cos [c + d x]^{5/2} (A + B \sec [c + d x] + C \sec [c + d x]^2)}{\sqrt{a + b \sec [c + d x]}} dx$$

Optimal (type 4, 291 leaves, 10 steps):

$$- \left( \left( 2 (8 A b^3 - 5 a^3 B - 10 a b^2 B + a^2 b (7 A + 15 C)) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \right. \\ \left. \left. \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right) / \left( 15 a^3 d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \right) \right) + \\ \left( 2 (8 A b^2 - 10 a b B + 3 a^2 (3 A + 5 C)) \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right. \\ \left. \sqrt{a + b \sec [c + d x]} \right) / \left( 15 a^3 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right) - \\ \frac{2 (4 A b - 5 a B) \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{15 a^2 d} + \\ \frac{2 A \cos [c + d x]^{3/2} \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{5 a d}$$

Result (type 8, 47 leaves):

$$\int \frac{\cos [c+d x]^{5 / 2} (A+B \sec [c+d x]+C \sec [c+d x]^2)}{\sqrt{a+b \sec [c+d x]}} d x$$

**Problem 1358: Attempted integration timed out after 120 seconds.**

$$\int \frac{\cos [c+d x]^{3 / 2} (A+B \sec [c+d x]+C \sec [c+d x]^2)}{\sqrt{a+b \sec [c+d x]}} d x$$

Optimal (type 4, 216 leaves, 9 steps):

$$\begin{aligned} & \left( 2 (2 A b^2 - 3 a b B + a^2 (A + 3 C)) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \right) / \\ & \left( 3 a^2 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]} \right) - \\ & \left( 2 (2 A b - 3 a B) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]} \right) / \\ & \left( 3 a^2 d \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \right) + \frac{2 A \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{3 a d} \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 1359: Unable to integrate problem.**

$$\int \frac{\sqrt{\cos [c+d x]} (A+B \sec [c+d x]+C \sec [c+d x]^2)}{\sqrt{a+b \sec [c+d x]}} d x$$

Optimal (type 4, 219 leaves, 12 steps):

$$\begin{aligned} & \frac{2 (A b - a B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{a d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\ & \frac{2 C \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\ & \frac{2 A \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}}{a d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}} \end{aligned}$$

Result (type 8, 47 leaves):

$$\int \frac{\sqrt{\cos [c+d x]} \left(A+B \sec [c+d x]+C \sec [c+d x]^2\right)}{\sqrt{a+b \sec [c+d x]}} d x$$

**Problem 1360: Unable to integrate problem.**

$$\int \frac{A+B \sec [c+d x]+C \sec [c+d x]^2}{\sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} d x$$

Optimal (type 4, 260 leaves, 13 steps):

$$\begin{aligned} & \frac{(2 A+C) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\ & \frac{(2 b B-a C) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{b d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} - \\ & \frac{C \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}}{b d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}} + \\ & \frac{C \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{b d \sqrt{\cos [c+d x]}} \end{aligned}$$

Result (type 8, 47 leaves):

$$\int \frac{A+B \sec [c+d x]+C \sec [c+d x]^2}{\sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} d x$$

**Problem 1361: Unable to integrate problem.**

$$\int \frac{A+B \sec [c+d x]+C \sec [c+d x]^2}{\cos [c+d x]^{3 / 2} \sqrt{a+b \sec [c+d x]}} d x$$

Optimal (type 4, 350 leaves, 14 steps):

$$\begin{aligned}
 & \frac{(4 b B - a C) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{4 b d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\
 & \left( (8 A b^2 - 4 a b B + 3 a^2 C + 4 b^2 C) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \right) / \\
 & \left( 4 b^2 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]} \right) - \\
 & \left( (4 b B - 3 a C) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]} \right) / \\
 & \left( 4 b^2 d \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \right) + \frac{C \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{2 b d \cos [c+d x]^{3/2}} + \\
 & \frac{(4 b B - 3 a C) \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{4 b^2 d \sqrt{\cos [c+d x]}}
 \end{aligned}$$

Result (type 8, 47 leaves):

$$\int \frac{A + B \sec [c + d x] + C \sec [c + d x]^2}{\cos [c + d x]^{3/2} \sqrt{a + b \sec [c + d x]}} dx$$

**Problem 1362: Unable to integrate problem.**

$$\int \frac{\sqrt{\cos [c + d x]} (a A + (A b + a B) \sec [c + d x] + b B \sec [c + d x]^2)}{\sqrt{a + b \sec [c + d x]}} dx$$

Optimal (type 4, 208 leaves, 13 steps):

$$\begin{aligned}
 & \frac{2 a B \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\
 & \frac{2 b B \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\
 & \frac{2 A \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}}{d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}}
 \end{aligned}$$

Result (type 8, 56 leaves):

$$\int \frac{\sqrt{\cos [c + d x]} (a A + (A b + a B) \sec [c + d x] + b B \sec [c + d x]^2)}{\sqrt{a + b \sec [c + d x]}} dx$$

**Problem 1363: Attempted integration timed out after 120 seconds.**

$$\int \frac{\text{Cos}[c + d x]^{5/2} (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2)}{(a + b \text{Sec}[c + d x])^{3/2}} dx$$

Optimal (type 4, 461 leaves, 11 steps):

$$- \left( \left( 2 (48 A b^3 - 5 a^3 B - 40 a b^2 B + 6 a^2 b (2 A + 5 C)) \sqrt{\frac{b + a \text{Cos}[c + d x]}{a + b}} \right. \right. \\ \left. \left. \text{EllipticF}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right) / \left( 15 a^4 d \sqrt{\text{Cos}[c + d x]} \sqrt{a + b \text{Sec}[c + d x]} \right) \right) - \\ \left( 2 (48 A b^4 + 25 a^3 b B - 40 a b^3 B - 6 a^2 b^2 (4 A - 5 C) - 3 a^4 (3 A + 5 C)) \sqrt{\text{Cos}[c + d x]} \right. \\ \left. \text{EllipticE}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b} \sqrt{a + b \text{Sec}[c + d x]}\right] \right) / \left( 15 a^4 (a^2 - b^2) d \sqrt{\frac{b + a \text{Cos}[c + d x]}{a + b}} \right) + \\ \frac{2 (A b^2 - a (b B - a C)) \text{Cos}[c + d x]^{3/2} \text{Sin}[c + d x]}{a (a^2 - b^2) d \sqrt{a + b \text{Sec}[c + d x]}} + \frac{1}{15 a^3 (a^2 - b^2) d} \\ \frac{2 (24 A b^3 + 5 a^3 B - 20 a b^2 B - a^2 (9 A b - 15 b C)) \sqrt{\text{Cos}[c + d x]} \sqrt{a + b \text{Sec}[c + d x]} \text{Sin}[c + d x] -}{5 a^2 (a^2 - b^2) d} \\ \frac{2 (6 A b^2 - 5 a b B - a^2 (A - 5 C)) \text{Cos}[c + d x]^{3/2} \sqrt{a + b \text{Sec}[c + d x]} \text{Sin}[c + d x]}{5 a^2 (a^2 - b^2) d}$$

Result (type 1, 1 leaves):

???

**Problem 1364: Attempted integration timed out after 120 seconds.**

$$\int \frac{\text{Cos}[c + d x]^{3/2} (A + B \text{Sec}[c + d x] + C \text{Sec}[c + d x]^2)}{(a + b \text{Sec}[c + d x])^{3/2}} dx$$

Optimal (type 4, 350 leaves, 10 steps):

$$\begin{aligned}
 & \left( 2 (8 A b^2 - 6 a b B + a^2 (A + 3 C)) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right) / \\
 & \left( 3 a^3 d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \right) + \\
 & \left( 2 (8 A b^3 + 3 a^3 B - 6 a b^2 B - a^2 (5 A b - 3 b C)) \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right. \\
 & \left. \sqrt{a + b \sec [c + d x]} \right) / \left( 3 a^3 (a^2 - b^2) d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right) + \\
 & \frac{2 (A b^2 - a (b B - a C)) \sqrt{\cos [c + d x]} \sin [c + d x]}{a (a^2 - b^2) d \sqrt{a + b \sec [c + d x]}} - \frac{1}{3 a^2 (a^2 - b^2) d} \\
 & 2 (4 A b^2 - 3 a b B - a^2 (A - 3 C)) \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \sin [c + d x]
 \end{aligned}$$

Result (type 1, 1 leaves):

???

### Problem 1365: Unable to integrate problem.

$$\int \frac{\sqrt{\cos [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2)}{(a + b \sec [c + d x])^{3/2}} dx$$

Optimal (type 4, 249 leaves, 9 steps):

$$\begin{aligned}
 & \frac{2 (2 A b - a B) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right]}{a^2 d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]}} - \\
 & \left( 2 (2 A b^2 - a b B - a^2 (A - C)) \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \sec [c + d x]} \right) / \\
 & \left( a^2 (a^2 - b^2) d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right) + \frac{2 (A b^2 - a (b B - a C)) \sin [c + d x]}{a (a^2 - b^2) d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]}}
 \end{aligned}$$

Result (type 8, 47 leaves):

$$\int \frac{\sqrt{\cos [c + d x]} (A + B \sec [c + d x] + C \sec [c + d x]^2)}{(a + b \sec [c + d x])^{3/2}} dx$$

### Problem 1366: Unable to integrate problem.

$$\int \frac{A + B \sec [c + d x] + C \sec [c + d x]^2}{\sqrt{\cos [c + d x]} (a + b \sec [c + d x])^{3/2}} dx$$

Optimal (type 4, 311 leaves, 13 steps):

$$\frac{2 A \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{a d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} +$$

$$\frac{2 C \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{b d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} +$$

$$\left(2\left(A b^2-a(b B-a C)\right) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}\right) /$$

$$\left(a b\left(a^2-b^2\right) d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}\right) - \frac{2\left(A b^2-a(b B-a C)\right) \sin [c+d x]}{b\left(a^2-b^2\right) d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}}$$

Result (type 8, 47 leaves):

$$\int \frac{A+B \sec [c+d x]+C \sec [c+d x]^2}{\sqrt{\cos [c+d x]}(a+b \sec [c+d x])^{3 / 2}} d x$$

Problem 1367: Attempted integration timed out after 120 seconds.

$$\int \frac{A+B \sec [c+d x]+C \sec [c+d x]^2}{\cos [c+d x]^{3 / 2}(a+b \sec [c+d x])^{3 / 2}} d x$$

Optimal (type 4, 393 leaves, 14 steps):

$$\frac{C \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{b d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} +$$

$$\frac{(2 b B-3 a C) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{b^2 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} -$$

$$\left(\left(2 A b^2-2 a b B+3 a^2 C-b^2 C\right) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}\right) /$$

$$\left(b^2\left(a^2-b^2\right) d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}\right) - \frac{2\left(A b^2-a(b B-a C)\right) \sin [c+d x]}{b\left(a^2-b^2\right) d \cos [c+d x]^{3 / 2} \sqrt{a+b \sec [c+d x]}} +$$

$$\frac{\left(2 A b^2-2 a b B+3 a^2 C-b^2 C\right) \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{b^2\left(a^2-b^2\right) d \sqrt{\cos [c+d x]}}$$

Result (type 1, 1 leaves):

???



**Problem 1368: Attempted integration timed out after 120 seconds.**

$$\int \frac{\cos [c+d x]^{5 / 2} (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2)}{(a+b \operatorname{Sec}[c+d x])^{5 / 2}} d x$$

Optimal (type 4, 663 leaves, 12 steps):

$$\begin{aligned} & \left( 2 (128 A b^5 + 5 a^5 B + 80 a^3 b^2 B - 80 a b^4 B - 4 a^2 b^3 (29 A - 10 C) - a^4 b (17 A + 45 C)) \right. \\ & \quad \left. \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \right) / \\ & \quad (15 a^5 (a^2-b^2) d \sqrt{\cos [c+d x]} \sqrt{a+b \operatorname{Sec}[c+d x]}) + \\ & \quad \left( 2 (128 A b^6 - 40 a^5 b B + 140 a^3 b^3 B - 80 a b^5 B + 5 a^4 b^2 (11 A - 15 C) - 4 a^2 b^4 (53 A - 10 C) + \right. \\ & \quad \left. 3 a^6 (3 A + 5 C)) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \operatorname{Sec}[c+d x]} \right) / \\ & \quad \left( 15 a^5 (a^2-b^2)^2 d \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \right) + \frac{2 (A b^2 - a (b B - a C)) \cos [c+d x]^{3 / 2} \sin [c+d x]}{3 a (a^2-b^2) d (a+b \operatorname{Sec}[c+d x])^{3 / 2}} - \\ & \quad (2 (8 A b^4 + 9 a^3 b B - 5 a b^3 B - 2 a^2 b^2 (6 A - C) - 6 a^4 C) \cos [c+d x]^{3 / 2} \sin [c+d x]) / \\ & \quad (3 a^2 (a^2-b^2)^2 d \sqrt{a+b \operatorname{Sec}[c+d x]}) - \frac{1}{15 a^4 (a^2-b^2)^2 d} \\ & \quad 2 (64 A b^5 - 5 a^5 B + 65 a^3 b^2 B - 40 a b^4 B + 2 a^4 b (7 A - 20 C) - 2 a^2 b^3 (49 A - 10 C)) \\ & \quad \sqrt{\cos [c+d x]} \sqrt{a+b \operatorname{Sec}[c+d x]} \sin [c+d x] + \frac{1}{15 a^3 (a^2-b^2)^2 d} \\ & \quad 2 (48 A b^4 + 50 a^3 b B - 30 a b^3 B + a^4 (3 A - 35 C) - a^2 b^2 (71 A - 15 C)) \\ & \quad \cos [c+d x]^{3 / 2} \sqrt{a+b \operatorname{Sec}[c+d x]} \sin [c+d x] \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 1369: Attempted integration timed out after 120 seconds.**

$$\int \frac{\cos [c+d x]^{3 / 2} (A+B \operatorname{Sec}[c+d x]+C \operatorname{Sec}[c+d x]^2)}{(a+b \operatorname{Sec}[c+d x])^{5 / 2}} d x$$

Optimal (type 4, 521 leaves, 11 steps):

$$\begin{aligned}
 & - \left( \left( 2 (16 A b^4 + 9 a^3 b B - 8 a b^3 B - 2 a^2 b^2 (8 A - C) - a^4 (A + 3 C)) \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \right. \right. \\
 & \quad \left. \left. \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right) / \left( 3 a^4 (a^2 - b^2) d \sqrt{\operatorname{Cos}[c + d x]} \sqrt{a + b \operatorname{Sec}[c + d x]} \right) \right) - \\
 & \left( 2 (16 A b^5 - 3 a^5 B + 15 a^3 b^2 B - 8 a b^4 B - 2 a^2 b^3 (14 A - C) + a^4 (8 A b - 6 b C)) \right. \\
 & \quad \left. \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \operatorname{Sec}[c + d x]} \right) / \\
 & \left( 3 a^4 (a^2 - b^2)^2 d \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \right) + \frac{2 (A b^2 - a (b B - a C)) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{Sin}[c + d x]}{3 a (a^2 - b^2) d (a + b \operatorname{Sec}[c + d x])^{3/2}} + \\
 & \left( 2 (10 a^2 A b^2 - 6 A b^4 - 7 a^3 b B + 3 a b^3 B + 4 a^4 C) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{Sin}[c + d x] \right) / \\
 & \left( 3 a^2 (a^2 - b^2)^2 d \sqrt{a + b \operatorname{Sec}[c + d x]} \right) + \frac{1}{3 a^3 (a^2 - b^2)^2 d} \\
 & \frac{2 (8 A b^4 + 8 a^3 b B - 4 a b^3 B + a^4 (A - 5 C) - a^2 b^2 (13 A - C))}{\sqrt{\operatorname{Cos}[c + d x]} \sqrt{a + b \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

### Problem 1370: Unable to integrate problem.

$$\int \frac{\sqrt{\operatorname{Cos}[c + d x]} (A + B \operatorname{Sec}[c + d x] + C \operatorname{Sec}[c + d x]^2)}{(a + b \operatorname{Sec}[c + d x])^{5/2}} dx$$

Optimal (type 4, 401 leaves, 10 steps):

$$\begin{aligned}
 & \left( 2 (8 A b^3 + 3 a^3 B - 2 a b^2 B - a^2 b (9 A + C)) \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right) / \\
 & \left( 3 a^3 (a^2 - b^2) d \sqrt{\operatorname{Cos}[c + d x]} \sqrt{a + b \operatorname{Sec}[c + d x]} \right) + \\
 & \left( 2 (8 A b^4 + 6 a^3 b B - 2 a b^3 B + 3 a^4 (A - C) - a^2 b^2 (15 A + C)) \sqrt{\operatorname{Cos}[c + d x]} \right. \\
 & \quad \left. \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \operatorname{Sec}[c + d x]} \right) / \left( 3 a^3 (a^2 - b^2)^2 d \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \right) + \\
 & \frac{2 (A b^2 - a (b B - a C)) \operatorname{Sin}[c + d x]}{3 a (a^2 - b^2) d \sqrt{\operatorname{Cos}[c + d x]} (a + b \operatorname{Sec}[c + d x])^{3/2}} - \\
 & \frac{2 (4 A b^4 + 5 a^3 b B - a b^3 B - 2 a^4 C - 2 a^2 b^2 (4 A + C)) \operatorname{Sin}[c + d x]}{3 a^2 (a^2 - b^2)^2 d \sqrt{\operatorname{Cos}[c + d x]} \sqrt{a + b \operatorname{Sec}[c + d x]}}
 \end{aligned}$$

Result (type 8, 47 leaves):

$$\int \frac{\sqrt{\cos [c+d x]} (A+B \sec [c+d x]+C \sec [c+d x]^2)}{(a+b \sec [c+d x])^{5/2}} dx$$

Problem 1371: Unable to integrate problem.

$$\int \frac{A+B \sec [c+d x]+C \sec [c+d x]^2}{\sqrt{\cos [c+d x]} (a+b \sec [c+d x])^{5/2}} dx$$

Optimal (type 4, 378 leaves, 10 steps):

$$\begin{aligned} & - \left( \left( 2 (2 A b^2 + a b B - a^2 (3 A + C)) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \right) / \right. \\ & \quad \left. (3 a^2 (a^2 - b^2) d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}) \right) - \\ & \left( 2 (2 A b^3 + 3 a^3 B + a b^2 B - 2 a^2 b (3 A + 2 C)) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \right. \\ & \quad \left. \sqrt{a+b \sec [c+d x]} \right) / \left( 3 a^2 (a^2 - b^2)^2 d \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \right) - \\ & \frac{2 (A b^2 - a (b B - a C)) \sin [c+d x]}{3 b (a^2 - b^2) d \sqrt{\cos [c+d x]} (a+b \sec [c+d x])^{3/2}} + \\ & \frac{2 (A b^4 + 2 a^3 b B + 2 a b^3 B + a^4 C - 5 a^2 b^2 (A + C)) \sin [c+d x]}{3 a b (a^2 - b^2)^2 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} \end{aligned}$$

Result (type 8, 47 leaves):

$$\int \frac{A+B \sec [c+d x]+C \sec [c+d x]^2}{\sqrt{\cos [c+d x]} (a+b \sec [c+d x])^{5/2}} dx$$

Problem 1372: Attempted integration timed out after 120 seconds.

$$\int \frac{A+B \sec [c+d x]+C \sec [c+d x]^2}{\cos [c+d x]^{3/2} (a+b \sec [c+d x])^{5/2}} dx$$

Optimal (type 4, 447 leaves, 14 steps):

$$\begin{aligned}
 & - \frac{2 (A b^2 - a (b B - a C)) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{3 a b\left(a^2-b^2\right) d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\
 & \frac{2 C \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{b^2 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} - \\
 & \left(2\left(A b^4-4 a b^3 B-3 a^4 C+a^2 b^2(3 A+7 C)\right) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \right. \\
 & \left. \sqrt{a+b \sec [c+d x]}\right) / \left(3 a b^2\left(a^2-b^2\right)^2 d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}\right) - \\
 & \frac{2(A b^2-a(b B-a C)) \sin [c+d x]}{3 b\left(a^2-b^2\right) d \cos [c+d x]^{3 / 2}(a+b \sec [c+d x])^{3 / 2}} + \\
 & \frac{2\left(A b^4-4 a b^3 B-3 a^4 C+a^2 b^2(3 A+7 C)\right) \sin [c+d x]}{3 b^2\left(a^2-b^2\right)^2 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 1373: Attempted integration timed out after 120 seconds.**

$$\int \frac{A+B \sec [c+d x]+C \sec [c+d x]^2}{\cos [c+d x]^{5 / 2}(a+b \sec [c+d x])^{5 / 2}} d x$$

Optimal (type 4, 563 leaves, 15 steps):

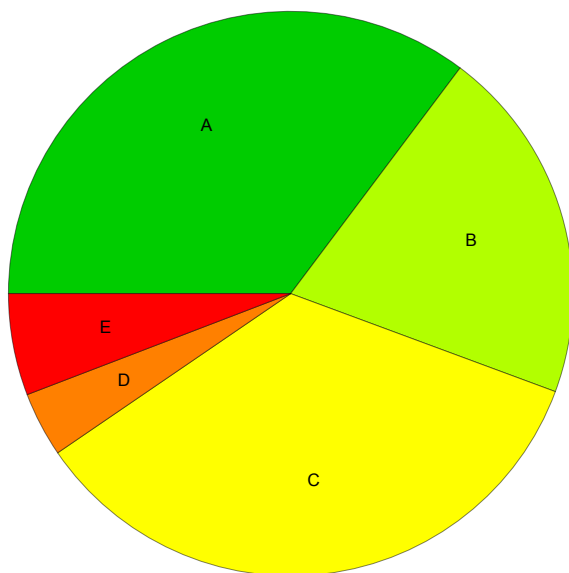
$$\begin{aligned}
 & \left( (2 A b^2 - 2 a b B + 5 a^2 C - 3 b^2 C) \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right) / \\
 & \left( 3 b^2 (a^2 - b^2) d \sqrt{\operatorname{Cos}[c + d x]} \sqrt{a + b \operatorname{Sec}[c + d x]} \right) + \\
 & \frac{(2 b B - 5 a C) \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c + d x), \frac{2 a}{a + b}\right]}{b^3 d \sqrt{\operatorname{Cos}[c + d x]} \sqrt{a + b \operatorname{Sec}[c + d x]}} + \\
 & \left( (8 A b^4 + 6 a^3 b B - 14 a b^3 B - 15 a^4 C + 26 a^2 b^2 C - 3 b^4 C) \sqrt{\operatorname{Cos}[c + d x]} \right. \\
 & \left. \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \operatorname{Sec}[c + d x]} \right) / \left( 3 b^3 (a^2 - b^2)^2 d \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \right) - \\
 & \frac{2 (A b^2 - a (b B - a C)) \operatorname{Sin}[c + d x]}{3 b (a^2 - b^2) d \operatorname{Cos}[c + d x]^{5/2} (a + b \operatorname{Sec}[c + d x])^{3/2}} + \\
 & \frac{2 (3 A b^4 + 2 a^3 b B - 6 a b^3 B - 5 a^4 C + a^2 b^2 (A + 9 C)) \operatorname{Sin}[c + d x]}{3 b^2 (a^2 - b^2)^2 d \operatorname{Cos}[c + d x]^{3/2} \sqrt{a + b \operatorname{Sec}[c + d x]}} - \\
 & \left( (8 A b^4 + 6 a^3 b B - 14 a b^3 B - 15 a^4 C + 26 a^2 b^2 C - 3 b^4 C) \sqrt{a + b \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x] \right) / \\
 & \left( 3 b^3 (a^2 - b^2)^2 d \sqrt{\operatorname{Cos}[c + d x]} \right)
 \end{aligned}$$

Result(type 1, 1 leaves):

???

## Summary of Integration Test Results

1373 integration problems



A - 484 optimal antiderivatives

B - 280 more than twice size of optimal antiderivatives

C - 478 unnecessarily complex antiderivatives

D - 51 unable to integrate problems

E - 80 integration timeouts